5.1---:) https://github.com/AvinashShrivastav/MATHEMATICS-FOR-COMPUTING

CHAPTER FIVE

Basic Computer Organization and Design

IN THIS CHAPTER

5-1 Instruction Codes

In this chapter we introduce a basic computer and show how its operation can be specified with register transfer statements. The organization of the computer is defined by its internal registers, the riming and control structure, and the set of instructions that it uses. The design of the computer is then carried out in detail. Although the basic computer presented in this chapter is very small compared to commercial computers, it has the advantage of being simple enough so we can demonstrate the design process without too many complications.

The internal organization of a digital system is defined by the sequence of microoperations it performs on data stored in its registers. The general-purpose digital computer is capable of executing various microoperations and, in addition, can be instructed as to what specific sequence of operations it must perform. The user of a computer can control the process by means of a program. A program is a set of instructions that specify the operations,

operands, and the sequence by which processing has to occur. The data-processing task may be altered by specifying a new program with different instructions or specifying the same instructions with different data.

A computer instruction is a binary code that specifies a sequence of microoperations for the computer. Instruction codes together with data are stored in memory. The computer reads each instruction from memory and places it in a control register. The control then interprets the binary code of the instruction and proceeds to execute it by issuing a sequence of microoperations. Every computer has its own unique instruction set. The ability to store and execute instructions, the stored program concept, is the most important property of a general-purpose computer.

instruction code

An instruction code is a group of bits that instruct the computer to perform a specific operation. It is usually divided into parts, each having its own particular interpretation. The most basic part of an instruction code is its operation part. The operation code of an instruction is a group of bits that define such operations as add, subtract, multiply, shift, and complement. The number of bits required for the operation code of an instruction depends on the total number of operations available in the computer. The operation code must consist of at least n bits for a given 2^n (or less) distinct operations. As an illustration, consider a computer with 64 distinct operations, one of them being an ADD operation. The operation code consists of six bits, with a bit configuration 110010 assigned to the ADD operation. When this operation code is decoded in the control unit, the computer issues control signals to read an operand from memory and add the operand to a processor register.

operation code

At this point we must recognize the relationship between a computer operation and a microoperation. An operation is part of an instruction stored in computer memory. It is a binary code that tells the computer to perform a specific operation. The control unit receives the instruction from memory and interprets the operation code bits. It then issues a sequence of control signals to initiate microoperations in internal computer registers. For every operation code, the control issues a sequence of microoperations needed for the hardware implementation of the specified operation. For this reason, an operation code is sometimes called a macrooperation because it specifies a set of micro-operations.

The operation part of an instruction code specifies the operation to be performed. This operation must be performed on some data stored in processor registers or in memory. An instruction code must therefore specify not only the operation but also the registers or the memory words where the operands are to be found, as well as the register or memory word where the result is to be stored. Memory words can be specified in instruction codes by their address. Processor registers can be specified by assigning to the instruction another binary code of k bits that specifies one of 2^k registers. There are many variations for arranging the binary code of instructions, and each computer has its own particular instruction code format. Instruction code formats

are conceived by computer designers who specify the architecture of the computer. In this chapter we choose a particular instruction code to explain the basic organization and design of digital computers.

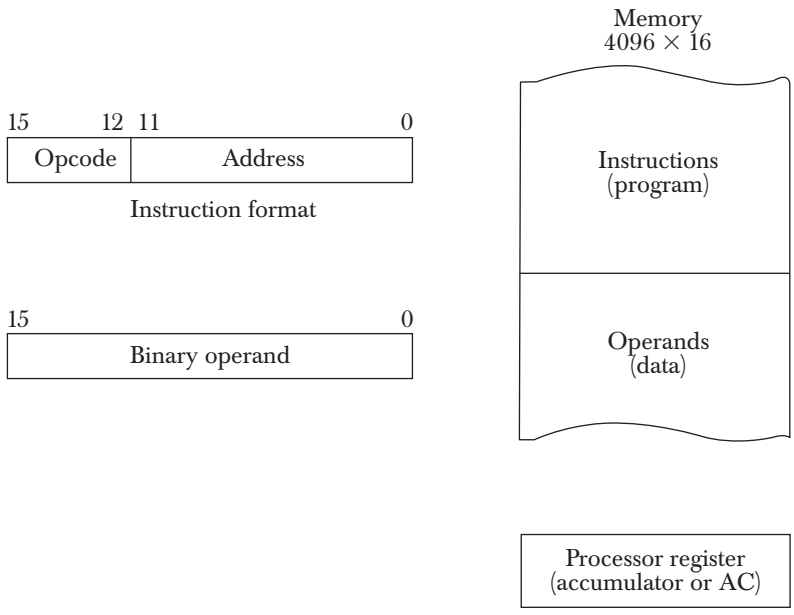
Stored Program Organization

The simplest way to organize a computer is to have one processor register and an instruction code format with two parts. The first part specifies the operation to be performed and the second specifies an address. The memory address tells the control where to find an operand in memory. This operand is read from memory and used as the data to be operated on together with the data stored in the processor register.

Figure 5-1 depicts this type of organization. Instructions are stored in one section of memory and data in another. For a memory unit with 4096 words we need 12 bits to specify an address since $2^{12} = 4096$. If we store each instruction code in one 16-bit memory word, we have available four bits for the operation code (abbreviated opcode) to specify one out of 16 possible operations, and 12 bits to specify the address of an operand. The control reads a 16-bit instruction from the program portion of memory. It uses the 12-bit address part of the instruction to read a 16-bit operand from the data portion of memory. It then executes the operation specified by the operation code.

opcode

Figure 5-1 Stored program organization.



accumulator (AC)

Computers that have a single-processor register usually assign to it the name accumulator and label it *AC*. The operation is performed with the memory operand and the content of *AC*.

If an operation in an instruction code does not need an operand from memory, the rest of the bits in the instruction can be used for other purposes. For example, operations such as clear *AC*, complement *AC*, and increment *AC* operate on data stored in the *AC* register. They do not need an operand from memory. For these types of operations, the second part of the instruction code (bits 0 through 11) is not needed for specifying a memory address and can be used to specify other operations for the computer.

Indirect Address

immediate instruction

It is sometimes convenient to use the address bits of an instruction code not as an address but as the actual operand. When the second part of an instruction code specifies an operand, the instruction is said to have an immediate operand. When the second part specifies the address of an operand, the instruction is said to have a direct address. This is in contrast to a third possibility called indirect address, where the bits in the second part of the instruction designate an address of a memory word in which the address of the operand is found. One bit of the instruction code can be used to distinguish between a direct and an indirect address.

As an illustration of this configuration, consider the instruction code format shown in Fig. 5-2(a). It consists of a 3-bit operation code, a 12-bit address, and an indirect address mode bit designated by *I*. The mode bit is 0 for a direct address and 1 for an indirect address. A direct address instruction is shown in Fig. 5-2(b). It is placed in address 22 in memory. The *I* bit is 0, so the instruction is recognized as a direct address instruction. The opcode specifies an ADD instruction, and the address part is the binary equivalent of 457. The control finds the operand in memory at address 457 and adds it to the content of *AC*. The instruction in address 35 shown in Fig. 5-2(c) has a mode bit $I = 1$. Therefore, it is recognized as an indirect address instruction. The address part is the binary equivalent of 300. The control goes to address 300 to find the address of the operand. The address of the operand in this case is 1350. The operand found in address 1350 is then added to the content of *AC*. The indirect address instruction needs two references to memory to fetch an operand. The first reference is needed to read the address of the operand; the second is for the operand itself. We define the *effective address* to be the address of the operand in a computation-type instruction or the target address in a branch-type instruction. Thus the effective address in the instruction of Fig. 5-2(b) is 457 and in the instruction of Fig 5-2(c) is 1350.

effective address

The direct and indirect addressing modes are used in the computer presented in this chapter. The memory word that holds the address of the operand in an indirect address instruction is used as a pointer to an array of

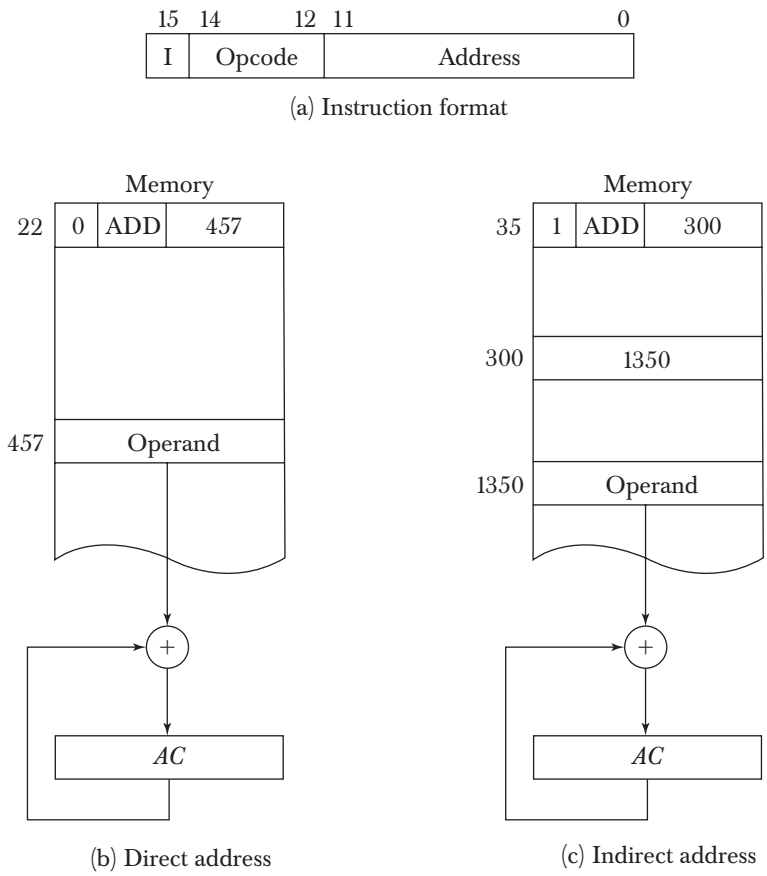


Figure 5-2 Demonstration of direct and indirect address.

data. The pointer could be placed in a processor register instead of memory as done in commercial computers.

5-2 Computer Registers

Computer instructions are normally stored in consecutive memory locations and are executed sequentially one at a time. The control reads an instruction from a specific address in memory and executes it. It then continues by reading the next instruction in sequence and executes it, and so on. This type of instruction sequencing needs a counter to calculate the address of the next instruction after execution of the current instruction is completed. It is also necessary to provide a register in the control unit for storing the instruction code after it is read

from memory. The computer needs processor registers for manipulating data and a register for holding a memory address. These requirements dictate the register configuration shown in Fig. 5-3. The registers are also listed in Table 5-1 together with a brief description of their function and the number of bits that they contain.

The memory unit has a capacity of 4096 words and each word contains 16 bits. Twelve bits of an instruction word are needed to specify the address of an operand. This leaves three bits for the operation, part of the instruction and a bit to specify a direct or indirect address. The data register (*DR*) holds the operand read from memory. The accumulator (*AC*) register is a general-purpose processing register. The instruction read from memory is placed in the instruction register (*IR*). The temporary register (*TR*) is used for holding temporary data during the processing.

TABLE 5-1 List of Registers for the Basic Computer

Register symbol	Number of bits	Register name	Function
DR	16	Data register	Holds memory operand
AR	12	Address register	Holds address for memory
AC	16	Accumulator	Processor register
IR	16	Instruction register	Holds instruction code
PC	12	Program counter	Holds address of instruction
TR	16	Temporary register	Holds temporary data
INPR	8	Input register	Holds input character
OUTR	8	Output register	Holds output character

program counter (PC)

The memory address register (*AR*) has 12 bits since this is the width of a memory address. The program counter (*PC*) also has 12 bits and it holds the address of the next instruction to be read from memory after the current instruction is executed. The *PC* goes through a counting sequence and causes the computer to read sequential instructions previously stored in memory. Instruction words are read and executed in sequence unless a branch instruction is encountered. A branch instruction calls for a transfer to a nonconsecutive instruction in the program. The address part of a branch instruction is transferred to *PC* to become the address of the next instruction. To read an instruction, the content of *PC* is taken as the address for memory and a memory read cycle is initiated. *PC* is then incremented by one, so it holds the address of the next instruction in sequence.

Two registers are used for input and output. The input register (*INPR*) receives an 8-bit character from an input device. The output register (*OUTR*) holds an 8-bit character for an output device.

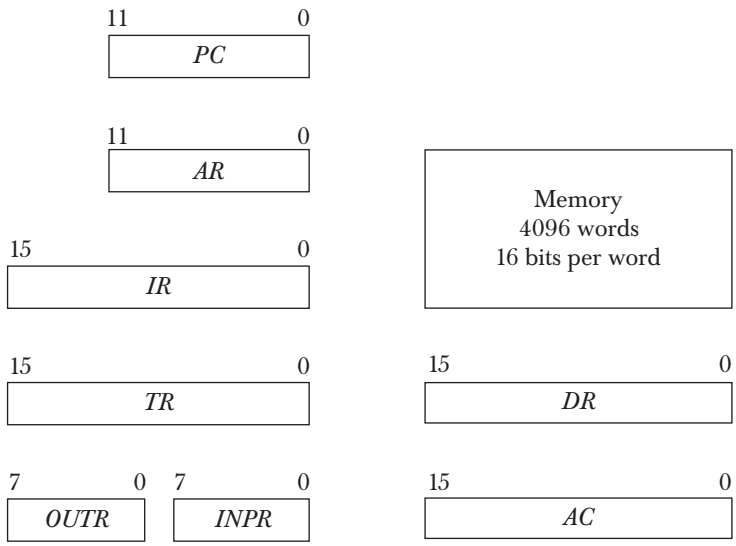


Figure 5-3 Basic computer registers and memory.

Common Bus System

The basic computer has eight registers, a memory unit, and a control unit (to be presented in Sec. 5-4). Paths must be provided to transfer information from one register to another and between memory and registers. The number of wires will be excessive if connections are made between the outputs of each register and the inputs of the other registers. A more efficient scheme for transferring information in a system with many registers is to use a common bus. We have shown in Sec. 4-3 how to construct a bus system using multiplexers or three-state buffer gates. The connection of the registers and memory of the basic computer to a common bus system is shown in Fig. 5-4.

The outputs of seven registers and memory are connected to the common bus. The specific output that is selected for the bus lines at any given time is determined from the binary value of the selection variables S_2, S_1, and S_0. The number along each output shows the decimal equivalent of the required binary selection. For example, the number along the output of *DR* is 3. The 16-bit outputs of *DR* are placed on the bus lines when $S_2S_1S_0 = 011$ since this is the binary value of decimal 3. The lines from the common bus are connected to the inputs of each register and the data inputs of the memory. The particular register whose LD (load) input is enabled receives the data from the bus during the next clock pulse transition. The memory receives the contents of the bus when its write input is activated. The memory places its 16-bit output onto the bus when the read input is activated and $S_2S_1S_0 = 111$.

load (LD)

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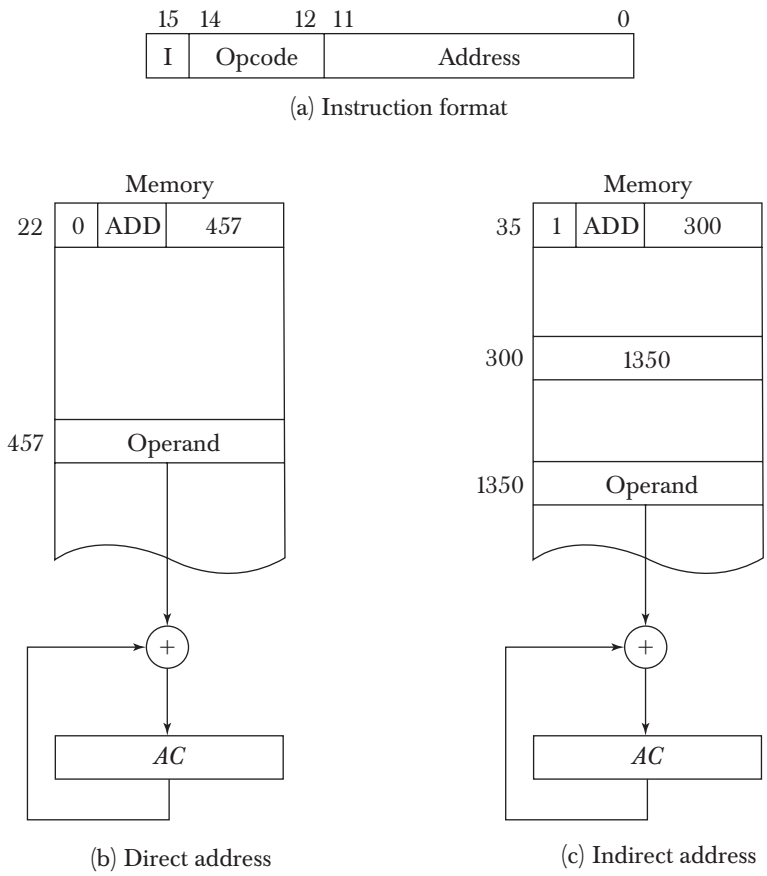

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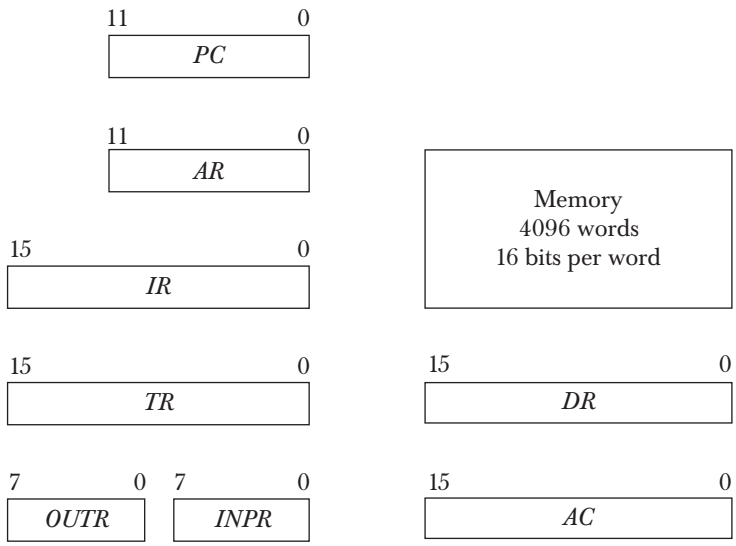

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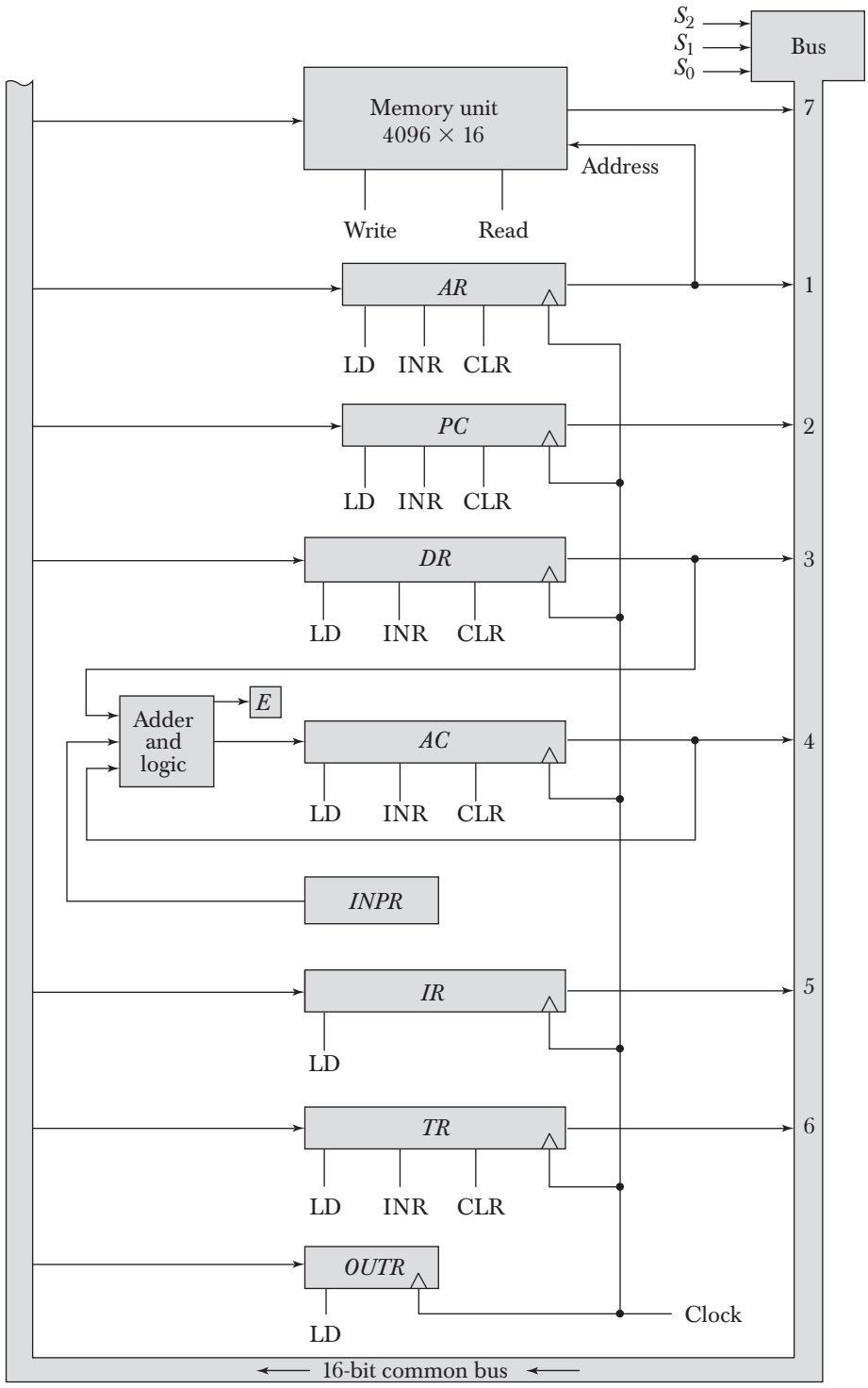
load (LD)


S_2
S_1
S_0
Bus
Memory unit
4096 × 16
Address
Write
Read
7
AR
LD INR CLR
1
PC
LD INR CLR
2
DR
LD INR CLR
3
Adder and logic
E
AC
LD INR CLR
4
INPR
IR
LD
5
TR
LD INR CLR
6
OUTR
LD
Clock
16-bit common bus

Four registers, *DR*, *AC*, *IR*, and *TR*, have 16 bits each. Two registers, *AR* and *PC*, have 12 bits each since they hold a memory address. When the contents of *AR* or *PC* are applied to the 16-bit common bus, the four most significant bits are set to 0's. When *AR* or *PC* receive information from the bus, only the 12 least significant bits are transferred into the register.

The input register *INPR* and the output register *OUTR* have 8 bits each and communicate with the eight least significant bits in the bus. *INPR* is connected to provide information to the bus but *OUTR* can only receive information from the bus. This is because *INPR* receives a character from an input device which is then transferred to *AC*. *OUTR* receives a character from *AC* and delivers it to an output device. There is no transfer from *OUTR* to any of the other registers.

The 16 lines of the common bus receive information from six registers and the memory unit. The bus lines are connected to the inputs of six registers and the memory. Five registers have three control inputs: LD (load), INR (increment), and CLR (clear). This type of register is equivalent to a binary counter with parallel load and synchronous clear similar to the one shown in Fig. 2-11. The increment operation is achieved by enabling the count input of the counter. Two registers have only a LD input. This type of register is shown in Fig. 2-7.

memory address

The input data and output data of the memory are connected to the common bus, but the memory address is connected to *AR*. Therefore, *AR* must always be used to specify a memory address. By using a single register for the address, we eliminate the need for an address bus that would have been needed otherwise. The content of any register can be specified for the memory data input during a write operation. Similarly, any register can receive the data from memory after a read operation except *AC*.

The 16 inputs of *AC* come from an adder and logic circuit. This circuit has three sets of inputs. One set of 16-bit inputs come from the outputs of *AC*. They are used to implement register microoperations such as complement *AC* and shift *AC*. Another set of 16-bit inputs come from the data regisler *DR*. The inputs from *DR* and *AC* are used for arithmetic and logic microoperations, such as add *DR* to *AC* or AND *DR* to *AC*. The result of an addition is transferred to *AC* and the end carry-out of the addition is transferred to flip-flop *E* (extended *AC* bit). A third set of 8-bit inputs come from the input register *INPR*. The operation of *INPR* and *OUTR* is explained in Sec. 5-7.

Note that the content of any register can be applied onto the bus and an operation can be performed in the adder and logic circuit during the same clock cycle. The clock transition at the end of the cycle transfers the content of the bus into the designated destination register and the output of the adder and logic circuit into *AC*. For example, the two microoperations

$$DR \leftarrow AC \quad \text{and} \quad AC \leftarrow DR$$

can be executed at the same time. This can be done by placing the content of *AC* on the bus (with $S_2S_1S_0 = 100$), enabling the LD (load) input of *DR*,

transferring the content of *DR* through the adder and logic circuit into *AC*, and enabling the LD (load) input of *AC*, all during the same clock cycle. The two transfers occur upon the arrival of the clock pulse transition at the end of the clock cycle.

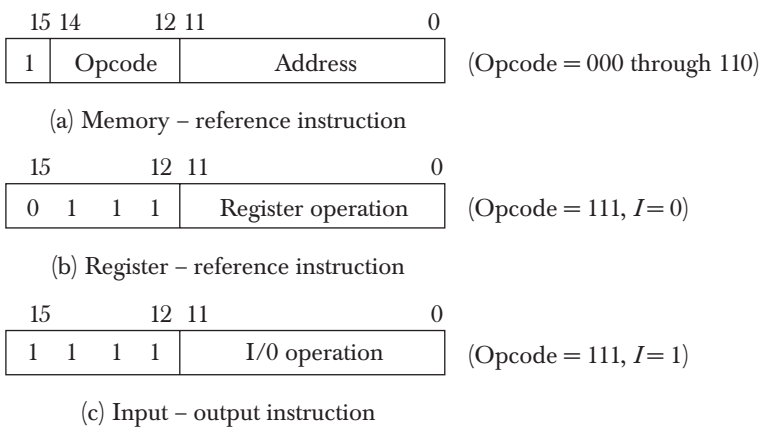
5-3 Computer Instructions

Instruction format

The basic computer has three instruction code formats, as shown in Fig. 5-5. Each format has 16 bits. The operation code (opcode) part of the instruction contains three bits and the meaning of the remaining 13 bits depends on the operation code encountered. A memory-reference instruction uses 12 bits to specify an address and one bit to specify the addressing mode *I*. *I* is equal to 0 for direct address and to 1 for indirect address (see Fig. 5-2). The register-reference instructions are recognized by the operation code 111 with a 0 in the leftmost bit (bit 15) of the instruction. A register-reference instruction specifies an operation on or a test of the *AC* register. An operand from memory is not needed; therefore, the other 12 bits are used to specify the operation or test to be executed. Similarly, an input–output instruction does not need a reference to memory and is recognized by the operation code 111 with a 1 in the leftmost bit of the instruction. The remaining 12 bits are used to specify the type of input–output operation or test performed.

The type of instruction is recognized by the computer control from the four bits in positions 12 through 15 of the instruction. If the three opcode bits in positions 12 though 14 are not equal to 111, the instruction is a memory-reference type and the bit in position 15 is taken as the addressing mode *I*. If the 3-bit opcode is equal to 111, control then inspects the bit in position 15. If

Figure 5-5 Basic computer instruction formats.



this bit is 0, the instruction is a register-reference type. If the bit is 1, the instruction is an input–output type. Note that the bit in position 15 of the instruction code is designated by the symbol *I* but is not used as a mode bit when the operation code is equal to 111.

Only three bits of the instruction are used for the operation code. It may seem that the computer is restricted to a maximum of eight distinct operations. However, since register-reference and input–output instructions use the remaining 12 bits as part of the operation code, the total number of instructions can exceed eight. In fact, the total number of instructions chosen for the basic computer is equal to 25.

The instructions for the computer are listed in Table 5-2. The symbol designation is a three-letter word and represents an abbreviation intended for

TABLE 5-2 Basic Computer Instructions

	Hexadecimal code		
Symbol	$I = 0$	$I = 1$	Description
AND	0xxx	8xxx	AND memory word to *AC*
ADD	lxxx	9xxx	Add memory word to *AC*
LDA	2xxx	Axxx	Load memory word to *AC*
STA	3xxx	Bxxx	Store content of *AC* in memory
BUN	4xxx	Cxxx	Branch unconditionally
BSA	5xxx	Dxxx	Branch and save return address
ISZ	6xxx	Exxx	Increment and skip if zero
CLA	7800		Clear *AC*
CLE	7400		Clear *E*
CMA	7200		Complement *AC*
CME	7100		Complement *E*
CIR	7080		Circulate right *AC* and *E*
CIL	7040		Circulate left *AC* and *E*
INC	7020		Increment *AC*
SPA	7010		Skip next instruction if *AC* positive
SNA	7008		Skip next instruction if *AC* negative
SZA	7004		Skip next instruction if *AC* zero
SZE	7002		Skip next instruction if *E* is 0
HLT	7001		Halt computer
INP	F800		Input character to *AC*
OUT	F400		Output character from *AC*
SKI	F200		Skip on input flag
SKO	F100		Skip on output flag
ION	F080		Interrupt on
IOF	F040		Interrupt off

hexadecimal code

programmers and users. The hexadecimal code is equal to the equivalent hexadecimal number of the binary code used for the instruction. By using the hexadecimal equivalent we reduced the 16 bits of an instruction code to four digits with each hexadecimal digit being equivalent to four bits. A memory-reference instruction has an address part of 12 bits. The address part is denoted by three x's and stand for the three hexadecimal digits corresponding to the 12-bit address. The last bit of the instruction is designated by the symbol *I*. When $I = 0$, the last four bits of an instruction have a hexadecimal digit equivalent from 0 to 6 since the last bit is 0. When $I = 1$, the hexadecimal digit equivalent of the last four bits of the instruction ranges from 8 to *E* since the last bit is 1.

Register-reference instructions use 16 bits to specify an operation. The leftmost four bits are always 0111, which is equivalent to hexadecimal 7. The other three hexadecimal digits give the binar) equivalent of the remaining 12 bits. The input–output instructions also use all 16 bits to specify an operation. The last four bits are always 1111, equivalent to hexadecimal F.

Instruction Set Completeness

Before investigating the operations performed by the instructions, let us discuss the type of instructions that must be included in a computer. A computer should have a set of instructions so that the user can construct machine language programs to evaluate any function that is known to be computable. The set of instructions are said to be complete if the computer includes a sufficient number of instructions in each of the following categories:

1. Arithmetic, logical, and shift instructions
2. Instructions for moving information to and from memory and processor registers
3. Program control instructions together with instructions that check status conditions
4. Input and output instructions

Arithmetic, logical, and shift instructions provide computational capabilities for processing the type of data that the user may wish to employ. The bulk of the binary information in a digital computer is stored in memory, but all computations are done in processor registers. Therefore, the user must have the capability of moving information between these two units. Decision-making capabilities are an important aspect of digital computers. For example, two numbers can be compared, and if the first is greater than the second, it may be necessary to proceed differently than if the second is greater than the first. Program control instructions such as branch instructions are used to change the sequence in which the program is executed. Input and output instructions are needed for communication between the computer and the

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transferring the content of *DR* through the adder and logic circuit into *AC*, and enabling the LD (load) input of *AC*, all during the same clock cycle. The two transfers occur upon the arrival of the clock pulse transition at the end of the clock cycle.

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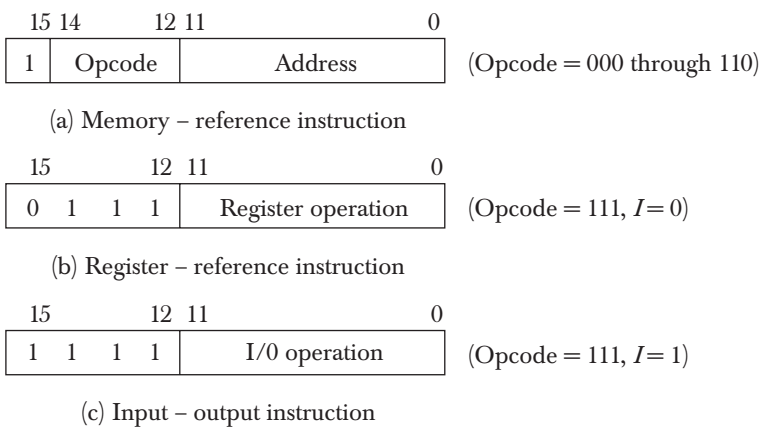
The type of instruction is recognized by the computer control from the four bits in positions 12 through 15 of the instruction. If the three opcode bits in positions 12 though 14 are not equal to 111, the instruction is a memory-reference type and the bit in position 15 is taken as the addressing mode *I*. If the 3-bit opcode is equal to 111, control then inspects the bit in position 15. If

Figure 5-5 Basic computer instruction formats.



this bit is 0, the instruction is a register-reference type. If the bit is 1, the instruction is an input–output type. Note that the bit in position 15 of the instruction code is designated by the symbol *I* but is not used as a mode bit when the operation code is equal to 111.

Only three bits of the instruction are used for the operation code. It may seem that the computer is restricted to a maximum of eight distinct operations. However, since register-reference and input–output instructions use the remaining 12 bits as part of the operation code, the total number of instructions can exceed eight. In fact, the total number of instructions chosen for the basic computer is equal to 25.

The instructions for the computer are listed in Table 5-2. The symbol designation is a three-letter word and represents an abbreviation intended for

TABLE 5-2 Basic Computer Instructions

	Hexadecimal code		
Symbol	$I = 0$	$I = 1$	Description
AND	0xxx	8xxx	AND memory word to *AC*
ADD	lxxx	9xxx	Add memory word to *AC*
LDA	2xxx	Axxx	Load memory word to *AC*
STA	3xxx	Bxxx	Store content of *AC* in memory
BUN	4xxx	Cxxx	Branch unconditionally
BSA	5xxx	Dxxx	Branch and save return address
ISZ	6xxx	Exxx	Increment and skip if zero
CLA	7800		Clear *AC*
CLE	7400		Clear *E*
CMA	7200		Complement *AC*
CME	7100		Complement *E*
CIR	7080		Circulate right *AC* and *E*
CIL	7040		Circulate left *AC* and *E*
INC	7020		Increment *AC*
SPA	7010		Skip next instruction if *AC* positive
SNA	7008		Skip next instruction if *AC* negative
SZA	7004		Skip next instruction if *AC* zero
SZE	7002		Skip next instruction if *E* is 0
HLT	7001		Halt computer
INP	F800		Input character to *AC*
OUT	F400		Output character from *AC*
SKI	F200		Skip on input flag
SKO	F100		Skip on output flag
ION	F080		Interrupt on
IOF	F040		Interrupt off

hexadecimal code

programmers and users. The hexadecimal code is equal to the equivalent hexadecimal number of the binary code used for the instruction. By using the hexadecimal equivalent we reduced the 16 bits of an instruction code to four digits with each hexadecimal digit being equivalent to four bits. A memory-reference instruction has an address part of 12 bits. The address part is denoted by three x's and stand for the three hexadecimal digits corresponding to the 12-bit address. The last bit of the instruction is designated by the symbol *I*. When $I = 0$, the last four bits of an instruction have a hexadecimal digit equivalent from 0 to 6 since the last bit is 0. When $I = 1$, the hexadecimal digit equivalent of the last four bits of the instruction ranges from 8 to *E* since the last bit is 1.

Register-reference instructions use 16 bits to specify an operation. The leftmost four bits are always 0111, which is equivalent to hexadecimal 7. The other three hexadecimal digits give the binar) equivalent of the remaining 12 bits. The input–output instructions also use all 16 bits to specify an operation. The last four bits are always 1111, equivalent to hexadecimal F.

Instruction Set Completeness

Before investigating the operations performed by the instructions, let us discuss the type of instructions that must be included in a computer. A computer should have a set of instructions so that the user can construct machine language programs to evaluate any function that is known to be computable. The set of instructions are said to be complete if the computer includes a sufficient number of instructions in each of the following categories:

1. Arithmetic, logical, and shift instructions
2. Instructions for moving information to and from memory and processor registers
3. Program control instructions together with instructions that check status conditions
4. Input and output instructions

Arithmetic, logical, and shift instructions provide computational capabilities for processing the type of data that the user may wish to employ. The bulk of the binary information in a digital computer is stored in memory, but all computations are done in processor registers. Therefore, the user must have the capability of moving information between these two units. Decision-making capabilities are an important aspect of digital computers. For example, two numbers can be compared, and if the first is greater than the second, it may be necessary to proceed differently than if the second is greater than the first. Program control instructions such as branch instructions are used to change the sequence in which the program is executed. Input and output instructions are needed for communication between the computer and the

user. Programs and data must be transferred into memory and results of computations must be transferred back to the user.

The instructions listed in Table 5-2 constitute a minimum set that provides all the capabilities mentioned above. There is one arithmetic instruction, ADD, and two related instructions, complement *AC*(CMA) and increment *AC*(INC). With these three instructions we can add and subtract binary numbers when negative numbers are in signed-2's complement representation. The circulate instructions, CIR and CIL, can be used for arithmetic shifts as well as any other type of shifts desired. Multiplication and division can be performed using addition, subtraction, and shifting. There are three logic operations: AND, complement *AC*(CMA), and clear *AC*(CLA). The AND and complement provide a NAND operation. It can be shown that with the NAND operation it is possible to implement all the other logic operations with two variables (listed in Table 4-6). Moving information from memory to *AC* is accomplished with the load *AC*(LDA) instruction. Storing information from *AC* into memory is done with the store *AC*(STA) instruction. The branch instructions BUN, BSA, and ISZ, together with the four skip instructions, provide capabilities for program control and checking of status conditions. The input (INP) and output (OUT) instructions cause information to be transferred between the computer and external devices.

Although the set of instructions for the basic computer is complete, it is not efficient because frequently used operations are not performed rapidly. An efficient set of instructions will include such instructions as subtract, multiply, OR, and exclusive-OR. These operations must be programmed in the basic computer. The programs are presented in Chap. 6 together with other programming examples for the basic computer. By using a limited number of instructions it is possible to show the detailed logic design of the computer. A more complete set of instructions would have made the design too complex. In this way we can demonstrate the basic principles of computer organization and design without going into excessive complex details. In Chap. 8 we present a complete list of computer instructions that are included in most commercial computers.

The function of each instruction listed in Table 5-2 and the microoperations needed for their execution are presented in Secs. 5-5 through 5-7 We delay this discussion because we must first consider the control unit and understand its internal organization.

5-4 Timing and Control

clock pulses

The timing for all registers in the basic computer is controlled by a master clock generator. The clock pulses are applied to all flip-flops and registers in the system, including the flip-flops and registers in the control unit. The clock pulses do not change the state of a register unless the register is enabled by a

control signal. The control signals are generated in the control unit and provide control inputs for the multiplexers in the common bus, control inputs in processor registers, and microoperations for the accumulator.

hardwired control

There are two major types of control organization: hardwired control and microprogrammed control. In the hardwired organization, the control logic is implemented with gates, flip-flops, decoders, and other digital circuits. It has the advantage that it can be optimized to produce a fast mode of operation. In the microprogrammed organization, the control information is stored in a control memory. The control memory is programmed to initiate the required sequence of microoperations. A hardwired control, as the name implies, requires changes in the wiring among the various components if the design has to be modified or changed. In the microprogrammed control, any required changes or modifications can be done by updating the microprogram in control memory. A hardwired control for the basic computer is presented in this section. A microprogrammed control unit for a similar computer is presented in Chap. 7.

microprogrammed control

control unit

The block diagram of the control unit is shown in Fig. 5-6. It consists of two decoders, a sequence counter, and a number of control logic gates. An instruction read from memory is placed in the instruction register (*IR*). The position of this register in the common bus system is indicated in Fig. 5-4. The instruction register is shown again in Fig. 5-6, where it is divided into three parts: the *I* bit, the operation code, and bits 0 through 11. The operation code in bits 12 through 14 are decoded with a 3×8 decoder. The eight outputs of the decoder are designated by the symbols D_0 through D_7. The subscripted decimal number is equivalent to the binary value of the corresponding operation code. Bit 15 of the instruction is transferred to a flip-flop designated by the symbol *I*. Bits 0 through 11 are applied to the control logic gates. The 4-bit sequence counter can count in binary from 0 through 15. The outputs of the counter are decoded into 16 timing signals T_0 through T_{15}. The internal logic of the control gates will be derived later when we consider the design of the computer in detail.

timing signals

The sequence counter *SC* can be incremented or cleared synchronously (see the counter of Fig. 2-11). Most of the time, the counter is incremented to provide the sequence of timing signals out of the 4×16 decoder. Once in awhile, the counter is cleared to 0, causing the next active timing signal to be T_0. As an example, consider the case where *SC* is incremented to provide timing signals T_0, T_1, T_2, T_3, and T_4 in sequence. At time T_4, *SC* is cleared to 0 if decoder output D_3 is active. This is expressed symbolically by the statement

$$D_3T_4: \quad SC \leftarrow 0$$

The timing diagram of Fig. 5-7 shows the time relationship of the control signals. The sequence counter *SC* responds to the positive transition of the clock. Initially, the CLR input of *SC* is active. The first positive transition of the clock

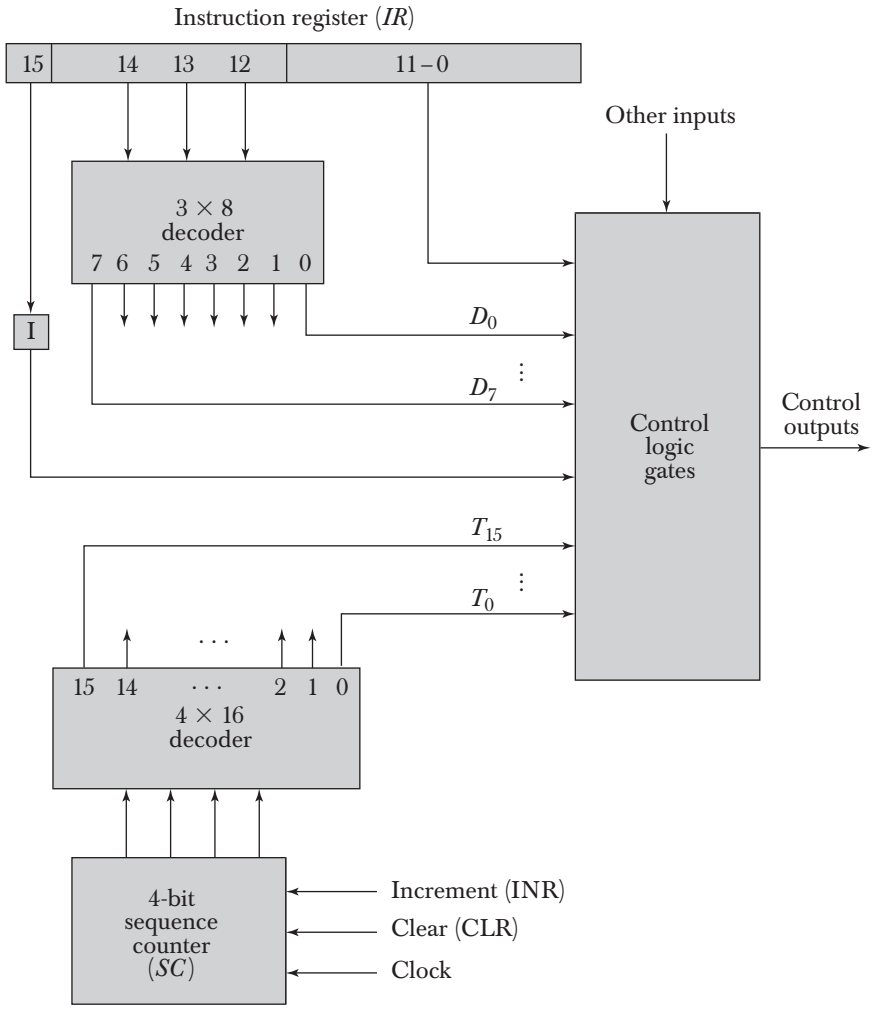


Figure 5-6 Control unit of basic computer.

clears *SC* to 0, which in turn activates the timing signal T_0 out of the decoder. T_0 is active during one clock cycle. The positive clock transition labeled T_0 in the diagram will trigger only those registers whose control inputs are connected to timing signal T_0. *SC* is incremented with every positive clock transition, unless its CLR input is active. This produces the sequence of timing signals T_0, T_1, T_2, T_3, T_4, and so on, as shown in the diagram. (Note the relationship between the timing signal and its corresponding positive clock transition.) If *SC* is not cleared, the timing signals will continue with T_5, T_6, up to T_{15} and back to T_0.

5.4 (up to pg. 137)---:) https://github.com/AvinashShrivastav/MATHEMATICS-FOR-COMPUTING

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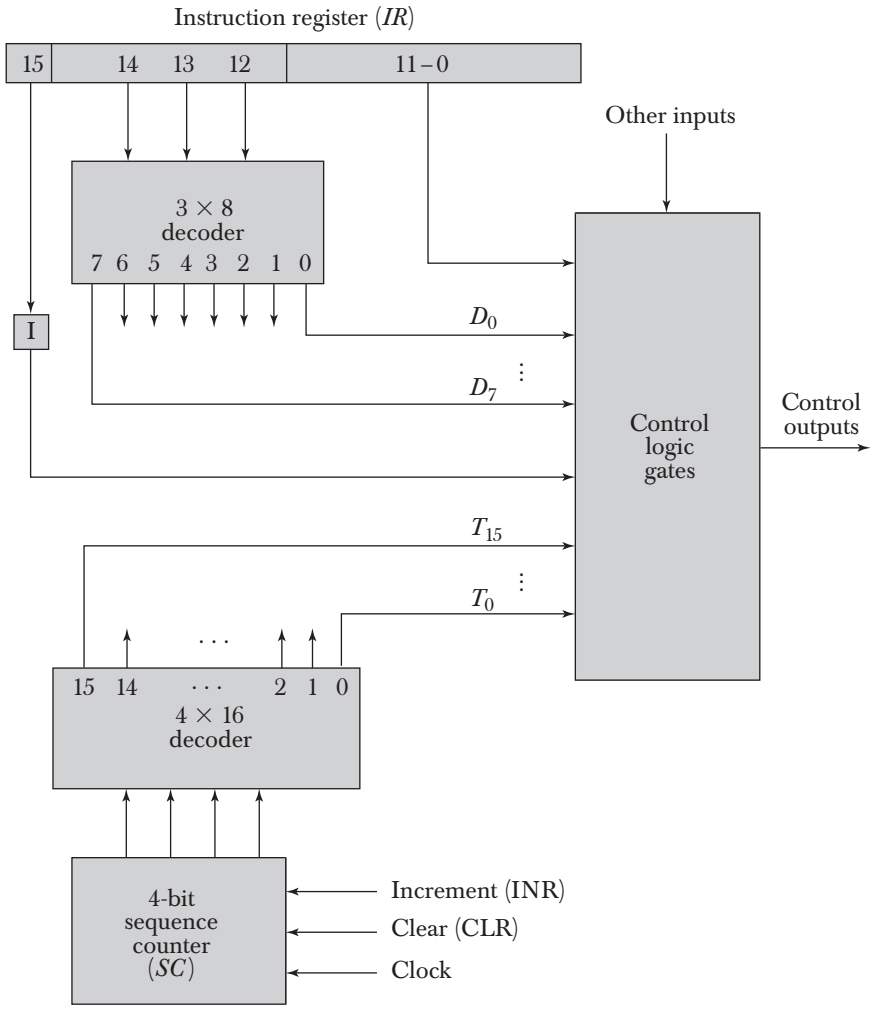


Figure 5-6 Control unit of basic computer.

clears *SC* to 0, which in turn activates the timing signal T_0 out of the decoder. T_0 is active during one clock cycle. The positive clock transition labeled T_0 in the diagram will trigger only those registers whose control inputs are connected to timing signal T_0. *SC* is incremented with every positive clock transition, unless its CLR input is active. This produces the sequence of timing signals T_0, T_1, T_2, T_3, T_4, and so on, as shown in the diagram. (Note the relationship between the timing signal and its corresponding positive clock transition.) If *SC* is not cleared, the timing signals will continue with T_5, T_6, up to T_{15} and back to T_0.

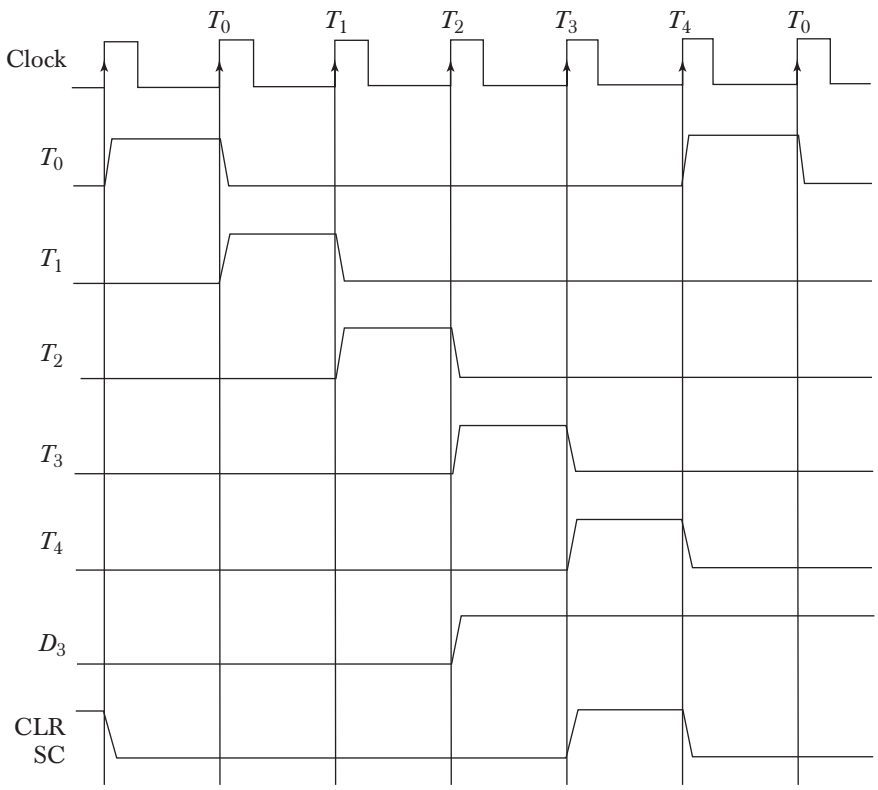


Figure 5-7 Example of control timing signals.

The last three waveforms in Fig. 5-7 show how *SC* is cleared when $D_3T_4 = 1$. Output D_3 from the operation decoder becomes active at the end of timing signal T_2. When timing signal T_4 becomes active, the output of the AND gate that implements the control function D_3T_4 becomes active. This signal is applied to the CLR input of *SC*. On the next positive clock transition (the one marked T_4 in the diagram) the counter is cleared to 0. This causes the timing signal T_0 to become active instead of T_5 that would have been active if *SC* were incremented instead of cleared.

A memory read or write cycle will be initiated with the rising edge of a timing signal. It will be assumed that a memory cycle time is less than the clock cycle time. According to this assumption, a memory read or write cycle initiated by a timing signal will be completed by the time the next clock goes through its positive transition. The clock transition will then be used to load the memory word into a register. This timing relationship is not valid in many computers because the memory cycle time is usually longer than the processor clock cycle. In such a case it is necessary to provide wait cycles in the

5.5---:) https://github.com/AvinashShrivastav/MATHEMATICS-FOR-COMPUTING

processor until the memory word is available. To facilitate the presentation, we will assume that a wait period is not necessary in the basic computer.

To fully comprehend the operation of the computer, it is crucial that one understands the timing relationship between the clock transition and the timing signals. For example, the register transfer statement

$$T_0: \quad AR \leftarrow PC$$

specifies a transfer of the content of *PC* into *AR* if timing signal T_0 is active. T_0 is active during an entire clock cycle interval. During this time the content of *PC* is placed onto the bus (with $S_2S_1S_0 = 010$) and the LD (load) input of *AR* is enabled. The actual transfer does not occur until the end of the clock cycle when the clock goes through a positive transition. This same positive clock transition increments the sequence counter *SC* from 0000 to 0001. The next clock cycle has T_1 active and T_0 inactive.

5-5 Instruction Cycle

A program residing in the memory unit of the computer consists of a sequence of instructions. The program is executed in the computer by going through a cycle for each instruction. Each instruction cycle in turn is subdivided into a sequence of subcycles or phases. In the basic computer each instruction cycle consists of the following phases:

1. Fetch an instruction from memory.
2. Decode the instruction.
3. Read the effective address from memory if the instruction has an indirect address.
4. Execute the instruction.

Upon the completion of step 4, the control goes back to step 1 to fetch, decode, and execute the next instruction. This process continues indefinitely unless a HALT instruction is encountered.

Fetch and Decode

Initially, the program counter *PC* is loaded with the address of the first instruction in the program. The sequence counter *SC* is cleared to 0, providing a decoded timing signal T_0. After each clock pulse, *SC* is incremented by one, so that the timing signals go through a sequence T_0, T_1, T_2, and so on. The microoperations for the fetch and decode phases can be specified by the following register transfer statements.

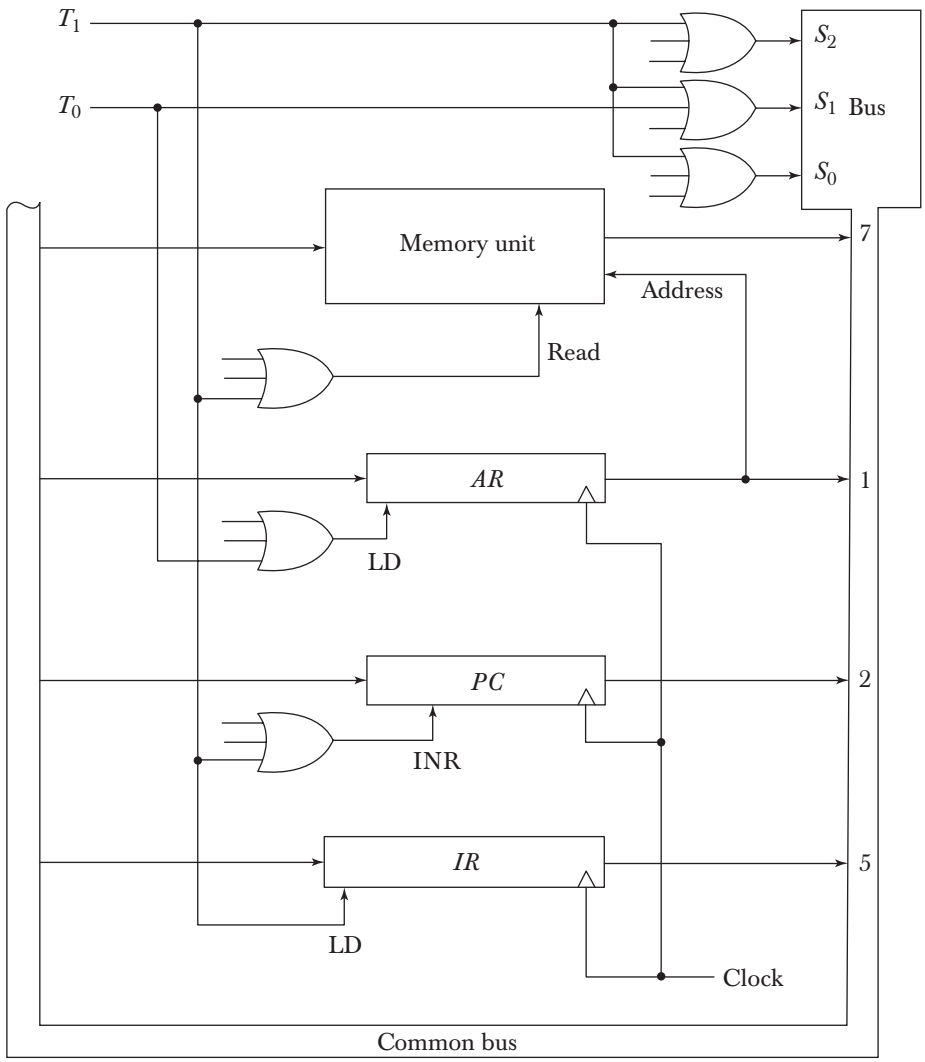
T_0: $AR \leftarrow PC$

T_1: $IR \leftarrow M[AR]$, $PC \leftarrow PC + 1$

T_2: $D_0, \ldots, D_7 \leftarrow$ Decode $IR(12\text{–}14)$, $AR \leftarrow IR(0-11)$, $I \leftarrow IR(15)$

Since only *AR* is connected to the address inputs of memory, it is necessary to transfer the address from *PC* to *AR* during the clock transition associated with timing signal T_0. The instruction read from memory is then placed in the instruction register *IR* with the clock transition associated with timing

Figure 5-8 Register transfers for the fetch phase.



signal T_1. At the same time, *PC* is incremented by one to prepare it for the address of the next instruction in the program. At rime T_2, the operation code in *IR* is decoded, the indirect bit is transferred to flip-flop *I*, and the address part of the instruction is transferred to *AR*. Note that *SC* is incremented after each clock pulse to produce the sequence T_0, T_1, and T_2.

Figure 5-8 shows how the first two register transfer statements are implemented in the bus system. To provide the data path for the transfer of *PC* to *AR* we must apply timing signal T_0 to achieve the following connection:

1. Place the content of *PC* onto the bus by making the bus selection inputs $S_2S_1S_0$ equal to 010.
2. Transfer the content of the bus to *AR* by enabling the LD input of *AR*.

The next clock transition initiates the transfer from *PC* to *AR* since $T_0 = 1$. In order to implement the second statement

$$T_1: \qquad IR \leftarrow M[AR], \qquad PC \leftarrow PC + 1$$

it is necessary to use timing signal T_1 to provide the following connections in the bus system.

1. Enable the read input of memory.
2. Place the content of memory onto the bus by making $S_2S_1S_0 = 111$.
3. Transfer the content of the bus to *IR* by enabling the LD input of *IR*.
4. Increment *PC* by enabling the INR input of *PC*.

The next clock transition initiates the read and increment operations since $T_1 = 1$.

Figure 5-8 duplicates a portion of the bus system and shows how T_0 and T_1 are connected to the control inputs of the registers, the memory, and the bus selection inputs. Multiple input OR gates are included in the diagram because there are other control functions that will initiate similar operations.

Determine the Type of Instruction

The timing signal that is active after the decoding is T_3. During time T_3, the control unit determines the type of instruction that was just read from memory. The flowchart of Fig. 5-9 presents an initial configuration for the instruction cycle and shows how the control determines the instruction type after the decoding. The three possible instruction types available in the basic computer are specified in Fig. 5-5.

Decoder output D_7 is equal to 1 if the operation code is equal to binary 111. From Fig. 5-5 we determine that if $D_7 = 1$, the instruction must be a

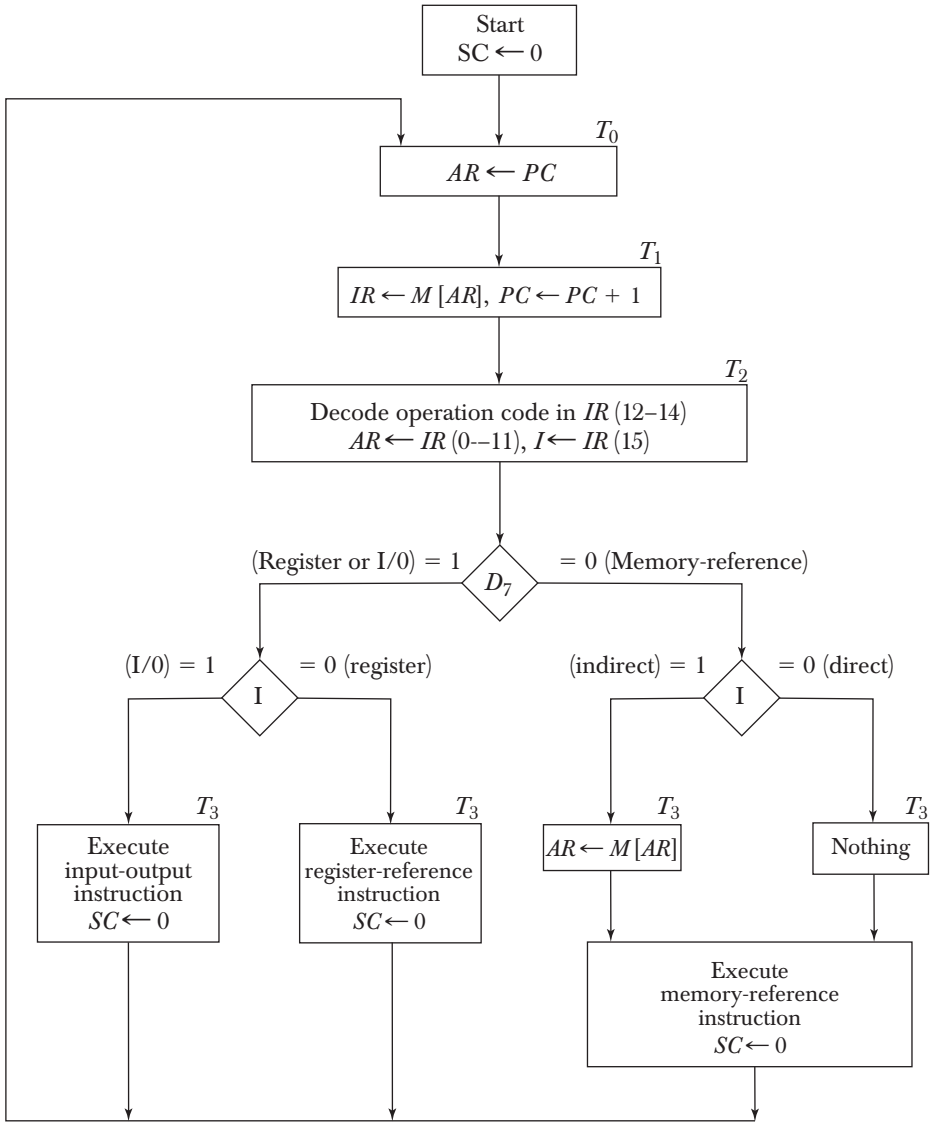


Figure 5-9 Flowchart for instruction cycle (initial configuration).

register-reference or input–output type. If $D_7 = 0$, the operation code must be one of the other seven values 000 through 110, specifying a memory-reference instruction. Control then inspects the value of the first bit of the instruction, which is now available in flip-flop I. If $D_7 = 0$ and $I = 1$, we have a memory-reference instruction with an indirect address. It is then necessary to read the

indirect address

effective address from memory. The microoperation for the indirect address condition can be symbolized by the register transfer statement

$$AR \leftarrow M[AR]$$

Initially, *AR* holds the address part of the instruction. This address is used during the memory read operation. The word at the address given by *AR* is read from memory and placed on the common bus. The LD input of *AR* is then enabled to receive the indirect address that resided in the 12 least significant bits of the memory word.

The three instruction types are subdivided into four separate paths. The selected operation is activated with the clock transition associated with timing signal T_3. This can be symbolized as follows:

$D_7' I T_3$: $AR \leftarrow M[AR]$

$D_7' I T_3$: Nothing

$D_7 I' T_3$: Execute a register-reference instruction

$D_7 I T_3$: Execute an input–output instruction

When a memory-reference instruction with $I = 0$ is encountered, it is not necessary to do anything since the effective address is already in *AR*. However, the sequence counter *SC* must be incremented when $D_7' T_3 = 1$, so that the execution of the memory-reference instruction can be continued with timing variable T_4. A register-reference or input-output instruction can be executed with the clock associated with timing signal T_3. After the instruction is executed, *SC* is cleared to 0 and control returns to the fetch phase with $T_0 = 1$.

Note that the sequence counter *SC* is either incremented or cleared to 0 with every positive clock transition. We will adopt the convention that if *SC* is incremented, we will not write the statement $SC \leftarrow SC + 1$, but it will be implied that the control goes to the next timing signal in sequence. When *SC* is to be cleared, we will include the statement $SC \leftarrow 0$.

The register transfers needed for the execution of the register-reference instructions are presented in this section. The memory-reference instructions are explained in the next section. The input-output instructions are included in Sec. 5-7.

Register-Reference Instructions

Register-reference instructions are recognized by the control when $D_7 = 1$ and $I = 0$. These instructions use bits 0 through 11 of the instruction code to specify one of 12 instructions. These 12 bits are available in *IR* (0–11). They were also transferred to *AR* during time T_2.

The control functions and microoperations for the register-reference instructions are listed in Table 5-3. These instructions are executed with the

clock transition associated with timing variable T_3. Each control function needs the Boolean relation $D_7 I' T_3$, which we designate for convenience by the symbol r. The control function is distinguished by one of the bits in $IR(0–11)$. By assigning the symbol B, to bit i of IR, all control functions can be simply denoted by rB_i. For example, the instruction CLA has the hexadecimal code 7800 (see Table 5-2), which gives the binary equivalent 0111 1000 0000 0000. The first bit is a zero and is equivalent to I'. The next three bits constitute the operation code and are recognized from decoder output D_7. Bit 11 in IR is 1 and is recognized from B_{11}. The control function that initiates the microoperation for this instruction is $D_7 I' T_3 B_{11} = rB_{11}$. The execution of a register-reference instruction is completed at time T_3. The sequence counter SC is cleared to 0 and the control goes back to fetch the next instruction with timing signal T_0.

The first seven register-reference instructions perform clear, complement, circular shift, and increment microoperations on the AC or E registers. The next four instructions cause a skip of the next instruction in sequence when a stated condition is satisfied. The skipping of the instruction is achieved by incrementing PC once again (in addition, it is being incremented during the fetch phase at time T_1). The condition control statements must be recognized as part of the control conditions. The AC is positive when the sign bit in AC $(15) = 0$; it is negative when $AC(15) = 1$. The content of AC is zero $(AC = 0)$ if all the flip-flops of the register are zero. The HLT instruction clears a start-stop flip-flop S and stops the sequence counter from counting. To restore the operation of the computer, the start–stop flip-flop must be set manually.

TABLE 5-3 Execution of Register-Reference Instructions

$D_7 I' T_3 = r$ (common to all registcr-reference instructions)
$IR(i) = B_i$ [bit in $IR(0–11)$ that specifies the operation]

	r:	$SC \leftarrow 0$	Clear SC
CLA	rB_{11}:	$AC \leftarrow 0$	Clear AC
CLE	rB_{10}:	$E \leftarrow 0$	Clear E
CMA	rB_9:	$AC \leftarrow \overline{AC}$	Complement AC
CME	rB_8:	$E \leftarrow \overline{E}$	Complement E
CIR	rB_7:	$AC \leftarrow$ shr AC, $AC(15) \leftarrow E$, $E \leftarrow AC(0)$	Circulate right
CIL	rB_6:	$AC \leftarrow$ shl AC, $AC(0) \leftarrow E$, $E \leftarrow AC(15)$	Circulate left
INC	rB_5:	$AC^* \rightarrow AC + 1$	Increment AC
SPA	rB_4:	If $(AC(15) = 0)$ then $(PC \leftarrow PC + 1)$	Skip if positive
SNA	rB_3:	If $(AC(15) = 1)$ then $(PC \leftarrow PC + 1)$	Skip if negative
SZA	rB_2:	If $(AC = 0)$ then $PC \leftarrow PC + 1$	Skip if AC zero
SZE	rB_1:	If $(E = 0)$ then $(PC \leftarrow PC + 1)$	Skip if E zero
HLT	rB_0:	$S \leftarrow 0$ (S is a start–stop flip-flop)	Halt computer

5-6 Memory-Reference Instructions

In order to specify the microoperations needed for the execution of each instruction, it is necessary that the function that they are intended to perform be defined precisely. Looking back to Table 5-2, where the instructions are listed, we find that some instructions have an ambiguous description. This is because the explanation of an instruction in words is usually lengthy, and not enough space is available in the table for such a lengthy explanation. We will now show that the function of the memory-reference instructions can be defined precisely by means of register transfer notation.

effective address

Table 5-4 lists the seven memory-reference instructions. The decoded output D_i for $i = 0, 1, 2, 3, 4, 5$, and 6 from the operation decoder that belongs to each instruction is included in the table. The effective address of the instruction is in the address register AR and was placed there during timing signal T_2 when $I = 0$, or during timing signal T_3 when $I = 1$. The execution of the memory-reference instructions starts with timing signal T_4. The symbolic description of each instruction is specified in the table in terms of register transfer notation. The actual execution of the instruction in the bus system will require a sequence of microoperations. This is because data stored in memory cannot be processed directly. The data must be read from memory to a register where they can be operated on with logic circuits. We now explain the operation of each instruction and list the control functions and microoperations needed for their execution. A flowchart that summarizes all the microoperations is presented at the end of this section.

TABLE 5-4 Memory-Reference Instructions

Symbol	Operation decoder	Symbolic description
AND	D_0	$AC \leftarrow AC \wedge M[AR]$
ADD	D_1	$AC \leftarrow AC + M[AR]$, $E \leftarrow C_{out}$
LDA	D_2	$AC \leftarrow M[AR]$
STA	D_3	$M[AR] \leftarrow AC$
BUN	D_4	$PC \leftarrow AR$
BSA	D_5	$M[AR] \leftarrow PC$, $PC \leftarrow AR + 1$
ISZ	D_6	$M[AR] \leftarrow M[AR] + 1$, If $M[AR] + 1 = 0$ then $PC \leftarrow PC + 1$

AND to AC

This is an instruction that performs the AND logic operation on pairs of bits in AC and the memory word specified by the effective address. The result of

the operation is transferred to *AC*. The microoperations that execute this instruction are:

$$D_0T_4: \quad DR \leftarrow M[AR]$$
$$D_0T_5: \quad AC \leftarrow AC \wedge DR, \quad SC \leftarrow 0$$

The control function for this instruction uses the operation decoder D_0 since this output of the decoder is active when the instruction has an AND operation whose binary code value is 000. Two timing signals are needed to execute the instruction. The clock transition associated with timing signal T_4 transfers the operand from memory into *DR*. The clock transition associated with the next timing signal T_5 transfers to *AC* the result of the AND logic operation between the contents of *DR* and *AC*. The same clock transition clears *SC* to 0, transferring control to timing signal T_0 to start a new instruction cycle.

ADD to AC

This instruction adds the content of the memory word specified by the effective address to the value of *AC*. The sum is transferred into *AC* and the output carry C_{out} is transferred to the *E* (extended accumulator) flip-flop. The microoperations needed to execute this instruction are

$$D_1T_4: \quad DR \leftarrow M[AR]$$
$$D_1T_5: \quad AC \leftarrow AC + DR, \quad E \leftarrow C_{out}, \quad SC \leftarrow 0$$

The same two timing signals, T_4 and T_5, are used again but with operation decoder D_1 instead of D_0, which was used for the AND instruction. After the instruction is fetched from memory and decoded, only one output of the operation decoder will be active, and that output determines the sequence of microoperations that the control follows during the execution of a memory-reference instruction.

LDA: Load to AC

This instruction transfers the memory word specified by the effective address to *AC*. The microoperations needed to execute this instruction are

$$D_2T_4: \quad DR \leftarrow M[AR]$$
$$D_2T_5: \quad AC \leftarrow DR, \quad SC \leftarrow 0$$

Looking back at the bus system shown in Fig. 5-4 we note that there is no direct path from the bus into *AC*. The adder and logic circuit receive information

5.6---:) https://github.com/AvinashShrivastav/MATHEMATICS-FOR-COMPUTING

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$$D_0T_5: \quad AC \leftarrow AC \wedge DR, \quad SC \leftarrow 0$$

The control function for this instruction uses the operation decoder D_0 since this output of the decoder is active when the instruction has an AND operation whose binary code value is 000. Two timing signals are needed to execute the instruction. The clock transition associated with timing signal T_4 transfers the operand from memory into *DR*. The clock transition associated with the next timing signal T_5 transfers to *AC* the result of the AND logic operation between the contents of *DR* and *AC*. The same clock transition clears *SC* to 0, transferring control to timing signal T_0 to start a new instruction cycle.

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$$D_1T_4: \quad DR \leftarrow M[AR]$$
$$D_1T_5: \quad AC \leftarrow AC + DR, \quad E \leftarrow C_{out}, \quad SC \leftarrow 0$$

The same two timing signals, T_4 and T_5, are used again but with operation decoder D_1 instead of D_0, which was used for the AND instruction. After the instruction is fetched from memory and decoded, only one output of the operation decoder will be active, and that output determines the sequence of microoperations that the control follows during the execution of a memory-reference instruction.

LDA: Load to AC

This instruction transfers the memory word specified by the effective address to *AC*. The microoperations needed to execute this instruction are

$$D_2T_4: \quad DR \leftarrow M[AR]$$
$$D_2T_5: \quad AC \leftarrow DR, \quad SC \leftarrow 0$$

Looking back at the bus system shown in Fig. 5-4 we note that there is no direct path from the bus into *AC*. The adder and logic circuit receive information

from *DR* which can be transferred into *AC*. Therefore, it is necessary to read the memory word into *DR* first and then transfer the content of *DR* into *AC*. The reason for not connecting the bus to the inputs of *AC* is the delay encountered in the adder and logic circuit. It is assumed that the time it takes to read from memory and transfer the word through the bus as well as the adder and logic circuit is more than the time of one clock cycle. By not connecting the bus to the inputs of *AC* we can maintain one clock cycle per microoperation.

STA: Store AC

This instruction stores the content of *AC* into the memory word specified by the effective address. Since the output of *AC* is applied to the bus and the data input of memory is connected to the bus, we can execute this instruction with one microoperation:

$$D_3T_4: \qquad M[AR] \leftarrow AC, \quad SC \leftarrow 0$$

BUN: Branch Unconditionally

This instruction transfers the program to the instruction specified by the effective address. Remember that *PC* holds the address of the instruction to be read from memory in the next instruction cycle. *PC* is incremented at time T_1 to prepare it for the address of the next instruction in the program sequence. The BUN instruction allows the programmer to specify an instruction out of sequence and we say that the program branches (or jumps) unconditionally. The instruction is executed with one microoperation:

$$D_4T_4: \qquad PC \leftarrow AR, \quad SC \leftarrow 0$$

The effective address from *AR* is transferred through the common bus to *PC*. Resetting *SC* to 0 transfers control to T_0. The next instruction, is then fetched and executed from the memory address given by the new value in *PC*.

BSA: Branch and Save Return Address

This instruction is useful for branching to a portion of the program called a subroutine or procedure. When executed, the BSA instruction stores the address of the next instruction in sequence (which is available in *PC*) into a memory location specified by the effective address. The effective address plus one is then transferred to *PC* to serve as the address of the first instruction in the subroutine. This operation was specified in Table 5-4 with the following register transfer:

$$M[AR] \leftarrow PC, \quad PC \leftarrow AR + 1$$

A numerical example that demonstrates how this instruction is used with a subroutine is shown in Fig. 5-10. The BSA instruction is assumed to be in memory at address 20. The *I* bit is 0 and the address part of the instruction has the binary equivalent of 135. After the fetch and decode phases, *PC* contains 21, which is the address of the next instruction in the program (referred to as the *return address*). *AR* holds the effective address 135. This is shown in part (a) of the figure. The BSA instruction performs the following numerical operation:

return address

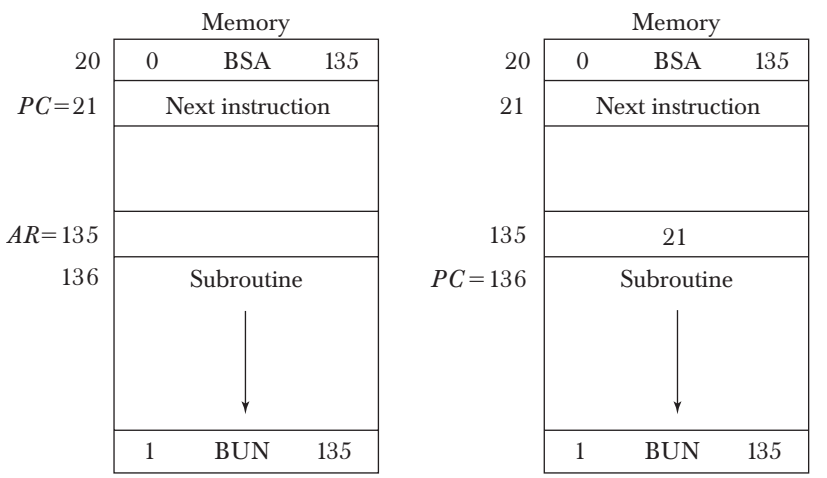
$$M[135] \leftarrow 21, \qquad PC \leftarrow 135 + 1 = 136$$

The result of this operation is shown in part (b) of the figure. The return address 21 is stored in memory location 135 and control continues with the subroutine program starting from address 136. The return to the original program (at address 21) is accomplished by means of an indirect BUN instruction placed at the end of the subroutine. When this instruction is executed, control goes to the indirect phase to read the effective address at location 135, where it finds the previously saved address 21. When the BUN instruction is executed, the effective address 21 is transferred to *PC*. The next instruction cycle finds *PC* with the value 21, so control continues to execute the instruction at the return address.

subroutine call

The BSA instruction performs the function usually referred to as a subroutine call. The indirect BUN instruction at the end of the subroutine performs the function referred to as a subroutine return. In most commercial computers, the return address associated with a subroutine is stored in either a processor register or in a portion of memory called a stack. This is discussed in more detail in Sec. 8-7.

Figure 5-10 Example of BSA instruction execution.



(a) Memory, *PC*, and *AR* at time T_4 (b) Memory and *PC* after execution

It is not possible to perform the operation of the BSA instruction in one clock cycle when we use the bus system of the basic computer. To use the memory and the bus properly, the BSA instruction must be executed with a sequence of two microoperations:

$$D_5T_4: \quad M[AR] \leftarrow PC, \quad AR \leftarrow AR + 1$$
$$D_5T_5: \quad PC \leftarrow AR, \quad SC \leftarrow 0$$

Timing signal T_4 initiates a memory write operation, places the content of *PC* onto the bus, and enables the INR input of *AR*. The memory write operation is completed and *AR* is incremented by the time the next clock transition occurs. The bus is used at T_5 to transfer the content of *AR* to *PC*.

ISZ: Increment and Skip if Zero

This instruction increments the word specified by the effective address, and if the incremented value is equal to 0, *PC* is incremented by 1. The programmer usually stores a negative number (in 2's complement) in the memory word. As this negative number is repeatedly incremented by one, it eventually reaches the value of zero. At that time *PC* is incremented by one in order to skip the next instruction in the program.

Since it is not possible to increment a word inside the memory, it is necessary to read the word into *DR*, increment *DR*, and store the word back into memory. This is done with the following sequence of microoperations:

$$D_6T_4: \quad DR \leftarrow M[AR]$$
$$D_6T_5: \quad DR \leftarrow DR + 1$$
$$D_6T_6: \quad M[AR] \leftarrow DR, \quad \text{if } (DR = 0) \text{ then } (PC \leftarrow PC + 1), \quad SC \leftarrow 0$$

Control Flowchart

A flowchart showing all microoperations for the execution of the seven memory-reference instructions is shown in Fig. 5-11. The control functions are indicated on top of each box. The microoperations that are performed during time T_4, T_5, or T_6 depend on the operation code value. This is indicated in the flowchart by six different paths, one of which the control takes after the instruction is decoded. The sequence counter *SC* is cleared to 0 with the last timing signal in each case. This causes a transfer of control to timing signal T_0 to start the next instruction cycle.

Note that we need only seven timing signals to execute the longest instruction (ISZ). The computer can be designed with a 3-bit sequence counter. The reason for using a 4-bit counter for *SC* is to provide additional timing signals for other instructions that are presented in the problems section.

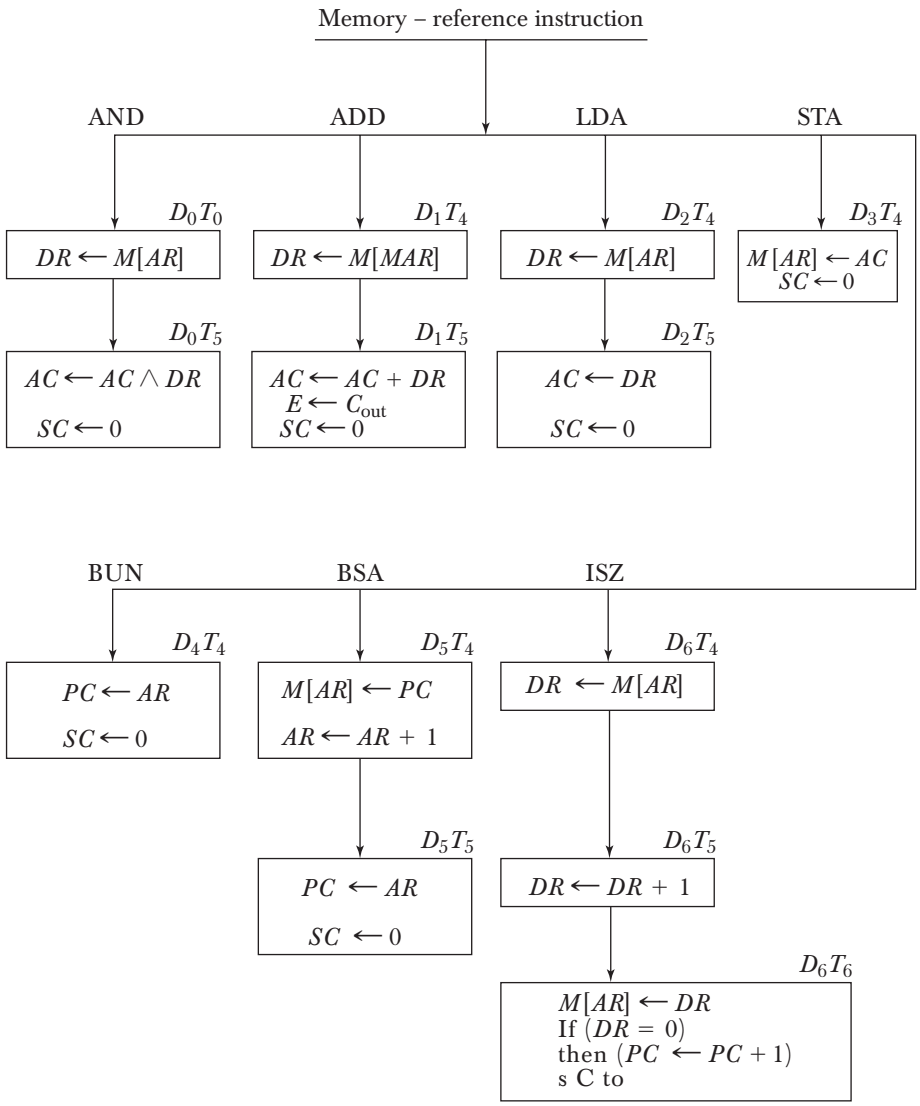


Figure 5-11 Flowchart for memory-reference instructions.

5-7 Input–Output and Interrupt

A computer can serve no useful purpose unless it communicates with the external environment. Instructions and data stored in memory must come from some input device. Computational results must be transmitted to the user through some output device. Commercial computers include many types

of input and output devices. To demonstrate the most basic requirements for input and output communication, we will use as an illustration a terminal unit with a keyboard and printer. Input–output organization is discussed further in Chap. 11.

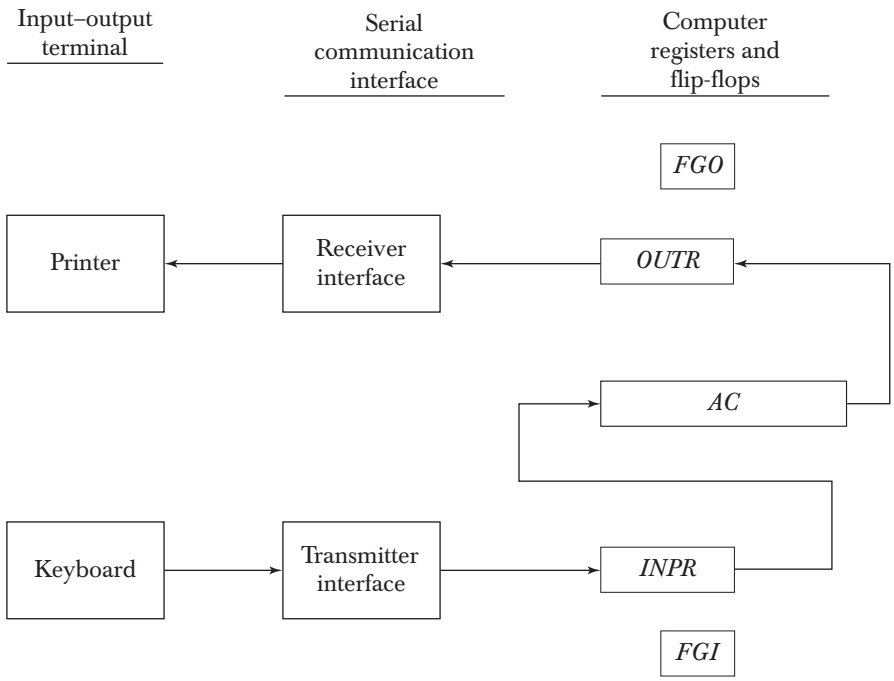
Input–Output Configuration

The terminal sends and receives serial information. Each quantity of information has eight bits of an alphanumeric code. The serial information from the keyboard is shifted into the input register *INPR*. The serial information for the printer is stored in the output register *OUTR*. These two registers communicate with a communication interface serially and with the *AC* in parallel. The input–output configuration is shown in Fig. 5-12. The transmitter interface receives serial information from the keyboard and transmits it to *INPR*. The receiver interface receives information from *OUTR* and sends it to the printer serially. The operation of the serial communication interface is explained in Sec. 11-3.

input register

The input register *INPR* consists of eight bits and holds an alphanumeric input information. The 1-bit input flag *FGI* is a control flip-flop. The flag bit is

Figure 5-12 Input–output configuration.



set to 1 when new information is available in the input device and is cleared to 0 when the information is accepted by the computer. The flag is needed to synchronize the timing rate difference between the input device and the computer. The process of information transfer is as follows. Initially, the input flag *FGI* is cleared to 0. When a key is struck in the keyboard, an 8-bit alphanumeric code is shifted into *INPR* and the input flag *FGI* is set to 1. As long as the flag is set, the information in *INPR* cannot be changed by striking another key. The computer checks the flag bit; if it is 1, the information from *INPR* is transferred in parallel into *AC* and *FGI* is cleared to 0. Once the flag is cleared, new information can be shifted into *INPR* by striking another key.

output register

The output register *OUTR* works similarly but the direction of information flow is reversed. Initially, the output flag *FGO* is set to 1. The computer checks the flag bit; if it is 1, the information from *AC* is transferred in parallel to *OUTR* and *FGO* is cleared to 0. The output device accepts the coded information, prints the corresponding character, and when the operation is completed, it sets *FGO* to 1. The computer does not load a new character into *OUTR* when *FGO* is 0 because this condition indicates that the output device is in the process of printing the character.

Input–Output Instructions

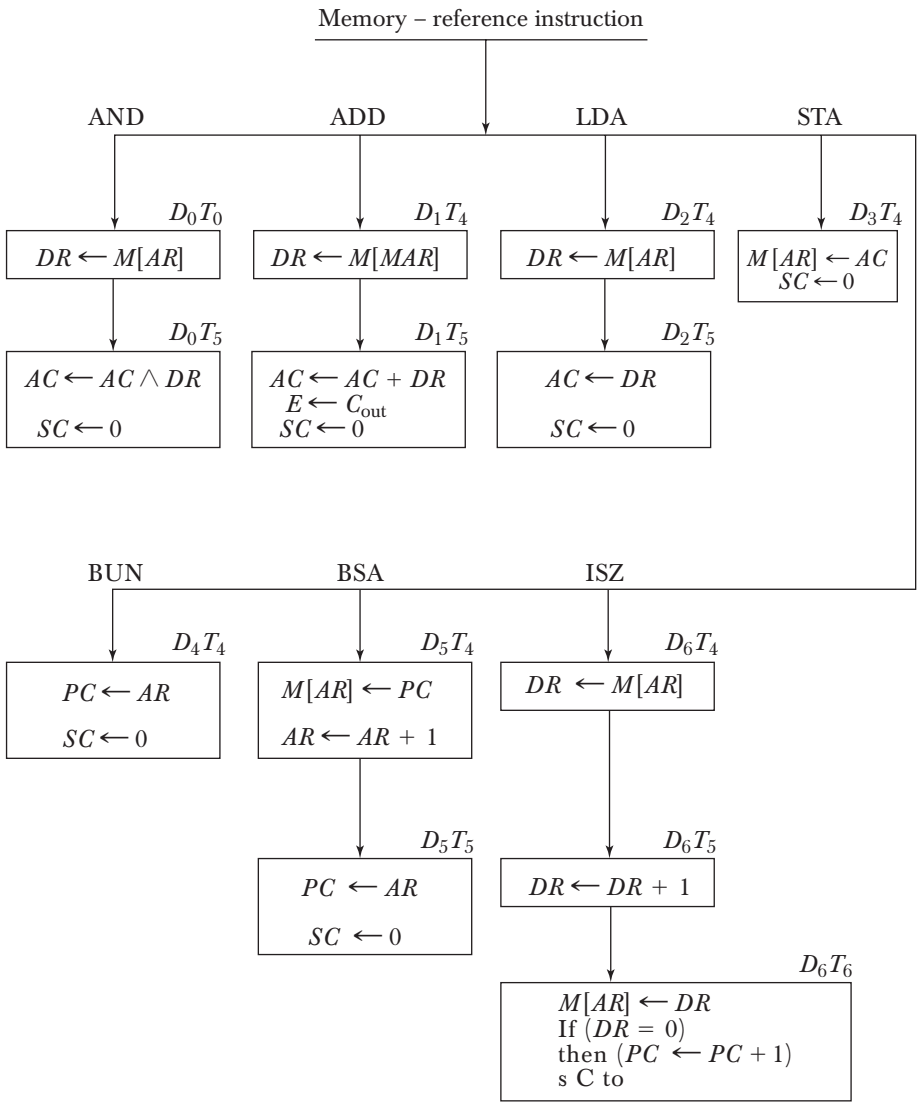
Input and output instructions are needed for transferring information to and from *AC* register, for checking the flag bits, and for controlling the interrupt facility. Input–output instructions have an operation code 1111 and are recognized by the control when $D_7 = 1$ and $I = 1$. The remaining bits of the instruction specify the particular operation. The control functions and microoperations for the input–output instructions are listed in Table 5-5. These instructions are executed with the clock transition associated with timing signal T_3. Each control function needs a Boolean relation D_7IT_3, which we designate for convenience by the symbol p. The control function is distinguished by one of the bits in $IR(6–11)$. By assigning the symbol B_i to bit i of IR, all control functions can

TABLE 5-5 Input–Output Instructions

$D_7IT_3 = p$ (common to all input–output instructions)
$IR(i) = B_i$ [bit in $IR(6–11)$ that specifies the instruction]

	p:	$SC \leftarrow 0$	Clear *SC*
INP	pB_{11}:	$AC(0–7) \leftarrow INPR$, $FGI \leftarrow 0$	Input character
OUT	pB_{10}:	$OUTR \leftarrow AC(0–7)$, $FGO \leftarrow 0$	Output character
SKI	pB_9:	If $(FGI = 1)$ then $(PC \leftarrow PC + 1)$	Skip on input flag
SKO	pB_8:	If $(FGO = 1)$ then $(PC \leftarrow PC + 1)$	Skip on output flag
ION	pB_7:	$IEN \leftarrow 1$	Interrupt enable on
IOF	pB_6:	$IEN \leftarrow 0$	Interrupt enable off

5.7---:) https://github.com/AvinashShrivastav/MATHEMATICS-FOR-COMPUTING



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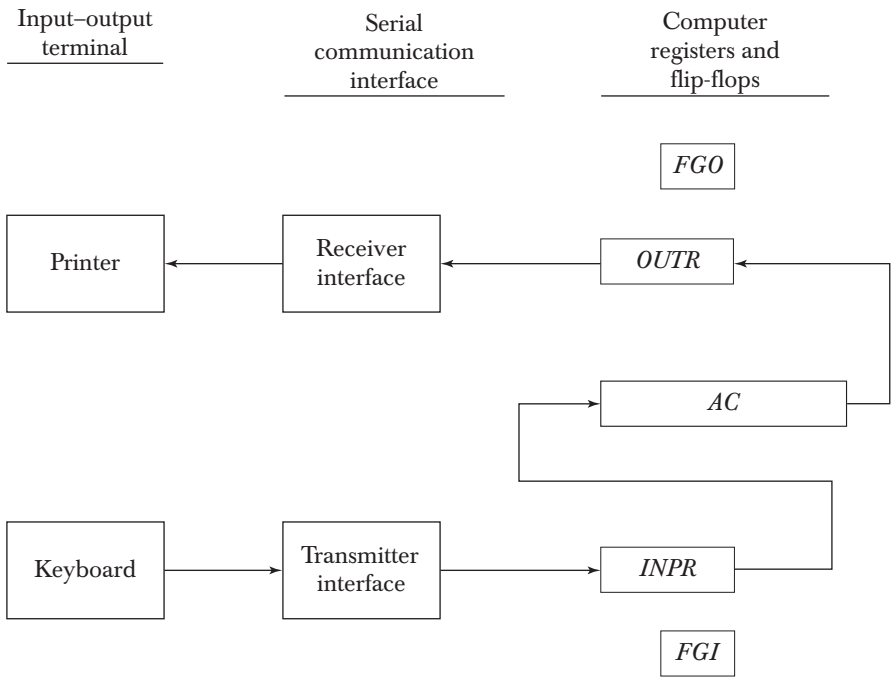

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ION	pB_7:	$IEN \leftarrow 1$	Interrupt enable on
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be denoted by pB_i for $i = 6$ though 11. The sequence counter *SC* is cleared to 0 when $p = D_7IT_3 = 1$.

The INP instruction transfers the input information from *INPR* into the eight low-order bits of *AC* and also clears the input flag to 0. The OUT instruction transfers the eight least significant bits of *AC* into the output register *OUTR* and clears the output flag to 0. The next two instructions in Table 5-5 check the status of the flags and cause a skip of the next instruction if the flag is 1. The instruction that is skipped will normally be a branch instruction to return and check the flag again. The branch instruction is not skipped if the flag is 0. If the flag is 1, the branch instruction is skipped and an input or output instruction is executed. (Examples of input and output programs are given in Sec. 6-8.) The last two instructions set and clear an interrupt enable flip-flop *IEN*. The purpose of *IEN* is explained in conjunction with the interrupt operation.

Program Interrupt

The process of communication just described is referred to as programmed control transfer. The computer keeps checking the flag bit, and when it finds it set, it initiates an information transfer. The difference of information flow rate between the computer and that of the input–output device makes this type of transfer inefficient. To see why this is inefficient, consider a computer that can go through an instruction cycle in 1 μs. Assume that the input–output device can transfer information at a maximum rate of 10 characters per second. This is equivalent to one character every 100,000 μs. Two instructions are executed when the computer checks the flag bit and decides not to transfer the information. This means that at the maximum rate, the computer will check the flag 50,000 times between each transfer. The computer is wasting time while checking the flag instead of doing some other useful processing task.

An alternative to the programmed controlled procedure is to let the external device inform the computer when it is ready for the transfer. In the meantime the computer can be busy with other tasks. This type of transfer uses the interrupt facility. While the computer is running a program, it does not check the flags. However, when a flag is set, the computer is momentarily interrupted from proceeding with the current program and is informed of the fact that a flag has been set. The computer deviates momentarily from what it is doing to take eare of the input or output transfer. It then returns to the current program to continue what it was doing before the interrupt.

The interrupt enable flip-flop *IEN* can be set and cleared with two instructions. When *IEN* is cleared to 0 (with the IOF instruction), the flags cannot interrupt the computer. When *IEN* is set to 1 (with the ION instruction), the computer can be interrupted. These two instructions provide the programmer with the capability of making a decision as to whether or not to use the interrupt facility.

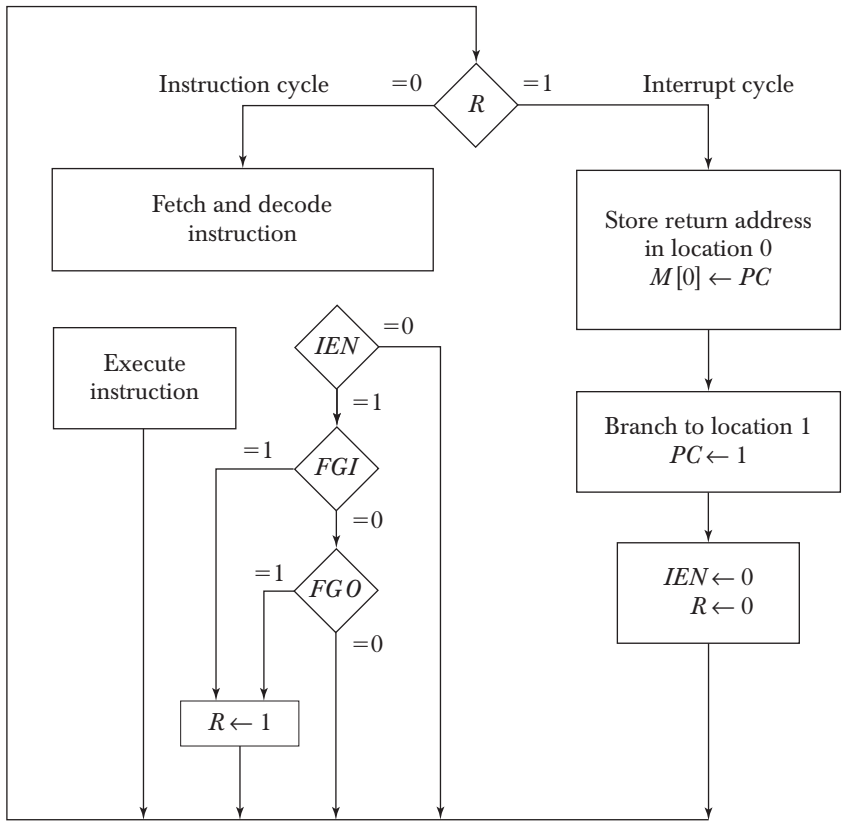


Figure 5-13 Flowchart for interrupt cycle.

The way that the interrupt is handled by the computer can be explained by means of the flowchart of Fig. 5-13. An interrupt flip-flop R is included in the computer. When $R = 0$, the computer goes through an instruction cycle. During the execute phase of the instruction cycle IEN is checked by the control. If it is 0, it indicates that the programmer does not want to use the interrupt, so control continues with the next instruction cycle. If *IEN* is 1, control checks the flag bits. If both flags are 0, it indicates that neither the input nor the output registers are ready for transfer of information. In this case, control continues with the next instruction cycle. If either flag is set to 1 while $IEN = 1$, flip-flop R is set to 1. At the end of the execute phase, control checks the value of R, and if it is equal to 1, it goes to an interrupt cycle instead of an instruction cycle.

interrupt cycle

The interrupt cycle is a hardware implementation of a branch and save return address operation. The return address available in *PC* is stored in a specific location where it can be found later when the program returns to the instruction at which it was interrupted. This location may be a processor

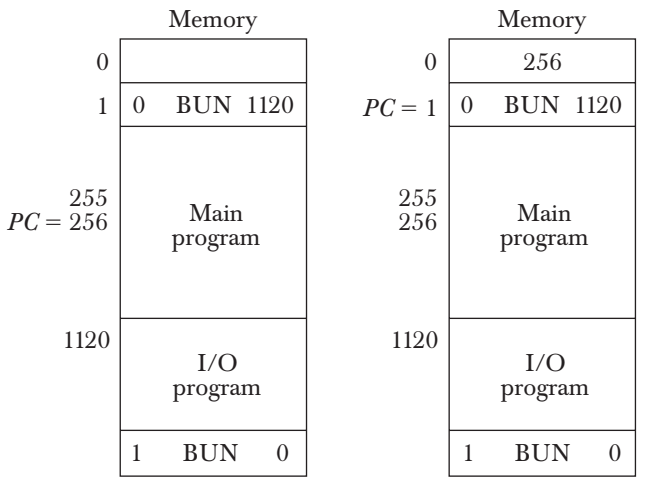
register, a memory stack, or a specific memory location. Here we choose the memory location at address 0 as the place for storing the return address. Control then inserts address 1 into *PC* and clears *IEN* and *R* so that no more interruptions can occur until the interrupt request from the flag has been serviced.

An example that shows what happens during the interrupt cycle is shown in Fig. 5-14. Suppose that an interrupt occurs and *R* is set to 1 while the control is executing the instruction at address 255. At this time, the return address 256 is in *PC*. The programmer has previously placed an input–output service program in memory starting from address 1120 and a BUN 1120 instruction at address 1. This is shown in Fig. 5-14(a).

When control reaches timing signal T_0 and finds that $R = 1$, it proceeds with the interrupt cycle. The content of *PC* (256) is stored in memory location 0, *PC* is set to 1, and *R* is cleared to 0. At the beginning of the next instruction cycle, the instruction that is read from memory is in address 1 since this is the content of *PC*. The branch instruction at address 1 causes the program to transfer to the input–output service program at address 1120. This program checks the flags, determines which flag is set, and then transfers the required input or output information. Once this is done, the instruction ION is executed to set *IEN* to 1 (to enable further interrupts), and the program returns to the location where it was interrupted. This is shown in Fig. 5-14(b).

The instruction that returns the computer to the original place in the main program is a branch indirect instruction with an address part of 0. This instruction is placed at the end of the I/O service program. After this instruction

Figure 5-14 Demonstration of the interrupt cycle.



(a) Before interrupt (b) After interrupt cycle

is read from memory during the fetch phase, control goes to the indirect phase (because $I = 1$) to read the effective address. The effective address is in location 0 and is the return address that was stored there during the previous interrupt cycle. The execution of the indirect BUN instruction results in placing into *PC* the return address from location 0.

Interrupt Cycle

We are now ready to list the register transfer statements for the interrupt cycle. The interrupt cycle is initiated after the last execute phase if the interrupt flip-flop *R* is equal to 1. This flip-flop is set to 1 if *IEN* = 1 and either *FGI* or *FGO* are equal to 1. This can happen with any clock transition except when timing signals T_0, T_1, or T_2 are active. The condition for setting flip-flop *R* to 1 can be expressed with the following register transfer statement:

$$T_0' T_1' T_2' (IEN)(FGI + FGO): \quad R \leftarrow 1$$

modified fetch phase

The symbol + between *FGI* and *FGO* in the control function designates a logic OR operation. This is ANDed with *IEN* and $T_0' T_1' T_2'$.

We now modify the fetch and decode phases of the instruction cycle. Instead of using only timing signals T_0, T_1, and T_2 (as shown in Fig. 5-9) we will AND the three timing signals with R' so that the fetch and decode phases will be recognized from the three control functions $R' T_0$, $R' T_1$, and $R' T_2$. The reason for this is that after the instruction is executed and *SC* is cleared to 0, the control will go through a fetch phase only if $R = 0$. Otherwise, if $R = 1$, the control will go through an interrupt cycle. The interrupt cycle stores the return address (available in *PC*) into memory location 0, branches to memory location 1, and clears *IEN*, *R*, and *SC* to 0. This can be done with the following sequence of microoperations:

$$\begin{aligned}
RT_0: &\quad AR \leftarrow 0, \quad TR \leftarrow PC \\
RT_1: &\quad M[AR] \leftarrow TR, \quad PC \leftarrow 0 \\
RT_2: &\quad PC \leftarrow PC + 1, \quad IEN \leftarrow 0, \quad R \leftarrow 0, \quad SC \leftarrow 0
\end{aligned}$$

During the first timing signal *AR* is cleared to 0, and the content of *PC* is transferred to the temporary register *TR*. With the second timing signal, the return address is stored in memory at location 0 and *PC* is cleared to 0. The third timing signal increments *PC* to 1, clears *IEN* and *R*, and control goes back to T_0 by clearing *SC* to 0. The beginning of the next instruction cycle has the condition $R' T_0$ and the content of *PC* is equal to 1. The control then goes through an instruction cycle that fetches and executes the BUN instruction in location 1.

5-8 Complete Computer Description

flowchart for basic computer

The final flowchart of the instruction cycle, including the interrupt cycle for the basic computer, is shown in Fig. 5-15. The interrupt flip-flop R may be set at any time during the indirect or execute phases. Control returns to timing signal T_0 after SC is cleared to 0. If $R = 1$, the computer goes through an interrupt cycle. If $R = 0$, the computer goes through an instruction cycle. If the instruction is one of the memory-reference instructions, the computer first checks if there is an indirect address and then continues to execute the decoded instruction according to the flowchart of Fig. 5-11. If the instruction is one of the register-reference instructions, it is executed with one of the microoperations listed in Table 5-3. If it is an input–output instruction, it is executed with one of the microoperations listed in Table 5-5.

Instead of using a flowchart, we can describe the operation of the computer with a list of register transfer statements. This is done by accumulating all the control functions and microoperations in one table. The entries in the table are taken from Figs. 5-11 and 5-16, and Tables 5-3 and 5-5.

The control functions and microoperations for the entire computer are summarized in Table 5-6. The register transfer statements in this table describe in a concise form the internal organization of the basic computer. They also give all the information necessary for the design of the logic circuits of the computer. The control functions and conditional control statements listed in the table formulate the Boolean functions for the gates in the control unit. The list of microoperations specifies the type of control inputs needed for the registers and memory. A register transfer language is useful not only for describing the internal organization of a digital system but also for specifying the logic circuits needed for its design.

5-9 Design of Basic Computer

The basic computer consists of the following hardware components:

1. A memory unit with 4096 words of 16 bits each
2. Nine registers: *AR*, *PC*, *DR*, *AC*, *IR*, *TR*, *OUTR*, *INPR*, and *SC*
3. Seven flip-flops: *I*, *S*, *E*, *R*, *IEN*, *FGI*, and *FGO*
4. Two decoders: a 3×8 operation decoder and a 4×16 timing decoder
5. A 16-bit common bus
6. Control logic gates
7. Adder and logic circuit connected to the input of *AC*

The functional block diagram of the hypothetic BASIC computer is as shown below:

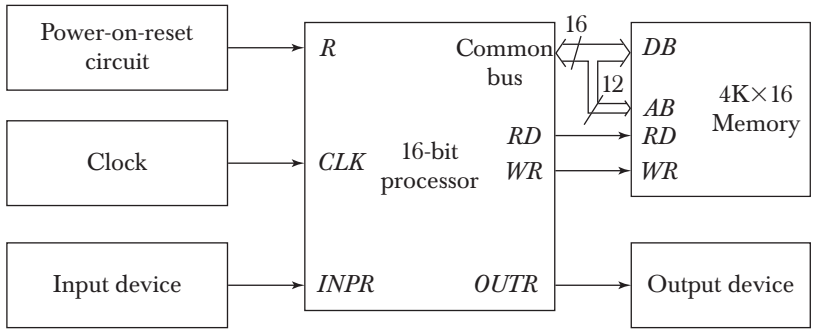


Figure 5-15 Flow chart for hypothetic basic computer.

The memory unit is a standard component that can be obtained readily from a commercial source. The registers are of the type shown in Fig. 2-11 and are similar to integrated circuit type 74163. The flip-flops can be either of the *D* or *JK* type, as described in Sec. 1-6. The two decoders are standard components similar to the ones presented in Sec. 2-2. The common bus system can be constructed with sixteen 8 × 1 multiplexers in a configuration similar to the one shown in Fig. 4-3. We are now going to show how to design the control logic gates. The next section deals with the design of the adder and logic circuit associated with *AC*.

Control Logic Gates

The block diagram of the control logic gates is shown in Fig. 5-6. The inputs to this circuit come from the two decoders, the *I* flip-flop, and bits 0 through 11 of *IR*. The other inputs to the control logic are: *AC* bits 0 through 15 to check if $AC = 0$ and to detect the sign bit in $AC(15)$; *DR* bits 0 through 15 to check if $DR = 0$; and the values of the seven flip-flops.

control unit

The outputs of the control logic circuit are:

1. Signals to control the inputs of the nine registers
2. Signals to control the read and write inputs of memory
3. Signals to set, clear, or complement the flip-flops
4. Signals for S_2, S_1, and S_0 to select a register for the bus
5. Signals to control the *AC* adder and logic circuit

The specifications for the various control signals can be obtained directly from the list of register transfer statements in Table 5-6.

Control of Registers and Memory

The registers of the computer connected to a common bus system are shown in Fig. 5-4. The control inputs of the registers are LD (load), INR (increment),

9.2---:) https://github.com/AvinashShrivastav/MATHEMATICS-FOR-COMPUTING

characteristics of the computer system rather than its operational and structural interconnections. One type of parallel processing that does not fit Flynn's classification is pipelining. The only two categories used from this classification are SIMD array processors discussed in Sec. 9-7, and MIMD multiprocessors presented in Chap. 13.

Parallel processing computers are required to meet the demands of large scale computations in many scientific, engineering, military, medical, artificial intelligence, and basic research areas. The following are some representative applications of parallel processing computers: Numerical weather forecasting, computational aerodynamics, finite-element analysis, remote-sensing applications, genetic engineering, computer-asseted tomography, and weapon research and defence.

In this chapter we consider parallel processing under the following main topics:

1. Pipeline processing
2. Vector processing
3. Array processors

Pipeline processing is an implementation technique where arithmetic suboperations or the phases of a computer instruction cycle overlap in execution. Vector processing deals with computations involving large vectors and matrices. Array processors perform computations on large arrays of data.

9-2 Pipelining

Pipelining is a technique of decomposing a sequential process into suboperations, with each subprocess being executed in a special dedicated segment that operates concurrently with all other segments. A pipeline can be visualized as a collection of processing segments through which binary information flows. Each segment performs partial processing dictated by the way the task is partitioned. The result obtained from the computation in each segment is transferred to the next segment in the pipeline. The final result is obtained after the data have passed through all segments. The name "pipeline" implies a flow of information analogous to an industrial assembly line. It is characteristic of pipelines that several computations can be in progress in distinct segments at the same time. The overlapping of computation is made possible by associating a register with each segment in the pipeline. The registers provide isolation between each segment so that each can operate on distinct data simultaneously.

Perhaps the simplest way of viewing the pipeline structure is to imagine that each segment consists of an input register followed by a combinational circuit. The register holds the data and the combinational circuit performs the suboperation in the particular segment. The output of the combinational circuit in a given segment is applied to the input register of the next segment. A clock is applied to all registers after enough time has elapsed to perform all

segment activity. In this way the information flows through the pipeline one step at a time.

an example

The pipeline organization will be demonstrated by means of a simple example. Suppose that we want to perform the combined multiply and add operations with a stream of numbers.

$$A_i * B_i + C_i \quad \text{for } i = 1, 2, 3, \ldots, 7$$

Each suboperation is to be implemented in a segment within a pipeline. Each segment has one or two registers and a combinational circuit as shown in Fig. 9-2. $R1$ through $R5$ are registers that receive new data with every clock pulse. The multiplier and adder are combinational circuits. The suboperations performed in each segment of the pipeline are as follows:

$R1 \leftarrow A_i, \quad R2 \leftarrow B_i$	Input A_i and B_i
$R3 \leftarrow R1 * R2, \quad R4 \leftarrow C_i$	Multiply and input C_i
$R5 \leftarrow R3 + R4$	Add C_i to product

The five registers are loaded with new data every clock pulse. The effect of each clock is shown in Table 9-1. The first clock pulse transfers A_1 and B_1 into

Figure 9-2 Example or pipeline processing.

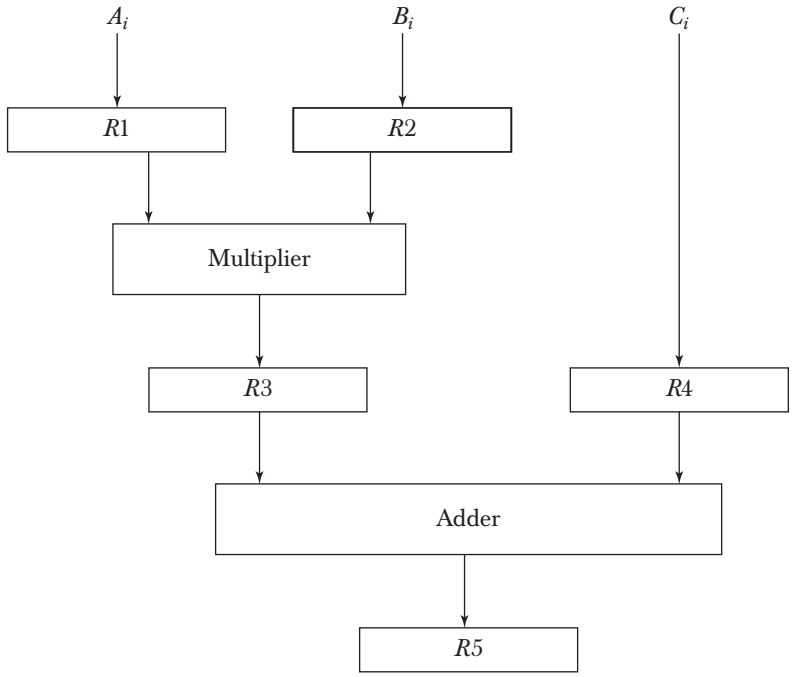


TABLE 9-1 Content of Registers in Pipeline Example

Clock Pulse Number	Segment 1		Segment 2		Segment 3
	*R*1	*R*2	*R*3	*R*4	*R*5
1	A_1	B_1	–	–	–
2	A_2	B_2	$A_1 * B_1$	C_1	–
3	A_3	B_3	$A_2 * B_2$	C_2	$A_1 * B_1 + C_1$
4	A_4	B_4	$A_3 * B_3$	C_3	$A_2 * B_2 + C_2$
5	A_5	B_5	$A_4 * B_4$	C_4	$A_3 * B_3 + C_3$
6	A_6	B_6	$A_5 * B_5$	C_5	$A_4 * B_4 + C_4$
7	A_7	B_7	$A_6 * B_6$	C_6	$A_5 * B_5 + C_5$
8	–	–	$A_7 * B_7$	C_7	$A_6 * B_6 + C_6$
9	–	–	–	–	$A_7 * B_7 + C_7$

*R*1 and *R*2. The second clock pulse transfers the product of *R*1 and *R*2 into *R*3 and C_1 into *R*4. The same clock pulse transfers A_2 and B_2 into *R*1 and *R*2. The third clock pulse operates on all three segments simultaneously. It places A_3 and B_3 into *R*1 and *R*2, transfers the product of *R*1 and *R*2 into *R*3, transfers C_2 into *R*4, and places the sum of *R*3 and *R*4 into *R*5. It takes three clock pulses to fill up the pipe and retrieve the first output from *R*5. From there on, each clock produces a new output and moves the data one step down the pipeline. This happens as long as new input data flow into the system. When no more input data are available, the clock must continue until the last output emerges out of the pipeline.

General Considerations

Any operation that can be decomposed into a sequence of suboperations of about the same complexity can be implemented by a pipeline processor. The technique is efficient for those applications that need to repeat the same task many times with different sets of data. The general structure of a four-segment pipeline is illustrated in Fig. 9-3. The operands pass through all four segments in a fixed sequence. Each segment consists of a combinational circuit S_i that performs a suboperation over the data stream flowing through the pipe. The segments are separated by registers R_i that hold the intermediate results between the stages. Information flows between adjacent stages under the control of a common clock applied to all the registers simultaneously. We define

task a *task* as the total operation performed going through all the segments in the pipeline.

space-time diagram The behavior of a pipeline can be illustrated with a *space-time* diagram. This is a diagram that shows the segment utilization as a function of time. The space-time diagram of a four-segment pipeline is demonstrated in Fig. 9-4. The horizontal axis displays the time in clock cycles and the vertical axis gives

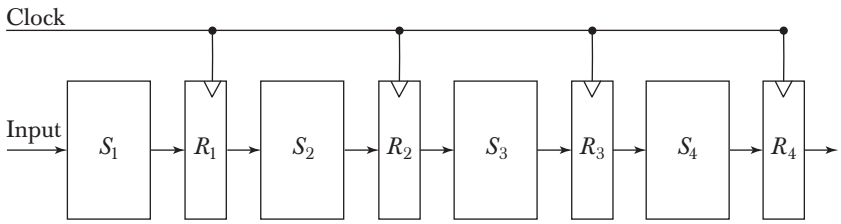


Figure 9-3 Four-segment pipeline.

the segment number. The diagram shows six tasks T_1 through T_6 executed in four segments. Initially, task T_1 is handled by segment 1. After the first clock, segment 2 is busy with T_1, while segment 1 is busy with task T_2. Continuing in this manner, the first task T_1 is completed after the fourth clock cycle. From then on, the pipe completes a task every clock cycle. No matter how many segments there are in the system, once the pipeline is full, it takes only one clock period to obtain an output.

Now consider the case where a k-segment pipeline with a clock cycle time t_p is used to execute n tasks. The first task T_1 requires a time equal to kt_p to complete its operation since there are k segments in the pipe. The remaining $n - 1$ tasks emerge from the pipe at the rate of one task per clock cycle and they will be completed after a time equal to $(n - 1)t_p$. Therefore, to complete n tasks using a k-segment pipeline requires $k + (n - 1)$ clock cycles. For example, the diagram of Fig. 9-4 shows four segments and six tasks. The time required to complete all the operations is $4 + (6 - 1) = 9$ clock cycles, as indicated in the diagram.

Next consider a nonpipeline unit that performs the same operation and takes a time equal to t_n to complete each task. The total time required for n tasks is nt_n. The speedup of a pipeline processing over an equivalent nonpipeline processing is defined by the ratio

speedup

$$S = \frac{nt_n}{(k + n - 1)t_p}$$

Figure 9-4 Space-time diagram for pipeline.

	1	2	3	4	5	6	7	8	9	→ Clock cycles
Segment: 1	T_1	T_2	T_3	T_4	T_5	T_6				
2		T_1	T_2	T_3	T_4	T_5	T_6			
3			T_1	T_2	T_3	T_4	T_5	T_6		
4				T_1	T_2	T_3	T_4	T_5	T_6	

As the number of tasks increases, n becomes much larger than $k - 1$, and $k + n - 1$ approaches the value of n. Under this condition, the speedup becomes

$$S = \frac{t_n}{t_p}$$

If we assume that the time it takes to process a task is the same in the pipeline and nonpipeline circuits, we will have $t_n = kt_p$. Including this assumption, the speedup reduces to

$$S = \frac{Kt_p}{t_p} = K$$

This shows that the theoretical maximum speedup that a pipeline can provide is k, where k is the number of segments in the pipeline.

To clarify the meaning of the speedup ratio, consider the following numerical example. Let the time it takes to process a suboperation in each segment be equal to $t_p = 20$ ns. Assume that the pipeline has $k = 4$ segments and executes $n = 100$ tasks in sequence. The pipeline system will take $(k + n - 1)\ t_p = (4 + 99) \times 20 = 2060$ ns to complete. Assuming that $t_n = kt_p = 4 \times 20 = 80$ ns, a nonpipeline system requires $nkt_p = 100 \times 80 = 8000$ ns to complete the 100 tasks. The speedup ratio is equal to 8000/2060 = 3.88. As the number of tasks increases, the speedup will approach 4, which is equal to the number of segments in the pipeline. If we assume that $t_n = 60$ ns, the speedup becomes 60/20 = 3.

To duplicate the theoretical speed advantage of a pipeline process by means of multiple functional units, it is necessary to construct k identical units that will be operating in parallel. The implication is that a k-segment pipeline processor can be expected to equal the performance of k copies of an equivalent nonpipeline circuit under equal operating conditions. This is illustrated in Fig. 9-5, where four identical circuits are connected in parallel. Each P circuit performs the same task of an equivalent pipeline circuit. Instead of operating with the input data in sequence as in a pipeline, the parallel circuits accept four input data items simultaneously and perform four tasks at the same rime. As far as the speed of operation is concerned, this is equivalent to a four segment pipeline. Note that the four-unit circuit of Fig. 9-5 constitutes a single-instruction multiple-data (SIMD) organization since the same instruction is used to operate on multiple data in parallel.

There are various reasons why the pipeline cannot operate at its maximum theoretical rate. Different segments may take different times to complete their suboperation. The clock cycle must be chosen to equal the time delay of the segment with the maximum propagation time. This causes all other

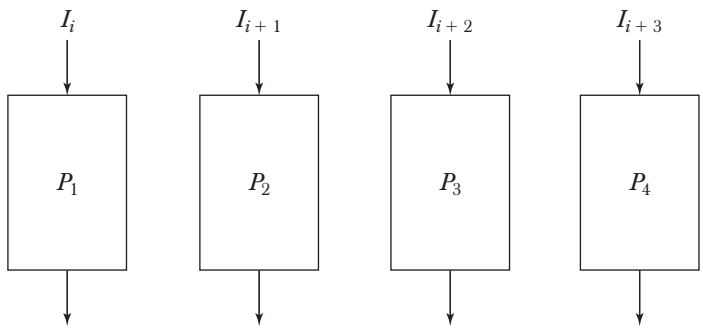


Figure 9-5 Multiple functional units in parallel.

segments to waste time while waiting for the next clock. Moreover, it is not always correct to assume that a nonpipe circuit has the same time delay as that of an equivalent pipeline circuit. Many of the intermediate registers will not be needed in a single-unit circuit, which can usually be constructed entirely as a combinational circuit. Nevertheless, the pipeline technique provids a faster operation over a purely serial sequence even though the maximum theoretical speed is never fully achieved.

There are two areas of computer design where the pipeline organization is applicable. An *arithmetic pipeline* divides an arithmetic operation into suboperations for execution in the pipeline segments. An *instruction pipeline* operates on a stream of instructions by overlapping the fetch, decode, and execute phases of the instruction cycle. The two types of pipelines are explained in the following sections.

9-3 Arithmetic Pipeline

Pipeline arithmetic units are usually found in very high speed computers. They are used to implement floating-point operations, multiplication of fixed-point numbers, and similar computations encountered in scientific problems. A pipeline multiplier is essentially an array multiplier as described in Fig. 10-10, with special adders designed to minimize the carry propagation time through the partial products. Floating-point operations are easily decomposed into suboperations as demonstrated in Sec. 10-5. We will now show an example of a pipeline unit for floating-point addition and subtraction.

The inputs to the floating-point adder pipeline are two normalized floating-point binary numbers.

$$X = A \times 2^a$$
$$Y = B \times 2^b$$

A and B are two fractions that represent the mantissas and a and b are the exponents. The floating-point addition and subtraction can be performed in four segments, as shown in Fig. 9-6. The registers labeled R are placed between the segments to store intermediate results. The suboperations that are performed in the four segments are:

1. Compare the exponents.
2. Align the mantissas.
3. Add or subtract the mantissas.
4. Normalize the result.

This follows the procedure outlined in the flowchart of Fig. 10-15 but with some variations that are used to reduce the execution time of the suboperations. The exponents are compared by subtracting them to determine their difference. The larger exponent is chosen as the exponent of the result. The exponent difference determines how many times the mantissa associated with the smaller exponent must be shifted to the right. This produces an alignment of the two mantissas. It should be noted that the shift must be designed as a combinational circuit to reduce the shift time. The two mantissas are added or subtracted in segment 3. The result is normalized in segment 4. When an overflow occurs, the mantissa of the sum or difference is shifted right and the exponent incremented by one. If an underflow occurs, the number of leading zeros in the mantissa determines the number of left shifts in the mantissa and the number that must be subtracted from the exponent.

The following numerical example may clarify the suboperations performed in each segment. For simplicity, we use decimal numbers, although Fig. 9-6 refers to binary numbers. Consider the two normalized floating-point numbers:

$$X = 0.9504 \times 10^3$$
$$Y = 0.8200 \times 10^2$$

The two exponents are subtracted in the first segment to obtain $3 - 2 = 1$. The larger exponent 3 is chosen as the exponent of the result. The next segment shifts the mantissa of Y to the right to obtain

$$X = 0.9504 \times 10^3$$
$$Y = 0.0820 \times 10^3$$

This aligns the two mantissas under the same exponent. The addition of the two mantissas in segment 3 produces the sum

$$Z = 1.0324 \times 10^3$$

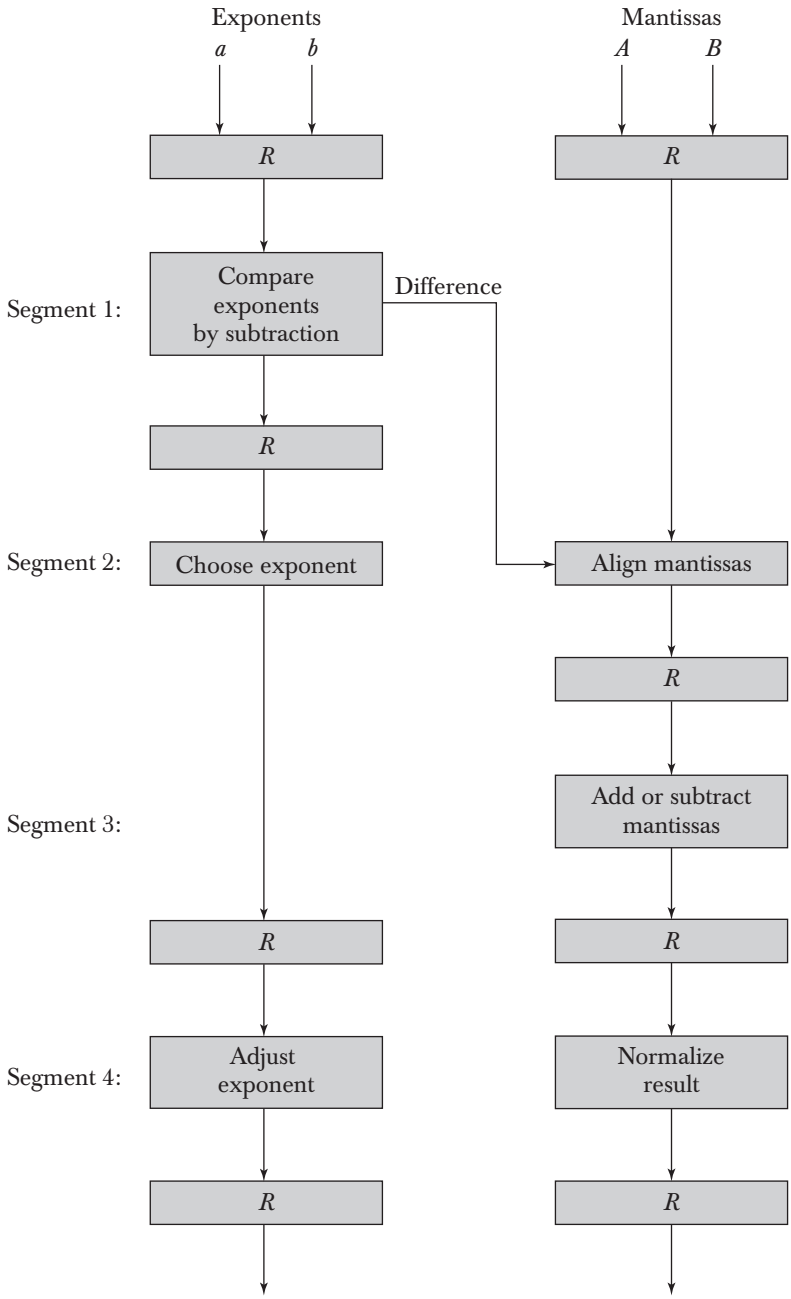


Figure 9-6 Pipeline for floating-point addition and subtraction.