## Discrete Assignment (10.5.3.20)

## Avani Chouhan EE23BTECH11205

## Question:

The sum of some terms of G.P. is 315 whose first term and the common ratio are 5 and 2, respectively. Find the last term and the number of terms.

## Solution:

Given:

$$x(0) = 5 \tag{1}$$

$$r = 2 \tag{2}$$

$$x(n) = x(0)r^n \tag{3}$$

$$x(z) = \frac{x(0)}{1 - rz^{-1}} \tag{4}$$

$$S(z) = X(z)U(z) \tag{5}$$

$$S(z) = \frac{x(0)(\frac{r}{1-rz^{-1}} - \frac{1}{1-z^{-1}})}{r-1}$$
 (6)

By contour integration:

$$s(n) = x(0) \left(\frac{r^{n+1} - 1}{r - 1}\right) u(n) \tag{7}$$

From (7):

$$315 = 5(2^{n+1} - 1) \tag{8}$$

$$63 = 2^{n+1} - 1 \tag{9}$$

$$64 = 2^{n+1} \tag{10}$$

$$n = 5 \tag{11}$$

$$x(n) = x(0) \cdot r^n \tag{12}$$

$$x(5) = 5 \cdot 2^5 \tag{13}$$

$$= 160 \tag{14}$$

Therefore, the number of terms is 6, and the last term is 160.