

## Encoders

An encoder is a digital circuit that performs the inverse operation of a decoder. An encoder has  $2^n$  (or less) input lines and  $n$  outputs lines. The output lines generate the binary code corresponding to the input value. An example of an encoder is the octal-to-binary encoder, whose truth table is given in Table 2-2. It has eight inputs, one for each of the octal digits, and three outputs that generate the corresponding binary number. It is assumed that only one input has a value of 1 at any given time; otherwise, the circuit has no meaning.

TABLE 2-2 Truth Table for Octal-to-Binary Encoder

Inputs								Outputs		
$D_7$	$D_6$	$D_5$	$D_4$	$D_3$	$D_2$	$D_1$	$D_0$	$A_2$	$A_1$	$A_0$
0	0	0	0	0	0	0	1	0	0	0
0	0	0	0	0	0	1	0	0	0	1
0	0	0	0	0	1	0	0	0	1	0
0	0	0	0	1	0	0	0	0	1	1
0	0	0	1	0	0	0	0	1	0	0
0	0	1	0	0	0	0	0	1	0	1
0	1	0	0	0	0	0	0	1	1	0
1	0	0	0	0	0	0	0	1	1	1

The encoder can be implemented with OR gates whose inputs are determined directly from the truth table. Output  $A_0 = 1$  if the input octal digit is 1 or 3 or 5 or 7. Similar conditions apply for the other two outputs. These conditions can be expressed by the following Boolean functions:

$$A_0 = D_1 + D_3 + D_5 + D_7$$

$$A_1 = D_2 + D_3 + D_6 + D_7$$

$$A_2 = D_4 + D_5 + D_6 + D_7$$

The encoder can be implemented with three OR gates.

## 2-3 Multiplexers

*multiplexer*

A multiplexer is a combinational circuit that receives binary information from one of  $2^n$  input data lines and directs it to a single output line. The selection of a particular input data line for the output is determined by a set of selection inputs. A  $2^n$ -to-1 multiplexer has  $2^n$  input data lines and  $n$  input selection lines whose bit combinations determine which input data are selected for the output.

A 4-to-1-line multiplexer is shown in Fig. 2-5. Each of the four data inputs  $I_0$  through  $I_3$  is applied to one input of an AND gate. The two selection inputs  $S_1$  and

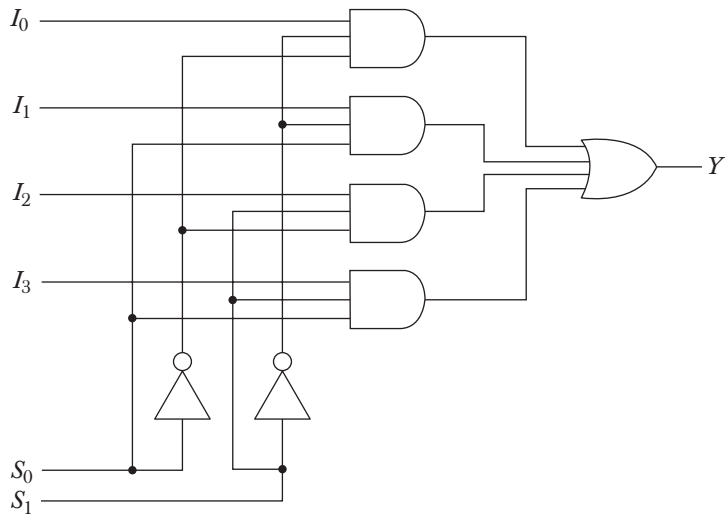


Figure 2-5 4-to-1-line multiplexer.

$S_0$  are decoded to select a particular AND gate. The outputs of the AND gates are applied to a single OR gate to provide the single output. To demonstrate the circuit operation, consider the case when  $S_1 S_0 = 10$ . The AND gate associated with input  $I_2$  has two of its inputs equal to 1. The third input of the gate is connected to  $I_2$ . The other three AND gates have at least one input equal to 0, which makes their outputs equal to 0. The OR gate output is now equal to the value of  $I_2$ , thus providing a path from the selected input to the output.

The 4-to-1 line multiplexer of Fig. 2-5 has six inputs and one output. A truth table describing the circuit needs 64 rows since six input variables can have  $2^6$  binary combinations. This is an excessively long table and will not be shown here. A more convenient way to describe the operation of multiplexers is by means of a function table. The function table for the multiplexer is shown in Table 2-3. The table demonstrates the relationship between the four data inputs and the single output as a function of the selection inputs  $S_1$  and  $S_0$ . When the selection inputs

TABLE 2-3 Function Table for 4-to-1-Line Multiplexer

Select		Output
$S_1$	$S_0$	$Y$
0	0	$I_0$
0	1	$I_1$
1	0	$I_2$
1	1	$I_3$

*data selector*

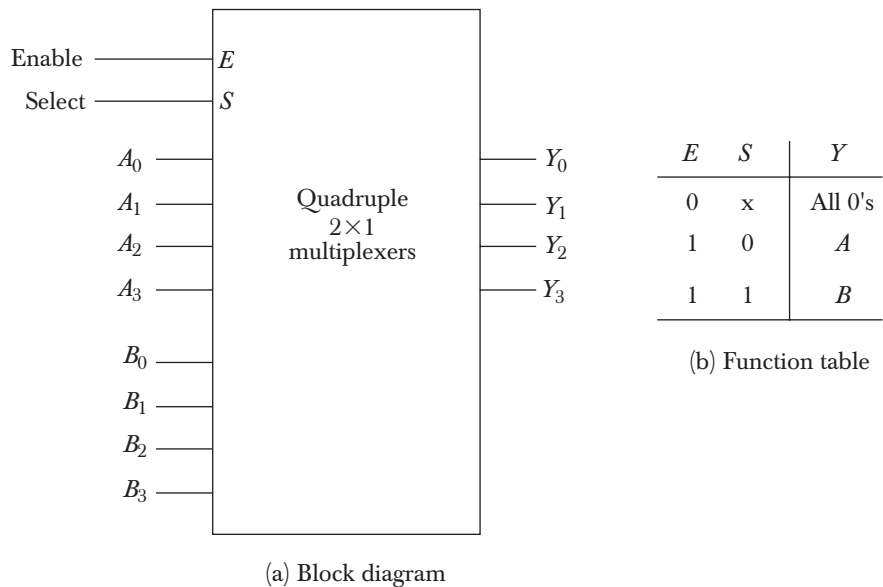
are equal to 00, output  $Y$  is equal to input  $I_0$ . When the selection inputs are equal to 01, input  $I_1$  has a path to output  $Y$ , and similarly for the other two combinations. The multiplexer is also called a *data selector*, since it selects one of many data inputs and steers the binary information to the output.

The AND gates and inverters in the multiplexer resemble a decoder circuit, and indeed they decode the input selection lines. In general, a  $2^n$ -to-1-line multiplexer is constructed from an  $n$ -to- $2^n$  decoder by adding to it  $2^n$  input lines, one from each data input. The size of the multiplexer is specified by the number  $2^n$  of its data inputs and the single output. It is then implied that it also contains  $n$  input selection lines. The multiplexer is often abbreviated as MUX.

As in decoders, multiplexers may have an enable input to control the operation of the unit. When the enable input is in the inactive state, the outputs are disabled, and when it is in the active state, the circuit functions as a normal multiplexer. The enable input is useful for expanding two or more multiplexers to a multiplexer with a larger number of inputs.

In some cases two or more multiplexers are enclosed within a single integrated circuit package. The selection and the enable inputs in multiple-unit construction are usually common to all multiplexers. As an illustration, the block diagram of a quadruple 2-to-1-line multiplexer is shown in Fig. 2-6. The circuit has four multiplexers, each capable of selecting one of two input lines. Output  $Y_0$  can be selected to come from either input  $A_0$  or  $B_0$ . Similarly, output  $Y_1$  may have the value of  $A_1$  or  $B_1$  and so on. One input selection line  $S$  selects one of the lines in each of the four multiplexers. The enable input  $E$  must be active for normal

Figure 2-6 Quadruple 2-to-1 line multiplexers.



operation. Although the circuit contains four multiplexers, we can also think of it as a circuit that selects one of two 4-bit data lines. As shown in the function table, the unit is enabled when  $E = 1$ . Then, if  $S = 0$ , the four  $A$  inputs have a path to the four outputs. On the other hand, if  $S = 1$ , the four  $B$  inputs are applied to the outputs. The outputs have all 0's when  $E = 0$ , regardless of the values of  $S$ .

Typical applications of multiplexers are data routing, parallel-to-serial conversion, and logic function generation. An  $n$ -variable logic function can be generated using  $n$ -select inputs of a multiplexer. Digital Multiplexers are thus considered universal logic modules.

## 2-4 Registers

A register is a group of flip-flops with each flip-flop capable of storing one bit of information. An  $n$ -bit register has a group of  $n$  flip-flops and is capable of storing any binary information of  $n$  bits. In addition to the flip-flops, a register may have combinational gates that perform certain data-processing tasks. In its broadest definition, a register consists of a group of flip-flops and gates that effect their transition. The flip-flops hold the binary information and the gates control when and how new information is transferred into the register.

Various types of registers are available commercially. The simplest register is one that consists only of flip-flops, with no external gates. Figure 2-7 shows such a register constructed with four  $D$  flip-flops. The common clock input triggers all flip-flops on the rising edge of each pulse, and the binary data available at the four inputs are transferred into the 4-bit register. The four outputs can be sampled at any time to obtain the binary information stored in the register. The *clear* input goes to a special terminal in each flip-flop. When this input goes to 0, all flip-flops are reset asynchronously. The clear input is useful for clearing the register to all 0's prior to its clocked operation. The clear input must be maintained at logic 1 during normal clocked operation. Note that the clock signal enables the  $D$  input but that the clear input is independent of the clock.

*register load*

The transfer of new information into a register is referred to as *loading* the register. If all the bits of the register are loaded simultaneously with a common clock pulse transition, we say that the loading is done in parallel. A clock transition applied to the  $C$  inputs of the register of Fig. 2-7 will load all four inputs  $I_0$  through  $I_3$  in parallel. In this configuration, the clock must be inhibited from the circuit if the content of the register must be left unchanged.

### Register with Parallel Load

Most digital systems have a master clock generator that supplies a continuous train of clock pulses. The clock pulses are applied to all flip-flops and registers in the system. The master clock acts like a pump that supplies a constant beat to all parts of the system. A separate control signal must be used to decide which specific clock pulse will have an effect on a particular register.

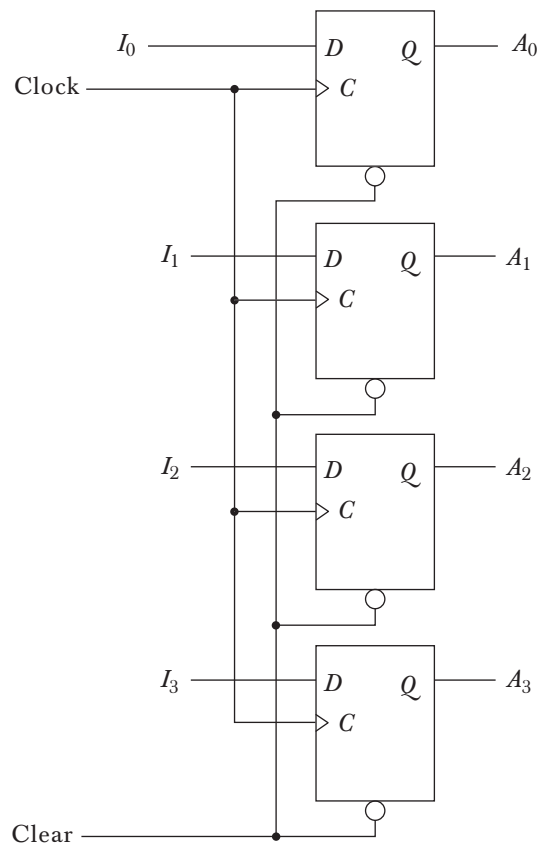


Figure 2-7 4-bit register.

A 4-bit register with a load control input that is directed through gates and into the  $D$  inputs is shown in Fig. 2-8. The  $C$  inputs receive clock pulses at all times. The buffer gate in the clock input reduces the power requirement from the clock generator. Less power is required when the clock is connected to only one input gate instead of the power consumption that four inputs would have required if the buffer were not used.

#### load input

The load input in the register determines the action to be taken with each clock pulse. When the load input is 1, the data in the four inputs are transferred into the register with the next positive transition of a clock pulse. When the load input is 0, the data inputs are inhibited and the  $D$  inputs of the flip-flops are connected to their outputs. The feedback connection from output to input is necessary because the  $D$  flip-flop does not have a “no change” condition. With each clock pulse, the  $D$  input determines the next state of the output. To leave the output unchanged, it is necessary to make the  $D$  input equal to the present value of the output.

Note that the clock pulses are applied to the  $C$  inputs at all times. The load input determines whether the next pulse will accept new information or leave the

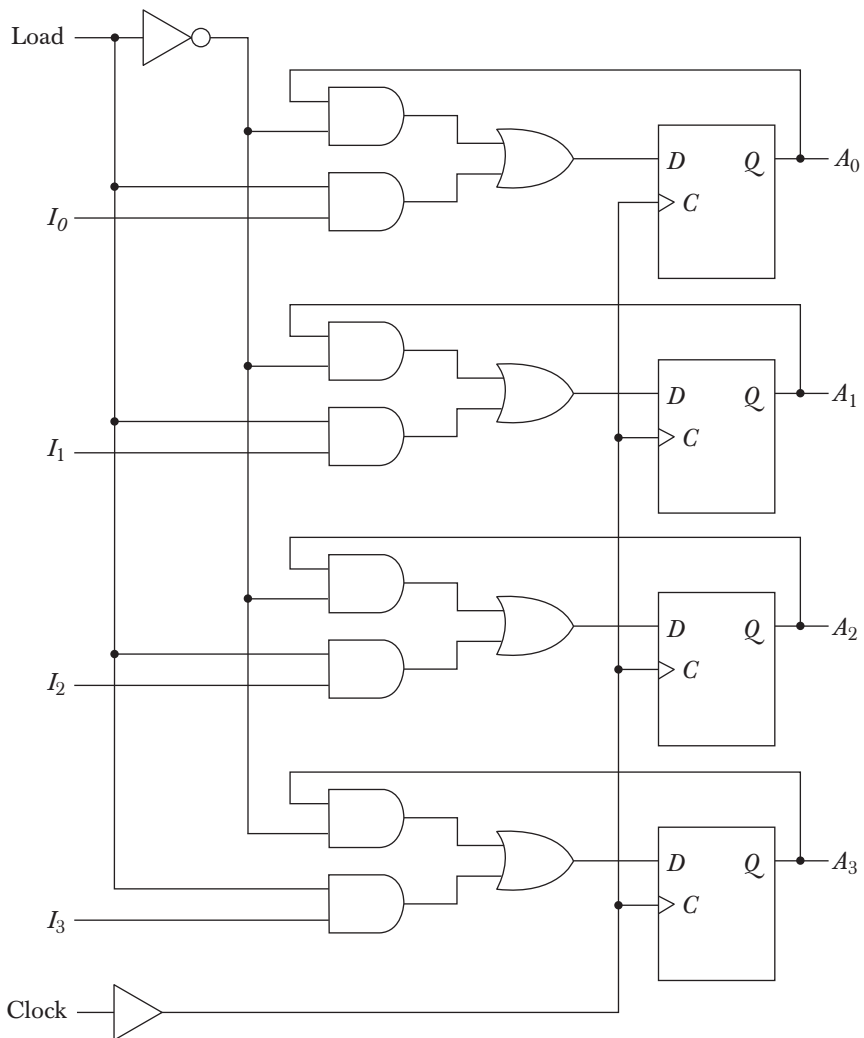


Figure 2-8 4-bit register with parallel load.

information in the register intact. The transfer of information from the inputs into the register is done simultaneously with all four bits during a single pulse transition.

## 2-5 Shift Registers

A register capable of shifting its binary information in one or both directions is called a shift register. The logical configuration of a shift register consists of a chain of flip-flops in cascade, with the output of one flip-flop connected to the input of