## Discrete Simulation: Homework 1

Austin J. Maddison

Mahidol University International College

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### 1. Birthday Problem

The simulations ran were set to seed = 27 and N = 100000.

a)

$$p_{10} = 0.1169$$
  
 $CI = [0.1169, 0.1189]$ 

b)

$$p_{20} = 0.4113$$
  
 $CI = [0.4113, 0.4143]$ 

c)

$$p_{30} = 0.7059$$
  
 $CI = [0.7059, 0.7088]$ 

d) Found n that satisfies the condition  $p_n \le 0.5$  from extracting the smallest difference from varying n's of  $p_n$  and the function of p = 0.5.

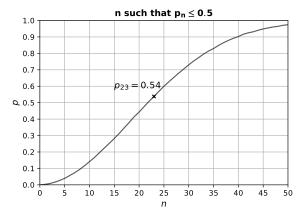


Figure 1: Closest point to p = 0.5 was  $p_{23} = 0.54$  which satisfies the condition.

## 2. Alice and Bob Play a Game

The strategy I let Alice have is the following...

#### **Case 1: Found Exclusive Output**

She presses the button recording n output values  $x_1, x_2, ... x_n$ . As she records each output she checks whether  $x_i$  is exclusive to one of the buttons output range. If  $x_i$  is exclusive she returns the corresponding button as the answer.

#### Case 2: No Exclusive Output

After she presses the button n times with no exclusive output appearing. She calculates  $\bar{x}$  and finds the minimum difference between the mean output range of the 2 buttons. She returns the corresponding button that gets the minimum distance.

#### **Psuedocode**

Although the source code differs because loops are removed for speed, the idea is the same.

```
xs = []
for i in range(0, n):
    x_n = button_unknown.get_next_value()
    xs.append(x_n)

# Case 1: Found exclusive output.
    if(x_n == 1)
        return 1 # it is button 1
    if(x_n == 100)
        return 2 # it is button 2

# Case 2: No exclusive output. Evaluate
    the minimum distance of means.
x_mean = sum(xs) / n
button_1_mean = (1 + 99)/2
button_2_mean = (2 + 100)/2

return argmin([abs(x_mean - button_1_mean)
    , abs(x_mean - button_2_mean)]) + 1
```

#### Find n such that Alice is correct $\leq 0.9$

Similar to problem 1.Birthday Problem, I sampled Alice's strategy over some reasonable range of n

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[0,500] and extract the n that results in probability p that Alice is correct is at least 0.99. I set the seed=27 and ran 1000 trials for each all n's.

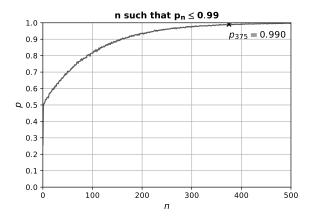


Figure 2: Closest point to p = 0.99 was  $p_{375} = 0.990$  which satisfies the condition.

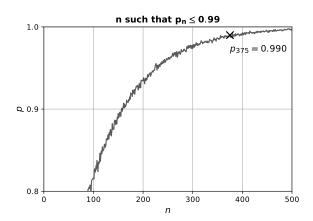


Figure 3: y-lim[0.8, 1.0] of Figure 2.

# 3. Practice with Uniform and Geometric Distributions

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#### 4. Source Code

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