

#### 4. Directed or Undirected

```
public class IsDirected {
    public static boolean isDirected(int[][] matrix) {
        // check that is a valid graph
        O(1) time and space, nothing being initialized and constant time
        operations
        if(matrix == null || matrix.length <= 1 || matrix.length !=
matrix[0].length)
            return false;

        Space O(1), nothing being initialized
        Outer Looper Time: O(n) where n is the number of rows in an nxn matrix
        for(int row = 0; row < matrix.length; row++) {
            Inner Looper Time: O(n) where n is the number of cols which is
            equal to the number of rows in an nxn matrix
            for(int col = 0; col < matrix[row].length; col++) {
                // check for symmetry across diagonal
                if(matrix[row][col] != matrix[col][row]) {
                    return true;
                }
            }
        }
        return false;
    }
}
```

**Time Complexity:**  $O(n^2)$  where  $n$  is the amount of rows (`matrix.length`) in the input matrix.

**Space Complexity:**  $O(1)$ .

## 5. Every Path

```
public static void findEveryPath(int[][] matrix, int u, int w) {  
    O(1) time and space  
    Queue<ArrayList<Integer>> frontier = new LinkedList<>();  
    ArrayList<Integer> visited = new ArrayList<>();  
    ArrayList<Integer> path = new ArrayList<>();  
    path.add(u);  
    frontier.add(path);  
  
    We visit each node only once, so this loop iterates V time where V is  
    the number of vertices in the adjacency matrix  
    while(!frontier.isEmpty()) {  
        path = frontier.poll();  
        int vertex = path.getLast();  
  
        if(vertex == w && path.size() == 5)  
            System.out.println(path);  
  
        if(!visited.contains(vertex)) {  
            visited.add(vertex); We add a vertex to the visited list  
  
            The loop will iterate E times or the number of  
            outgoing edges of that node  
            for (int adjacentVertex = 0; adjacentVertex < matrix[0].length;  
adjacentVertex++) {  
                if (matrix[vertex][adjacentVertex] != 0) {  
                    Copy the list of the path taken so far, O(V) time  
                    O(V) space  
                    ArrayList<Integer> tempPath = new ArrayList<>(path);  
                    Add to the new list the next adjacent node you step  
                    towards  
                    tempPath.add(adjacentVertex);  
                    Add current path to the list of all paths taken, the  
                    last node of the path defines what nodes should be  
                    explored  
                    frontier.offer(tempPath);  
                }  
            }  
        }  
    }  
}
```

**Time Complexity:**  $O(V+E \cdot V)$  where  $V$  is the number of vertices in the input matrix which is also equal to `matrix.length`, and  $E$  is the maximum amount of outgoing edges from one node which is also less than or equal to `matrix.length`. It is  $O(V+E \cdot V)$  instead of  $O(V+E)$  because we must copy the array of all of the previously visited nodes for every outgoing edge.

**Space Complexity:**  $O(V^2)$  where  $V$  is the number of vertices in the input matrix which is also equal to `matrix.length`. Not  $O(V)$  because the frontier stack does not only store the nodes that will be explored, it stores all of the nodes to be explored AND all the paths to get that node.

## 5. Draw Graph

```
input = [('I', 1), ('A', 5), ('E', 4), ('F', 1), ('T', 2), ('S', 3)]

Initialize DiGraph Object  $O(1)$  time and space
https://github.com/networkx/networkx/blob/main/networkx/classes/digraph.py#L21
G = nx.DiGraph()

Iterates the same amount of times as vertices in the input which is also equal
to the length of the input array
for vertex, adjacent in input:
     $O(1)$  space and time, add node hashmap of successor nodes, hashmap of
    predecessor nodes, and hashmap of all nodes and their attributes
    G.add_node(vertex)

Iterates the same amount of times as vertices in the input which is also equal
to the length of the input array
for index, vertex_pair in enumerate(input):
    vertex, adjacent_index = vertex_pair
    left_adjacent_index = (index - adjacent_index) % len(input)
    right_adjacent_index = (index + adjacent_index) % len(input)
    left_adjacent = input[left_adjacent_index][0]
    right_adjacent = input[right_adjacent_index][0]
    Each node has a left and right neighbor which will be added to the internal
    hashmaps of successor, predecessor, and node attributes
    G.add_edge(vertex, left_adjacent)
    G.add_edge(vertex, right_adjacent)

 $O(V+E) \Rightarrow O(V)$  time because each node and edge must be drawn, where  $V$  is the
amount of vertices in the input and  $E$  is the amount of edges, but every vertex
has at most 2 edges so  $E \leq 2*V$ .  $O(V+2*V) \Rightarrow O(V)$ 

https://gist.github.com/koorukuroo/5efb58a86c5396f13650
nx.draw_networkx(G, arrows=True)

https://github.com/matplotlib/matplotlib/blob/main/lib/matplotlib/pyplot.py
Time  $O(1)$ 
plt.show()
```

**Time Complexity:**  $O(V)$  where  $V$  is the number of vertices in the input equal to the array's length. Every vertex and edge must be added to the DiGraph object and drawn on the plot, but it is not  $O(V+E)$  because there are at most  $2*V$

outgoing edges. If  $E$  is less than or equal to  $2*V$ , the worst case is  $O(V+2*V)$ , which simplifies to  $O(V)$ .

**Space Complexity:**  $O(V)$ , where  $V$  is the number of vertices in the input equal to the length of the array. Every vertex and edge is stored internally in the DiGraph object, but it is not  $O(V+E)$  because there are at most  $2*V$  outgoing edges, so  $E$  is less than or equal to  $2*V$ . So, the new worst case is  $O(V+2*V)$ , which simplifies to  $O(V)$ .