NCERT Discrete - 10.5.3.20

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Parameter	Value	Description
x(0)	5	First term
r	2	Common ratio
y(n)	315	Sum of terms
x(l)	?	Last term
TABLE 0		

INPUT PARAMETERS

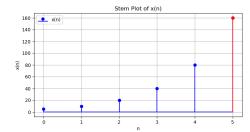


Fig. 0. Stem plot of x(n)

Question: 10.5.3.20 The sum of some terms of G.P. is 315 whose first term and the common ratio are 5 and 2, respectively. Find the last term and the number of terms.

Solution:

Given:

$$x(n) = x(0)r^n u(n) \tag{1}$$

$$X(z) = \frac{x(0)}{1 - rz^{-1}} \tag{2}$$

$$=\frac{5}{1-2z^{-1}}\tag{3}$$

By contour integration:

$$y(n) = x(0) \left(\frac{r^{n+1} - 1}{r - 1} \right) u(n) \tag{4}$$

$$\implies 315 = 5\left(2^{n+1} - 1\right) \tag{5}$$

$$\implies n = 5$$
 (6)

From (1):

$$x(5) = 5\left(2^5\right) \tag{7}$$

$$= 160$$
 (8)

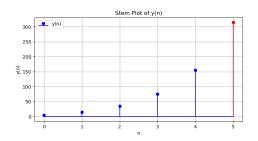


Fig. 0. Stem plot of y(n)