

Basic

Multiples of 10, 24

x2	20	X
x3	30	X
x4	40	X
...	50	X
...	...	...
...	120	✓

(Efficient

$$LCM \times \underset{\substack{\uparrow \\ \log(A)}}{gcd} = a \times b$$

$$LCM = \frac{a \times b}{gcd} \quad \checkmark$$

$$N = 5$$

$$N! = 120$$

1 zero

$$\text{Hist} \rightarrow 1028 \times \boxed{2 \times 5} \times 10 \times 10$$

$$1028 \underline{00}$$

$$\uparrow$$

$$\text{2 zeroes}$$

$$N = 100$$

$$\underline{\underline{100!}} =$$

No of 2's and 5's pairs in  $N!$



$$100! = (1 \times 2 \times 3 \times 4 \times \boxed{5} \times 6 \times 7 \times 8 \dots \boxed{10} - \boxed{15} - \boxed{20} - \boxed{25} - \boxed{30} - \boxed{35} \times 45 \times 55 \times 65 \times 75 \times 85 \times 95 \times 100)$$

higher  $\leftarrow$  Multiples of 2 : 50  $\leftarrow \left(\frac{100}{2}\right)$  1-100  
lower  $\leftarrow$  Multiples of 5 : 20  $\leftarrow \left(\frac{100}{5}\right)$  1-100  $\rightarrow$  once  
— of 5x5 : 4  $\leftarrow \left(\frac{100}{25}\right)$

no of zeros = No of ~~few~~ times  
5 is multiplied  
in N!

— of  $\frac{5 \times 5 \times 5}{5}$  :  $\frac{125}{5} = 25$  0  $\leftarrow \left(\frac{100}{125}\right)$

Zeros =  $\left\lfloor \frac{2}{5} \right\rfloor + \left\lfloor \frac{2}{25} \right\rfloor + \left\lfloor \frac{2}{125} \right\rfloor + \dots + 0$

$$1001 = \frac{100}{5} + \frac{100}{25} + \frac{100}{125}$$

$$= 20 + 4 + 0 = 24$$

→ 1000!

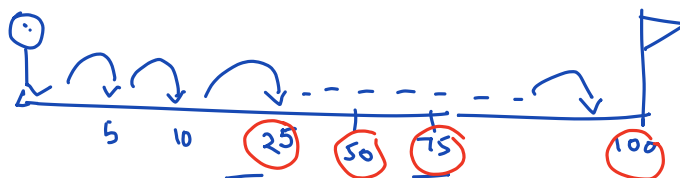
$$= \left( \frac{1000}{5} \right) + \left( \frac{1000}{25} \right) + \left( \frac{1000}{125} \right) + \left( \frac{1000}{625} \right) + \left( \frac{1000}{3125} \right)$$

$$= 20 + 40 + 8 + 1 + 0$$

$$= \boxed{249} \checkmark$$

$$\frac{N}{5^p} = 0$$

↑  
Stop

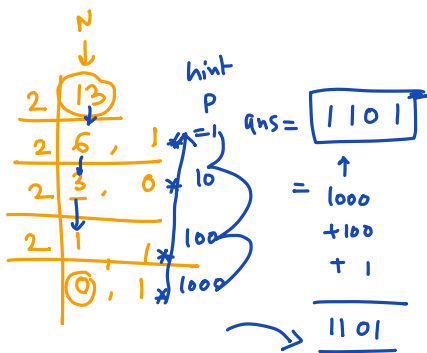


$$\frac{100}{5} = 20 \text{ coins}$$

$$\frac{100}{25} = 4 \text{ coins}$$

## Decimal to Binary

$$5 \rightarrow 101$$



## Binary to Decimal

$$\begin{matrix} 2^2 & 2^1 & 2^0 \\ 1 & 1 & 0 \end{matrix}$$

$$= 4 + 2 + 0$$

$$\rightarrow \boxed{6}$$

$$p = 1 \quad 2 \quad 3 \quad 4$$

$$2^0 \quad 2^1 \quad 2^2 \quad 2^3$$

$$\text{Ans} = 0 + 0 \times 1 + 1 \times 2 + 1 \times 4$$

$$= 0 + 2 + 4 = \boxed{6}$$

$$0 \times 1$$

$$1 \times 2$$

$$1 \times 4$$

$$h = \begin{bmatrix} 1 & 1 & 0 \end{bmatrix}$$

$$h = \begin{bmatrix} 1 & 1 & 0 \end{bmatrix}$$

$$h = \begin{bmatrix} 1 & 1 & 0 \end{bmatrix}$$

$$h \Rightarrow \boxed{0} \text{ Stop}$$

$$\begin{matrix} 2^2 & 2^1 & 2^0 \\ 1 & 1 & 0 \end{matrix}$$

Magic No  $N^{\text{th}}$  Magic  
 ↓  
 Powers of 5

5, 25, 30, 125, 130, 155, ....

Given an integer A, find and return the Ath magic number.

A magic number is defined as a number which can be expressed as a power of 5 or sum of unique powers of 5.

First few magic numbers are 5, 25, 30(5 + 25), 125, 130(125 + 5), ....

Solution

5, 25, 30, 125, 130, 155, ....  
 ↑ ↑ ↑ ↑ ↑ ↑  
 1 2 3 4 5 6 7 ...  
 ...  $N^{\text{th}}$

5, 25, 125, 625

Decimal → Binary No Base 2

1	001	$= 2^0$
2	010	$= 2^1$
3	011	$= 2^0 + 2^1$
4	100	$= 2^2$
5	101	$= 2^2 + 2^0$
6	110	$= 2^2 + 2^1 + 0$
7	111	$= 2^2 + 2^1 + 2^0$

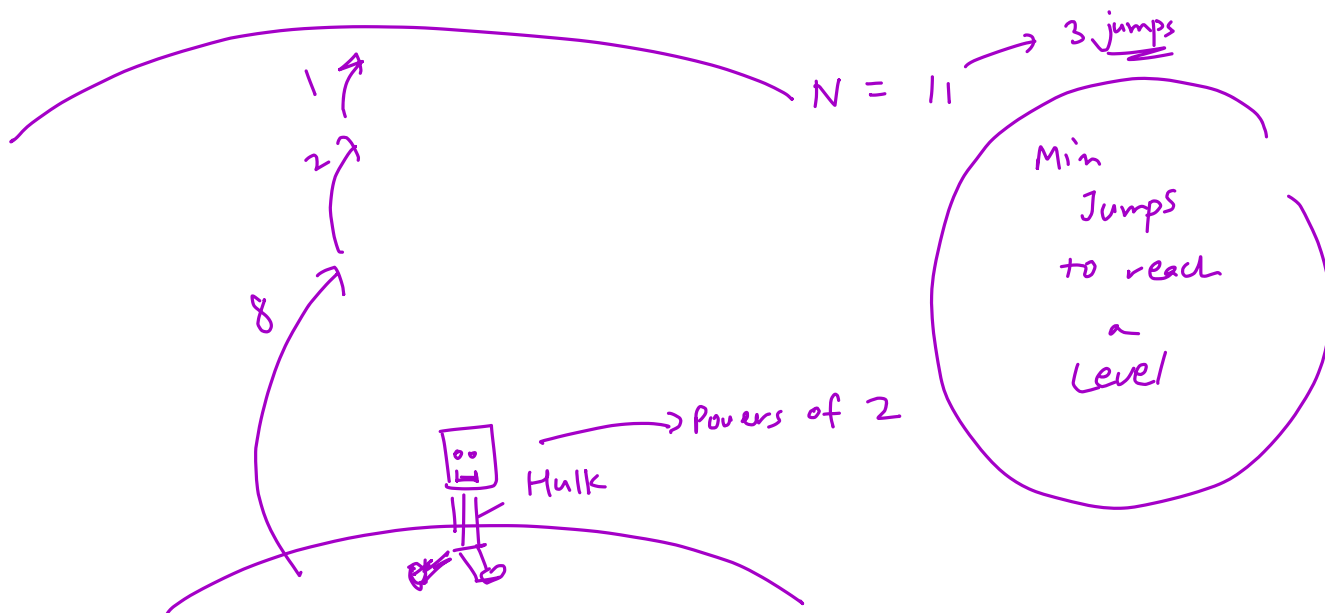
Base 5  $5^i$  min power

→ 001	$= 5^1 = 5$
010	$= 25$
011	$= 30$
100	$= 125$
101	$= 130$
110	$= 150$
111	$= 155$

7

2	7		$P=5$
2	3,	①	$\times 5 \quad P$
2	1,	1	$\times 25 \quad P^2$
	0,	1	$\times 125 \quad P^3$

$= 5 + 25 + 125$   
 $= 155$



11

0 8 10 11

+8 +2 +1

11 =

Min jumps

one's

$1 \quad 0 \quad 1 \quad 1$   
 $2^3 \quad 2^2 \quad 2^1 \quad 2^0$   
 $= 8 + 2 + 1$

# Binomial Coefficient ${}^N C_R$

$$= \frac{N!}{(N-R)! R!} \quad \text{--- (1)}$$

$${}^N C_R = {}^N C_{N-R}$$

$$= \frac{N!}{(N - (N-R))! (N-R)!}$$

$$= \frac{N!}{R! (N-R)!} \quad \text{--- (2)}$$

$${}^5 C_3 = \frac{5!}{2! 3!} = \frac{1 \times 2 \times 3 \times 4 \times 5}{1 \times 2 \times 1 \times 2 \times 3} = 10$$

Shortcut

$$\frac{\text{Num} (5)}{\text{Denom} (1)}$$

$$\frac{5 \times 4 \times 3}{1 \times 2 \times 3} = 10$$

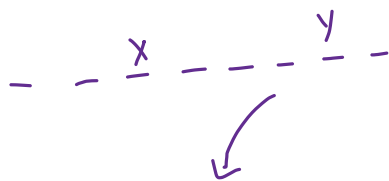
$${}^{11}C_q = \frac{11 \times 10 \times 9 \times 8 \dots}{1 \times 2 \dots 9}$$

$${}^{11}C_{11-9} = {}^{11}C_2 = \frac{11 \times 10}{1 \times 2} = 55$$

## Permutation

Cricket Team 11 ppl

Choose 2 ppl. for post of captain & vice captain

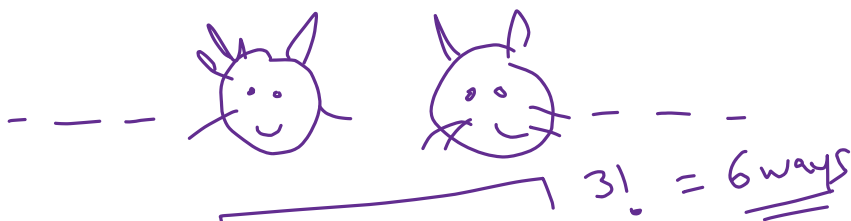


$$\begin{pmatrix} X, Y \\ Y, X \end{pmatrix} \text{ in } {}^{11}C_2 \text{ ways}$$

${}^{11}C_2$  ways choosing \* 2! ways of Arrang'g

$$= {}^{11}C_2 \times 2!$$

$$= {}^{11}P_2$$



A	C	B
A	B	C
C	B	A
C	A	B

$${}^5C_3 \times 3!$$

$$= {}^5P_3$$

B C A  
B A C

$${}^N P_R = {}^N C_R \times R!$$

$$= \frac{N!}{(N-R)!} \times \cancel{R!}$$

$$\boxed{{}^N P_R = \frac{N!}{(N-R)!}}$$

$$\log_{10} 1000 = 3$$

$$\log_2 64 = 6$$

$$\log_b 1 = 0$$

$$\log_{10} 10^{18} = 18$$

