165.

1. To Implement the Median of Medians algorithm ensures that you handle the worst-case time complexity efficiently while finding the k-th smallest element in an unsorted array.
   arr = [12, 3, 5, 7, 19] k = 2 Expected Output:5

code:

```
def partition(arr, low, high, pivot):
    pivot_index = arr.index(pivot)
    arr[pivot_index], arr[high] = arr[high], arr[pivot_index]
    i = low
    for j in range(low, high):
        if arr[j] < pivot:
            arr[i], arr[j] = arr[j], arr[i]
            i += 1
    arr[i], arr[high] = arr[high], arr[i]
    return i
def select(arr, low, high, k):
    if low == high:
        return arr[low]
    n = high - low + 1
    medians = []
    for i in range(low, high + 1, 5):
        group = sorted(arr[i:i + 5])
        medians.append(group[len(group) // 2])
    median_of_medians = select(medians, 0, len(medians) - 1, len(medians) // 2)
    pivot_index = partition(arr, low, high, median_of_medians)
    if pivot_index - low == k - 1:
        return arr[pivot_index]
    elif pivot_index - low > k - 1:
        return select(arr, low, pivot_index - 1, k)
    else:
        return select(arr, pivot_index + 1, high, k - pivot_index + low - 1)
def find_kth_smallest(arr, k):
    return select(arr, 0, len(arr) - 1, k)
arr = [12, 3, 5, 7, 19]
k = 2
output = find_kth_smallest(arr, k)
print(f"Expected Output: {output}")
```

output:

```
PS C:\Users\karth>
PS C:\Users\karth> & C:/Users/karth/AppData/Local/Programs/Python/Python312/python.exe c:/Users/karth/OneDrive/Desktop/csa0863_karthik/PROBLEM.py
Expected Output: 7
PS C:\Users\karth>
```

Time complexity:f(n)=o(n)