Space Complexity of Array VS Space Complexity of Stack

Now after learning the working of space complexity that why Push of Space Complexity takes n times and insertion of Array takes O(1).

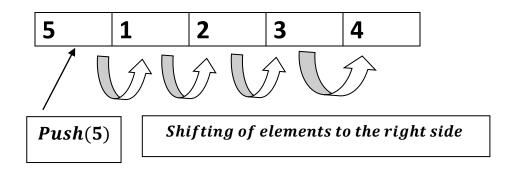
The reason is:

Push operation inserts elements at the begining of stack which shifts the rest of the element to the right.

Suppose we have stack:

1	2	3	4

Now we push 5 in stack:

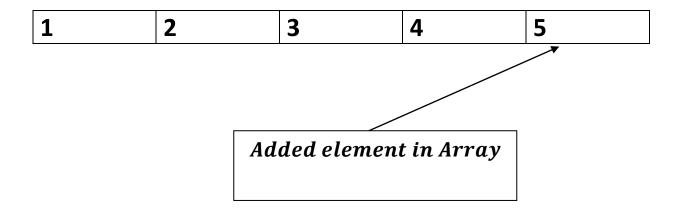


Hence, the whole operation takes O(n) space complexity.

Where as inserting elements in array works like:

Such as we have an array of size 4 i.e.a[4]

Now we want to insert an element 5



That is just expanding the auxiliary space and insert element at the end of the array with no shifting activity.

Similary, if we talk of inserting an element in Array at a position:

Here just we are swapping the elements from one index to another index:

Suppose size = 5.

Now, size = size + 1 = 6

such as:

$$a[5] = a[4] = 4$$

$$a[4] = a[3] = 3$$

$$a[3] = a[2] = 2$$

$$a[2] = a[1] = 1$$

And now we insert a[0] = 5

Though we are replacing or overriding elements from one position to another and just inserting at a given position.

Where as in push operation of a stack there is

no overdding or swapping of elements rather shifting of elements to the right and adding elements to the top creating a new data structure.

Where as in array no new data structure is created.

When Stack Is Implemented Through Array

As we can implement stack through array inserting element at top or begining will able to shift other element by 1 to the right side.

Hence Push operation takes O(n) space complexity.