§8.1 直角坐标下的二重积分

-、填空题(一)

$$\iint\limits_{x^2+y^2\leq a^2} \sqrt{a^2-x^2-y^2}\,\mathrm{d}\sigma = \underbrace{\frac{2}{3}\pi\,a^3}_{x^2+y^2\leq a^2} \cdot \text{ \sharp \sharp \sharp \sharp \sharp $;}$$

2. 已知
$$I_1 = \iint\limits_{x^2+y^2 \le 1} |xy| \mathrm{d}x\mathrm{d}y, I_2 = \iint\limits_{|x|+|y| \le 1} |xy| \mathrm{d}x\mathrm{d}y, I_3 = \iint\limits_{\substack{|x| \le 1 \ |y| \le 1}} |xy| \mathrm{d}x\mathrm{d}y$$
,则 I_1, I_2, I_3 的大小为



3. 设D是三角形闭区域,三顶点分别为(1,0),(1,1),(e,0),比较 $I_1 = \iint_{\Omega} \ln(x+y) d\sigma$ 与

$$I_2 = \iint_D \left(\ln \left(x + y \right) \right)^2 d\sigma \text{ 的大小关系为} \qquad I_1 < I_1$$

4. 改换二次积分
$$\int_0^1 dx \int_0^{\ln x} f(x,y) dy$$
 的积分次序为 $\int_0^1 dy \int_0^y f(x,y) dx$. 5. 改换二次积分 $\int_0^1 dy \int_0^{\sqrt{1-y^2}} f(x,y) dx$ 的积分次序为 $\int_0^1 dx \int_0^{\sqrt{1-x^2}} f(x,y) dy$.

5. 改换二次积分
$$\int_0^1 dy \int_{-\sqrt{1-y^2}}^{\sqrt{1-y^2}} f(x,y) dx$$
 的积分次序为 $\int_{-1}^1 dx \int_0^{\sqrt{1-x^2}} f(x,y) dy$

6. 设
$$D = \{(x,y) | -3 \le x \le 2, 0 \le y \le 1\}$$
, 计算二重积分 $I = \iint_D xy^2 d\sigma = \underline{\qquad 5}$

二、试估计二重积分
$$I = \iint_D \ln\left(1+x^2+y^2\right) \mathrm{d}\sigma$$
 的值,其中 $D = \left\{\left(x,y\right) | 1 \le x^2+y^2 \le 2\right\}$.



三、计算下列二重积分

1.
$$I = \iint_D xyd\sigma$$
, 其中 D 由 $y = x, x = 1$ 及 x 轴所围成.

$$D = \{(x,y) \mid b \in y \in x, c \in x \in Y\}$$

$$I = \{(x,y) \mid b \in y \in x, c \in x \in Y\}$$

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2 .
$$I = \iint_D (x^2 + y^2) d\sigma$$
 , 其中 D 由 $y = x, y = x + 1, y = 1, y = 2$ 围成.

$$D = \{(x,y) \mid y + \leq x \leq y, \quad p \leq y \leq z \}$$

$$I = \int_{1}^{2} dy \int_{y-1}^{y} (x^{2} + y^{2}) dx$$

$$= \int_{1}^{2} \left(\frac{x^{3}}{3} + y^{2} \cdot x \right) \Big|_{y-1}^{y} dy = \left(\frac{1}{3} (y^{3} - y^{2} - y^{3}) \right)^{2} + y^{2} \int_{1}^{2} dy$$

$$= \int_{1}^{2} \frac{1}{3} (2y^{2} - y^{2} + \frac{1}{3}) dy = \left(\frac{1}{3} (y^{3} - y^{2} - \frac{1}{3}) \right)^{2} = \frac{7}{3}$$

3.
$$I = \iint_D \frac{\sin x}{x} dxdy$$
, 其中 D 是直线 $y = x$ 及曲线 $y = x^2$ 所围成. $D = \{(x, y) \mid x^2 \le y \le x \}$ のそれ ミリ



$$V = \{(x,y) \mid x^2 \leq y \leq y \quad o \in x \leq 1\}$$

$$V = \{(x,y) \mid x^2 \leq y \leq y \quad o \in x \leq 1\}$$

$$I = \int_{0}^{1} dx \int_{x^{2}}^{x} \frac{\sin x}{x} dy$$

$$= \int_{0}^{1} \frac{\sin x}{x} \cdot y \Big|_{x^{2}}^{x} dx = \int_{0}^{1} \frac{\sin x}{x} (x - x^{2}) dx$$

$$= \int_{0}^{1} \sin x \cdot y \Big|_{x^{2}}^{x} dx = \int_{0}^{1} \frac{\sin x}{x} (x - x^{2}) dx$$

$$= \int_{0}^{1} \sin x \cdot y \Big|_{x^{2}}^{x} dx = - \cos x \Big|_{0}^{1} + \int_{0}^{1} \pi \cdot (\cos x)^{2} dx$$

$$= - \cos (1 + 1 + x) \cos x \Big|_{0}^{1} - \sin x \Big|_{0}^{1} = 1 - \sin x$$

4 .
$$I=\iint_{\mathbb{R}}x^2\sin y^2\mathrm{d}\sigma$$
 .其中 D 是曲线 $y=x^3$ 和直线 $y=1, x=0$ 所围的位于第一象限的闭区

域.

$$I = \int_{3}^{1} dy \int_{3}^{3/5} x^{2} \sin^{2} dx$$

$$= \int_{3}^{1} \sin^{2} x \cdot \frac{x^{3}}{3} \Big|_{3}^{3/5} dy = \frac{1}{3} \int_{3}^{1} \sin^{2} x \cdot y dy$$

$$= \frac{1}{3} \int_{3}^{1} \sin^{2} x \cdot \frac{x^{3}}{3} \Big|_{3}^{3/5} dy = -\frac{1}{3} \cos^{2} x \cdot \frac{1}{3} - \frac{1}{3} (1 - \cos x)$$

六.计算

1.平面 $\frac{x}{a} + \frac{y}{b} + \frac{z}{c} = 1$ 被三坐标面所割出的有限部分的面积.

$$\delta = (-\frac{c}{a}x - \frac{b}{a}y), \quad \delta_{x} = -\frac{c}{a}, \quad \delta_{y} = -\frac{b}{b}, \quad D_{xy} = \{(x \cdot y)\} \xrightarrow{x} + \frac{y}{b} \leq 1, \quad x \neq 0, \quad y \neq 0\}$$

$$\therefore S = \iint \sqrt{(+\frac{c}{a}x + \frac{b}{b}x)} dx dy$$

$$= \iint \sqrt{(+\frac{c}{a}x + \frac{b}{b}x)} dx dy = \frac{ab}{2}\sqrt{(+\frac{c}{a}x + \frac{c}{b}x)}$$

$$= \frac{1}{2}\sqrt{a^{4}b^{4} + b^{4}c^{4} + c^{4}a^{4}}$$

2.曲面 $x^2+y^2-z+1=0$ 在点P(1,1,1)处的切平面被柱面 $x^2+y^2=1$ 所截下的面积.

$$4\pi \stackrel{?}{=} \stackrel{?}{=} \stackrel{?}{=} \frac{1}{2} = 2(x-1) + 2(y-1)$$
 $\Rightarrow 2 = 2x + 2y - 3$
 $\therefore S = \iint_{x^2 + y^2 \le 1} \sqrt{1 + 2^2 + 2^2} dx dy = 3\pi$

七、求圆锥面 $z = \sqrt{x^2 + y^2}$ 被柱面 $x^2 + y^2 = x$ 所割下部分的曲面面积.

$$\frac{\partial}{\partial x} = \frac{x}{|x^2 + y|^2}$$

$$\frac{\partial}{\partial x} = \frac{x}{|x^2 + y|^2}$$

$$\frac{\partial}{\partial y} = \frac{y}{|x^2 + y|^2}$$

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$$\frac{\partial$$

四、计算下列二次积分

1.
$$I = \int_0^2 dx \int_x^2 e^{-y^2} dy$$
.

必须改为先《再》的积分

$$D = \{(x,y) \mid 0 < x < y, \alpha < y < z\}$$

$$I = \int_{0}^{2} dy \int_{0}^{y} e^{-y^{2}} dx = \int_{0}^{2} e^{-y^{2}} x \Big|_{0}^{y} dy$$

$$= \int_{0}^{2} y e^{-y^{2}} dy = -\frac{1}{2} \int_{0}^{2} e^{-y^{2}} d(-y^{2}) = \frac{1}{2} e^{-y^{2}} \Big|_{0}^{y}$$

$$= \frac{1}{2} (1 - e^{-y})$$

2. $I = \int_{0}^{1} dx \int_{0}^{1} x \sin y^{3} dy$.

$$D_{y} = \{ (x,y) \mid 0 \le x \le y , 0 \le y \le 1 \}$$

$$I = \int_{0}^{1} dy \int_{0}^{y} dx = \int_{0}^{1} \int_{0}^{y} dy = \int_{0}^{1} \int_{0}^{y} y^{2} \cdot \sin y^{3} dy$$

$$= \int_{0}^{1} \int_{0}^{1} \sin y^{3} \cdot \sum_{i=1}^{n} \int_{0}^{y} dy = \int_{0}^{1} \int_{0}^{y} y^{2} \cdot \sin y^{3} dy$$

$$= \int_{0}^{1} \int_{0}^{1} \sin y^{3} \cdot \sum_{i=1}^{n} \int_{0}^{y} dy^{3} = -\int_{0}^{1} \cos y^{3} \Big|_{0}^{1} = \int_{0}^{1} (1 - \cos y)$$

五. 若 f(x,y) 在两坐标轴与直线 x+y=1 所围区域上连续,且

$$x \iint_{\Omega} f(x, y) dx dy = f(x, y) - y , \quad \text{$\Re \iint_{\Omega} f(x, y) dx dy $.}$$

§8.2 二重积分的计算(续)

一填空
$$1. \text{ 化下列二次积分为极坐标形式的二次积分 } \int_0^4 dx \int_0^{\sqrt{4x-x^2}} f\left(x^2+y^2\right) dy = \int_{-\sqrt{8}}^{\frac{\pi}{4}} \int_0^{\sqrt{4x-x^2}} f\left(x^2+y^2\right) dy = \int_0^{\frac{\pi}{4}} \int_0^{\sqrt{4x-x^2}} f\left(x^2+y^2\right) dx = \int_0^{\frac{\pi}{4}} f\left(x^2+y^2\right) dx =$$

 $\iint_{D} \left(\frac{x^{2}}{9} + \frac{y^{2}}{4} \right) d\sigma = \underbrace{\left(\frac{1}{7} + \frac{1}{4} \right) \times \frac{\pi}{4} R^{4}}_{D} = \underbrace{\frac{13}{144} \pi R^{4}}_{D}$

1.
$$I = \iint_{D} \sin \sqrt{x^{2} + y^{2}} d\sigma$$
,其中 $D = \{(x, y) | \pi^{2} \le x^{2} + y^{2} \le 4\pi^{2}\}$.

$$D = \{(\ell, 0) | \pi \le \ell \le 2\pi, \pi \le 0 \le 2\pi\}$$

$$\tilde{L} = \int_{0}^{2\pi} d\theta \int_{\pi}^{2\pi} s d\rho \cdot \rho d\rho$$

$$= -2\pi \int_{\pi}^{2\pi} \rho \cdot (\cos \rho)' d\rho$$

$$= -2\pi \left[(\ell \cos \rho)' d\rho\right] = -2\pi \times 3\pi + 0$$

$$= -6\pi^{2}$$

2 . $I=\iint \ln \left(1+x^2+y^2\right) \mathrm{d}\sigma$,其中是D由圆周 $x^2+y^2=1$ 与坐标轴所围成在第一象限内的

闭区域.



三、计算二次积分 $I = \int_0^1 dx \int_{x^2}^x \frac{1}{\sqrt{x^2 + y^2}} dy$.

$$D = \left\{ (\ell, 0) \middle| \quad \text{osp} \leq \frac{S_{1} = 0}{co^{2} 0}, \quad \text{oso} \leq \frac{T_{1}}{c} \right\}$$

$$I = \int_{0}^{T_{1}} du \int_{0}^{S_{1} = 0} \frac{S_{1} = 0}{co^{2} 0} du$$

$$= \frac{1}{cono} \left[\frac{T_{1}}{c} = \int_{0}^{T_{2}} -1 \right]$$

四、求由曲面 $z = 2x^2 + 4y^2$ 及 $z = 6 - 4x^2 - 2y^2$ 所围成的立体的体积.

$$= \int_{0}^{2\pi} d\theta \int_{0}^{2\pi} 6(1-e^{2}) e^{2} d\theta$$

$$= 2\pi \times 6 \times (\frac{1}{2} - \frac{1}{4}) = 3\pi$$
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五.用适当的方法计算二重积分

1. $\iint_D (x+y) dxdy$, 其中 $D=\{(x,y)|x^2+y^2 \le 2x\}$.

$$I = \iint_{\mathbb{R}} x \, dx \, dy + \iint_{\mathbb{R}} y \, dx \, dy$$

$$= \iint_{\mathbb{R}} x \, dx \, dy + O \left(= \overline{\chi} \cdot A(0) = 0 \text{ in distribution} \right)$$

$$= \iint_{\mathbb{R}} x \, dx \, dy + O \left(= \overline{\chi} \cdot A(0) = 0 \text{ in distribution} \right)$$

$$= \int_{-\frac{\pi}{2}}^{\frac{\pi}{2}} \frac{g}{2} \cos \theta \cdot \cos \theta d\theta = \int_{-\frac{\pi}{2}}^{\frac{\pi}{2}} \cos \theta \cdot \frac{g^{3}}{2} \left[\cos \theta \cdot \frac{g^{3}}{2} \right] \cos \theta d\theta$$

$$= \int_{-\frac{\pi}{2}}^{\frac{\pi}{2}} \frac{g}{2} \cos \theta \cdot \cos \theta d\theta = \frac{g}{3} \cos \theta \cdot \frac{g}{2} \left[\cos \theta \cdot \frac{g}{2} \right]$$

$$= \frac{g}{3} \times 2 \times \frac{3 \times 1}{4 \times 2} \times \frac{\pi}{2} = \pi$$

2.计算二重积分 $\iint_{D} \sqrt{\frac{1-x^2-y^2}{1+x^2+y^2}} d\sigma$, 其中 D 为 $x^2+y^2 \le 1$ 在第一象限部分.

$$[=\int_{0}^{2\pi}d\theta\int_{0}^{1}\sqrt{\frac{1-\theta^{2}}{1+\theta^{2}}}\,\theta\,d\theta=\pi\int_{0}^{1}\sqrt{\frac{1-\theta^{2}}{1+\theta^{2}}}\,d\theta^{2}$$

$$=\frac{e^{\frac{1}{2}}}{\pi}\int_{0}^{1}\sqrt{\frac{1-t}{1+t}}\,dt=\pi\int_{0}^{1}\frac{1-t}{\sqrt{1-t}}\,dt$$

$$=\pi\left(ansint+\sqrt{1-t^{2}}\right)\Big|_{0}^{1}=\pi\left(\frac{\pi}{2}-1\right)$$

3.
$$\iint_{x^2+y^2 \le 1} (|x|+|y|) dxdy = 4 \iint_{x^2+y^2 \le 1} (x+y) dx dy = 8 \iint_{x^2+y^2 \le 1} x dxdy$$

$$= 8 \iint_{x^2} (x+y) dx dy = 8 \iint_{x^2+y^2 \le 1} x dxdy$$

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 $=\frac{32}{3}+57$

§8.3 三重积分

一、填空

2. 设
$$\Omega$$
为 $a \le x \le b, c \le y \le d, l \le z \le m$,则 $\iint_{\Omega} xy^2 z^3 dx dy dz = \frac{1}{2k} (b^2 - c^3) (m^4 - l^4)$

3. 设
$$\Omega$$
 由曲面 $z=2x^2+3y^2$ 及 $z=3-x^2$ 所围成的闭区域, 化三重积分
$$I=\iiint_{\Omega}f(x,y,z)\mathrm{d}x\mathrm{d}y\mathrm{d}z$$
 为三次积分是 $\int_{-\sqrt{1-x^2}}^{1}\mathrm{d}x\int_{-\sqrt{1-x^2}}^{\sqrt{1-x^2}}\int_{2x^2+3y^2}^{(x,y,y)}\mathrm{d}y$

二、设 Ω 是由平面x+y+z=1及三坐标面所围成的区域,计算

$$1. I = \iiint_{\Omega} z dv;$$

1. $I = \iiint_{\Omega} z dv$; $\frac{1}{2} - \frac{1}{2} = \frac{1}{2} (x \cdot y, 1) = = \frac{1}{2} (x$

$$= \int_{3}^{3} \frac{1}{2} (1-2)^{3} d3$$

$$= \frac{1}{2} \int_{3}^{3} (1-2)^{3} d3 - \frac{1}{2} \int_{3}^{3} (1-2)^{3} d3$$

$$= \frac{1}{2} - \frac{1}{8} = \frac{1}{2} \times 1$$

$$= \frac{1}{2} \cdot \frac{1}{8} \cdot \frac{1$$

$$2. I = \iiint_{\Omega} (x+2y+3z) dv .$$

五度、计算 $I = \iiint z\sqrt{x^2+y^2}\,\mathrm{d}x\mathrm{d}y\mathrm{d}z$,其中 Ω 是由 $z = \sqrt{x^2+y^2}$ 与平面 z = 1 所围成的形体.

= (27) do (de) 3. e2 d3 $= \int_{0}^{2\pi} d0 \int_{0}^{1} e^{2} \cdot \frac{3^{2}}{2} \Big|_{0}^{1} d\theta = 2\pi \cdot \frac{1}{2} \int_{0}^{1} (e^{2} - e^{x}) d\theta$ $= \pi \cdot (\frac{1}{3} - \frac{1}{5}) - \frac{2}{5}\pi$

 $_{\sim}$ 四、计算 $I=\iiint z\mathrm{d}x\mathrm{d}y\mathrm{d}z$,其中 Ω 是由上半球面 $z=\sqrt{4-x^2-y^2}$ 及抛物面

 $x^2 + y^2 = 3z$ 所围成的形体. 注一. 大災的注: $L = \int_0^{2\pi} du \int_0^{2\pi} du \int_0^{\pi} e^{2u} du = 2\pi \int_0^{\pi} e^{2u} du$ = 4TT \(\int \left(\frac{1}{2} \right) \right) \right(\frac{1}{2} \right) \right) \right(\frac{1}{2} \right) \right) \right(\frac{1}{2} \right) \right) \frac{1}{2} = \frac{13}{27} 浅=.稻面法

 $I = \int_{0}^{3} dx \int_{0}^{3} \int_{0}^{3} dx dy + \int_{0}^{3} \int_{0}^{3} dx \int_{0}^{3} \int_{0}^{3} dx dy$ = 5/2dx (33.17)+ (,3d1.(4-32).17 = 17),332d}+75,3(4-12)& $= \pi \left[\frac{3}{3} \right]_{3}^{1} + \pi \left[\frac{28^{2} - \frac{3}{2}^{2}}{2} \right]_{3}^{2} = \pi + \pi \left(6 - \frac{15}{4} \right) = \frac{13}{4} \pi$

 ν 鱼、设 Ω : $x^2+y^2+z^2 \le 1$, 计算

1 . $I = \iiint z dx dy dz$;

几美于《Oy面对称,《美子》是奇字数 :. I=0

 $\left(\vec{\mathbf{A}} \quad \vec{\mathbf{I}} = \vec{\mathbf{Z}} \cdot \mathbf{V}(\mathbf{A}) = \mathbf{O} \times \frac{\mathbf{V}(\vec{\mathbf{I}})}{2} = \mathbf{O}\right)$

2 .
$$I = \iiint_{\Omega} z^2 dx dy dz$$
;

3.
$$I = \iiint_{\Omega} \left(\frac{x^2}{a^2} + \frac{y^2}{b^2} + \frac{z^2}{c^2} \right) dxdydz.$$

$$\Rightarrow \sqrt[4]{2} + \sqrt[4$$

1.
$$\iint_{\Omega} z dx dy dz;$$

$$\therefore SSSS dx dy dx = \begin{cases} (x, y, y) & 0 < \beta \leq y, x \leq y \leq 1, \exists ex \leq 1 \end{cases}$$

$$= \begin{cases} (x, y, y) & 0 < \beta \leq y, x \leq y \leq 1, \exists ex \leq 1 \end{cases}$$

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2.
$$\iiint_{\Omega} xz dx dy dz$$
.

$$I = \int_{-1}^{1} x \cdot (\frac{5}{6}) \Big|_{x=0}^{1} dx = \frac{1}{6} \int_{-1}^{1} x (1-x^{6}) dx = 0$$