Diagrams and algebraic expressions at order (2,2;2) in BIMSRG

The ADG Dev Team

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$$C = [A, B]$$
 with $N_A = 2$, $N_B = 2$ and $N_C = 2$ $d_{\text{max}} \equiv \max(d_A, d_B, d_C)$

Valid diagrams: 82 $d_{\rm max} = 1 \ {\rm diagrams:} \ 10$ $d_{\rm max} = 2 \ {\rm diagrams:} \ 72$

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3.6 & C^{02} & \\ 3.7 & C^{22} & \\ 3.8 & C^{13} & \end{aligned}$	$\begin{aligned} d_{\text{max}} &= 1 \\ 2.1 C^{00} \\ 2.2 C^{20} \\ 2.3 C^{11} \\ 2.4 C^{02} \\ \ldots \end{aligned}$ $\begin{aligned} d_{\text{max}} &= 2 \\ 3.1 C^{00} \\ 3.2 C^{20} \\ \ldots \\ 3.4 C^{11} \\ \ldots \\ 3.5 C^{31} \\ 3.6 C^{02} \\ \ldots \\ 3.7 C^{22} \\ \ldots \\ 3.8 C^{13} \\ \ldots \end{aligned}$	$\begin{aligned} d_{\text{max}} &= 1 \\ 2.1 C^{00} \\ 2.2 C^{20} \\ 2.3 C^{11} \\ 2.4 C^{02} \\ 3.1 C^{00} \\ 3.2 C^{20} \\ 3.3 C^{40} \\ 3.4 C^{11} \\ 3.5 C^{31} \\ 3.6 C^{02} \\ 3.7 C^{22} \\ 3.8 C^{13} \\ \ldots \end{aligned}$	$\begin{aligned} d_{\text{max}} &= 1 \\ 2.1 C^{00} \\ 2.2 C^{20} \\ 2.3 C^{11} \\ 2.4 C^{02} \\ &\vdots \\ d_{\text{max}} &= 2 \\ 3.1 C^{00} \\ 3.2 C^{20} \\ 3.3 C^{40} \\ &\vdots \\ 3.5 C^{31} \\ 3.6 C^{02} \\ &\vdots \\ 3.7 C^{22} \\ &\vdots \\ 3.8 C^{13} \\ &\vdots \\ &$	$\begin{aligned} d_{\text{max}} &= 1 \\ 2.1 C^{00} & \dots & \dots \\ 2.2 C^{20} & \dots & \dots \\ 2.3 C^{11} 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1 Permutators definitions

$$\begin{split} P(k_1/k_2) &= 1 - P_{k_1k_2} \\ P(k_1/k_2k_3) &= 1 - P_{k_1k_2} - P_{k_1k_3} \\ P(k_1/k_2k_3k_4) &= 1 - P_{k_1k_2} - P_{k_1k_3} - P_{k_1k_4} \\ P(k_1k_2/k_3k_4) &= 1 - P_{k_1k_3} - P_{k_1k_4} - P_{k_2k_3} - P_{k_2k_4} + P_{k_1k_3}P_{k_2k_4} + P_{k_2k_3}P_{k_1k_4} \end{split}$$

2
$$d_{\text{max}} = 1$$

2.1 C^{00}

Diagram 1 (+AB):

$$C^{00}(02,20) = \frac{1}{2} \sum_{p_1 p_2} A^{02}_{p_1 p_2} B^{20}_{p_1 p_2}$$
(1)



Diagram 2 (-BA):

$$C^{00}(20,02) = -\frac{1}{2} \sum_{p_1 p_2} B_{p_1 p_2}^{02} A_{p_1 p_2}^{20}$$
(2)



2.2 C^{20}

Diagram 3 (+AB):

$$C_{k_1 k_2}^{20}(11, 20) = P(k_1/k_2) \sum_{p_1} A_{k_1 p_1}^{11} B_{p_1 k_2}^{20}$$
(3)



Diagram 4 (-BA):

$$C_{k_1k_2}^{20}(20,11) = -P(k_1/k_2) \sum_{p_1} B_{k_1p_1}^{11} A_{p_1k_2}^{20}$$
(4)



2.3 C^{11}

Diagram 5 (+AB):

$$C_{k_1k_2}^{11}(11,11) = \sum_{p_1} A_{k_1p_1}^{11} B_{p_1k_2}^{11}$$
(5)



Diagram 6 (+AB):

$$C_{k_1k_2}^{11}(02,20) = \sum_{p_1} A_{k_2p_1}^{02} B_{p_1k_1}^{20}$$
(6)



Diagram 7 (-BA):

$$C_{k_1k_2}^{11}(11,11) = -\sum_{p_1} B_{k_1p_1}^{11} A_{p_1k_2}^{11}$$

$$\tag{7}$$



Diagram 8 (-BA):

$$C_{k_1k_2}^{11}(20,02) = -\sum_{p_1} B_{k_2p_1}^{02} A_{p_1k_1}^{20}$$
(8)



2.4 C^{02}

Diagram 9 (+AB):

$$C_{k_1k_2}^{02}(02,11) = P(k_1/k_2) \sum_{p_1} A_{k_1p_1}^{02} B_{p_1k_2}^{11}$$
(9)



Diagram 10 (-BA):

$$C_{k_1 k_2}^{02}(11,02) = -P(k_1/k_2) \sum_{p_1} B_{k_1 p_1}^{02} A_{p_1 k_2}^{11}$$
(10)



 $3 \quad d_{\max} = 2$

3.1 C^{00}

Diagram 11 (+AB):

$$C^{00}(04,40) = \frac{1}{24} \sum_{p_1 p_2 p_3 p_4} A^{04}_{p_1 p_2 p_3 p_4} B^{40}_{p_1 p_2 p_3 p_4}$$

$$\tag{11}$$



Diagram 12 (-BA):

$$C^{00}(40,04) = -\frac{1}{24} \sum_{p_1 p_2 p_3 p_4} B^{04}_{p_1 p_2 p_3 p_4} A^{40}_{p_1 p_2 p_3 p_4}$$

$$\tag{12}$$



3.2 C^{20}

Diagram 13 (+AB):

$$C_{k_1k_2}^{20}(02,40) = \frac{1}{2} \sum_{p_1p_2} A_{p_1p_2}^{02} B_{p_1p_2k_1k_2}^{40}$$
 (13)



Diagram 14 (+AB):

$$C_{k_1k_2}^{20}(13,40) = P(k_1/k_2) \frac{1}{6} \sum_{p_1p_2p_3} A_{k_1p_1p_2p_3}^{13} B_{p_1p_2p_3k_2}^{40}$$
(14)



Diagram 15 (+AB):

$$C_{k_1k_2}^{20}(22,20) = \frac{1}{2} \sum_{p_1p_2} A_{k_1k_2p_1p_2}^{22} B_{p_1p_2}^{20}$$
 (15)



Diagram 16 (-BA):

$$C_{k_1k_2}^{20}(40,02) = -\frac{1}{2} \sum_{p_1p_2} B_{p_1p_2}^{02} A_{p_1p_2k_1k_2}^{40}$$
(16)



Diagram 17 (-BA):

$$C_{k_1k_2}^{20}(40,13) = -P(k_1/k_2) \frac{1}{6} \sum_{p_1p_2p_3} B_{k_1p_1p_2p_3}^{13} A_{p_1p_2p_3k_2}^{40}$$
(17)



Diagram 18 (-BA):

$$C_{k_1k_2}^{20}(20,22) = -\frac{1}{2} \sum_{p_1p_2} B_{k_1k_2p_1p_2}^{22} A_{p_1p_2}^{20}$$
(18)



3.3 C^{40}

Diagram 19 (+AB):

$$C_{k_1 k_2 k_3 k_4}^{40}(11, 40) = P(k_1/k_2 k_3 k_4) \sum_{p_1} A_{k_1 p_1}^{11} B_{p_1 k_2 k_3 k_4}^{40}$$
(19)



Diagram 20 (+AB):

$$C_{k_1k_2k_3k_4}^{40}(22,40) = P(k_1k_2/k_3k_4) \frac{1}{2} \sum_{p_1p_2} A_{k_1k_2p_1p_2}^{22} B_{p_1p_2k_3k_4}^{40}$$
(20)



Diagram 21 (+AB):

$$C_{k_1 k_2 k_3 k_4}^{40}(31, 20) = P(k_1 k_2 k_3 / k_4) \sum_{p_1} A_{k_1 k_2 k_3 p_1}^{31} B_{p_1 k_4}^{20}$$
(21)



Diagram 22 (-BA):

$$C_{k_1 k_2 k_3 k_4}^{40}(40, 11) = -P(k_1/k_2 k_3 k_4) \sum_{p_1} B_{k_1 p_1}^{11} A_{p_1 k_2 k_3 k_4}^{40}$$
(22)



Diagram 23 (-BA):

$$C_{k_1k_2k_3k_4}^{40}(40,22) = -P(k_1k_2/k_3k_4)\frac{1}{2}\sum_{p_1p_2}B_{k_1k_2p_1p_2}^{22}A_{p_1p_2k_3k_4}^{40}$$
 (23)



Diagram 24 (-BA):

$$C_{k_1 k_2 k_3 k_4}^{40}(20,31) = -P(k_1 k_2 k_3 / k_4) \sum_{p_1} B_{k_1 k_2 k_3 p_1}^{31} A_{p_1 k_4}^{20}$$
(24)



3.4 C^{11}

Diagram 25 (+AB):

$$C_{k_1k_2}^{11}(02,31) = \frac{1}{2} \sum_{p_1p_2} A_{p_1p_2}^{02} B_{p_1p_2k_1k_2}^{31}$$
 (25)



Diagram 26 (+*AB*):

$$C_{k_1 k_2}^{11}(13,31) = \frac{1}{6} \sum_{p_1 p_2 p_3} A_{k_1 p_1 p_2 p_3}^{13} B_{p_1 p_2 p_3 k_2}^{31}$$
(26)



Diagram 27 (+AB):

$$C_{k_1k_2}^{11}(04,40) = \frac{1}{6} \sum_{p_1p_2p_3} A_{k_2p_1p_2p_3}^{04} B_{p_1p_2p_3k_1}^{40}$$
(27)



Diagram 28 (+*AB*):

$$C_{k_1k_2}^{11}(13,20) = \frac{1}{2} \sum_{p_1p_2} A_{k_1k_2p_1p_2}^{13} B_{p_1p_2}^{20}$$
(28)



Diagram 29 (-BA):

$$C_{k_1 k_2}^{11}(31,02) = -\frac{1}{2} \sum_{p_1 p_2} B_{p_1 p_2}^{02} A_{p_1 p_2 k_1 k_2}^{31}$$
(29)



Diagram 30 (-BA):

$$C_{k_1k_2}^{11}(31,13) = -\frac{1}{6} \sum_{p_1p_2p_3} B_{k_1p_1p_2p_3}^{13} A_{p_1p_2p_3k_2}^{31}$$

$$\tag{30}$$



Diagram 31 (-BA):

$$C_{k_1 k_2}^{11}(40,04) = -\frac{1}{6} \sum_{p_1 p_2 p_3} B_{k_2 p_1 p_2 p_3}^{04} A_{p_1 p_2 p_3 k_1}^{40}$$
(31)



Diagram 32 (-BA):

$$C_{k_1k_2}^{11}(20,13) = -\frac{1}{2} \sum_{p_1p_2} B_{k_1k_2p_1p_2}^{13} A_{p_1p_2}^{20}$$
(32)



3.5 C^{31}

Diagram 33 (+AB):

$$C_{k_1 k_2 k_3 k_4}^{31}(11,31) = P(k_1/k_2 k_3) \sum_{p_1} A_{k_1 p_1}^{11} B_{p_1 k_2 k_3 k_4}^{31}$$
(33)



Diagram 34 (+AB):

$$C_{k_1 k_2 k_3 k_4}^{31}(22,31) = P(k_1 k_2 / k_3) \frac{1}{2} \sum_{p_1 p_2} A_{k_1 k_2 p_1 p_2}^{22} B_{p_1 p_2 k_3 k_4}^{31}$$
(34)



Diagram 35 (+AB):

$$C^{31}_{k_1 k_2 k_3 k_4}(31,11) = \sum_{p_1} A^{31}_{k_1 k_2 k_3 p_1} B^{11}_{p_1 k_4}$$

$$\tag{35}$$



Diagram 36 (+AB):

$$C_{k_1 k_2 k_3 k_4}^{31}(02, 40) = \sum_{p_1} A_{k_4 p_1}^{02} B_{p_1 k_1 k_2 k_3}^{40}$$
(36)



Diagram 37 (+AB):

$$C_{k_1 k_2 k_3 k_4}^{31}(13, 40) = P(k_1/k_2 k_3) \frac{1}{2} \sum_{p_1 p_2} A_{k_1 k_4 p_1 p_2}^{13} B_{p_1 p_2 k_2 k_3}^{40}$$
(37)



Diagram 38 (+AB):

$$C_{k_1 k_2 k_3 k_4}^{31}(22, 20) = P(k_1 k_2 / k_3) \sum_{p_1} A_{k_1 k_2 k_4 p_1}^{22} B_{p_1 k_3}^{20}$$
(38)



Diagram 39 (-BA):

$$C^{31}_{k_1 k_2 k_3 k_4}(31, 11) = -P(k_1/k_2 k_3) \sum_{p_1} B^{11}_{k_1 p_1} A^{31}_{p_1 k_2 k_3 k_4}$$
(39)



Diagram 40 (-BA):

$$C_{k_1 k_2 k_3 k_4}^{31}(31, 22) = -P(k_1 k_2 / k_3) \frac{1}{2} \sum_{p_1 p_2} B_{k_1 k_2 p_1 p_2}^{22} A_{p_1 p_2 k_3 k_4}^{31}$$

$$\tag{40}$$



Diagram 41 (-BA):

$$C_{k_1 k_2 k_3 k_4}^{31}(11,31) = -\sum_{p_1} B_{k_1 k_2 k_3 p_1}^{31} A_{p_1 k_4}^{11}$$

$$\tag{41}$$



Diagram 42 (-BA):

$$C_{k_1 k_2 k_3 k_4}^{31}(40,02) = -\sum_{p_1} B_{k_4 p_1}^{02} A_{p_1 k_1 k_2 k_3}^{40}$$

$$\tag{42}$$



Diagram 43 (-BA):

$$C_{k_1 k_2 k_3 k_4}^{31}(40, 13) = -P(k_1/k_2 k_3) \frac{1}{2} \sum_{p_1 p_2} B_{k_1 k_4 p_1 p_2}^{13} A_{p_1 p_2 k_2 k_3}^{40}$$

$$\tag{43}$$



Diagram 44 (-BA):

$$C_{k_1 k_2 k_3 k_4}^{31}(20, 22) = -P(k_1 k_2 / k_3) \sum_{p_1} B_{k_1 k_2 k_4 p_1}^{22} A_{p_1 k_3}^{20}$$

$$\tag{44}$$



3.6 C^{02}

Diagram 45 (+AB):

$$C_{k_1k_2}^{02}(02,22) = \frac{1}{2} \sum_{p_1p_2} A_{p_1p_2}^{02} B_{p_1p_2k_1k_2}^{22}$$

$$\tag{45}$$



Diagram 46 (+AB):

$$C_{k_1k_2}^{02}(04,31) = P(k_1/k_2) \frac{1}{6} \sum_{p_1p_2p_3} A_{k_1p_1p_2p_3}^{04} B_{p_1p_2p_3k_2}^{31}$$

$$\tag{46}$$



Diagram 47 (+*AB*):

$$C_{k_1k_2}^{02}(04,20) = \frac{1}{2} \sum_{p_1p_2} A_{k_1k_2p_1p_2}^{04} B_{p_1p_2}^{20}$$

$$\tag{47}$$



Diagram 48 (-BA):

$$C_{k_1k_2}^{02}(22,02) = -\frac{1}{2} \sum_{p_1p_2} B_{p_1p_2}^{02} A_{p_1p_2k_1k_2}^{22}$$

$$\tag{48}$$



Diagram 49 (-BA):

$$C_{k_1k_2}^{02}(31,04) = -P(k_1/k_2) \frac{1}{6} \sum_{p_1p_2p_3} B_{k_1p_1p_2p_3}^{04} A_{p_1p_2p_3k_2}^{31}$$

$$\tag{49}$$



Diagram 50 (-BA):

$$C_{k_1k_2}^{02}(20,04) = -\frac{1}{2} \sum_{p_1p_2} B_{k_1k_2p_1p_2}^{04} A_{p_1p_2}^{20}$$

$$\tag{50}$$



3.7 C^{22}

Diagram 51 (+AB):

$$C_{k_1 k_2 k_3 k_4}^{22}(11, 22) = P(k_1/k_2) \sum_{p_1} A_{k_1 p_1}^{11} B_{p_1 k_2 k_3 k_4}^{22}$$
(51)



Diagram 52 (+AB):

$$C_{k_1k_2k_3k_4}^{22}(22,22) = \frac{1}{2} \sum_{p_1p_2} A_{k_1k_2p_1p_2}^{22} B_{p_1p_2k_3k_4}^{22}$$
 (52)



Diagram 53 (+AB):

$$C_{k_1 k_2 k_3 k_4}^{22}(02,31) = P(k_3/k_4) \sum_{p_1} A_{k_3 p_1}^{02} B_{p_1 k_1 k_2 k_4}^{31}$$

$$(53)$$

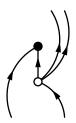


Diagram 54 (+AB):

$$C_{k_1k_2k_3k_4}^{22}(13,31) = P(k_1/k_2)P(k_3/k_4)\frac{1}{2}\sum_{p_1p_2}A_{k_1k_3p_1p_2}^{13}B_{p_1p_2k_2k_4}^{31}$$
(54)



Diagram 55 (+AB):

$$C_{k_1 k_2 k_3 k_4}^{22}(22,11) = P(k_3/k_4) \sum_{p_1} A_{k_1 k_2 k_3 p_1}^{22} B_{p_1 k_4}^{11}$$
(55)



Diagram 56 (+AB):

$$C_{k_1k_2k_3k_4}^{22}(04,40) = \frac{1}{2} \sum_{p_1p_2} A_{k_3k_4p_1p_2}^{04} B_{p_1p_2k_1k_2}^{40}$$
(56)



Diagram 57 (+*AB*):

$$C_{k_1 k_2 k_3 k_4}^{22}(13, 20) = P(k_1/k_2) \sum_{p_1} A_{k_1 k_3 k_4 p_1}^{13} B_{p_1 k_2}^{20}$$
(57)



Diagram 58 (-BA):

$$C_{k_1 k_2 k_3 k_4}^{22}(22,11) = -P(k_1/k_2) \sum_{p_1} B_{k_1 p_1}^{11} A_{p_1 k_2 k_3 k_4}^{22}$$
(58)



Diagram 59 (-BA):

$$C_{k_1k_2k_3k_4}^{22}(22,22) = -\frac{1}{2} \sum_{p_1p_2} B_{k_1k_2p_1p_2}^{22} A_{p_1p_2k_3k_4}^{22}$$
(59)



Diagram 60 (-BA):

$$C_{k_1 k_2 k_3 k_4}^{22}(31,02) = -P(k_3/k_4) \sum_{p_1} B_{k_3 p_1}^{02} A_{p_1 k_1 k_2 k_4}^{31}$$

$$\tag{60}$$



Diagram 61 (-BA):

$$C_{k_1 k_2 k_3 k_4}^{22}(31, 13) = -P(k_1/k_2)P(k_3/k_4)\frac{1}{2} \sum_{p_1 p_2} B_{k_1 k_3 p_1 p_2}^{13} A_{p_1 p_2 k_2 k_4}^{31}$$

$$\tag{61}$$



Diagram 62 (-BA):

$$C_{k_1 k_2 k_3 k_4}^{22}(11, 22) = -P(k_3/k_4) \sum_{p_1} B_{k_1 k_2 k_3 p_1}^{22} A_{p_1 k_4}^{11}$$

$$(62)$$



Diagram 63 (-BA):

$$C_{k_1k_2k_3k_4}^{22}(40,04) = -\frac{1}{2} \sum_{p_1p_2} B_{k_3k_4p_1p_2}^{04} A_{p_1p_2k_1k_2}^{40}$$
(63)



Diagram 64 (-BA):

$$C_{k_1k_2k_3k_4}^{22}(20,13) = -P(k_1/k_2) \sum_{p_1} B_{k_1k_3k_4p_1}^{13} A_{p_1k_2}^{20}$$
(64)



3.8 C^{13}

Diagram 65 (+AB):

$$C_{k_1k_2k_3k_4}^{13}(11,13) = \sum_{p_1} A_{k_1p_1}^{11} B_{p_1k_2k_3k_4}^{13}$$

$$(65)$$



Diagram 66 (+AB):

$$C_{k_1 k_2 k_3 k_4}^{13}(02, 22) = P(k_2/k_3 k_4) \sum_{p_1} A_{k_2 p_1}^{02} B_{p_1 k_1 k_3 k_4}^{22}$$

$$(66)$$



Diagram 67 (+*AB*):

$$C_{k_1 k_2 k_3 k_4}^{13}(13, 22) = P(k_2/k_3 k_4) \frac{1}{2} \sum_{p_1 p_2} A_{k_1 k_2 p_1 p_2}^{13} B_{p_1 p_2 k_3 k_4}^{22}$$

$$(67)$$



Diagram 68 (+AB):

$$C_{k_1 k_2 k_3 k_4}^{13}(04,31) = P(k_2 k_3 / k_4) \frac{1}{2} \sum_{p_1 p_2} A_{k_2 k_3 p_1 p_2}^{04} B_{p_1 p_2 k_1 k_4}^{31}$$

$$(68)$$



Diagram 69 (+AB):

$$C_{k_1k_2k_3k_4}^{13}(13,11) = P(k_2k_3/k_4) \sum_{p_1} A_{k_1k_2k_3p_1}^{13} B_{p_1k_4}^{11}$$

$$(69)$$



Diagram 70 (+AB):

$$C_{k_1 k_2 k_3 k_4}^{13}(04, 20) = \sum_{p_1} A_{k_2 k_3 k_4 p_1}^{04} B_{p_1 k_1}^{20}$$

$$(70)$$



Diagram 71 (-BA):

$$C_{k_1 k_2 k_3 k_4}^{13}(13, 11) = -\sum_{p_1} B_{k_1 p_1}^{11} A_{p_1 k_2 k_3 k_4}^{13}$$

$$(71)$$



Diagram 72 (-BA):

$$C_{k_1 k_2 k_3 k_4}^{13}(22,02) = -P(k_2/k_3 k_4) \sum_{p_1} B_{k_2 p_1}^{02} A_{p_1 k_1 k_3 k_4}^{22}$$
(72)



Diagram 73 (-BA):

$$C_{k_1 k_2 k_3 k_4}^{13}(22, 13) = -P(k_2/k_3 k_4) \frac{1}{2} \sum_{p_1 p_2} B_{k_1 k_2 p_1 p_2}^{13} A_{p_1 p_2 k_3 k_4}^{22}$$

$$(73)$$



Diagram 74 (-BA):

$$C_{k_1 k_2 k_3 k_4}^{13}(31,04) = -P(k_2 k_3 / k_4) \frac{1}{2} \sum_{p_1 p_2} B_{k_2 k_3 p_1 p_2}^{04} A_{p_1 p_2 k_1 k_4}^{31}$$

$$(74)$$



Diagram 75 (-BA):

$$C_{k_1k_2k_3k_4}^{13}(11,13) = -P(k_2k_3/k_4) \sum_{p_1} B_{k_1k_2k_3p_1}^{13} A_{p_1k_4}^{11}$$

$$\tag{75}$$



Diagram 76 (-BA):

$$C_{k_1 k_2 k_3 k_4}^{13}(20,04) = -\sum_{p_1} B_{k_2 k_3 k_4 p_1}^{04} A_{p_1 k_1}^{20}$$

$$\tag{76}$$



3.9 C^{04}

Diagram 77 (+AB):

$$C_{k_1 k_2 k_3 k_4}^{04}(02, 13) = P(k_1/k_2 k_3 k_4) \sum_{p_1} A_{k_1 p_1}^{02} B_{p_1 k_2 k_3 k_4}^{13}$$

$$(77)$$



Diagram 78 (+AB):

$$C_{k_1 k_2 k_3 k_4}^{04}(04, 22) = P(k_1 k_2 / k_3 k_4) \frac{1}{2} \sum_{p_1 p_2} A_{k_1 k_2 p_1 p_2}^{04} B_{p_1 p_2 k_3 k_4}^{22}$$

$$(78)$$



Diagram 79 (+*AB*):

$$C_{k_1 k_2 k_3 k_4}^{04}(04, 11) = P(k_1 k_2 k_3 / k_4) \sum_{p_1} A_{k_1 k_2 k_3 p_1}^{04} B_{p_1 k_4}^{11}$$

$$(79)$$



Diagram 80 (-BA):

$$C_{k_1 k_2 k_3 k_4}^{04}(13,02) = -P(k_1/k_2 k_3 k_4) \sum_{p_1} B_{k_1 p_1}^{02} A_{p_1 k_2 k_3 k_4}^{13}$$

$$\tag{80}$$



Diagram 81 (-BA):

$$C_{k_1 k_2 k_3 k_4}^{04}(22,04) = -P(k_1 k_2 / k_3 k_4) \frac{1}{2} \sum_{p_1 p_2} B_{k_1 k_2 p_1 p_2}^{04} A_{p_1 p_2 k_3 k_4}^{22}$$
(81)



Diagram 82 (-BA):

$$C_{k_1 k_2 k_3 k_4}^{04}(11,04) = -P(k_1 k_2 k_3 / k_4) \sum_{p_1} B_{k_1 k_2 k_3 p_1}^{04} A_{p_1 k_4}^{11}$$
(82)

