Lazy Caterer's Sequence

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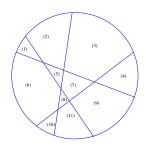
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Illustration of structures

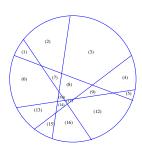
1. n = 4

0.1

(a) Pancake structure



- (b) AA
- 2. n = 4
 - (a) Pancake structure



(b) AA

0.2 Formula Demonstrations

1. $a(n) = Binomial(n+2,1) - 2 \times Binomial(n+1,1) + Binomial(n+2,2)$

$$\binom{n+2}{1} - 2 \times \binom{n+1}{1} + \binom{n+2}{2}$$

(a) n = 4

$$a(4) = {4+2 \choose 1} - 2 \times {4+1 \choose 1} + {4+2 \choose 2}$$

$$a(4) = \binom{6}{1} - 2 \times \binom{5}{1} + \binom{6}{2}$$

$$a(4) = 6 - 10 + 15$$

$$a(4) = 11$$

(b) n = 5

$$a(5) = {5+2 \choose 1} - 2 \times {5+1 \choose 1} + {5+2 \choose 2}$$

$$a(5) = \binom{7}{1} - 2 \times \binom{6}{1} + \binom{7}{2}$$

$$a(5) = 7 - 12 + 21$$

$$a(4) = 16$$

- 2. $G.f: A(x) = (1 x + x^2)/(1 x)^3$
 - (a) n = 4

(b) n = 5