Report of Assignment – 3

Performance o MAX_CUT Using GRASP

Roll: 1905120

The maximum cut (MAX-CUT) problem

Given an undirected graph, G = (V, U), where V is the set of vertices and U is the set of edges, and weights w_{uv} associated with each edge $(u, v) \in U$, the maximum cut (MAX-CUT) problem consists in finding a nonempty proper subset of vertices $S \subset V$ ($S \neq \emptyset$), such that the weight of the cut (S, \overline{S}) , given by $w(S, \overline{S}) = \sum_{u \in S, v \in S} w_{uv}$, is maximized.

To find MAX_CUT of a graph, I used these 8 algorithms:

Constructive Algorithm:

- Random
- Greedy
- Semi-greedy

Local Search:

- LS:1 with random initialization
- LS:2 with greedy initialization,
- LS:3 with semi-greedy ($\alpha = 0.7$)

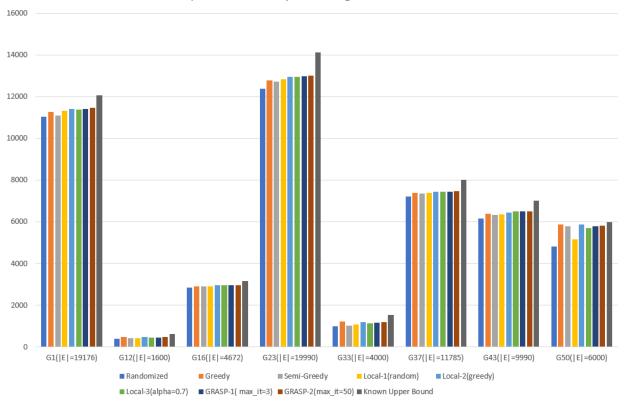
GRASP:

- GRASP-1 with maximum iteration = 3
- GRASP-2 with maximum iteration = 50

Problem		1		Constructive Algori	onstructive Algorithm		Local searc	h	1				GRASP		My Best Value		Upper Bour	ınd
Name		IEI	Randomized			Local-1(random)		Local-2(greedy)		Local-3(alpha=0.7)		GRASP-1(max_it=3)		GRASP-2(max_it=50)		, Door Julius	-ppr Boun	_
· tunie	111				Julii Orceuy		Best Value		Best value		Best value		Best value		Best value			
G1	800	19176	11032	11268	11108		11316	60	11417	82	11382	286	11421			11466	12078	
G2		19176	11091	11292	11203		11344	61	11365		11426		11454		11463		12084	
G3		19176	11049	11295	11229		11316	108	11447	121	11388	281	11418		11469		12077	
G4		19176	10974	11231	11199		11391	69	11400	113	11421	261	11456		11489		12011	
G5		19176	11070	11264	11277		11400	64	11407	138	11426		11378		11468			
G6		19176	1501	1744	1722		1851	121	1910		1924		1951		2009			
G7		19176	1413	1601	1502		1708	83	1797	131	1721	324	1780		1854			
G8		19176	1410	1609	1585		1736	92	1801	158	1787	274	1808		1868			
G9		19176	1471	1631	1515		1783	92	1807	120	1800		1925	5100	1904			
G10		19176	1247	1599	1561	146	1746		1759	123	1809		1785		1841	1841		
G11	800	1600	390	480	428	11	426	6	480	19	470	10	478	392	494	494	627	_
G12	800	1600	406	474	434	10	418	7	494	7	452	21	470	407	482	494	621	
G13	800	1600	434	510	470	17	460	3	508	10	472	19	500	422	506	510	645	
G14	800	4694	2865	2949	2944	42	2921	21	2968	24	2973	70	2973	1210	2988	2988	3187	
G15	800	4661	2842	2915	2918	52	2921	18	2932	15	2944	57	2956	1248	2976	2976	3169	
G16	800	4672	2855	2914	2923	60	2917	29	2955	24	2960	70	2967	1246	2980	2980	3172	
G17	800	4667	2875	2925	2917	46	2933	22	2948	21	2947	63	2948	1263	2972	2972		
G18	800	4694	700	816	744	70	782	51	866	64	840	135	859	2169	911	911		
G19	800	4661	587	724	668	89	778	20	798	48	784	123	789	2073	824	824		
G20	800	4672	628	796	751	64	755	43	797	53	748	117	828	2082	858	858		
G21	800	4667	622	748	716	119	813	40	824	38	766	119	797	2168	849	849		
G22	2000	19990	12460	12810	12784	246	12839	121	12968	89	12911	362	12984	5441	13016	13016	14123	
G23	2000	19990	12396	12790	12729	238	12852	126	12965	132	12958	311	12990	5499	13005	13005	14129	
G24	2000	19990	12290	12820	12719	259	12877	91	12906	108	12882	348	12934	5679	13023	13023	14131	
G25	2000	19990	12311	12773	12768	256	12865	100	12943	143	12980	306	12963	5500	13013	13013		
G26		19990	12332	12772	12698		12801	115	12953	125	12947	339	12959		12990			
G27	2000	19990	2305	2712	2604	309	2782	133	3005	196	2839	447	2921	7323	2944	3005		
G28	2000	19990	2281	2670	2474		2766	106	2861	165	2818		2884		2938	2938		
G29		19990	2314	2734	2614		2928	103	2962	138	2881	475	2994		3045			
G30	2000	19990	2390	2808	2599		2815		2950	171	2974		3007		3037	3037		
G31		19990	2340	2647	2599		2844	103	2759		2812		2898		2982			
G32	2000	4000	1032	1196	1112		1086	16	1218	28	1132		1198		1230		1560	
G33	2000	4000	998	1214	1024		1074	14	1194	32	1128		1182		1202		1537	
G34	2000	4000	998	1176	986		1072		1190	24	1144		1180		1192		1541	
G35		11778	7202	7373	7366		7362	51	7450	69	7466		7463		7476		8000	
G36		11766	7170	7385	7371	131	7351	54	7427	65	7454		7432		7468		7996	
G37		11785	7209	7380	7351	138	7382	63	7454	75	7458		7457		7479		8009	'
G38		11779	7196		7364		7349		7460		7428		7443		7480			'
G39		11778	1705		1832		2038		2147	125	2060		2143		2171			'
G40		11766	1715	2005	1884		1995		2130		2052		2137		2149			
G41		11785	1679		1816		1987	73	2136		2031	293	2080		2143			
G42		11779	1773		1801	208	2067	48	2184	109	2113		2184		2238			_
G43	1000		6170		6347		6361	74	6461	83	6492		6505		6511		7027	
G44	1000	9990	6116		6343		6400		6455		6406		6471		6514		7022	
G45	1000		6196		6359		6410		6446		6464		6483				7020	'
G46	1000	9990	6205	6389	6385		6411		6425	44	6452		6483		6494			
G47	1000	9990	6134	6391	6375		6389		6493		6460		6472		6508		2077	
G48	3000	6000	5004	6000	5816		5096		6000	2	5742				6000	6000	6000	
G49	3000	6000	4952	6000	5810		5148		6000	4	5738		5694		5930		6000	_
G50	3000	6000	4828	5880	5798		5156		5880	5	5716		5788		5856		5988	_
G51	1000	5909	3609	3679	3679		3671	29	3725	26	3712			1568	3748			
G52	1000	5916	3627	3711	3690		3708		3743		3734		3738		3761			
G53	1000	5914	3623	3685	3677		3688	25	3740		3732		3742		3757	3757		
G54	1000	5916	3615	3706	3690	58	3675	20	3733	27	3724	88	3740	1461	3754	3754		'

Figure: The resultant table

Graphs with different number edges and performance of my differnt algorithms on them



Observation:

1. From the table it is clear, that the best solutions among all these algorithms are almost near Upper Bounds.

In fact, 2 cases (G48 and G49) were able to achieve the upper bound.

Name	V	E	My Best Val	ue	Upper Bound		
G48	3000	6000	6000		60	00	
G49	3000	6000	6000		60	00	

- 2. In 46 cases out of 54 cases the best Maximum Cut value among all the algorithms came from **GRASP-2 with maximum iteration=50** which is colorless section in **MY BEST VALUE** column.
- 3. In 8 cases out of 54 cases, are highlighted using red color in the **MY BEST VALUE** column. The best value came from either Greedy or LS-2 with greedy initialization.

The common characteristic between these cases: They have lower edge count than other cases.

4. The most noticeable trend in most cases is the improvement of Maximum Cut value as we go from left side of the table to right side (few except: greedy > semi-greedy and LS-2 > LS-3) of the table.

So, our most efficient algo sequence:

- 1. GRASP-2 with maximum iteration = 50
- 2. GRASP-1 with maximum iteration = 3
- 3. LS-2 with greedy initialization
- 4. LS-3 with semi-greedy ($\alpha = 0.7$)
- 5. LS-1 with random initialization
- 6. Greedy
- 7. Semi-greedy
- 8. Random

Explanation:

This result is predictable as constructive algorithm always gives the best solution in one iteration.

Local search is an improvement over constructive algorithm as it always takes us to local optimum.

GRASP is further improvement of local search as it random initialize and start local search a few times iteratively.

Greedy performs better than Semi-greedy because greedy aims at acquiring the best optimum always where semi-greedy will randomly select from Restricted Candidate list which may not always be the best optimum value.

Conclusion:

GRASP > Local Search > Greedy > Semi-Greedy > Random