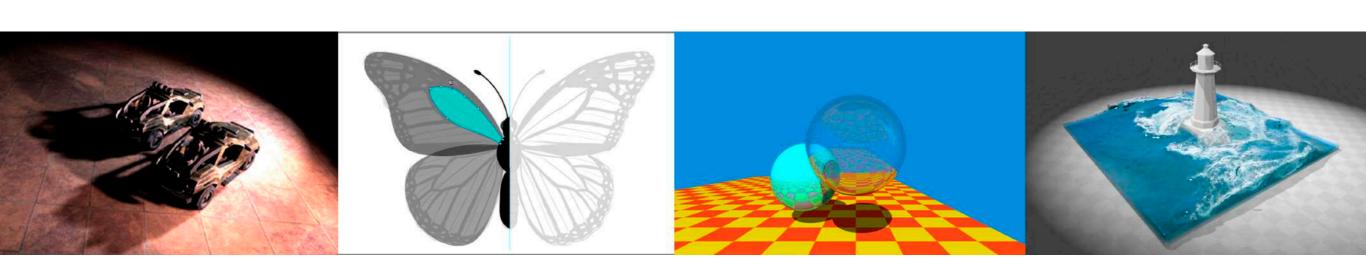
Introduction to Computer Graphics

GAMES101, Lingqi Yan, UC Santa Barbara

Lecture 9: Shading 3 (Texture Mapping cont.)



Announcements

- About homework
 - Homework 1 is being graded
 - Homework 2
 - 271 submissions so far
 - Homework 3 will be released soon

Last Lectures

- Shading 1 & 2
 - Blinn-Phong reflectance model
 - Shading models / frequencies
 - Graphics Pipeline
 - Texture mapping

Today

- Shading 3
 - Barycentric coordinates
 - Texture queries
 - Applications of textures
- Shadow mapping

Interpolation Across Triangles: Barycentric Coordinates

(重心坐标)

Interpolation Across Triangles

Why do we want to interpolate?

- Specify values at vertices
- Obtain smoothly varying values across triangles

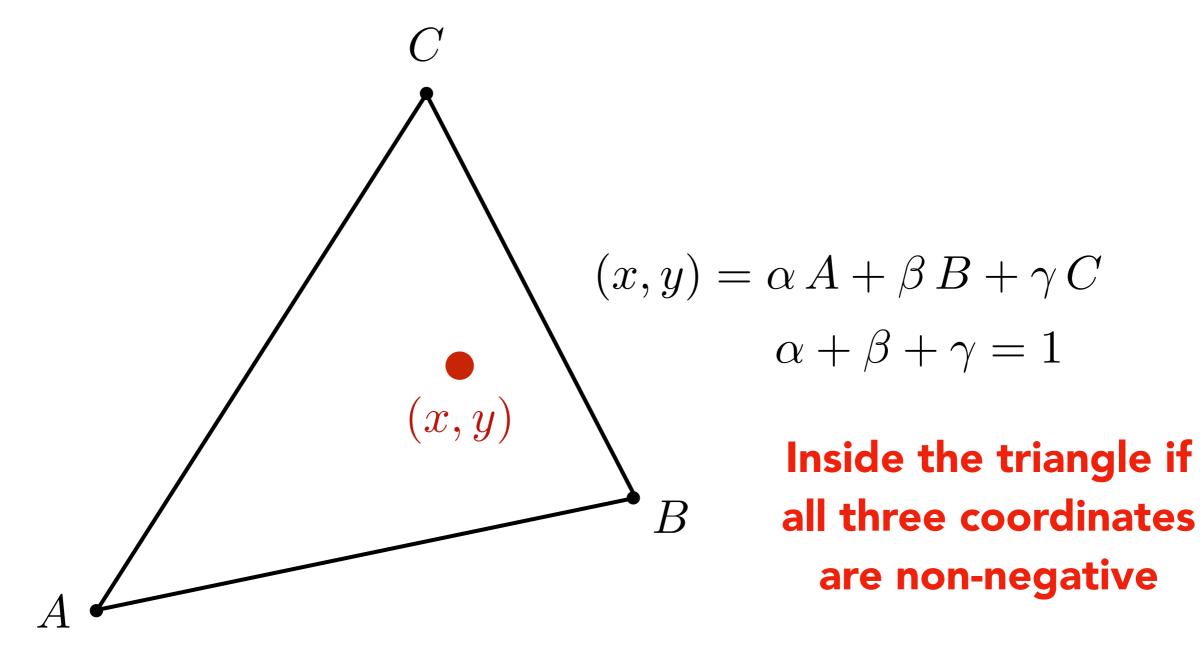
What do we want to interpolate?

Texture coordinates, colors, normal vectors, ...

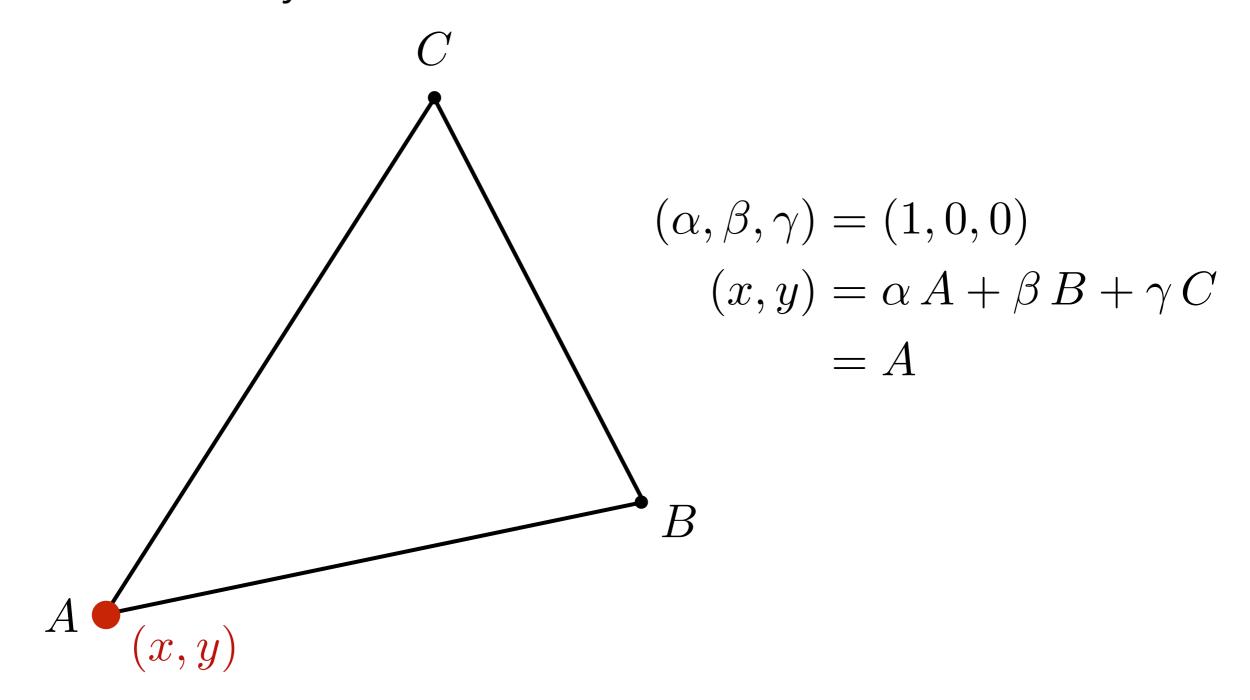
How do we interpolate?

Barycentric coordinates

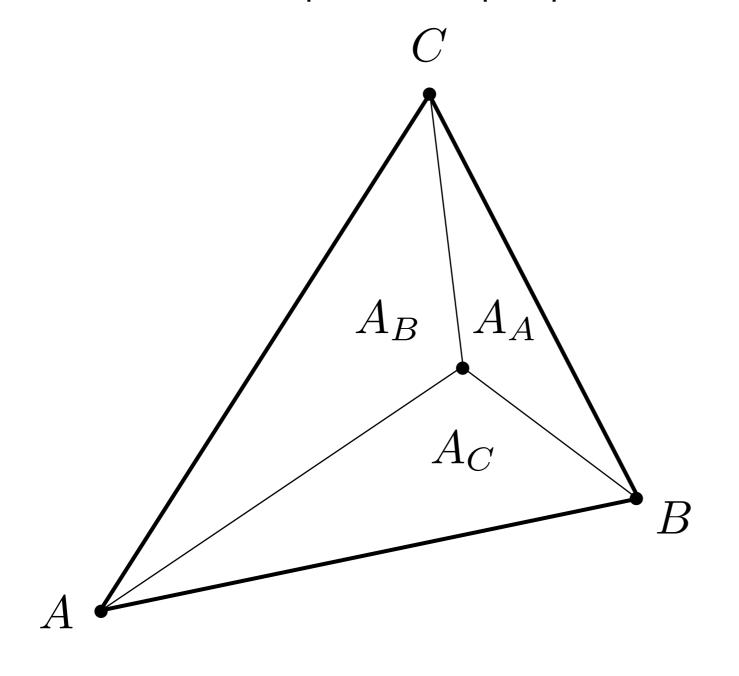
A coordinate system for triangles (α, β, γ)



What's the barycentric coordinate of A?



Geometric viewpoint — proportional areas

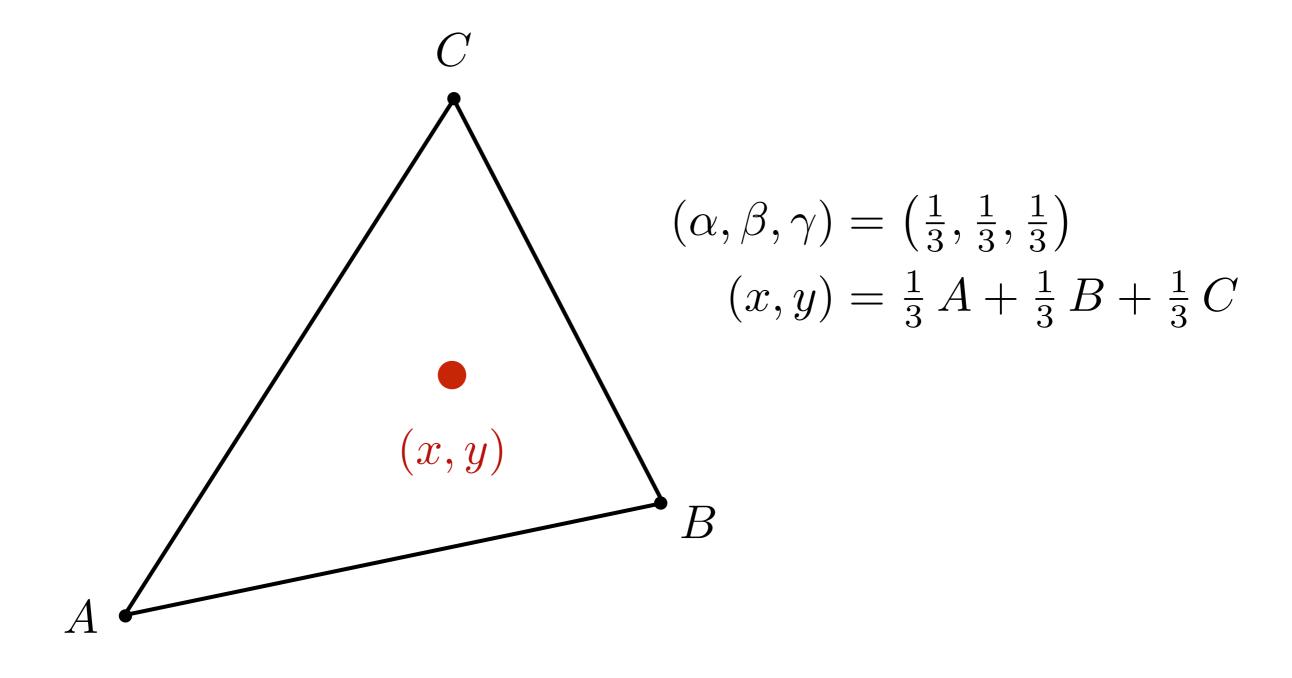


$$\alpha = \frac{A_A}{A_A + A_B + A_C}$$

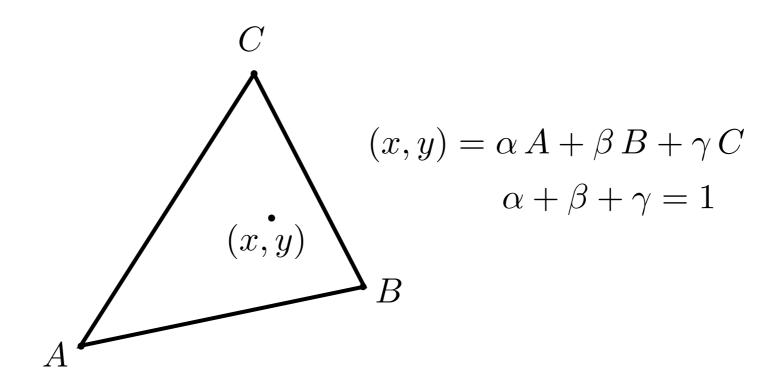
$$\beta = \frac{A_B}{A_A + A_B + A_C}$$

$$\gamma = \frac{A_C}{A_A + A_B + A_C}$$

What's the barycentric coordinate of the centroid?



Barycentric Coordinates: Formulas



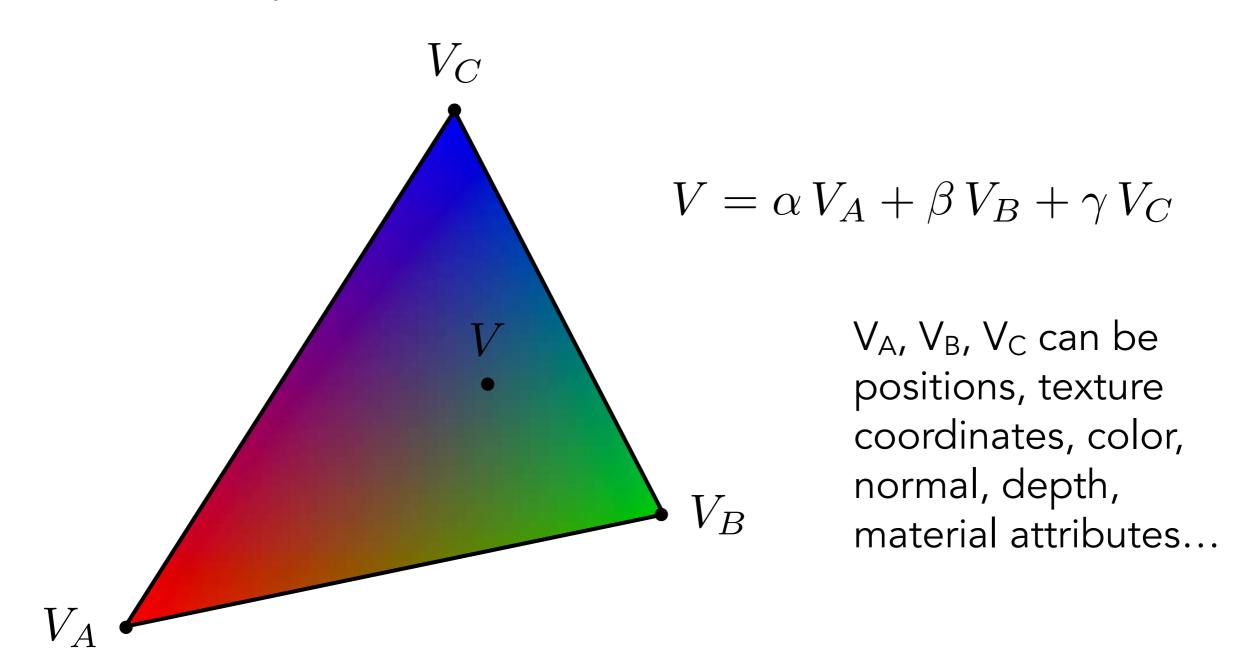
$$\alpha = \frac{-(x - x_B)(y_C - y_B) + (y - y_B)(x_C - x_B)}{-(x_A - x_B)(y_C - y_B) + (y_A - y_B)(x_C - x_B)}$$

$$\beta = \frac{-(x - x_C)(y_A - y_C) + (y - y_C)(x_A - x_C)}{-(x_B - x_C)(y_A - y_C) + (y_B - y_C)(x_A - x_C)}$$

$$\gamma = 1 - \alpha - \beta$$

Using Barycentric Coordinates

Linearly interpolate values at vertices



However, barycentric coordinates are not invariant under projection!

Applying Textures

Simple Texture Mapping: Diffuse Color

Usually a pixel's center

for each rasterized screen sample (x,y):

(u,v) = evaluate texture coordinate at (x,y)

texcolor = texture.sample(u,v);

set sample's color to texcolor;

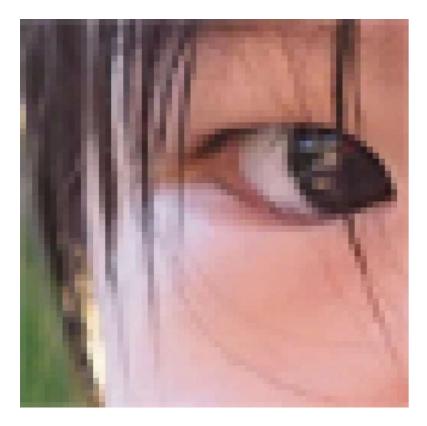
Usually the diffuse albedo Kd (recall the Blinn-Phong reflectance model)

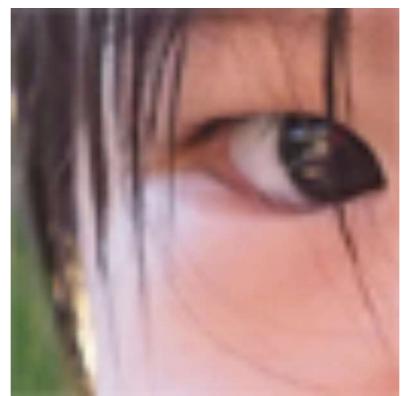
Using barycentric coordinates!

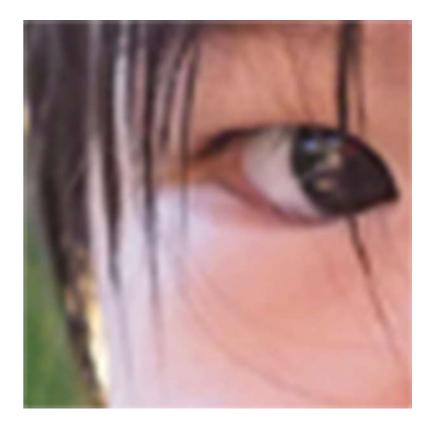
Texture Magnification (What if the texture is too small?)

Texture Magnification - Easy Case

Generally don't want this — insufficient texture resolution A pixel on a texture — a **texel** (纹理元素、纹素)



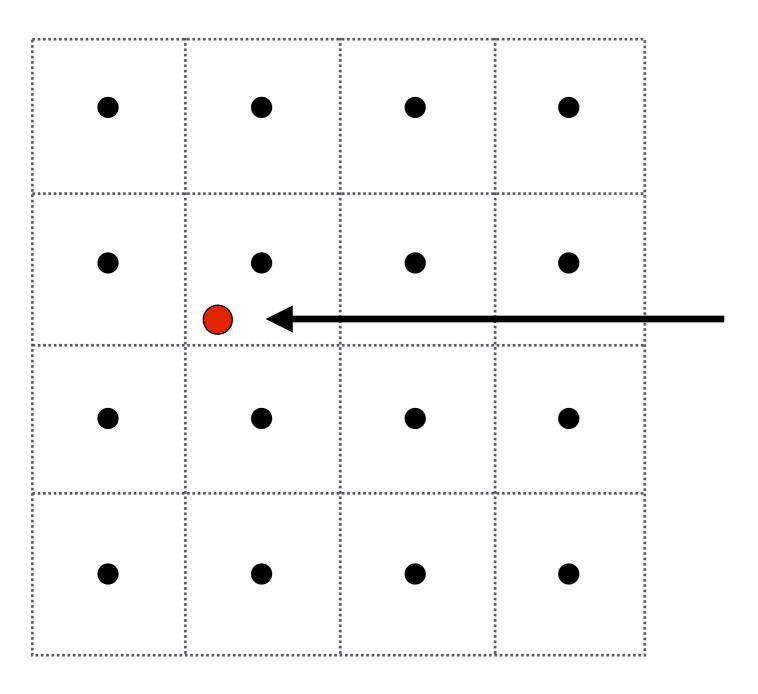




Nearest

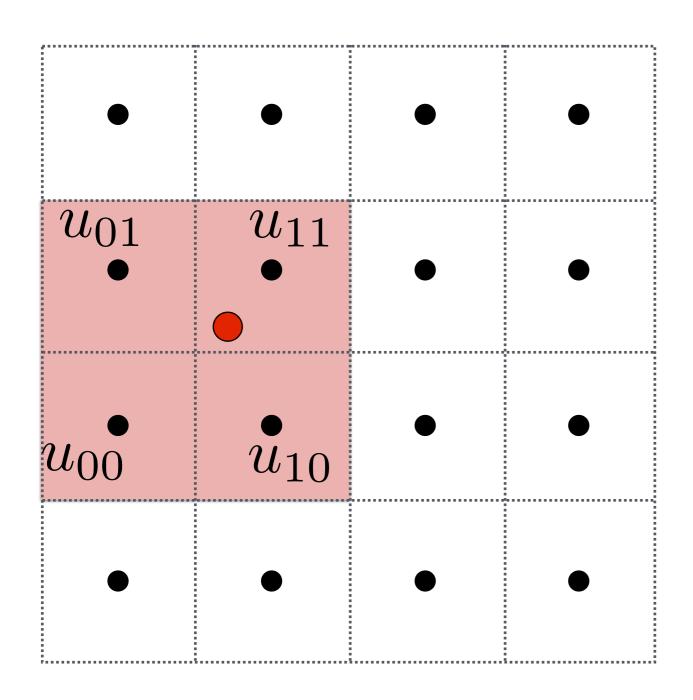
Bilinear

Bicubic

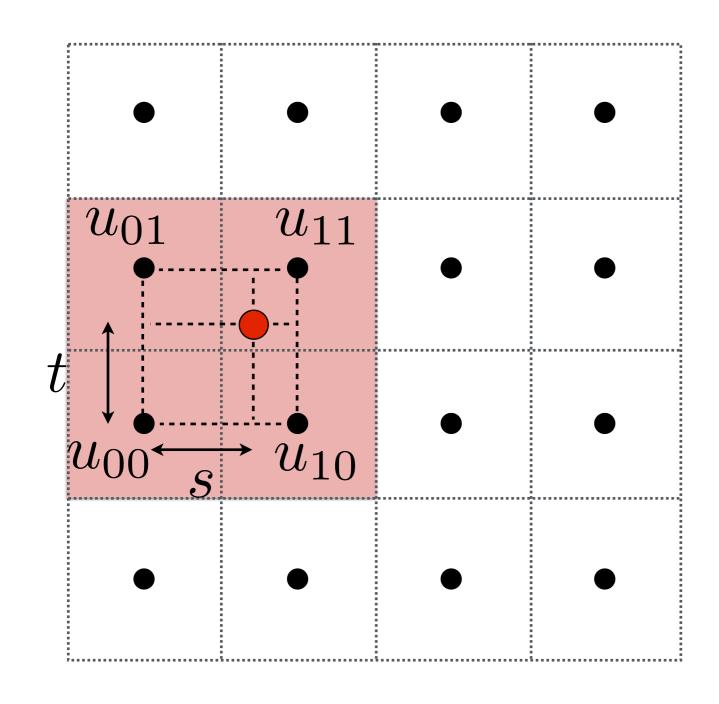


Want to sample texture value f(x,y) at red point

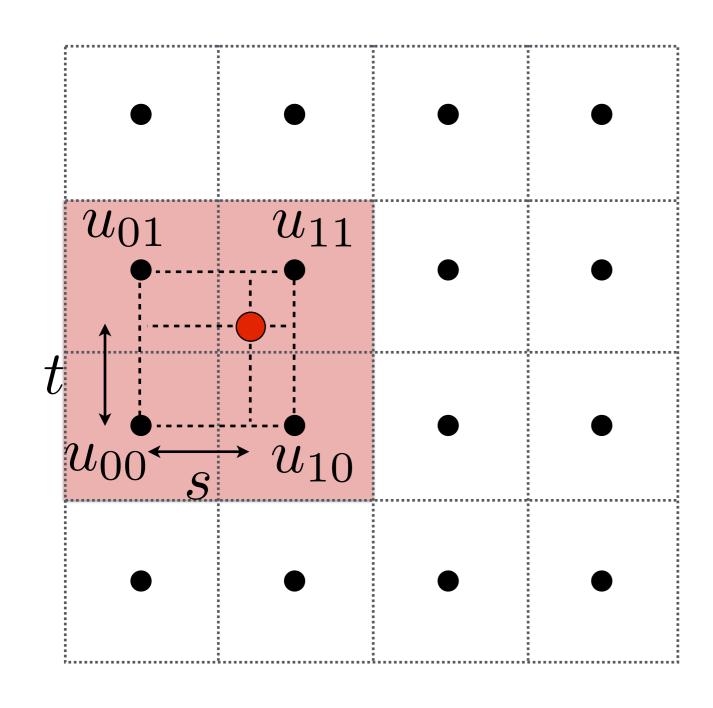
Black points indicate texture sample locations



Take 4 nearest sample locations, with texture values as labeled.

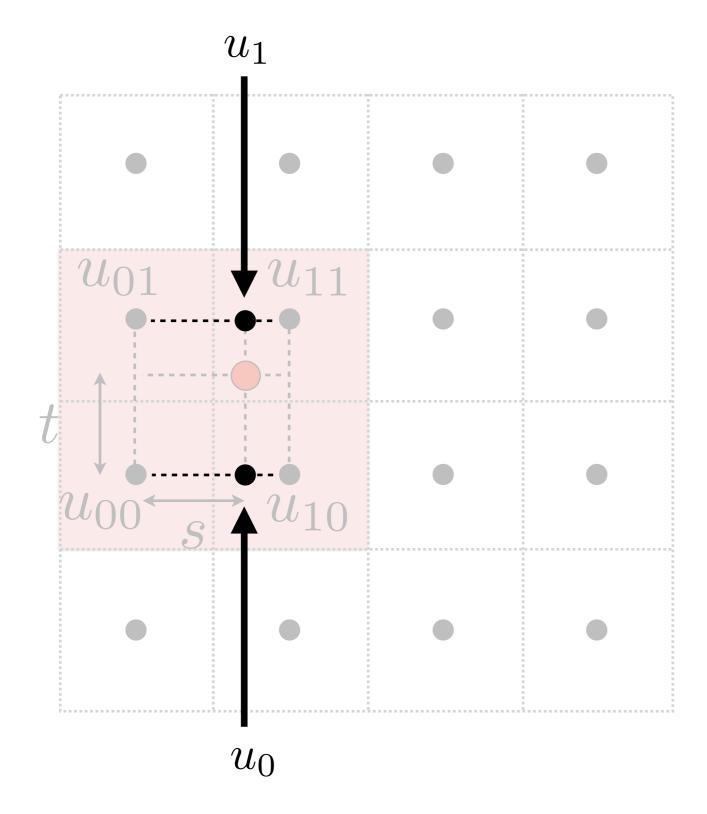


And fractional offsets, (s,t) as shown



Linear interpolation (1D)

$$lerp(x, v_0, v_1) = v_0 + x(v_1 - v_0)$$



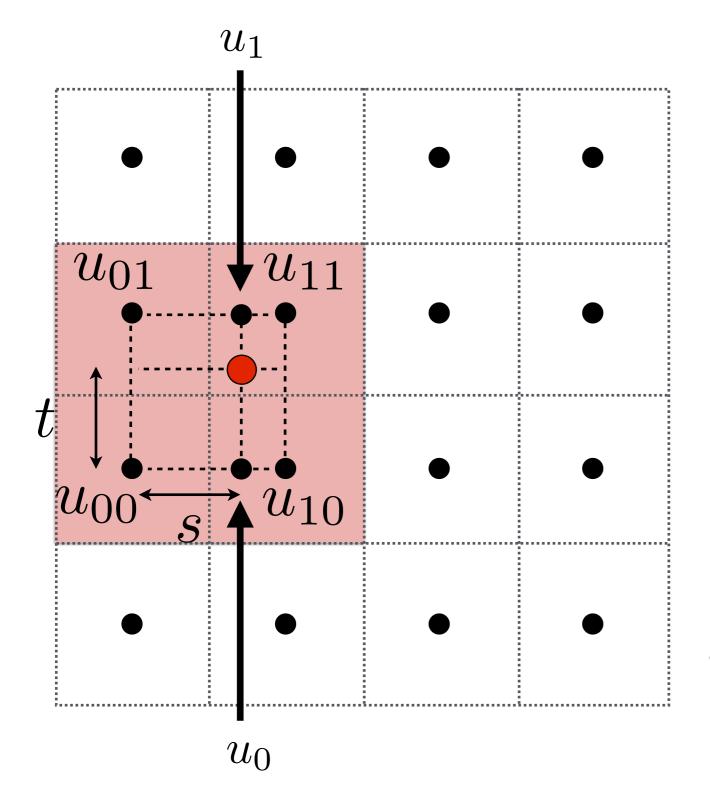
Linear interpolation (1D)

$$lerp(x, v_0, v_1) = v_0 + x(v_1 - v_0)$$

Two helper lerps (horizontal)

$$u_0 = \text{lerp}(s, u_{00}, u_{10})$$

$$u_1 = \text{lerp}(s, u_{01}, u_{11})$$



Linear interpolation (1D)

$$lerp(x, v_0, v_1) = v_0 + x(v_1 - v_0)$$

Two helper lerps

$$u_0 = \text{lerp}(s, u_{00}, u_{10})$$

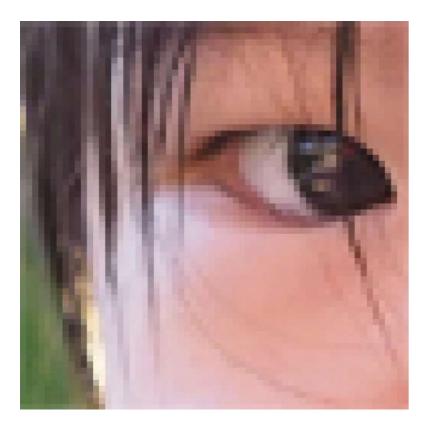
$$u_1 = \text{lerp}(s, u_{01}, u_{11})$$

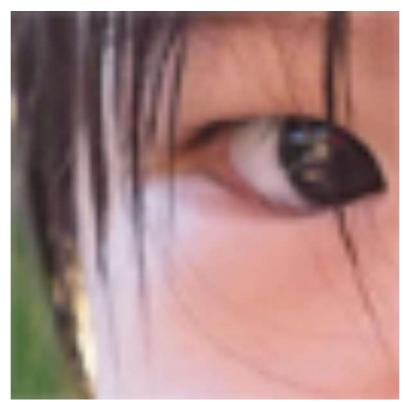
Final vertical lerp, to get result:

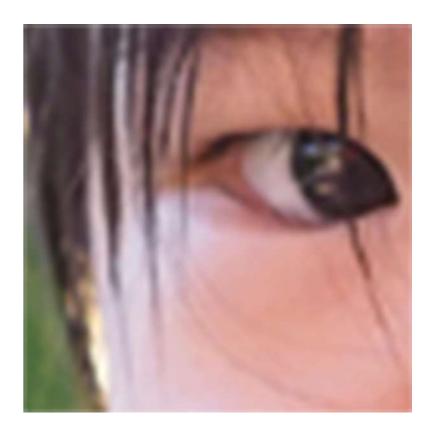
$$f(x,y) = \operatorname{lerp}(t, u_0, u_1)$$

Texture Magnification - Easy Case

Bilinear interpolation usually gives pretty good results at reasonable costs







Nearest

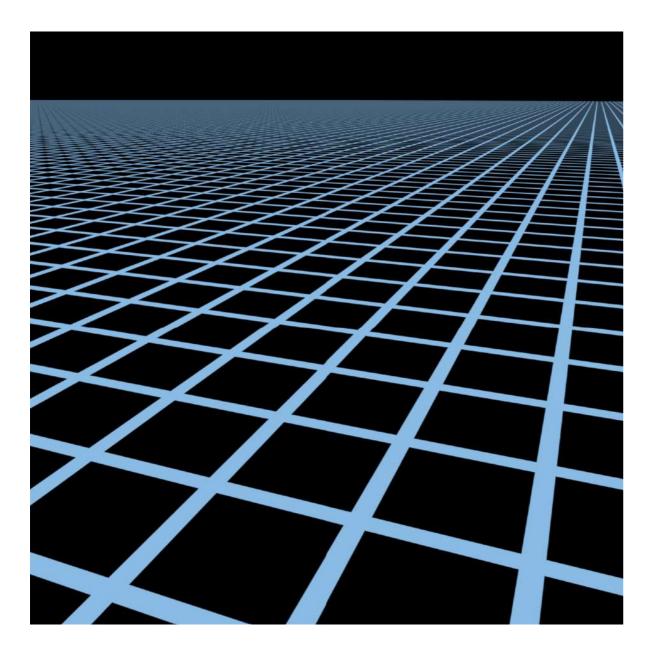
Bilinear

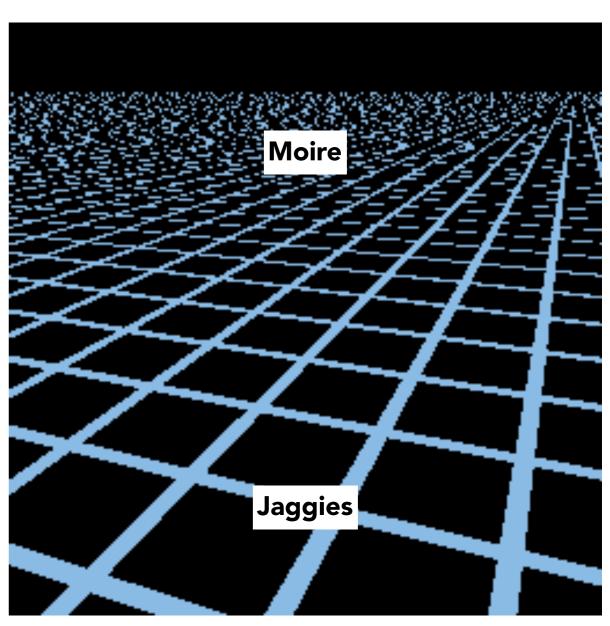
Bicubic

Texture Magnification (hard case)

(What if the texture is too large?)

Point Sampling Textures — Problem

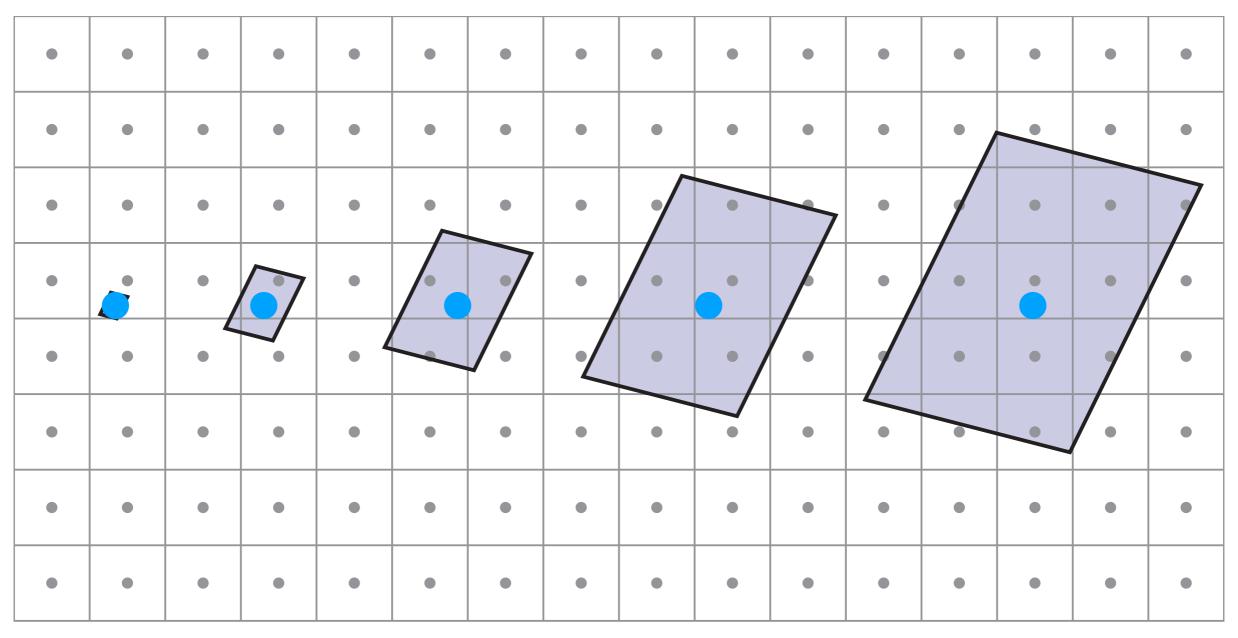




Reference

Point sampled

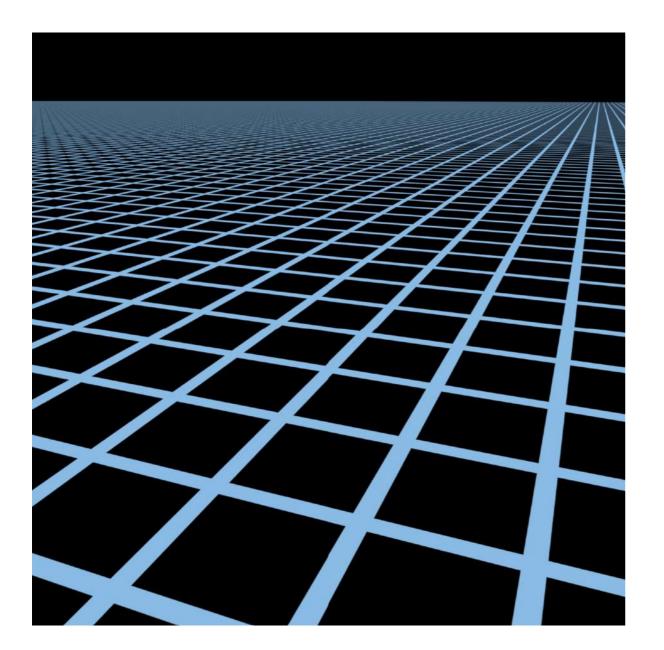
Screen Pixel "Footprint" in Texture

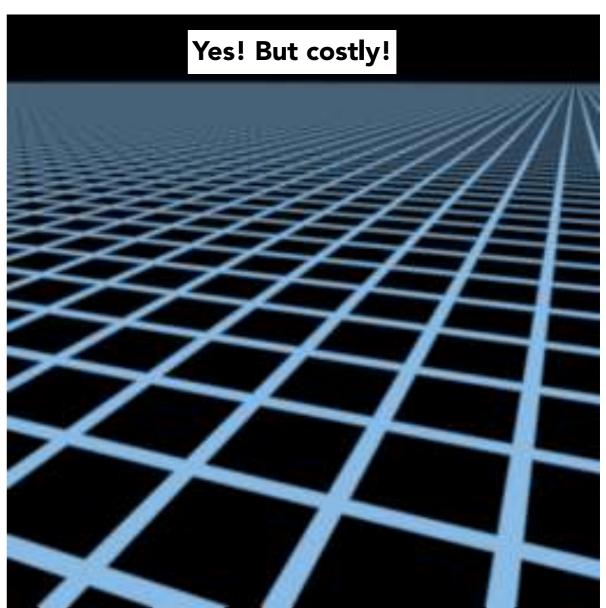


Upsampling (Magnification)

Downsampling (Minification)

Will Supersampling Do Antialiasing?





512x supersampling

Antialiasing — Supersampling?

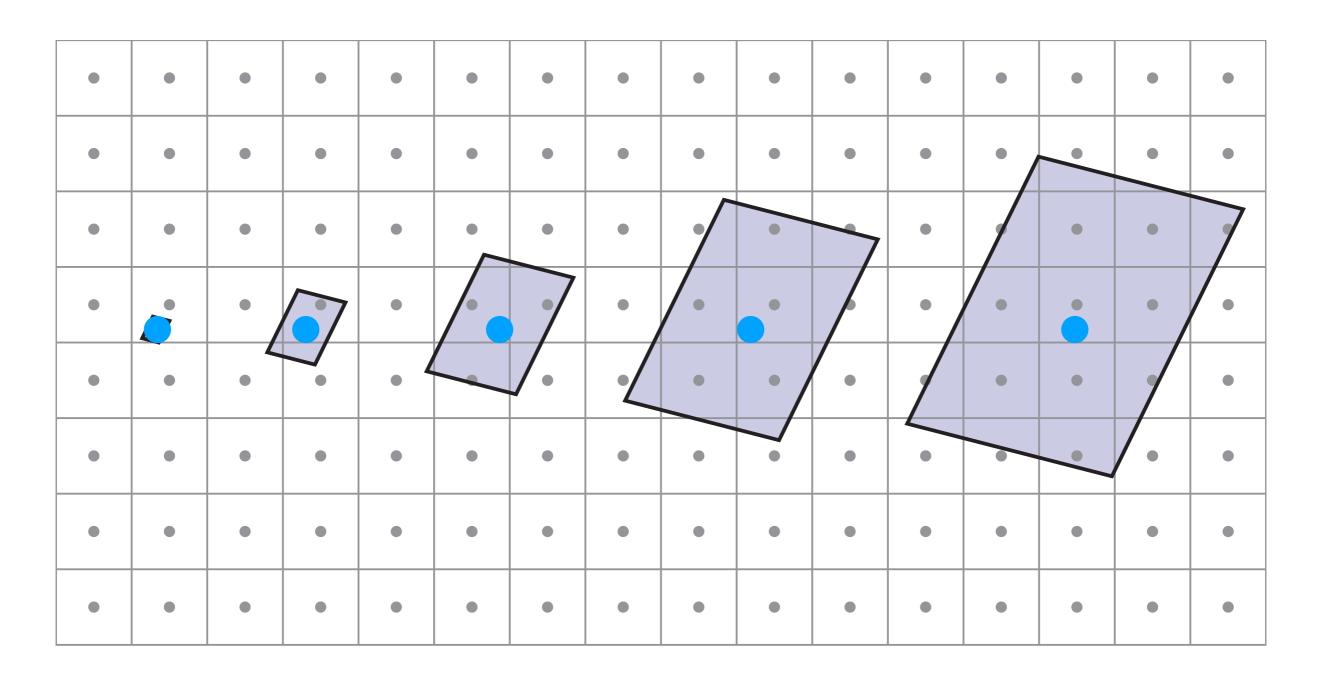
Will supersampling work?

- Yes, high quality, but costly
- When highly minified, many texels in pixel footprint
- Signal frequency too large in a pixel
- Need even higher sampling frequency

Let's understand this problem in another way

- What if we don't sample?
- Just need to get the average value within a range!

Point Query vs. (Avg.) Range Query



Different Pixels -> Different-Sized Footprints

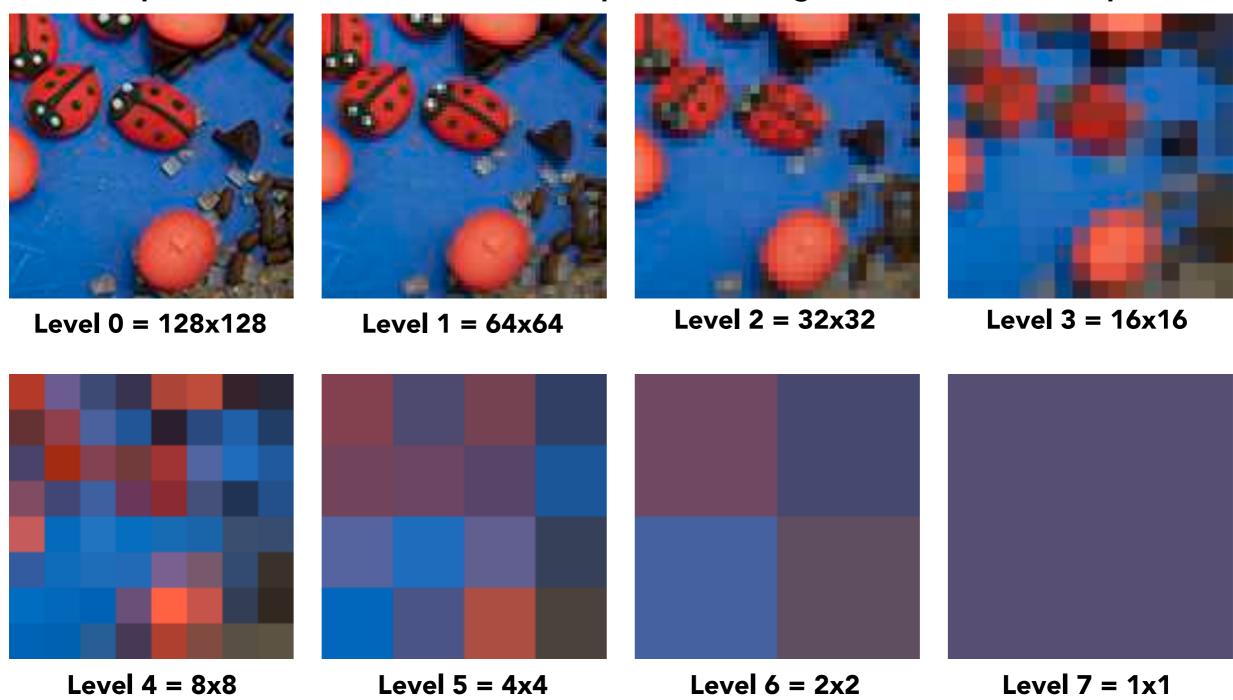


Mipmap

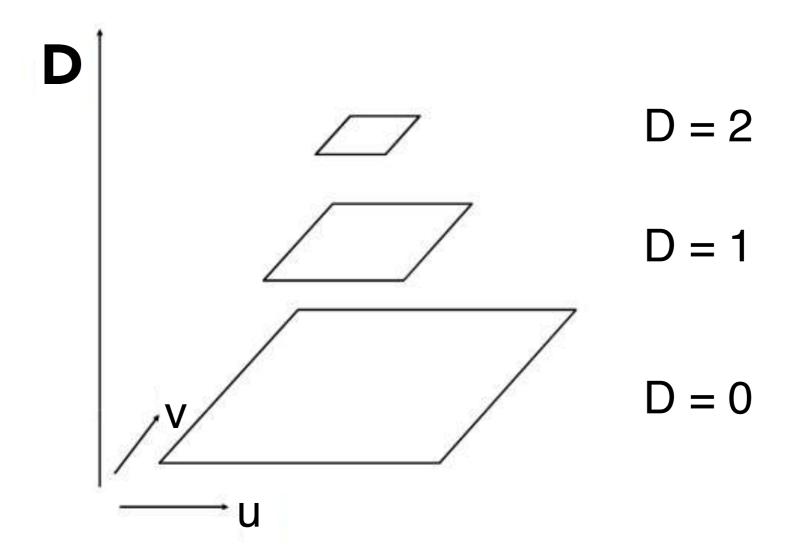
Allowing (fast, approx., square) range queries

Mipmap (L. Williams 83)

"Mip" comes from the Latin "multum in parvo", meaning a multitude in a small space

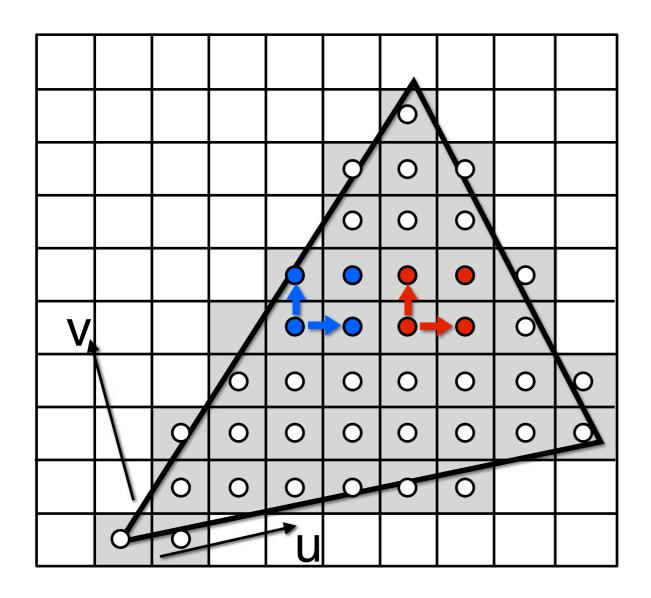


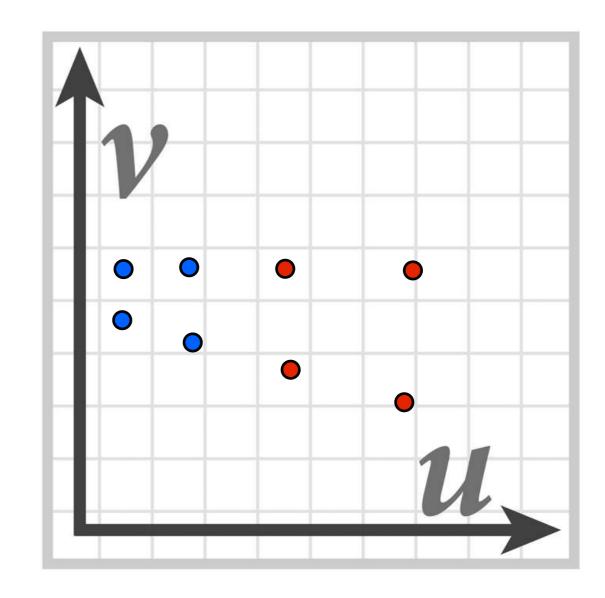
Mipmap (L. Williams 83)



"Mip hierarchy"
level = D
What is the storage overhead of a mipmap?

Computing Mipmap Level D



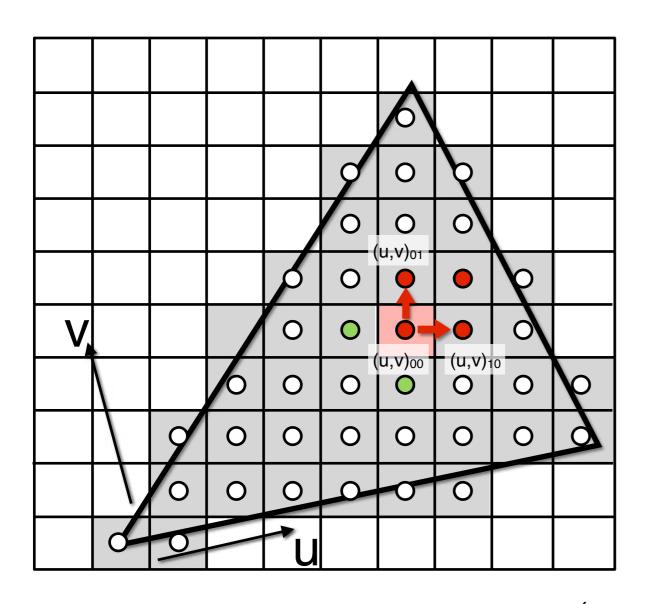


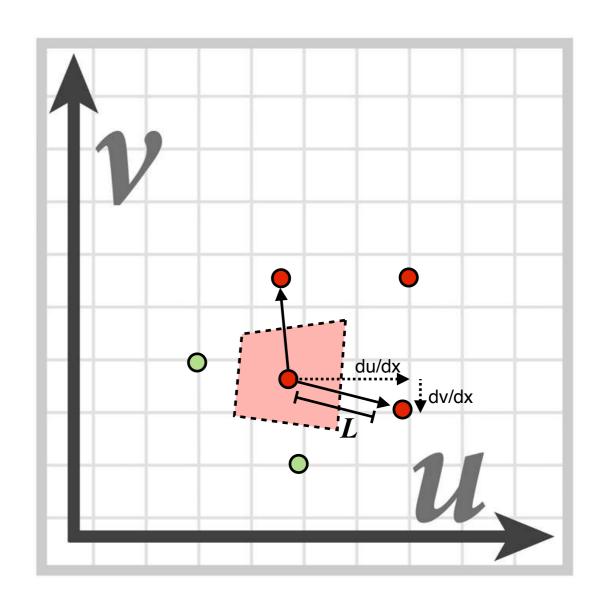
Screen space (x,y)

Texture space (u,v)

Estimate texture footprint using texture coordinates of neighboring screen samples

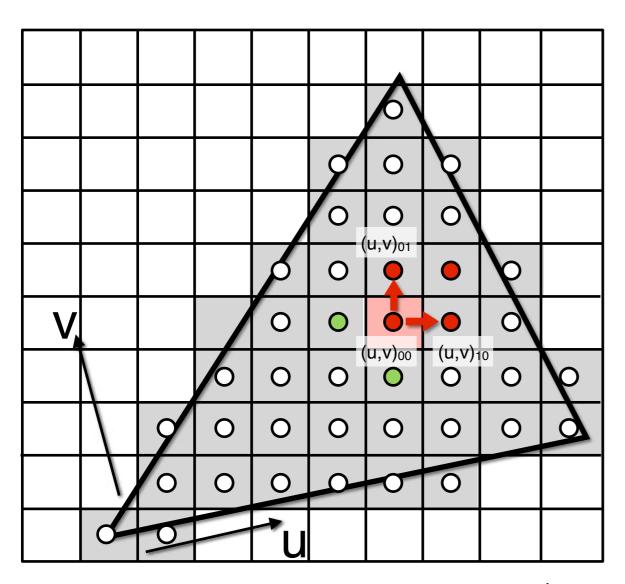
Computing Mipmap Level D

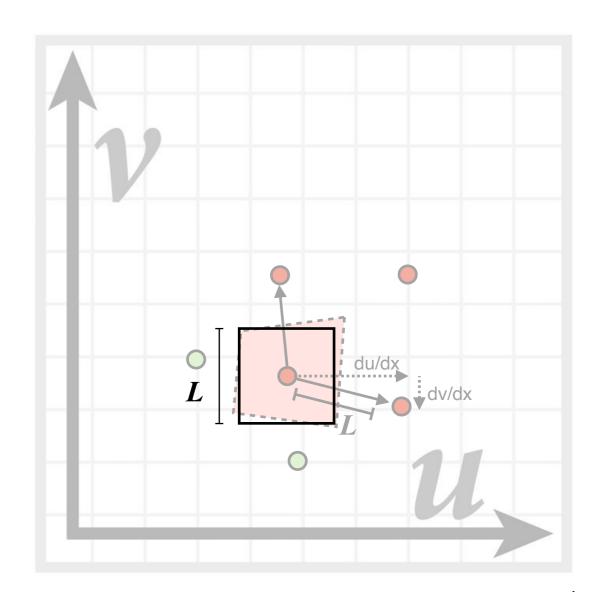




$$D = \log_2 L \qquad L = \max\left(\sqrt{\left(\frac{du}{dx}\right)^2 + \left(\frac{dv}{dx}\right)^2}, \sqrt{\left(\frac{du}{dy}\right)^2 + \left(\frac{dv}{dy}\right)^2}\right)$$

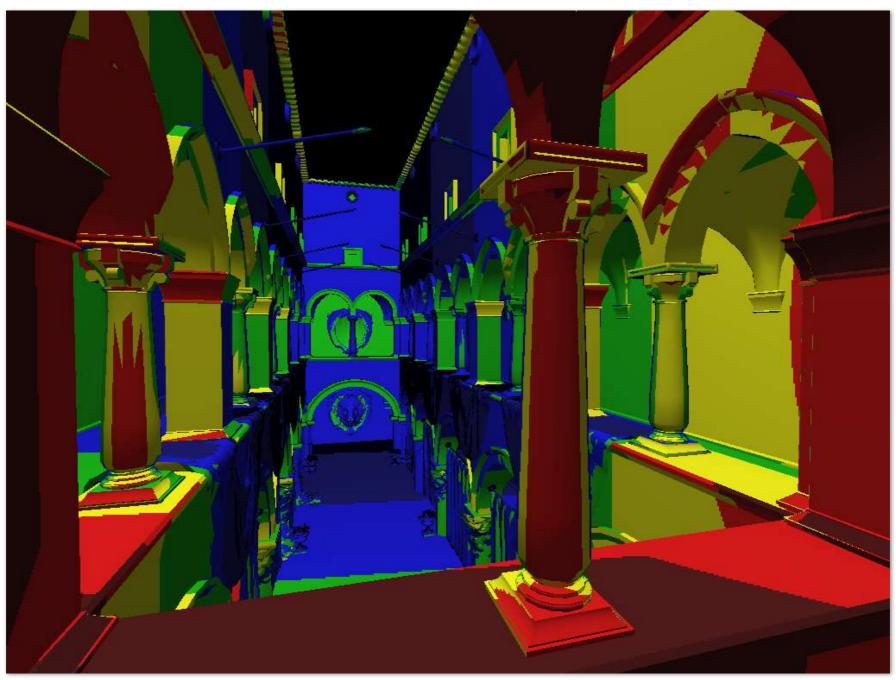
Computing Mipmap Level D



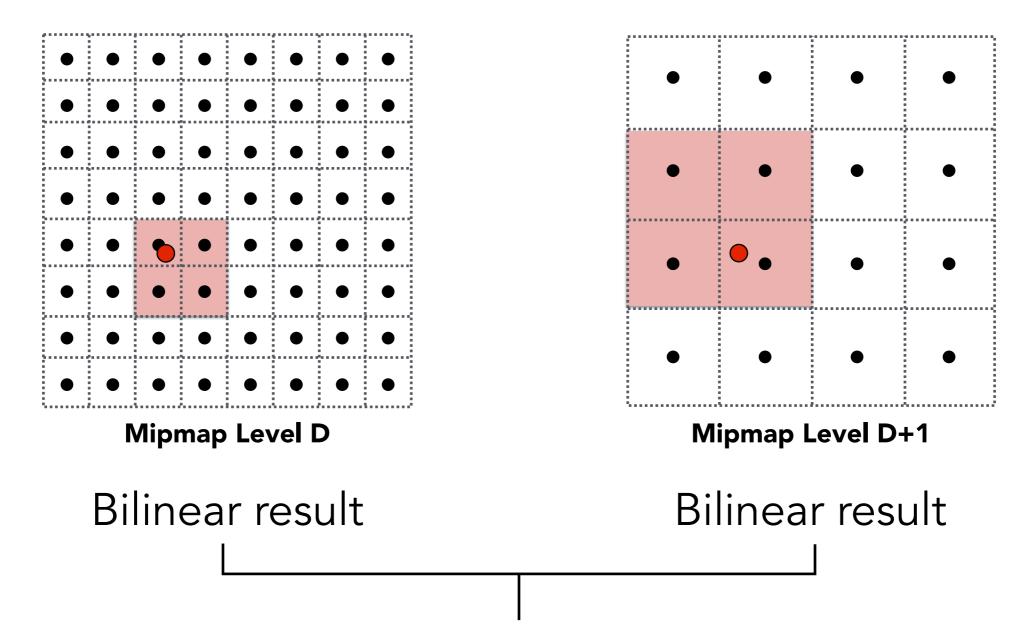


$$D = \log_2 L \qquad L = \max\left(\sqrt{\left(\frac{du}{dx}\right)^2 + \left(\frac{dv}{dx}\right)^2}, \sqrt{\left(\frac{du}{dy}\right)^2 + \left(\frac{dv}{dy}\right)^2}\right)$$

Visualization of Mipmap Level

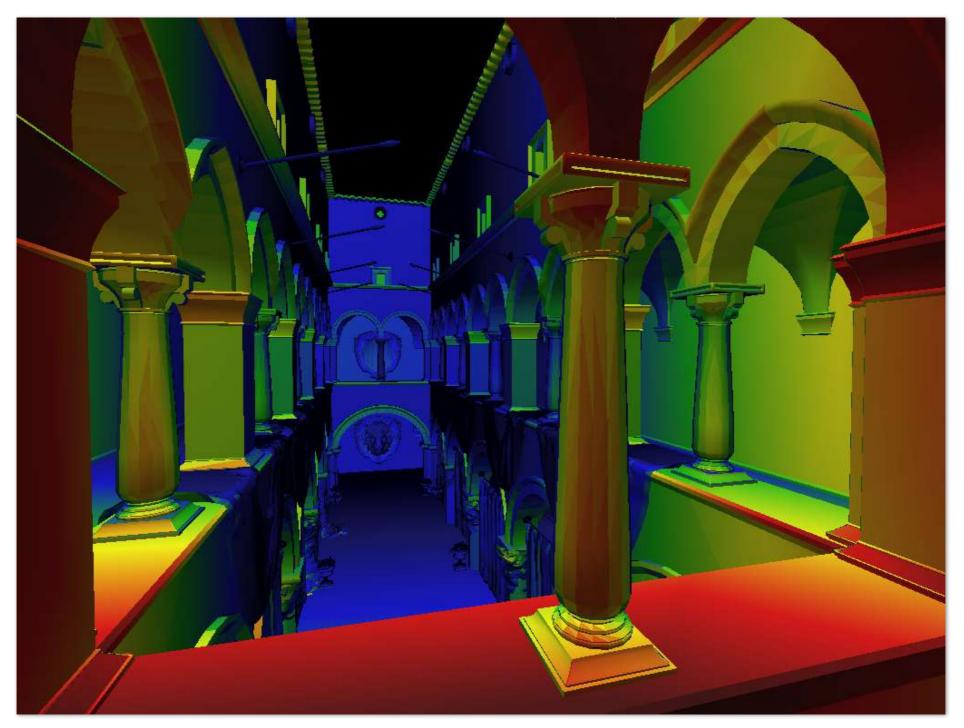


D rounded to nearest integer level



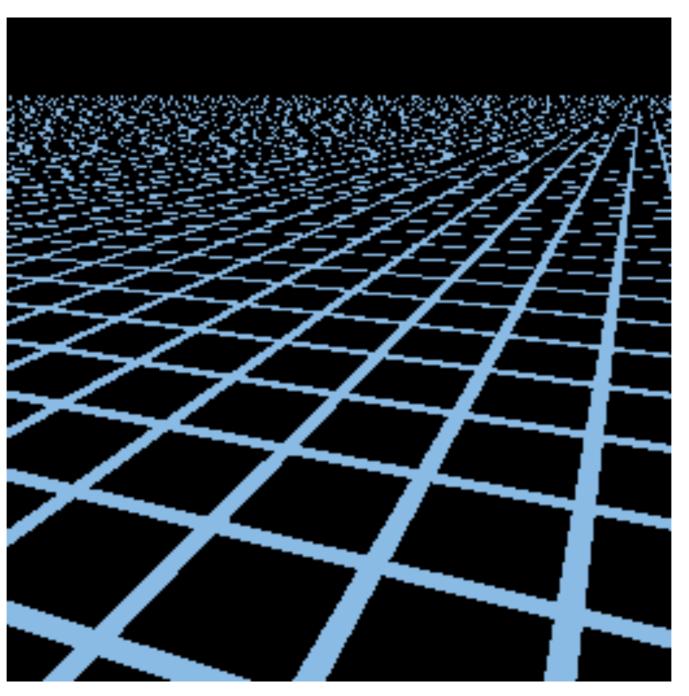
Linear interpolation based on continuous D value

Visualization of Mipmap Level



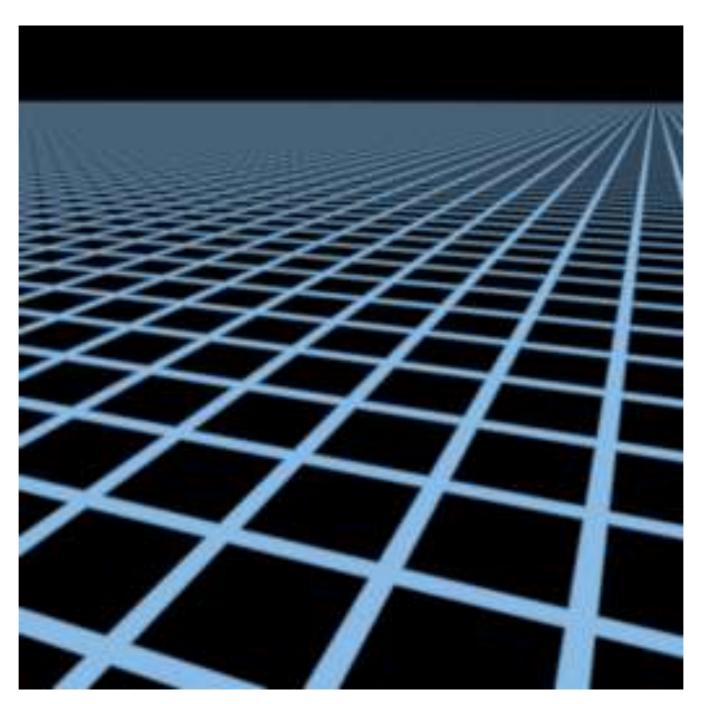
Trilinear filtering: visualization of continuous D

Mipmap Limitations



Point sampling

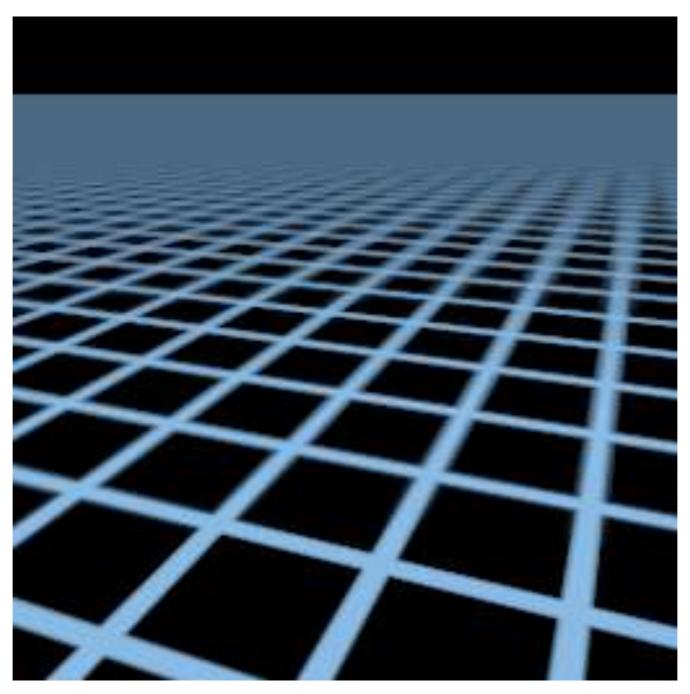
Mipmap Limitations



Supersampling 512x (assume this is correct)

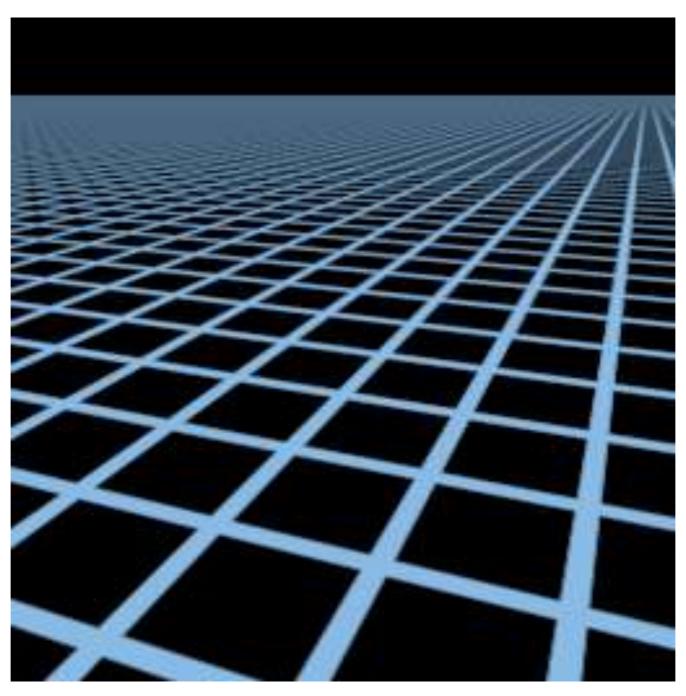
Mipmap Limitations

Overblur Why?



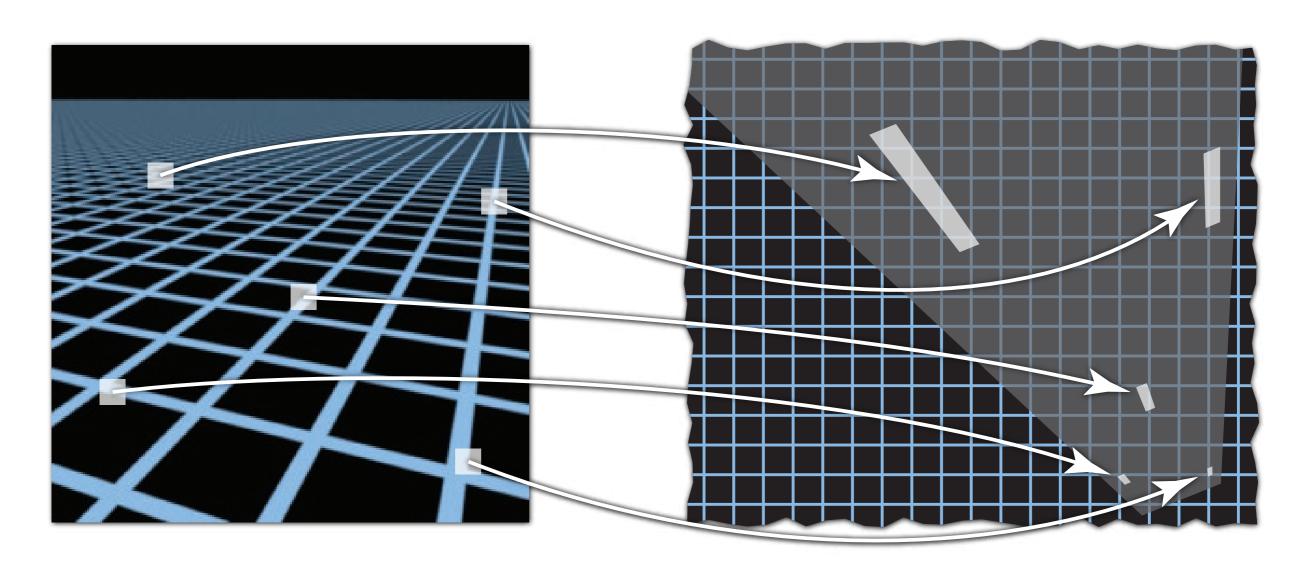
Mipmap trilinear sampling

Anisotropic Filtering



Better than Mipmap!

Irregular Pixel Footprint in Texture



Screen space

Texture space

Anisotropic Filtering

Ripmaps and summed area tables

- Can look up axis-aligned rectangular zones
- Diagonal footprints still a problem



Wikipedia

Anisotropic Filtering

Ripmaps and summed area tables

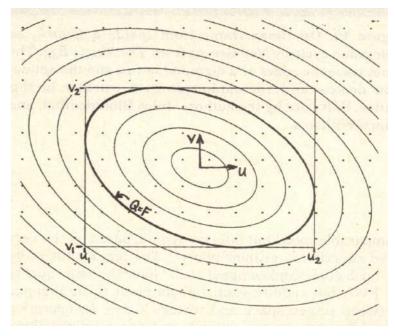
- Can look up axis-aligned rectangular zones
- Diagonal footprints still a problem

EWA filtering

- Use multiple lookups
- Weighted average
- Mipmap hierarchy still helps
- Can handle irregular footprints



Wikipedia



Greene & Heckbert '86

Thank you!

(And thank Prof. Ravi Ramamoorthi and Prof. Ren Ng for many of the slides!)