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#### 1) Dijkstra's Algorithm - Single Source Shortest Path

- i. In every iteration find the min node. Which has time complexity of  $n$ .

$$T.C = O(n^2)$$

$$S.C = O(n)$$

- ii. Below we are using min heap so it only takes  $\log n$  time.

```
class Pair implements Comparator<Pair>{
    int node;
    int dist;
    Pair(int n, int d){
        node = n;
        dist = d;
    }
    Pair(){
    }
    public int compare(Pair o1,Pair o2){
        if(o1.dist<o2.dist)
            return -1;
        else if(o1.dist>o2.dist)
            return 1;

        return 0;
    }
}
class Solution
{
    static int[] dijkstra(int v, ArrayList<ArrayList<ArrayList<Integer>>> adj, int s)
    {
        PriorityQueue<Pair> pq = new PriorityQueue<Pair>(v, new Pair());
        int distance[] = new int[v];
        Arrays.fill(distance,Integer.MAX_VALUE);
        distance[s] = 0;
        pq.add(new Pair(s,0));

        while(!pq.isEmpty()){
            Pair cur = pq.poll();
            int n = cur.node;
            int d = cur.dist;
```

```

        for(ArrayList<Integer> it:adj.get(n)){
            int adjNode = it.get(0);
            int weight = it.get(1);
            if(distance[n]+weight<distance[adjNode]){
                distance[adjNode] = distance[n]+weight;
                pq.add(new Pair(adjNode, distance[adjNode]));
            }
        }
    }
}

return distance;
}

```

**T.C =  $O(n \log n)$**

**S.C =  $O(n)$**

## 2) Prims Algorithm - Minimum Spanning Tree

```

class Node{
    int node;
    int weight;
    Node(int n, int w){
        node = n;
        weight = w;
    }
}

class Solution
{
    static int spanningTree(int v, ArrayList<ArrayList<ArrayList<Integer>>> adj)
    {
        int distance[] = new int[v];
        boolean inMST[] = new boolean[v];
        Arrays.fill(distance,Integer.MAX_VALUE);
        PriorityQueue<Node> pq = new PriorityQueue<>((o1,o2)-> o1.weight-o2.weight);
        pq.add(new Node(0,0));
        distance[0] = 0;

        while(!pq.isEmpty()){
            Node cur = pq.poll();
            int u = cur.node;
            inMST[u] = true;

            for(ArrayList<Integer> it : adj.get(u)){
                int adjNode = it.get(0);
                int weight = it.get(1);
                if(!inMST[adjNode] && distance[adjNode]>weight){
                    distance[adjNode] = weight;
                    pq.add(new Node(adjNode, weight));
                }
            }
        }
    }
}

```

```
}  
int ans = 0;  
for(int i=0;i<v;i++)  
    ans+=distance[i];  
  
return ans;  
}
```

**T.C =  $O(n \log n)$**

**S.C =  $O(n)$**