Real Variable Power: Implement of the high-level programing function 关于高级编程语言对实变幂函数的实现

Given the power function definition in real number field 给定幂函数实数域定义

$$f(x) = x^a; (x, a \in R) \tag{1}$$

and there will be 3 conditions for calculating the result. 并且会有 3 种计算结果

$$f(x) = \begin{cases} 0 & x = 0\\ e^{a \ln x} & x > 0\\ |x|^a e^{i(2k+1)\pi a} & x < 0 \end{cases}$$
 (2)

With the definition of Euler Equation 根据尤拉公式的定义

$$e^{ix} = \cos x + i \sin x \tag{3}$$

then the condition equation of (x < 0) can be (x < 0)情况的等式为

$$|x|^{a}e^{i(2k+1)\pi a} = |x|^{a}(\cos T + i\sin T)$$
(4)

$$T = (2k+1) \pi a \tag{5}$$

The answer can be calculated by using the Taylor Series. 结果可以通过泰勒级数计算。