

20.14. TIME COMPLEXITY CALCULATION FOR LOOP (BASED ON FOR LOOP EXPRESSION).

EXPLANATION:

for(initialization; condition ; increment){}

*And we know for initialization it can take more than 1 variable ,
increment also more than 1 but condition will remain same.*

for(i = 1, j = 1, s = 1 ... n no. of variables = 1;

i ≤ n && j ≤ n || s ≥ n ...;

i ++; j ++; s ++; ... n no. of variable ++)

{...}

*Hence in initialization we can take n no. of variables
seperated by , (comma).*

.

EXAMPLE 1

```
for(i = 1; j = 2; i ≤ n && j ≤ n ; i ++, j ++){  
    k = k + 1;  
}
```

SOLUTION

The above will take upper bound as 2 and because of Anding and will print $k = k + 1$, $n - 2$ times. $O(n - 2) = O(n)$.

EXAMPLE 2

```
for(i = 1; j = 2; i ≤ n || j ≤ n ; i ++, j ++){  
    k = k + 1;  
}
```

SOLUTION

j will run from 2 to $n + 2$ times and i run from 1 to n times because of ORing and $k = k + 1$ will get printed 1 to n times i. e.

$$\sum_{i=1}^n 1 = (1 + 1 + 1 \dots n \text{ times}) = n, \text{ hence } O(n)$$

EXAMPLE 3

```
for(i = n; j = n + 1; i ≥ 1 && j ≥ 1; i--, j--) {
    k = k + 1;
}
```

SOLUTION

Here n will be considered as upper bound and loop will execute from 1 to n

$\Rightarrow k = k + 1$ will be printed :

$$\sum_{i=1}^n 1 = (1 + 1 + \dots n \text{ times}) = O(n)$$

EXAMPLE 4

```
for( $i = n; j = n + 1; i \geq 1 || j \geq 1; i--, j--$ ){  
   $k = k + 1;$   
}
```

SOLUTION

Here $n + 1$ will be considered as upper bound and loop will execute from 1 to $n + 1$

$\Rightarrow k = k + 1$ will be printed :

$$\sum_{i=1}^{n+1} 1 = (1 + 1 + \cdots (n + 1) \text{ times}) = O(n + 1) = O(n)$$