

02/02/22

DSML Intermediate - DSA

Sorting

Today's Content :

1. Intro - Sorting
 2. problem 1 : Min Cost To Remove All Elements
 3. Problem 2: Noble Integer 1 & 2
 4. Problem 3: Minimum Difference
 5. Comparator - What, How, Where?
 6. Problem 4: Largest Number
-

Sorting = Arranging data in an orderly manner

↙ ↓ based on

asc. desc. some
② parameter

✓ $L_1 = [5, 8, 12, 14, 16, 17]$

Based on values in asc. order!

$L_2 = [14, 11, 5, 3, 1]$

Based on values in desc. order!

$L_3 = [0, 0, -1, \underline{-1}, 1, 1, 1] \Rightarrow [0, 0, 1, 1, 1, 1]$

Based on abs(vcl) in asc. order.

$L_4 = [1, 5, 3, 9, 6, 10, 12]$

↓ ↓ ↓ ↓ ↓ ↓ ↓

parameter = # factors.

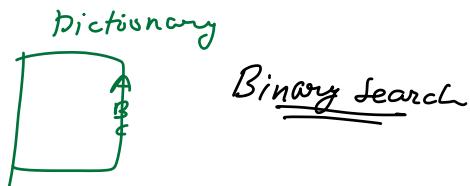
$\xrightarrow{1, 2, 3, 4, 6, 12}$

$\xrightarrow{[1, 2, 2, 3, 4, 4, 6]}$

L_4 is sorted based on # factors in asc. order.

(Q) Why need sorting?

- easy access for data.
- reduce access time.



Python

Focus on Applications
of Sorting.

3 sessions in Adv
Batch.

① $l = [2, 1, 4, 5, 7, 3]$

* $l.sort()$ → input list l itself is sorted.
In-place sorting

$l \rightarrow [1, 2, 3, 4, 5, 7]$

* $l.sort(reverse=True)$

$l \rightarrow [7, 5, 4, 3, 2, 1]$

$l.sort(key=factors)$

def factors

return cnt.

② $l = [2, 1, 3, 4]$

$l_2 = \underline{\text{sorted}}(l)$ # return a sorted $l_2 = \text{sorted}(l, reverse=True)$

$l_2 \rightarrow [1, 2, 3, 4]$

$l \rightarrow [2, 1, 3, 4]$ has not changed

T.C. = $O(N \log N)$

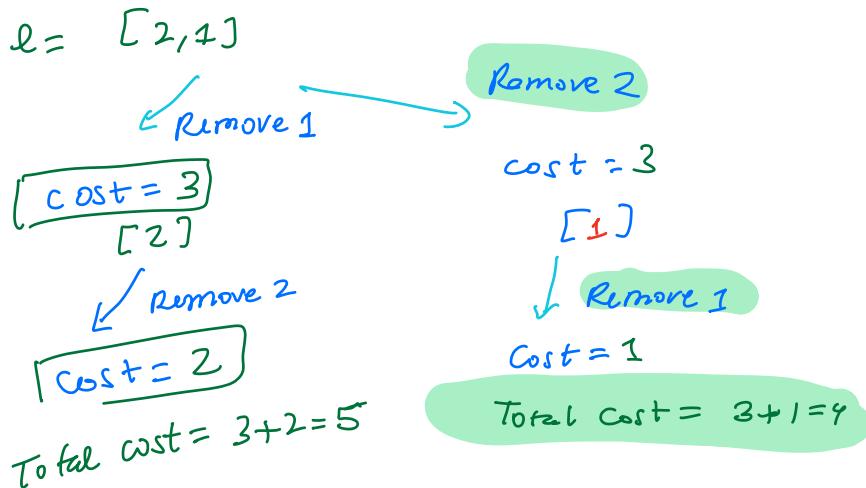
Q1 Amazon, DE Shaw

Given list of size N ,

→ At every step remove 1 element.

Cost of removing = sum of all elements present till now
(include element being deleted)

Find the min cost to remove all elts one by one.



Ex 2 $[4, 6, 1]$

$[4, 6, 1] \quad \textcircled{6} : 6+4+1 = 11$

$[4, 1] \quad 4 : 4+1 = 5$

$[1] \quad 1 : 1$

$\underline{11+5+1=17}$

* Observation(1):
Total Cost depends on
order of operations.

* (2):
Element never
contributes after its
is deleted.

$$a_1, a_2, a_3, a_4$$

$$\text{Delete } a_4 : \quad a_1 + a_2 + a_3 + \underline{a_4}$$

$$a_3 : \quad a_1 + a_2 + a_3$$

$$a_2 : \quad a_1 + a_2$$

$$a_1 : \quad a_1$$

Minimize this
total cost

$$\text{Total cost} = 4*a_1 + 3*a_2 + 2*a_3 + \underline{a_4}$$

4th max 3rd max 2nd max 1st max
 1st min

$$[2, 4, 1]$$

$$\text{Remove } 4 : \quad 4 + 2 + 1$$

$$2 : \quad 2 + 1$$

$$1 : \quad 1$$

$$[4, 2, 1]$$

4 2 1
 1 2 3

$$4 + 2*2 + 3*1$$

$$= 4 + 4 + 3 = \underline{\underline{11}}$$

[4, 2, 2]

$$4*1 + \underline{2*2} + \underline{3*2}$$

$$= 4 + 4 + 6$$

$$= \boxed{14}$$

Idea

$O(N \log N) \leftarrow$ ① Sort array in desc. order

\leftarrow ② Compute the min cost

$O(N)$

$a_1, a_2, a_3, \dots, a_n$

$* \quad * \quad * \quad \dots \quad *$

1

2

3

\dots

n

$$\text{res} = \boxed{\sum_{i=1}^n (a_i) * i}$$

$$\text{T.C. } O(N + N \log N)$$

$$= O(N \log N)$$

$$\text{S.C. } O(1)$$

Q2. Google

Given N array elements / list ' l '

Return cnt of
noble integers
in l .

$l[i]$ is noble if:

$$(\text{Count of elements} < \underline{\underline{l[i]}}) = \underline{\underline{l[i]}}$$

NOTE: All the elements are distinct.

$$l = \begin{bmatrix} 0 & 1 & 2 \\ -10, \underline{\underline{1}}, 3 \end{bmatrix} \quad \text{ans} = 2$$

$\downarrow \quad \downarrow \quad \downarrow$

smaller than $\underline{\underline{l[i]}}$:

0 1 2

$$l = [3, 5, \underline{\underline{0}}, 1] \quad \text{ans} = 2$$

$\downarrow \quad \downarrow \quad \downarrow \quad \downarrow$

smaller than $\underline{\underline{l[i]}}$

2 3 0 1

Brute Force

For every elt
check if noble or not.

↓

1. sort() Ascending order.

$\leftarrow < 5$

$$l = [0, 1, 3, \underline{\underline{5}}]$$

Tc. $O(N^2)$

$$\begin{matrix} 0 & \underline{\underline{1}} & 2 & 3 \\ 0, 1, 3, 5 \end{matrix}$$

No duplicates

① Sort in asc. order $\Rightarrow O(N \log N)$

② count = 0

③ for i in range(0, N):
 if $A[i] == i$:
 count += 1

$O(N)$

④ return count

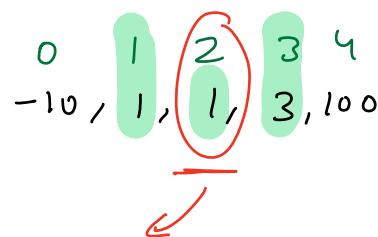
Tc : $O(N \log N)$

$$A = [-10, -5, 1, 3, 5, 6, 10]$$

$$[-10, -5, 1, 3, 4, 5, 6]$$

Ans = 3

Q2 ii) With duplicates



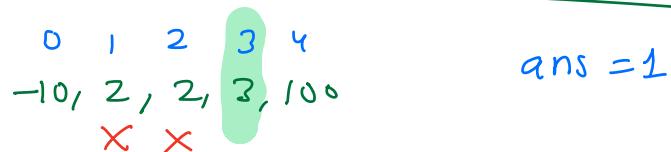
TC: $O(N \log N)$
SC: $O(1)$
ans = 3

$$\text{cnt of elements} < 1 = 1$$

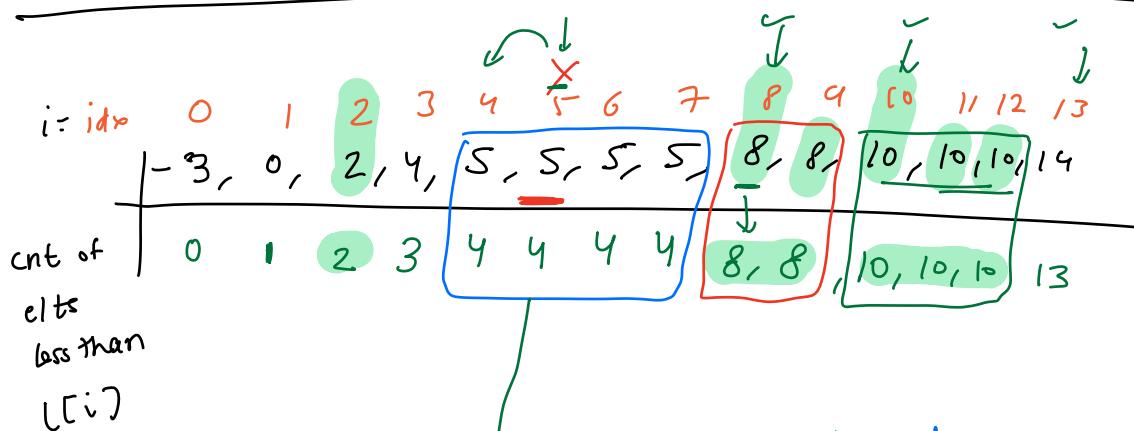
$$\text{cnt of elements} < 3 = 3$$

\downarrow
 $[-10, 1, 1]$

Think
2 mins



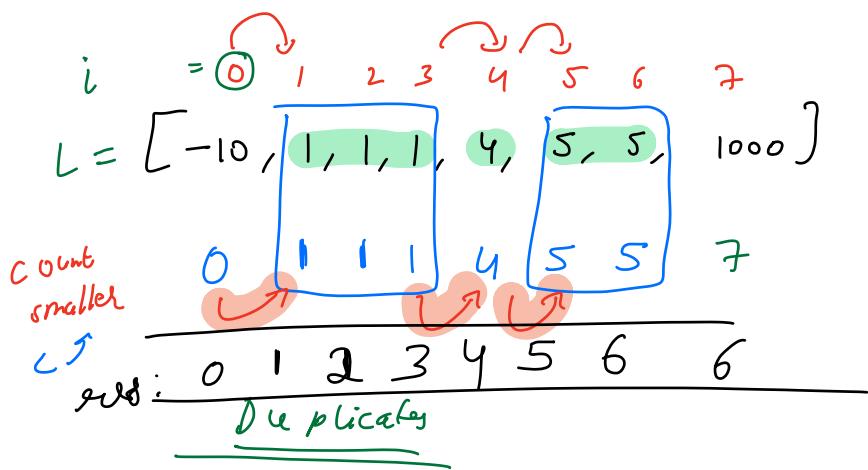
ans = 1



Observation: For duplicate elements,
Count of smaller elts. is same.

$i = c[i]$

$c[i] = c[i-1]$ (There are some duplicate before it)



\Rightarrow ① Sort in asc. order $\Rightarrow O(N \log N)$

② $res = 0$ if ($arr[0] == 0$): $res = 1$
 $c = 0$

③ for i in range(1, N):

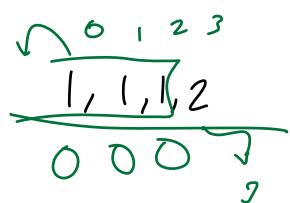
if $l[i] != l[i-1]$: # non-duplicate

$c = i$

if $c == l[i]$:

$res += 1$

④ return res



Time = $O(N \log N)$

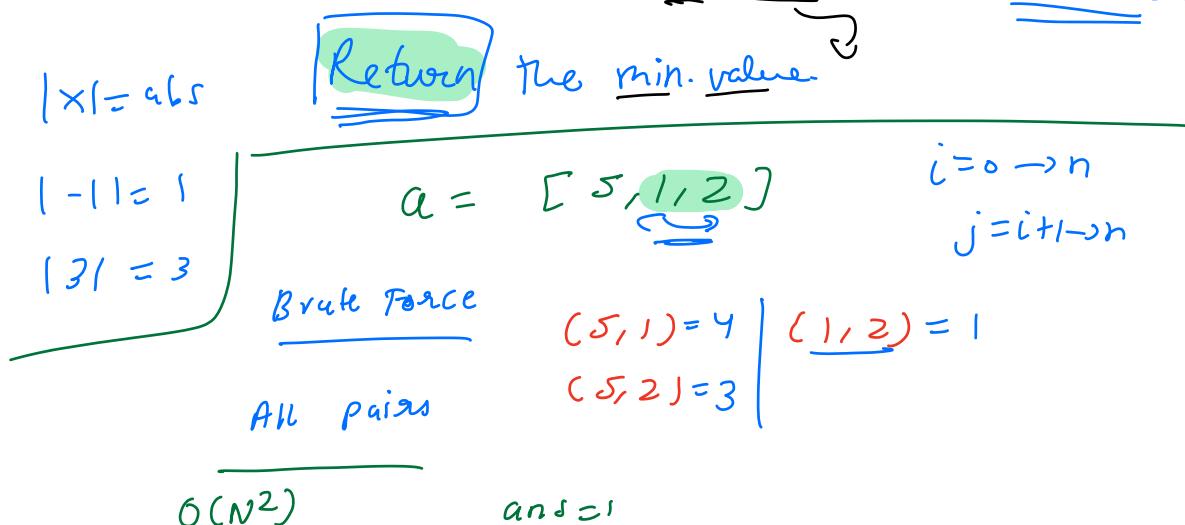
Space = $O(1)$

Q4. Minimize Difference

NOTE: $i \neq j$

Given N array elements, find the pair of indices

(i, j) such that $|l[i] - l[j]|$ is minimized.



Ex 2 $[9, 14, 21, 7, -3, 4, 26, 10]$

$\text{ans} = 1$.

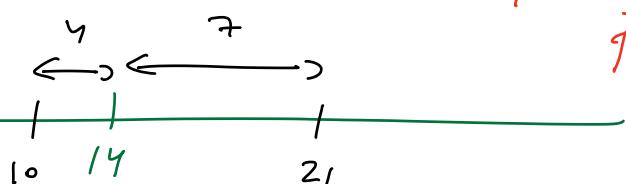
$$|9 - 10| = 1 - 1 = 1$$

Observation:

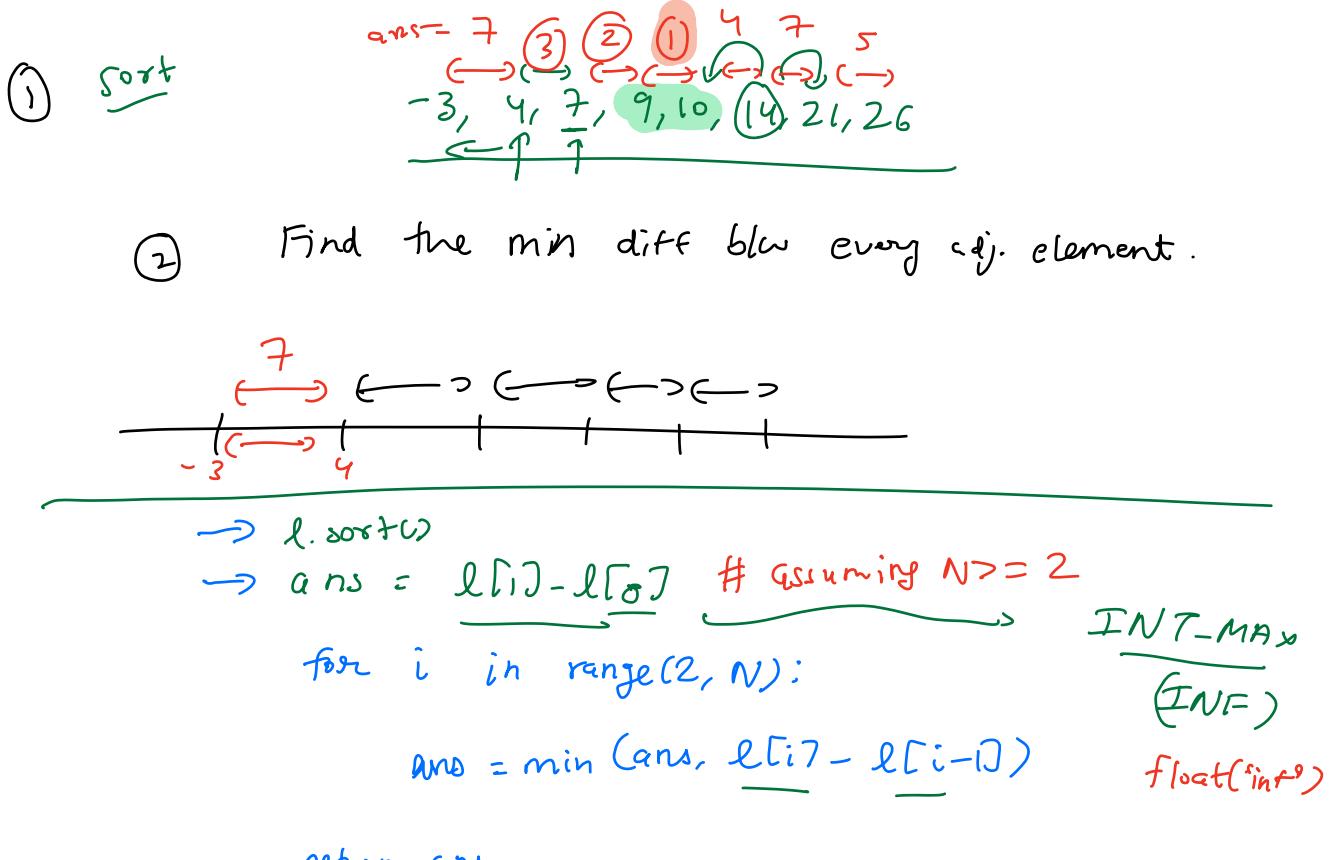
⑨ $14, 21, 7, -3, 4, 26, 10$

Fix one element
→ Closest left
→ Closest right

$10/2$
 $|14 - 10|$



Either of 2 will give me smallest diff



Q5:

* Largest Number gt0

(the numbers)

Given an array of numbers, arrange the numbers such that they form the largest num.

$$l = [2, 3, 7, 0]$$

$$\left(\Rightarrow \begin{array}{c} \boxed{9320} \\ \uparrow \\ [9, 3, 2, 0] \end{array} \right)$$

1) Sort in decr. order

2) Join the numbers

Eg 2. $l = [3, 30, 34, 5, 9]$

$l.sort(\text{reverse=True})$

$[34, 30, 9, 5, 3]$

$3430953 \times$

$\frac{4 \ 3 \ 2 \ , \ 0 \ , \ 1}{9, \ 5, \ 34, \ 3, \ 30}$

Input:
 $\frac{6}{3, \ 34}$

$\frac{3 \ 34}{34 \ 3}$

✓ Comparator \Rightarrow allows to sort based on custom parameter

$$l = [1, 2, 4, 10, 5, 6, 3]$$

1, 2, 3, 4, 2, 4, 2

Given

$\Rightarrow l.sort(key = \underline{\text{factors}})$

def factors:

return cnt

(1) Order parameter $l = [1, 2, 5, 3, 4, 10, 6] \Rightarrow [1, 2, 3, 5, 4, 6, 10]$

(2) factors ↓ ↓ ↓ ↓ ↓ ↓ ↓
 1 2 2 2 3 4 5

\Rightarrow If 2 elements have same cnt factors
 smaller elt should come before

Remember

def myCmp(x, y): \rightarrow return True | -1
 when $x < y$

$c_1 = \text{factors}(x)$

$c_2 = \text{factors}(y)$

$x < y \leftarrow \text{if } (c_1 < c_2):$
 return -1}

return False | 1
 when $x > y$

$y < x \leftarrow \text{if } (c_2 < c_1):$
 return 1}

$= y < x$

if $x < y$

0 ($x = y$)

return -1

1st num comes
 before 2nd

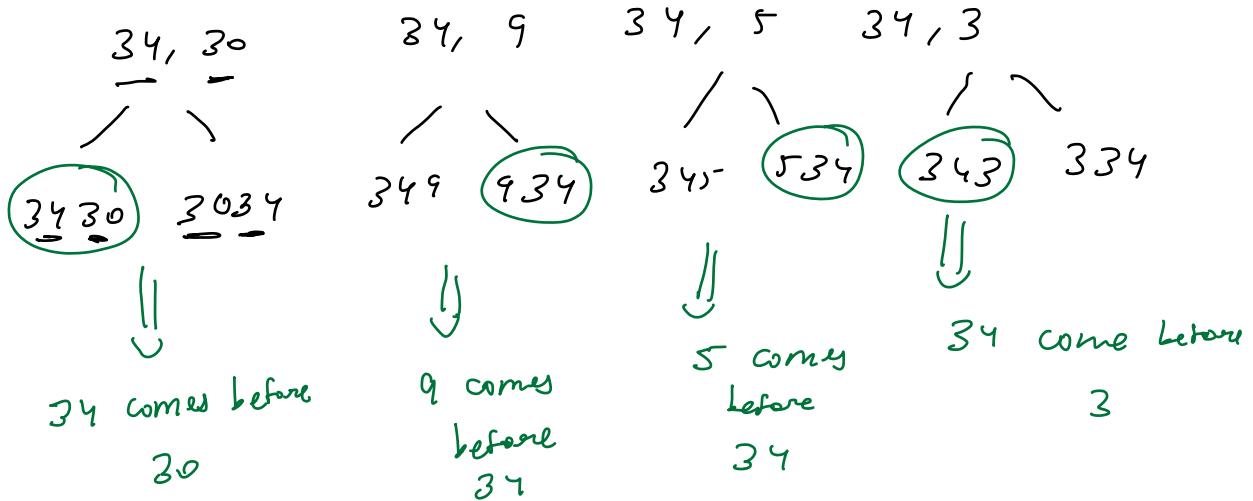
if $y < x$

1st num after 2nd num.

return 1

return 0

$[\underline{34}, 30, 9, 5, 3]$



def myCmp (x, y): # x & y are strings.

$3, 3$ \downarrow $33 \quad 33.$	if $x+y > y+x$: # $xy > yx$ return -1
	if $y+x > x+y$: # <u>$yx > xy$</u> return 1
	return 0

$l = [3, 30, 34, 5, \underline{9}] \Rightarrow O(\underline{\underline{N \log N}})$

$\Rightarrow l.sort(key = \underline{\underline{\text{myCmp}}})$

$[9, 5, 34, 3, 30] \Rightarrow$

Code

$l = [2, 1, 3, 4, 5, 6]$

$l.sort()$

$\rightarrow O(N \log N)$

$[1, 2, 3, 4, 5, 6]$

Merge sort

Quick sort

By default

```
def comp(x, y):  
    if x < y:  
        return -1  
    if x > y:  
        return 1  
    return 0
```