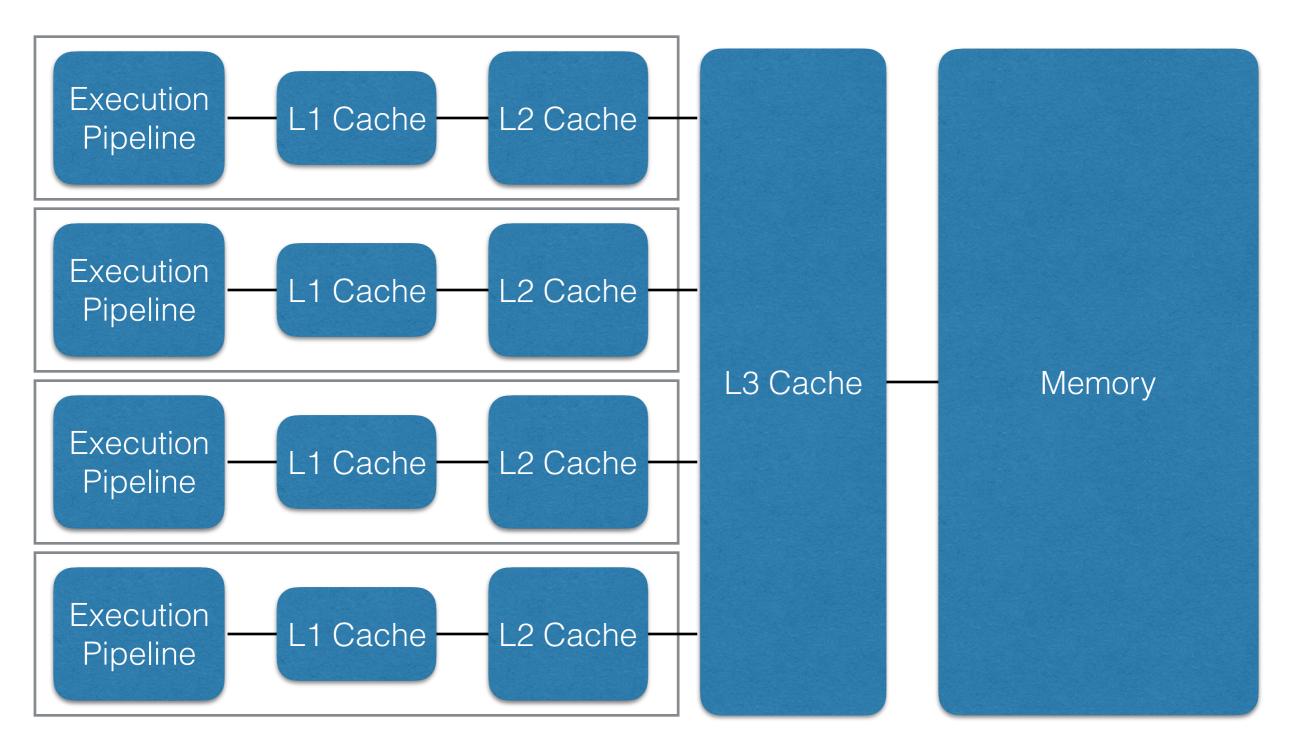
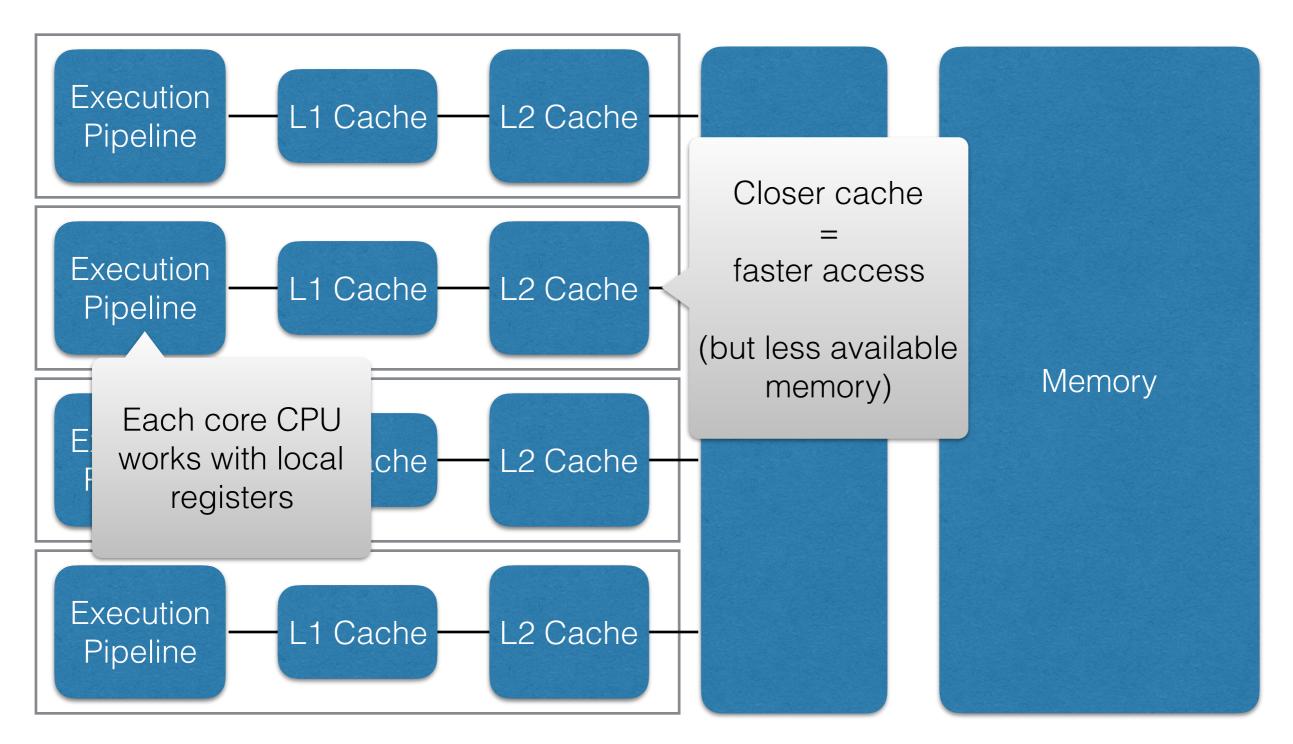
# Lecture #08 Performance Considerations

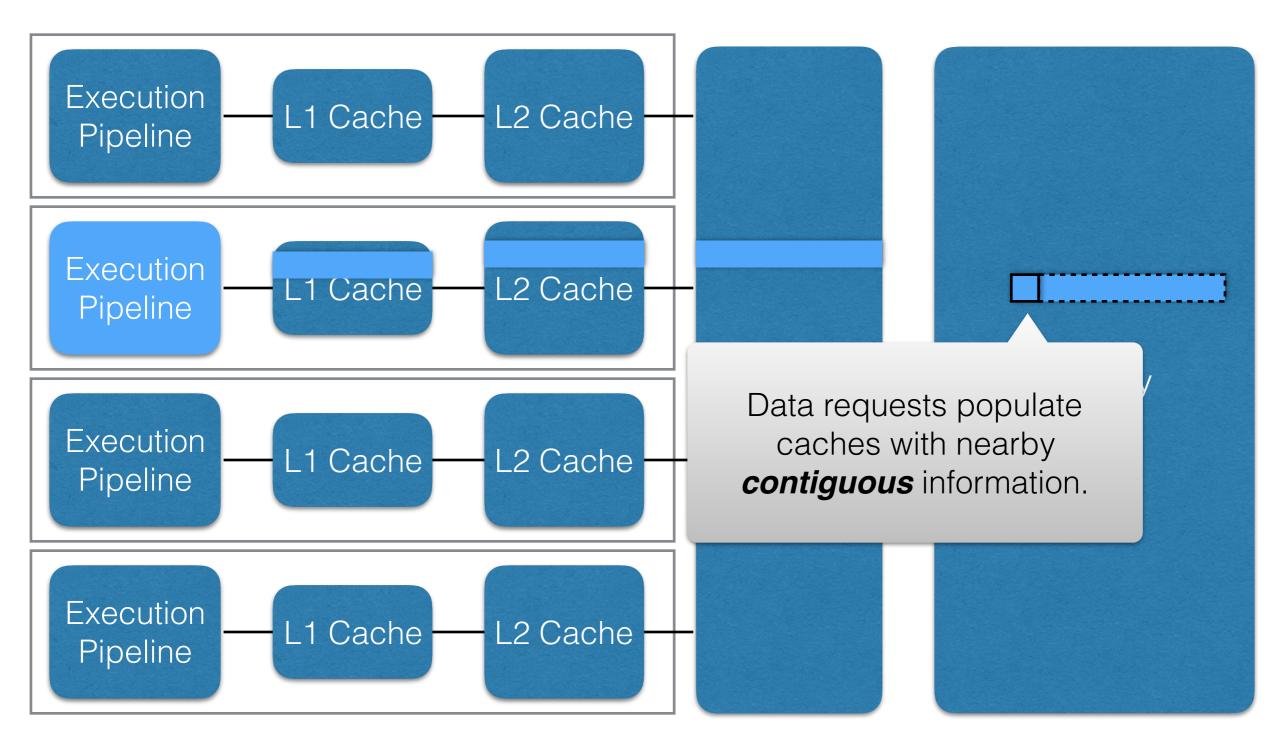
AMath 483/583

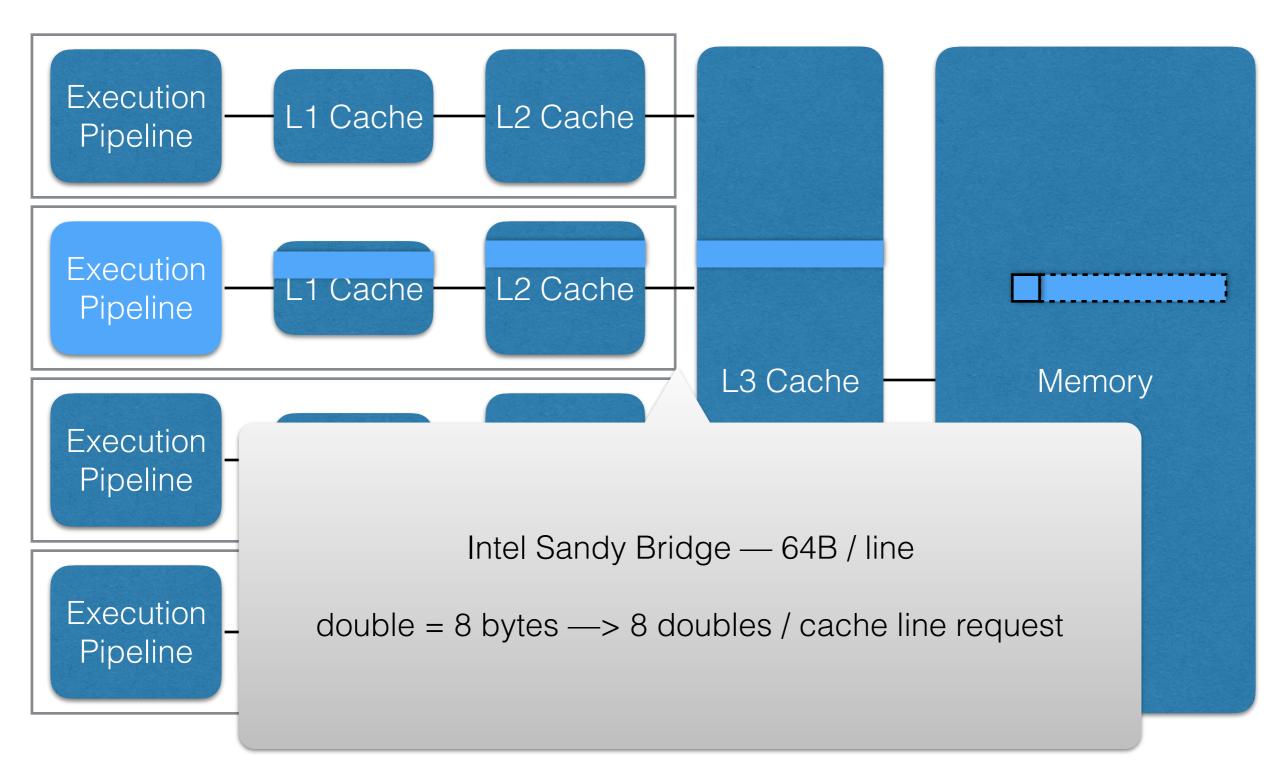
#### Announcements

- Primary references online
- Next week: parallelization





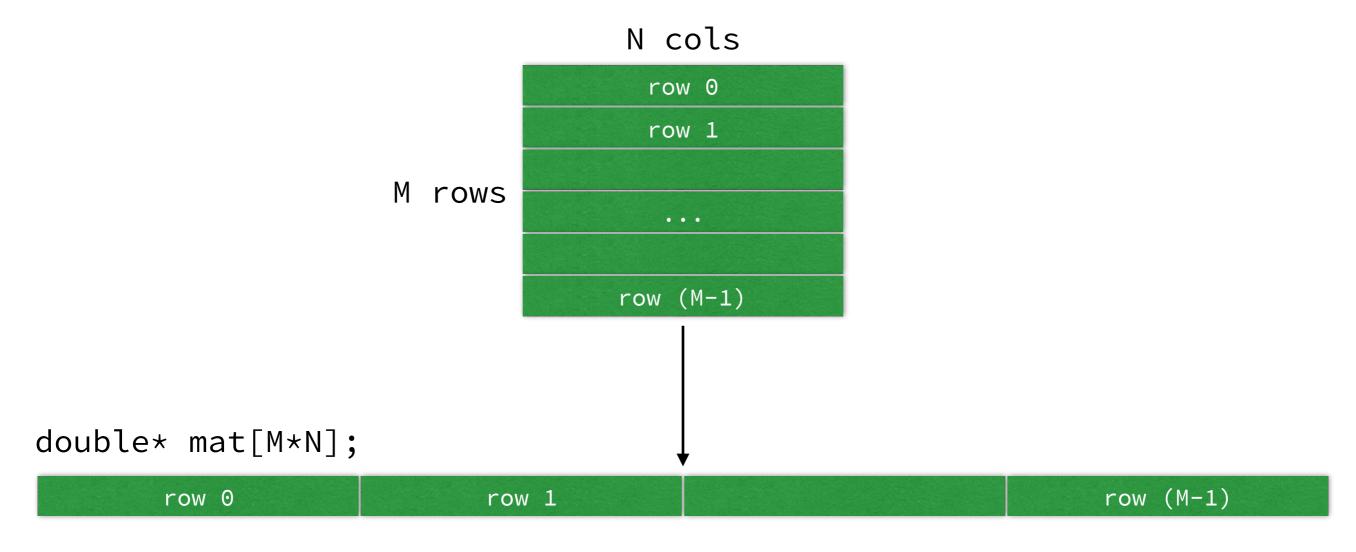




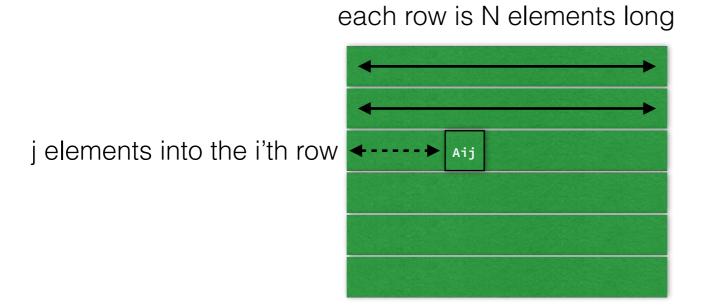
## Main Takeaway

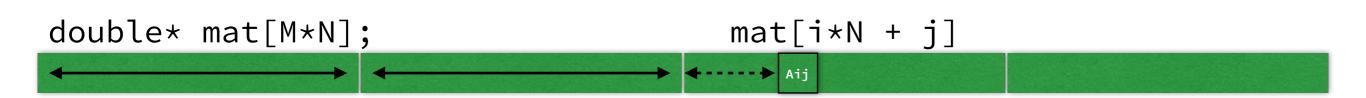
Data contiguity is essential to fast code

Matrices typically stored in single array: (row-ordered)



How do you access the (i,j) element?

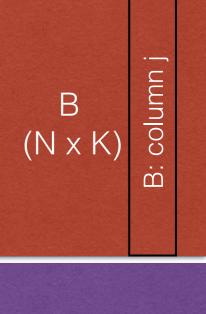


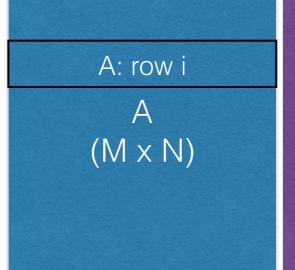


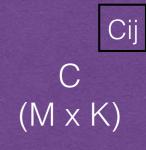
• Compute AB = C

$$C_{i,j} = \sum_{k=0}^{N} A_{i,k} B_{k,j}$$

```
// for each row of C
for (int i=0; i<M; ++i) {
    // for each column of C
    for (int j=0; i<K; ++j) {
        // compute the inner product
        for (int k=0; k<N; ++k)
            C[i*N + j] += A[i*N + k]*B[k*N + j];
    }
}</pre>
```







```
for (int i=0; i<M; ++i) {
    for (int j=0; i<K; ++j) {

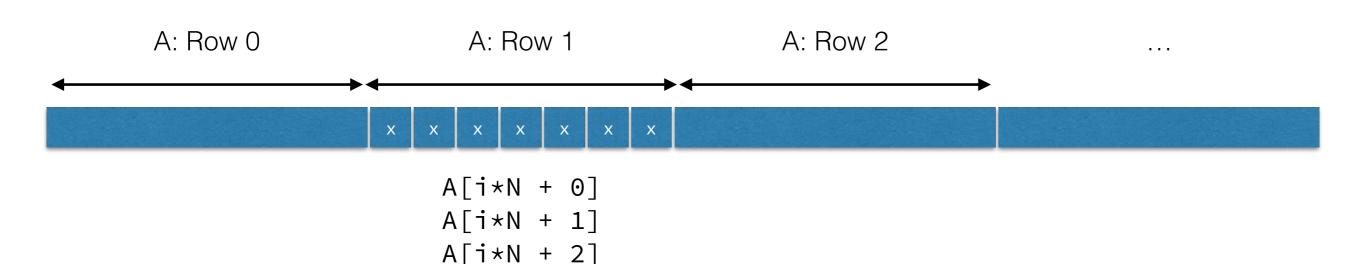
        for (int k=0; k<N; ++k)

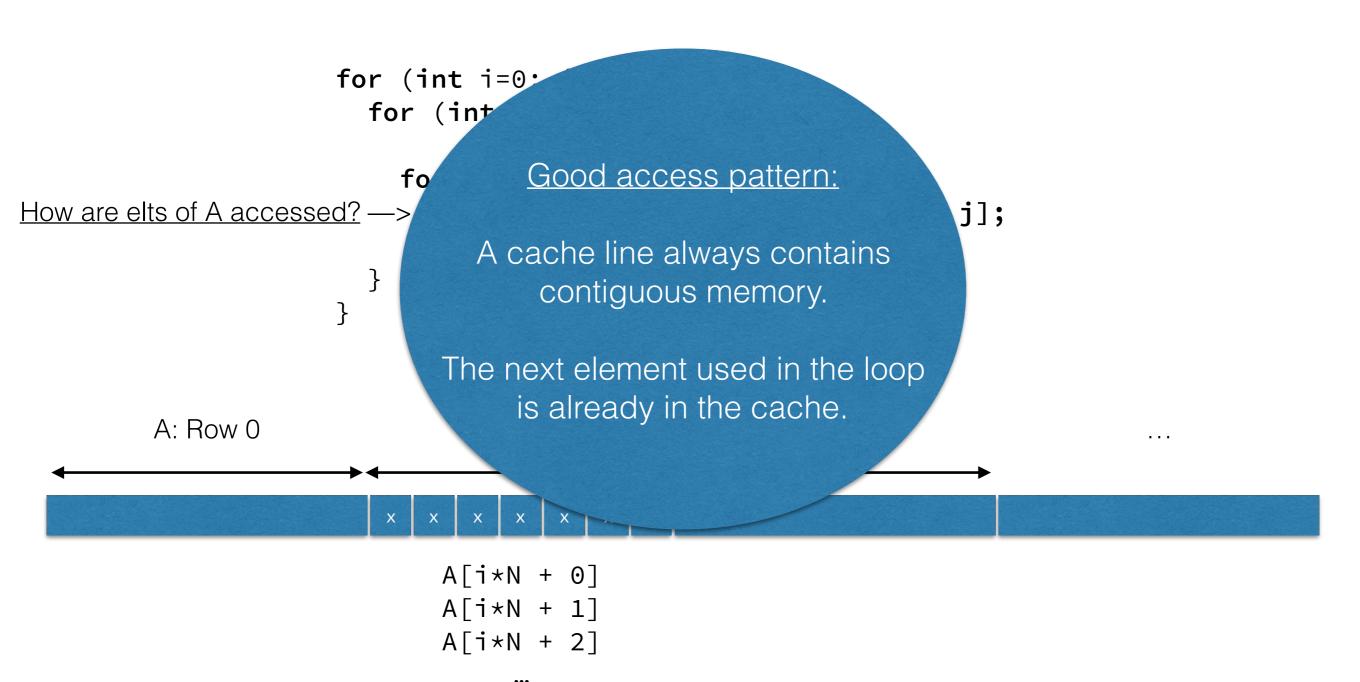
How are elts of A accessed? -> C[i*N + j] += A[i*N + k]*B[k*N + j];

}
}
```

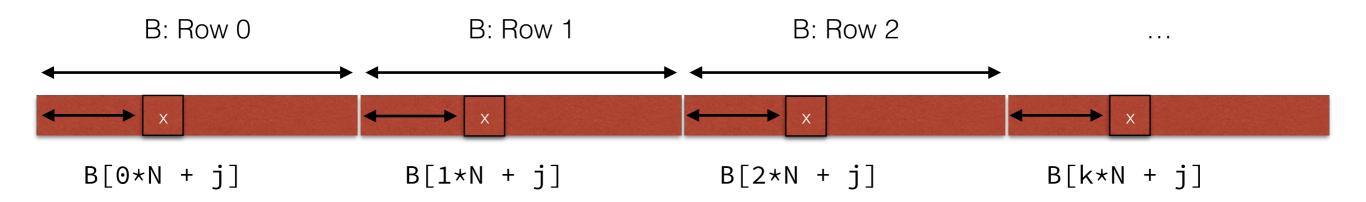
```
for (int i=0; i<M; ++i) {
    for (int j=0; i<K; ++j) {
        for (int k=0; k<N; ++k)
        How are elts of A accessed? --> C[i*N + j] += A[i*N + k]*B[k*N + j];
    }
}
```

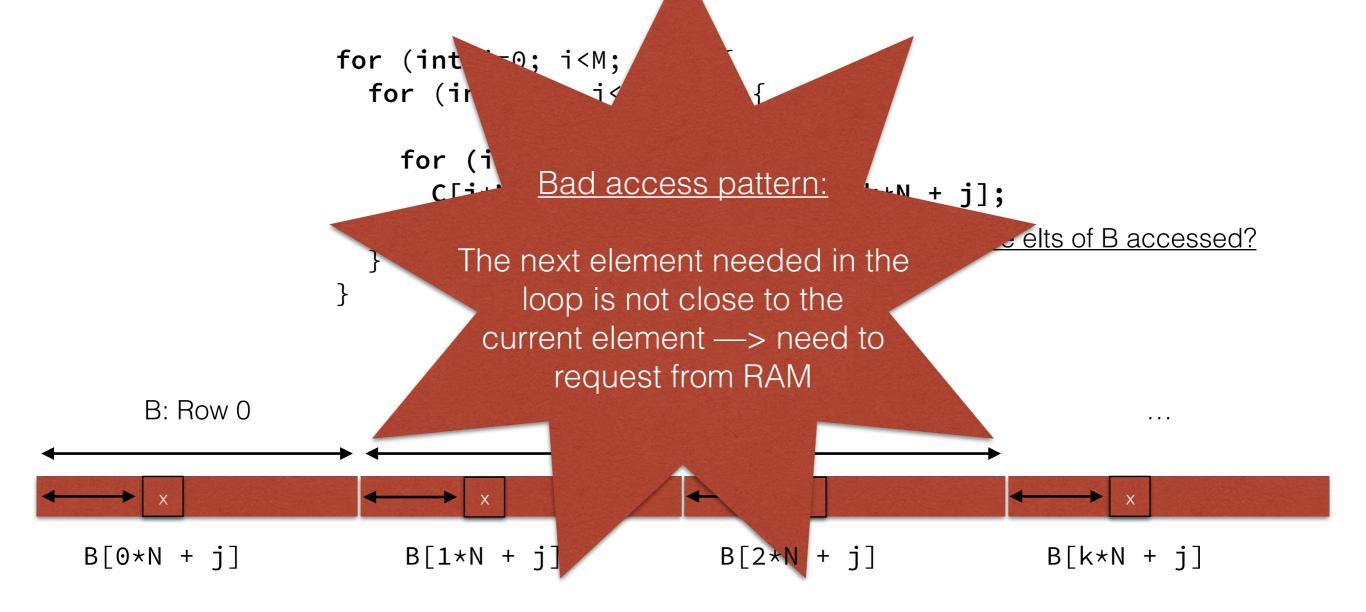
A[i\*N + (N-1)]





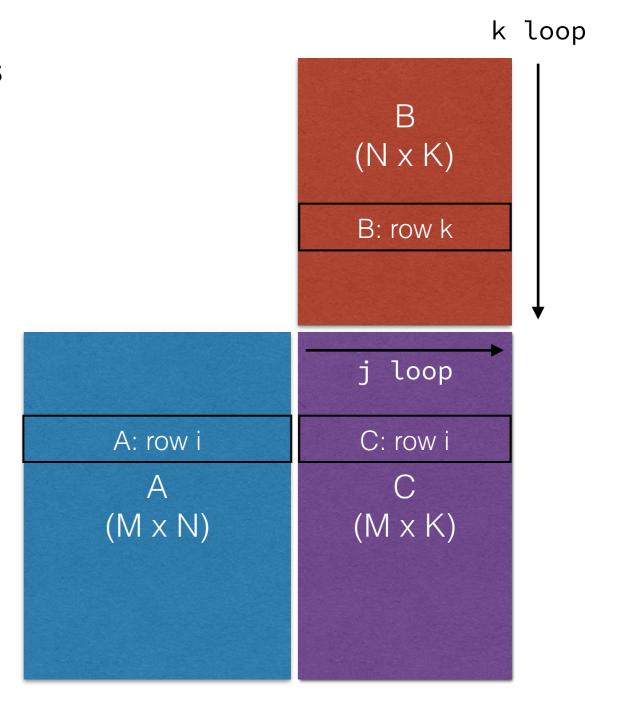
A[i\*N + (N-1)]

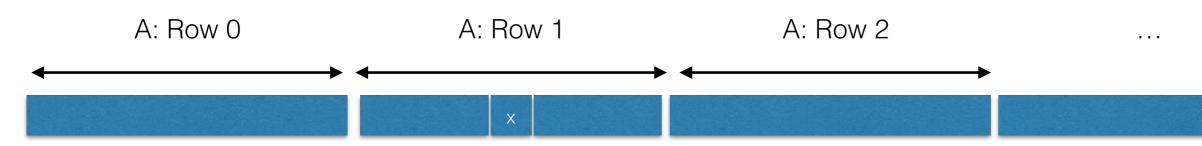




 One solution: add each row of B's contribution to all inner products in row i of C

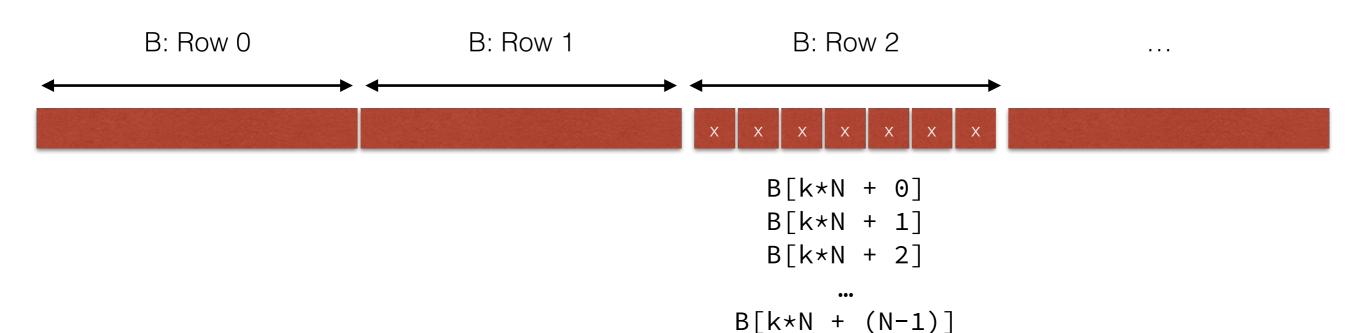
$$C_{i,j} = \sum_{k=0}^{N} A_{i,k} B_{k,j}$$





A[i\*N + k]

(outer k-loop is contiguous)



#### Demo

MatMul and speed improvements

## Memory Optimization

- Access patterns are key to performance
- Locality of reference
  - spatial locality if a memory location is referenced will nearby locations be ref'd as well?
  - temporal locality if a memory location is referenced will it be ref'd again soon?
  - branch locality are there only a few / infrequently occurring possible alternatives in program loop?

# Memory Optimization

- General strategies
  - rearrange change layout to increase spatial locality
  - reuse group data accesses to increase temporal locality
  - reduce smaller formats / compression to minimize number of cache lines read

## Memory Optimization

- Goal is to reduce / hide "latency" of memory requests
  - (in this case: reduce total number of requests)
- Herb Sutter: "increasing bandwidth is easy, but we can't buy our way out of latency"

## Operation Costs

- comparisons
- (u) int addition, subtraction, bitops, shifting
- float addition, subtraction
- indexed array access (subject to cache)
- (u) int multiplication
- float multiplication
- float division, remainder
- (u) int division, remainder

# Example: Digit Count

- Count number of digits in an unsigned long.
- Integer division = "divide + floor"

```
1234 / 10 = 123
123 / 10 = 12
12 / 10 = 1
1 / 10 = 0
```

Divide while non-zero

# Example: Digit Count

```
unsigned int digits_naive(unsigned long v)
  unsigned int result = 0;
  do
      ++result;
      v /= 10U; // very costly
    } while (v);
  return result;
```

# Example: Digit Count

 Key observation: integer division is equally expensive no matter the input. Comparison is cheap.

```
while (1)
{
   if (v < 10) return result;
   if (v < 100) return result + 1;
   if (v < 1000) return result + 2;
   if (v < 10000) return result + 3;

   v /= 10000U; // same cost as /= 10U
   result += 4;
}</pre>
```

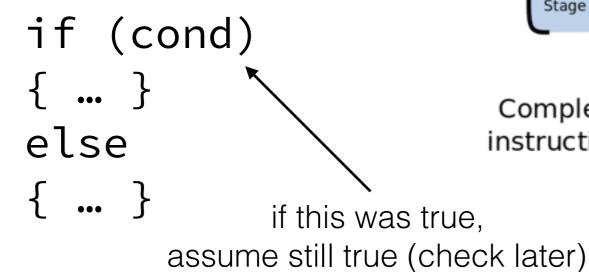
#### Demo

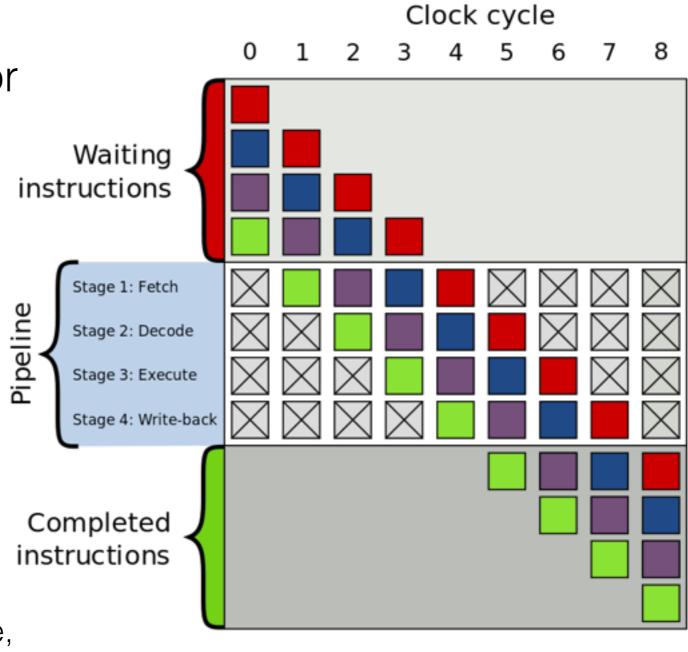
Digit count and expensive operations

#### Branch Prediction

 Branch locality - take advantage of processor pipelining (parallelism)

 modern processors perform "branch prediction"





loop if condition is always true then proc. will keep instruction set A in memory check condition "predict" the branch false true instruction set A instruction set B

```
long array[size]; // random data
for (size_t n=0; n<size; ++n)
    if (array[n] <= 128) // branch
    {
       threshold += 1;
       sum += array[n];
    }
printf("no. lets < 128 = %d", sum);</pre>
```

```
long array[size]; // random data
for (size_t n=0; n<size; ++n)</pre>
     if (array[n] <= 128) // branch</pre>
                 Branch prediction fail
          Data is random —> random branch at each
                      iteration
printf(
                                         sum);
```

```
for (size_t n=0; n<size; ++n)</pre>
    if (array[n] <= 128) // branch
            Branch prediction success
        sorted data—> high occurrence of correct
                 prediction
printf
                                 sum);
```

#### Demo

Branch prediction

#### Inline Functions

- Functions live in memory CPU spends time looking for it
- Inlined functions literally copy contents of function into calling function
- Occasionally effective, depending on situation.

```
inline void swap(int& m, int& n)
{
   int temp = m;
   m = n;
   n = temp;
}

int main()
{
   int a=1,b=2;
   int temp = a;
   a = b;
   b = temp;
}

int a=1,b=2;
   swap(&a,&b);
}
```

# Compiler Optimizations

Compilers can optimize code for you (to an extent). More time compiling

 —> (usually) faster code

```
$ gcc -01 ... # (or -02, or -03, etc.)
```

- See <u>gcc optimizations</u> for details.
- Example:
  - -fdelayed-branch

If supported for the target machine, attempt to reorder instructions to exploit instruction slots available after delayed branch instructions.

Enabled at levels -O, -O2, -O3, -Os.

# Compiler Optimizations

- Still need to manually handle memory contiguity
- Compiler optimizations transformations that produce provably equivalent code
  - reordering data is not (in general) provably equivalent