

5. Given a graph represented by an adjacency matrix, implement Dijkstra's Algorithm to find the shortest path from a given source vertex to all other vertices in the graph. The graph is represented as an adjacency matrix where `graph[i][j]` denote the weight of the edge from vertex `i` to vertex `j`. If there is no edge between vertices `i` and `j`, the value is Infinity (or a very large number).

Test Case 1:

Input:

`n = 5`

```
graph = [[0, 10, 3, Infinity, Infinity], [Infinity, 0, 1, 2, Infinity], [Infinity, 4, 0, 8, 2],  
         [Infinity, Infinity, Infinity, 0, 7], [Infinity, Infinity, Infinity, 9, 0]]
```

`source = 0`

Output: `[0, 7, 3, 9, 5]`

Test Case 2:

Input:

`n = 4`

```
graph = [[0, 5, Infinity, 10], [Infinity, 0, 3, Infinity], [Infinity, Infinity, 0, 1],  
         [Infinity, Infinity, Infinity, 0] ]
```

`source = 0`

Output: `[0, 5, 8, 9]`

Program:

```
import heapq  
  
def dijkstra(graph, source):  
    n = len(graph)  
    distances = [float('inf')] * n  
    distances[source] = 0  
    min_heap = [(0, source)]  
    visited = [False] * n  
    while min_heap:  
        current_distance, u = heapq.heappop(min_heap)
```

```

    if visited[u]:
        continue

    visited[u] = True

    for v in range(n):
        if graph[u][v] != float('inf') and not visited[v]:
            new_distance = current_distance + graph[u][v]

            if new_distance < distances[v]:
                distances[v] = new_distance

                heapq.heappush(min_heap, (new_distance, v))

    return distances

n = 5

graph = [
    [0, 10, 3, float('inf'), float('inf')],
    [float('inf'), 0, 1, 2, float('inf')],
    [float('inf'), 4, 0, 8, 2],
    [float('inf'), float('inf'), float('inf'), 0, 7],
    [float('inf'), float('inf'), float('inf'), 9, 0]
]

source = 0

print(dijkstra(graph, source)) # Output: [0, 7, 3, 9, 5]

n = 4

graph = [
    [0, 5, float('inf'), 10],
    [float('inf'), 0, 3, float('inf')],
    [float('inf'), float('inf'), 0, 1],
    [float('inf'), float('inf'), float('inf'), 0]
]

```

```
source = 0

print(dijkstra(graph, source))
```

Output:

```
C:\Users\srika\Desktop\CSA0863\pythonProject\.venv\Scripts\python.exe "C:\Users\srika\Desktop\CSA0863\pythonProject\DAA\practice 4.py"
[0, 7, 3, 9, 5]
[0, 5, 8, 9]

Process finished with exit code 0
```

Time complexity:

$O(n^2 \log n)$