$\begin{array}{c} MATH~272,~Exam~1\\ Take~Home~Portion\\ Due~February~19^{^{TH}}~at~the~start~of~class \end{array}$

Name				
our Canvas pag for this portion of your solution Ambiguous or	ge, but no other on n of the exam. D ons should be ea	nline resources o not discuss sily identifiabl will not be co	(including calcustance and supportion unted as correct	s, worksheets, material on alators or Wolfram Alpha). a any other person. Alling work must be shown. b. Print out this sheet ach problem.
	Problem 1	/10	Problem 2	/15

 $Note,\ these\ problems\ span\ two\ pages.$

In the heart of quantum mechanics lies probability theory. Since we can only compute the likelihood of observing something, we have to start thinking in this framework.

Problem 1. Consider a free particle constrained to the infinite line \mathbb{R} . Heisenberg's uncertainty principle states that one can never simultaneously know the position and momentum of a particle.

Suppose that we measure the *exact* position of a particle at time t = 0 to be at x_0 . Then the wavefunction for this particle is given by

$$\Psi(x) = \delta(x - x_0).$$

Thus, since we know the position exactly, we expect to know nothing about the particle's momentum.

(a)

Problem 2. Probability is described via probability distribution functions (PDFs) p(x). Intuitively, the value of p(x) at the point x describes the weighting of that point x. We require that

- $p(x) \ge 0$ for all $x \in \mathbb{R}$. (There is no negative probability.)
- $\int_{-\infty}^{\infty} p(x)dx = 1$. (The total probability is 1.)

We can then define the probability of measuring an outcome in the region [a,b] by

$$\mathcal{P}_{[a,b]}[p(x)] = \int_a^b p(x)dx.$$

- (a) free points problem for using $\delta(x-\mu)$ in an integral as a reminder of what the function does.
- (b) Consider the Gaussian with a variable σ , it's integral is 1. Maybe define erf(x)
- (c) take limit to get delta
- (d) Define delta as limit

Link to visual in desmos.