

# Introduction to Computer Graphics

GAMES101, Lingqi Yan, UC Santa Barbara

## Lecture 21: Animation



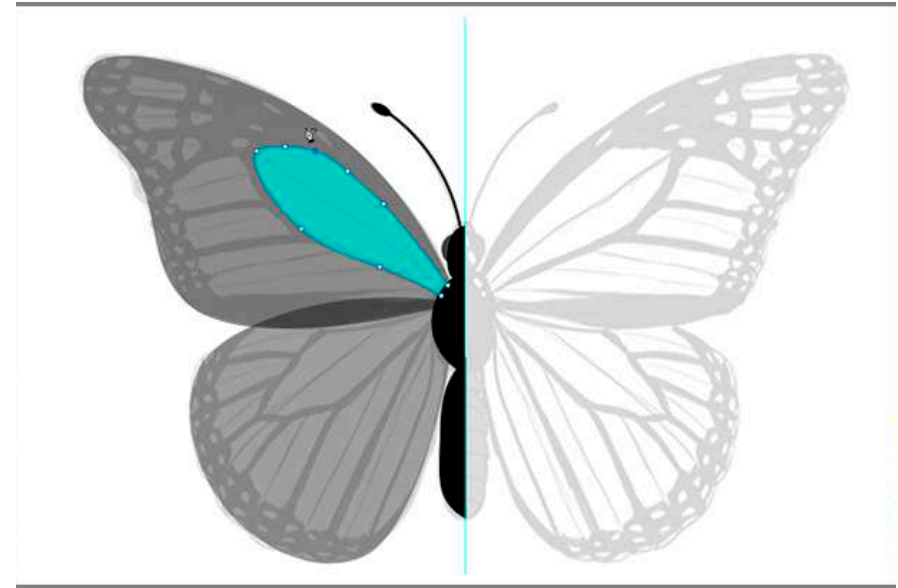
# Announcements

- Homework 7: 95 submissions so far
- Final project ideas: 18 submissions so far (expected more)
- My personal bad habit
  - Misuse of conjunctions
  - "OK", "so", etc. in English
  - "这个", "然后", etc. in Chinese
  - Can't really control when I'm thinking, but will try my best to avoid them

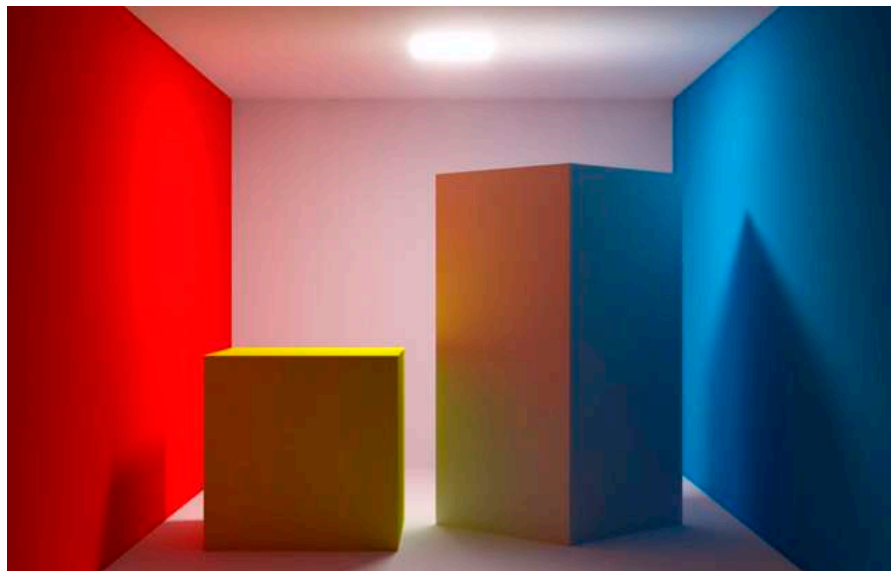
# Course Roadmap



Rasterization



Geometry



Light Transport



Animation / simulation

# Today

## Introduction to Computer Animation

- History
- Keyframe animation
- Physical simulation
- Kinematics
- Rigging

# Animation

“Bring things to life”

- Communication tool
- Aesthetic issues often dominate technical issues

An extension of modeling

- Represent scene models as a function of time

Output: sequence of images that when viewed sequentially provide a sense of motion

- Film: 24 frames per second
- Video (in general): 30 fps
- Virtual reality: 90 fps

# Historical Points in Animation

(slides courtesy of Prof. Keenan Crane @ CMU)

# First Animation



(Shahr-e Sukhteh, Iran 3200 BCE)



# History of Animation



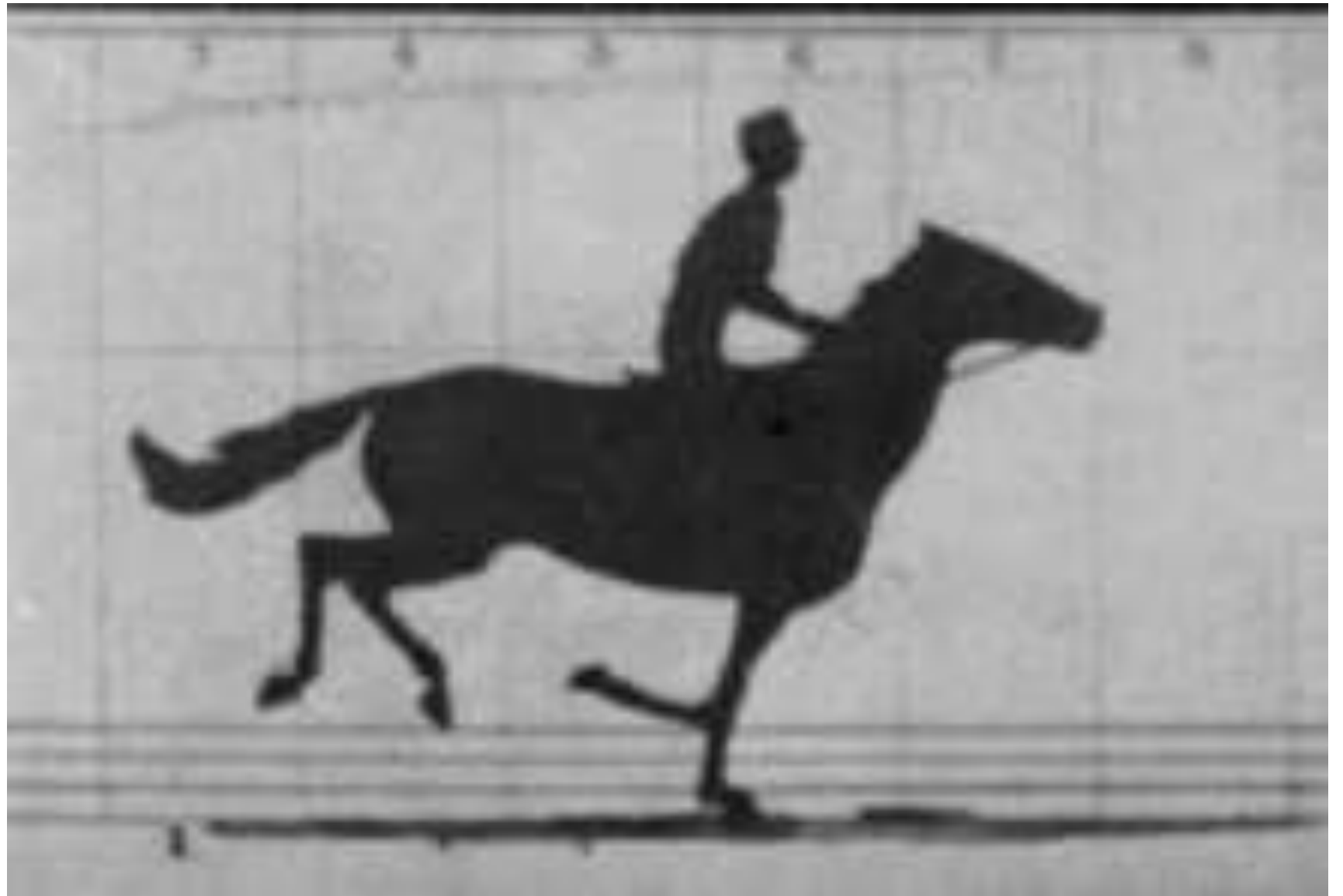
(Phenakistoscope, 1831)



# First Film

Originally used as scientific tool rather than for entertainment

Critical technology that accelerated development of animation



Edward Muybridge, *"Sallie Gardner"* (1878)

# First Hand-Drawn Feature-Length (>40 mins) Animation



Disney, "Snow White and the Seven Dwarfs" (1937)



# First Digital-Computer-Generated Animation



Ivan Sutherland, "Sketchpad" (1963) – Light pen, vector display

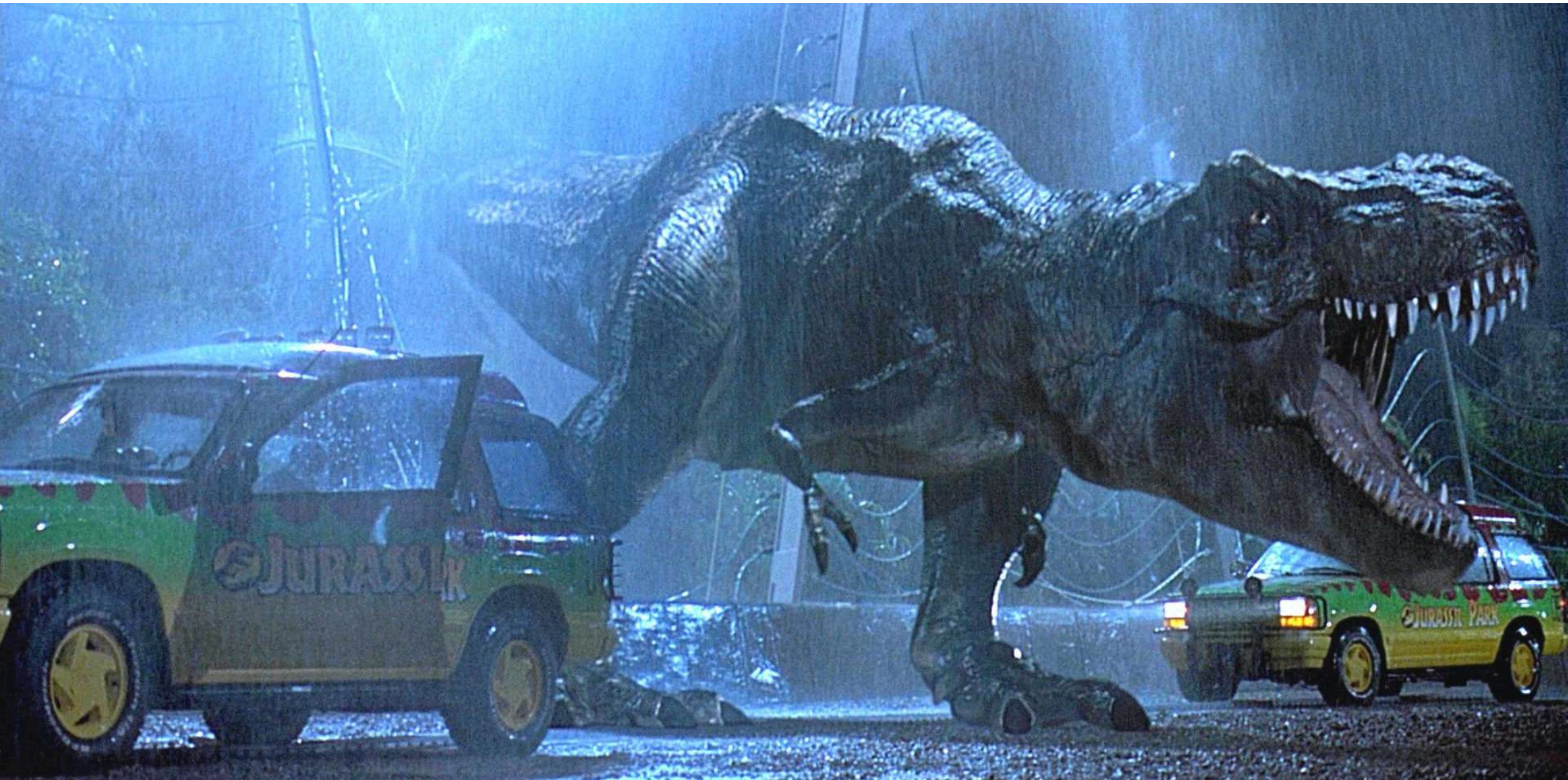
# Early Computer Animation



Ed Catmull & Frederick Parke, "Computer Animated Faces" (1972)



# Digital Dinosaurs!



Jurassic Park (1993)



# First CG Feature-Length Film



Pixar, "Toy Story" (1995)

# Computer Animation - 10 years ago



Sony Pictures Animation, "Cloudy With a Chance of Meatballs" (2009)



# Computer Animation - last year



Walt Disney Animation Studios, "Frozen 2" (2019)



# Keyframe Animation

# Keyframe Animation

Keyframes



"Tweens"

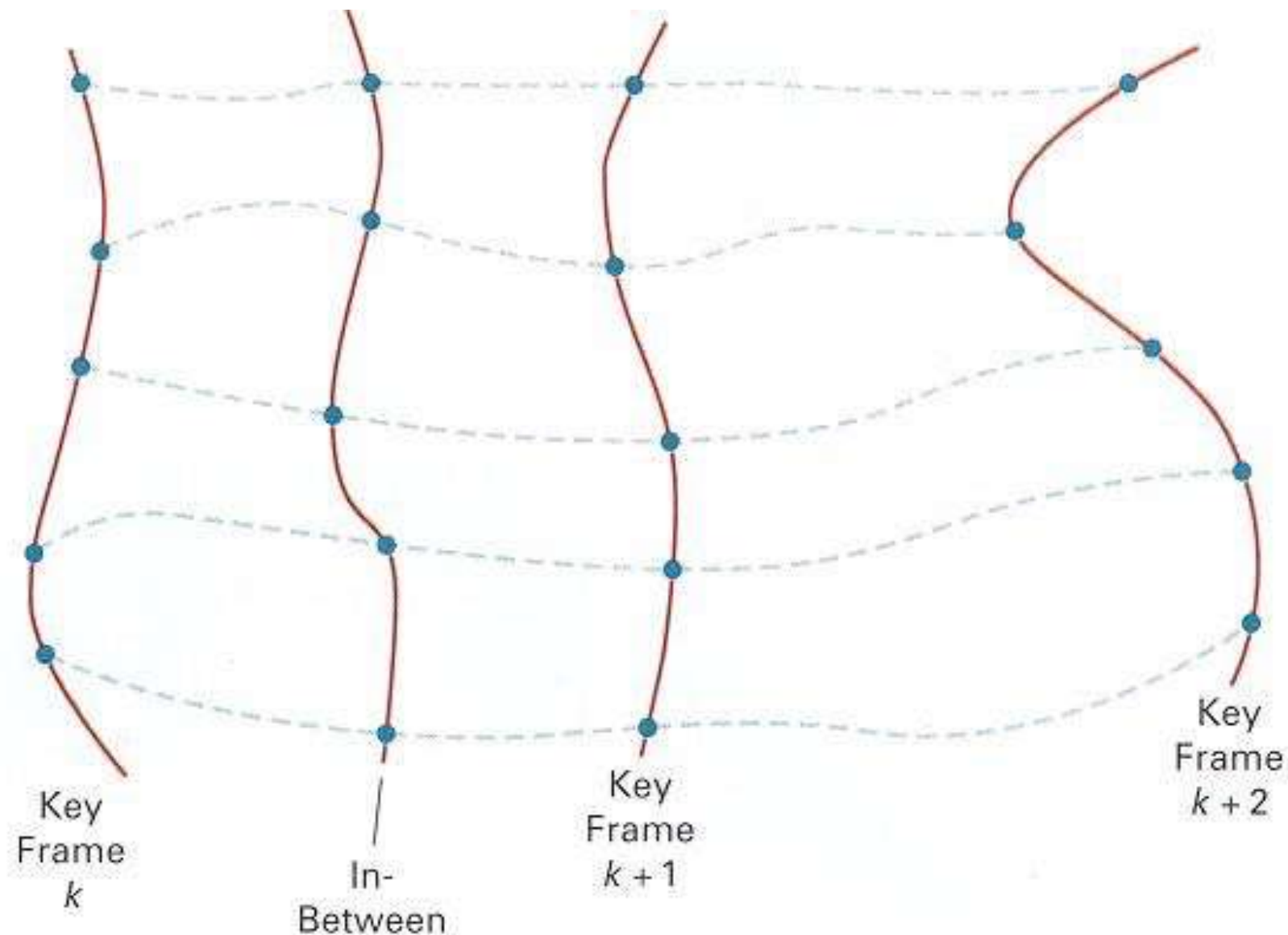


Animator (e.g. lead animator) creates keyframes

Assistant (person or computer) creates in-between frames  
("tweening")

# Keyframe Interpolation

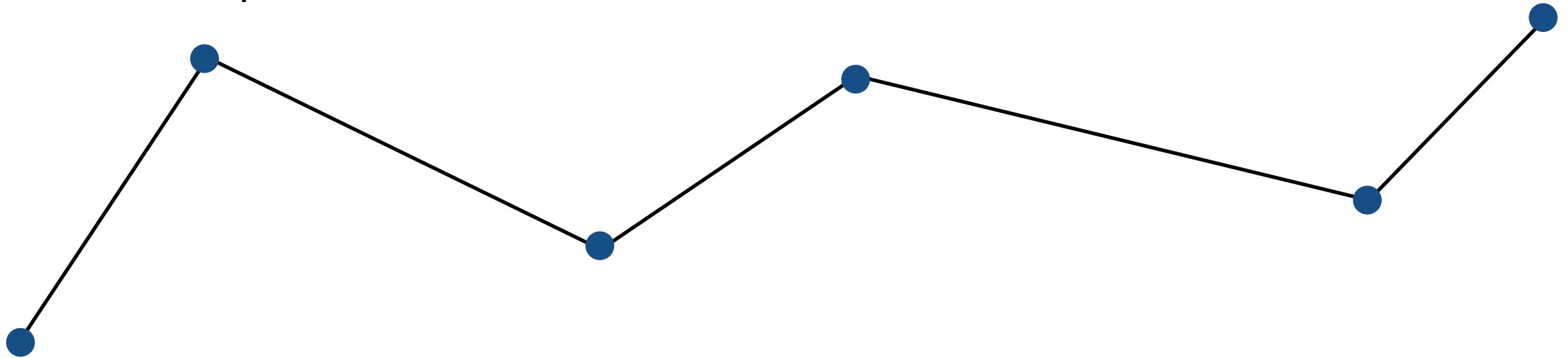
Think of each frame as a vector of parameter values



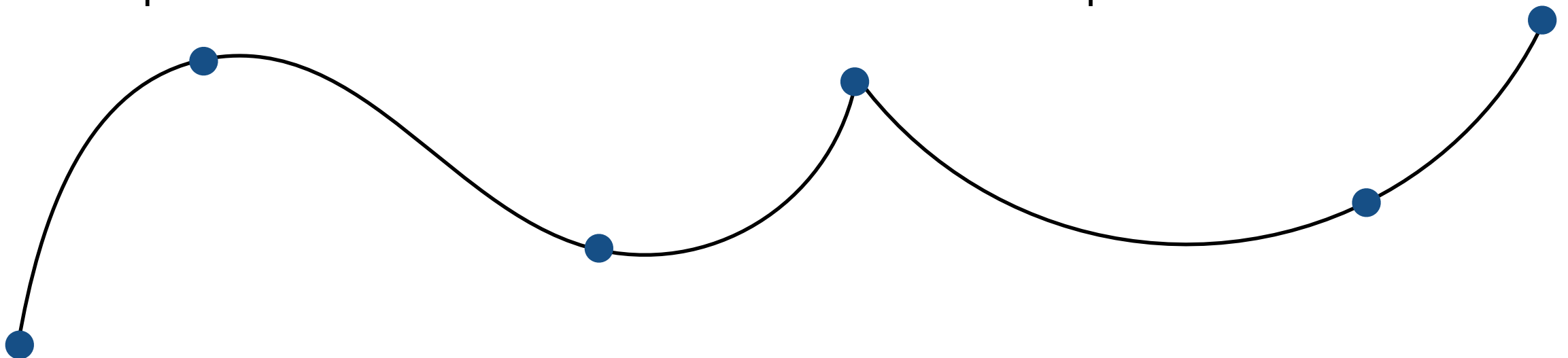
Hearn, Baker and Carithers, Figure 16.11

# Keyframe Interpolation of Each Parameter

Linear interpolation usually not good enough



Recall splines for smooth / controllable interpolation





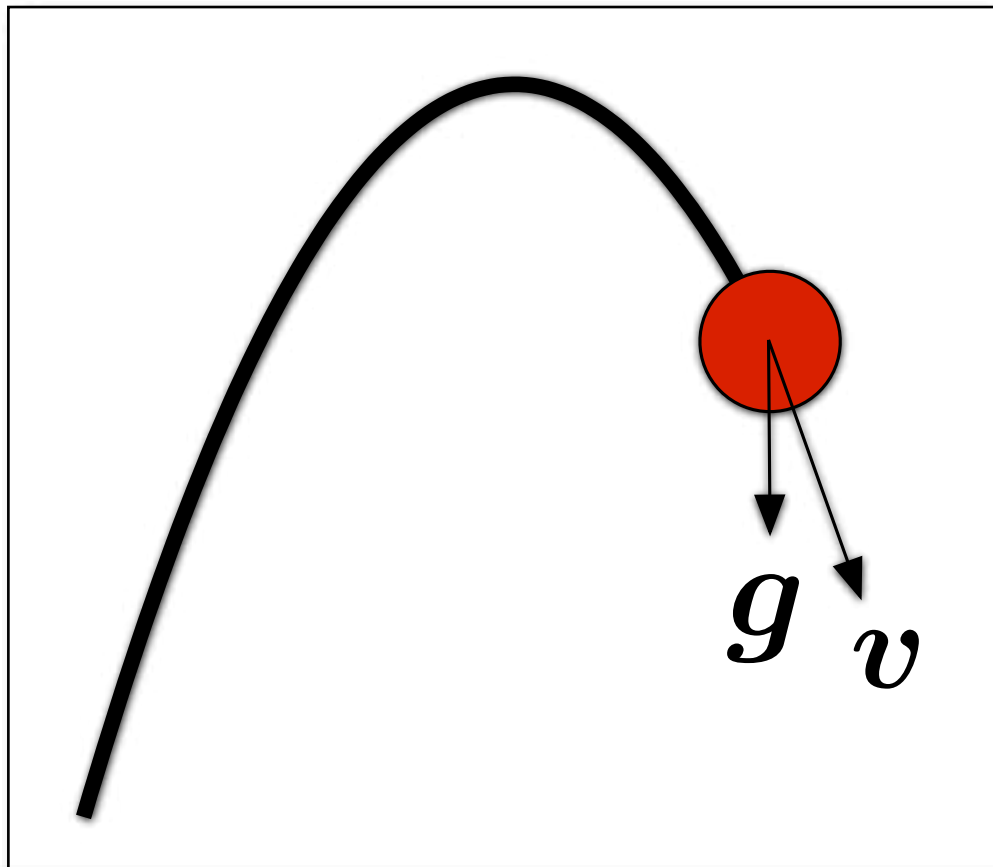
# Physical Simulation

# Newton's Law

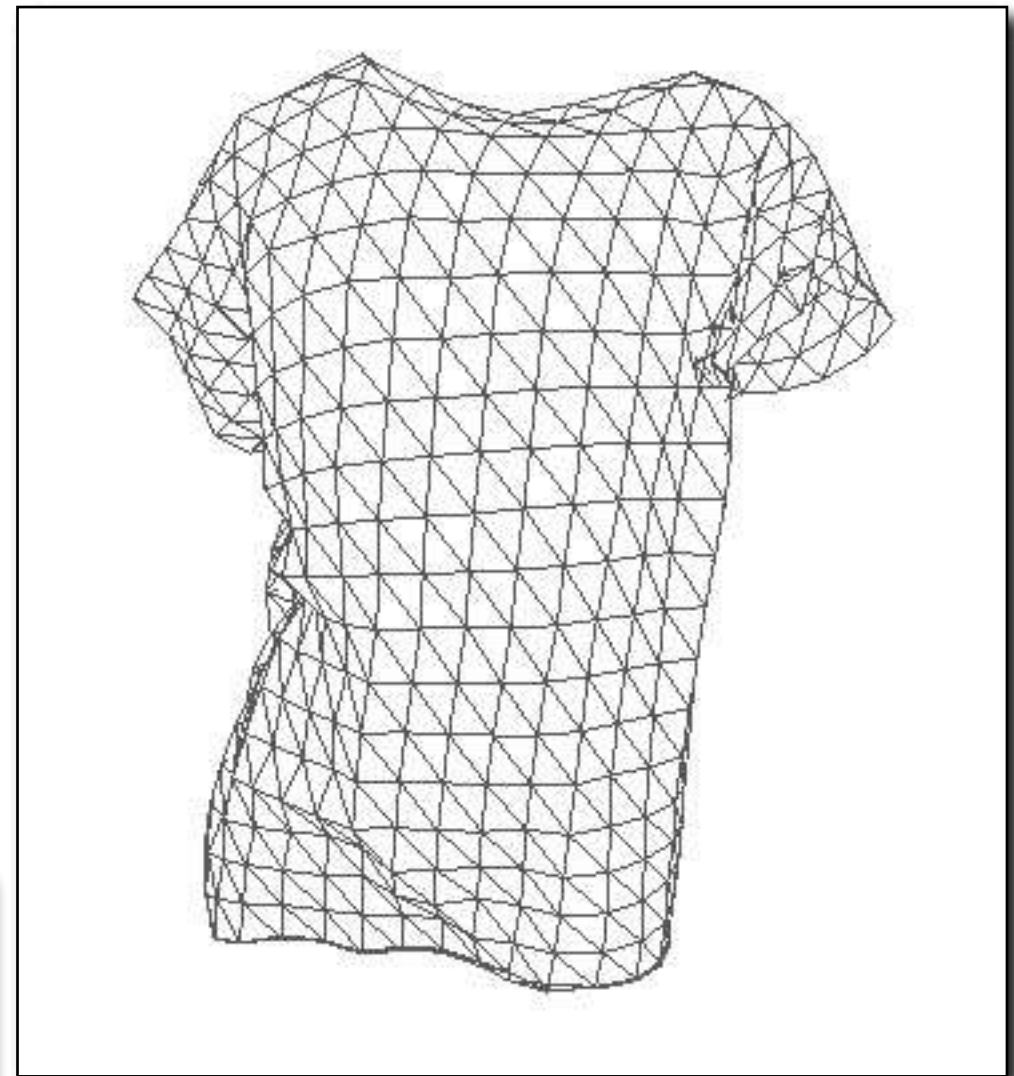
$$\underset{\substack{\uparrow \\ \text{Force}}}{F} = \underset{\substack{\uparrow \\ \text{Mass}}}{m} \underset{\substack{\uparrow \\ \text{Acceleration}}}{a}$$

# Physically Based Animation

Generate motion of objects using numerical simulation



$$\mathbf{x}^{t+\Delta t} = \mathbf{x}^t + \Delta t \mathbf{v}^t + \frac{1}{2} (\Delta t)^2 \mathbf{a}^t$$



# Example: Cloth Simulation





# Example: Fluids



Macklin and Müller, Position Based Fluids

# Mass Spring System:

## Example of Modeling a Dynamic System

# Example: Mass Spring Rope



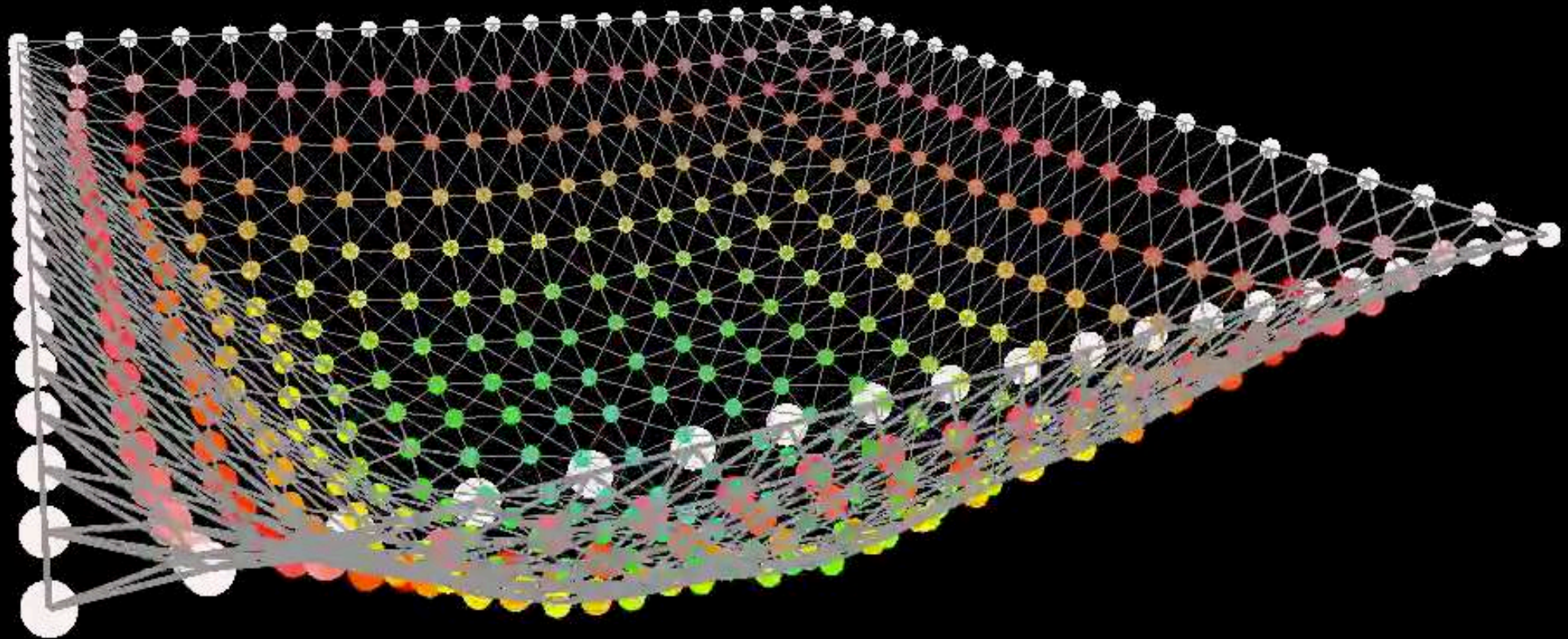
<https://youtu.be/Co8enp8CH34>

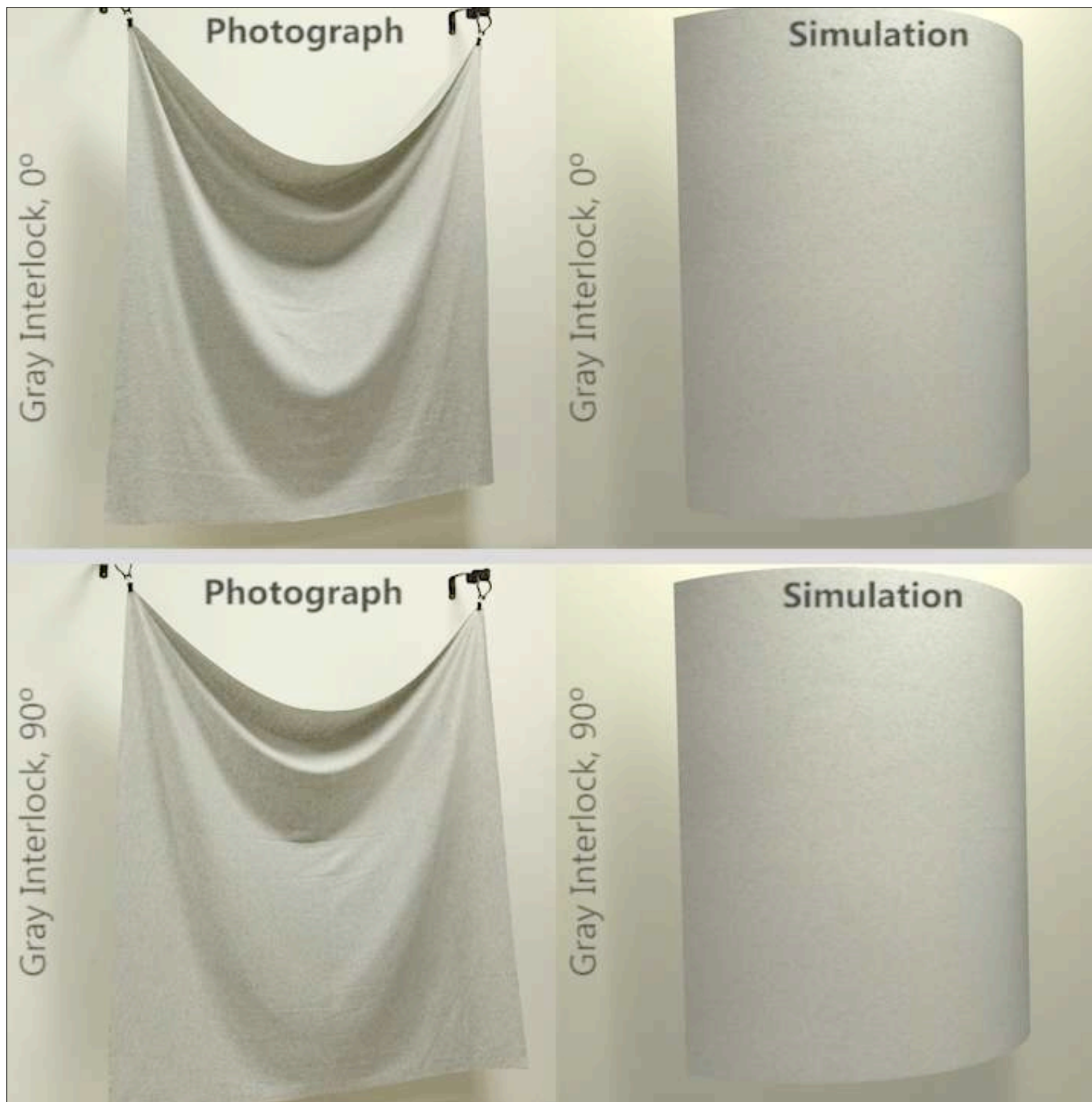
# Example: Hair





# Example: Mass Spring Mesh

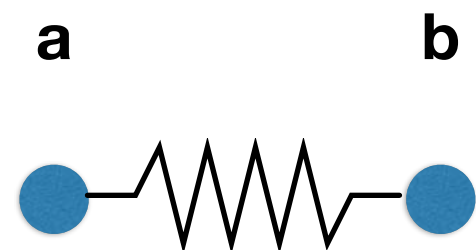




Huamin Wang, Ravi Ramamoorthi, and James F. O'Brien. "Data-Driven Elastic Models for Cloth: Modeling and Measurement". *ACM Transactions on Graphics*, 30(4):71:1–11, July 2011. Proceedings of ACM SIGGRAPH 2011, Vancouver, BC Canada.

# A Simple Spring

Idealized spring



The diagram shows two blue circular points, labeled 'a' and 'b' above them, connected by a zigzag line representing a spring. The spring is oriented horizontally.

$$\mathbf{f}_{a \rightarrow b} = k_s(\mathbf{b} - \mathbf{a})$$
$$\mathbf{f}_{b \rightarrow a} = -\mathbf{f}_{a \rightarrow b}$$

Force pulls points together

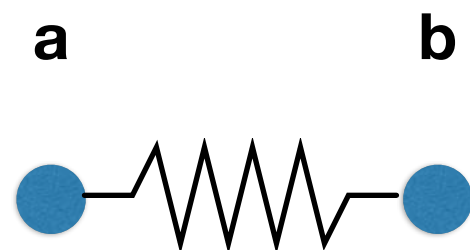
Strength proportional to displacement (Hooke's Law)

$k_s$  is a spring coefficient: stiffness

Problem: this spring wants to have zero length


# Non-Zero Length Spring

Spring with non-zero rest length



$$\mathbf{f}_{a \rightarrow b} = k_s \frac{\mathbf{b} - \mathbf{a}}{\|\mathbf{b} - \mathbf{a}\|} (\|\mathbf{b} - \mathbf{a}\| - l)$$

Rest length



Problem: oscillates forever



# Dot Notation for Derivatives

If  $\boldsymbol{x}$  is a vector for the position of a point of interest, we will use dot notation for velocity and acceleration:

$$\boldsymbol{x}$$

$$\dot{\boldsymbol{x}} = \boldsymbol{v}$$

$$\ddot{\boldsymbol{x}} = \boldsymbol{a}$$

# Introducing Energy Loss

Simple motion damping


$$\mathbf{f} = -k_d \dot{\mathbf{b}}$$


- Behaves like viscous drag on motion
- Slows down motion in the direction of velocity
- $k_d$  is a damping coefficient

Problem: slows down *all* motion

- Want a rusty spring's oscillations to slow down, but should it also fall to the ground more slowly?

# Internal Damping for Spring

Damp only the internal, spring-driven motion



Relative velocity of b, assuming a is static (vector)

$$f_b = -k_d \frac{b - a}{||b - a||} (\dot{b} - \dot{a}) \cdot \frac{b - a}{||b - a||}$$

Damping force applied on b

Relative velocity projected to the direction from a to b (scalar)

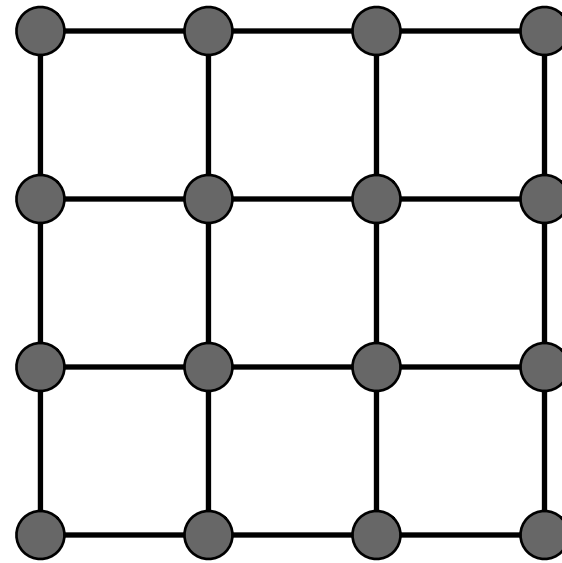
Direction from a to b

- Viscous drag only on change in spring length
  - Won't slow group motion for the spring system (e.g. global translation or rotation of the group)
- Note: This is only one specific type of damping

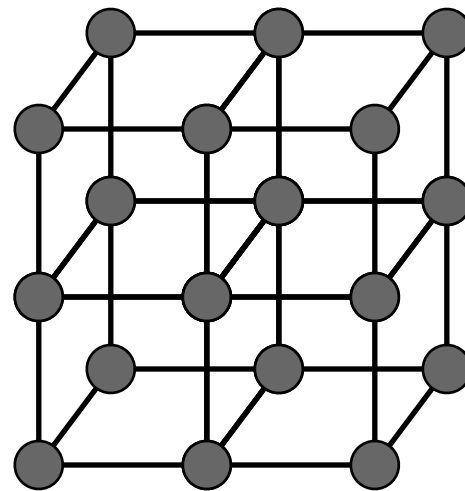


# Structures from Springs

Sheets



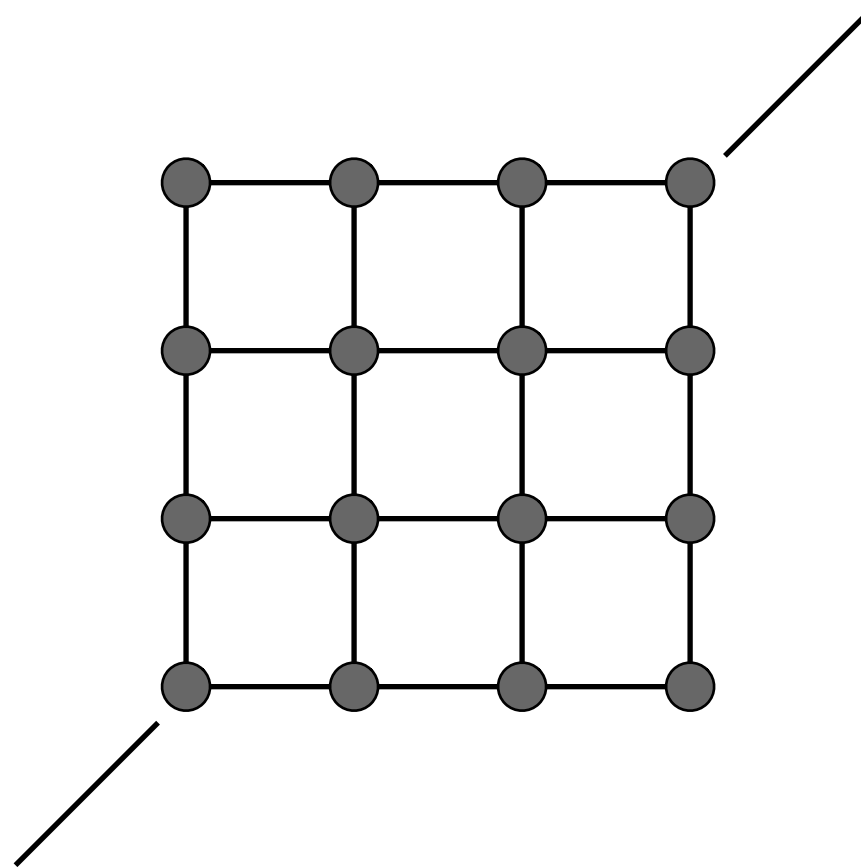
Blocks



Others

# Structures from Springs

Behavior is determined by structure linkages

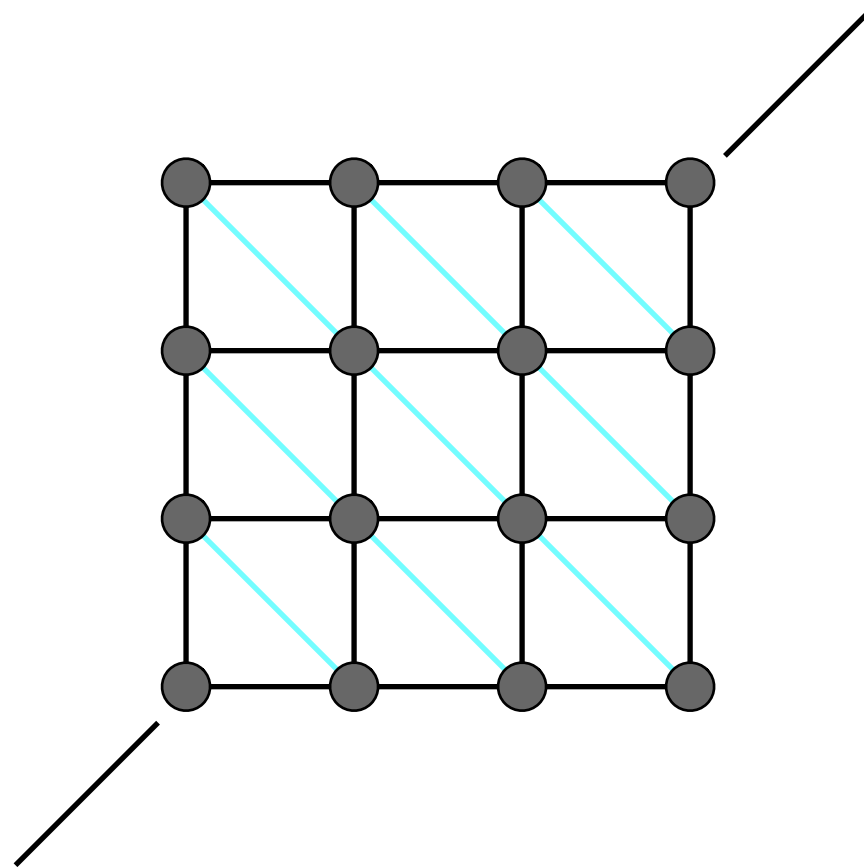


This structure will not resist shearing

This structure will not resist out-of-plane bending...

# Structures from Springs

Behavior is determined by structure linkages



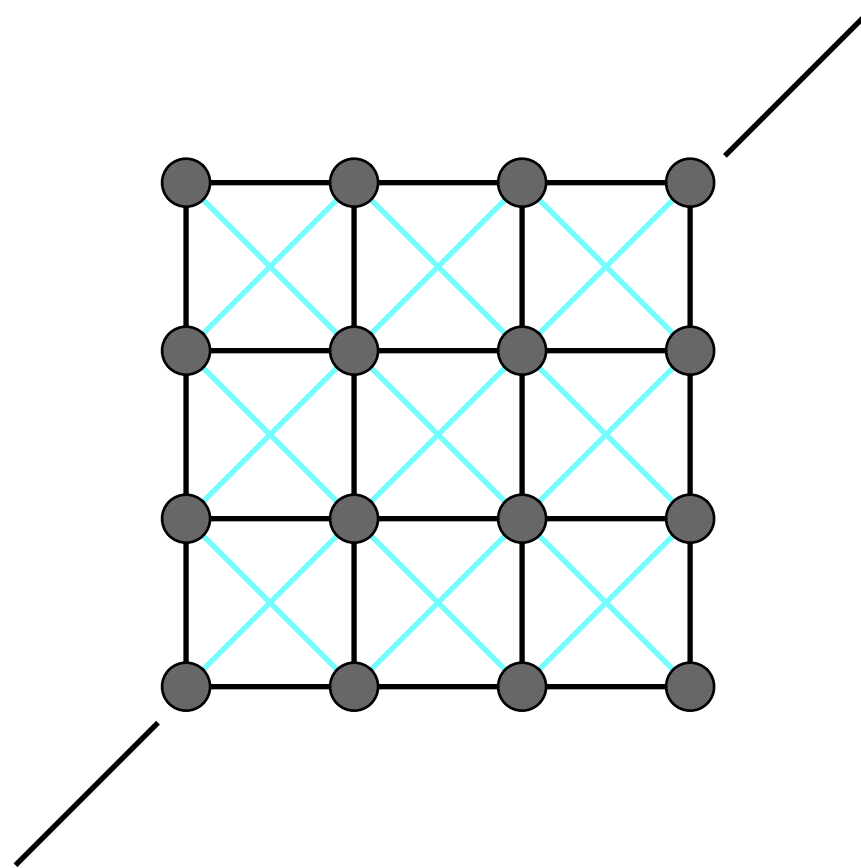
This structure will resist shearing  
but has anisotropic bias

This structure will not resist out-of-plane  
bending either...



# Structures from Springs

Behavior is determined by structure linkages

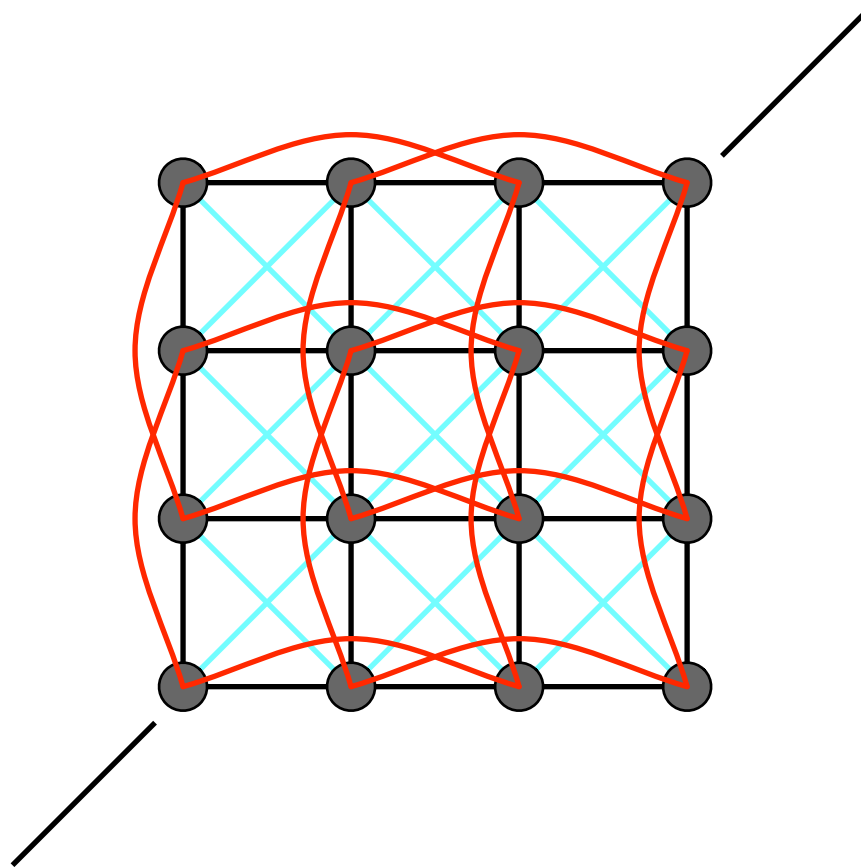


This structure will resist shearing.  
Less directional bias.

This structure will not resist out-of-plane  
bending either...

# Structures from Springs

They behave like what they are (obviously!)



This structure will resist shearing.  
Less directional bias.

This structure will resist out-of-plane bending  
Red springs should be much weaker

# Example: Mass Spring Dress + Character



# Aside: FEM (Finite Element Method) Instead of Springs





# Particle Systems

# Particle Systems

Model dynamical systems as collections of large numbers of particles

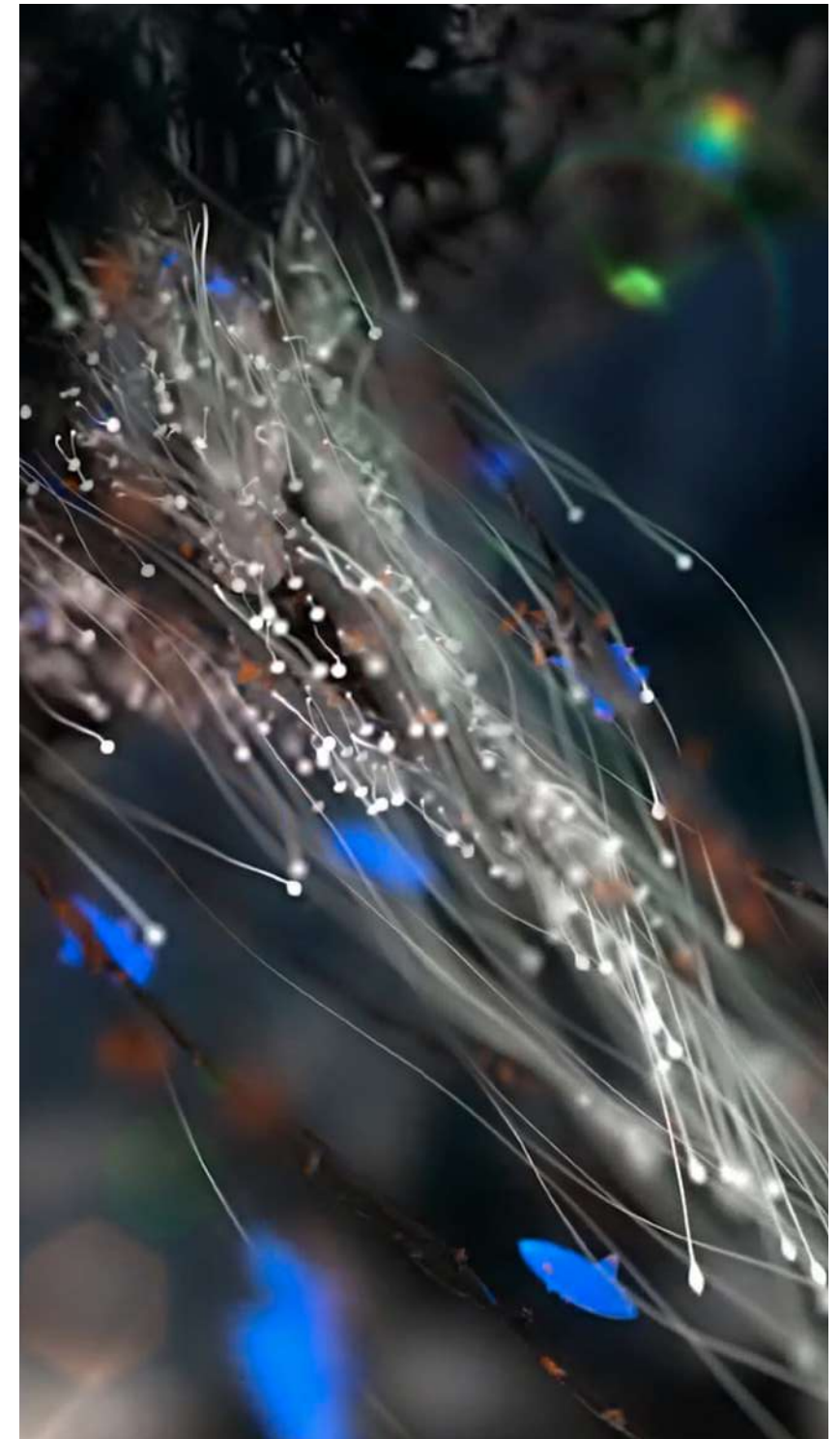
Each particle's motion is defined by a set of physical (or non-physical) forces

Popular technique in graphics and games

- Easy to understand, implement
- Scalable: fewer particles for speed, more for higher complexity

Challenges

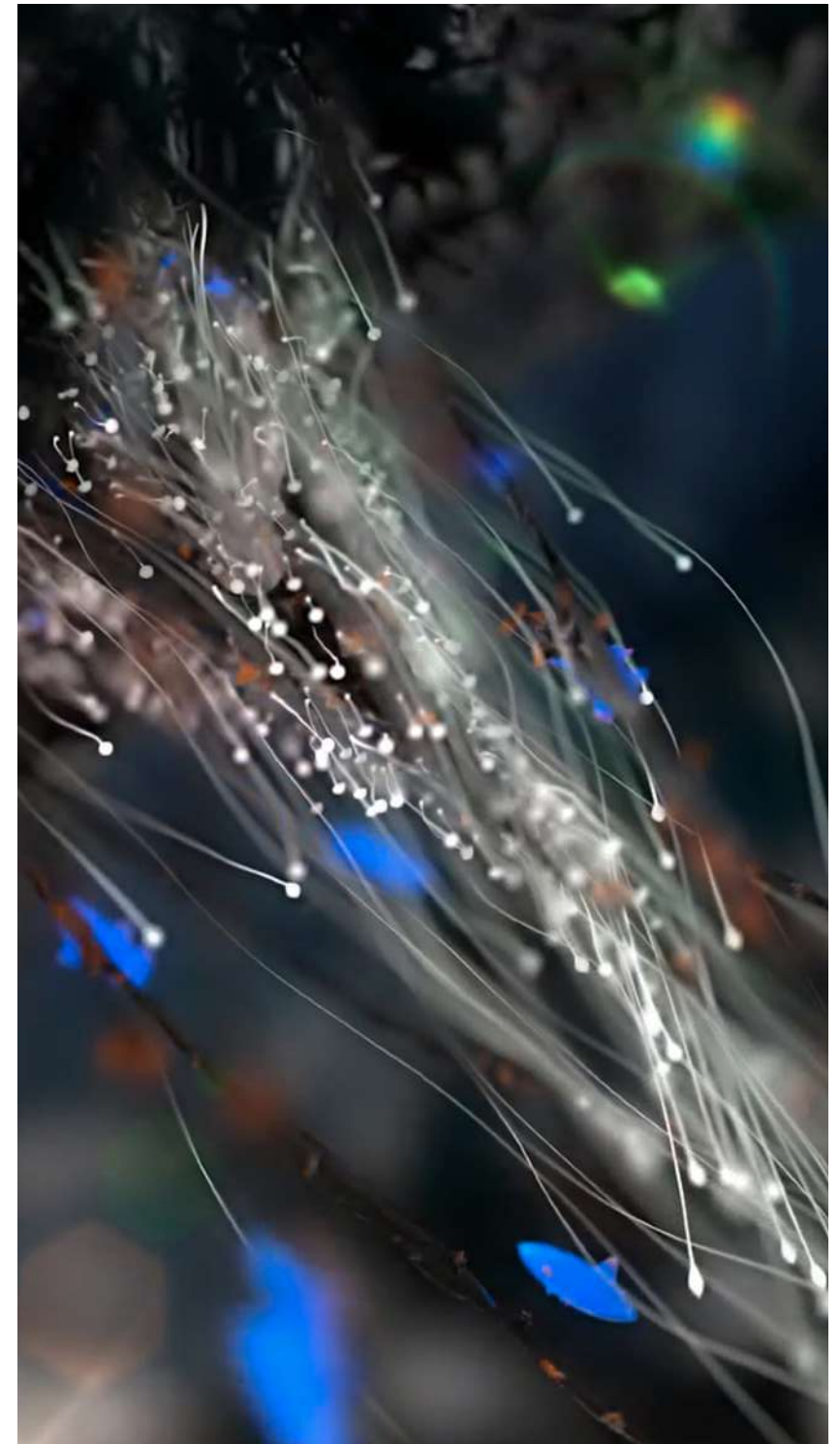
- May need *many* particles (e.g. fluids)
- May need acceleration structures (e.g. to find nearest particles for interactions)



# Particle System Animations

For each frame in animation

- [If needed] Create new particles
- Calculate forces on each particle
- Update each particle's position and velocity
- [If needed] Remove dead particles
- Render particles



# Particle System Forces

## Attraction and repulsion forces

- Gravity, electromagnetism, ...
- Springs, propulsion, ...

## Damping forces

- Friction, air drag, viscosity, ...

## Collisions

- Walls, containers, fixed objects, ...
- Dynamic objects, character body parts, ...



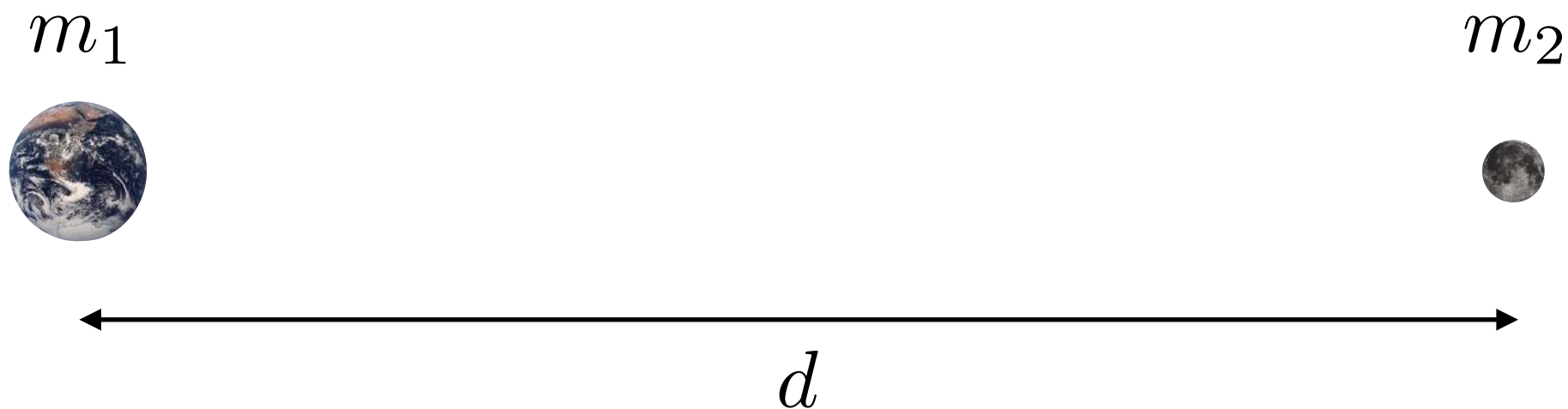
# Gravitational Attraction

Newton's universal law of gravitation

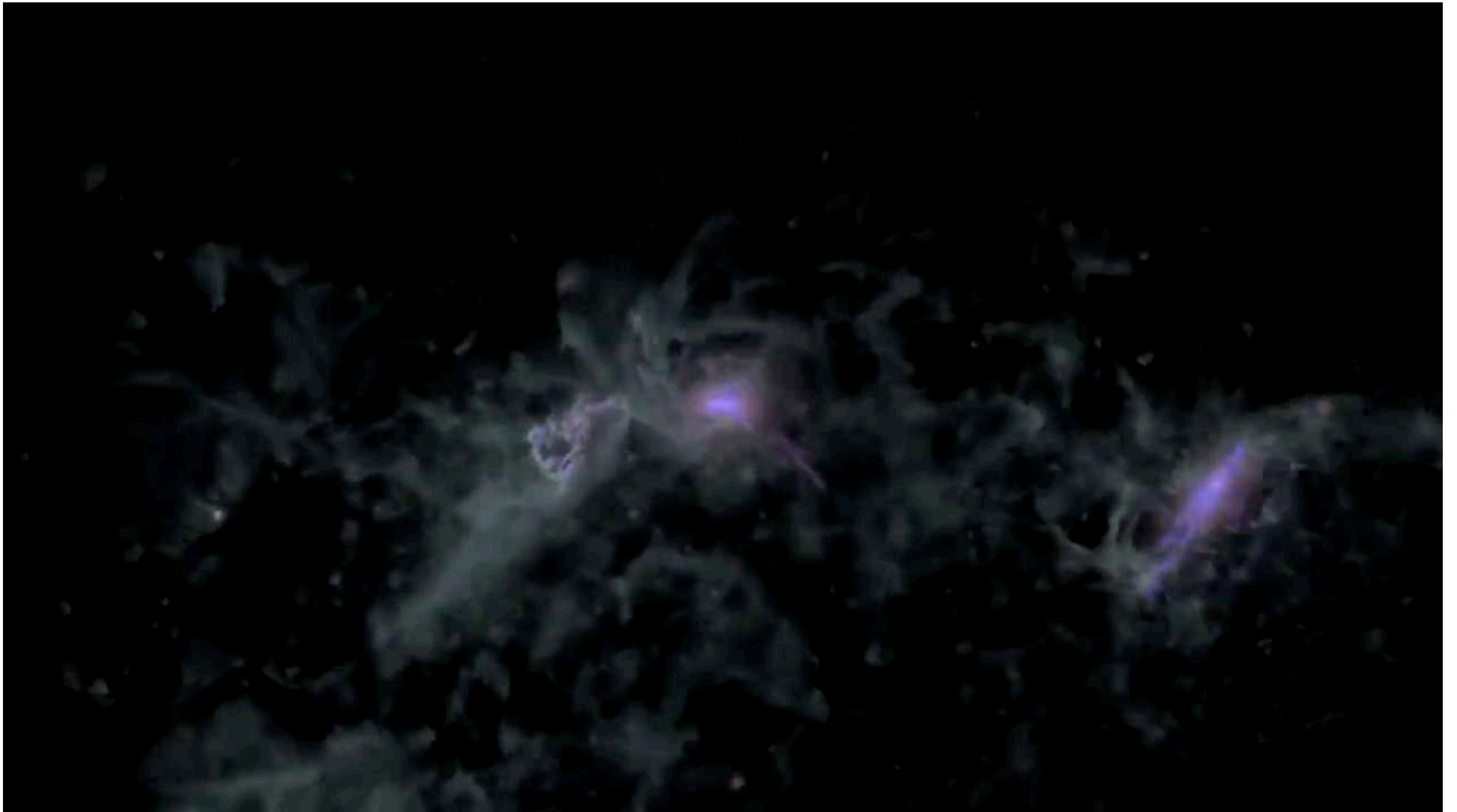
- Gravitational pull between particles

$$F_g = G \frac{m_1 m_2}{d^2}$$

$$G = 6.67428 \times 10^{-11} \text{ Nm}^2\text{kg}^{-2}$$

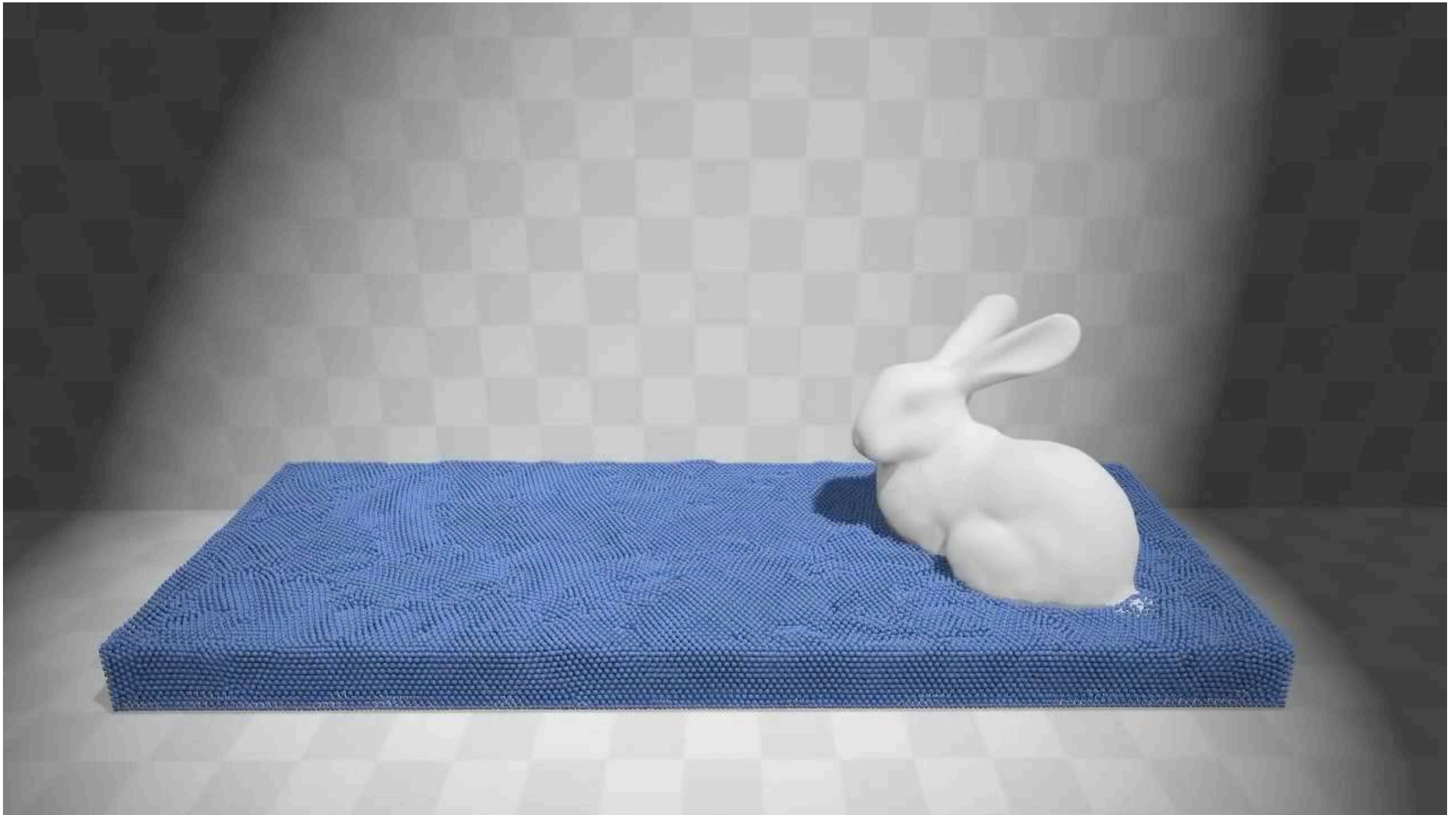


# Example: Galaxy Simulation



Disk galaxy simulation, NASA Goddard

# Example: Particle-Based Fluids



Macklin and Müller, Position Based Fluids

# Simulated Flocking as an ODE

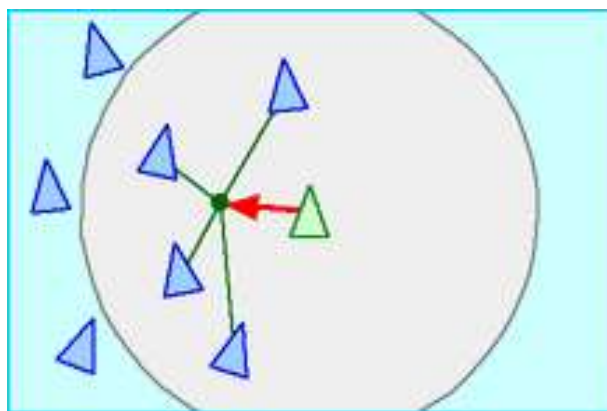
Model each bird as a particle

Subject to very simple forces:

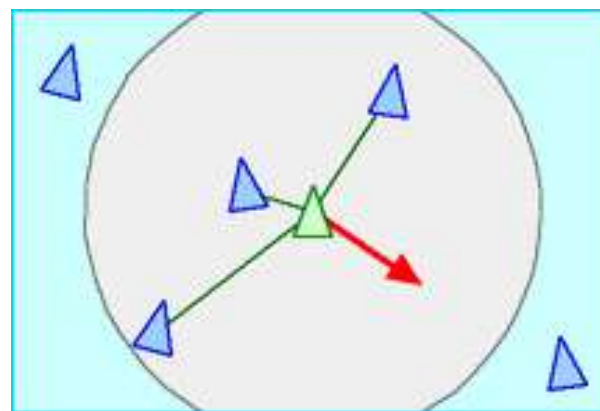
- attraction to center of neighbors
- repulsion from individual neighbors
- alignment toward average trajectory of neighbors

Simulate evolution of large particle system numerically

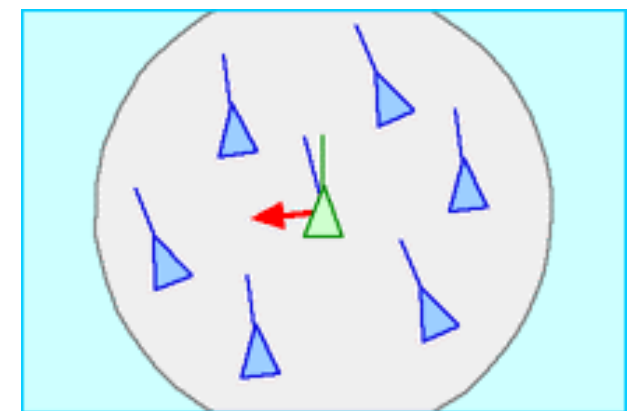
Emergent complex behavior (also seen in fish, bees, ...)



**attraction**



**repulsion**



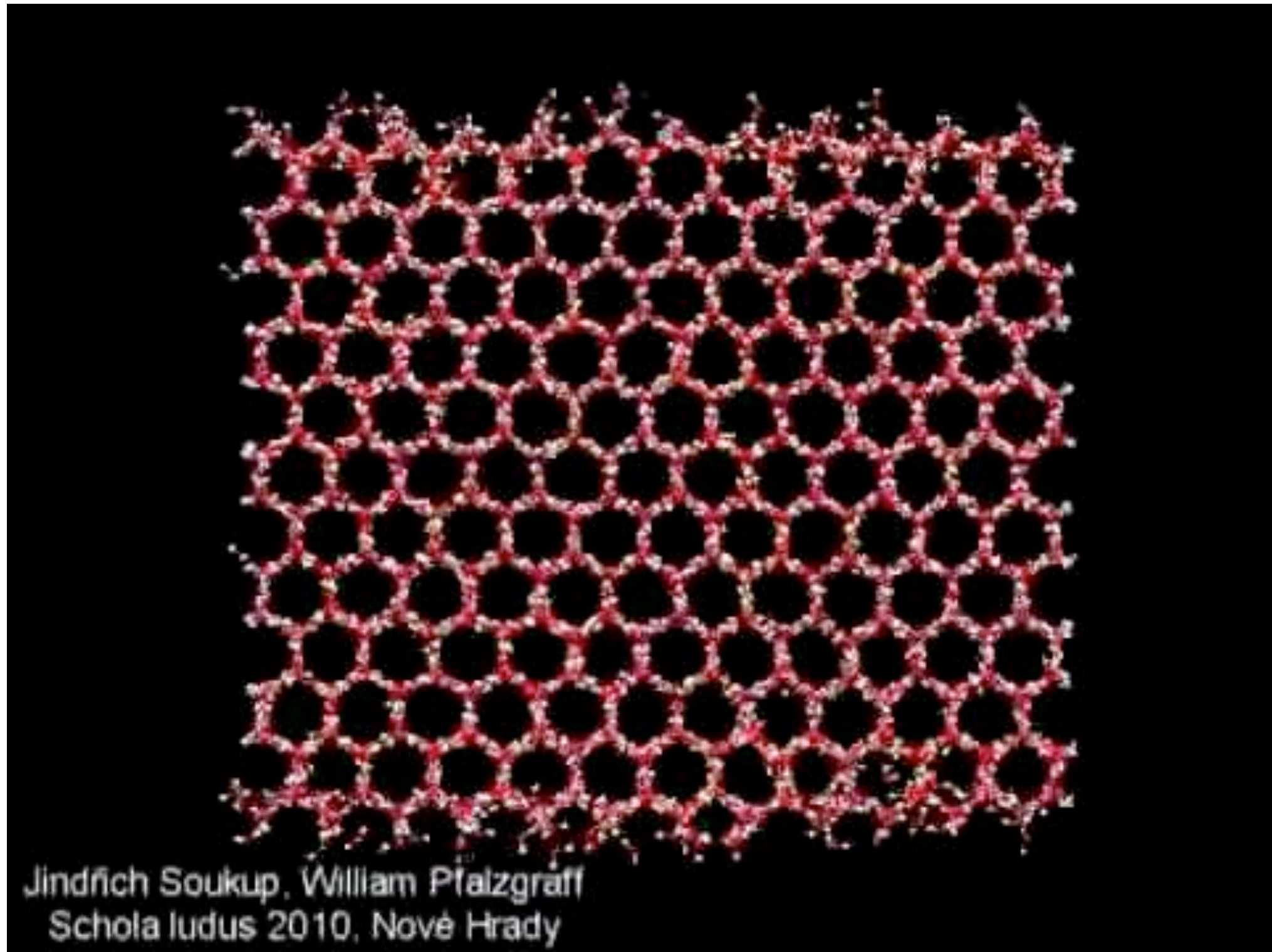
**alignment**

Credit: Craig Reynolds (see <http://www.red3d.com/cwr/boids/>)

Slide credit: Keenan Crane



# Example: Molecular Dynamics



(model of melting ice crystal)



# Example: Crowds + “Rock” Dynamics



# Forward Kinematics

(Slides by Prof. James O'Brien)

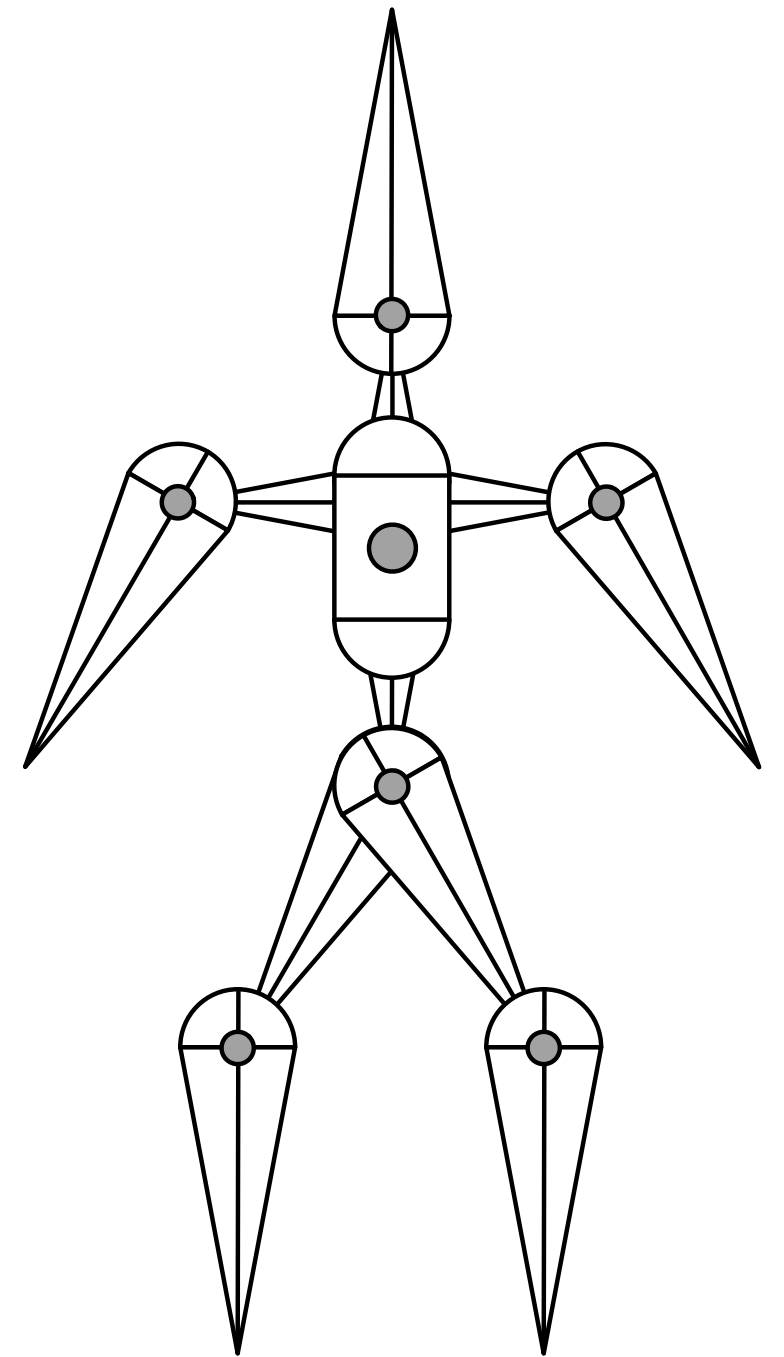
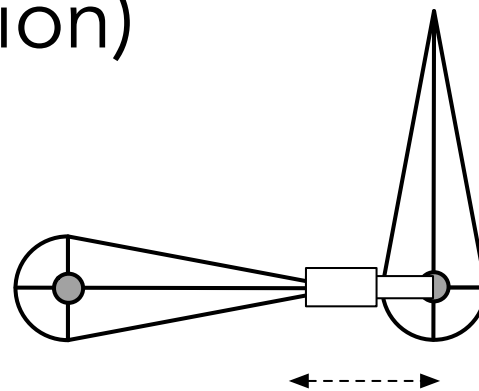
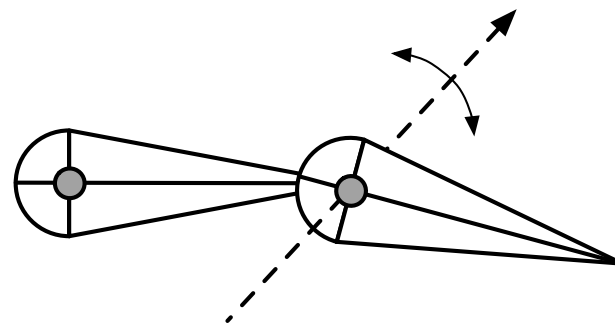
# Forward Kinematics

## Articulated skeleton

- Topology (what's connected to what)
- Geometric relations from joints
- Tree structure (in absence of loops)

## Joint types

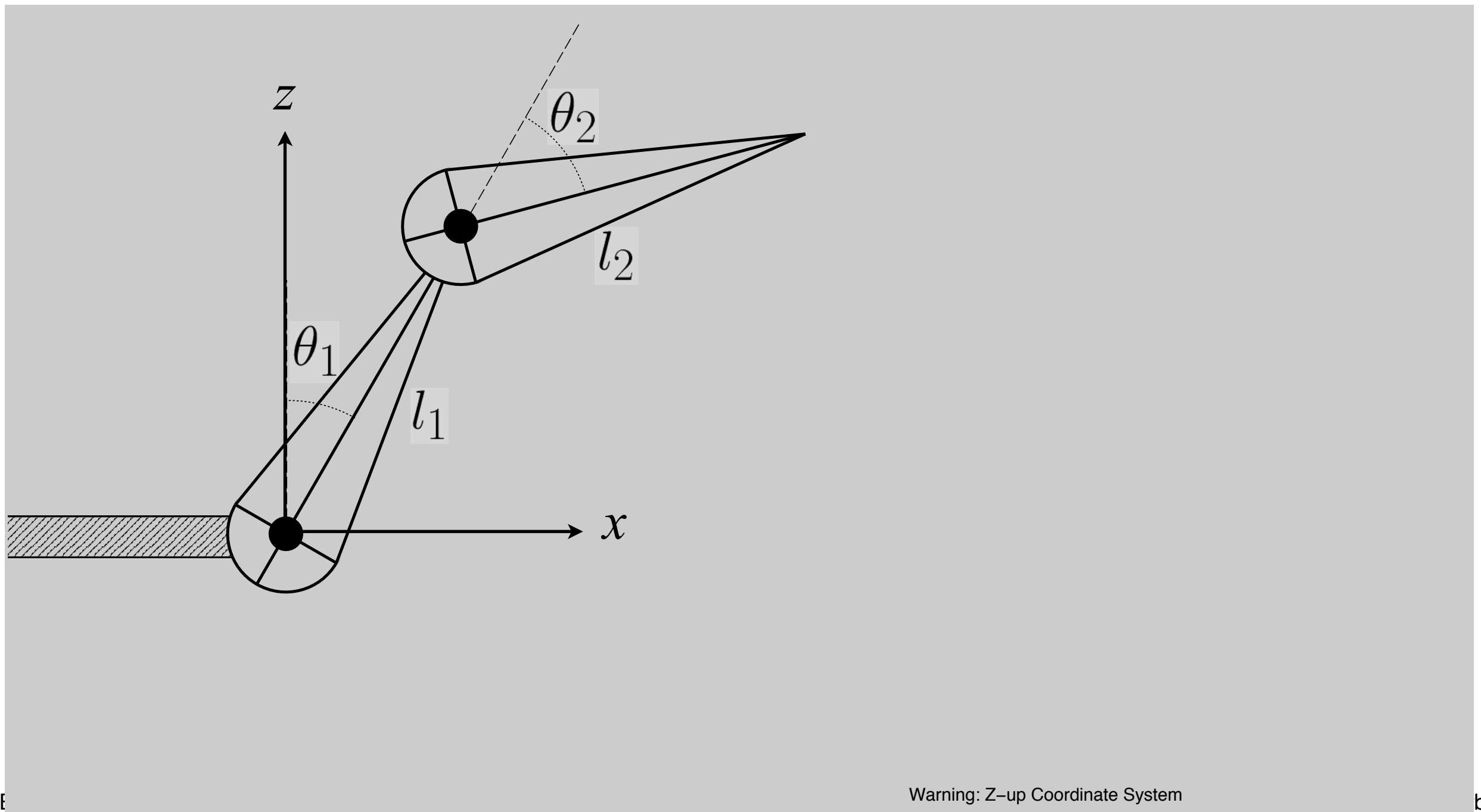
- Pin (1D rotation)
- Ball (2D rotation)
- Prismatic joint (translation)





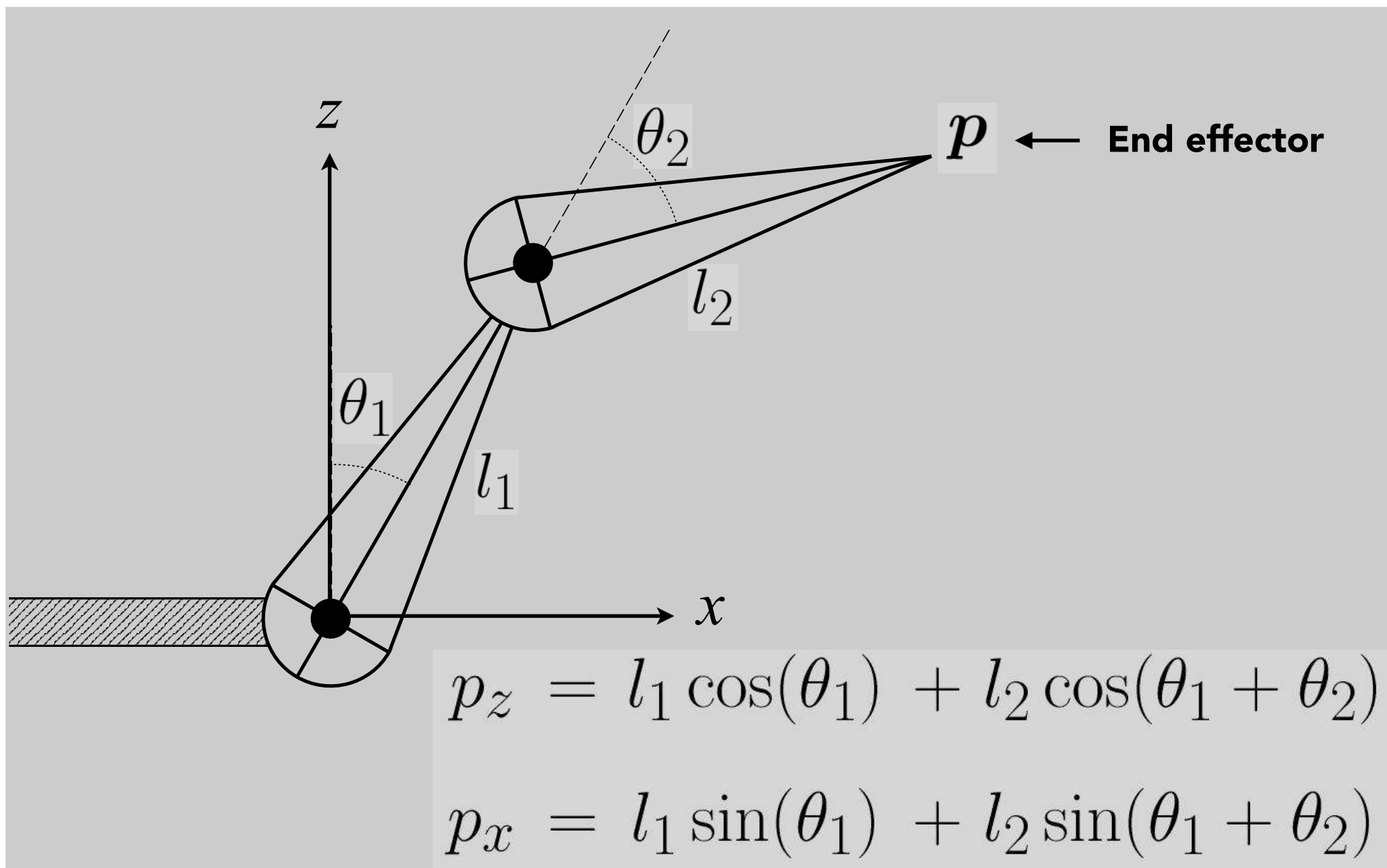
# Forward Kinematics

Example: simple two segment arm in 2D



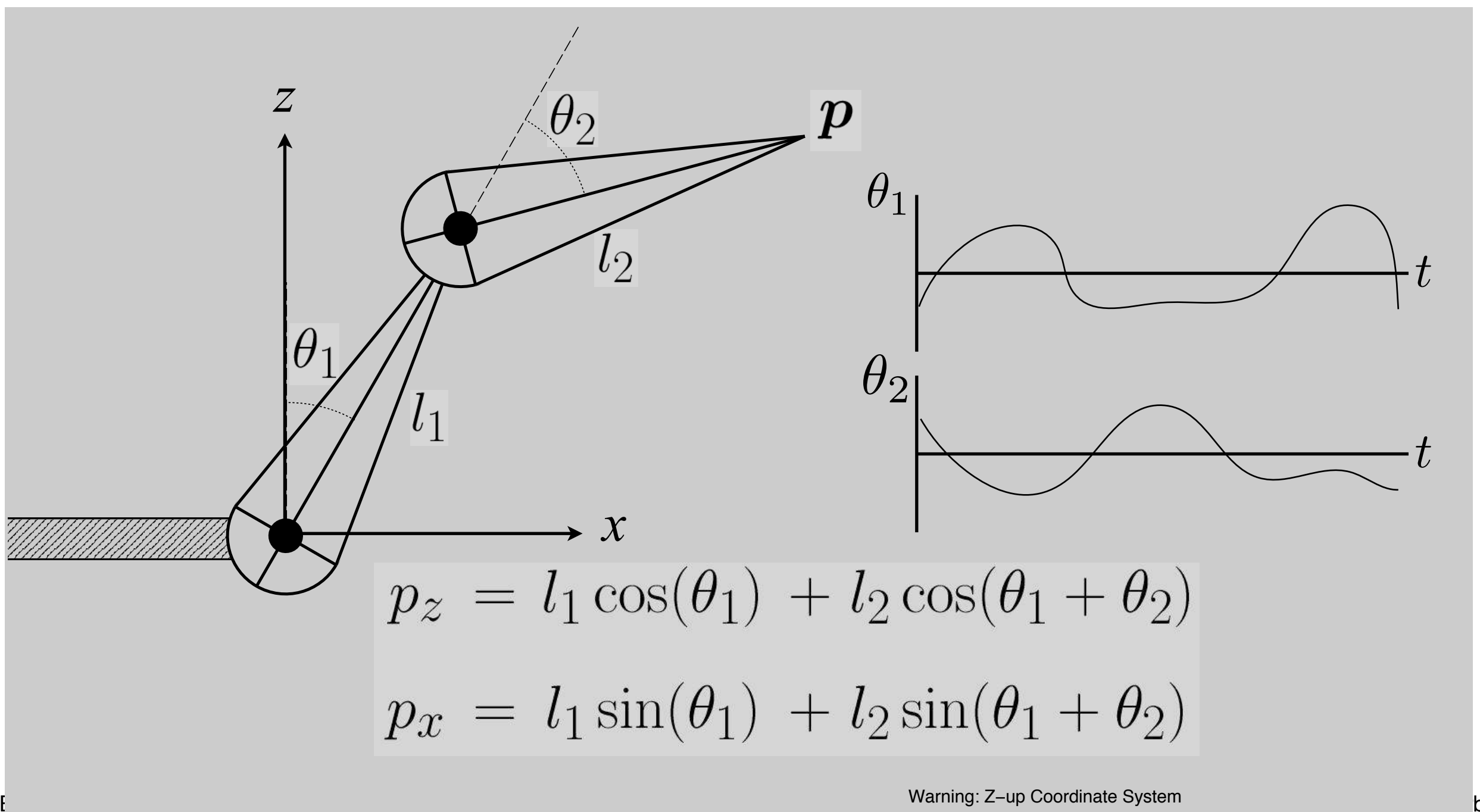
# Forward Kinematics

Animator provides angles, and computer determines position  $p$  of end-effector

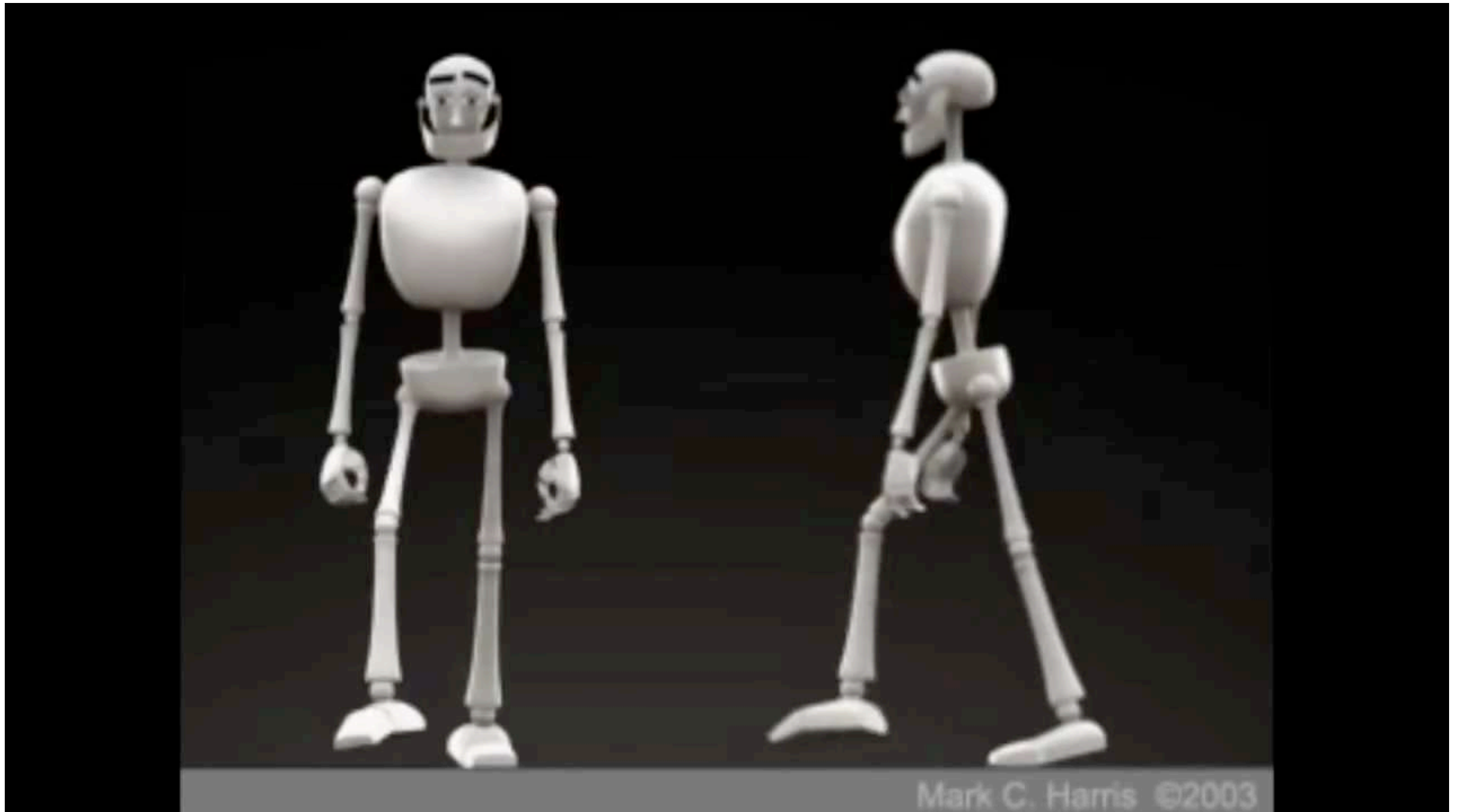


# Forward Kinematics

Animation is described as angle parameter values as a function of time



# Example Walk Cycle



# Kinematics Pros and Cons

## Strengths

- Direct control is convenient
- Implementation is straightforward

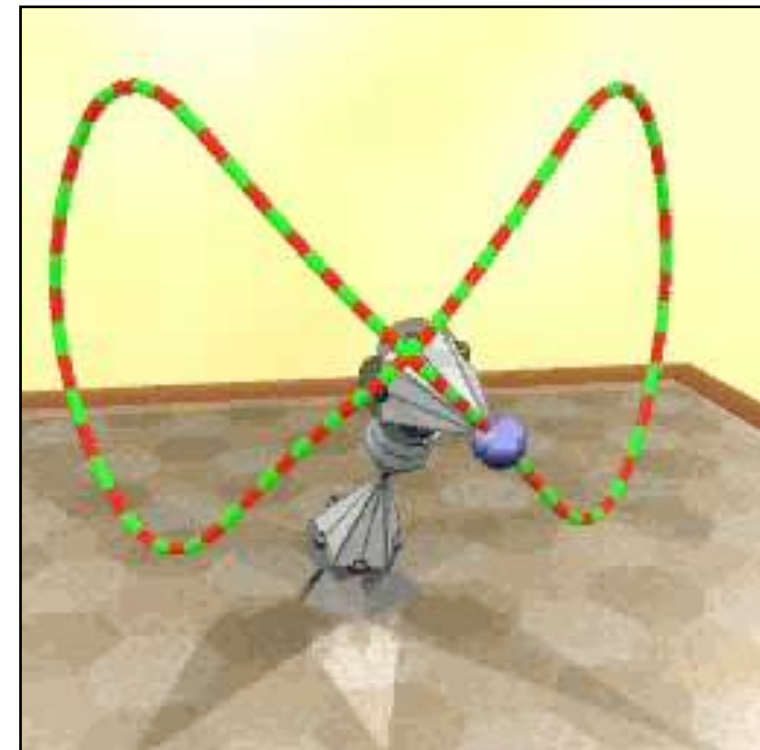
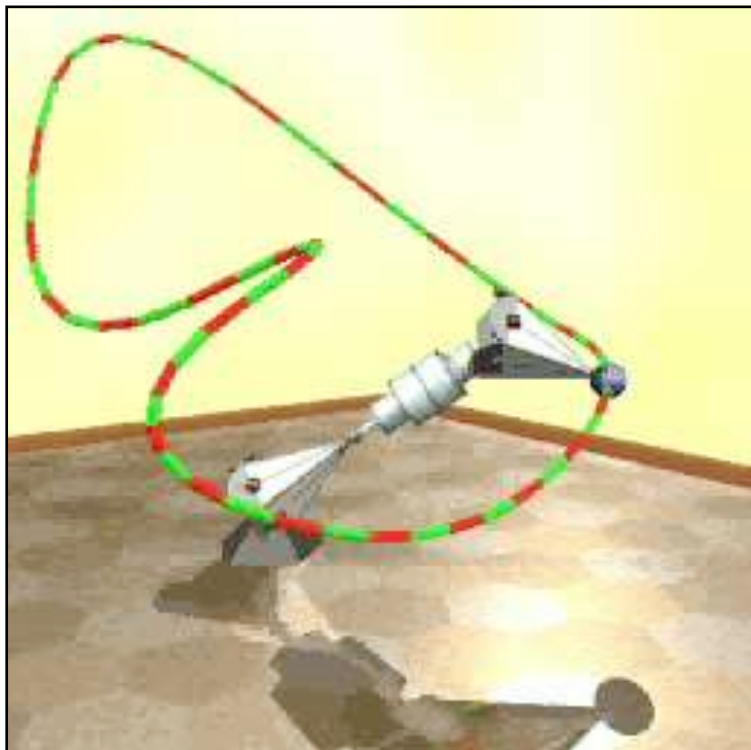
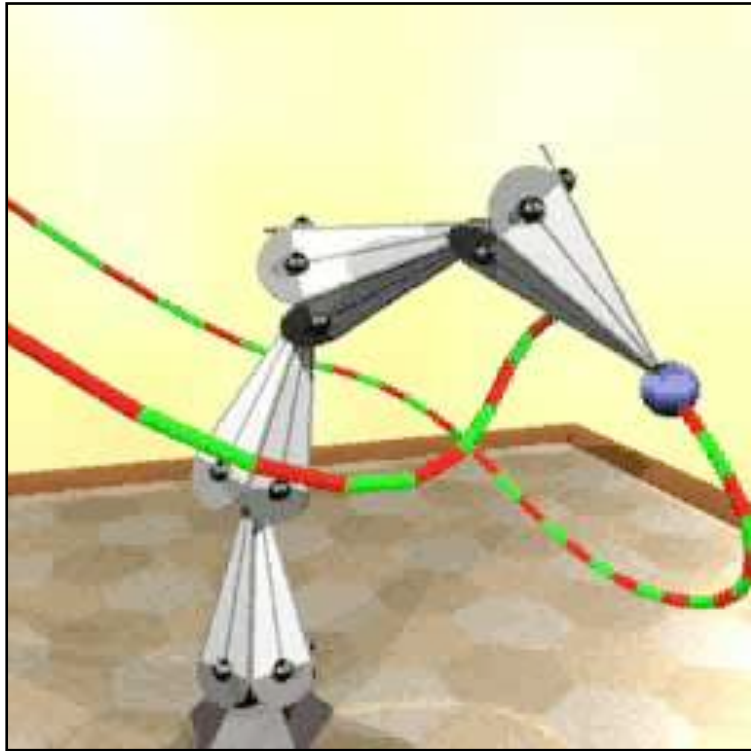
## Weaknesses

- Animation may be inconsistent with physics
- Time consuming for artists



# Inverse Kinematics

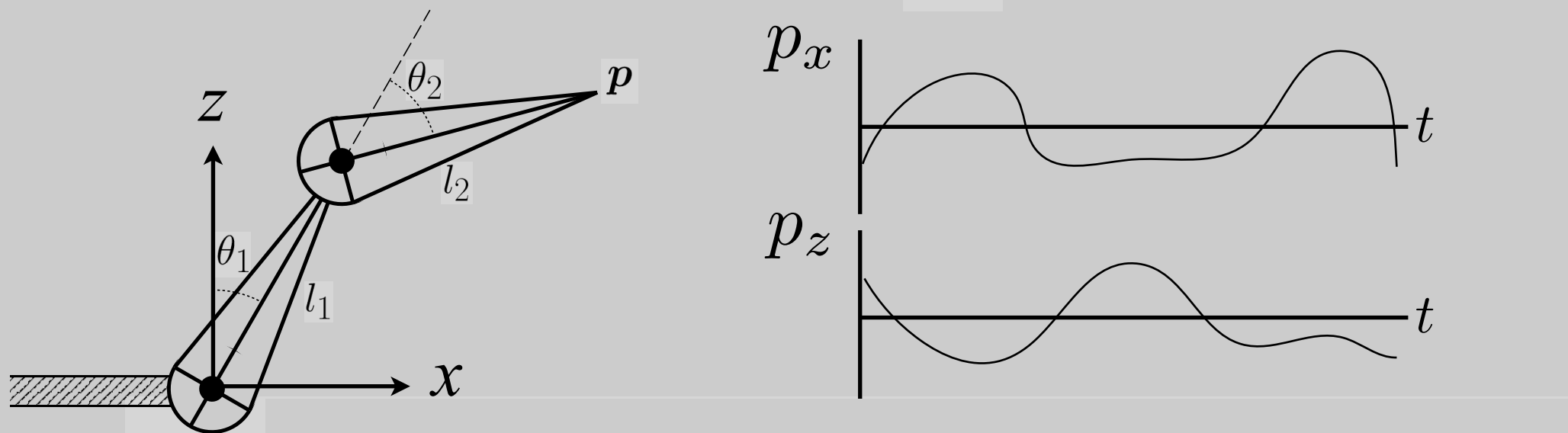
# Inverse Kinematics



Egon Pasztor

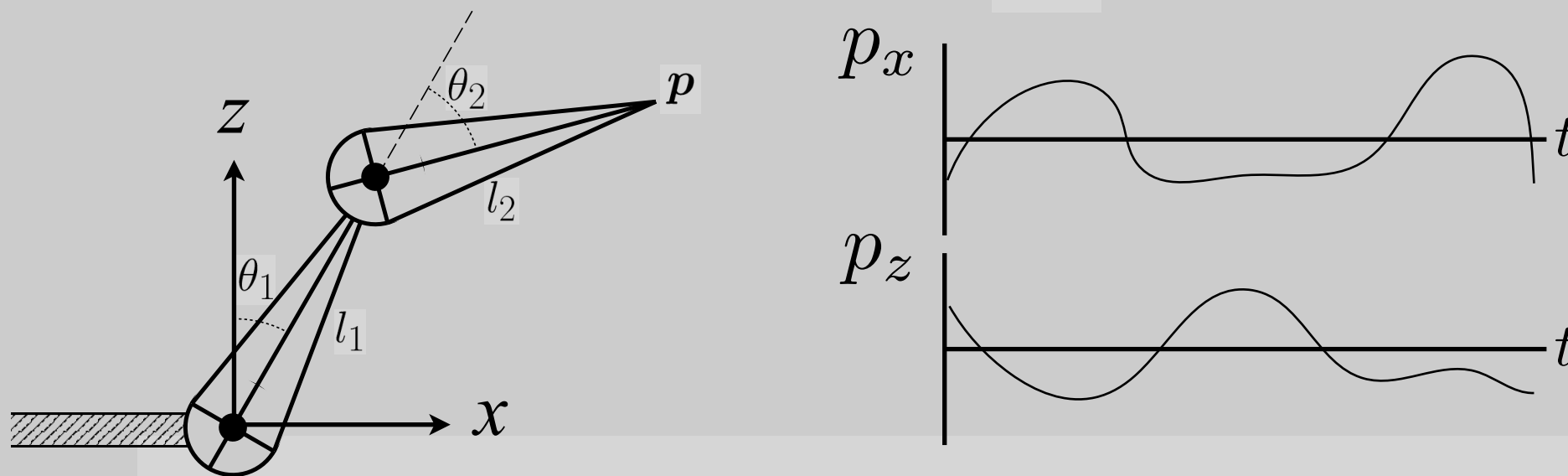
# Inverse Kinematics

Animator provides position of end-effector, and computer must determine joint angles that satisfy constraints



# Inverse Kinematics

Direct inverse kinematics: for two-segment arm, can solve for parameters analytically



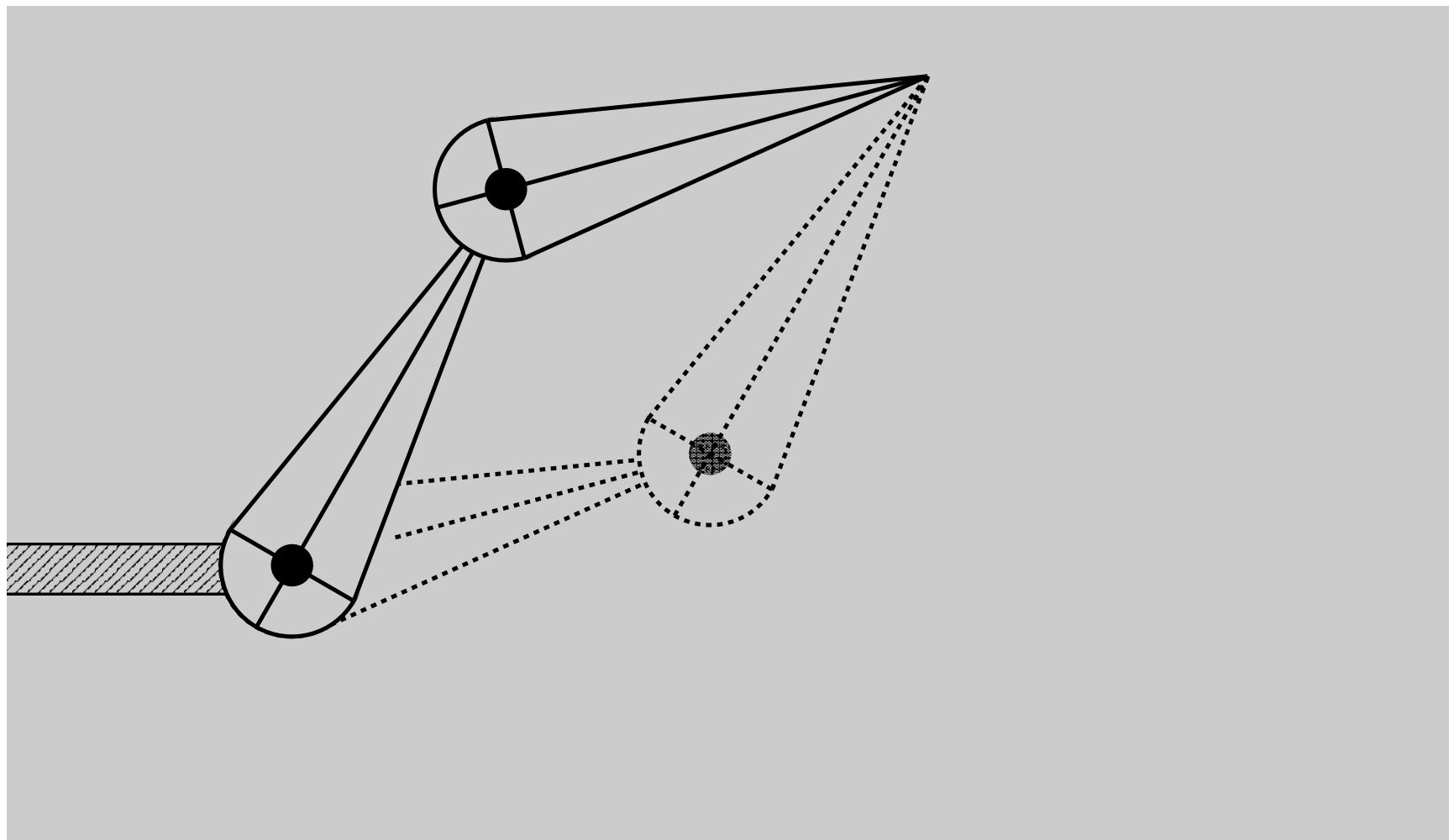
$$\theta_2 = \cos^{-1} \left( \frac{p_z^2 + p_x^2 - l_1^2 - l_2^2}{2l_1l_2} \right)$$

$$\theta_1 = \frac{-p_z l_2 \sin(\theta_2) + p_x (l_1 + l_2 \cos(\theta_2))}{p_x l_2 \sin(\theta_2) + p_z (l_1 + l_2 \cos(\theta_2))}$$

# Inverse Kinematics

Why is the problem hard?

- Multiple solutions in configuration space

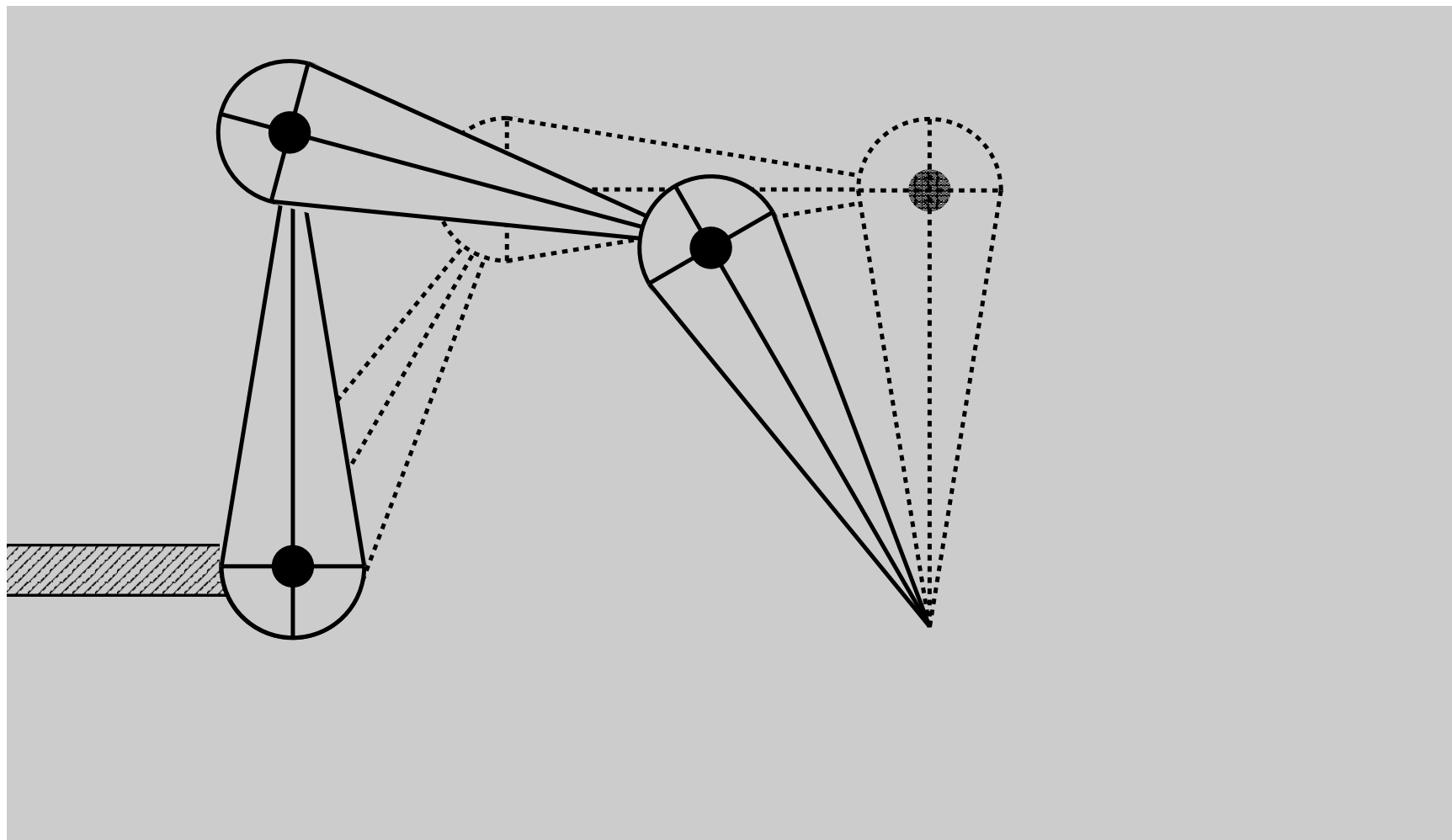




# Inverse Kinematics

Why is the problem hard?

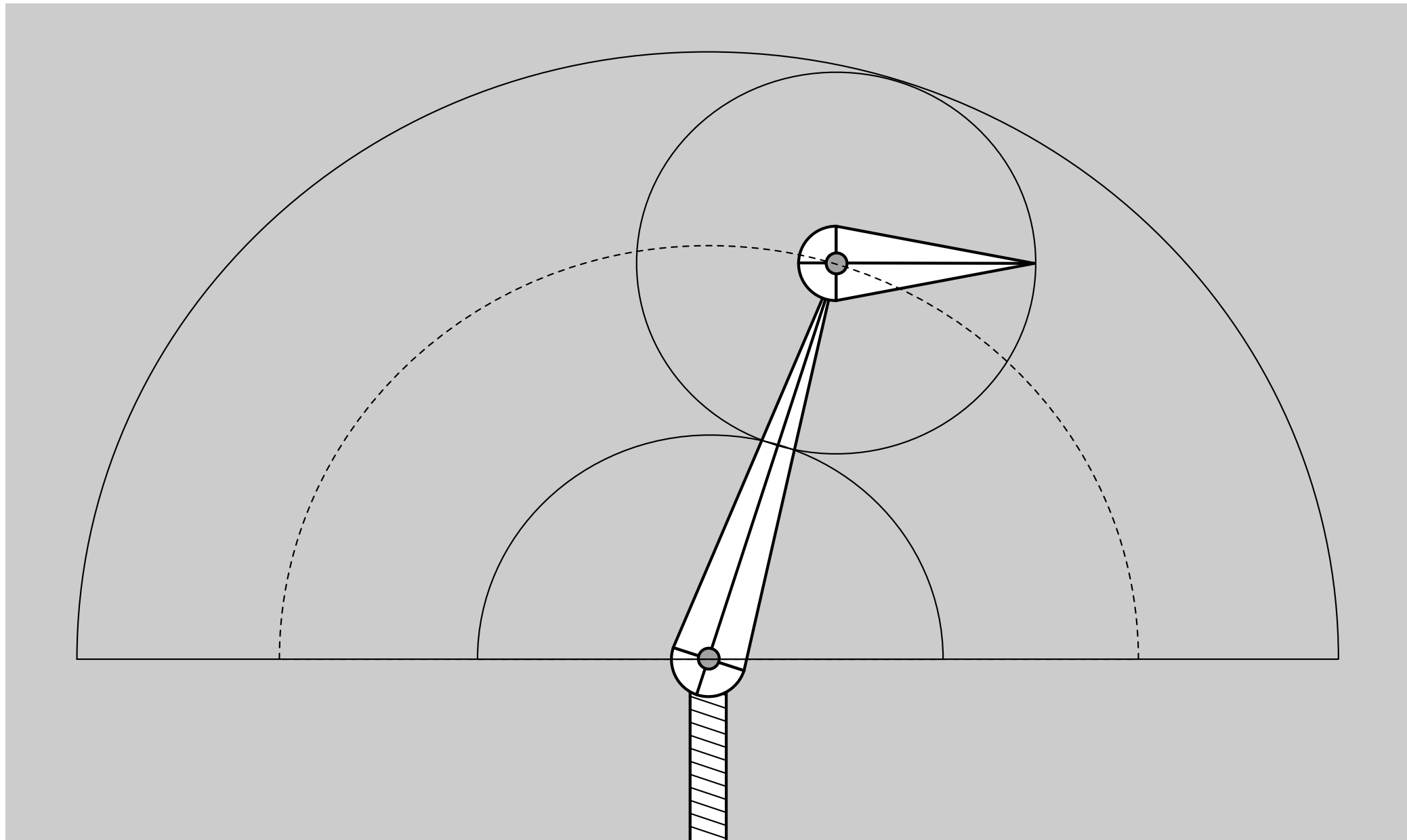
- Multiple solutions in configuration space



# Inverse Kinematics

Why is the problem hard?

- Solutions may not always exist

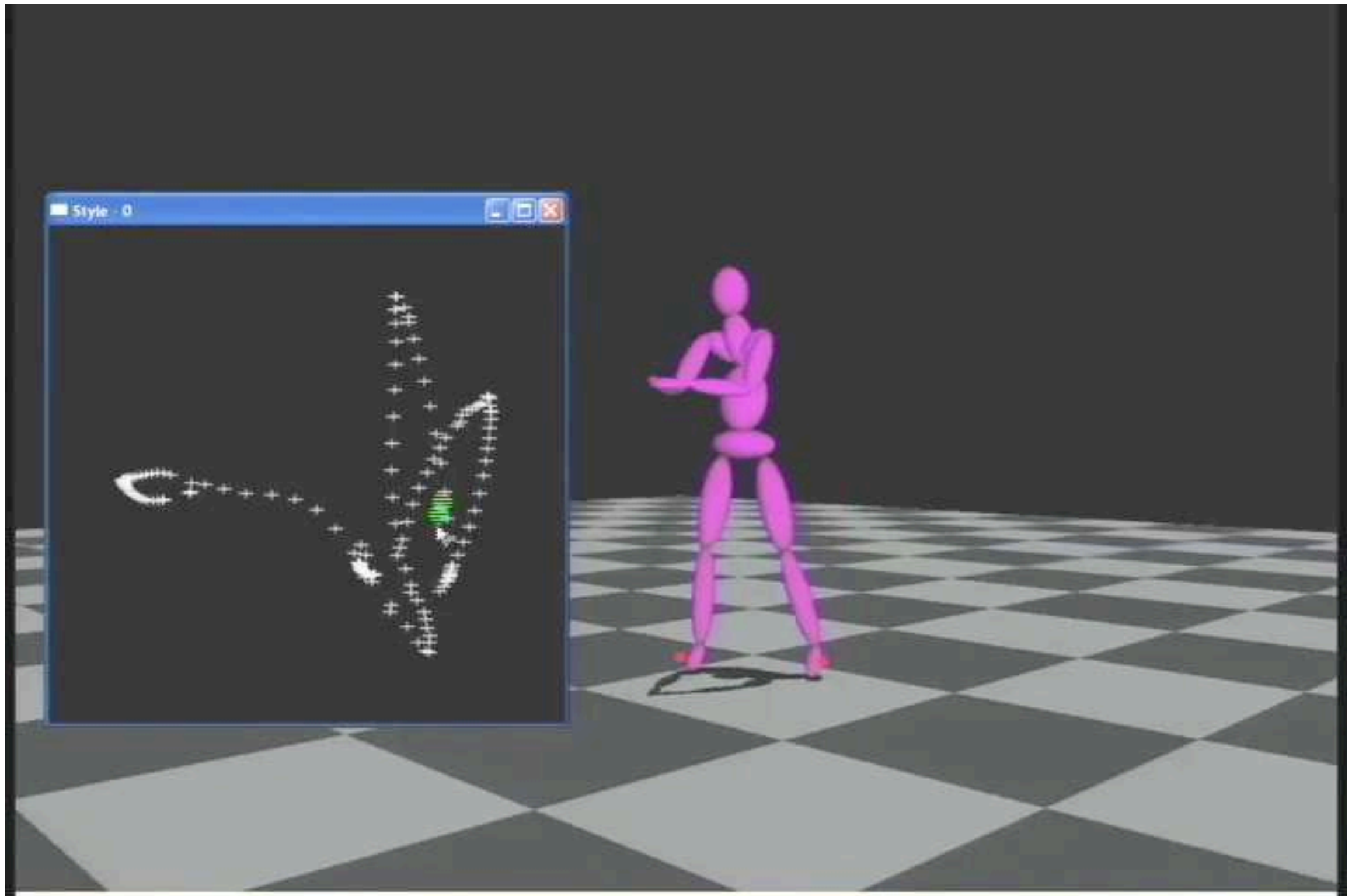


# Inverse Kinematics

Numerical solution to general N-link IK problem

- Choose an initial configuration
- Define an error metric (e.g. square of distance between goal and current position)
- Compute gradient of error as function of configuration
- Apply gradient descent (or Newton's method, or other optimization procedure)

# Style-Based IK



Grochow et al., Style Based Inverse Kinematics



Rigging

# Rigging

Rigging is a set of higher level controls on a character that allow more rapid & intuitive modification of pose, deformations, expression, etc.

Important

- Like strings on a puppet
- Captures all meaningful character changes
- Varies from character to character



Expensive to create

- Manual effort
- Requires both artistic and technical training

# Rigging Example



Courtesy Matthew Lailier via Keenan Crane

# Blend Shapes

Instead of skeleton, interpolate directly between surfaces

E.g., model a collection of facial expressions:

Simplest scheme: take linear combination of vertex positions

Spline used to control choice of weights over time



Courtesy Félix Ferrand

# Blend Shapes



Modeling  
Blendshapes  
Corrective  
No clothes  
full blendshapes

Courtesy Félix Ferrand



# Motion Capture

# Motion Capture

Data-driven approach to creating animation sequences

- Record real-world performances (e.g. person executing an activity)
- Extract pose as a function of time from the data collected



Motion capture room for ShaqFu

# Motion Capture Pros and Cons

## Strengths

- Can capture large amounts of real data quickly
- Realism can be high

## Weaknesses

- Complex and costly set-ups
- Captured animation may not meet artistic needs, requiring alterations

# Motion Capture Equipment



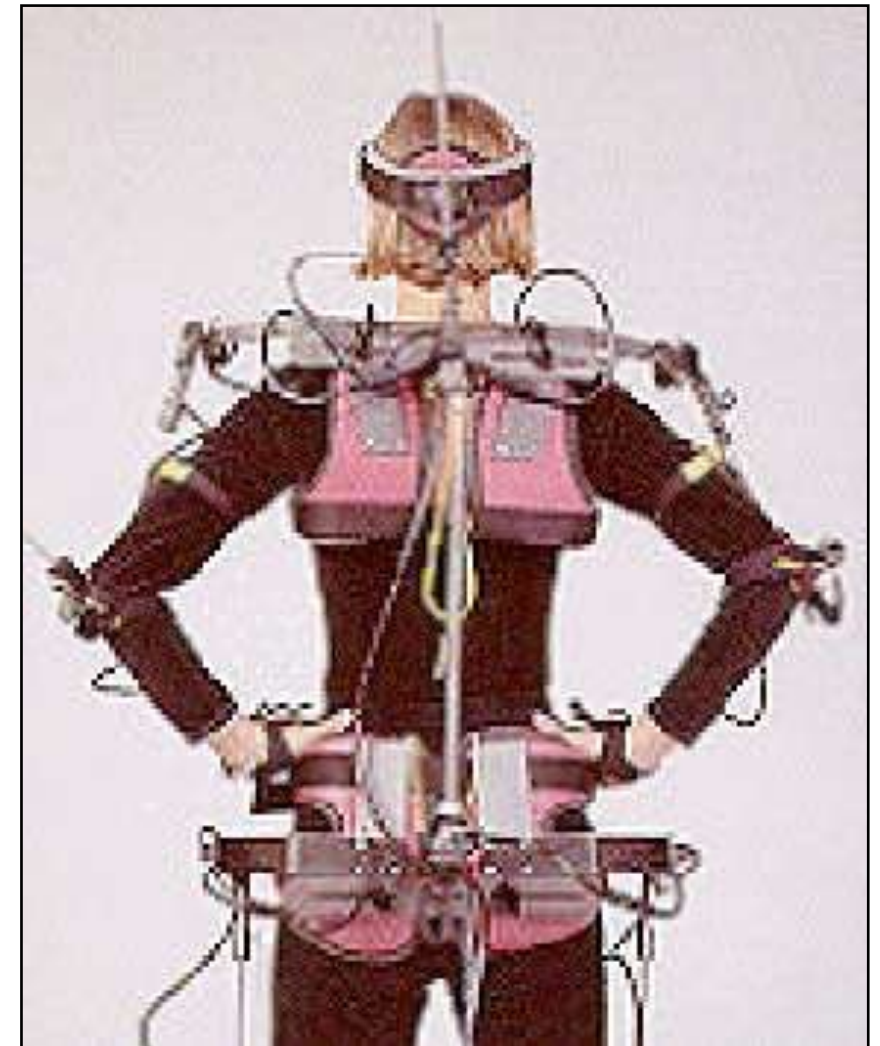
## **Optical**

(More on following slides)



## **Magnetic**

Sense magnetic fields to  
infer position / orientation.  
Tethered.



## **Mechanical**

Measure joint angles directly.  
Restricts motion.



# Optical Motion Capture



Retroreflective markers attached to subject



IR illumination and cameras

- Markers on subject
- Positions by triangulation from multiple cameras
- 8+ cameras, 240 Hz, occlusions are difficult

Slide credit: Prof. Steve Marschner @ Cornell



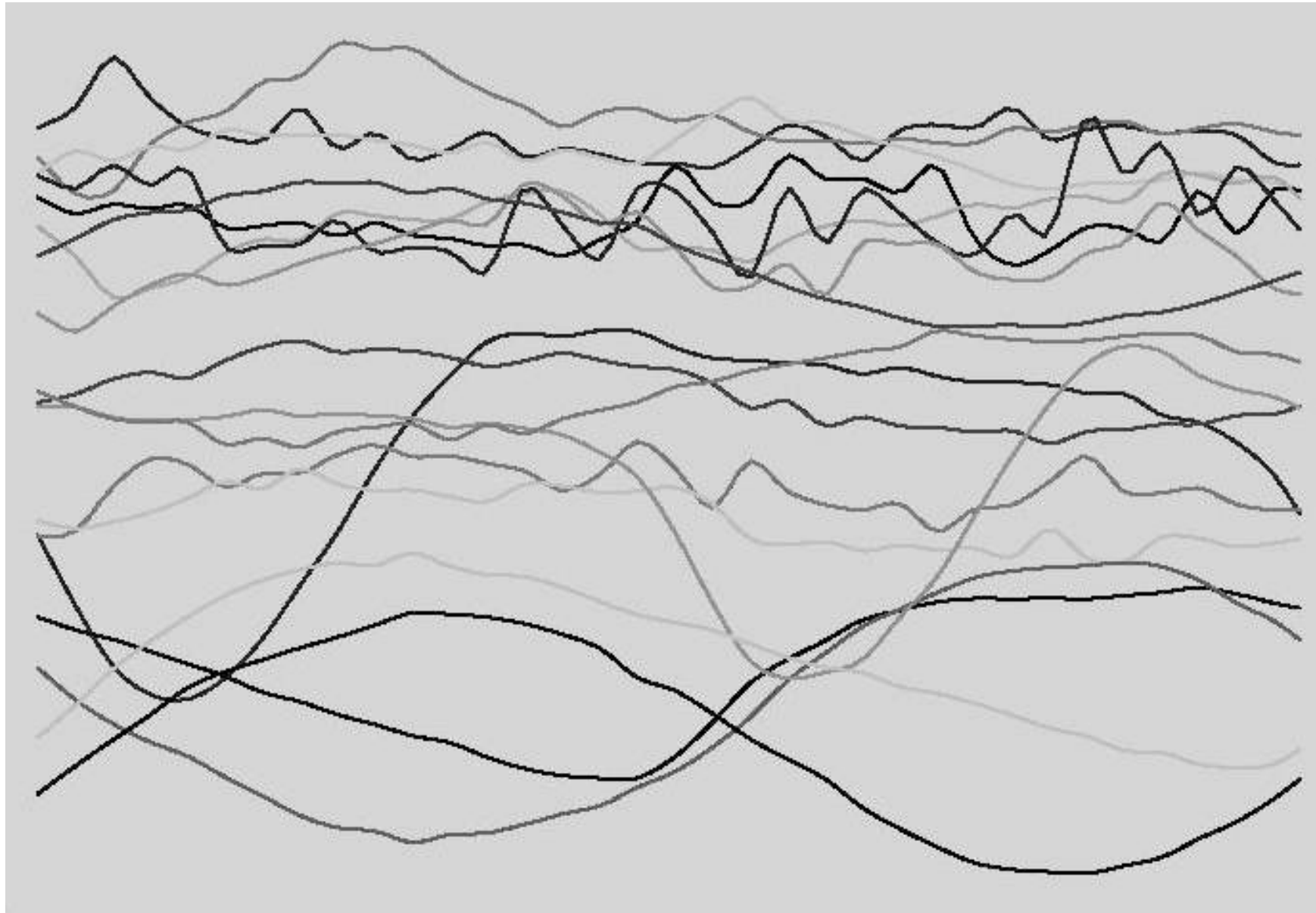
# Optical Motion Capture



Source: <http://fightland.vice.com/blog/ronda-rousey-20-the-queen-of-all-media>

Ronda Rousey in Electronic Arts' motion capture studio

# Motion Data



Subset of motion curves from captured walking motion.

From Witkin and Popovic, 1995

# Challenges of Facial Animation

Uncanny valley (恐怖谷效应)

- In robotics and graphics
- As artificial character appearance approaches human realism, our emotional response goes negative, until it achieves a sufficiently convincing level of realism in expression



Cartoon.  
Brave, Pixar



Semi-realistic. Polar Express, Warner Bros.



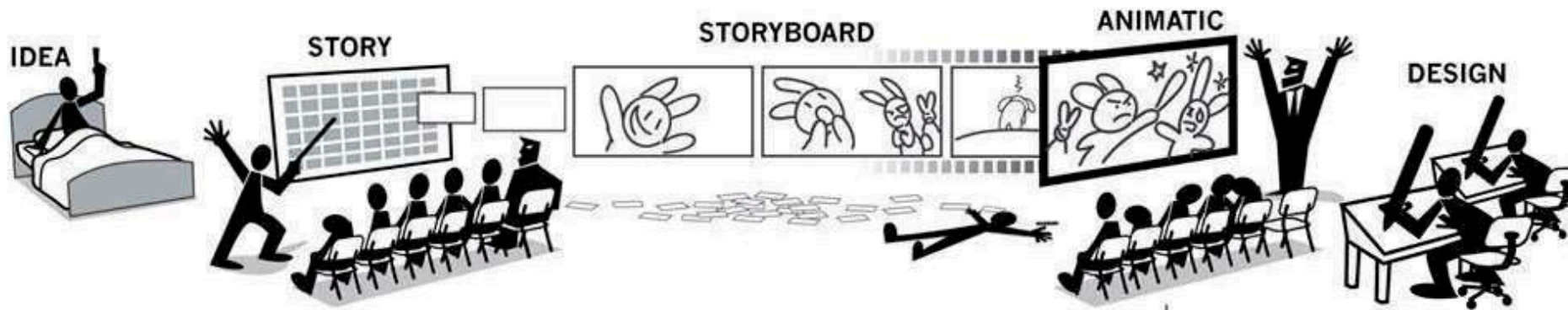
# Facial Motion Capture



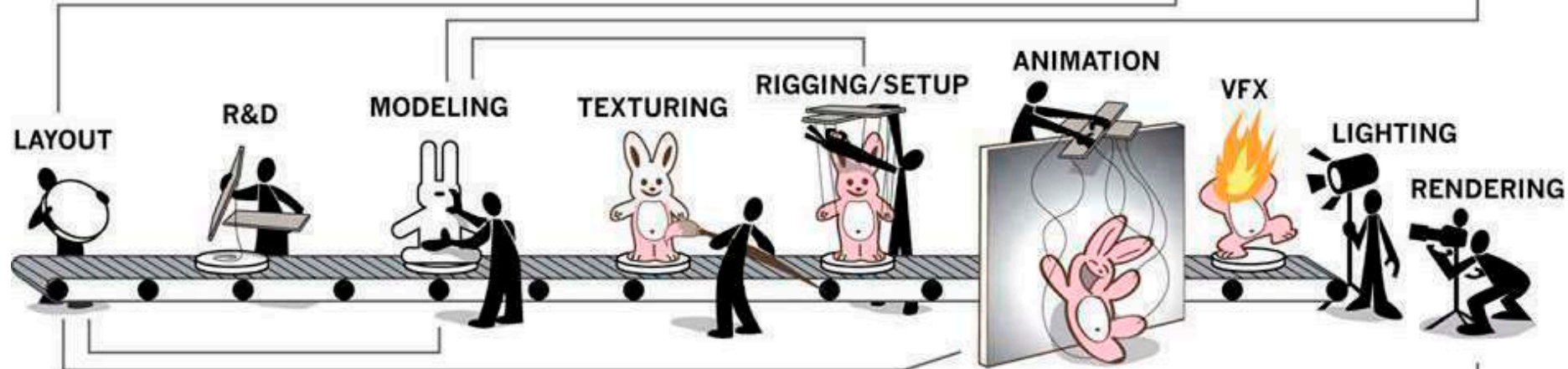
Discovery, "Avatar: Motion Capture Mirrors Emotions", <https://youtu.be/1wK1lxx-UmM>

# The Production Pipeline

## PRE-PRODUCTION



## PRODUCTION



## POST-PRODUCTION

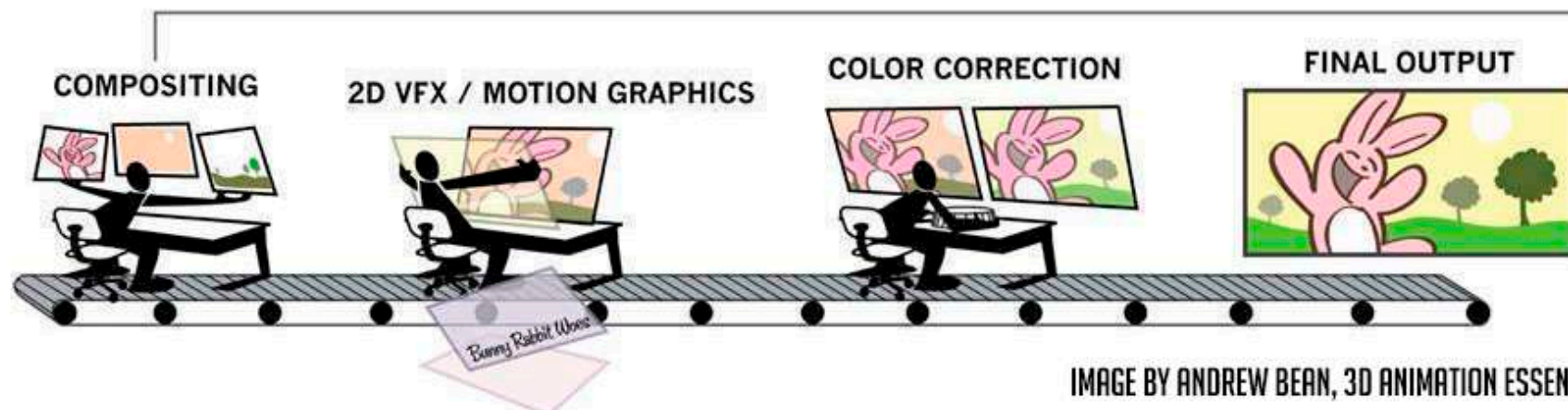


IMAGE BY ANDREW BEAN, 3D ANIMATION ESSENTIALS (2012)



# Next (Final) Lecture

Given the forces / physics / theory, how to simulate actual movements



Hint: what would he say in a fight?

Credit: JoJo's Bizarre Adventure

# Thank you!

(And thank Prof. Ren Ng for many of the slides!)