

1. Initialize Candidates Time and Space Complexity

```
public void initializeCandidates(LinkedList<String> candidates) {
    int size = candidates.size();
    Space O(N), N = size of candidates list
    - In the loop below, every node in candidates is put into the hash map
    this.votingMap = new HashMap<>();

    Space O(N), N = size of candidates list
    this.candidateMaxHeap = new String[size];

    Time: O(N), N = size of candidates list
    for(int i = 0; i < size; i++) {\
        votingMap.put(candidates.get(i), 0);

        Time: O(N), N = size of candidates list
        - Searching a linked list node by node
        candidateMaxHeap[i] = candidates.get(i);
    }
}
```

Time: $O(N^2)$ where N is the size of the candidate's list

Space: $O(N)$ where N is the size of the candidate's list

2. Cast Vote Time and Space Complexity

```
public void castVote(String candidate) {
    Space O(1): We are not changing the number of items in the hashmap
    votingMap.put(candidate, votingMap.get(candidate) + 1);

    // Time: O(M), M = length of array candidateMaxHeap
    for(int i = candidateMaxHeap.length/2; i >= 0 ; i--) {
        // Time: log(M), M = length of array candidateMaxHeap
        heapify(candidateMaxHeap, i);
    }
}
```

Time: $O(M \cdot \log(M))$ where M is the length of array candidateMaxHeap, but M is equal to the length of the original candidate list (N). So, it can also be written as $O(N \cdot \log(N))$.

Space: $O(1)$

3. Cast Random Vote

```
public void castRandomVote() {
    // Time of generating next random int => O(1)
    // Space => O(1)
    https://docs.oracle.com/javase/1.5.0/docs/api/java/util/Random.html
    synchronized protected int next(int bits) {
        seed = (seed * 0x5DEECE66DL + 0xBL) & ((1L << 48) - 1);
        return (int)(seed >>> (48 - bits));
    }
    int rand_int = gen.nextInt(candidateMaxHeap.length);
    String candidate = candidateMaxHeap[rand_int];

    // Time O(M*log(M)) where M is the length of array candidateMaxHeap
    // Space(1)
    -Refer to cast vote space and time complexity above
    castVote(candidate);
}
```

Time: $O(M \cdot \log(M))$ where M is the length of array `candidateMaxHeap`, but M is equal to the length of the original candidate list (N). So, it can also be written as $O(N \cdot \log(N))$.

Space: $O(1)$

4. Rig Election

```
public void rigElection(String candidate) {
    // Space O(1)
    int totalVotes = 0;

    // Space O(1)
    // Time O(P) where P total amount of key-value pairs stored in votingMap
    for(int votes : votingMap.values()) {
        totalVotes += votes;
    }

    // Time O(P) where P total amount of key-value pairs stored in votingMap
    for(String key : votingMap.keySet()) {
        votingMap.put(key, 0);
    }

    // Time O(1)
    votingMap.put(candidate, totalVotes);
}
```

Time: $O(P)$ where P is the amount of key-value pairs stored in votingMap, but P is equal to the length of the original candidate list (N). So, it can also be written as $O(N)$.

Space: $O(1)$

5. Get Top K Candidates

```
public String[] getTopKCandidates ( int k){
    // Space: O(k), we have to create an array of size k
    String[] topk = new String[k];
    int heapLen = candidateMaxHeap.length;

    // Remove root of heap K times
    // Time: O(k)
    for (int i = 0; i < k && i < heapLen; i++) {
        topk[i] = candidateMaxHeap[0];
        candidateMaxHeap[0] = candidateMaxHeap[heapLen - 1 - i];
        candidateMaxHeap[heapLen - 1 - i] = null;

        // Time: O(M), M = length of array candidateMaxHeap
        for (int j = candidateMaxHeap.length / 2; j >= 0; j--) {
            // Time: log(M), M = length of array candidateMaxHeap
            heapify(candidateMaxHeap, j);
        }
    }

    // Add removed nodes back into heap
    // Time: O(k)
    for (int i = 0; i < k && i < heapLen; i++) {
        candidateMaxHeap[heapLen - 1 - i] = topk[i];
    }

    //reheapify
    // Time: O(M), M = length of array candidateMaxHeap
    for (int j = candidateMaxHeap.length / 2; j >= 0; j--) {
        // Time: log(M), M = length of array candidateMaxHeap
        heapify(candidateMaxHeap, j);
    }

    return topk;
}
```

Time: $O(k \cdot M \cdot \log(M))$ where M is the length of the candidateMaxHeap and k is the int parameter for the function. Because M is equal to N , we can also rewrite this as $O(k \cdot N \cdot \log(N))$, where N is the length of the original candidate list.

Space: $O(k)$, where k is the int variable named k .

6. Audit Election

```
public void auditElection () {
    // Time  $O(k*M*\log(M))$ , where  $M$  is the length of array candidateMaxHeap, but
    // since  $k = M$ , the length of the array candidateMaxHeap,
    // Time =>  $O(M^2*\log(M))$ 

    // Space  $O(k)$   $k = M$ , the length of the array candidateMaxHeap, Time =>  $O(M)$ 
    String[] candidates = getTopKCandidates(candidateMaxHeap.length);

    // Time:  $O(M)$  loop iterates the length of candidateMaxHeap( $M$ )
    // Space:  $O(1)$ 
    for (int i = 0; i < candidateMaxHeap.length; i++) {
        //  $O(S)$  where  $S$  is the number of characters in the candidate's name with
        // the most characters. String concatenation requires a new String to be
        // created and copied character by character.
        System.out.println(candidates[i] + " - " + votingMap.get(candidates[i]));
    }
}
```

Time: $O(M^2*\log(M)) + O(M*S)$, where M is the length of the array candidateMaxHeap, and S is the number of characters in the candidate's name with the most characters. Realistically, $O(M^2*\log(M))$ will grow faster, so $O(M*S)$ can be excluded. Also, because M equals N , the length of the original candidate list, the time complexity can be rewritten as $O(N^2*\log(N))$.

Space: $O(M)$, where M is the length of the array candidateMaxHeap.