

Assignment 3

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1 The Skyline Problem:

1. Rectangular Buildings

- a. The series of buildings is generated randomly (format: left, height, right)
- b. They are arranged using Quicksort ($O(n \log n)$)
- c. A structure called Skyline is used here which is basically a linked list with two data points (left, height), in each node.
- d. Now the sorted building array is divided into left and right parts until the size is 1 (divide)
- e. The base case is when there is only one building, in this case the skyline data structure to be returned will have only two nodes: (left, height)–;(right, 0)
- f. The left and right lists(skylines) are now merged recursively on the basis of their x coordinates (left) in increasing order .(conquer).
- g. In this merge function two things are kept in mind: If the incoming node has the same x coordinate as the previous, but has a different height, the bigger height is taken. And if the incoming node has same height but a different x coordinate, it is dropped, as it is redundant (building overlapped by another).
- h. Thus the above algorithm is a simple merge sort type algorithm which has $O(n \log n)$ complexity.

2. Slant Buildings

This problem is largely similar to the previous one.

- a. Buildings are represented by (left, left height, right, right height) format.
- b. They are arranged using Quicksort ($O(n \log n)$)
- c. A structure called Skyline is used here which is basically a linked list with two data points (left, height), in each node.
- d. Now the sorted building array is divided into left and right parts until the size is **2** (divide).
- e. This is because for two overlapping buildings, there will now be a third point to be taken into consideration, which is basically the point of intersection of the two roof lines of the two buildings.
- f. 5 points are returned in base case. (2 for left, 2 for right and 1 intersection if valid).

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