

# MDF: Magnetic Particle Imaging Data Format

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## Abstract

Magnetic particle imaging (MPI) is a tomographic method to determine the spatial distribution of magnetic nanoparticles. In this document a file format for the standardized storage of MPI and MPS data is introduced. The aim of the Magnetic Particle Imaging Data Format (MDF) is to provide a coherent way of exchanging MPI and MPS data acquired with different scanners worldwide. The focus of the file format is on sequence parameters, raw measurement data, calibration data, and reconstruction data. The format is based on the hierarchical document format (HDF) in version 5 (HDF5).

## 1 Introduction

The purpose of this document is to introduce a file format for exchanging Magnetic Particle Imaging (MPI) and Magnetic Particle Spectroscopy (MPS) data. The Magnetic Particle Imaging Data Format (MDF) is based on the hierarchical document format (HDF) in version 5 (HDF5) [1]. HDF5

allows to store multiple datasets within a single file and is thus very flexible to use. To allow the exchange of MPI data, one has to specify a naming scheme within HDF5 files which is the purpose of this document. In order to create and access HDF5 data, an Open Source C library is available. For most programming languages bindings to this library exist. Matlab supports HDF5 by the functions `h5read` and `h5write`. For Python the `h5py` package exists. The Julia programming language provides access to HDF5 files via the `HDF5` package. For languages based on the .NET framework the `HDF5DotNet` library is available.

The current version is mainly focused on storing raw measurement data, system matrices, or reconstruction data together with corresponding sequence parameters and meta data. Though it is possible to combine measurement data and reconstruction data into a single file it is recommended to use a single file for each of the following dataset types:

1. Measurement data
2. System calibration data
3. Reconstruction data

## 1.1 Datatypes

For most parameters a fixed datatype is used, i.e. the drive-field amplitudes are stored as `H5T_NATIVE_DOUBLE` values. For our convinience we refer to the HDF5 datatypes `H5T_STRING`, `H5T_NATIVE_DOUBLE` and `H5T_NATIVE_INT64` as `String`, `Float64` and `Int64`. The datatype of the measurement data and the calibration data offers more freedom and is denoted by `Number`, which can be any of the following HDF5 data types: `H5T_NATIVE_FLOAT`, `H5T_NATIVE_DOUBLE`, `H5T_NATIVE_INT8`, `H5T_NATIVE_INT16`, `H5T_NATIVE_INT32`, and `H5T_NATIVE_INT64`. Whenever Boolean data has to be stored we use `H5T_NATIVE_INT8` for storage.

MPI parameters are stored as regular *HDF5 datasets*. *HDF5 attributes* are not used in the current specification of the MDF.

Since storing complex data in HDF5 is not standardized, we extend the dimensionality of an existing array and store the real and imaginary part in the last dimension with size 2 (index 0 = real part, index 1 = imaginary part). In this way the real and imaginary part of a complex datum is stored sequentially on disk. When loading the data it is possible to cast it to a complex array in most programming languages.

## 1.2 Units

Physical quantities are given in SI units with one exception. The field strength is reported in  $T\mu_0^{-1} = 4\pi \text{ Am}^{-1}\mu_0^{-1}$ . This convention has been proposed in the first MPI publication and since that time consistently used in most MPI related publications. The aim of this convention is to report the numbers on a Tesla scale, which most readers with a background in MRI are familiar with, but, on the other hand still use the correct unit for the magnetic field strength.

## 1.3 Sanity Check

In order to check if a generated MDF file is valid, we provide a sanity check script that can be found in the gitub repository:

<https://github.com/MagneticParticleImaging/MDF>

The code is written in the Julia programming language [2, 3, 4], which has to be downloaded from:

<http://julialang.org>.

More detailed instructions can be found in the `README` of the repository.

## 1.4 Parameter Extension

Often you will find that you want to store parameters or meta data which are specific to your side. For example the temperature of the room in which your MPI device is operated. In this case you are free to add a new parameters to any of the existing groups. Moreover if necessary you are also free to introduce new groups. To be able to distinguish these datasets

and groups from the specified ones we recommend to use the prefix **E** for all parameters and groups. In our example I could add a new group **Eroom** and within the dataset **Etemperature**.

## 1.5 Contact

If you find mistakes in this document or the specified file format or if you want to discuss extensions to this specification, please open an issue on GitHub:

<https://github.com/MagneticParticleImaging/MDF>

As the file format is versionized it will be possible to extend it for future

needs of MPI. The current version discussed in this document is version 2.0.0-pre.

## 1.6 arXiv

As of version 1.0.1 the most recent release of these specifications can also be also found on the arXiv:

<http://arxiv.org/abs/1602.06072>

If you use MDF please cite us using the arXiv reference, which is also available for download as **MDF.bib** from GitHub.

# 2 Data (group: /)

**Remarks:** Within the root group metadata about the file itself is stored. Within several subgroups, metadata about the experimental setting, the MPI tracer, and the MPI scanner can be provided. The actual data is

stored in dedicated groups on measurement data, calibration data, and/or reconstruction data.

Parameter	Type	Dim	Unit/Format	Optional	Description
version	<a href="#">String</a>	1	0.1	no	Version of the file format
uuid	<a href="#">String</a>	1	f81d4fae-7dec-11d0-a765-00a0c91e6bf6	no	Universally Unique Identifier (RFC 4122)
time	<a href="#">String</a>	1	yyyy-mm-ddThh:mm:ss.ms	no	UTC creation time of MDF data set

## 2.1 Study Description (group: /study/)

**Remarks:** A study is supposed to group a series of experiments to support, refute, or validate a hypothesis. The study group may contain **name**, **number**, and **description** of the study.

Parameter	Type	Dim	Unit/Format	Optional	Description
name	String	1		yes	Name of the study
number	Int64	1		yes	Experiment number within study
description	String	1		yes	Short description of the experiment

## 2.2 Experiment Description (group: /experiment/)

**Remarks:** For each experiment within a study **name**, **number**, and **description** may be provided. Additionally, the name of the imaged subject and a flag indicating if data has been obtained via simulations can be stored.

Parameter	Type	Dim	Unit/Format	Optional	Description
name	String	1		yes	Experiment name
number	Int64	1		yes	Experiment number
description	String	1		yes	Short description of the experiment
subject	String	1		yes	Name of the subject that was imaged
isSimulation	Int8	1		yes	Flag indicating if the data in this file is simulated rather than measured

## 2.3 Tracer Parameters (group: /tracer/)

**Remarks:** The tracer parameter group contains information about the MPI tracers used during the experiment. For each tracer its **name**, **batch**, **vendor**, its **volume**, its molar **concentration** of **solute** per litre and the time point of injection can be provided.

This version of the MDF can handle two basic scenarios. In the first one static tracer phantoms are used. In this case the phantom contains  $A$  distinct tracers. These might be particles of different core sizes, mobile

or immobilized particles for example. In this case **injectionTime** is not used. In the second case  $A$  boli (e.g. pulsed boli) are administrated during the measurement, in which case the approximate administration volume, tracer type and time point of injection can be provided. Note that the injection clock recording the injection time should be synchronized with the clock, which provides the starting time of the measurement.

Parameter	Type	Dim	Unit/Format	Optional	Description
name	<a href="#">String</a>	A		yes	Name of tracer used in experiment
batch	<a href="#">String</a>	A		yes	Batch of tracer
vendor	<a href="#">String</a>	A		yes	Name of tracer supplier
volume	<a href="#">Float64</a>	A	L	yes	Total volume of applied tracer
concentration	<a href="#">Float64</a>	A	mol(solute)/L	yes	Molar concentration of solute per litre
solute	<a href="#">String</a>	A		yes	Solute, e.g. Fe
injectionTime	<a href="#">String</a>	A	yyyy-mm-ddThh:mm:ss.ms	yes	UTC time at which tracer injection started

## 2.4 Scanner Parameters (group: /scanner/)

**Remarks:** The scanner parameter group contains information about the MPI scanner used such as the manufacturer, the model, bore size, the field topology, and the facility where the scanner is installed.

Parameter	Type	Dim	Unit/Format	Optional	Description
facility	<a href="#">String</a>	1		yes	Facility where the MPI scanner is installed
operator	<a href="#">String</a>	1		yes	User who operates the MPI scanner
manufacturer	<a href="#">String</a>	1		yes	Scanner manufacturer
model	<a href="#">String</a>	1		yes	Scanner model
topology	<a href="#">String</a>	1		no	Scanner topology (e.g. FFP, FFL, MPS)
boreSize	<a href="#">Float64</a>	1		yes	Scanner model

## 2.5 Acquisition Parameters (group: /acquisition/)

**Remarks:** The acquisition parameter group can describe different imaging protocols and trajectory settings. The corresponding data is organized into general information within this group, a subgroup containing information on the  $D$  excitation channels and a subgroup containing information on the  $C$  receive channels.

In general each MPI dataset consists of measurement data of  $N + M$  frames, where  $N$  is the number of subject measurements and  $M$  is the number of background measurements. A frame groups together all data that will can used to reconstruct a single MPI image/tomogram. In the simplest scenario a frame consist of the data acquired during a single drive field cy-

cle. If averaging is applied at the receiver the time it takes to capture a single frame increases by `receiver/numAverages`, but the amount of data captured remains the same. In a multi patch setting  $J$  `offsetFields` or mechanical movements shift the gradient field by `offsetFieldShift` to different spatial positions. Here  $J$  is the number patches of a multi patch measurement. In such a scenario a frame may consist of  $J$  sub-measurements, each of which is acquired and averaged over `receiver/numAverages` drive field cycles. For instance a Cartesian 2D trajectory with 100 lines would be realized by setting `numPatches = 100`.

Parameter	Type	Dim	Unit/Format	Optional	Description
<code>startTime</code>	<a href="#">String</a>	1	yyyy-mm-ddThh:mm:ss.ms	no	UTC start time of MPI measurement
<code>numFrames</code>	<a href="#">Int64</a>	1	1	no	Number of available measurement frames, denoted by $N$
<code>numBackgroundFrames</code>	<a href="#">Int64</a>	1	1	no	Number of available background measurement frames, denoted by $M$
<code>framePeriod</code>	<a href="#">Float64</a>	1	s	no	Complete time to acquire data of a full frame (product of drive field <code>period</code> , <code>numPatches</code> , and <code>numAverages</code> )
<code>numPatches</code>	<a href="#">Int64</a>	1	1	no	Number of patches within a frame denoted by $J$
<code>gradient</code>	<a href="#">Float64</a>	$J \times 3$	$\text{Tm}^{-1}\mu_0^{-1}$	yes	Gradient strength of the selection field in $x$ , $y$ , and $z$ directions
<code>offsetField</code>	<a href="#">Float64</a>	$J \times 3$	$\text{T}\mu_0^{-1}$	yes	Offset field applied for each patch in the measurement sequence
<code>offsetFieldShift</code>	<a href="#">Float64</a>	$J \times 3$	m	yes	Position of the field free point (relative to origin/center)

### 2.5.1 Drive Field (group: `/acquisition/drivefield/`)

**Remarks:** The drive field subgroup describes the excitation details of the imaging protocol. On the lowest level each MPI scanner contains  $D$  chan-

nels for particle excitation. Since most drive-field parameters may change from patch to patch they have a leading dimension  $J$ .

These excitation signals are usually sinusoidal and can be described by  $D$  amplitudes (drive field strengths),  $D$  phases, a base frequency, and  $D$  dividers. In a more general setting generated drive-fields of channel  $d$  can be described by

$$H_d(t) = \sum_{l=1}^F A_l \Lambda_l(2\pi f_l t + \varphi_l)$$

where  $F$  is the number of frequencies on the channel,  $A_l$  is the drive-field strength,  $\phi_l$  is the phase,  $f_l$  is the frequency (described by the base fre-

quency and the divider), and  $\Lambda_l$  is the waveform. The waveform is specified by a dedicated parameter **waveform**. it can be set to *sine*, *triangle* or *custom*. If set to *custom*, one can specify a custom waveform using the parameter **customWaveform**. The number of sampling points of the **customWaveform** is denoted by  $U$ . The triangle is defined to be a  $2\pi$  periodization of the triangle function:

$$\Lambda_{\text{tri}}(t) = \left| t + \frac{\pi}{2} \right| - \frac{\pi}{2} \quad \text{for} \quad -\frac{3}{2}\pi \leq t \leq \frac{\pi}{2}$$

Parameter	Type	Dim	Unit/Format	Optional	Description
numChannels	Int64	1	1	no	Number of drive field channels, denoted by $D$
strength	Float64	$J \times D \times F$	$\text{T}\mu_0^{-1}$	no	Applied drive field strength
phase	Float64	$J \times D \times F$	rad	no	Applied drive field phase $\varphi$ in radians in the range $[-\pi, \pi)$
baseFrequency	Float64	1	Hz	no	Base frequency to derive drive field frequencies
customWaveform	Float64	$D \times F \times U$	1	yes	Custom waveform table
divider	Int64	$D \times F$	1	no	Divider for drive fields frequencies ( <b>baseFrequency</b> / <b>divider</b> )
waveform	String	$D \times F$	1	no	Waveform type: <i>sine</i> , <i>triangle</i> or <i>custom</i>
period	Float64	1	s	no	Drive field trajectory period

### 2.5.2 Receiver (group: /acquisition/receiver/)

**Remarks:** The receiver subgroup describes details on the MPI receiver. For a multi-patch sequence it is assumed, that signal acquisition only takes place during particle excitation. During each drive-field cycle,  $C$  receive channels record some quantity related to the magnetization dynamic. In most cases these will be a voltage signals induced into the  $C$  receive coils, which are proportional to the change of the particle magnetization.

The MPI signal is obtained at  $Z$  equidistant time points. Note that in most cases the voltages are not measured directly at the receive coils but amplified and filtered first. To be able to compensate these changes the transfer function can optionally be stored in the parameter **transferFunction**. It is stored in frequency space representation where  $K = \frac{Z}{2} + 1$  is the number of discrete frequency components.

Parameter	Type	Dim	Unit/Format	Optional	Description
numChannels	Int64	1		no	Number of receive channels $C$
numAverages	Int64	1		no	Internal block averaging over a number of drive field cycles
bandwidth	Float64	1	Hz	no	Bandwidth of the receiver unit
numSamplingPoints	Int64	1		no	Number of sampling point within one drive-field period denoted by $Z$
transferFunction	Float64	$C \times K \times 2$		yes	Transfer function of the receive channel

## 2.6 Measurement (group: /measurement/)

**Remarks: TODO Tobi: Update group with the changes from latest discussion.** MPI data is usually acquired by a series of  $N$  measurements and  $M$  background measurements. Here we refer to background measurements as MPI data captured, when any signal generating material, e.g. a phantom or a delta sample is removed from the scanner bore. Both the  $N$  measurements and the  $M$  background measurements can be stored in an arbitrary order, e.g. with respect to the spatial position of a delta sample if the data corresponds to a calibration measurement. To be able to recover the time order in which the measurements were taken each of the  $N + M$  data sets can be assigned an integer number  $o = 1, 2, \dots, N + M$  ordering the measurements and background measurements with respect to time. I.e. data set  $o_1$  is acquired prior to data set  $o_2$ , if and only if  $o_1 < o_2$ .

The resulting  $N$  measurements and  $M$  background measurements should be stored in time domain, where the data of a single frame consists

of the signal recorded for all patches in each receive channel, i.e.  $J \times C \times Z$  data points per set with the temporal index being the fastest to access. If several measurements are acquired (indicated by *numFrames*), the  $N$  measurements and  $M$  background measurements are concatenated along the slowest dimension respectively.

During measurements the analog signal measured is usually converted into  $(r_1, \dots, r_{JZ}) \in \mathbb{Z}^J \times \mathbb{Z}^Z$  integer values per channel  $c \in C$  and frame using analog to digital converters. Often this raw data is stored instead of the physical quantities they represent. To bring the raw values into a physical representation one can map  $r_i \mapsto (a_c r_i + b_c)U$ , where  $a_c$  and  $b_c$  are the characteristic dimensionless scaling factor and offset the receive channel  $c \in C$  and  $U$  is the corresponding unit of measurement, i.e. usually voltages.



Parameter	Type	Dim	Unit/Format	Optional	Description
unit	String	1		yes	SI unit of the measured quantity, usually V
dataConversionFactor	Number	$C \times 2$		yes	Dimension less scaling factor and offset ( $a_c, b_c$ ) to convert raw data into a physical quantity with corresponding unit of measurement <b>unit</b>
data	Number	$N + M \times J \times C \times Z$		yes	Measurement data stored in time domain representation
isBackgroundData	Int8	$N + M$		yes	Boolean mask indicating for each frame if it contains background data or not.

## 2.7 Processing (group: /processing/)

Parameter	Type	Dim	Unit/Format	Optional	Description
processedData	Number	$Q \times J \times C \times K \times 2$		yes	Processed data stored in frequency domain representation
processedDataTransposed	Number	$J \times C \times K \times Q \times 2$		yes	As processed data but transposed
isSpectralLeakageCorrected	Int8	1		yes	flag indicating if spectral leakage correction has been applied
isTransferFunctionCorrected	Int8	1		yes	flag indicating if the transfer function has been corrected
isAveraged	Int8	1		yes	flag indicating if the raw data has been averaged in a processing step
isFramesSelected	Int8	1		yes	flag indicating if the processed data contains only a selection of the raw data
isBackgroundCorrected	Int8	1		yes	flag indicating if a background has been corrected
permutation	Int64	$Q$		yes	Index vector indicating a permutation of the $Q$ frames

## 2.8 Calibration (group: /calibration/)

Remarks: TODO Tobi: Update group with the changes from latest discussion.

Parameter	Type	Dim	Unit/Format	Optional	Description
snr	Float64	$J \times C \times K$		yes	Signal-to-noise estimate for recorded frequency components
fieldOfView	Float64	3	m	yes	Field of view of system matrix
fieldOfViewCenter	Float64	3	m	yes	Center of the system matrix (relative to origin/center)
size	Int64	3		yes	Number of voxels in each dimension
orderDimensions	String	1		yes	Ordering of the dimensions, default is <i>xyz</i>
positions	Float64	$Q \times 3$	m	yes	Position of each of the grid points, stored as $(x, y, z)$ triples
offsetField	Float64	$Q \times 3$	$T\mu_0^{-1}$	yes	Applied offset field strength to emulate a spatial position $(x, y, z)$
deltaSampleSize	Float64	3	m	yes	Size of delta sample used for calibration scan
method	String	1		yes	Method used to obtain calibration data. Can for instance be robot, hybrid, or simulation

## 2.9 Reconstruction Results (group: /reconstruction/)

Reconstruction results are stored in the parameter **data**. Dependent on the number of individual channels  $S$  obtained by the reconstruction the results can be stored in a  $L \times P$  array for  $S = 1$  or in a  $L \times P \times S$  array for  $S > 1$ . Since the grid of the reconstruction data can be different than the

system matrix grid, the grid parameter are mirrored in the reconstruction parameter group.

Usually the data is stored in a real data format but it is also possible to store complex data if the reconstruction output is complex.

Parameter	Type	Dim	Unit/Format	Optional	Description
data	Number	$L \times P \times S$		yes	Reconstructed data
fieldOfView	Float64	3	m	yes	Field of view of reconstructed data
fieldOfViewCenter	Float64	3	m	yes	Center of the reconstructed data (relative to origin/center)
size	Int64	3		yes	Number of voxels in each dimension
order	String	1		yes	Ordering of the dimensions, default is <i>xyz</i>
positions	Float64	$P \times 3$	m	yes	Position of each of the grid points, stored as $(x, y, z)$ tripels
overscanMask TODO martin :-)	Float64	$P \times 3$	m	yes	Position of each of the grid points, stored as $(x, y, z)$ tripels

## 3 Changelog

### 3.1 v2.0.0

- Updated Affiliations in the MDF specification.
- Made extensive improvements to the descriptions of fields and groups.
- In v1.x the MDF allowed certain fields to have varying dimensions depending on the context. This has been removed such that starting from v2.0 all dimensions have to be specified. This change should make implementations handling MDF files less complex.
- Specified supported data types for the storage of measurement data and reconstruction data.
- Rename `/date` to `/time` for consistency reasons.
- Remove `/study/reference` since this functionality is now covered by the integrated background measurements.
- Rename `/study/simulation` to `/study/isSimulation` for consistency reasons and changed type to `Int8`.
- Created new group `/experiment` with fields `/experiment/name`, `/experiment/number` and `/experiment/description` to be able to provide more fine grained information on study and experiment.
- Moved `/study/subject` and `/study/isSimulation` to `/experiment/subject` and `/experiment/isSimulation`.
- Renamed `/tracer/time` to `/tracer/injectionTime`.
- Added the possibility store the tracer concentration also for non iron based tracer materials by adding the `/tracer/solute` field and re-defining the field `tracer/concentration`.
- Renamed field `/tracer/time` to `/tracer/injectionTime` to be more specific.
- Added the dimension `A` to all fields of the `tracer` group to be able to describe settings where multiple tracers are used or tracers are administered multiple times.
- Added field `/scanner/boreSize` to describe the scanner.
- Set all fields but `topology` in the `/scanner` group to be optional.
- Rename `/acquisition/time` to `/acquisition/startTime`.
- `/acquisition/gradient` is now optional since it is now mandatory for MPS measurements.
- Added field `/acquisition/numBackgroundFrames` as counter for the number of measurements used for background subtraction.
- Added `/acquisition/offsetField` and `/acquisition/offsetFieldShift` to describe homogeneous offset fields.
- Support for triangle wave forms and fully arbitrary excitation waveforms has been added by adding the fields `/drivefield/phase`, `/drivefield/customWaveform`, `/drivefield/waveform`.
- Support for multiple excitation frequencies on a drive-field channel has been added by introducing a new dimension `F` to the fields `/drivefield/strength`, `/drivefield/phase`, `/drivefield/customWaveform`, `/drivefield/waveform`, and `/drivefield/divider`.
- Removed `fieldOfView` and `fieldOfViewCenter` from `/drivefield` group. `/acquisition/offsetField` and `/acquisition/offsetFieldShift` replace `fieldOfViewCenter`. The `fieldOfView` can be derived from the gradient strength and drive field strength.
- Moved `/drivefield/averages` to `/receiver/numAverages`

- Remove `/acquisition/receiver/frequencies` since it can be directly derived from `/acquisition/receiver/bandwidth` and `/acquisition/receiver/numSamplingPoints`.
- **TODO Tobi: record changes to /measurement group here.** Added possibility to store the transformation from raw data to a physical representation with units. Signal to noise ratios can now be stored for each patch individually. To do so the dimension  $J$  was added to this field.
- **TODO Tobi: record changes to /calibration group here.**
- Added new section changelog to the MDF documentation to record the development of the MDF.

### 3.2 v1.0.5

- Added the possibility to store different channels of reconstructed data.
- Added support for receive channels with different characteristics (e.g. bandwidth).
- Made dataset `/acquisition/receiver/frequencies` optional.
- Extended the description on the data types, which are used to store data.
- Added references for Julia and HDF5 to the specifications.

### 3.3 v1.0.4

- Clarify that HDF5 datasets are used to store MPI parameters.

### 3.4 v1.0.3

- Updated Affiliations in the MDF specification.
- Included data download into the Python and Matlab example code.
- Changes in the Python and Matlab example code to be better comparable to the Julia example code.

### 3.5 v1.0.2

- Added reference to arXiv paper and bibtex file for reference.

### 3.6 v1.0.1

- A sanity check within the Julia code shipped alongside the specifications.
- An update to the specification documenting the availability of a sanity check.
- Updated MDF files on <https://www.tuhh.de/ibi/research/mpi-data-format.html>.
- Updated documentation to the Julia, Matlab and Python reconstruction scripts.
- Improved Julia reconstruction script, automatically downloading the required MDF files.

## References

- [1] The HDF Group. Hierarchical Data Format, version 5, 1997-2016. <http://www.hdfgroup.org/HDF5/>.

- [2] Jeff Bezanson, Stefan Karpinski, Viral B. Shah, and Alan Edelman. Julia: A fast dynamic language for technical computing. *CoRR*, abs/1209.5145, 2012.
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