

GUIDELINES of B.Sc. (H) COMPUTER SCIENCE COMPUTER SYSTEM ARCHITECTURE

(Under NEP Scheme 2022)

Semester I

Core Course - II

Semester	DSC No.	Title	L	T*	P*	Total credits	Pre- requisites
I	DSC-02	Computer System Architecture	3	0	1	4	None

S. No	Unit Name	Chapter Number and Name	Section Numbers	Referen ce	No. of Lectures*	Week No.	Chapter wise Weightage* (Marks)
1	Unit 1: Digital Logic Circuits	Ch 1: Digital Logic Circuits	1.1, 1.2, 1.3, 1.4, 1.5, 1.6 1.7 (up to pg. 28)		6	1-2	14
	Unit 2: Digital	Ch 2: Digital Components	2.2, 2.3, 2.7		5		6
2	Components (Fundamental building blocks):	Ch 4: Register Transfer and Micro-operations	4.4 (up to fig. 4.7)		4	3-5	5
3	Unit 3: Data Representation and Basic Computer Arithmetic	Ch 3: Data Representation	3.1, 3.2, 3.3	[1]	6	6-7	8
4	Unit 4: Basic Computer Organization and Design	Ch 5: Basic Computer Organization and Design	5.1, 5.2, 5.3, 5.4 (up to pg. 137), 5.5, 5.6, 5.7		10	8-11	15

		Ch 9: Pipeline and Vector Processing	9.2		2		4
	Unit 5: Processors:	Ch 8: Central Processing Unit	8.1, 8.2, 8.3 (up to pg. 247), 8.5, 8.8 (only characteristics, i.e., pg. 282 – 284)		4		10
5		Ch-7: Multicores, Multiprocessors, and Clusters	7.1 (page 632-Introduction of Multicore Processor) 7.7 (page 654-656) Characteristics of GPU Vs. CPU	[2]	1	12-13	3
6	Unit 6: Memory and Input-Output Organization	Ch 11: Input Output Organization	11.2 (up to pg-388), 11.4, 11.6 (up to pg-416)	[1]	6	14-15	8
	organization	Ch 12: Memory Organization	12.1 (up to pg-446)	[-]	1	1. 20	2

^{*}The number of lectures and chapter wise weightage may be treated as indicative only.

References:

- [1] Computer System Architecture: Morris M. Mano (Pearson Education, 3rd Edition)
- [2] Patterson and John L. Hennessy. "Computer Organization and Design: The Hardware/Software interface", 5th edition, Elsevier, 2012.





CHAPTER ONE

Digital Logic Circuits

IN THIS CHAPTER

- 1-1 Digital Computers
- 1-2 Logic Gates
- 1-3 Boolean Algebra
- 1-4 Map Simplification
- 1-5 Combinational Circuits
- 1-6 Flip-Flops
- 1-7 Sequential Circuits

1-1 Digital Computers

The digital computer is a digital system that performs various computational tasks. The word *digital* implies that the information in the computer is represented by variables that take a limited number of discrete values. These values are processed internally by components that can maintain a limited number of discrete states. The decimal digits 0, 1, 2, . . . , 9, for example, provide 10 discrete values. The first electronic digital computers, developed in the late 1940s, were used primarily for numerical computations. In this case the discrete elements are the digits. From this application the term *digital computer* has emerged. In practice, digital computers function more reliably if only two states are used. Because of the physical restriction of components, and because human logic tends to be binary (i.e., true-or-false, yes-or-no statements), digital components that are constrained to take discrete values are further constrained to take only two values and are said to be *binary*.

Digital computers use the binary number system, which has two digits: 0 and 1. A binary digit is called a *bit*. Information is represented in digital computers in groups of bits. By using various coding techniques, groups of bits can be made to represent not only binary numbers but also other discrete symbols, such as decimal digits or letters of the alphabet. By judicious use of binary arrangements and by using various coding techniques, the groups of bits are used to develop complete sets of instructions for performing various types of computations.

In contrast to the common decimal numbers that employ the base 10 system, binary numbers use a base 2 system with two digits: 0 and 1. The decimal equivalent of a binary number can be found by expanding it into a power series with a base of 2. For example, the binary number 1001011 represents a quantity that can be converted to a decimal number by multiplying each bit by the base 2 raised to an integer power as follows:

$$1 \times 2^6 + 0 \times 2^5 + 0 \times 2^4 + 1 \times 2^3 + 0 \times 2^2 + 1 \times 2^1 + 1 \times 2^0 = 75$$

The seven bits 1001011 represent a binary number whose decimal equivalent is 75. However, this same group of seven bits represents the letter K when used in conjunction with a binary code for the letters of the alphabet. It may also represent a control code for specifying some decision logic in a particular digital computer. In other words, groups of bits in a digital computer are used to represent many different things. This is similar to the concept that the same letters of an alphabet are used to construct different languages, such as English and French.

A computer system is sometimes subdivided into two functional entities: hardware and software. The hardware of the computer consists of all the electronic components and electromechanical devices that comprise the physical entity of the device. Computer software consists of the instructions and data that the computer manipulates to perform various data-processing tasks. A sequence of instructions for the computer is called a *program*. The data that are manipulated by the program constitute the *data base*.

A computer system is composed of its hardware and the system software available for its use. The system software of a computer consists of a collection of programs whose purpose is to make more effective use of the computer. The programs included in a systems software package are referred to as the operating system. They are distinguished from application programs written by the user for the purpose of solving particular problems. For example, a high-level language program written by a user to solve particular data-processing needs is an application program, but the compiler that translates the high-level language program to machine language is a system program. The customer who buys a computer system would need, in addition to the hardware, any available software needed for effective operation of the computer. The system software is an indispensable part of a total computer system. Its function is to compensate for the differences that exist between user needs and the capability of the hardware.

The hardware of the computer is usually divided into three major parts, as shown in Fig. 1-1. The central processing unit (CPU) contains an arithmetic and logic unit for manipulating data, a number of registers for storing data, and control circuits for fetching and executing instructions. The memory of a computer contains storage for instructions and data. It is called a random-access memory (RAM) because the CPU can access any location in memory at random and retrieve the binary information within a fixed interval of time. The input and

program

computer hardware

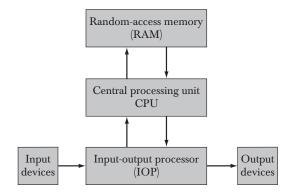


Figure 1-1 Block diagram of a digital computer.

output processor (IOP) contains electronic circuits for communicating and controlling the transfer of information between the computer and the outside world. The input and output devices connected to the computer include keyboards, printers, terminals, magnetic disk drives, and other communication devices.

This book provides the basic knowledge necessary to understand the hardware operations of a computer system. The subject is sometimes considered from three different points of view, depending on the interest of the investigator. When dealing with computer hardware it is customary to distinguish between what is referred to as computer organization, computer design, and computer architecture.

Computer organization is concerned with the way the hardware components operate and the way they are connected together to form the computer system. The various components are assumed to be in place and the task is to investigate the organizational structure to verify that the computer parts operate as intended.

Computer design is concerned with the hardware design of the computer. Once the computer specifications are formulated, it is the task of the designer to develop hardware for the system. Computer design is concerned with the determination of what hardware should be used and how the parts should be connected. This aspect of computer hardware is sometimes referred to as computer implementation.

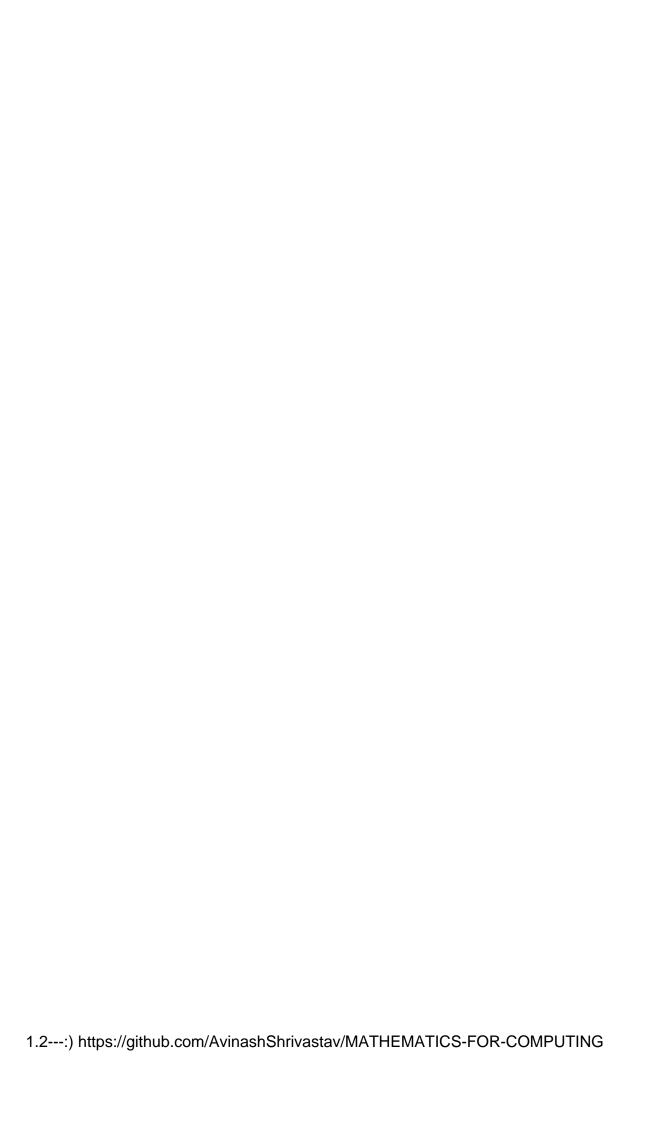
Computer architecture is concerned with the structure and behavior of the computer as seen by the user. It includes the information, formats, the instruction set, and techniques for addressing memory. The architectural design of a computer system is concerned with the specifications of the various functional modules, such as processors and memories, and structuring them together into a computer system.

Two basic types of computer architectures are von Neumann architecture and Harvard architecture. von Neumann architecture describes a general framework, or structure, that a computer's hardware, programming, and data should follow. Although other structures for computing have been devised and implemented, the vast majority of computers in use today operate according to the von

computer organization

computer design

computer architecture



1-2 Logic Gates

Binary information is represented in digital computers by physical quantities called *signals*. Electrical signals such as voltages exist throughout the computer in either one of two recognizable states. The two states represent a binary variable that can be equal to 1 or 0. For example, a particular digital computer may employ a signal of 3 volts to represent binary 1 and 0.5 volt to represent binary 0. The input terminals of digital circuits accept binary signals of 3 and 0.5 volts and the circuits respond at the output terminals with signals of 3 and 0.5 volts to represent binary input and output corresponding to 1 and 0, respectively.

Binary logic deals with binary variables and with operations that assume a logical meaning. It is used to describe, in algebraic or tabular form, the manipulation and processing of binary information. The manipulation of binary information is done by logic circuits called *gates*. Gates are blocks of hardware that produce signals of binary 1 or 0 when input logic requirements are satisfied. A variety of logic gates are commonly used in digital computer systems. Each gate has a distinct graphic symbol and its operation can be described by means of an algebraic expression. The input—output relationship of the binary variables for each gate can be represented in tabular form by a *truth table*. The basic logic gates are AND and inclusive OR with multiple inputs and NOT with a single input. Each gate with more than one input is sensitive to either logic 0 or logic 1 input at any one of its inputs, generating the output according to its function. For example, a multi-input AND gate is sensitive to logic 0 on any one of its inputs, irrespective of any values at other inputs.

The names, graphic symbols, algebraic functions, and truth tables of eight logic gates are listed in Fig. 1-2, with applicable sensitivity input values. Each gate has one or two binary input variables designated by A and B and one binary output variable designated by x. The AND gate produces the AND logic function: that is, the output is 1 if input A and input B are both equal to 1; otherwise, the output is 0. These conditions are also specified in the truth table for the AND gate. The table shows that output x is 1 only when both input A and input B are 1. The algebraic operation symbol of the AND function is the same as the multiplication symbol of ordinary arithmetic. We can either use a dot between the variables or concatenate the variables without an operation symbol between them. AND gates may have more than two inputs, and by definition, the output is 1 if and only if all inputs are 1.

The OR gate produces the inclusive-OR function; that is, the output is 1 if input A or input B or both inputs are 1; otherwise, the output is 0. The algebraic symbol of the OR function is +, similar to arithmetic addition. OR gates may have more than two inputs, and by definition, the output is 1 if any input is 1.

The inverter circuit inverts the logic sense of a binary signal. It produces the NOT, or complement, function. The algebraic symbol used for the logic complement is either a prime or a bar over the variable symbol. In this book we use a prime for the logic complement of a binary variable, while a bar over the letter is reserved for designating a complement microoperation as defined in Chap. 4.

The small circle in the output of the graphic symbol of an inverter designates a logic complement. A triangle symbol by itself designates a buffer circuit. A

gates

OR

inverter

Name	Graphic symbol	Algebraic function	Truth table	Input sensitivity
AND	A x	$x = A \cdot B$ or $x = AB$	A B x 0 0 0 0 1 0 1 0 0 1 1 1	0
OR	A x	x = A + B	A B x 0 0 0 0 1 1 1 0 1 1 1 1	1
Inverter	Ax	x = A'	$\begin{array}{c c} A & x \\ \hline 0 & 1 \\ 1 & 0 \end{array}$	Not Applicable
Buffer	A x	x = A	$\begin{array}{c c} A & x \\ \hline 0 & 0 \\ 1 & 1 \end{array}$	Not Applicable
NAND	A	x = (AB)'	$\begin{array}{c cccc} A & B & x \\ \hline 0 & 0 & 1 \\ 0 & 1 & 1 \\ 1 & 0 & 1 \\ 1 & 1 & 0 \\ \end{array}$	0
NOR	$A \longrightarrow X$	x = (A + B)'	$\begin{array}{c cccc} A & B & x \\ \hline 0 & 0 & 1 \\ 0 & 1 & 0 \\ 1 & 0 & 0 \\ 1 & 1 & 0 \\ \end{array}$	1
Exclusive-OR (XOR)	A	$x = A \oplus B$ or $x = A'B + AB'$	$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	Not Applicable
Exclusive-NOR or equivalence	$A \longrightarrow A \longrightarrow A$	$x = (A \oplus B)$ or $x = AB + AB'$	$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	Not Applicable

Figure 1-2 Digital logic gates with applicable input sensitivity values.



buffer does not produce any particular logic function since the binary value of the output is the same as the binary value of the input. This circuit is used merely for power amplification. For example, a buffer that uses 3 volts for binary 1 will produce an output of 3 volts when its input is 3 volts. However, the amount of electrical power needed at the input of the buffer is much less than the power produced at the output of the buffer. The main purpose of the buffer is to drive other gates that require a large amount of power.

The NAND function is the complement of the AND function, as indicated by the graphic symbol, which consists of an AND graphic symbol followed by a small circle. The designation NAND is derived from the abbreviation of NOT-AND. The NOR gate is the complement of the OR gate and uses an OR graphic symbol followed by a small circle. Both NAND and NOR gates may have more than two inputs, and the output is always the complement of the AND or OR function, respectively.

The exclusive-OR gate has a graphic symbol similar to the OR gate except for the additional curved line on the input side. The output of this gate is 1 if any input is 1 but excludes the combination when both inputs are 1. The exclusive-OR function has its own algebraic symbol or can be expressed in terms of AND, OR, and complement operations as shown in Fig. 1-2. The exclusive-NOR is the complement of the exclusive-OR, as indicated by the small circle in the graphic symbol. The output of this gate is 1 only if both inputs are equal to 1 or both inputs are equal to 0. A more fitting name for the exclusive-OR operation would be an odd function; that is, its output is 1 if an odd number of inputs are 1. Thus in a three-input exclusive-OR (odd) function, the output is 1 if only one input is 1 or if all three inputs are 1. The exclusive-OR and exclusive-NOR gates are commonly available with two inputs, and only seldom are they found with three or more inputs.

1-3 Boolean Algebra

A Boolean algebra is an algebra (set, operations, elements) consisting of a set B with ≥ 2 elements, together with three operations—the AND operation \cdot (Boolean product), the OR operation + (Boolean sum), and the NOT operation' (complement)—defined on the set, such that for any element a, b, c, \ldots of set $B, a \cdot b, a + b$, and a' are in B. Consider the four-element Boolean algebra $B_4 = (\{0, x, y, 1\}; \cdot, +, '; 0, 1)$. The AND, OR, and NOT operations are described by the following tables:

•	0	\boldsymbol{x}	y	1	$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	<u>'</u>
0	0	0	0	0	$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	0 1
x	0	\boldsymbol{x}	0	$\boldsymbol{\mathcal{X}}$	$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	$x \mid y$
y	0	0 x	y	y	y y 1 y 1	$y \mid x$
1	0	$\boldsymbol{\mathcal{X}}$	y	1	$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	1 0

NAND

NOR

exclusive-OR

Consider the two-element Boolean algebra $B_2 = (\{0, 1\}; \cdot, +, '; 0, 1)$. The three operations. (AND), + (OR), '(NOT) are defined as follows:

•	0	1	+	0	1	,	
0	0	0	0	0	1	0	1
1	0	1	1	1	1	1	0

The two-element Boolean algebra B_2 among all other B_i , where i > 2, defined as switching algebra, is the most useful. Switching algebra consists of two elements represented by 1 and 0 as the largest number and the smallest number respectively.

*Boolean algebra is a switching algebra that deals with binary variables and logic operations. The variables are designated by letters such as *A*, *B*, *x*, and *y*. The three basic logic operations are AND, OR, and complement. A Boolean function can be expressed algebraically with binary variables, the logic operation symbols, parentheses, and equal sign. For a given value of the variables, the Boolean function can be either 1 or 0. Consider, for example, the Boolean function

$$F = x + y'z$$

The function F is equal to 1 if x is 1 or if both y' and z are equal to 1; F is equal to 0 otherwise. But saying that y' = 1 is equivalent to saying that y = 0 since y' is the complement of y. Therefore, we may say that F is equal to 1 if x = 1 or if yz = 01. The relationship between a function and its binary variables can be represented in a truth table. To represent a function in a truth table we need a list of the 2^n combinations of the n binary variables. As shown in Fig. 1-3(a), there are eight possible distinct combinations for assigning bits to the three variables x, y, and z. The function F is equal to 1 for those combinations where x = 1 or yz = 01; it is equal to 0 for all other combinations.

A Boolean function can be transformed from an algebraic expression into a logic diagram composed of AND, OR, and inverter gates. The logic diagram for F is shown in Fig. 1-3(b). There is an inverter for input y to generate its

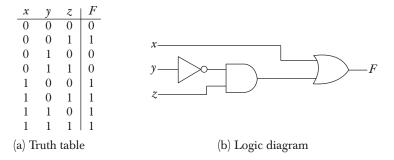


Figure 1-3 Truth table and logic diagram for F = x + y'z.

Boolean function

truth table

logic diagram

^{*}Two Element

complement y'. There is an AND gate for the term y'z, and an OR gate is used to combine the two terms. In a logic diagram, the variables of the function are taken to be the inputs of the circuit, and the variable symbol of the function is taken as the output of the circuit.

The purpose of Boolean algebra is to facilitate the analysis and design of digital circuits. It provides a convenient tool to:

- Express in algebraic form a truth table relationship between binary variables.
- 2. Express in algebraic form the input-output relationship of logic diagrams.
- 3. Find simpler circuits for the same function.

A Boolean function specified by a truth table can be expressed algebraically in many different ways. Two ways of forming Boolean expressions are canonical and non-canonical forms. Canonical forms express all binary variables in every product (AND) or sum (OR) term of the Boolean function. To determine the canonical sum-of-products form for a Boolean function F(A, B, C) = A'B + C' + ABC, which is in non-canonical form, the following steps are used:

$$F = A'B + C' + ABC$$

$$= A'B(C + C') + (A + A')(B + B')C' + ABC,$$
where $x + x' = 1$ is a basic identity of Boolean algebra
$$= A'BC + A'BC' + ABC' + AB'C' + A'BC' + A'B'C' + ABC$$

$$= A'BC + A'BC' + ABC' + ABC' + ABC' + ABC$$

By manipulating a Boolean expression according to Boolean algebra rules, one may obtain a simpler expression that will require fewer gates. To see how this is done, we must first study the manipulative capabilities of Boolean algebra.

Table 1-1 lists the most basic identities of Boolean algebra. All the identities in the table can be proven by means of truth tables. The first eight identities show the basic relationship between a single variable and itself, or in

TABLE 1-1 Basic Identities of Boolean Algebra

(1) x + 0 = x	$(2) x \cdot 0 = 0$
(3) $x + 1 = 1$	$(4) x \cdot 1 = x$
(5) x + x = x	$(6) x \cdot x = x$
(7) x + x' = 1	$(8) x \cdot x' = 0$
(9) x + y = y + x	(10) xy = yx
(11) x + (y + z) = (x + y) + z	(12) x(yz) = (xy)z
(13) x (y + z) = xy + xz	(x + y)(x + z)
(15) (x + y)' = x'y'	(16) (xy)' = x' + y'
(17) (x')' = x	

conjunction with the binary constants 1 and 0. The next five identities (9 through 13) are similar to ordinary algebra. Identity 14 does not apply in ordinary algebra but is very useful in manipulating Boolean expressions. Identities 15 and 16 are called DeMorgan's theorems and are discussed below. The last identity states that if a variable is complemented twice, one obtains the original value of the variable.

The identities listed in the table apply to single variables or to Boolean functions expressed in terms of binary variables. For example, consider the following Boolean algebra expression:

$$AB' + C'D + AB' + C'D$$

By letting x = AB' + C'D the expression can be written as x + x. From identity 5 in Table 1-1 we find that x + x = x. Thus the expression can be reduced to only two terms:

$$AB' + C'D + A'B + C'D = AB' + CD$$

DeMorgan's theorem

DeMorgan's theorem is very important in dealing with NOR and NAND gates. It states that a NOR gate that performs the (x + y)' function is equivalent to the function x'y'. Similarly, a NAND function can be expressed by either (xy)' or (x' + y'). For this reason the NOR and NAND gates have two distinct graphic symbols, as shown in Figs. 1-4 and 1-5. Instead of representing a NOR gate with an OR graphic symbol followed by a circle, we can represent it by an AND graphic symbol preceded by circles in all inputs. The invert-AND symbol for the NOR gate follows from DeMorgan's theorem and from the convention that small circles denote complementation. Similarly, the NAND gate has two distinct symbols, as shown in Fig. 1-5. NAND and NOR gates can be used to implement any Boolean function, including basic logic gates such as AND, OR, and NOT. Hence, NAND and NOR gates are called as Universal gates.

Figure 1-4 Two graphic symbols for NOR gate.

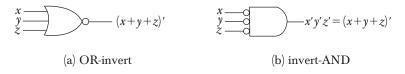
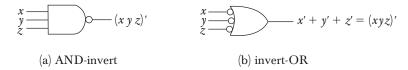


Figure 1-5 Two graphic symbols for NAND gate.



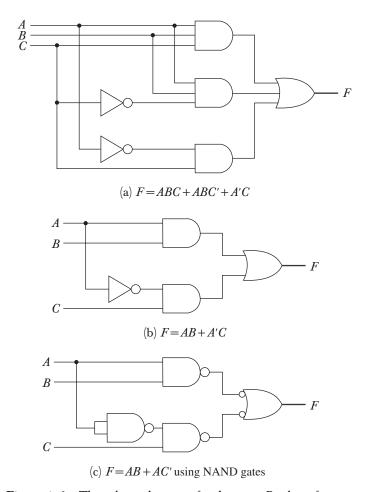


Figure 1-6 Three logic diagrams for the same Boolean function.

To see how Boolean algebra manipulation is used to simplify digital circuits, consider the logic diagram of Fig. l-6(a). The output of the circuit can be expressed algebraically as follows:

$$F = ABC + ABC' + A'C$$

Each term corresponds to one AND gate, and the OR gate forms the logical sum of the three terms. Two inverters are needed to complement A' and C'. The expression can be simplified using Boolean algebra.

$$F = ABC + ABC' + A'C = AB(C + C') + A'C = AB + A'C$$

Note that (C + C)' = 1 by identity 7 and $AB \cdot 1 = AB$ by identity 4 in Table 1-1.



The logic diagram of the simplified expression is drawn in Fig. l-6(b) and Fig. l-6(c). It requires only four gates rather than the six gates used in the circuit of Fig. l-6(a). The two circuits are equivalent and produce the same truth table relationship between inputs A, B, C and output F.

Complement of a Function

The complement of a function F when expressed in a truth table is obtained by interchanging l's and O's in the values of F in the truth table. When the function is expressed in algebraic form, the complement of the function can be derived by means of DeMorgan's theorem. The general form of DeMorgan's theorem can be expressed as follows:

$$(x_1 + x_2 + x_3 + \dots + x_n)' = x_1' x_2' x_3' \dots x_n'$$
$$(x_1 x_2 x_3 \dots x_n)' = x_1' + x_2' + x_3' + \dots + x_n'$$

From the general DeMorgan's theorem we can derive a simple procedure for obtaining the complement of an algebraic expression. This is done by changing all OR operations to AND operations and all AND operations to OR operations and then complementing each individual letter variable. As an example, consider the following expression and its complement:

$$F = AB + C'D' + B'D$$

 $F' = (A' + B')(C + D)(B + D')$

The complement expression is obtained by interchanging AND and OR operations and complementing each individual variable. Note that the complement of *C*′ is *C*.

1-4 Map Simplification

The complexity of the logic diagram that implements a Boolean function is related directly to the complexity of the algebraic expression from which the function is implemented. The truth table representation of a function is unique, but the function can appear in many different forms when expressed algebraically. The expression may be simplified using the basic relations of Boolean algebra. However, this procedure is sometimes difficult because it lacks specific rules for predicting each succeeding step in the manipulative process. Two methods of simplifying Boolean algebraic expressions are the map method and the tabular method. The map method is used for functions upto six variables. To manipulate functions of a large number of variables, the tabular method also known as the Quine-McCluskey method, is used. If a function to be minimized is not in a canonical form, it must first be converted into canonical form before applying Quine-McCluskey tabular

procedure. Another tabular method, known as the iterative consensus method, begins the simplification process even if the function is not in a canonical form. The map method provides a simple, straightforward procedure for simplifying Boolean expressions. This method may be regarded as a pictorial arrangement of the truth table which allows an easy interpretation for choosing the minimum number of terms needed to express the function algebraically. The map method is also known as the Karnaugh map or K-map.

Each combination of the variables in a truth table is called a minterm. For example, the truth table of Fig. 1-3 contains eight minterms. When expressed in a truth table a function of n variables will have 2^n minterms, equivalent to the 2^n binary numbers obtained from n bits. A Boolean function is equal to 1 for some minterms and to 0 for others. The information contained in a truth table may be expressed in compact form by listing the decimal equivalent of those minterms that produce a 1 for the function. For example, the truth table of Fig. 1-3 can be expressed as follows:

$$F(x, y, z) = \sum (1, 4, 5, 6, 7)$$

The letters in parentheses list the binary variables in the order that they appear in the truth table. The symbol Σ stands for the sum of the minterms that follow in parentheses. The minterms that produce 1 for the function are listed in their decimal equivalent. The minterms missing from the list are the ones that produce 0 for the function.

The map is a diagram made up of squares, with each square representing one minterm. The squares corresponding to minterms that produce 1 for the function are marked by a 1 and the others are marked by a 0 or are left empty. By recognizing various patterns and combining squares marked by l's in the map, it is possible to derive alternative algebraic expressions for the function, from which the most convenient may be selected.

The maps for functions of two, three, and four variables are shown in Fig. 1-7. The number of squares in a map of n variables is 2^n . The 2^n minterms are listed by an equivalent decimal number for easy reference. The minterm numbers are assigned in an orderly arrangement such that adjacent squares represent minterms that differ by only one variable. The variable names are listed across both sides of the diagonal line in the corner of the map. The 0's and 1's marked along each row and each column designate the value of the variables. Each variable under brackets contains half of the squares in the map where that variable appears unprimed. The variable appears with a prime (complemented) in the remaining half of the squares.

The minterm represented by a square is determined from the binary assignments of the variables along the left and top edges in the map. For example, minterm 5 in the three-variable map is 101 in binary, which may be obtained from the 1 in the second row concatenated with the 01 of the second column. This minterm represents a value for the binary variables A, B, and C, with A and C

minterm

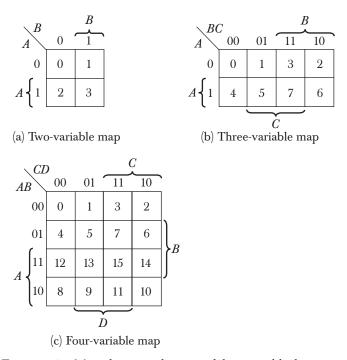


Figure 1-7 Maps for two-, three-, and four-variable functions.

being unprimed and B being primed (i.e., AB'C). On the other hand, minterm 5 in the four-variable map represents a minterm for four variables. The binary number contains the four bits 0101, and the corresponding term it represents is A'BC'D.

Minterms of adjacent squares in the map are identical except for one variable, which appears complemented in one square and uncomplemented in the adjacent square. According to this definition of adjacency, the squares at the extreme ends of the same horizontal row are also to be considered adjacent. The same applies to the top and bottom squares of a column. As a result, the four corner squares of a map must also be considered to be adjacent.

A Boolean function represented by a truth table is plotted into the map by inserting l's in those squares where the function is the squares containing l's are combined in groups of adjacent squares. These groups must contain a number of squares that is an integral power of 2. Groups of combined adjacent squares may share one or more squares with one or more groups. Each group of squares represents an algebraic term, and the OR of those terms gives the simplified algebraic expression for the function. The following examples show the use of the map for simplifying Boolean functions.

In the first example we will simplify the Boolean function

$$F(A, B, C) = \sum (3, 4, 6, 7)$$

adjacent squares

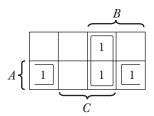


Figure 1-8 Map for $F(A, B, C) = \sum (3, 4, 6, 7)$.

The three-variable map for this function is shown in Fig. 1-8. There are four squares marked with l's, one for each minterm that produces 1 for the function. These squares belong to minterms 3, 4, 6, and 7 and are recognized from Fig. 1-7(b). Two adjacent squares are combined in the third column. This column belongs to both B and C and produces the term BC. The remaining two squares with l's in the two corners of the second row are adjacent and belong to row A and the two columns of C', so they produce the term AC'. The simplified algebraic expression for the function is the OR of the two terms:

$$F = BC + AC'$$

The second example simplifies the following Boolean function:

$$F(A, B, C) = \sum (0, 2, 4, 5, 6)$$

The five minterms are marked with l's in the corresponding squares of the three-variable map shown in Fig. 1-9. The four squares in the first and fourth columns are adjacent and represent the term C'. The remaining square marked with a 1 belongs to minterm 5 and can be combined with the square of minterm 4 to produce the term AB'. The simplified function is

$$F = C' + AB'$$

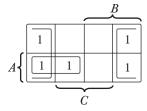


Figure 1-9 Map for $F(A, B, C) = \sum (3, 4, 6, 7)$.

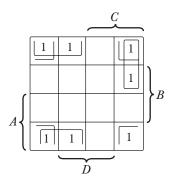


Figure 1-10 Map for $F(A, B, C, D) = \sum (0, 1, 2, 6, 8, 9, 10)$.

The third example needs a four-variable map.

$$F(A, B, C, D) = \sum_{i=1}^{n} (0, 1, 2, 6, 8, 9, 10)$$

The area in the map covered by this four-variable function consists of the squares marked with l's in Fig. 1-10. The function contains l's in the four corners that, when taken as a group, give the term B'D'. This is possible because these four squares are adjacent when the map is considered with top and bottom or left and right edges touching. The two l's on the left of the top row are combined with the two l's on the left of the bottom row to give the term B'C'. The remaining 1 in the square of minterm 6 is combined with minterm 2 to give the term A'CD'. The simplified function is

$$F = B'D' + B'C' + A'CD'$$

Product-of-Sums Simplification

The Boolean expressions derived from the maps in the preceding examples were expressed in sum-of-products form. The product terms are AND terms and the sum denotes the ORing of these terms. It is sometimes convenient to obtain the algebraic expression for the function in a product-of-sums form. The sums are OR terms and the product denotes the ANDing of these terms. With a minor modification, a product-of-sums form can be obtained from a map.

The procedure for obtaining a product-of-sums expression follows from the basic properties of Boolean algebra. The I's in the map represent the minterms that produce 1 for the function. The squares not marked by 1 represent the minterms that produce 0 for the function. If we mark the empty squares with 0's and combine them into groups of adjacent squares, we obtain the complement of the function, F'. Taking the complement of F' produces an expression for F in product-of-sums form. The best way to show this is by example.

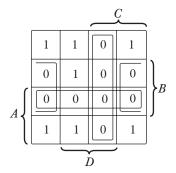


Figure 1-11 Map for $F(A, B, C, D) = \sum (0, 1, 2, 5, 8, 9, 10)$.

We wish to simplify the following Boolean function in both sum-of-products form and product-of-sums form:

$$F(A, B, C, D) = \sum (0, 1, 2, 5, 8, 9, 10)$$

The l's marked in the map of Fig. 1-11 represent the minterms that produce a 1 for the function. The squares marked with 0's represent the minterms not included in F and therefore denote the complement of F. Combining the squares with l's gives the simplified function in sum-of-products form:

$$F = B'D' + B'C' + A'C'D$$

If the squares marked with 0's are combined, as shown in the diagram, we obtain the simplified complemented function:

$$F' = AB + CD + BD'$$

Taking the complement of F', we obtain the simplified function in product-of-sums form:

$$F = (A' + B')(C' + D')(B' + D)$$

The logic diagrams of the two simplified expressions are shown in Fig. 1-12. The sum-of-products expression is implemented in Fig. 1-12(a) with a group of AND gates, one for each AND term. The outputs of the AND gates are connected to the inputs of a single OR gate. The same function is implemented in Fig. 1-12(b) in product-of-sums form with a group of OR gates, one for each OR term. The outputs of the OR gates are connected to the inputs of a single AND gate. In each case it is assumed that the input variables are directly available in their complement, so inverters are not included. The pattern established in Fig. 1-12 is the general form by which any Boolean function is implemented when expressed in one of the standard

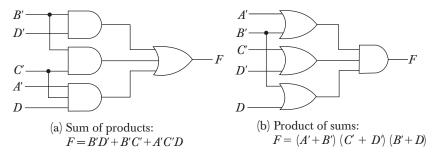


Figure 1-12 Logic diagrams with AND and OR gates.

forms. AND gates are connected to a single OR gate when in sum-of-products form. OR gates are connected to a single AND gate when in product-of-sums form.

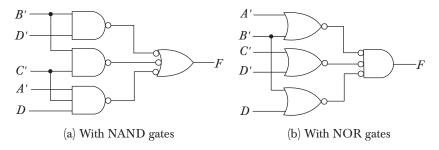
A sum-of-products expression can be implemented with NAND gates as shown in Fig. 1-13(a). Note that the second NAND gate is drawn with the graphic symbol of Fig. 1-5(b). There are three lines in the diagram with small circles at both ends. Two circles in the same line designate double complementation, and since (x')' = x, the two circles can be removed and the resulting diagram is equivalent to the one shown in Fig. 1-12(a). Similarly, a product-of-sums expression can be implemented with NOR gates as shown in Fig. 1-13(b). The second NOR gate is drawn with the graphic symbol of Fig. 1-4(b). Again the two circles on both sides of each line may be removed, and the diagram so obtained is equivalent to the one shown in Fig. 1-12(b).

Don't-Care Conditions

The l's and 0's in the map represent the minterms that make the function equal to 1 or 0. There are occasions when it does not matter if the function produces 0 or 1 for a given minterm. Since the function may be either 0 or 1, we say that we don't care what the function output is to be for this minterm. Minterms that may produce either 0 or 1 for the function are said to be don't-care conditions and are marked with an \times in the map. These don't-care conditions can be used to provide further simplification of the algebraic expression.

don't-care

Figure 1-13 Logic diagrams with NAND or NOR gates.



NAND implementation

NOR implementation

When choosing adjacent squares for the function in the map, the \times 's may be assumed to be either 0 or 1, whichever gives the simplest expression. In addition, an \times need not be used at all if it does not contribute to the simplification of the function. In each case, the choice depends only on the simplification that can be achieved. As an example, consider the following Boolean function together with the don't-care minterms:

$$F(A, B, C) = \sum (0, 2, 6)$$

 $d(A, B, C) = \sum (1, 3, 5)$

The minterms listed with F produce a 1 for the function. The don't-care minterms listed with d may produce either a 0 or a 1 for the function. The remaining minterms, 4 and 7, produce a 0 for the function. The map is shown in Fig. 1-14. The minterms of F are marked with 1's, those of d are marked with \times 's, and the remaining squares are marked with 0's. The l's and \times 's are combined in any convenient manner so as to enclose the maximum number of adjacent squares. It is not necessary to include all or any of the \times 's, but all the l's must be included. By including the don't care minterms 1 and 3 with the l's in the first row we obtain the term A'. The remaining 1 for minterm 6 is combined with minterm 2 to obtain the term BC'. The simplified expression is

$$F = A' + BC'$$

Note that don't-care minterm 5 was not included because it does not contribute to the simplification of the expression. Note also that if don't-care minterms 1 and 3 were not included with the l's, the simplified expression for F would have been

$$F = A'C' + BC'$$

This would require two AND gates and an OR gate, as compared to the expression obtained previously, which requires only one AND and one OR gate.

The function is determined completely once the \times 's are assigned to the l's or 0's in the map. Thus the expression

$$F = A' + BC'$$

represents the Boolean function

$$F(A, B, C) = \sum (0, 1, 2, 3, 6)$$

It consists of the original minterms 0, 2, and 6 and the don't-care minterms 1 and 3. Minterm 5 is not included in the function. Since minterms 1, 3, and 5 were specified as being don't-care conditions, we have chosen minterms 1 and 3 to produce a 1 and minterm 5 to produce a 0. This was chosen because this assignment produces the simplest Boolean expression.



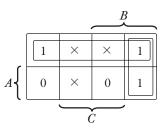


Figure 1-14 Example of map with don't-care conditions.

1-5 Combinational Circuits

Digital logic circuits are basically categorized into two types:

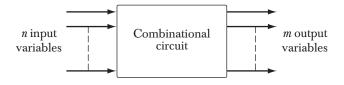
- 1. Combinational circuits in which there are no feedback paths from outputs to inputs and there is no memory.
- 2. Sequential circuits in which feedback paths exist from outputs to inputs, and they have memory.

A combinational circuit is a connected arrangement of logic gates with a set of inputs and outputs. At any given time, the binary values of the outputs are a function of the binary combination of the inputs. A block diagram of a combinational circuit is shown in Fig. 1-15. The *n* binary input variables come from an external source, the *m* binary output variables go to an external destination, and in between there is an interconnection of logic gates. A combinational circuit transforms binary information from the given input data to the required output data. Combinational circuits are employed in digital computers for generating binary control decisions and for providing digital components required for data processing.

A combinational circuit can be described by a truth table showing the binary relationship between the n input variables and the m output variables. The truth table lists the corresponding output binary values for each of the 2^n input combinations. A combinational circuit can also be specified with m Boolean functions, one for each output variable. Each output function is expressed in terms of the n input variables.

The analysis of a combinational circuit starts with a given logic circuit diagram and culminates with a set of Boolean functions or a truth table. If the digital

Figure 1-15 Block diagram of a combinational circuit.



block diagram

analysis

circuit is accompanied by a verbal explanation of its function, the Boolean functions or the truth table is sufficient for verification. If the function of the circuit is under investigation, it is necessary to interpret the operation of the circuit from the derived Boolean functions or the truth table. The success of such investigation is enhanced if one has experience and familiarity with digital circuits. The ability to correlate a truth table or a set of Boolean functions with an information-processing task is an art that one acquires with experience.

The design of combinational circuits starts from the verbal outline of the problem and ends in a logic circuit diagram. The procedure involves the following steps:

- 1. The problem is stated.
- 2. The input and output variables are assigned letter symbols.
- The truth table that defines the relationship between inputs and outputs is derived.
- 4. The simplified Boolean functions for each output are obtained.
- **5.** The logic diagram is drawn.

To demonstrate the design of combinational circuits, we present two examples of simple arithmetic circuits. These circuits serve as basic building blocks for the construction of more complicated arithmetic circuits.

Half-Adder

The most basic digital arithmetic circuit is the addition of two binary digits. A combinational circuit that performs the arithmetic addition of two bits is called a half-adder. One that performs the addition of three bits (two significant bits and a previous carry) is called a full-adder. The name of the former stems from the fact that two half-adders are needed to implement a full-adder.

The input variables of a half-adder are called the augend and addend bits. The output variables the sum and carry. It is necessary to specify two output variables because the sum of 1+1 is binary 10, which has two digits. We assign symbols x and y to the two input variables, and S (for sum) and C (for carry) to the two output variables. The truth table for the half-adder is shown in Fig. 1-16(a). The C output is 0 unless both inputs are 1. The S output represents the least significant bit of the sum. The Boolean functions for the two outputs can be obtained directly from the truth table:

$$S = x'y + xy' = x \oplus y$$
$$C = xy$$

The logic diagram is shown in Fig. l-16(b). It consists of an exclusive-OR gate and an AND gate. A half-adder logic module of an exclusive-OR gate and an AND gate can be used to implement universal logic gates NAND and NOR.

design

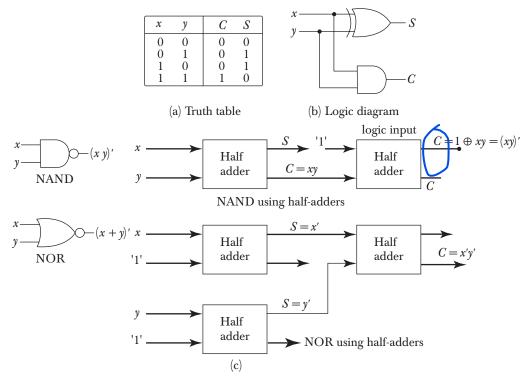


Figure 1-16 Half-adder.

Figure 1-16(c) shows the use of half-adder modules to construct NAND and NOR gates.

Full-Adder

A full-adder is a combinational circuit that forms the arithmetic sum of three input bits. It consists of three inputs and two outputs. Two of the input variables, denoted by x and y, represent the two significant bits to be added. The third input, z, represents the carry from the previous lower significant position. Two outputs are necessary because the arithmetic sum of three binary digits ranges in value from 0 to 3, and binary 2 or 3 needs two digits. The two outputs are designated by the symbols S (for sum) and C (for carry). The binary variable S gives the value of the least significant bit of the sum. The binary variable C gives the output carry. The truth table of the full-adder is shown in Table 1-2. The eight rows under the input variables designate all possible combinations that the binary variables may have. The value of the output variables are determined from the arithmetic sum of the input bits. When all input bits are 0, the output is 0. The S output is equal to 1 when only one input is equal to 1 or when all three inputs are equal to 1. The C output has a carry of 1 if two or three inputs are equal to 1.

The maps of Fig. 1-17 are used to find algebraic expressions for the two output variables. The 1's in the squares for the maps of S and C are determined

Inputs			Ou	tputs		
x	у	z	\overline{C}	S		
 0	0	0	0	1	\checkmark	
0	0	1	0			
0	1	0	0	1	•	
0	1	1	1	0		
1	0	0	0	1		
1	0	1	1	0		
1	1	0	1	0		
1	1	1	1	1		

TABLE 1-2 Truth Table for Full-Adder

directly from the minterms in the truth table. The squares with l's for the S output do not combine in groups of adjacent squares. But since the output is 1 when an odd number of inputs are 1, S is an odd function and represents the exclusive-OR relation of the variables (see the discussion at the end of Sec. 1-2). The squares with l's for the C output may be combined in a variety of ways. One possible expression for C is

$$C = xy + (x'y + xy')z$$

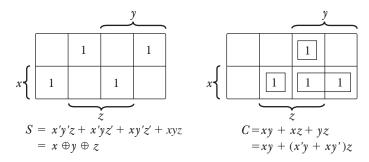
Realizing that $x'y + xy' = x \oplus y$ and including the expression for output *S*, we obtain the two Boolean expressions for the full-adder:

$$S = x \oplus y \oplus z$$

$$C = xy + (x \oplus y)z$$

The logic diagram of the full-adder is drawn in Fig. 1-18. Note that the full adder circuit consists of two half-adders and an OR gate. When used in subsequent chapters, the full-adder (FA) will be designated by a block diagram as shown in Fig. 1-18(b).

Figure 1-17 Maps for full-adder.





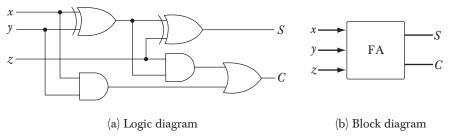


Figure 1-18 Full-adder circuit.

1-6 Flip-Flops

The digital circuits considered thus far have been combinational, where the outputs at any given time are entirely dependent on the inputs that are present at that time. Although every digital system is likely to have a combinational circuit, most systems encountered in practice also include storage elements, which require that the system be described in terms of sequential circuits. The most common type of sequential circuit is the synchronous type. Synchronous sequential circuits employ signals that affect the storage elements only at discrete instants of time. Synchronization is achieved by a timing device called a clock pulse generator that produces a periodic train of *clock pulses*. The clock pulses are distributed throughout the system in such a way that storage elements are affected only with the arrival of the synchronization pulse. Clocked synchronous sequential circuits are the type most frequently encountered in practice. They seldom manifest instability problems and their timing is easily broken down into independent discrete steps, each of which may be considered separately.

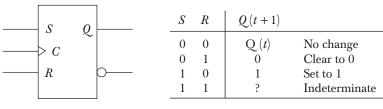
clocked sequential circuit

The storage elements employed in clocked sequential circuits are called flipflops. A flip-flop is a binary cell capable of storing one bit of information. It has two outputs, one for the normal value and one for the complement value of the bit stored in it. A flip-flop maintains a binary state until directed by a clock pulse to switch states. The difference among various types of flip-flops is in the number of inputs they possess and in the manner in which the inputs affect the binary state. The most common types of flip-flops are presented below.

SR Flip-Flop

The graphic symbol of the SR flip-flop is shown in Fig. l-19(a). It has three inputs, labeled S (for set), R (for reset), and C (for clock). It has an output Q and sometimes the flip-flop has a complemented output, which is indicated with a small circle at the other output terminal. There is an arrowhead-shaped symbol in front of the letter C to designate a *dynamic input*. The dynamic indicator symbol denotes the fact that the flip-flop responds to a positive transition (from 0 to 1) of the input clock signal.

The operation of the SR flip-flop is as follows. If there is no signal at the clock input C, the output of the circuit cannot change irrespective of the values at inputs



(a) Graphic symbol

(b) Characteristic table

Figure 1-19 *SR* flip-flop.

S and R. Only when the clock signal changes from 0 to 1 can the output be affected according to the values in inputs S and R. If S=1 and R=0 when C changes from 0 to 1, output Q is set to 1. If S=0 and R=1 when C changes from 0 to 1, output Q is cleared to 0. If both S and R are 0 during the clock transition, the output does not change. When both S and R are equal to 1, the output is unpredictable and may go to either 0 or 1, depending on internal timing delays that occur within the circuit.

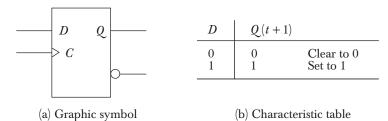
The characteristic table shown in Fig. 1-19(b) summarizes the operation of the SR flip-flop in tabular form. The S and R columns give the binary values of the two inputs. Q(t) is the binary state of the Q output at a given time (referred to as *present state*). Q(t+1) is the binary state of the Q output after the occurrence of a clock transition (referred to as next state). If S = R = 0, a clock transition produces no change of state [i.e., Q(t+1) = Q(t)]. If S = 0 and R = 1, the flip-flop goes to the 0 (clear) state. If S = 1 and S = 0, the flip-flop goes to the 1 (set) state. The SR flip-flop should not be pulsed when S = R = 1 since it produces an indeterminate next state. This indeterminate condition makes the SR flip-flop difficult to manage and therefore it is seldom used in practice.

D Flip-Flop

The D (data) flip-flop is a slight modification of the SR flip-flop. An SR flip-flop is converted to a D flip-flop by inserting an inverter between S and R and assigning the symbol D to the single input. The D input is sampled during the occurrence of a clock transition from 0 to 1. If D=1, the output of the flip-flop goes to the 1 state, but if D=0, the output of the flip-flop goes to the 0 state.

The graphic symbol and characteristic table of the D flip-flop are shown in Fig. 1-20. From the characteristic table we note that the next state Q(t + 1) is

Figure 1-20 D flip-flop



determined from the D input. The relationship can be expressed by a characteristic equation:

$$Q(t+1)=D$$

This means that the Q output of the flip-flop receives its value from the D input every time that the clock signal goes through a transition from 0 to 1.

Note that no input condition exists that will leave the state of the D flip-flop unchanged. Although a D flip-flop has the advantage of having only one input (excluding C), it has the disadvantage that its characteristic table does not have a "no change" condition Q(t+1) = Q(t). The "no change" condition can be accomplished either by disabling the clock signal or by feeding the output back into the input, so that clock pulses keep the state of the flip-flop unchanged.

JK Flip-Flop

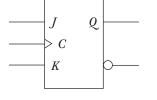
A JK flip-flop is a refinement of the SR flip-flop in that the indeterminate condition of the SR type is defined in the JK type. Inputs J and K behave like inputs S and SR to set and clear the flip-flop, respectively. When inputs SR and SR are both equal to 1, a clock transition switches the outputs of the flip-flop to their complement state.

The graphic symbol and characteristic table of the JK flip-flop are shown in Fig. 1-21. The J input is equivalent to the S (set) input of the SR flip-flop, and the K input is equivalent to the R (clear) input. Instead of the indeterminate condition, the JK flip-flop has a complement condition Q(t+1) = Q'(t) when both J and K are equal to 1.

T Flip-Flop

Another type of flip-flop found in textbooks is the T(toggle) flip-flop. This flip-flop, shown in Fig. 1-22, is obtained from a JK type when inputs J and K are connected to provide a single input designated by T. The T flip-flop therefore has only two conditions. When T = 0 (J = K = 0) a clock transition does not change the state of

Figure 1-21 JK flip-flop



(a) Graphic symbol

J	K	Q(t + 1)	
0	0	Q(t)	No change
0	1	0	Clear to 0
1	0	1	Set to 1
1	1	Q'(t)	Complement

(b) Characteristic table

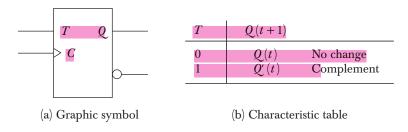


Figure 1-22 *T* flip-flop

the flip-flop. When T = 1 (J = K = 1) a clock transition complements the state of the flip-flop. These conditions can be expressed by a characteristic equation:

$$Q(t+1) = Q(t) \oplus T$$

Edge-Triggered Flip-Flops

The most common type of flip-flop used to synchronize the state change during a clock pulse transition is the edge-triggered flip-flop. In this type of flip-flop, output transitions occur at a specific level of the clock pulse. When the pulse input level exceeds this threshold level, the inputs are locked out so that the flip-flop is unresponsive to further changes in inputs until the clock pulse returns to 0 and another pulse occurs. Some edge-triggered flip-flops cause a transition on the rising edge of the clock signal (positive-edge transition), and others cause a transition on the falling edge (negative-edge transition).

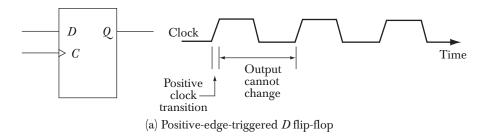
Figure 1-23(a) shows the clock pulse signal in a positive-edge-triggered D flip-flop. The value in the D input is transferred to the Q output when the clock makes a positive transition. The output cannot change when the clock is in the 1 level, in the 0 level, or in a transition from the 1 level to the 0 level. The effective positive clock transition includes a minimum time called the setup time in which the D input must remain at a constant value before the transition, and a definite time called the *hold time* in which the D input must not change after the positive transition. The effective positive transition is usually a very small fraction of the total period of the clock pulse.

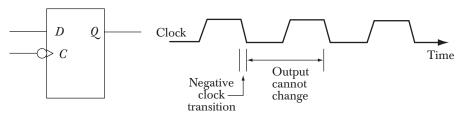
Figure 1-23(b) shows the corresponding graphic symbol and timing diagram for a negative-edge-triggered D flip-flop. The graphic symbol includes a negation small circle in front of the dynamic indicator at the C input. This denotes a negative-edge-triggered behavior. In this case the flip-flop responds to a transition from the 1 level to the 0 level of the clock signal.

Another type of flip-flop used in some systems is the master-slave flip-flop. This type of circuit consists of two flip-flops. The first is the master, which responds to the positive level of the clock, and the second is the slave, which responds to the negative level of the clock. The result is that the output changes

clock pulses

master-slave flip-flop





(b) Negative-edge-triggered D flip-flop

Figure 1-23 Edge-triggered flip-flop.

during the l-to-0 transition of the clock signal. The trend is away from the use of master-slave flip-flops and toward edge-triggered flip-flops.

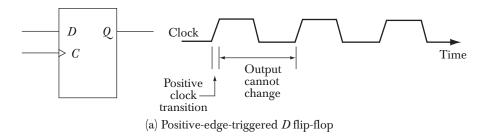
Flip-flops available in integrated circuit packages will sometimes provide special input terminals for setting or clearing the flip-flop asynchronously. These inputs are usually called "preset" and "clear." They affect the flip-flop on a negative level of the input signal without the need of a clock pulse. These inputs are useful for bringing the flip-flops to an initial state prior to its clocked operation.

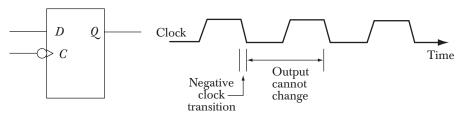
Excitation Tables

The characteristic tables of flip-flops specify the next state when the inputs and the present state are known. During the design of sequential circuits we usually know the required transition from present state to next state and wish to find the flip-flop input conditions that will cause the required transition. For this reason we need a table that lists the required input combinations for a given change of state. Such a table is called a flip-flop excitation table.

Table 1-3 lists the excitation tables for the four types of flip-flops. Each table consists of two columns, Q(t) and Q(t+1), and a column for each input to show how the required transition is achieved. There are four possible transitions from present state Q(t) to next state Q(t+1). The required input conditions for each of these transitions are derived from the information available in the characteristic tables. The symbol \times in the tables represents a don't-care condition; that is, it does not matter whether the input to the flip-flop is 0 or 1.







(b) Negative-edge-triggered D flip-flop

Figure 1-23 Edge-triggered flip-flop.

during the l-to-0 transition of the clock signal. The trend is away from the use of master-slave flip-flops and toward edge-triggered flip-flops.

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Excitation Tables

The characteristic tables of flip-flops specify the next state when the inputs and the present state are known. During the design of sequential circuits we usually know the required transition from present state to next state and wish to find the flip-flop input conditions that will cause the required transition. For this reason we need a table that lists the required input combinations for a given change of state. Such a table is called a flip-flop excitation table.

Table 1-3 lists the excitation tables for the four types of flip-flops. Each table consists of two columns, Q(t) and Q(t+1), and a column for each input to show how the required transition is achieved. There are four possible transitions from present state Q(t) to next state Q(t+1). The required input conditions for each of these transitions are derived from the information available in the characteristic tables. The symbol \times in the tables represents a don't-care condition; that is, it does not matter whether the input to the flip-flop is 0 or 1.





Family	Speed $(n \text{ sec})$	Power Dissipation (<i>m</i> watts)	Faxout	Polar Supply (V)	High Logic Level (V)	Low Logic Level (V)
TTL	10	10	10	+5	+3	0.2
ECL	2	40	high	-5.2	-0.9	+1.75
CMOS	25	low	high	3-15	V _{cc}	0

Figure 2-1 Comparison of the basic logic families.

The metal-oxide semiconductor (MOS) is a unipolar transistor that depends on the flow of only one type of carrier, which may be electrons (*n*-channel) or holes (*p*-channel). This is in contrast to the bipolar transistor used in TTL and ECL gates, where both carriers exist during normal operation. A *p*-channel MOS is referred to as PMOS and an *n*-channel as NMOS. NMOS is the one that is commonly used in circuits with only one type of MOS transistor. The complementary MOS (CMOS) technology uses PMOS and NMOS transistors connected in a complementary fashion in all circuits. The most important advantages of CMOS over bipolar are the high packing density of circuits, a simpler processing technique during fabrication, and a more economical operation because of low power consumption. Figure 2-1 is a comparison of the basic logic families.

Because of their many advantages, integrated circuits are used exclusively to provide various digital components needed in the design of computer systems. To understand the organization and design of digital computers it is very important to be familiar with the various components encountered in integrated circuits. For this reason, the most basic components are introduced in this chapter with an explanation of their logical properties. These components provide a catalog of elementary digital functional units commonly used as basic building blocks in the design of digital computers.

2-2 Decoders

Discrete quantities of information are represented in digital computers with binary codes. A binary code of n bits is capable of representing up to 2^n distinct elements of the coded information. A decoder is a combinational circuit that converts binary information from the n coded inputs to a maximum of 2^n unique outputs. If the n-bit coded information has unused bit combinations, the decoder may have less than 2^n outputs.

The decoders presented in this section are called n-to-m-line decoders, where $m \le 2^n$. Their purpose is to generate the 2^n (or fewer) binary combinations of the n input variables. A decoder has n inputs and m outputs and is also referred to as an $n \times m$ decoder.

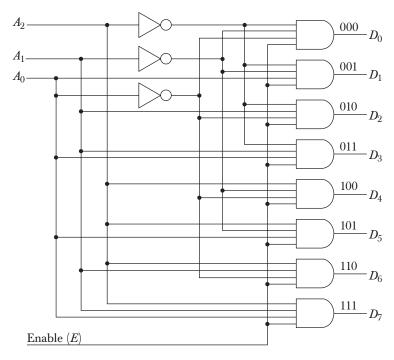


Figure 2-2 3-to-8-line decoder.

The logic diagram of a 3-to-8-line decoder is shown in Fig. 2-2. The three data inputs, A_0 , A_1 , and A_2 are decoded into eight outputs, each output representing one of the combinations of the three binary input variables. The three inverters provide the complement of the inputs, and each of the eight AND gates generates one of the binary combination. A particular application of this decoder is a binary-to-octal conversion. The input variables represent a binary number and the outputs represent the eight digits of the octal number system. However, a 3-to-8-line decoder can be used for decoding any 3-bit code to provide eight outputs, one for each combination of the binary code.

Commercial decoders include one or more enable inputs to control the operation of the circuit. The decoder of Fig. 2-2 has one enable input, E. The decoder is enabled when E is equal to 1 and disabled when E is equal to 0.

The operation of the decoder can be clarified using the truth table listed in Table 2-1. When the enable input E is equal to 0, all the outputs are equal to 0 regardless of the values of the other three data inputs. The three \times 's in the table designate don't-care conditions. When the enable input is equal to 1, the decoder operates in a normal fashion. For each possible input combination, there are seven outputs that are equal to 0 and only one that is equal to 1. The output variable whose value is equal to 1 represents the octal number equivalent of the binary number that is available in the input data lines.

Enable input

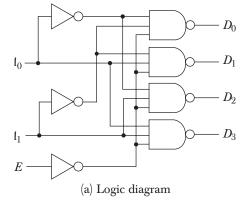
Enable		Inputs					Outp	outs			
	$\overline{A_2}$	A_1	$\overline{A_0}$	$\overline{D_7}$	D_6	D_5	D_4	D_3	D_2	D_1	D_0
0	×	×	×	0	0	0	0	0	0	0	0
1	0	0	0	0	0	0	0	0	0	0	1
1	0	0	1	0	0	0	0	0	0	1	0
1	0	1	0	0	0	0	0	0	1	0	0
1	0	1	1	0	0	0	0	1	0	0	0
1	1	0	0	0	0	0	1	0	0	0	0
1	1	0	0	0	0	1	0	0	0	0	0
1	1	1	0	0	1	0	0	0	0	0	0
1	1	1	1	1	0	0	0	0	0	0	0

TABLE 2-1 Truth Table for 3-to-8-Line Decoder

NAND Gate Decoder

Some decoders are constructed with NAND instead of AND gates. Since a NAND gate produces the AND operation with an inverted output, it becomes more economical to generate the decoder outputs in their complement form. A 2-to-4-line decoder with an enable input constructed with NAND gates is shown in-Fig. 2-3. The circuit operates with complemented outputs and a complemented enable input E. The decoder is enabled when E is equal to 0. As indicated by the truth table, only one output is equal to 0 at any given time; the other three outputs are equal to 1. The output whose value is equal to 0 represents the equivalent binary number in inputs A_1 and A_0 . The circuit is disabled when E is equal to 1, regardless of the values of the other two inputs. When the circuit is disabled, none of the outputs are selected and all outputs are equal to 1. In general, a decoder may operate with complemented or uncomplemented outputs. The enable input may be activated with a 0 or with a 1 signal level. Some decoders have two or

Figure 2-3 2-to-4-line decoder with NAND gates.



E	A_1	A_0	D_0	D_1	D_2	D_3
0	0	0	0	1	1	1
0	0	1	1	0	1	1
0	1	0	1	1	0	1
0	1	1	1	1	1	0
1	X	0 1 0 1 x	1	1	1	1

(b) Truth table

more enable inputs that must satisfy a given logic condition in order to enable the circuit.

Decoder Expansion

There are occasions when a certain-size decoder is needed but only smaller sizes are available. When this occurs it is possible to combine two or more decoders with enable inputs to form a larger decoder. Thus if a 6-to-64-line decoder is needed, it is possible to construct it with four 4-to-16-line decoders.

Figure 2-4 shows how decoders with enable inputs can be connected to form a larger decoder. Two 2-to-4-line decoders are combined to achieve a 3-to-8-line decoder. The two least significant bits of the input are connected to both decoders. The most significant bit is connected to the enable input of one decoder and through an inverter to the enable input of the other decoder. It is assumed that each decoder is enabled when its E input is equal to 1. When E is equal to 0, the decoder is disabled and all its outputs are in the 0 level. When $A_2 = 0$, the upper decoder is enabled and the lower is disabled. The lower decoder outputs become inactive with all outputs at 0. The outputs of the upper decoder generate outputs D_0 through D_3 , depending on the values of A_1 and A_0 (while $A_2 = 0$). When $A_2 = 1$, the lower decoder is enabled and the upper is disabled. The lower decoder output generates the binary equivalent D_4 through D_7 since these binary numbers have a 1 in the A_2 position.

The example demonstrates the usefulness of the enable input in decoders or any other combinational logic component. Enable inputs are a convenient feature for interconnecting two or more circuits for the purpose of expanding the digital component into a similar function but with more inputs and outputs.

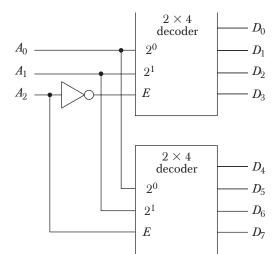


Figure 2-4 A 3×8 decoder constructed with two 2×4 decoders.



Encoders

An encoder is a digital circuit that performs the inverse operation of a decoder. An encoder has 2^n (or less) input lines and n outputs lines. The output lines generate the binary code corresponding to the input value. An example of an encoder is the octal-to-binary encoder, whose truth table is given in Table 2-2. It has eight inputs, one for each of the octal digits, and three outputs that generate the corresponding binary number. It is assumed that only one input has a value of 1 at any given time; otherwise, the circuit has no meaning.

			Inp	outs					Output	S
$\overline{D_7}$	D_6	D_5	D_4	D_3	D_2	D_1	D_0	$\overline{A_2}$	A_1	A_0
0	0	0	0	0	0	0	1	0	0	0
0	0	0	0	0	0	1	0	0	0	1
0	0	0	0	0	1	0	0	0	1	0
0	0	0	0	1	0	0	0	0	1	1
0	0	0	1	0	0	0	0	1	0	0
0	0	1	0	0	0	0	0	1	0	1
0	1	0	0	0	0	0	0	1	1	0
1	0	0	0	0	0	0	0	1	1	1

TABLE 2-2 Truth Table for Octal-to-Binary Encoder

The encoder can be implemented with OR gates whose inputs are determined directly from the truth table. Output $A_0 = 1$ if the input octal digit is 1 or 3 or 5 or 7. Similar conditions apply for the other two outputs. These conditions can be expressed by the following Boollean functions:

$$A_0 = D_1 + D_3 + D_5 + D_7$$

$$A_1 = D_2 + D_3 + D_6 + D_7$$

$$A_2 = D_4 + D_5 + D_6 + D_7$$

The encoder can be implemented with three OR gates.

2-3 Multiplexers

multiplexer

A multiplexer is a combinational circuit that receives binary information from one of 2^n input data lines and directs it to a single output line. The selection of a particular input data line for the output is determined by a set of selection inputs. A 2^n -to-1 multiplexer has 2^n input data lines and n input selection lines whose bit combinations determine which input data are selected for the output.

A 4-to-l-line multiplexer is shown in Fig. 2-5. Each of the four data inputs I_0 through I_3 is applied to one input of an AND gate. The two selection inputs S_1 and

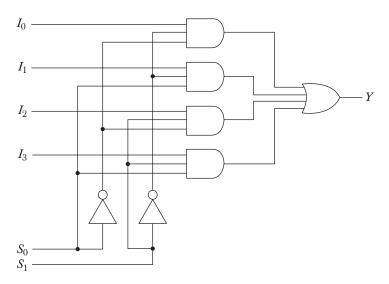


Figure 2-5 4-to-1-line multiplexer.

 S_0 are decoded to select a particular AND gate. The outputs of the AND gates are applied to a single OR gate to provide the single output. To demonstrate the circuit operation, consider the case when $S_1S_0=10$. The AND gate associated with input I_2 has two of its inputs equal to 1. The third input of the gate is connected to I_2 . The other three AND gates have at least one input equal to 0, which makes their outputs equal to 0. The OR gate output is now equal to the value of I_2 , thus providing a path from the selected input to the output.

The 4-to-l line multiplexer of Fig. 2-5 has six inputs and one output. A truth table describing the circuit needs 64 rows since six input variables can have 2^6 binary combinations. This is an excessively long table and will not be shown here. A more convenient way to describe the operation of multiplexers is by means of a function table. The function table for the multiplexer is shown in Table 2-3. The table demonstrates the relationship between the four data inputs and the single output as a function of the selection inputs S_1 and S_0 . When the selection inputs

TABLE 2-3 Function Table for 4-to-1-Line Multiplexer

	Sele	ect	Output
-	S_1	S_o	<u> </u>
	0	0	I_0
	0	1	I_1
	1	0	I_2
	1	1	I_3

data selector

are equal to 00, output Y is equal to input I_0 . When the selection inputs are equal to 01, input I_1 has a path to output Y, and similarly for the other two combinations. The multiplexer is also called a *data selector*, since it selects one of many data inputs and steers the binary information to the output.

The AND gates and inverters in the multiplexer resemble a decoder circuit, and indeed they decode the input selection lines. In general, a 2^n -to-l-line multiplexer is constructed from an n-to- 2^n decoder by adding to it 2^n input lines, one from each data input. The size of the multiplexer is specified by the number 2^n of its data inputs and the single output. It is then implied that it also contains n input selection lines. The multiplexer is often abbreviated as MUX.

As in decoders, multiplexers may have an enable input to control the operation of the unit. When the enable input is in the inactive state, the outputs are disabled, and when it is in the active state, the circuit functions as a normal multiplexer. The enable input is useful for expanding two or more multiplexers to a multiplexer with a larger number of inputs.

In some cases two or more multiplexers are enclosed within a single integrated circuit package. The selection and the enable inputs in multiple-unit construction are usually common to all multiplexers. As an illustration, the block diagram of a quadruple 2-to-l-line multiplexer is shown in Fig. 2-6. The circuit has four multiplexers, each capable of selecting one of two input lines. Output Y_0 can be selected to come from either input A_0 or B_0 . Similarly, output Y_1 may have the value of A_1 or B_1 and so on. One input selection line S selects one of the lines in each of the four multiplexers. The enable input E must be active for normal

Enable — Select — EYQuadruple 0 Y_1 x All 0's 2×1 $-Y_{9}$ 1 0 Amultiplexers A_3 - $-Y_3$ 1 1 B(b) Function table B_1 - B_{2} - B_3 – (a) Block diagram

Figure 2-6 Quadruple 2-to-1 line multiplexers.



Clock	Clear	Load	Increment	Operation
↑	0	0	0 1	No change Increment count by 1
↑	0 1	1 ×	×	Load inputs I_0 through I_3 Clear outputs to 0

TABLE 2-5 Function Table for the Register of Fig. 2-12

increment

operations. The *increment* operation adds one to the content of a register. By enabling the count input during one clock period, the content of the register can be incremented by one.

2-7 Memory Unit

word

byte

A memory unit is a collection of storage cells together with associated circuits needed to transfer information in and out of storage. The memory stores binary information in groups of bits called *words*. A word in memory is an entity of bits that move in and out of storage as a unit. A memory word is a group of l's and 0's and may represent a number, an instruction code, one or more alphanumeric characters, or any other binary-coded information. A group of eight bits is called a *byte*. Most computer memories use words whose number of bits is a multiple of 8. Thus a 16-bit word contains two bytes, and a 32-bit word is made up of four bytes. The capacity of memories in commercial computers is usually stated as the total number of bytes that can be stored.

The internal structure of a memory unit is specified by the number of words it contains and the number of bits in each word. Special input lines called address lines select one particular word. Each word in memory is assigned an identification number, called an address, starting from 0 and continuing with 1, 2, 3, up to $2^k - 1$ where k is the number of address lines. The selection of a specific word inside the memory is done by applying the k-bit binary address to the address lines. A decoder inside the memory accepts this address and opens the paths needed to select the bits of the specified word. Computer memories may range from 1024 words, requiring an address of 10 bits, to 2^{32} words, requiring 32 address bits. It is customary to refer to the number of words (or bytes) in a memory with one of the letters K (kilo), M (mega), or G (giga). K is equal to 2^{10} , M is equal to 2^{20} , and G is equal to 2^{30} . Thus, $64K = 2^{16}$, $2M = 2^{21}$, and $4G = 2^{32}$.

Two major types of memories are used in computer systems: random-access memory (RAM) and read-only memory (ROM). These semiconductor memories are classified into Random Access Memories (RAMs) and Sequential Access Memories (SAMs) based on access time. Memories constructed with shift registers, Charge Coupled Devices (CCDs), or bubble memories are examples of SAMs. RAMs are categorized into ROMs, Read Mostly Memories (RMMs), and Read Write Memories (RWMs). ROMs are of two types: Masked Programmed

ROMs and user Programmed PROMs. Two types of RMMs are Erasable and Programmable (EPROM), and Electrically Erasable (EEPROM). RWMs are Static RAM (SRAM) and Dynamic RAM (DRAM). Static RAMs have memory cells as common Flip-Flops. Dynamic RAMs have memory cells that must be refreshed, read and written periodically to avoid loss of memory cells.

Random-Access Memory

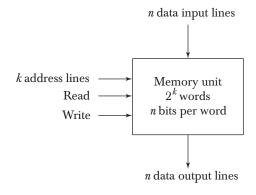
In random-access memory (RAM) the memory cells can be accessed for information transfer from any desired random location. That is, the process of locating a word in memory is the same and requires an equal amount of time no matter where the cells are located physically in memory: thus the name "random access."

Communication between a memory and its environment is achieved through data input and output lines, address selection lines, and control lines that specify the direction of transfer. A block diagram of a RAM unit is shown in Fig. 2-13. The n data input lines provide the information to be stored in memory, and the n data output lines supply the information coming out of memory. The k address lines provide a binary number of k bits that specify a particular word chosen among the 2^k available inside the memory. The two control inputs specify the direction of transfer desired.

The two operations that a random-access memory can perform are the write and read operations. The write signal specifies a transfer-in operation and the read signal specifies a transfer-out operation. On accepting one of these control signals, the internal circuits inside the memory provide the desired function. The steps that must be taken for the purpose of transferring a new word to be stored into memory are as follows:

- **1.** Apply the binary address of the desired word into the address lines.
- **2.** Apply the data bits that must be stored in memory into the data input lines.
- **3.** Activate the *write* input.

Figure 2-13 Block diagram of random access memory (RAM).



RAM

write and read operations

The memory unit will then take the bits presently available in the input data lines and store them in the word specified by the address lines.

The steps that must be taken for the purpose of transferring a stored word out of memory are as follows:

- 1. Apply the binary address of the desired word into the address lines.
- 2. Activate the *read* input.

The memory unit will then take the bits from the word that has been selected by the address and apply them into the output data lines. The content of the selected word does not change after reading.

Read-Only Memory

As the name implies, a read-only memory (ROM) is a memory unit that performs the read operation only; it does not have a write capability. This implies that the binary information stored in a ROM is made permanent during the hardware production of the unit and cannot be altered by writing different words into it. Whereas a RAM is a general-purpose device whose contents can be altered during the computational process, a ROM is restricted to reading words that are permanently stored within the unit. The binary information to be stored, specified by the designer, is then embedded in the unit to form the required interconnection pattern. ROMs come with special internal electronic fuses that can be "programmed" for a specific configuration. Once the pattern is established, it stays within the unit even when power is turned off and on again.

An $m \times n$ ROM is an array of binary cells organized into m words of n bits each. As shown in the block diagram of Fig. 2-14, a ROM has k address input lines to select one of $2^k = m$ words of memory, and n output lines, one for each bit of the word. An integrated circuit ROM may also have one or more enable inputs for expanding a number of packages into a ROM with larger capacity.

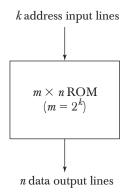


Figure 2-14 Block diagram of read only memory (ROM).

The ROM does not need a read-control line since at any given time, the output lines automatically provide the *n* bits of the word selected by the address value. Because the outputs are a function of only the present inputs (the address lines), a ROM is classified as a combinational circuit. In fact, a ROM is constructed internally with decoders and a set of OR gates. There is no need for providing storage capabilities as in a RAM, since the values of the bits in the ROM are permanently fixed.

ROMs find a wide range of applications in the design of digital systems. Basically, a ROM generates an input–output relation specified by a truth table. As such, it can implement any combinational circuit with k inputs and n outputs. When employed in a computer system as a memory unit, the ROM is used for storing fixed programs that are not to be altered and for tables of constants that are not subject to change. ROM is also employed in the design of control units for digital computers. As such, they are used to store coded information that represents the sequence of internal control variables needed for enabling the various operations in the computer. A control unit that utilizes a ROM to store binary control information is called a microprogrammed control unit. This subject is dicsussed in more detail in Chapter 7.

Types of ROMs

The required paths in a ROM may be programmed in three different ways. The first, *mask programming*, is done by the semiconductor company during the last fabrication process of the unit. The procedure for fabricating a ROM requires that the customer fill out the truth table that he or she wishes the ROM to satisfy. The truth table may be submitted in a special form provided by the manufacturer or in a specified format on a computer output medium. The manufacturer makes the corresponding mask for the paths to produce the l's and 0's according to the customer's truth table. This procedure is costly because the vendor charges the customer a special fee for custom masking the particular ROM. For this reason, mask programming is economical only if a large quantity of the same ROM configuration is to be ordered.

For small quantities it is more economical to use a second type of ROM called a *programmable read-only memory* or PROM. When ordered, PROM units contain all the fuses intact, giving all l's in the bits of the stored words. The fuses in the PROM are blown by application of current pulses through the output terminals for each address. A blown fuse defines a binary 0 state, and an intact fuse gives a binary 1 state. This allows users to program PROMs in their own laboratories to achieve the desired relationship between input addresses and stored words. Special instruments called *PROM programmers* are available commercially to facilitate this procedure. In any case, all procedures for programming ROMs are hardware procedures even though the word "programming" is used.

The hardware procedure for programming ROMs or PROMs is irreversible, and once programmed, the fixed pattern is permanent and cannot be altered. Once a bit pattern has been established, the unit must be discarded if the bit pattern is to be changed. A third type of ROM available is called *erasable PROM* or EPROM.

PROM



*R*1 and the address is in *AR*. The write operation can be stated symbolically as follows:

Write:
$$M[AR] \leftarrow R1$$

This causes a transfer of information from R1 into the memory word M selected by the address in AR.

4-4 Arithmetic Microoperations

A microoperation is an elementary operation performed with the data stored in registers. The microoperations most often encountered in digital computers are classified into four categories:

- **1.** Register transfer microoperations transfer binary information from one register to another.
- **2.** Arithmetic microoperations perform arithmetic operation on numeric data stored in registers.
- **3.** Logic microoperations perform bit manipulation operations on nonnumeric data stored in registers.
- **4.** Shift microoperations perform shift operations on data stored in registers.

The register transfer microoperation was introduced in Sec. 4-2. This type of microoperation does not change the information content when the binary information moves from the source register to the destination register. The other three types of microoperations change the information content during the transfer. In this section we introduce a set of arithmetic microoperations. In the next two sections we present the logic and shift microoperations.

The basic arithmetic microoperations are addition, subtraction, increment, decrement, and shift. Arithmetic shifts are explained later in conjunction with the shift microoperations. The arithmetic microoperation defined by the statement

$$R3 \leftarrow R1 + R2$$

add microoperation specifies an add microoperation. It states that the contents of register R1 are added to the contents of register R2 and the sum transferred to register R3. To implement this statement with hardware we need three registers and the digital component that performs the addition operation. The other basic arithmetic microoperations are listed in Table 4-3. Subtraction is most often

subtract microoperation implemented through complementation and addition. Instead of using the minus operator, we can specify the subtraction by the following statement:

$$R3 \leftarrow R1 + \overline{R2} + 1$$

 $\overline{R2}$ is the symbol for the 1's complement of R2. Adding 1 to the 1's complement produces the 2's complement. Adding the contents of R1 to the 2's complement of R2 is equivalent to R1 - R2.

Symbolic designation $R3 \leftarrow R1 + R2$ $R3 \leftarrow R1 - R2$ $R3 \leftarrow R1 - R2$ $R3 \leftarrow R1 - R2$ Contents of R1 plus R2 transferred to R3 $R2 \leftarrow \overline{R2}$ Contents of R1 minus R2 transferred to R3 $R2 \leftarrow \overline{R2}$ Complement the contents of R2 (1's complement) $R2 \leftarrow \overline{R2} + 1$ $R3 \leftarrow R1 + \overline{R2} + 1$ R1 plus the 2's complement of R2 (subtraction) $R1 \leftarrow R1 + 1$ Increment the contents of R1 by one

TABLE 4-3 Arithmetic Microoperations

The increment and decrement microoperations are symbolized by plusone and minus-one operations, respectively. These microoperations are implemented with a combinational circuit or with a binary up-down counter.

Decrement the contents of R1 by one

The arithmetic operations of multiply and divide are not listed in Table 4-3. These two operations are valid arithmetic operations but are not included in the basic set of microoperations. The only place where these operations can be considered as microoperations is in a digital system, where they are implemented by means of a combinational circuit. In such a case, the signals that perform these operations propagate through gates, and the result of the operation can be transferred into a destination register by a clock pulse as soon as the output signal propagates through the combinational circuit. In most computers, the multiplication operation is implemented with a sequence of add and shift microoperations. Division is implemented with a sequence of subtract and shift microoperations. To specify the hardware in such a case requires a list of statements that use the basic microoperations of add, subtract, and shift (see Chapter 10).

Binary Adder

 $R1 \leftarrow R1 - 1$

To implement the add microoperation with hardware, we need the registers that hold the data and the digital component that performs the arithmetic addition. The digital circuit that forms the arithmetic sum of two bits and a previous carry is called a full-adder (see Fig. 1-17). The digital circuit that

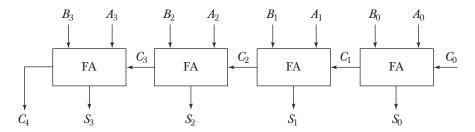


Figure 4-6 4-bit binary adder.

binary adder

full-adder

generates the arithmetic sum of two binary numbers of any length is called a binary adder. The binary adder is constructed with full-adder circuits connected in cascade, with the output carry from one full-adder connected to the input carry of the next full-adder. Figure 4-6 shows the interconnections of four full-adders (FA) to provide a 4-bit binary adder. The augend bits of A and the addend bits of B are designated by subscript numbers from right to left, with subscript 0 denoting the low-order bit. The carries are connected in a chain through the full-adders. The input carry to the binary adder is C_0 and the output carry is C_4 . The S outputs of the full-adders generate the required sum bits.

An n-bit binary adder requires n full-adders. The output carry from each full-adder is connected to the input carry of the next-high-order full-adder. The n data bits for the A inputs come from one register (such as R1), and the n data bits for the B inputs come from another register (such as R2). The sum can be transferred to a third register or to one of the source registers (R1 or R2), replacing its previous content.

Binary Adder-Subtractor

The subtraction of binary numbers can be done most conveniently by means of complements as discussed in Sec. 3-2. Remember that the subtraction A-B can be done by taking the 2's complement of B and adding it to A. The 2's complement can be obtained by taking the 1's complement and adding one to the least significant pair of bits. The 1's complement can be implemented with inverters and a one can be added to the sum through the input carry.

The addition and subtraction operations can be combined into one common circuit by including an exclusive-OR gate with each full-adder. A 4-bit adder-subtractor circuit is shown in Fig. 4-7. The mode input M controls the operation. When M=0 the circuit is an adder and when M=1 the circuit becomes a subtractor. Each exclusive-OR gate receives input M and one of the inputs of B. When M=0, we have $B\oplus 0=B$. The full-adders receive the value of B, the input carry is D0, and the circuit performs D1 plus D2. When D3 we have D4 and D5 inputs are all complemented and a 1 is added through the input carry. The circuit performs the operation D4 plus the

adder-subtractor





CHAPTER THREE

Data Representation

IN THIS CHAPTER

- 3-1 Data Types
- 3-2 Complements
- **3-3** Fixed-Point Representation
- **3-4** Floating-Point Representation
- 3-5 Other Binary Codes
- **3-6** Error Detection Codes

3-1 Data Types

The term data refers to factual information used for analysis or reasoning. Data itself has no meaning, but becomes information when it is assigned a meaning or interpreted. Information is a collection of facts or data that is communicated. Binary information in digital computers is stored in memory or processor registers. Registers contain either data or control information. Control information is a bit or a group of bits used to specify the sequence of command signals needed for manipulation of the data in other registers. Data are numbers and other binary-coded information that are operated on to achieve required computational results. In this chapter we present the most common types of data found in digital computers and show how the various data types are represented in binary-coded form in computer registers.

The data types found in the registers of digital computers may be classified as being one of the following categories: (1) numbers used in arithmetic computations, (2) letters of the alphabet used in data processing, and (3) other discrete symbols used for specific purposes. All types of data, except binary numbers, are represented in computer registers in binary-coded form. This is because registers are made up of flip-flops and flip-flops are two-state devices that can store only I's and 0's. The binary number system is the most natural system to use in a digital computer. But sometimes it is convenient to employ different number systems, especially the decimal number system, since it is used by people to perform arithmetic computations.

Number Systems

radix

decimal

A number system of *base*, or *radix*, r is a system that uses distinct symbols for r digits. Numbers are represented by a string of digit symbols. To determine the quantity that the number represents, it is necessary to multiply each digit by an integer power of r and then form the sum of all weighted digits. For example, the decimal number system in everyday use employs the radix 10 system. The 10 symbols are 0, 1, 2, 3, 4, 5, 6, 7, 8, and 9. The string of digits 724.5 is interpreted to represent the quantity

$$7 \times 10^2 + 2 \times 10^1 + 4 \times 10^0 + 5 \times 10^{-1}$$

that is, 7 hundreds, plus 2 tens, plus 4 units, plus 5 tenths. Every decimal number can be similarly interpreted to find the quantity it represents.

The *binary* number system uses the radix 2. The two digit symbols used are 0 and 1. The string of digits 101101 is interpreted to represent the quantity

$$1 \times 2^5 + 0 \times 2^4 + 1 \times 2^3 + 1 \times 2^2 + 0 \times 2^1 + 1 \times 2^0 = 45$$

To distinguish between different radix numbers, the digits will be enclosed in parentheses and the radix of the number inserted as a subscript. For example, to show the equality between decimal and binary forty-five we will write $(101101)_2 = (45)_{10}$.

Besides the decimal and binary number systems, the *octal* (radix 8) and *hexadecimal* (radix 16) are important in digital computer work. The eight symbols of the octal system are 0, 1, 2, 3, 4, 5, 6, and 7. The 16 symbols of the hexadecimal system are 0, 1, 2, 3, 4, 5, 6, 7, 8, 9, A, B, C, D, E, and F. The last six symbols are, unfortunately, identical to the letters of the alphabet and can cause confusion at times. However, this is the convention that has been adopted. When used to represent hexadecimal digits, the symbols A, B, C, D, E, F correspond to the decimal numbers 10, 11, 12, 13, 14, 15, respectively.

A number in radix r can be converted to the familiar decimal system by forming the sum of the weighted digits. For example, octal 736.4 is converted to decimal as follows:

$$(736.4)_8 = 7 \times 8^2 + 3 \times 8^1 + 6 \times 8^0 + 4 \times 8^{-1}$$

= $7 \times 64 + 3 \times 8 + 6 \times 1 + 4/8 = (478.5)_{10}$

The equivalent decimal number of hexadecimal F3 is obtained from the following calculation:

$$(F3)_{16} = F \times 16 + 3 = 15 \times 16 + 3 = (243)_{10}$$

conversion

Conversion from decimal to its equivalent representation in the radix r system is carried out by separating the number into its *integer* and *fraction* parts and

binary

octal hexadecimal converting each part separately. The conversion of a decimal integer into a base r representation is done by successive divisions by r and accumulation of the remainders. The conversion of a decimal fraction to radix r representation is accomplished by successive multiplications by r and accumulation of the integer digits so obtained. Figure 3-1 demonstrates these procedures.

The conversion of decimal 41.6875 into binary is done by first separating the number into its integer part 41 and fraction part .6875. The integer part is converted by dividing 41 by r=2 to give an integer quotient of 20 and a remainder of 1. The quotient is again divided by 2 to give a new quotient and remainder. This process is repeated until the integer quotient becomes 0. The coefficients of the binary number are obtained from the remainders with the first remainder giving the low-order bit of the converted binary number.

The fraction part is converted by multiplying it by r=2 to give an integer and a fraction. The new fraction (*without* the integer) is multiplied again by 2 to give a new integer and a new fraction. This process is repeated until the fraction part becomes zero or until the number of digits obtained gives the required accuracy. The coefficients of the binary fraction are obtained from the integer digits with the first integer computed being the digit to be placed next to the binary point. Finally, the two parts are combined to give the total required conversion.

Octal and Hexadecimal Numbers

The conversion from and to binary, octal, and hexadecimal representation plays an important part in digital computers. Since $2^3 = 8$ and $2^4 = 16$, each octal digit corresponds to three binary digits and each hexadecimal digit corresponds to four binary digits. The conversion from binary to octal is easily accomplished by partitioning the binary number into groups of three bits each. The corresponding octal digit is then assigned to each group of bits and the string of digits so obtained gives the octal equivalent of the binary number. Consider, for example, a 16-bit register. Physically, one may think of the

Figure 3-1 Conversion of decimal 41.6875 into binary.

Integer = 41	Fraction = 0.6875			
41	0.6875			
20 1 10 0	$\frac{2}{1.3750}$			
	1.3730 × 2			
$ \begin{array}{c cccc} 5 & 0 \\ 2 & 1 \\ 1 & 0 \end{array} $	$\frac{0.7500}{0.7500}$			
$\begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}$	$\underline{\hspace{1cm} \times 2}$			
0 1	1.5000			
	$\frac{\times 2}{1.0000}$			
$(41)_{10} = (101001)_2$	$(0.6875)_{10} = (0.1011)_2$			
$(41.6875)_{10} = (101001.1011)_2$				

$$\underbrace{\frac{1}{1} \underbrace{\frac{2}{0} \underbrace{1} \underbrace{0}}_{A} \underbrace{\frac{7}{1} \underbrace{1} \underbrace{1}_{1} \underbrace{\frac{5}{0} \underbrace{1}_{1} \underbrace{1}_{0} \underbrace{0}_{0} \underbrace{0}_{1} \underbrace{1}_{1}}_{6}}_{\mathbf{f}_{0}} \underbrace{\frac{3}{0} \underbrace{0}_{1} \underbrace{0}$$

Figure 3-2 Binary, octal, and hexadecimal conversion.

register as composed of 16 binary storage cells, with each cell capable c holding either a 1 or a 0. Suppose that the bit configuration stored in the register is as shown in Fig. 3-2. Since a binary number consists of a string of l's and 0's, the 16-bit register can be used to store any binary number from 0 to $2^{16}-1$. For the particular example shown, the binary number stored in the register is the equivalent of decimal 44899. Starting from the low-order bit, we partition the register into groups of three bits each (the sixteenth bit remains in a group by itself). Each group of three bits is assigned its octal equivalent and placed on top of the register. The string of octal digits so obtained represents the octal equivalent of the binary number.

Conversion from binary to hexadecimal is similar except that the bits are divided into groups of four. The corresponding hexadecimal digit for each group of four bits is written as shown below the register of Fig. 3-2. The string of hexadecimal digits so obtained represents the hexadecimal equivalent of the binary number. The corresponding octal digit for each group of three bits is easily remembered after studying the first eight entries listed in Table 3-1. The correspondence between a hexadecimal digit and its equivalent 4-bit code can be found in the first 16 entries of Table 3-2.

Octal number	Binary-coded octal	Decimal equivalent	
0	000	0	A
1	001	1	
2	010	2	Code
3	011	3	for one
4	100	4	octal
5	101	5	digit
6	110	6	
7	111	7	\
10	001 000	8	
11	001 001	9	
12	001 010	10	
24	010 100	20	
62	110 010	50	
143	001 100 011	99	
370	011 111 000	248	

TABLE 3-1 Binary-Coded Octal Numbers

Table 3-1 lists a few octal numbers and their representation in registers in binary-coded form. The binary code is obtained by the procedure explained above. Each octal digit is assigned a 3-bit code as specified by the entries of the first eight digits in the table. Similarly, Table 3-2 lists a few hexadecimal numbers and their representation in registers in binary-coded form. Here the binary code is obtained by assigning to each hexadecimal digit the 4-bit code listed in the first 16 entries of the table.

Comparing the binary-coded octal and hexadecimal numbers with their binary number equivalent we find that the bit combination in all three representations is exactly the same. For example, decimal 99, when converted to binary, becomes 1100011. The binary-coded octal equivalent of decimal 99 is 001 100 011 and the binary-coded hexadecimal of decimal 99 is 0110 0011. If we neglect the leading zeros in these three binary representations, we find that their bit combination is identical. This should be so because of the straightforward conversion that exists between binary numbers and octal or hexadecimal. The point of all this is that a string of l's and 0's stored in a register could represent a binary number, but this same string of bits may be interpreted as holding an octal number in binary-coded form (if we divide the bits in groups of three) or as holding a hexadecimal number in binary-coded form (if we divide the bits in groups of four).

TABLE 3-2 Binary-Coded Hexadecimal Numbers

Hexadecimal number	Binary-coded hexadecimal	Decimal equivalent	
0	0000	0	<u> </u>
1	0001	1	T
2	0010	2	
3	0011	3	
4	0100	4	
5	0101	5	
6	0110	6	Code
7	0111	7	for one
8	1000	8	hexadecimal
9	1001	9	digit
A	1010	10	1
В	1011	11	
C	1100	12	
D	1101	13	
E	1110	14	
F	1111	15	Y
14	0001 0100	20	
32	0011 0010	50	
63	0110 0011	99	
F8	1111 1000	248	

The registers in a digital computer contain many bits. Specifying the content of registers by their binary values will require a long string of binary digits. It is more convenient to specify content of registers by their octal or hexadecimal equivalent. The number of digits is reduced by one-third in the octal designation and by one-fourth in the hexadecimal designation. For example, the binary number 1111 1111 1111 has 12 digits. It can be expressed in octals as 7777 (four digits) or in hexadecimal as FFF (three digits). Computer manuals invariably choose either the octal or the hexadecimal designation for specifying contents of registers.

Decimal Representation

The binary number system is the most natural system for a computer, but people are accustomed to the decimal system. One way to solve this conflict is to convert all input decimal numbers into binary numbers, let the computer perform all arithmetic operations in binary and then convert the binary results back to decimal for the human user to understand. However, it is also possible for the computer to perform arithmetic operations directly with decimal numbers provided they are placed in registers in a coded form. Decimal numbers enter the computer usually as binary-coded alphanumeric characters. These codes, introduced later, may contain from six to eight bits for each decimal digit. When decimal numbers are used for internal arithmetic computations, they are converted to a binary code with four bits per digit.

A binary code is a group of n bits that assume up to 2^n distinct combinations of l's and 0's with each combination representing one element of the set that is being coded. For example, a set of four elements can be coded by a 2-bit code with each element assigned one of the following bit combinations; 00, 01, 10, or 11. A set of eight elements requires a 3-bit code, a set of 16 elements requires a 4-bit code, and so on. A binary code will have some unassigned bit combinations if the number of elements in the set is not a multiple power of 2. The 10 decimal digits form such a set. A binary code that distinguishes among 10 elements must contain at least four bits, but six combinations will remain unassigned. Numerous different codes can be obtained by arranging four bits in 10 distinct combinations. The bit assignment most commonly used for the decimal digits is the straight binary assignment listed in the first 10 entries of Table 3-3. This particular code is called *binary-coded decimal* and is commonly referred to by its abbreviation BCD. Other decimal codes are sometimes used and a few of them are given in Sec. 3-5.

It is very important to understand the difference between the *conversion* of decimal numbers into binary and the *binary coding* of decimal numbers. For example, when *converted* to a binary number, the decimal number 99 is represented by the string of bits 1100011, but when represented in BCD, it becomes 1001 1001. The *only* difference between a decimal number represented by the familiar digit symbols 0, 1, 2, . . . , 9 and the BCD symbols 0001, 0010, . . . , 1001 is in the symbols used to represent the digits—the

binary code

BCD

Decimal Binary-coded decimal (BCD) number number 0 0000 1 0001 2 0010 3 Code 0011 4 0100 for one 5 0101 decimal 6 0110 digit 7 0111 8 1000 9 1001 10 0001 0000 20 0010 0000 50 0101 0000 99 1001 1001 248 0010 0100 1000

TABLE 3-3 Binary-Coded Decimal (BCD) Numbers

number itself is exactly the same. A few decimal numbers and their representation in BCD are listed in Table 3-3.

Alphanumeric Representation

Many applications of digital computers require the handling of data that consist not only of numbers, but also of the letters of the alphabet and certain special characters. An *alphanumeric character set* is a set of elements that includes the 10 decimal digits, the 26 letters of the alphabet and a number of special characters, such as \$, +, and =. Such a set contains between 32 and 64 elements (if only uppercase letters are included) or between 64 and 128 (if both uppercase and lowercase letters are included). In the first case, the binary code will require six bits and in the second case, seven bits. The standard alphanumeric binary code is the ASCII (American Standard Code for Information Interchange), which uses seven bits to code 128 characters. The binary code for the uppercase letters, the decimal digits, and a few special characters is listed in Table 3-4. Note that the decimal digits in ASCII can be converted to BCD by removing the three high-order bits, 011. A complete list of ASCII characters is provided in Table 11-1.

Binary codes play an important part in digital computer operations. The codes must be in binary because registers can only hold binary information. One must realize that binary codes merely change the symbols, not the meaning of the discrete elements they represent. The operations specified for digital computers must take into consideration the meaning of the

character

ASCII



TABLE 5-4 American Standard Code for information interchange (ASCII)					
Character	Binary code	Character	Binary code		
A	100 0001	0	011 0000		
В	100 0010	1	011 0001		
C	100 0011	2	011 0010		
D	100 0100	3	011 0011		
E	100 0101	4	011 0100		
F	100 0110	5	011 0101		
G	100 0111	6	011 0110		
Н	100 1000	7	011 0111		
I	100 1001	8	011 1000		
J	100 1010	9	011 1001		
K	100 1011				
L	100 1100				
M	100 1101	space	010 0000		
N	100 1110	•	010 1110		
O	100 1111	(010 1000		
P	101 0000	+	010 1011		
Q	101 0001	\$	010 0100		
Ř	101 0010	*	010 1010		
S	101 0011)	010 1001		
T	101 0100	_	010 1101		
U	101 0101	/	010 1111		
V	101 0110	,	010 1100		
W	101 0111	=	011 1101		
X	101 1000				
Y	101 1001				

TABLE 3-4 American Standard Code for information Interchange (ASCII)

bits stored in registers so that operations are performed on operands of the same type. In inspecting the bits of a computer register at random, one is likely to find that it represents some type of coded information rather than a binary number.

101 1010

Binary codes can be formulated for any set of discrete elements such as the musical notes and chess pieces and their positions on the chessboard. Binary codes are also used to formulate instructions that specify control information for the computer. This chapter is concerned with *data* representation. Instruction codes are discussed in Chap. 5.

3-2 Complements

Z

Complements are used in digital computers for simplifying the subtraction operation and for logical manipulation. There are two types of complements for each base r system: the r's complement and the (r-1)'s complement.

When the value of the base r is substituted in the name, the two types are referred to as the 2's and 1's complement for binary numbers and the 10's and 9's complement for decimal numbers.

(r-1)'s Complement

9's complement

Given a number N in base r having n digits, the (r-1)'s complement of N is defined as $(r^n-1)-N$. For decimal numbers r=10 and r-1=9, so the 9's complement of N is $(10^n-1)-N$. Now, 10^n represents a number that consists of a single 1 followed by n 0's. 10^n-1 is a number represented by n 9's. For example, with n=4 we have $10^4=10000$ and $10^4-1=9999$. It follows that the 9's complement of a decimal number is obtained by subtracting each digit from 9. For example, the 9's complement of 546700 is 999999-546700=453299 and the 9's complement of 12389 is 99999-12389=87610.

1's complement

For binary numbers, r = 2 and r - 1 = 1, so the 1's complement of N is $(2^n - 1) - N$. Again, 2^n is represented by a binary number that consists of a 1 followed by n 0's. $2^n - 1$ is a binary number represented by n 1's. For example, with n = 4, we have $2^4 = (10000)_2$ and $2^4 - 1 = (1111)_2$. Thus the 1's complement of a binary number is obtained by subtracting each digit from 1. However, the subtraction of a binary digit from 1 causes the bit to change from 0 to 1 or from 1 to 0. Therefore, the 1's complement of a binary number is formed by changing 1's into 0's and 0's into 1's. For example, the 1's complement of 1011001 is 0100110 and the 1's complement of 0001111 is 1110000.

The (r-1)'s complement of octal or hexadecimal numbers are obtained by subtracting each digit from 7 or F (decimal 15) respectively.

(r's) Complement

The r's complement of an n-digit number N in base r is defined as $r^n - N$ for $N \neq 0$ and 0 for N = 0. Comparing with the (r - 1)'s complement, we note that the r's complement is obtained by adding 1 to the (r - 1)'s complement since $r^n - N = [(r^n - 1) - N] + 1$. Thus the 10's complement of the decimal 2389 is 7610 + 1 = 7611 and is obtained by adding 1 to the 9's complement value. The 2's complement of binary 101100 is 010011 + 1 = 010100 and is obtained by adding 1 to the 1's complement value.

10's complement

Since 10^n is a number represented by a 1 followed by n 0's, then $10^n - N$, which is the 10's complement of N, can be formed also be leaving all least significant 0's unchanged, subtracting the first nonzero least significant digit from 10, and then subtracting all higher significant digits from 9. The 10's complement of 246700 is 753300 and is obtained by leaving the two zeros unchanged, subtracting 7 from 10, and subtracting the other three digits from 9. Similarly, the 2's complement can be formed by leaving all least significant 0's and the first 1 unchanged, and then replacing l's by 0's and 0's by l's in all other higher, significant bits. The 2's complement of 1101100 is 0010100 and is obtained by leaving the two low-order 0's and the first 1 unchanged, and then replacing l's by 0's and 0's by l's in the other four most significant bits.

2's complement

In the definitions above it was assumed that the numbers do not have a radix point. If the original number N contains a radix point, it should be removed temporarily to form the r's or (r-1)'s complement. The radix point is then restored to the complemented number in the same relative position. It is also worth mentioning that the complement of the complement restores the number to its original value. The r's complement of N is $r^n - N$. The complement of the complement is $r^n - (r^n - N) = N$ giving back the original number.

Subtraction of Unsigned Numbers

The direct method of subtraction taught in elementary schools uses the borrow concept. In this method we borrow a 1 from a higher significant position when the minuend digit is smaller than the corresponding subtrahend digit. This seems to be easiest when people perform subtraction with paper and pencil. When subtraction is implemented with digital hardware, this method is found to be less efficient than the method that uses complements.

The subtraction of two n-digit unsigned numbers $M - N(N \neq 0)$ in base r can be done as follows:

- **1.** Add the minuend M to the r's complement of the subtrahend N. This performs $M + (r^n N) = M N + r^n$.
- **2.** If $M \ge N$, the sum will produce an end carry r^n which is discarded, and what is left is the result M N.
- **3.** If M < N, the sum does not produce an end carry and is equal to $r^n (N M)$, which is the r's complement of (N M). To obtain the answer in a familiar form, take the r's complement of the sum and place a negative sign in front.

Consider, for example, the subtraction 72532 - 13250 = 59282. The 10's complement of 13250 is 86750. Therefore:

```
M = 72532

10's complement of N = +86750

Sum = 159282

Discard end carry 10^5 = -\frac{100000}{59282}

Answer = \frac{100000}{59282}
```

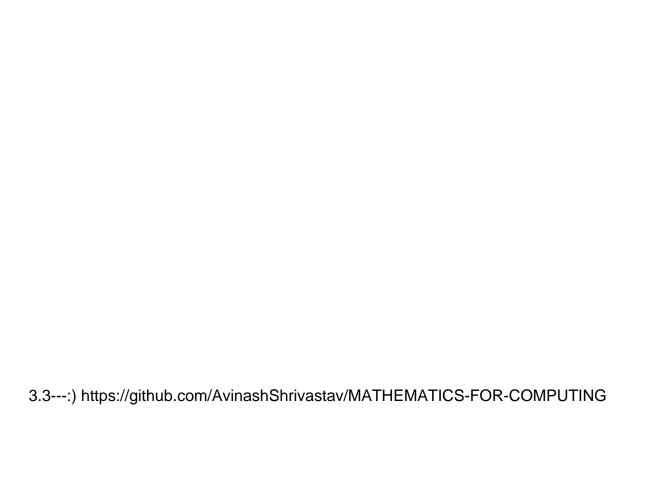
Now consider an example with M < N. The subtraction 13250 - 72532 produces negative 59282. Using the procedure with complements, we have

$$M = 13250$$
10's complement of $N = +27468$

$$Sum = 40718$$

subtraction

end carry



There is no end carry

Answer is negative 59282 = 10's complement of 40718

Since we are dealing with unsigned numbers, there is really no way to get an unsigned result for the second example. When working with paper and pencil, we recognize that the answer must be changed to a signed negative number. When subtracting with complements, the negative answer is recognized by the absence of the end carry and the complemented result.

Subtraction with complements is done with binary numbers in a similar manner using the same procedure outlined above. Using the two binary numbers X = 1010100 and Y = 1000011, we perform the subtraction X - Y and Y - X using 2's complements:

```
X = 1010100
2's complement of Y = \frac{+0111101}{10010001}
Sum = \frac{10010001}{10010001}
Discard end carry 2^7 = -10000000
Answer: X - Y = 0010001
Y = \frac{+000011}{+0101100}
Sum = \frac{1101111}{11011111}
```

There is no end carry

Answer is negative 0010001 = 2's complement of 1101111

3-3 Fixed-Point Representation

Positive integers, including zero, can be represented as unsigned numbers. However, to represent negative integers, we need a notation for negative values. In ordinary arithmetic, a negative number is indicated by a minus sign and a positive number by a plus sign. Because of hardware limitations, computers must represent everything with l's and 0's, including the sign of a number. As a consequence, it is customary to represent the sign with a bit placed in the leftmost position of the number. The convention is to make the sign bit equal to 0 for positive and to 1 for negative.

binary point

In addition to the sign, a number may have a binary (or decimal) point. The position of the binary point is needed to represent fractions, integers, or mixed integer-fraction numbers. The representation of the binary point in a register is complicated by the fact that it is characterized by a position in the register. There are two ways of specifying the position of the binary point in a register: by giving it a fixed position or by employing a floating-point representation. The fixed-point method assumes that the binary point is

always fixed in one position. The two positions most widely used are (1) a binary point in the extreme left of the register to make the stored number a fraction, and (2) a binary point in the extreme right of the register to make the stored number an integer. In either case, the binary point is not actually present, but its presence is assumed from the fact that the number stored in the register is treated as a fraction or as an integer. The floating-point representation uses a second register to store a number that designates the position of the decimal point in the first register. Floating-point representation is discussed further in the next section.

Integer Representation

signed numbers

When an integer binary number is positive, the sign is represented by 0 and the magnitude by a positive binary number. When the number is negative, the sign is represented by 1 but the rest of the number may be represented in one of three possible ways:

- 1. Signed-magnitude representation
- 2. Signed-1's complement representation
- 3. Signed 2's complement representation

The signed-magnitude representation of a negative number consists of the magnitude and a negative sign. In the other two representations, the negative number is represented in either the l's or 2's complement of its positive value. As an example, consider the signed number 14 stored in an 8-bit register. +14 is represented by a sign bit of 0 in the leftmost position followed by the binary equivalent of 14:00001110. Note that each of the eight bits of the register must have a value and therefore 0's must be inserted in the most significant positions following the sign bit. Although there is only one way to represent +14, there are three different ways to represent -14 with eight bits.

In signed-magnitude representation	1 0001110
In signed-1's complement representation	1 1110001
In signed-2's complement representation	1 1110010

The signed-magnitude representation of -14 is obtained from +14 by complementing only the sign bit. The signed-1's complement representation of -14 is obtained by complementing all the bits of +14, including the sign bit. The signed-2's complement representation is obtained by taking the 2's complement of the positive number, including its sign bit.

The signed-magnitude system is used in ordinary arithmetic but is awkward when employed in computer arithmetic. Therefore, the signedcomplement is normally used. The l's complement imposes difficulties because

11111010

00001101

00000111

it has two representations of $0 \ (+0 \ and \ -0)$. It is seldom used for arithmetic operations except in some older computers. The l's complement is useful as a logical operation since the change of 1 to 0 or 0 to 1 is equivalent to a logical complement operation. The following discussion of signed binary arithmetic deals exclusively with the signed-2's complement representation of negative numbers.

Arithmetic Addition

The addition of two numbers in the signed-magnitude system follows the rules of ordinary arithmetic. If the signs are the same, we add the two magnitudes and give the sum the common sign. If the signs are different, we subtract the smaller magnitude from the larger and give the result the sign of the larger magnitude. For example, (+25) + (-37) = -(37 - 25) = -12 and is done by subtracting the smaller magnitude 25 from the larger magnitude 37 and using the sign of 37 for the sign of the result. This is a process that requires the comparison of the signs and the magnitudes and then performing either addition or subtraction. (The procedure for adding binary numbers in signed-magnitude representation is described in Sec. 10-2.) By contrast, the rule for adding numbers in the signed-2's complement system does not require a comparison or subtraction, only addition and complementation. The procedure is very simple and can be stated as follows: Add the two numbers, including their sign bits, and discard any carry out of the sign (leftmost) bit position. Numerical examples for addition are shown below. Note that negative numbers must initially be in 2's complement and that if the sum obtained after the addition is negative, it is in 2's complement form.

In each of the four cases, the operation performed is always addition, including the sign bits. Any carry out of the sign bit position is discarded, and negative results are automatically in 2's complement form.

The complement form of representing negative numbers is unfamiliar to people used to the signed-magnitude system. To determine the value of a negative number when in signed-2's complement, it is necessary to convert it to a positive number to place it in a more familiar form. For example, the signed binary number 11111001 is negative because the leftmost bit is 1. Its 2's complement is 00000111, which is the binary equivalent of +7. We therefore recognize the original negative number to be equal to -7.

2's complement addition

Arithmetic Subtraction

2's complement subtraction

Subtraction of two signed binary numbers when negative numbers are in 2's complement form is very simple and can be stated as follows: Take the 2's complement of the subtrahend (including the sign bit) and add it to the minuend (including the sign bit). A carry out of the sign bit position is discarded.

This procedure stems from the fact that a subtraction operation can be changed to an addition operation if the sign of the subtrahend is changed .This is demonstrated by the following relationship:

$$(\pm A) - (+B)$$
 = $(\pm A) + (-B)$
 $(\pm A) - (-B)$ = $(\pm A) + (+B)$

But changing a positive number to a negative number is easily done by taking its 2's complement. The reverse is also true because the complement of a negative number in complement form produces the equivalent positive number. Consider the subtraction of (-6) - (-13) = +7. In binary with eight bits this is written as 11111010 - 11110011. The subtraction is changed to addition by taking the 2's complement of the subtrahend (-13) to give (+13). In binary this is 11111010 + 00001101 = 100000111. Removing the end carry, we obtain the correct answer 00000111 (+7).

It is worth noting that binary numbers in the signed-2's complement system are added and subtracted by the same basic addition and subtraction rules as unsigned numbers. Therefore, computers need only one common hardware circuit to handle both types of arithmetic. The user or programmer must interpret the results of such addition or subtraction differently depending on whether it is assumed that the numbers are signed or unsigned.

Overflow

overflow

When two numbers of n digits each are added and the sum occupies n+1 digits, we say that an overflow occurred. When the addition is performed with paper and pencil, an overflow is not a problem since there is no limit to the width of the page to write down the sum. An overflow is a problem in digital computers because the width of registers is finite. A result that contains n+1 bits cannot be accommodated in a register with a standard length of n bits. For this reason, many computers detect the occurrence of an overflow, and when it occurs, a corresponding flip-flop is set which can then be checked by the user.

The detection of an overflow after the addition of two binary numbers depends on whether the numbers are considered to be signed or unsigned. When two unsigned numbers are added, an overflow is detected from the end carry out of the most significant position. In the case of signed numbers, the leftmost bit always represents the sign, and negative numbers are in 2's complement form. When two signed numbers are added, the

sign bit is treated as part of the number and the end carry does not indicate an overflow.

An overflow cannot occur after an addition if one number is positive and the other is negative, since adding a positive number to a negative number produces a result that is smaller than the larger of the two original numbers. An overflow may occur if the two numbers added are both positive or both negative. To see how this can happen, consider the following example. Two signed binary numbers, +70 and +80, are stored in two 8-bit registers. The range of numbers that each register can accommodate is from binary +127 to binary -128. Since the sum of the two numbers is +150, it exceeds the capacity of the 8-bit register. This is true if the numbers are both positive or both negative. The two additions in binary are shown below together with the last two carries.

carries:	0 1	carries:	1 0
+70	0 1000110	-70	1 0111010
+80	0 1010000	-80	1 0110000
$+1\overline{50}$	1 0010110	$-1\overline{50}$	0 1101010

Note that the 8-bit result that should have been positive has a negative sign bit and the 8-bit result that should have been negative has a positive sign bit. If, however, the carry out of the sign bit position is taken as the sign bit of the result, the 9-bit answer so obtained will be correct. Since the answer cannot be accommodated within 8 bits, we say that an overflow occurred.

overflow detection

An overflow condition can be detected by observing the carry into the sign bit position and the carry out of the sign bit position. If these two carries are not equal, an overflow condition is produced. This is indicated in the examples where the two carries are explicitly shown. If the two carries are applied to an exclusive-OR gate, an overflow will be detected when the output of the gate is equal to 1.

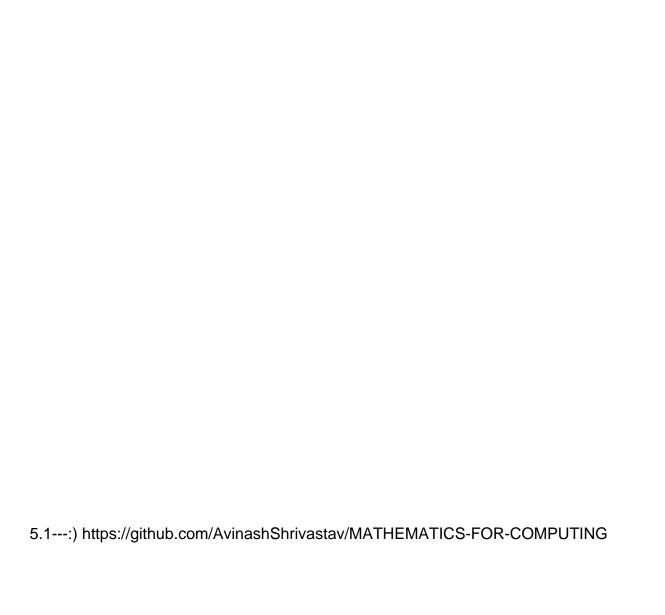
Decimal Fixed-Point Representation

The representation of decimal numbers in registers is a function of the binary code used to represent a decimal digit. A 4-bit decimal code requires four flip-flops for each decimal digit. The representation of 4385 in BCD requires 16 flip-flops, four flip-flops for each digit. The number will be represented in a register with 16 flip-flops as follows:

0100 0011 1000 0101

By representing numbers in decimal we are wasting a considerable amount of storage space since the number of bits needed to store a decimal number in a binary code is greater than the number of bits needed for its equivalent binary representation. Also, the circuits required to perform decimal





CHAPTER FIVE

Basic Computer Organization and Design

IN THIS CHAPTER

5-1	Instruction Codes
5-2	Computer Registers
5-3	Computer Instructions
5-4	Timing and Control
5-5	Instruction Cycle
5-6	Memory-Reference Instructions
5-7	Input-Output and Interrupt
5-8	Complete Computer Description
5-9	Design of Basic Computer
5-10	Design of Accumulator Logic

5-1 Instruction Codes

In this chapter we introduce a basic computer and show how its operation can be specified with register transfer statements. The organization of the computer is defined by its internal registers, the riming and control structure, and the set of instructions that it uses. The design of the computer is then carried out in detail. Although the basic computer presented in this chapter is very small compared to commercial computers, it has the advantage of being simple enough so we can demonstrate the design process without too many complications.

The internal organization of a digital system is defined by the sequence of microoperations it performs on data stored in its registers. The general-purpose digital computer is capable of executing various microoperations and, in addition, can be instructed as to what specific sequence of operations it must perform. The user of a computer can control the process by means of a program. A program is a set of instructions that specify the operations,

operands, and the sequence by which processing has to occur. The dataprocessing task may be altered by specifying a new program with different instructions or specifying the same instructions with different data.

A computer instruction is a binary code that specifies a sequence of microoperations for the computer. Instruction codes together with data are stored in memory. The computer reads each instruction from memory and places it in a control register. The control then interprets the binary code of the instruction and proceeds to execute it by issuing a sequence of microoperations. Every computer has its own unique instruction set. The ability to store and execute instructions, the stored program concept, is the most important property of a general-purpose computer.

An instruction code is a group of bits that instruct the computer to perform a specific operation. It is usually divided into parts, each having its own particular interpretation. The most basic part of an instruction code is its operation part. The operation code of an instruction is a group of bits that define such operations as add, subtract, multiply, shift, and complement. The number of bits required for the operation code of an instruction depends on the total number of operations available in the computer. The operation code must consist of at least n bits for a given 2^n (or less) distinct operations. As an illustration, consider a computer with 64 distinct operations, one of them being an ADD operation. The operation code consists of six bits, with a bit configuration 110010 assigned to the ADD operation. When this operation code is decoded in the control unit, the computer issues control signals to read an operand from memory and add the operand to a processor register.

At this point we must recognize the relationship between a computer operation and a microoperation. An operation is part of an instruction stored in computer memory. It is a binary code that tells the computer to perform a specific operation. The control unit receives the instruction from memory and interprets the operation code bits. It then issues a sequence of control signals to initiate microoperations in internal computer registers. For every operation code, the control issues a sequence of microoperations needed for the hardware implementation of the specified operation. For this reason, an operation code is sometimes called a macrooperation because it specifies a set of micro-operations.

The operation part of an instruction code specifies the operation to be performed. This operation must be performed on some data stored in processor registers or in memory. An instruction code must therefore specify not only the operation but also the registers or the memory words where the operands are to be found, as well as the register or memory word where the result is to be stored. Memory words can be specified in instruction codes by their address. Processor registers can be specified by assigning to the instruction another binary code of k bits that specifies one of 2^k registers. There are many variations for arranging the binary code of instructions, and each computer has its own particular instruction code format. Instruction code formats

instruction code

operation code

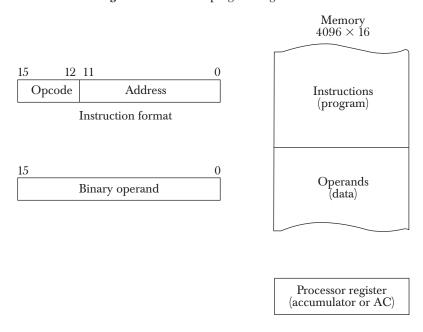
are conceived by computer designers who specify the architecture of the computer. In this chapter we choose a particular instruction code to explain the basic organization and design of digital computers.

Stored Program Organization

The simplest way to organize a computer is to have one processor register and an instruction code format with two parts. The first part specifies the operation to be performed and the second specifies an address. The memory address tells the control where to find an operand in memory. This operand is read from memory and used as the data to be operated on together with the data stored in the processor register.

Figure 5-1 depicts this type of organization. Instructions are stored in one section of memory and data in another. For a memory unit with 4096 words we need 12 bits to specify an address since $2^{12} = 4096$. If we store each instruction code in one 16-bit memory word, we have available four bits for the operation code (abbreviated opcode) to specify one out of 16 possible operations, and 12 bits to specify the address of an operand. The control reads a 16-bit instruction from the program portion of memory. It uses the 12-bit address part of the instruction to read a 16-bit operand from the data portion of memory. It then executes the operation specified by the operation code.

Figure 5-1 Stored program organization.



opcode

accumulator (AC)

Computers that have a single-processor register usually assign to it the name accumulator and label it AC. The operation is performed with the memory operand and the content of AC.

If an operation in an instruction code does not need an operand from memory, the rest of the bits in the instruction can be used for other purposes. For example, operations such as clear AC, complement AC, and increment AC operate on data stored in the AC register. They do not need an operand from memory. For these types of operations, the second part of the instruction code (bits 0 through 11) is not needed for specifying a memory address and can be used to specify other operations for the computer.

Indirect Address

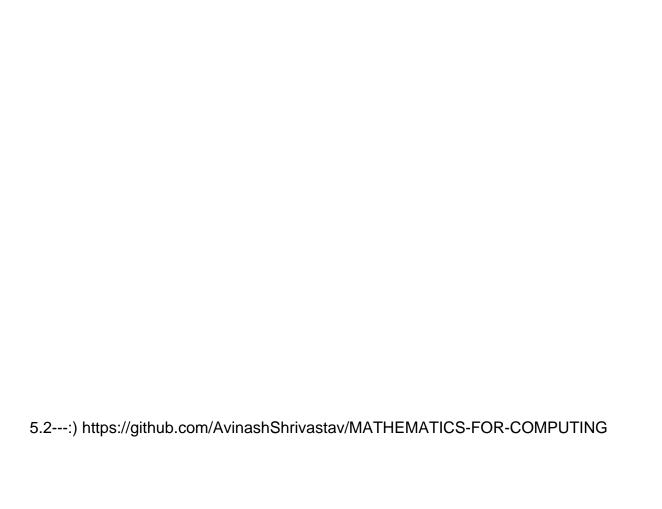
It is sometimes convenient to use the address bits of an instruction code not as an address but as the actual operand. When the second part of an instruction code specifies an operand, the instruction is said to have an immediate operand. When the second part specifies the address of an operand, the instruction is said to have a direct address. This is in contrast to a third possibility called indirect address, where the bits in the second part of the instruction designate an address of a memory word in which the address of the operand is found. One bit of the instruction code can be used to distinguish between a direct and an indirect address.

As an illustration of this configuration, consider the instruction code format shown in Fig. 5-2(a). It consists of a 3-bit operation code, a 12-bit address, and an indirect address mode bit designated by I. The mode bit is 0 for a direct address and 1 for an indirect address. A direct address instruction is shown in Fig. 5-2(b). It is placed in address 22 in memory. The *I* bit is 0, so the instruction is recognized as a direct address instruction. The opcode specifies an ADD instruction, and the address part is the binary equivalent of 457. The control finds the operand in memory at address 457 and adds it to the content of AC. The instruction in address 35 shown in Fig. 5-2(c) has a mode bit I = 1. Therefore, it is recognized as an indirect address instruction. The address part is the binary equivalent of 300. The control goes to address 300 to find the address of the operand. The address of the operand in this case is 1350. The operand found in address 1350 is then added to the content of AC. The indirect address instruction needs two references to memory to fetch an operand. The first reference is needed to read the address of the operand; the second is for the operand itself. We define the effective address to be the address of the operand in a computation-type instruction or the target address in a branch-type instruction. Thus the effective address in the instruction of Fig. 5-2(b) is 457 and in the instruction of Fig 5-2(c) is 1350.

The direct and indirect addressing modes are used in the computer presented in this chapter. The memory word that holds the address of the operand in an indirect address instruction is used as a pointer to an array of

immediate instruction

effective address



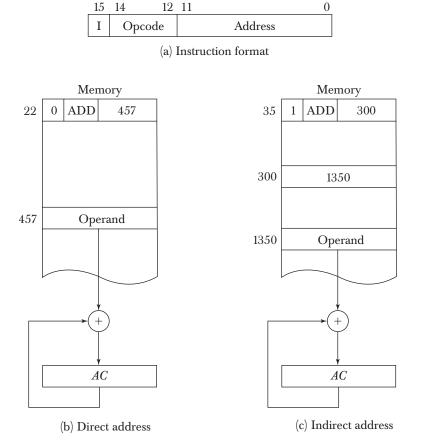


Figure 5-2 Demonstration of direct and indirect address.

data. The pointer could be placed in a processor register instead of memory as done in commercial computers.

5-2 Computer Registers

Computer instructions are normally stored in consecutive memory locations and are executed sequentially one at a time. The control reads an instruction from a specific address in memory and executes it. It then continues by reading the next instruction in sequence and executes it, and so on. This type of instruction sequencing needs a counter to calculate the address of the next instruction after execution of the current instruction is completed. It is also necessary to provide a register in the control unit for storing the instruction code after it is read

from memory. The computer needs processor registers for manipulating data and a register for holding a memory address. These requirements dictate the register configuration shown in Fig. 5-3. The registers are also listed in Table 5-1 together with a brief description of their function and the number of bits that they contain.

The memory unit has a capacity of 4096 words and each word contains 16 bits. Twelve bits of an instruction word are needed to specify the address of an operand. This leaves three bits for the operation, part of the instruction and a bit to specify a direct or indirect address. The data register (DR) holds the operand read from memory. The accumulator (AC) register is a general-purpose processing register. The instruction read from memory is placed in the instruction register (IR). The temporary register (TR) is used for holding temporary data during the processing.

Register symbol	Number of bits	Register name	Function
\overline{DR}	16	Data register	Holds memory operand
AR	12	Address register	Holds address for memory
AC	16	Accumulator	Processor register
IR	16	Instruction register	Holds instruction code
PC	12	Program counter	Holds address of instruction
TR	16	Temporary register	Holds temporary data
INPR	8	Input register	Holds input character
OUTR	8	Output register	Holds output character

TABLE 5-1 List of Registers for the Basic Computer

program counter (PC)

The memory address register (AR) has 12 bits since this is the width of a memory address. The program counter (PC) also has 12 bits and it holds the address of the next instruction to be read from memory after the current instruction is executed. The PC goes through a counting sequence and causes the computer to read sequential instructions previously stored in memory. Instruction words are read and executed in sequence unless a branch instruction is encountered. A branch instruction calls for a transfer to a nonconsecutive instruction in the program. The address part of a branch instruction is transferred to PC to become the address of the next instruction. To read an instruction, the content of PC is taken as the address for memory and a memory read cycle is initiated. PC is then incremented by one, so it holds the address of the next instruction in sequence.

Two registers are used for input and output. The input register (*INPR*) receives an 8-bit character from an input device. The output register (*OUTR*) holds an 8-bit character for an output device.

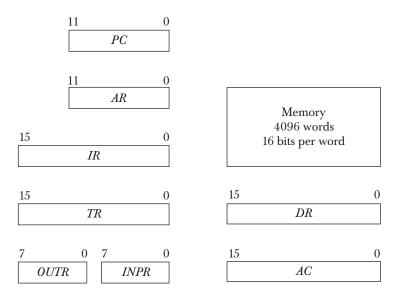


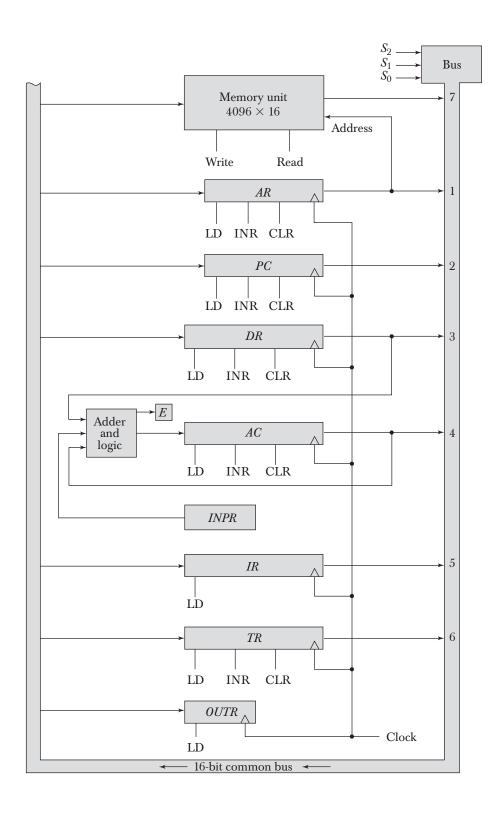
Figure 5-3 Basic computer registers and memory.

Common Bus System

The basic computer has eight registers, a memory unit, and a control unit (to be presented in Sec. 5-4). Paths must be provided to transfer information from one register to another and between memory and registers. The number of wires will be excessive if connections are made between the outputs of each register and the inputs of the other registers. A more efficient scheme for transferring information in a system with many registers is to use a common bus. We have shown in Sec. 4-3 how to construct a bus system using multiplexers or three-state buffer gates. The connection of the registers and memory of the basic computer to a common bus system is shown in Fig. 5-4.

The outputs of seven registers and memory are connected to the common bus. The specific output that is selected for the bus lines at any given time is determined from the binary value of the selection variables S_2 , S_1 , and S_0 . The number along each output shows the decimal equivalent of the required binary selection. For example, the number along the output of DR is 3. The 16-bit outputs of DR are placed on the bus lines when $S_2S_1S_0 = 011$ since this is the binary value of decimal 3. The lines from the common bus are connected to the inputs of each register and the data inputs of the memory. The particular register whose LD (load) input is enabled receives the data from the bus during the next clock pulse transition. The memory receives the contents of the bus when its write input is activated. The memory places its 16-bit output onto the bus when the read input is activated and $S_2S_1S_0 = 111$.

load (LD)



Four registers, DR, AC, IR, and TR, have 16 bits each. Two registers, AR and PC, have 12 bits each since they hold a memory address. When the contents of AR or PC are applied to the 16-bit common bus, the four most significant bits are set to 0's. When AR or PC receive information from the bus, only the 12 least significant bits are transferred into the register.

The input register *INPR* and the output register *OUTR* have 8 bits each and communicate with the eight least significant bits in the bus. *INPR* is connected to provide information to the bus but *OUTR* can only receive information from the bus. This is because *INPR* receives a character from an input device which is then transferred to *AC*. *OUTR* receives a character from *AC* and delivers it to an output device. There is no transfer from *OUTR* to any of the other registers.

The 16 lines of the common bus receive information from six registers and the memory unit. The bus lines are connected to the inputs of six registers and the memory. Five registers have three control inputs: LD (load), INR (increment), and CLR (clear). This type of register is equivalent to a binary counter with parallel load and synchronous clear similar to the one shown in Fig. 2-11. The increment operation is achieved by enabling the count input of the counter. Two registers have only a LD input. This type of register is shown in Fig. 2-7.

The input data and output data of the memory are connected to the common bus, but the memory address is connected to AR. Therefore, AR must always be used to specify a memory address. By using a single register for the address, we eliminate the need for an address bus that would have been needed otherwise. The content of any register can be specified for the memory data input during a write operation. Similarly, any register can receive the data from memory after a read operation except AC.

The 16 inputs of AC come from an adder and logic circuit. This circuit has three sets of inputs. One set of 16-bit inputs come from the outputs of AC. They are used to implement register microoperations such as complement AC and shift AC. Another set of 16-bit inputs come from the data regisler DR. The inputs from DR and AC are used for arithmetic and logic microoperations, such as add DR to AC or AND DR to AC. The result of an addition is transferred to AC and the end carry-out of the addition is transferred to flip-flop E (extended AC bit). A third set of 8-bit inputs come from the input register INPR. The operation of INPR and OUTR is explained in Sec. 5-7.

Note that the content of any register can be applied onto the bus and an operation can be performed in the adder and logic circuit during the same clock cycle. The clock transition at the end of the cycle transfers the content of the bus into the designated destination register and the output of the adder and logic circuit into *AC*. For example, the two microoperations

$$DR \leftarrow AC$$
 and $AC \leftarrow DR$

can be executed at the same time. This can be done by placing the content of AC on the bus (with $S_2S_1S_0 = 100$), enabling the LD (load) input of DR,

memory address

transferring the content of DR through the adder and logic circuit into AC, and enabling the LD (load) input of AC, all during the same clock cycle. The two transfers occur upon the arrival of the clock pulse transition at the end of the clock cycle.

5-3 Computer Instructions

Instruction format

The basic computer has three instruction code formats, as shown in Fig. 5-5. Each format has 16 bits. The operation code (opcode) part of the instruction contains three bits and the meaning of the remaining 13 bits depends on the operation code encountered. A memory-reference instruction uses 12 bits to specify an address and one bit to specify the addressing mode *I. I* is equal to 0 for direct address and to 1 for indirect address (see Fig. 5-2). The register-reference instructions are recognized by the operation code 111 with a 0 in the leftmost bit (bit 15) of the instruction. A register-reference instruction specifies an operation on or a test of the *AC* register. An operand from memory is not needed; therefore, the other 12 bits are used to specify the operation or test to be executed. Similarly, an input–output instruction does not need a reference to memory and is recognized by the operation code 111 with a 1 in the leftmost bit of the instruction. The remaining 12 bits are used to specify the type of input–output operation or test performed.

The type of instruction is recognized by the computer control from the four bits in positions 12 through 15 of the instruction. If the three opcode bits in positions 12 though 14 are not equal to 111, the instruction is a memory-reference type and the bit in position 15 is taken as the addressing mode *I*. If the 3-bit opcode is equal to 111, control then inspects the bit in position 15. If

15 14 12 11 (Opcode = 000 through 110)Opcode Address (a) Memory – reference instruction 15 12 11 0 0 Register operation (Opcode = 111, I = 0)(b) Register – reference instruction () 15 12 11 I/0 operation (Opcode = 111, I = 1)(c) Input – output instruction

Figure 5-5 Basic computer instruction formats.

this bit is 0, the instruction is a register-reference type. If the bit is 1, the instruction is an input–output type. Note that the bit in position 15 of the instruction code is designated by the symbol I but is not used as a mode bit when the operation code is equal to 111.

Only three bits of the instruction are used for the operation code. It may seem that the computer is restricted to a maximum of eight distinct operations. However, since register-reference and input-output instructions use the remaining 12 bits as part of the operation code, the total number of instructions can exceed eight. In fact, the total number of instructions chosen for the basic computer is equal to 25.

The instructions for the computer are listed in Table 5-2. The symbol designation is a three-letter word and represents an abbreviation intended for

TABLE 5-2 Basic Computer Instructions

Hexadecimal code			
Symbol	$\overline{I} = 0$	I=1	Description
AND	0xxx	8xxx	AND memory word to AC
ADD	lxxx	9xxx	Add memory word to AC
LDA	2xxx	Axxx	Load memory word to AC
STA	3xxx	Bxxx	Store content of AC in memory
BUN	4xxx	Cxxx	Branch unconditionally
BSA	5xxx	Dxxx	Branch and save return address
ISZ	6xxx	Exxx	Increment and skip if zero
CLA	780	00	Clear AC
CLE	740	00	Clear E
CMA	720	00	Complement AC
CME	710	0	Complement E
CIR	708	60	Circulate right AC and E
CIL	704	0	Circulate left AC and E
INC	702	0.0	Increment AC
SPA	701	0	Skip next instruction if AC positive
SNA	700	8	Skip next instruction if AC negative
SZA	700	4	Skip next instruction if AC zero
SZE	700	2	Skip next instruction if E is 0
HLT	700)1	Halt computer
INP	F80	00	Input character to AC
OUT	F40	00	Output character from AC
SKI	F20	00	Skip on input flag
SKO	F10	00	Skip on output flag
ION	F08	80	Interrupt on
IOF	F04	0.	Interrupt off

hexadecimal code

programmers and users. The hexadecimal code is equal to the equivalent hexadecimal number of the binary code used for the instruction. By using the hexadecimal equivalent we reduced the 16 bits of an instruction code to four digits with each hexadecimal digit being equivalent to four bits. A memory-reference instruction has an address part of 12 bits. The address part is denoted by three x's and stand for the three hexadecimal digits corresponding to the 12-bit address. The last bit of the instruction is designated by the symbol I. When I=0, the last four bits of an instruction have a hexadecimal digit equivalent from 0 to 6 since the last bit is 0. When I=1, the hexadecimal digit equivalent of the last four bits of the instruction ranges from 8 to E since the last bit is 1.

Register-reference instructions use 16 bits to specify an operation. The leftmost four bits are always 0111, which is equivalent to hexadecimal 7. The other three hexadecimal digits give the binar) equivalent of the remaining 12 bits. The input–output instructions also use all 16 bits to specify an operation. The last four bits are always 1111, equivalent to hexadecimal F.

Instruction Set Completeness

Before investigating the operations performed by the instructions, let us discuss the type of instructions that must be included in a computer. A computer should have a set of instructions so that the user can construct machine language programs to evaluate any function that is known to be computable. The set of instructions are said to be complete if the computer includes a sufficient number of instructions in each of the following categories:

- 1. Arithmetic, logical, and shift instructions
- 2. Instructions for moving information to and from memory and processor registers
- **3.** Program control instructions together with instructions that check status conditions
- 4. Input and output instructions

Arithmetic, logical, and shift instructions provide computational capabilities for processing the type of data that the user may wish to employ. The bulk of the binary information in a digital computer is stored in memory, but all computations are done in processor registers. Therefore, the user must have the capability of moving information between these two units. Decision-making capabilities are an important aspect of digital computers. For example, two numbers can be compared, and if the first is greater than the second, it may be necessary to proceed differently than if the second is greater than the first. Program control instructions such as branch instructions are used to change the sequence in which the program is executed. Input and output instructions are needed for communication between the computer and the



user. Programs and data must be transferred into memory and results of computations must be transferred back to the user.

The instructions listed in Table 5-2 constitute a minimum set that provides all the capabilities mentioned above. There is one arithmetic instruction, ADD, and two related instructions, complement AC(CMA) and increment AC(INC). With these three instructions we can add and subtract binary numbers when negative numbers are in signed-2's complement representation. The circulate instructions, CIR and CIL, can be used for arithmetic shifts as well as any other type of shifts desired. Multiplication and division can be performed using addition, subtraction, and shifting. There are three logic operations: AND, complement AC(CMA), and clear AC(CLA). The AND and complement provide a NAND operation. It can be shown that with the NAND operation it is possible to implement all the other logic operations with two variables (listed in Table 4-6). Moving information from memory to AC is accomplished with the load AC(LDA) instruction. Storing information from AC into memory is done with the store AC(STA) instruction. The branch instructions BUN, BSA, and ISZ, together with the four skip instructions, provide capabilities for program control and checking of status conditions. The input (INP) and output (OUT) instructions cause information to be transferred between the computer and external devices.

Although the set of instructions for the basic computer is complete, it is not efficient because frequently used operations are not performed rapidly. An efficient set of instructions will include such instructions as subtract, multiply, OR, and exclusive-OR. These operations must be programmed in the basic computer. The programs are presented in Chap. 6 together with other programming examples for the basic computer. By using a limited number of instructions it is possible to show the detailed logic design of the computer. A more complete set of instructions would have made the design too complex. In this way we can demonstrate the basic principles of computer organization and design without going into excessive complex details. In Chap. 8 we present a complete list of computer instructions that are included in most commercial computers.

The function of each instruction listed in Table 5-2 and the microoperations needed for their execution are presented in Secs. 5-5 through 5-7 We delay this discussion because we must first consider the control unit and understand its internal organization.

5-4 Timing and Control

clock pulses

The timing for all registers in the basic computer is controlled by a master clock generator. The clock pulses are applied to all flip-flops and registers in the system, including the flip-flops and registers in the control unit. The clock pulses do not change the state of a register unless the register is enabled by a

processor until the memory word is available. To facilitate the presentation, we will assume that a wait period is not necessary in the basic computer.

To fully comprehend the operation of the computer, it is crucial that one understands the timing relationship between the clock transition and the timing signals. For example, the register transfer statement

$$T_0$$
: $AR \leftarrow PC$

specifies a transfer of the content of PC into AR if timing signal T_0 is active. T_0 is active during an entire clock cycle interval. During this time the content of PC is placed onto the bus (with $S_2S_1S_0=010$) and the LD (load) input of AR is enabled. The actual transfer does not occur until the end of the clock cycle when the clock goes through a positive transition. This same positive clock transition increments the sequence counter SC from 0000 to 0001. The next clock cycle has T_1 active and T_0 inactive.

5-5 Instruction Cycle

A program residing in the memory unit of the computer consists of a sequence of instructions. The program is executed in the computer by going through a cycle for each instruction. Each instruction cycle in turn is subdivided into a sequence of subcycles or phases. In the basic computer each instruction cycle consists of the following phases:

- 1. Fetch an instruction from memory.
- **2.** Decode the instruction.
- **3.** Read the effective address from memory if the instruction has an indirect address.
- **4.** Execute the instruction.

Upon the completion of step 4, the control goes back to step 1 to fetch, decode, and execute the next instruction. This process continues indefinitely unless a HALT instruction is encountered.

Fetch and Decode

Initially, the program counter PC is loaded with the address of the first instruction in the program. The sequence counter SC is cleared to 0, providing a decoded timing signal T_0 . After each clock pulse, SC is incremented by one, so that the timing signals go through a sequence T_0 , T_1 , T_2 , and so on. The microoperations for the fetch and decode phases can be specified by the following register transfer statements.

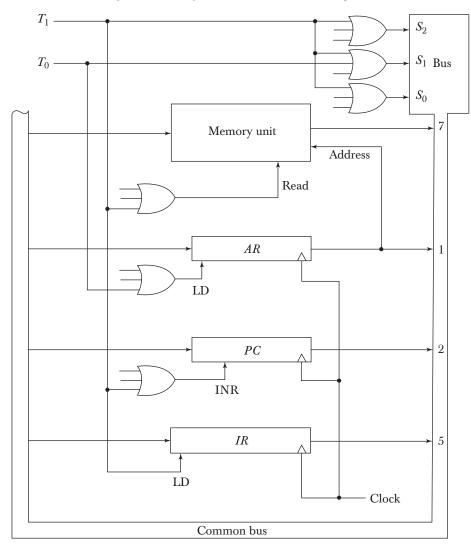
 T_0 : $AR \leftarrow PC$

 T_1 : $IR \leftarrow M[AR], PC \leftarrow PC + 1$

 T_2 : $D_0, \ldots, D_7 \leftarrow \text{Decode } IR(12-14), AR \leftarrow IR(0-11), I \leftarrow IR(15)$

Since only AR is connected to the address inputs of memory, it is necessary to transfer the address from PC to AR during the clock transition associated with timing signal T_0 . The instruction read from memory is then placed in the instruction register IR with the clock transition associated with timing

Figure 5-8 Register transfers for the fetch phase.



signal T_1 . At the same time, PC is incremented by one to prepare it for the address of the next instruction in the program. At rime T_2 , the operation code in IR is decoded, the indirect bit is transferred to flip-flop I, and the address part of the instruction is transferred to AR. Note that SC is incremented after each clock pulse to produce the sequence T_0 , T_1 , and T_2 .

Figure 5-8 shows how the first two register transfer statements are implemented in the bus system. To provide the data path for the transfer of PC to AR we must apply timing signal T_0 to achieve the following connection:

- **1.** Place the content of PC onto the bus by making the bus selection inputs $S_2S_1S_0$ equal to 010.
- 2. Transfer the content of the bus to AR by enabling the LD input of AR.

The next clock transition initiates the transfer from PC to AR since $T_0 = 1$. In order to implement the second statement

$$T_1$$
: $IR \leftarrow M[AR]$, $PC \leftarrow PC + 1$

it is necessary to use timing signal T_1 to provide the following connections in the bus system.

- **1.** Enable the read input of memory.
- **2.** Place the content of memory onto the bus by making $S_2S_1S_0 = 111$.
- 3. Transfer the content of the bus to IR by enabling the LD input of IR.
- 4. Increment *PC* by enabling the INR input of *PC*.

The next clock transition initiates the read and increment operations since $T_1 = 1$.

Figure 5-8 duplicates a portion of the bus system and shows how T_0 and T_1 are connected to the control inputs of the registers, the memory, and the bus selection inputs. Multiple input OR gates are included in the diagram because there are other control functions that will initiate similar operations.

Determine the Type of Instruction

The timing signal that is active after the decoding is T_3 . During time T_3 , the control unit determines the type of instruction that was just read from memory. The flowchart of Fig. 5-9 presents an initial configuration for the instruction cycle and shows how the control determines the instruction type after the decoding. The three possible instruction types available in the basic computer are specified in Fig. 5-5.

Decoder output D_7 is equal to 1 if the operation code is equal to binary 111. From Fig. 5-5 we determine that if $D_7 = 1$, the instruction must be a

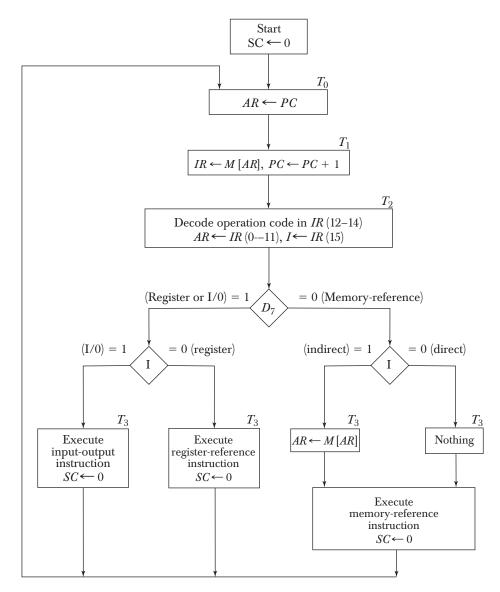


Figure 5-9 Flowchart for instruction cycle (initial configuration).

register-reference or input–output type. If $D_7 = 0$, the operation code must be one of the other seven values 000 through 110, specifying a memory-reference instruction. Control then inspects the value of the first bit of the instruction, which is now available in flip-flop I. If $D_7 = 0$ and I = 1, we have a memory-reference instruction with an indirect address. It is then necessary to read the

indirect address

effective address from memory. The microoperation for the indirect address condition can be symbolized by the register transfer statement

$$AR \leftarrow M[AR]$$

Initially, AR holds the address part of the instruction. This address is used during the memory read operation. The word at the address given by AR is read from memory and placed on the common bus. The LD input of AR is then enabled to receive the indirect address that resided in the 12 least significant bits of the memory word.

The three instruction types are subdivided into four separate paths. The selected operation is activated with the clock transition associated with timing signal T_3 . This can be symbolized as follows:

 $D_7'IT_3$: $AR \leftarrow M[AR]$

 $D_7'IT_3$: Nothing

 $D_7 I'T_3$: Execute a register-reference instruction

 $D_7 IT_3$: Execute an input-output instruction

When a memory-reference instruction with I=0 is encountered, it is not necessary to do anything since the effective address is already in AR. However, the sequence counter SC must be incremented when $D_7'T_3=1$, so that the execution of the memory-reference instruction can be continued with timing variable T_4 . A register-reference or input-output instruction can be executed with the clock associated with timing signal T_3 . After the instruction is executed, SC is cleared to 0 and control returns to the fetch phase with $T_0=1$.

Note that the sequence counter SC is either incremented or cleared to 0 with every positive clock transition. We will adopt the convention that if SC is incremented, we will not write the statement $SC \leftarrow SC + 1$, but it will be implied that the control goes to the next timing signal in sequence. When SC is to be cleared, we will include the statement $SC \leftarrow 0$.

The register transfers needed for the execution of the register-reference instructions are presented in this section. The memory-reference instructions are explained in the next section. The input-output instructions are included in Sec. 5-7.

Register-Reference Instructions

Register-reference instructions are recognized by the control when $D_7 = 1$ and I = 0. These instructions use bits 0 through 11 of the instruction code to specify one of 12 instructions. These 12 bits are available in IR (0–11). They were also transferred to AR during time T_2 .

The control functions and microoperations for the register-reference instructions are listed in Table 5-3. These instructions are executed with the

5-6 Memory-Reference Instructions

In order to specify the microoperations needed for the execution of each instruction, it is necessary that the function that they are intended to perform be defined precisely. Looking back to Table 5-2, where the instructions are listed, we find that some instructions have an ambiguous description. This is because the explanation of an instruction in words is usually lengthy, and not enough space is available in the table for such a lengthy explanation. We will now show that the function of the memory-reference instructions can be defined precisely by means of register transfer notation.

effective address

Table 5-4 lists the seven memory-reference instructions. The decoded output D_i for i=0,1,2,3,4,5, and 6 from the operation decoder that belongs to each instruction is included in the table. The effective address of the instruction is in the address register AR and was placed there during timing signal T_2 when I=0, or during timing signal T_3 when I=1. The execution of the memory-reference instructions starts with timing signal T_4 . The symbolic description of each instruction is specified in the table in terms of register transfer notation. The actual execution of the instruction in the bus system will require a sequence of microoperations. This is because data stored in memory cannot be processed directly. The data must be read from memory to a register where they can be operated on with logic circuits. We now explain the operation of each instruction and list the control functions and microoperations needed for their execution. A flowchart that summarizes all the microoperations is presented at the end of this section.

TABLE 5-4 Memory-Reference Instructions

Symbol	Operation decoder	Symbolic description
AND	D_0	$AC \leftarrow AC \land M[AR]$
ADD	D_1°	$AC \leftarrow AC + M[AR], E \leftarrow C_{\text{out}}$
LDA	D_2	$AC \leftarrow M[AR]$
STA	D_3	$M[AR] \leftarrow AC$
BUN	D_4	$PC \leftarrow AR$
BSA	D_5	$M[AR] \leftarrow PC, PC \leftarrow AR + 1$
ISZ	D_6°	$M[AR] \leftarrow M[AR] + 1,$
		If $M[AR] + 1 = 0$ then $PC \leftarrow PC + 1$

AND to AC

This is an instruction that performs the AND logic operation on pairs of bits in AC and the memory word specified by the effective address. The result of

the operation is transferred to AC. The microoperations that execute this instruction are:

$$D_0T_4$$
: $DR \leftarrow M[AR]$
 D_0T_5 : $AC \leftarrow AC \land DR$, $SC \leftarrow 0$

The control function for this instruction uses the operation decoder D_0 since this output of the decoder is active when the instruction has an AND operation whose binary code value is 000. Two timing signals are needed to execute the instruction. The clock transition associated with timing signal T_4 transfers the operand from memory into DR. The clock transition associated with the next timing signal T_5 transfers to AC the result of the AND logic operation between the contents of DR and AC. The same clock transition clears SC to 0, transferring control to timing signal T_0 to start a new instruction cycle.

ADD to AC

This instruction adds the content of the memory word specified by the effective address to the value of AC. The sum is transferred into AC and the output carry C_{out} is transferred to the E (extended accumulator) flip-flop. The microoperations needed to execute this instruction are

$$D_1T_4$$
: $DR \leftarrow M[AR]$
 D_1T_5 : $AC \leftarrow AC + DR$, $E \leftarrow C_{out}$, $SC \leftarrow 0$

The same two timing signals, T_4 and T_5 , are used again but with operation decoder D_1 instead of D_0 , which was used for the AND instruction. After the instruction is fetched from memory and decoded, only one output of the operation decoder will be active, and that output determines the sequence of microoperations that the control follows during the execution of a memory-reference instruction.

LDA: Load to AC

This instruction transfers the memory word specified by the effective address to AC. The microoperations needed to execute this instruction are

$$D_2T_4$$
: $DR \leftarrow M[AR]$
 D_2T_5 : $AC \leftarrow DR$, $SC \leftarrow 0$

Looking back at the bus system shown in Fig. 5-4 we note that there is no direct path from the bus into AC. The adder and logic circuit receive information

from DR which can be transferred into AC. Therefore, it is necessary to read the memory word into DR first and then transfer the content of DR into AC. The reason for not connecting the bus to the inputs of AC is the delay encountered in the adder and logic circuit. It is assumed that the time it takes to read from memory and transfer the word through the bus as well as the adder and logic circuit is more than the time of one clock cycle. By not connecting the bus to the inputs of AC we can maintain one clock cycle per microoperation.

STA: Store AC

This instruction stores the content of AC into the memory word specified by the effective address. Since the output of AC is applied to the bus and the data input of memory is connected to the bus, we can execute this instruction with one microoperation:

$$D_3T_4$$
: $M[AR] \leftarrow AC$, $SC \leftarrow 0$

BUN: Branch Unconditionally

This instruction transfers the program to the instruction specified by the effective address. Remember that PC holds the address of the instruction to be read from memory in the next instruction cycle. PC is incremented at time T_1 to prepare it for the address of the next instruction in the program sequence. The BUN instruction allows the programmer to specify an instruction out of sequence and we say that the program branches (or jumps) unconditionally. The instruction is executed with one microoperation:

$$D_A T_A$$
: $PC \leftarrow AR$, $SC \leftarrow 0$

The effective address from AR is transferred through the common bus to PC. Resetting SC to 0 transfers control to T_0 . The next instruction, is then fetched and executed from the memory address given by the new value in PC.

BSA: Branch and Save Return Address

This instruction is useful for branching to a portion of the program called a subroutine or procedure. When executed, the BSA instruction stores the address of the next instruction in sequence (which is available in PC) into a memory location specified by the effective address. The effective address plus one is then transferred to PC to serve as the address of the first instruction in the subroutine. This operation was specified in Table 5-4 with the following register transfer:

$$M[AR] \leftarrow PC, \quad PC \leftarrow AR + 1$$

A numerical example that demonstrates how this instruction is used with a subroutine is shown in Fig. 5-10. The BSA instruction is assumed to be in memory at address 20. The *I* bit is 0 and the address part of the instruction has the binary equivalent of 135. After the fetch and decode phases, *PC* contains 21, which is the address of the next instruction in the program (referred to as the *return address*). *AR* holds the effective address 135. This is shown in part (a) of the figure. The BSA instruction performs the following numerical operation:

return address

$$M[135] \leftarrow 21, \qquad PC \leftarrow 135 + 1 = 136$$

The result of this operation is shown in part (b) of the figure. The return address 21 is stored in memory location 135 and control continues with the subroutine program starting from address 136. The return to the original program (at address 21) is accomplished by means of an indirect BUN instruction placed at the end of the subroutine. When this instruction is executed, control goes to the indirect phase to read the effective address at location 135, where it finds the previously saved address 21. When the BUN instruction is executed, the effective address 21 is transferred to PC. The next instruction cycle finds PC with the value 21, so control continues to execute the instruction at the return address.

The BSA instruction performs the function usually referred to as a subroutine call. The indirect BUN instruction at the end of the subroutine performs the function referred to as a subroutine return. In most commercial computers, the return address associated with a subroutine is stored in either a processor register or in a portion of memory called a stack. This is discussed in more detail in Sec. 8-7.

Memory Memory 20 **BSA** 135 20 **BSA** 135 PC=21Next instruction 21 Next instruction AR = 135135 21 136 Subroutine PC = 136Subroutine BUN **BUN** 1 135 1 135

Figure 5-10 Example of BSA instruction execution.

(a) Memory, PC, and AR at time T_4

(b) Memory and PC after execution

subroutine call

It is not possible to perform the operation of the BSA instruction in one clock cycle when we use the bus system of the basic computer. To use the memory and the bus properly, the BSA instruction must be executed with a sequence of two microoperations:

$$D_5T_4$$
: $M[AR] \leftarrow PC$, $AR \leftarrow AR + 1$
 D_5T_5 : $PC \leftarrow AR$, $SC \leftarrow 0$

Timing signal T_4 initiates a memory write operation, places the content of PC onto the bus, and enables the INR input of AR. The memory write operation is completed and AR is incremented by the time the next clock transition occurs. The bus is used at T_5 to transfer the content of AR to PC.

ISZ: Increment and Skip if Zero

This instruction increments the word specified by the effective address, and if the incremented value is equal to 0, PC is incremented by 1. The programmer usually stores a negative number (in 2's complement) in the memory word. As this negative number is repeatedly incremented by one, it eventually reaches the value of zero. At that time PC is incremented by one in order to skip the next instruction in the program.

Since it is not possible to increment a word inside the memory, it is necessary to read the word into DR, increment DR, and store the word back into memory. This is done with the following sequence of microoperations:

$$D_6T_4$$
: $DR \leftarrow M[AR]$
 D_6T_5 : $DR \leftarrow DR + 1$
 D_6T_6 : $M[AR] \leftarrow DR$, if $(DR = 0)$ then $(PC \leftarrow PC + 1)$, $SC \leftarrow 0$

Control Flowchart

A flowchart showing all microoperations for the execution of the seven memory-reference instructions is shown in Fig. 5-11. The control functions are indicated on top of each box. The microoperations that are performed during time T_4 , T_5 , or T_6 depend on the operation code value. This is indicated in the flowchart by six different paths, one of which the control takes after the instruction is decoded. The sequence counter SC is cleared to 0 with the last timing signal in each case. This causes a transfer of control to timing signal T_0 to start the next instruction cycle.

Note that we need only seven timing signals to execute the longest instruction (ISZ). The computer can be designed with a 3-bit sequence counter. The reason for using a 4-bit counter for SC is to provide additional timing signals for other instructions that are presented in the problems section.



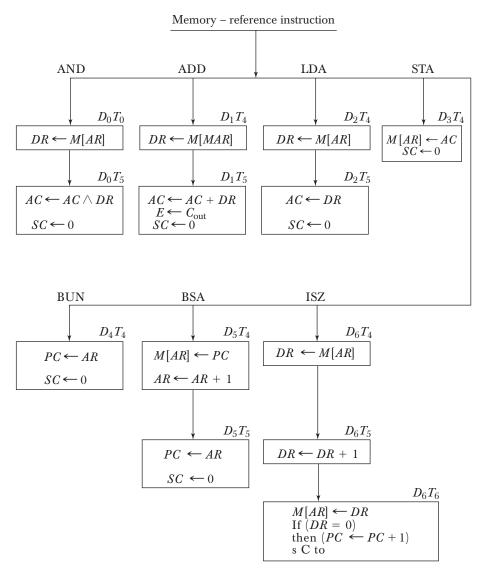


Figure 5-11 Flowchart for memory-reference instructions.

5-7 Input-Output and Interrupt

A computer can serve no useful purpose unless it communicates with the external environment. Instructions and data stored in memory must come from some input device. Computational results must be transmitted to the user through some output device. Commercial computers include many types

of input and output devices. To demonstrate the most basic requirements for input and output communication, we will use as an illustration a terminal unit with a keyboard and printer. Input–output organization is discussed further in Chap. 11.

Input-Output Configuration

The terminal sends and receives serial information. Each quantity of information has eight bits of an alphanumeric code. The serial information from the keyboard is shifted into the input register *INPR*. The serial information for the printer is stored in the output register *OUTR*. These two registers communicate with a communication interface serially and with the *AC* in parallel. The input–output configuration is shown in Fig. 5-12. The transmitter interface receives serial information from the keyboard and transmits it to *INPR*. The receiver interface receives information from *OUTR* and sends it to the printer serially. The operation of the serial communication interface is explained in Sec. 11-3.

input register

The input register INPR consists of eight bits and holds an alphanumeric input information. The 1-bit input flag FGI is a control flip-flop. The flag bit is

Input-output Computer Serial terminal communication registers and interface flip-flops FGOReceiver OUTRPrinter interface ACTransmitter **INPR** Keyboard interface FGI

Figure 5-12 Input-output configuration.

set to 1 when new information is available in the input device and is cleared to 0 when the information is accepted by the computer. The flag is needed to synchronize the timing rate difference between the input device and the computer. The process of information transfer is as follows. Initially, the input flag FGI is cleared to 0. When a key is struck in the keyboard, an 8-bit alphanumeric code is shifted into INPR and the input flag FGI is set to 1. As long as the flag is set, the information in INPR cannot be changed by striking another key. The computer checks the flag bit; if it is 1, the information from INPR is transferred in parallel into AC and FGI is cleared to 0. Once the flag is cleared, new information can be shifted into INPR by striking another key.

output register

The output register OUTR works similarly but the direction of information flow is reversed. Initially, the output flag FGO is set to 1. The computer checks the flag bit; if it is 1, the information from AC is transferred in parallel to OUTR and FGO is cleared to 0. The output device accepts the coded information, prints the corresponding character, and when the operation is completed, it sets FGO to 1. The computer does not load a new character into OUTR when FGO is 0 because this condition indicates that the output device is in the process of printing the character.

Input-Output Instructions

Input and output instructions are needed for transferring information to and from AC register, for checking the flag bits, and for controlling the interrupt facility. Input–output instructions have an operation code 1111 and are recognized by the control when $D_7 = 1$ and I = 1. The remaining bits of the instruction specify the particular operation. The control functions and microoperations for the input–output instructions are listed in Table 5-5. These instructions are executed with the clock transition associated with timing signal T_3 . Each control function needs a Boolean relation D_7IT_3 , which we designate for convenience by the symbol p. The control function is distinguished by one of the bits in IR(6-11). By assigning the symbol B_i to bit i of IR, all control functions can

TABLE 5-5 Input-Output Instructions

$D_7IT_3 = p$ (common to all input–output instructions) $IR(i) = B_i$ [bit in $IR(6-11)$ that specifies the instruction]					
	þ:	$SC \leftarrow 0$	Clear SC		
INP	$pB_{11}^{'}$:	$AC(0-7) \leftarrow INPR, FGI \leftarrow 0$	Input character		
OUT	pB_{10} :	$OUTR \leftarrow AC(0-7), FGO \leftarrow 0$	Output character		
SKI	pB_9 :	If $(FGI = 1)$ then $(PC \leftarrow PC + 1)$	Skip on input flag		
SKO	pB_8 :	If $(FGO = 1)$ then $(PC \leftarrow PC + 1)$	Skip on output flag		
ION	pB_7 :	$IEN \leftarrow 1$	Interrupt enable on		
IOF	pB_6 :	$IEN \leftarrow 0$	Interrupt enable off		

be denoted by pB_i for i=6 though 11. The sequence counter SC is cleared to 0 when $p=D_7IT_3=1$.

The INP instruction transfers the input information from INPR into the eight low-order bits of AC and also clears the input flag to 0. The OUT instruction transfers the eight least significant bits of AC into the output register OUTR and clears the output flag to 0. The next two instructions in Table 5-5 check the status of the flags and cause a skip of the next instruction if the flag is 1. The instruction that is skipped will normally be a branch instruction to return and check the flag again. The branch instruction is not skipped if the flag is 0. If the flag is 1, the branch instruction is skipped and an input or output instruction is executed. (Examples of input and output programs are given in Sec. 6-8.) The last two instructions set and clear an interrupt enable flip-flop IEN. The purpose of IEN is explained in conjunction with the interrupt operation.

Program Interrupt

The process of communication just described is referred to as programmed control transfer. The computer keeps checking the flag bit, and when it finds it set, it initiates an information transfer. The difference of information flow rate between the computer and that of the input–output device makes this type of transfer inefficient. To see why this is inefficient, consider a computer that can go through an instruction cycle in 1 μ s. Assume that the input–output device can transfer information at a maximum rate of 10 characters per second. This is equivalent to one character every 100,000 μ s. Two instructions are executed when the computer checks the flag bit and decides not to transfer the information. This means that at the maximum rate, the computer will check the flag 50,000 times between each transfer. The computer is wasting time while checking the flag instead of doing some other useful processing task.

An alternative to the programmed controlled procedure is to let the external device inform the computer when it is ready for the transfer. In the meantime the computer can be busy with other tasks. This type of transfer uses the interrupt facility. While the computer is running a program, it does not check the flags. However, when a flag is set, the computer is momentarily interrupted from proceeding with the current program and is informed of the fact that a flag has been set. The computer deviates momentarily from what it is doing to take eare of the input or output transfer. It then returns to the current program to continue what it was doing before the interrupt.

The interrupt enable flip-flop *IEN* can be set and cleared with two instructions. When *IEN* is cleared to 0 (with the IOF instruction), the flags cannot interrupt the computer. When *IEN* is set to 1 (with the ION instruction), the computer can be interrupted. These two instructions provide the programmer with the capability of making a decision as to whether or not to use the interrupt facility.

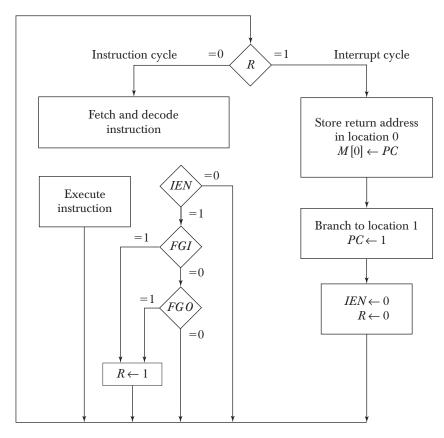


Figure 5-13 Flowchart for interrupt cycle.

The way that the interrupt is handled by the computer can be explained by means of the flowchart of Fig. 5-13. An interrupt flip-flop R is included in the computer. When R=0, the computer goes through an instruction cycle. During the execute phase of the instruction cycle IEN is checked by the control. If it is 0, it indicates that the programmer does not want to use the interrupt, so control continues with the next instruction cycle. If IEN is 1, control checks the flag bits. If both flags are 0, it indicates that neither the input nor the output registers are ready for transfer of information. In this case, control continues with the next instruction cycle. If either flag is set to 1 while IEN=1, flip-flop R is set to 1. At the end of the execute phase, control checks the value of R, and if it is equal to 1, it goes to an interrupt cycle instead of an instruction cycle.

interrupt cycle

The interrupt cycle is a hardware implementation of a branch and save return address operation. The return address available in PC is stored in a specific location where it can be found later when the program returns to the instruction at which it was interrupted. This location may be a processor

register, a memory stack, or a specific memory location. Here we choose the memory location at address 0 as the place for storing the return address. Control then inserts address 1 into *PC* and clears *IEN* and *R* so that no more interruptions can occur until the interrupt request from the flag has been serviced.

An example that shows what happens during the interrupt cycle is shown in Fig. 5-14. Suppose that an interrupt occurs and R is set to 1 while the control is executing the instruction at address 255. At this time, the return address 256 is in PC. The programmer has previously placed an input–output service program in memory starting from address 1120 and a BUN 1120 instruction at address 1. This is shown in Fig. 5-14(a).

When control reaches timing signal T_0 and finds that R=1, it proceeds with the interrupt cycle. The content of PC (256) is stored in memory location 0, PC is set to 1, and R is cleared to 0. At the beginning of the next instruction cycle, the instruction that is read from memory is in address 1 since this is the content of PC. The branch instruction at address 1 causes the program to transfer to the input–output service program at address 1120. This program checks the flags, determines which flag is set, and then transfers the required input or output information. Once this is done, the instruction ION is executed to set IEN to 1 (to enable further interrupts), and the program returns to the location where it was interrupted. This is shown in Fig. 5-14(b).

The instruction that returns the computer to the original place in the main program is a branch indirect instruction with an address part of 0. This instruction is placed at the end of the I/O service program. After this instruction

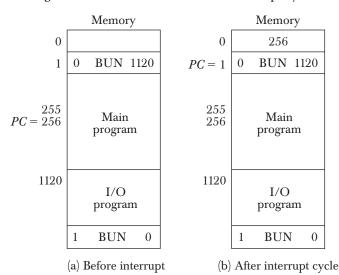


Figure 5-14 Demonstration of the interrupt cycle.



characteristics of the computer system rather than its operational and structural interconnections. One type of parallel processing that does not fit Flynn's classification is pipelining. The only two categories used from this classification are SIMD array processors discussed in Sec. 9-7, and MIMD multiprocessors presented in Chap. 13.

Parallel processing computers are required to meet the demands of large scale computations in many scientific, engineering, military, medical, artificial intelligence, and basic research areas. The following are some representative applications of parallel processing computers: Numerical weather forecasting, computational aerodynamics, finite-element analysis, remote-sensing applications, genetic engineering, computer-asseted tomography, and weapon research and defence.

In this chapter we consider parallel processing under the following main topics:

- 1. Pipeline processing
- 2. Vector processing
- **3.** Array processors

Pipeline processing is an implementation technique where arithmetic suboperations or the phases of a computer instruction cycle overlap in execution. Vector processing deals with computations involving large vectors and matrices. Array processors perform computations on large arrays of data.

9-2 Pipelining

Pipelining is a technique of decomposing a sequential process into suboperations, with each subprocess being executed in a special dedicated segment that operates concurrently with all other segments. A pipeline can be visualized as a collection of processing segments through which binary information flows. Each segment performs partial processing dictated by the way the task is partitioned. The result obtained from the computation in each segment is transferred to the next segment in the pipeline. The final result is obtained after the data have passed through all segments. The name "pipeline" implies a flow of information analogous to an industrial assembly line. It is characteristic of pipelines that several computations can be in progress in distinct segments at the same time. The overlapping of computation is made possible by associating a register with each segment in the pipeline. The registers provide isolation between each segment so that each can operate on distinct data simultaneously.

Perhaps the simplest way of viewing the pipeline structure is to imagine that each segment consists of an input register followed by a combinational circuit. The register holds the data and the combinational circuit performs the suboperation in the particular segment. The output of the combinational circuit in a given segment is applied to the input register of the next segment. A clock is applied to all registers after enough time has elapsed to perform all

segment activity. In this way the information flows through the pipeline one step at a time.

an example

The pipeline organization will be demonstrated by means of a simple example. Suppose that we want to perform the combined multiply and add operations with a stream of numbers.

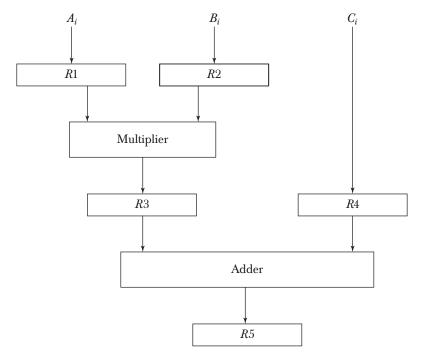
$$A_i * B_i + C_i$$
 for $i = 1, 2, 3, ..., 7$

Each suboperation is to be implemented in a segment within a pipeline. Each segment has one or two registers and a combinational circuit as shown in Fig. 9-2. *R*1 through *R*5 are registers that receive new data with every clock pulse. The multiplier and adder are combinational circuits. The suboperations performed in each segment of the pipeline are as follows:

$$R1 \leftarrow A_i, \quad R2 \leftarrow B_i$$
 Input A_i and B_i
 $R3 \leftarrow R1 * R2, \quad R4 \leftarrow C_i$ Multiply and input C_i
 $R5 \leftarrow R3 + R4$ Add C_i to product

The five registers are loaded with new data every clock pulse. The effect of each clock is shown in Table 9-1. The first clock pulse transfers A_1 and B_1 into

Figure 9-2 Example or pipeline processing.



Clock Pulse	Segm	ent 1	Segmen	nt 2	Segment 3
Number	R1	R2	<i>R</i> 3	R4	R5
1	A_1	B_1	_	_	_
2	A_2	B_{2}	$A_1 * B_1$	C_1	_
3	A_3	B_3	$A_2 * B_2$	C_2	$A_1 * B_1 + C_1$
4	A_4	B_4	$A_3 * B_3$	C_3	$A_2 * B_2 + C_2$
5	A_5	B_5	A_4*B_4	C_4	$A_3 * B_3 + C_3$
6	A_6	B_6	$A_5 * B_5$	C_5	$A_4 * B_4 + C_4$
7	A_7	B_7	$A_6 * B_6$	C_6	$A_5 * B_5 + C_5$
8	_	_	$A_7 * B_7$	C_7	$A_6 * B_6 + C_6$
9	_	_	_	_	$A_7 * B_7 + C_7$

TABLE 9-1 Content of Registers in Pipeline Example

R1 and R2. The second clock pulse transfers the product of R1 and R2 into R3 and C_1 into R4. The same clock pulse transfers A_2 and B_2 into R1 and R2. The third clock pulse operates on all three segments simultaneously. It places A_3 and B_3 into R1 and R2, transfers the product of R1 and R2 into R3, transfers C_2 into R4, and places the sum of R3 and R4 into R5. It takes three clock pulses to fill up the pipe and retrieve the first output from R5. From there on, each clock produces a new output and moves the data one step down the pipeline. This happens as long as new input data flow into the system. When no more input data are available, the clock must continue until the last output emerges out of the pipeline.

General Considerations

Any operation that can be decomposed into a sequence of suboperations of about the same complexity can be implemented by a pipeline processor. The technique is efficient for those applications that need to repeat the same task many times with different sets of data. The general structure of a four-segment pipeline is illustrated in Fig. 9-3. The operands pass through all four segments in a fixed sequence. Each segment consists of a combinational circuit S_i that performs a suboperation over the data stream flowing through the pipe. The segments are separated by registers R_i that hold the intermediate results between the stages. Information flows between adjacent stages under the control of a common clock applied to all the registers simultaneously. We define a *task* as the total operation performed going through all the segments in the pipeline.

The behavior of a pipeline can be illustrated with a *space-time* diagram. This is a diagram that shows the segment utilization as a function of time. The space-time diagram of a four-segment pipeline is demonstrated in Fig. 9-4. The horizontal axis displays the time in clock cycles and the vertical axis gives

task

space-time diagram

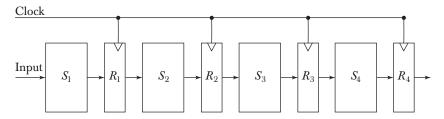


Figure 9-3 Four-segment pipeline.

the segment number. The diagram shows six tasks T_1 through T_6 executed in four segments. Initially, task T_1 is handled by segment 1. After the first clock, segment 2 is busy with T_1 , while segment 1 is busy with task T_2 . Continuing in this manner, the first task T_1 is completed after the fourth clock cycle. From then on, the pipe completes a task every clock cycle. No matter how many segments there are in the system, once the pipeline is full, it takes only one clock period to obtain an output.

Now consider the case where a k-segment pipeline with a clock cycle time t_p is used to execute n tasks. The first task T_1 requires a time equal to kt_p to complete its operation since there are k segments in the pipe. The remaining n-1 tasks emerge from the pipe at the rate of one task per clock cycle and they will be completed after a time equal to $(n-1)t_p$. Therefore, to complete n tasks using a k-segment pipeline requires k+(n-1) clock cycles. For example, the diagram of Fig. 9-4 shows four segments and six tasks. The time required to complete all the operations is 4+(6-1)=9 clock cycles, as indicated in the diagram.

Next consider a nonpipeline unit that performs the same operation and takes a time equal to t_n to complete each task. The total time required for n tasks is nt_n . The speedup of a pipeline processing over an equivalent nonpipeline processing is defined by the ratio

$$S = \frac{nt_n}{(k+n-1)t_p}$$

Space-time diagram for pipeline.

1 2 3 4 5 6 ➤ Clock cycles Segment: 1 T_1 T_2 T_3 T_4 T_5 T_6 2 T_1 T_2 T_3 T_4 T_5 T_6 3 T_3 T_1 T_2 T_4 T_5 T_6 4 T_1 T_2 T_3 T_4 T_5 T_6

Figure 9-4

speedup

As the number of tasks increases, n becomes much larger than k-1, and k+n-1 approaches the value of n. Under this condition, the speedup becomes

$$S = \frac{t_n}{t_p}$$

If we assume that the time it takes to process a task is the same in the pipeline and nonpipeline circuits, we will have $t_n = kt_p$. Including this assumption, the speedup reduces to

$$S = \frac{Kt_p}{t_b} = K$$

This shows that the theoretical maximum speedup that a pipeline can provide is k, where k is the number of segments in the pipeline.

To clarify the meaning of the speedup ratio, consider the following numerical example. Let the time it takes to process a suboperation in each segment be equal to $t_p = 20$ ns. Assume that the pipeline has k = 4 segments and executes n = 100 tasks in sequence. The pipeline system will take (k + n - 1) $t_p = (4 + 99) \times 20 = 2060$ ns to complete. Assuming that $t_n = kt_p = 4 \times 20 = 80$ ns, a nonpipeline system requires $nkt_p = 100 \times 80 = 8000$ ns to complete the 100 tasks. The speedup ratio is equal to 8000/2060 = 3.88. As the number of tasks increases, the speedup will approach 4, which is equal to the number of segments in the pipeline. If we assume that $t_n = 60$ ns, the speedup becomes 60/20 = 3.

To duplicate the theoretical speed advantage of a pipeline process by means of multiple functional units, it is necessary to construct k identical units that will be operating in parallel. The implication is that a k-segment pipeline processor can be expected to equal the performance of k copies of an equivalent nonpipeline circuit under equal operating conditions. This is illustrated in Fig. 9-5, where four identical circuits are connected in parallel. Each P circuit performs the same task of an equivalent pipeline circuit. Instead of operating with the input data in sequence as in a pipeline, the parallel circuits accept four input data items simultaneously and perform four tasks at the same rime. As far as the speed of operation is concerned, this is equivalent to a four segment pipeline. Note that the four-unit circuit of Fig. 9-5 constitutes a single-instruction multiple-data (SIMD) organization since the same instruction is used to operate on multiple data in parallel.

There are various reasons why the pipeline cannot operate at its maximum theoretical rate. Different segments may take different times to complete their suboperation. The clock cycle must be chosen to equal the time delay of the segment with the maximum propagation time. This causes all other



CHAPTER EIGHT

Central Processing Unit

IN THIS CHAPTER

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8-1 Introduction

The part of the computer that performs the bulk of data-processing operations is called the central processing unit and is referred to as the CPU. The CPU is made up of three major parts, as shown in Fig. 8-1. The register set stores intermediate data used during the execution of the instructions. The arithmetic logic unit (ALU) performs the required microoperations for executing the instructions. The control unit supervises the transfer of information among the registers and instructs the ALU as to which operation to perform.

The CPU performs a variety of functions dictated by the type of instructions that art Incorporated in the computer. Computer architecture is sometimes defined as the computer structure and behavior as seen by the programmer that uses machine language instructions. This includes the instruction formats, addressing modes, the instruction set, and the general organization of the CPU registers leading to two computer architectures as reduced instruction set computer (RISC) and complex instruction set computer (CISC). Based on memory usage for programs and data, two architectures, namely nonembedded and embedded are evolved. Nonembedded computer architectures are basically stored program computer (SPC) architectures in which programs and data reside in the same memory system. Embedded architectures are basically Harvard computer architectures in which programs and data

CPU

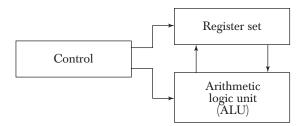


Figure 8-1 Major components of CPU.

reside in different memory systems leading to doubling the memory bandwidth. Example of nonembedded computers are all desktop systems such as personal computers. Example of embedded computers are microcontroller-based systems and digital signal processor-based (DSP) systems.

One boundary where the computer designer and the computer programmer see the same machine is the part of the CPU associated with the instruction set. From the designer's point of view, the computer instruction set provides the specifications for the design of the CPU. The design of a CPU is a task that in large part involves choosing the hardware for implementing the machine instructions. The user who programs the computer in machine or assembly language must be aware of the register set, the memory structure, the type of data supported by the instructions, and the function that each instruction performs.

Design examples of simple CPUs are carried out in Chaps. 5 and 7. This chapter describes the organization and architecture of the CPU with an emphasis on the user's view of the computer. We briefly describe how the registers communicate with the ALU through buses and explain the operation of the memory stack. We then present the type of instruction formats available, the addressing modes used to retrieve data from memory, and typical instructions commonly incorporated in computers. The last section presents the concept of reduced instruction set computer (RISC).

8-2 General Register Organization

In the programming examples of Chap. 6, we have shown that memory locations are needed for storing pointers, counters, return addresses, temporary results, and partial products during multiplication. Having to refer to memory locations for such applications is time consuming because memory access is the most time-consuming operation in a computer. It is more convenient and more efficient to store these intermediate values in processor registers. When a large number of registers are included in the CPU, it is most efficient to connect them through a common bus system. The registers communicate with each other not only for direct data transfers, but also while performing various microoperations. Hence it is necessary to provide a common unit that can perform all the arithmetic, logic, and shift microoperations in the processor.

bus system

A bus organization for seven CPU registers is shown in Fig. 8-2. The output of each register is connected to two multiplexers (MUX) to form the two buses A and B. The selection lines in each multiplexer select one register or the input data for the particular bus. The A and B buses form the inputs to a common arithmetic logic unit (ALU). The operation selected in the ALU determines the arithmetic or logic microoperation that is to be performed. The result of the microoperation is available for output data and also goes into the inputs of all the registers. The register that receives the information from the output bus is selected by a decoder. The decoder activates one of the register load inputs, thus providing a transfer path between the data in the output bus and the inputs of the selected destination register.

The control unit that operates the CPU bus system directs the information flow through the registers and ALU by selecting the various components in the system. For example, to perform the operation

$$R1 \leftarrow R2 + R3$$

the control must provide binary selection variables to the following selector inputs:

- **1.** MUX A selector (SELA): to place the content of R2 into bus A.
- **2.** MUX B selector (SELB): to place the content of *R*3 into bus *B*.
- **3.** ALU operation selector (OPR): to provide the arithmetic addition A + B.
- **4.** Decoder destination selector (SELD): to transfer the content of the output bus into R1.

The four control selection variables are generated in the control unit and must be available at the beginning of a clock cycle. The data from the two source registers propagate through the gates in the multiplexers and the ALU, to the output bus, and into the inputs of the destination register, all during the clock cycle interval. Then, when the next clock transition occurs, the binary information from the output bus is transferred into *R*1. To achieve a fast response time, the ALU is constructed with high-speed circuits. The buses are implemented with multiplexers or three-state gates, as shown in Sec. 4-3.

Control Word

control word

There are 14 binary selection inputs in the unit, and their combined value specifies a *control word*. The 14-bit control word is defined in Fig. 8-2(b). It consists of four fields. Three fields contain three bits each, and one field has five bits. The three bits of SELA select a source register for the *A* input of the ALU. The three bits of SELB select a register for the *B* input of the ALU. The three bits of SELD select a destination register using the decoder and its seven load outputs. The five bits of OPR select one of the operations in the ALU. The 14-bit control word when applied to the selection inputs specify a particular microoperation.

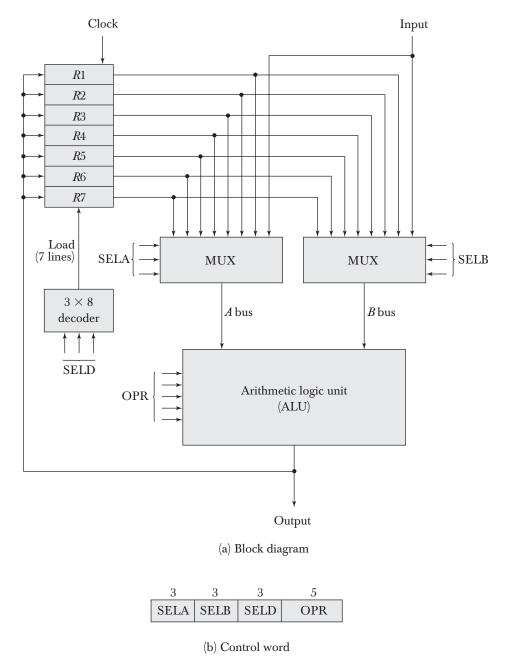


Figure 8-2 Register set with common ALU.

Binary Code **SELA SELB SELD** 000 Input Input None 001 R1R1R1R2R2R2010 011 R3R3R3100 R4R4R4101 R5R5R5110 R6R6R6111 R7R7R7

TABLE 8-1 Encoding of Register Selection Fields

The encoding of the register selections is specified in Table 8-1. The 3-bit binary code listed in the first column of the table specifies the binary code for each of the three fields. The register selected by fields SELA, SELB, and SELD is the one whose decimal number is equivalent to the binary number in the code. When SELA or SELB is 000, the corresponding multiplexer selects the external input data. When SELD = 000, no destination register is selected but the contents of the output bus are available in the external output.

The ALU provides arithmetic and logic operations. In addition, the CPU must provide shift operations. The shifter may be placed in the input of the ALU to provide a preshift capability, or at the output of the ALU to provide postshifting capability. In some cases, the shift operations are included with the ALU. An arithmetic logic and shift unit was designed in Sec. 4-7. The function table for this ALU is listed in Table 4-8. The encoding of the ALU operations for the CPU is taken from Sec. 4-7 and is specified in Table 8-2. The OPR field has five bits and each operation is designated with a symbolic name.

TABLE 8-2 Encoding of ALU Operations

OPR Select	Operation	Symbol
00000 00001 00010 00101 00110 01000 01010 01100 01110 10000	Transfer A Increment A Add $A + B$ Subtract $A - B$ Decrement A AND A and B OR A and B XOR A and B Complement A Shift right A	TSFA INCA ADD SUB DECA AND OR XOR COMA SHRA SHLA

ALU

 $R5 \leftarrow 0$

R5

Examples of Microoperations

A control word of 14 bits is needed to specify a microoperation in the CPU. The control word for a given microoperation can be derived from the selection variables. For example, the subtract microoperation given by the statement

$$R1 \leftarrow R2 - R3$$

specifies R2 for the A input of the ALU, R3 for the B input of the ALU, R1 for the destination register, and an ALU operation to subtract A-B. Thus the control word is specified by the four fields and the corresponding binary value for each field is obtained from the encoding listed in Tables 8-1 and 8-2. The binary control word for the subtract microoperation is 010 011 001 00101 and is obtained as follows:

Field:	SELA	SELB	SELD	OPR
Symbol:	R2	R 3	R1	SUB
Control word:	010	011	001	00101

The control word for this microoperation and a few others are listed in Table 8-3.

The increment and transfer microoperations do not use the *B* input of the ALU. For these cases, the B field is marked with a dash. We assign 000 to any unused field when formulating the binary control word, although any other binary number may be used. To place the content of a register into the output terminals we place the content of the register into the *A* input of the ALU, but none of the registers are selected to accept the data. The ALU operation TSFA places the data from the register, through the ALU, into the output terminals. The direct transfer from input to output is accomplished with a control word of all 0's (making the *B* field 000).

	Symbolic Designation				
Microoperation	SELA	SELB	SELD	OPR	Control Word
$R1 \leftarrow R2 - R3$	R2	R3	R1	SUB	010 011 001 00101
$R4 \leftarrow R4 \lor R5$	R4	R5	R4	OR	100 101 100 01010
$R6 \leftarrow R6 + 1$	R6	_	R6	INCA	110 000 110 00001
$R7 \leftarrow R1$	R1	_	R7	TSFA	001 000 111 00000
Output $\leftarrow R2$	R2	_	None	TSFA	010 000 000 000000
$Output \leftarrow Input$	Input	_	None	TSFA	000 000 000 00000
$R4 \leftarrow \text{sh} 1 R4$	R4	_	R4	SHLA	100 000 100 11000

R5

XOR

101 101 101 01100

R5

TABLE 8-3 Examples of Microoperations for the CPU



A register can be cleared to 0 with an exclusive-OR operation. This is because $x \oplus x = 0$.

It is apparent from these examples that many other microoperations can be generated in the CPU. The most efficient way to generate control words with a large number of bits is to store them in a memory unit. A memory unit that stores control words is referred to as a control memory. By reading consecutive control words from memory, it is possible to initiate the desired sequence of microoperations for the CPU. This type of control is referred to as microprogrammed control. A microprogrammed control unit is shown in Fig. 7-8. The binary control word for the CPU will come from the outputs of the control memory marked "micro-ops."

8-3 Stack Organization

A useful feature that is included in the CPU of most computers is a stack or last-in, first-out (LIFO) list. A stack is a storage device that stores information in such a manner that the item stored last is the first item retrieved. The operation of a stack can be compared to a stack of trays. The last tray placed on top of the stack is the first to be taken off.

The stack in digital computers is essentially a memory unit with an address register that can count only (after an initial value is loaded into it). The register that holds the address for the stack is called a stack pointer (SP) because its value always points at the top item in the stack. Contrary to a stack of trays where the tray itself may be taken out or inserted, the physical registers of a stack are always available for reading or writing. It is the content of the word that is inserted or deleted.

The two operations of a stack are the insertion and deletion of items. The operation of insertion is called *push* (or push-down) because it can be thought of as the result of pushing a new item on top. The operation of deletion is called *pop* (or pop-up) because it can be thought of as the result of removing one item so that the stack pops up. However, nothing is pushed or popped in a computer stack'. These operations are simulated by incrementing or decrementing the stack pointer register.

Register Stack

A stack can be placed in a portion of a large memory or it can be organized as a collection of a finite number of memory words or registers. Figure 8-3 shows the organization of a 64-word register stack. The stack pointer register SP contains a binary number whose value is equal to the address of the word that is currently on top of the stack. Three items are placed in the stack: A, B, and C, in that order. Item C is on top of the stack so that the content of SP is now 3. To remove the top item, the stack is popped by reading the memory word at address 3 and decrementing the content of SP. Item B is now on top of the stack

LIFO

stack pointer

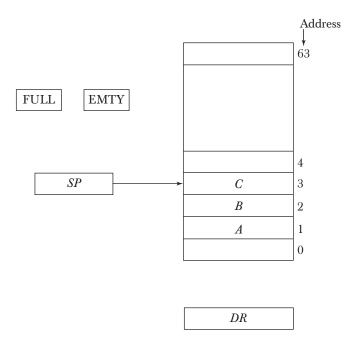


Figure 8-3 Block diagram of a 64-word stack.

since SP holds address 2. To insert a new item, the stack is pushed by incrementing SP and writing a word in the next-higher location in the stack. Note that item C has been read out but not physically removed. This does not matter because when the stack is pushed, a new item is written in its place.

In a 64-word stack, the stack pointer contains 6 bits because $2^6 = 64$. Since SP has only six bits, it cannot exceed a number greater than 63 (111111 in binary). When 63 is incremented by 1, the result is 0 since 111111 + 1 = 10000000 in binary, but SP can accommodate only the six least significant bits. Similarly, when 000000 is decremented by 1, the result is 111111. The one-bit register FULL is set to 1 when the stack is full, and the one-bit register EMTY is set to 1 when the stack is empty of items. DR is the data register that holds the binary data to be written into or read out of the stack.

Initially, SP is cleared to 0, EMTY is set to 1, and FULL is cleared to 0, so that SP points to the word at address 0 and the stack is marked empty and not full. If the stack is not full (if FULL = 0), a new item is inserted with a push operation. The push operation is implemented with the following sequence of microoperations:

$$SP \leftarrow SP + 1$$
 Increment stack pointer $M[SP] \leftarrow DR$ Write item on top of the stack

push

to the use of load and store instructions when communicating between memory and CPU. All other instructions are executed within the registers of the CPU without referring to memory. A program for a RISC-type CPU consists of LOAD and STORE instructions that have one memory and one register address, and computational-type instructions that have three addresses with all three specifying processor registers. The following is a program to evaluate X = (A + B) * (C + D).

LOAD	R1, A	$R1 \leftarrow M[A]$
LOAD	R2, B	$R2 \leftarrow M[B]$
LOAD	R3, C	$R3 \leftarrow M[C]$
LOAD	R4, D	$R4 \leftarrow M[D]$
ADD	R1, R1, R2	$R1 \leftarrow R1 + R2$
ADD	R3, R3, R2	$R3 \leftarrow R3 + R4$
MUL	R1, R1, R3	$R1 \leftarrow R1 * R3$
STORE	X, R1	$M[X] \leftarrow R1$

The load instructions transfer the operands from memory to CPU registers. The add and multiply operations are executed with data in the registers without accessing memory. The result of the computations is then stored in memory with a store instruction.

8-5 Addressing Modes

The operation field of an instruction specifies the operation to be performed. This operation must be executed on some data stored in computer registers or memory words. The way the operands are chosen during program execution is dependent on the addressing mode of the instruction. The addressing mode specifies a rule for interpreting or modifying the address field of the instruction before the operand is actually referenced. Computers use addressing mode techniques for the purpose of accommodating one or both of the following provisions:

- 1. To give programming versatility to the user by providing such facilities as pointers to memory, counters for loop control, indexing of data, and program relocation.
- 2. To reduce the number of bits in the addressing field of the instruction.

The availability of the addressing modes gives the experienced assembly language programmer flexibility for writing programs that are more efficient with respect to the number of instructions and execution time.

To understand the various addressing modes to be presented in this section, it is imperative that we understand the basic operation cycle of the

computer. The control unit of a computer is designed to go through an instruction cycle that is divided into three major phases:

- **1.** Fetch the instruction from memory.
- 2. Decode the instruction.
- **3.** Execute the instruction.

program counter (PC) There is one register in the computer called the program counter or PC that keeps track of the instructions in the program stored in memory. PC holds the address of the instruction to be executed next and is incremented each time an instruction is fetched from memory. The decoding done in step 2 determines the operation to be performed, the addressing mode of the instruction, and the location of the operands. The computer then executes the instruction and returns to step 1 to fetch the next instruction in sequence.

In some computers the addressing mode of the instruction is specified with a distinct binary code, just like the operation code is specified. Other computers use a single binary code that designates both the operation and the mode of the instruction. Instructions may be defined with a variety of addressing modes, and sometimes, two or more addressing modes are combined in one instruction.

An example of an instruction format with a distinct addressing mode field is shown in Fig. 8-6. The operation code specifies the operation to be performed. The mode field is used to locate the operands needed for the operation. There may or may not be an address field in the instruction. If there is an address field, it may designate a memory address or a processor register. Moreover, as discussed in the preceding section, the instruction may have more than one address field, and each address field may be associated with its own particular addressing mode.

Although most addressing modes modify the address field of the instruction, there are two modes that need no address field at all. These are the implied and immediate modes.

Implied Mode: In this mode the operands are specified implicitly in the definition of the instruction. For example, the instruction "complement accumulator" is an implied-mode instruction because the operand in the accumulator register is implied in the definition of the instruction. In fact, all register reference instructions that use an accumulator are implied-mode instructions. Zero-address

Figure 8-6 Instruction format with mode field.

Opcode	Mode	Address
--------	------	---------

mode field

instructions in a stack-organized computer are implied-mode instructions since the operands are implied to be on top of the stack.

Immediate Mode: In this mode the operand is specified in the instruction itself. In other words, an immediate-mode instruction has an operand field rather than an address field. The operand field contains the actual operand to be used in conjunction with the operation specified in the instruction. Immediate-mode instructions are useful for initializing registers to a constant value.

It was mentioned previously that the address field of an instruction may specify either a memory word or a processor register. When the address field specifies a processor register, the instruction is said to be in the register mode.

Register Mode: In this mode the operands are in registers that reside within the CPU. The particular register is selected from a register field in the instruction. A k-bit field can specify any one of 2^k registers.

Register Indirect Mode: In this mode the instruction specifies a register in the CPU whose contents give the address of the operand in memory. In other words, the selected register contains the address of the operand rather than the operand itself. Before using a register indirect mode instruction, the programmer must ensure that the memory address of the operand is placed in the processor register with a previous instruction. A reference to the register is then equivalent to specifying a memory address. The advantage of a register indirect mode instruction is that the address field of the instruction uses fewer bits to select a register than would have been required to specify a memory address directly.

Autoincrement or Autodecrement Mode: This is similar to the register indirect mode except that the register is incremented or decremented after (or before) its value is used to access memory. When the address stored in the register refers to a table of data in memory, it is necessary to increment or decrement the register after every access to the table. This can be achieved by using the increment or decrement instruction. However, because it is such a common requirement, some computers incorporate a special mode that automatically increments or decrements the content of the register after data access.

The address field of an instruction is used by the control unit in the CPU to obtain the operand from memory. Sometimes the value given in the address field is the address of the operand, but sometimes it is just an address from which the address of the operand is calculated. To differentiate among the various addressing modes it is necessary to distinguish between the address part of the instruction and the effective address used by the control when executing the instruction. The *effective address* is defined to be the memory address obtained from the computation dictated by the given addressing mode. The effective address is the address of the operand in a computational-type instruction. It is

effective address

the address where control branches in response to a branch-type instruction. We have already defined two addressing modes in Chap. 5. They are summarized here for reference.

Direct Address Mode: In this mode the effective address is equal to the address part of the instruction. The operand resides in memory and its address is given directly by the address field of the instruction. In a branch-type instruction the address field specifies the actual branch address.

Indirect Address Mode: In this mode the address field of the instruction gives the address where the effective address is stored in memory. Control fetches the instruction from memory and uses its address part to access memory again to read the effective address. The indirect address mode is also explained in Sec. 5-1 in conjunction with Fig. 5-2.

A few addressing modes require that the address field of the instruction be added to the content of a specific register in the CPU. The effective address in these modes is obtained from the following computation:

effective address = address part of instruction + content of CPU register

The CPU register used in the computation may be the program counter, an index register, or a base register. In either case we have a different addressing mode which is used for a different application.

Relative Address Mode: In this mode the content of the program counter is added to the address part of the instruction in order to obtain the effective address. The address part of the instruction is usually a signed number (in 2's complement representation) which can be either positive or negative. When this number is added to the content of the program counter, the result produces an effective address whose position in memory is relative to the address of the next instruction. To clarify with an example, assume that the program counter contains the number 825 and the address part of the instruction contains the number 24. The instruction at location 825 is read from memory during the fetch phase and the program counter is then incremented by one to 826. The effective address computation for the relative address mode is 826 + 24 = 850. This is 24 memory locations forward from the address of the next instruction. Relative addressing is often used with branch-type instructions when the branch address is in the area surrounding the instruction word itself. It results in a shorter address field in the instruction format since the relative address can be specified with a smaller number of bits compared to the number of bits required to designate the entire memory address.

Indexed Addressing Mode: In this mode the content of an index register is added to the address part of the instruction to obtain the effective address.

The index register is a special CPU register that contains an index value. The address field of the instruction defines the beginning address of a data array in memory. Each operand in the array is stored in memory relative to the beginning address. The distance between the beginning address and the address of the operand is the index value stored in the index register. Any operand in the array can be accessed with the same instruction provided that the index register contains the correct index value. The index register can be incremented to facilitate access to consecutive operands. Note that if an index-type instruction does not include an address field in its format, the instruction converts to the register indirect mode of operation.

Some computers dedicate one CPU register to function solely as an index register. This register is involved implicitly when, the index-mode instruction is used. In computers with many processor registers, any one of the CPU registers can contain the index number. In such a case the register must be specified explicitly in a register field within the instruction format.

Base Register Addressing Mode: In this mode the content of a base register is added to the address part of the instruction to obtain the effective address. This is similar to the indexed addressing mode except that the register is now called a base register instead of an index register. The difference between the two modes is in the way they are used rather than in the way that they are computed. An index register is assumed to hold an index number that is relative to the address part of the instruction. A base register is assumed to hold a base address and the address field of the instruction gives a displacement relative to this base address. The base register addressing mode is used in computers to facilitate the relocation of programs in memory. When programs and data are moved from one segment of memory to another, as required in multiprogramming systems, the address values of instructions must reflect this change of position. With a base register, the displacement values of instructions do not have to change. Only the value of the base register requires updating to reflect the beginning of a new memory segment.

Numerical Example

To show the differences between the various modes, we will show the effect of the addressing modes on the instruction defined in Fig. 8-7. The two-word instruction at address 200 and 201 is a "load to AC" instruction with an address field equal to 500. The first word of the instruction specifies the operation code and mode, and the second word specifies the address part. PC has the value 200 for fetching this instruction. The content of processor register R1 is 400, and the content of an index register XR is 100. AC receives the operand after the instruction is executed. The figure lists a few pertinent addresses and shows the memory content at each of these addresses.

	Address	Memory
PC = 200	200	Load to AC Mode
	201	Address = 500
R1 = 400	202	Next instruction
XR = 100		
	399	450
AC	400	700
	500	800
	600	900
	702	325
	800	300

Figure 8-7 Numerical example for addressing modes.

The mode field of the instruction can specify any one of a number of modes. For each possible mode we calculate the effective address and the operand that must be loaded into AC. In the direct address mode the effective address is the address part of the instruction 500 and the operand to be loaded into AC is 800. In the immediate mode the second word of the instruction is taken as the operand rather than an address, so 500 is loaded into AC. (The effective address in this case is 201.) In the indirect mode the effective address is stored in memory at address 500. Therefore, the effective address is 800 and the operand is 300. In the relative mode the effective address is 500 + 202 =702 and the operand is 325. (Note that the value in PC after the fetch phase and during the execute phase is 202.) In the index mode the effective address is XR + 500 = 100 + 500 = 600 and the operand is 900. In the register mode the operand is in R1 and 400 is loaded into AC. (There is no effective address in this case.) In the register indirect mode the effective address is 400, equal to the content of R1 and the operand loaded into AC is 700. The autoincrement mode is the same as the register indirect mode except that R1 is incremented to 401 after the execution of the instruction. The autodecrement mode decrements R1 to 399 prior to the execution of the instruction. The operand loaded into AC is now 450. Table 8-4 lists the values of the effective address and the operand loaded into AC for the nine addressing modes.



the program while external interrupts are asynchronous. If the program is rerun, the internal interrupts will occur in the same place each time. External interrupts depend on external conditions that are independent of the program being executed at the time.

software interrupt

External and internal interrupts are initiated from signals that occur in the hardware of the CPU. A software interrupt is initiated by executing an instruction. Software interrupt is a special call instruction that behaves like an interrupt rather than a subroutine call. It can be used by the programmer to initiate an interrupt procedure at any desired point in the program. The most common use of software interrupt is associated with a supervisor call instruction. This instruction provides means for switching from a CPU user mode to the supervisor mode. Certain operations in the computer may be assigned to the supervisor mode only, as for example, a complex input or output transfer procedure. A program written by a user must run in the user mode. When an input or output transfer is required, the supervisor mode is requested by means of a supervisor call instruction. This instruction causes a software interrupt that stores the old CPU state and brings in a new PSW that belongs to the supervisor mode. The calling program must pass information to the operating system in order to specify the particular task requested.

8-8 Reduced Instruction Set Computer (RISC)

An important aspect of computer architecture is the design of the instruction set for the processor. The instruction set chosen for a particular computer determines the way that machine language programs are constructed. Early computers had small and simple instruction sets, forced mainly by the need to minimize the hardware used to implement them. As digital hardware became cheaper with the advent of integrated circuits, computer instructions tended to increase both in number and complexity. Many computers have instruction sets that include more than 100 and sometimes even more than 200 instructions. These computers also employ a variety of data types and a large number of addressing modes. The trend into computer hardware complexity was influenced by various factors, such as upgrading existing models to provide more customer applications, adding instructions that facilitate the translation from high-level language into machine language programs, and striving to develop machines that move functions from software implementation into hardware implementation. A computer with a large number of instructions is classified as a *complex instruction set computer*, abbreviated CISC.

In the early 1980s, a number of computer designers recommended that computers use fewer instructions with simple constructs so they can be executed much faster within the CPU without having to use memory as often. This type of computer is classified as a *reduced instruction set computer* or RISC.

CISC

RISC

In this section we introduce the major characteristics of CISC and RISC architectures and then present the instruction set and instruction format of a RISC processor.

CISC Characteristics

The design of an instruction set for a computer must take into consideration not only machine language constructs, but also the requirements imposed on the use of high-level programming languages. The translation from high-level to machine language programs is done by means of a compiler program. One reason for the trend to provide a complex instruction set is the desire to simplify the compilation and improve the overall computer performance. The task of a compiler is to generate a sequence of machine instructions for each high-level language statement. The task is simplified if there are machine instructions that implement the statements directly. The essential goal of a CISC architecture is to attempt to provide a single machine instruction for each statement that is written in a high-level language. Examples of CISC architectures are the Digital Equipment Corporation VAX computer and the IBM 370 computer.

Another characteristic of CISC architecture is the incorporation of variable-length instruction formats. Instructions that require register operands may be only two bytes in length, but instructions that need two memory addresses may need five bytes to include the entire instruction code. If the computer has 32-bit words (four bytes), the first instruction occupies half a word, while the second instruction needs one word in addition to one byte in the next word. Packing variable instruction formats in a fixed-length memory word requires special decoding circuits that count bytes within words and frame the instructions according to their byte length.

The instructions in a typical CISC processor provide direct manipulation of operands residing in memory. For example, an ADD instruction may specify one operand in memory through index addressing and a second operand in memory through a direct addressing. Another memory location may be included in the instruction to store the sum. This requires three memory references during execution of the instruction. Although CISC processors have instructions that use only processor registers, the availability of other modes of operations tend to simplify high-level language compilation. However, as more instructions and addressing modes are incorporated into a computer, the more hardware logic is needed to implement and support them, and this may cause the computations to slow down. In summary, the major characteristics of CISC architecture are:

- 1. A large number of instructions—typically from 100 to 250 instructions
- 2. Some instructions that perform specialized tasks and are used infrequently

- 3. A large variety of addressing modes—typically from 5 to 20 different modes
- 4. Variable-length instruction formats
- 5. Instructions that manipulate operands in memory

RISC Characteristics

The concept of RISC architecture involves an attempt to reduce execution time by simplifying the instruction set of the computer. The major characteristics of a RISC processor are:

- 1. Relatively few instructions
- 2. Relatively few addressing modes
- 3. Memory access limited to load and store instructions
- 4. All operations done within the registers of the CPU
- 5. Fixed-length, easily decoded instruction format
- **6.** Single-cycle instruction execution
- 7. Hardwired rather than microprogrammed control

The small set of instructions of a typical RISC processor consists mostly of register-to-register operations, with only simple load and store operations for memory access. Thus each operand is brought into a processor register with a load instruction. All computations are done among the data stored in processor registers. Results are transferred to memory by means of store instructions. This architectural feature simplifies the instruction set and encourages the optimization of register manipulation. The use of only a few addressing modes results from the fact that almost all instructions have simple register addressing. Other addressing modes may be included, such as immediate operands and relative mode.

By using a relatively simple instruction format, the instruction length can be fixed and aligned on word boundaries. An important aspect of RISC instruction format is that it is easy to decode. Thus the operation code and register fields of the instruction code can be accessed simultaneously by the control. By simplifying the instructions and their format, it is possible to simplify the control logic. For faster operations, a hardwired control is preferable over a microprogrammed control. An example of hardwired control is presented in Chap. 5 in conjunction with the control unit of the basic computer. Examples of microprogrammed control are presented in Chap. 7.

A characteristic of RISC processors is their ability to execute one instruction per clock cycle. This is done by overlapping the fetch, decode, and execute phases of two or three instructions by using a procedure referred to as pipelining. A load or store instruction may require two clock cycles because access to



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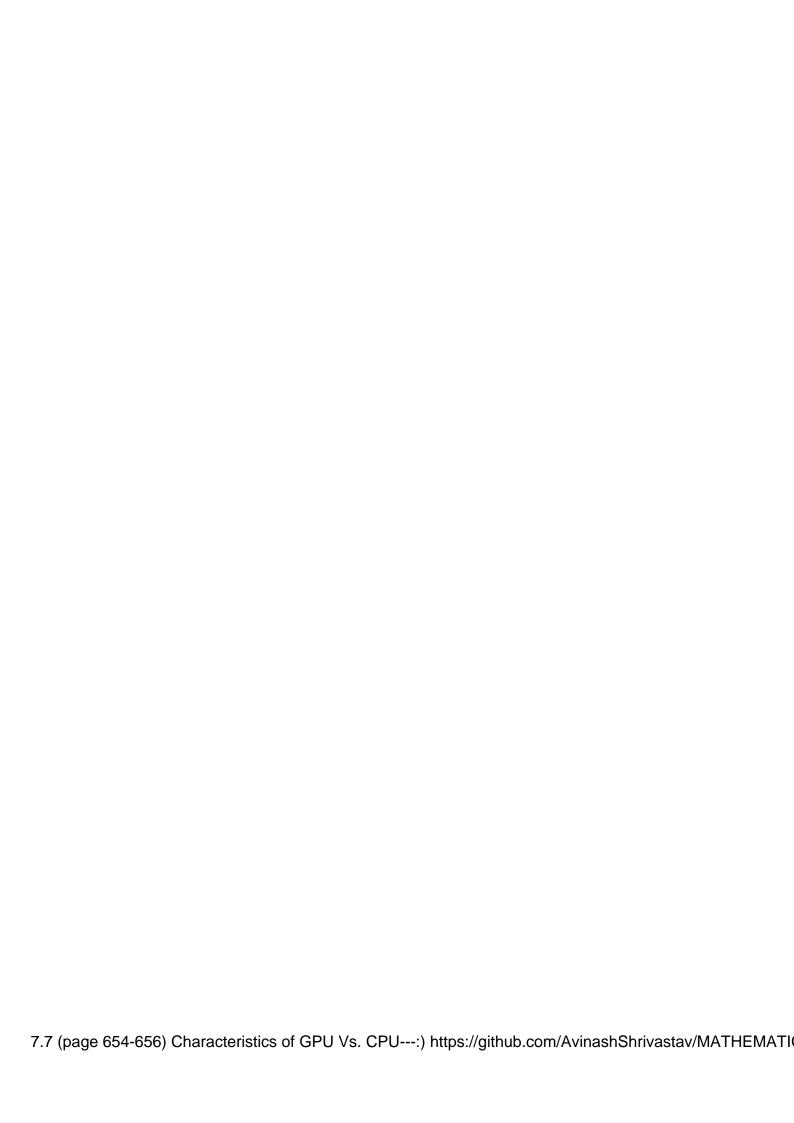
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record separator (RS) and file separator (FS). The communication control characters are useful during the transmission of text between remote terminals. Examples of communication control characters are STX (start of text) and ETX (end of text), which are used to frame a text message when transmitted through a communication medium.

ASCII is a 7-bit code, but most computers manipulate an 8-bit quantity as a single unit called a *byte*. Therefore, ASCII characters most often are stored one per byte. The extra bit is sometimes used for other purposes, depending on the application. For example, some printers recognize 8-bit ASCII characters with the most significant bit set to 0. Additional 128 8-bit characters with the most significant bit set to 1 are used for other symbols, such as the Greek alphabet or italic type font. When used in data communication, the eighth bit may be employed to indicate the parity of the binary-coded character.

11-2 Input-Output Interface

Input–output interface provides a method for transferring information between internal storage and external I/O devices. Peripherals connected to a computer need special communication links for interfacing them with the central processing unit. The purpose of the communication link is to resolve the differences that exist between the central computer and each peripheral. The major differences are:

- Peripherals are electromechanical and electromagnetic devices and their manner of operation is different from the operation of the CPU and memory, which are electronic devices. Therefore, a conversion of signal values may be required.
- 2. The data transfer rate of peripherals is usually slower than the transfer rate of the CPU, and consequently, a synchronization mechanism may be needed.
- **3.** Data codes and formats in peripherals differ from the word format in the CPU and memory.
- **4.** The operating modes of peripherals are different from each other and each must be controlled so as not to disturb the operation of other peripherals connected to the CPU.

To resolve these differences, computer systems include special hardware components between the CPU and peripherals to supervise and synchronize all input and output transfers. These components are called *interface* units because they interface between the processor bus and the peripheral device. The word "Interface" is a general term for the point of contact between two parts of a system. In digital computer system the interface is refered as a complementary set of signal connection points between two parts of a system. Therefore, "to interface" means to attach two or more components or systems,

byte

interface

via their respective interface points for data exchanges between them. Two main types of interface are CPU interface that corresponds to the system bus and input–output interface that depends on the nature of input–output device. To attach an input–output device to CPU and input–output interface, circuit is placed between the device and the system bus. This circuit is meant for matching the signal formats and timing characteristics of the CPU interface to those of the input–output device interface. The main function of input–output interface circuit are data conversion, synchronization and device selection. Data conversion refers to conversion between digital and analog signals, and conversion between serial and parallel data formats. Synchronation refers to matching of operating speeds of CPU and other peripherals. Device selection refers to the selection of I/O device by CPU in a queue manner. In addition, each device may have its own controller that supervises the operations of the particular mechanism in the peripheral.

I/O Bus and Interface Modules

A typical communication link between the processor and several peripherals is shown in Fig. 11-1. The I/O bus consists of data lines, address lines, and control lines. The magnetic disk, printer, and terminal are employed in practically any general-purpose computer. The magnetic tape is used in some computers for backup storage. Each peripheral device has associated with it an interface unit. Each interface decodes the address and control received from the I/O bus, interprets them for the peripheral, and provides signals for the peripheral controller. It also synchronizes the data flow and supervises the transfer between peripheral and processor. Each peripheral has its own controller that operates the particular electromechanical device. For example, the printer controller controls the paper motion, the print timing, and the selection of printing characters. A controller may be housed separately or may be physically integrated with the peripheral.

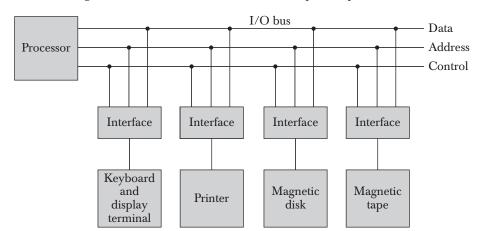


Figure 11-1 Connection of I/O bus to input–output devices.

directs the movement of data through the registers. Whenever the F_i bit of the control register is set $(F_i = 1)$ and the F_{i+1} bit is reset $(F'_{i+1} = 1)$, a clock is generated causing register R(I+1) to accept the data from register RI. The same clock transition sets F_{i+1} to 1 and resets F_i to 0. This causes the control flag to move one position to the right together with the data. Data in the registers move down the FIFO toward the output as long as there are empty locations ahead of it. This ripple-through operation stops when the data reach a register RI with the next flip-flop F_{i+1} being set to 1, or at the last register RI. An overall master clear is used to initialize all control register flip-flops to 0.

Data are inserted into the buffer provided that the *input ready* signal is enabled. This occurs when the first control flip-flop F_1 is reset, indicating that register R1 is empty. Data are loaded from the input lines by enabling the clock in R1 through the *insert* control line. The same clock sets F_1 , which disables the *input ready* control, indicating that the FIFO is now busy and unable to accept more data. The ripple-through process begins provided that R2 is empty. The data in R1 are transferred into R2 and F_1 is cleared. This enables the *input ready* line, indicating that the inputs are now available for another data word. If the FIFO is full, F_1 remains set and the *input ready* line stays in the 0 state. Note that the two control lines *input ready* and *insert* constitute a destination-initiated pair of handshake lines.

The data falling through the registers stack up at the output end. The *output ready* control line is enabled when the last control flip-flop F_4 is set, indicating that there are valid data in the output register R4. The output data from R4 are accepted by a destination unit, which then enables the *delete* control signal. This resets F_4 , causing *output ready* to disable, indicating that the data on the output are no longer valid. Only after the *delete* signal goes back to 0 can the data from R3 move into R4. If the FIFO is empty, there will be no data in R3 and F_4 will remain in the reset state. Note that the two control lines *output ready* and *delete* constitute a source-initiated pair of handshake lines.

11-4 Modes of Transfer

Binary information received from an external device is usually stored in memory for later processing. Information transferred from the central computer into an external device originates in the memory unit. The CPU merely executes the I/O instructions and may accept the data temporarily, but the ultimate source or destination is the memory unit. Data transfer between the central computer and I/O devices may be handled in a variety of modes. Some modes use the CPU as an intermediate path; others transfer the data directly to and from the memory unit. Data transfer to and from peripherals may be handled in one of three possible modes:

- 1. Programmed I/O
- 2. Interrupt-initiated I/O
- 3. Direct memory access (DMA)

programmed I/O

Programmed I/O operations are the result of I/O instructions written in the computer program. Each data item transfer is initiated by an instruction in the program. Usually, the transfer is to and from a CPU register and peripheral. Other instructions are needed to transfer the data to and from CPU and memory. Transferring data under program control requires constant monitoring of the peripheral by the CPU. Once a data transfer is initiated, the CPU is required to monitor the interface to see when a transfer can again be made. It is up to the programmed instructions executed in the CPU to keep close tabs on everything that is taking place in the interface unit and the I/O device.

In the programmed I/O method, the CPU stays in a program loop until the I/O unit indicates that it is ready for data transfer. This is a time-consuming process since it keeps the processor busy needlessly. It can be avoided by using an interrupt facility and special commands to inform the interface to issue an interrupt request signal when the data are available from the device. In the meantime the CPU can proceed to execute another program. The interface meanwhile keeps monitoring the device. When the interface determines that the device is ready for data transfer, it generates an interrupt request to the computer. Upon detecting the external interrupt signal, the CPU momentarily stops the task it is processing, branches to a service program to process the I/O

transfer, and then returns to the task it was originally performing.

Transfer of data under programmed I/O is between CPU and peripheral. In direct memory access (DMA), the interface transfers data into and out of the memory unit through the memory bus. The CPU initiates the transfer by supplying the interface with the starting address and the number of words needed to be transferred and then proceeds to execute other tasks. When the transfer is made, the DMA requests memory cycles through the memory bus. When the request is granted by the memory controller, the DMA transfers the data directly into memory. The CPU merely delays its memory access operation to allow the direct memory I/O transfer. Since peripheral speed is usually slower than processor speed, I/O-memory transfers are infrequent compared to processor access to memory. DMA transfer is discussed in more detail in Sec. 11-6.

Many computers combine the interface logic with the requirements for direct memory access into one unit and call it an I/O processor (IOP). The IOP can handle many peripherals through a DMA and interrupt facility. In such a system, the computer is divided into three separate modules: the memory unit, the CPU, and the IOP. I/O processors are presented in Sec. 11-7.

Example of Programmed I/O

In the programmed I/O method, the I/O device does not have direct access to memory. A transfer from an I/O device to memory requires the execution of several instructions by the CPU, including an input instruction to transfer the data from the device to the CPU and a store instruction to transfer the data from the CPU to memory. Other instructions may be needed to verify that the data are available from the device and to count the numbers of words transferred.

interrupt

DMA

ЮР

An example of data transfer from an I/O device through an interface into the CPU is shown in Fig. 11-10. The device transfers bytes of data one at a time as they are available. When a byte of data is available, the device places it in the I/O bus and enables its data valid line. The interface accepts the byte into its data register and enables the data accepted line. The interface sets a bit in the status register that we will refer to as an *F* or "flag" bit. The device can now disable the data valid line, but it will not transfer another byte until the data accepted line is disabled by the interface. This is according to the handshaking procedure established in Fig. 11-5.

A program is written for the computer to check the flag in the status register to determine if a byte has been placed in the data register by the I/O device. This is done by reading the status register into a CPU register and checking the value of the flag bit. If the flag is equal to 1, the CPU reads the data from the data register. The flag bit is then cleared to 0 by either the CPU or the interface, depending on how the interface circuits are designed. Once the flag is cleared, the interface disables the data accepted line and the device can then transfer the next data byte.

A flowchart of the program that must be written for the CPU is shown in Fig. 11-11. It is assumed that the device is sending a sequence of bytes that must be stored in memory. The transfer of each byte requires three instructions:

- 1. Read the status register.
- 2. Check the status of the flag bit and branch to step 1 if not set or to step 3 if set.
- 3. Read the data register.

Each byte is read into a CPU register and then transferred to memory with a store instruction. A common I/O programming task is to transfer a block of words from an I/O device and store them in a memory buffer. A program that

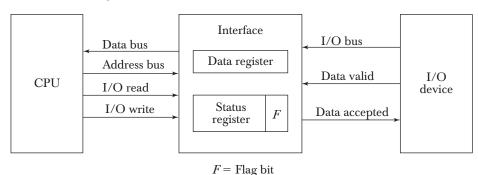


Figure 11-10 Data transfer from I/O device to CPU.

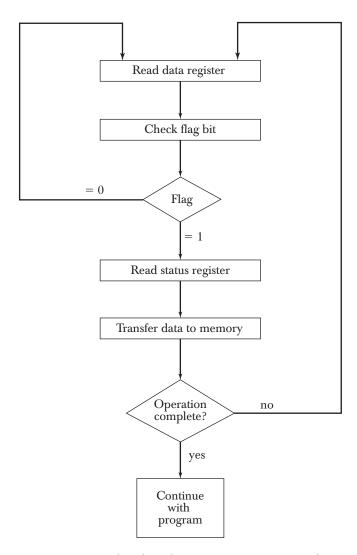


Figure 11-11 Flowchart for CPU program to input data.

stores input characters in a memory buffer using the instructions defined in Chap. 6 is listed in Table 6-21.

The programmed I/O method is particularly useful in small low-speed computers or in systems that are dedicated to monitor a device continuously. The difference in information transfer rate between the CPU and the I/O device makes this type of transfer inefficient. To see why this is inefficient, consider a typical computer that can execute the two instructions that read the status register and check the flag in 1 μs . Assume that the input device transfers

its data at an average rate of 100 bytes per second. This is equivalent to one byte every $10,000~\mu s$. This means that the CPU will check the flag $10,000~\mu s$ times between each transfer. The CPU is wasting time while checking the flag instead of doing some other useful processing task.

Interrupt-Initiated I/O

An alternative to the CPU constantly monitoring the flag is to let the interface inform the computer when it is ready to transfer data. This mode of transfer uses the interrupt facility. While the CPU is running a program, it does not check the flag. However, when the flag is set, the computer is momentarily interrupted from proceeding with the current program and is informed of the fact that the flag has been set. The CPU deviates from what it is doing to take care of the input or output transfer. After the transfer is completed, the computer returns to the previous program to continue what it was doing before the interrupt.

The CPU responds to the interrupt signal by storing the return address from the program counter into a memory stack and then control branches to a service routine that processes the required I/O transfer. The way that the processor chooses the branch address of the service routine varies from one unit to another. In principle, there are two methods for accomplishing this. One is called *vectored interrupt* and the other, *nonvectored interrupt*. In a nonvectored interrupt, the branch address is assigned to a fixed location in memory. In a vectored interrupt, the source that interrupts supplies the branch information to the computer. This information is called the *interrupt vector*. In some computers the interrupt vector is the first address of the I/O service routine. In other computers the interrupt vector is an address that points to a location in memory where the beginning address of the I/O service routine is stored. A system with vectored interrupt is demonstrated in Sec. 11-5.

Software Considerations

The previous discussion was concerned with the basic hardware needed to interface I/O devices to a computer system. A computer must also have software routines for controlling peripherals and for transfer of data between the processor and peripherals. I/O routines must issue control commands to activate the peripheral and to check the device status to determine when it is ready for data transfer. Once ready, information is transferred item by item until all the data are transferred. In some cases, a control command is then given to execute a device function such as stop tape or print characters. Error checking and other useful steps often accompany the transfers. In interrupt-controlled transfers, the I/O software must issue commands to the peripheral to interrupt when ready and to service the interrupt when it occurs. In DMA transfer, the I/O software must initiate the DMA channel to start its operation.

vectored interrupt

I/O routines



the programmer can use any bit configuration for the mask register. The interrupt status bit must be cleared so it can be set again when a higher-priority interrupt occurs. The contents of processor registers are saved because they may be needed by the program that has been interrupted after control returns to it. The interrupt enable *IEN* is then set to allow other (higher-priority) interrupts and the computer proceeds to service the interrupt request.

The final sequence in each interrupt service routine must have instructions to control the interrupt hardware in the following manner:

- **1.** Clear interrupt enable bit *IEN*.
- 2. Restore contents of processor registers.
- **3.** Clear the bit in the interrupt register belonging to the source that has been serviced.
- **4.** Set lower-level priority bits in the mask register.
- **5.** Restore return address into *PC* and set *IEN*.

The bit in the interrupt register belonging to the source of the interrupt must be cleared so that it will be available again for the source to interrupt. The lower-priority bits in the mask register (including the bit of the source being interrupted) are set so they can enable the interrupt. The return to the interrupted program is accomplished by restoring the return address to *PC*. Note that the hardware must be designed so that no interrupts occur while executing steps 2 through 5; otherwise, the return address may be lost and the information in the mask and processor registers may be ambiguous if an interrupt is acknowledged while executing the operations in these steps. For this reason *IEN* is initially cleared and then set after the return address is transferred into *PC*.

The initial and final operations listed above are referred to as *overhead* operations or *housekeeping* chores. They are not part of the service program proper but are essential for processing interrupts. All overhead operations can be implemented by software. This is done by inserting the proper instructions at the beginning and at the end of each service routine. Some of the overhead operations can be done automatically by the hardware. The contents of processor registers can be pushed into a stack by the hardware before branching to the service routine. Other initial and final operations can be assigned to the hardware. In this way, it is possible to reduce the time between receipt of an interrupt and the execution of the instructions that service the interrupt source.

11-6 Direct Memory Access (DMA)

The transfer of data between a fast storage device such as magnetic disk and memory is often limited by the speed of the CPU. Removing the CPU from the path and letting the peripheral device manage the memory buses directly



CHAPTER TWELVE

Memory Organization

IN THIS CHAPTER

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12-2	Main Memory
12-3	Auxiliary Memory
12-4	Associative Memory

Memory Hierarchy

12-5 Cache Memory12-6 Virtual Memory

12-7 Memory Management Hardware

12-1 Memory Hierarchy

12-1

The memory unit is an essential component in any digital computer since it is needed for storing programs and data. A very small computer with a limited application may be able to fulfill its intended task without the need of additional storage capacity. Most general-purpose computers would run more efficiently if they were equipped with additional storage beyond the capacity of the main memory. There is just not enough space in one memory unit to accommodate all the programs used in a typical computer. Moreover, most computer users accumulate and continue to accumulate large amounts of dataprocessing software. Not all accumulated information is needed by the processor at the same time. Therefore, it is more economical to use low-cost storage devices to serve as a backup for storing the information that is not currently used by the CPU. The memory unit that communicates directly with the CPU is called the *main memory*. Devices that provide backup storage are called auxiliary memory. The most common auxiliary memory devices used in computer systems are magnetic disks and tapes. They are used for storing system programs, large data files, and other backup information. Only programs and data currently needed by the processor reside in main memory. All other

auxiliary memory

informatior is stored in auxiliary memory and transferred to main memory when needed.

The total memory capacity of a computer can be visualized as being a hierarchy of components. The memory hierarchy system consists of all storage devices employed in a computer system from the slow but high-capacity auxiliary memory to a relatively faster main memory, to an even smaller and faster cache memory accessible to the high-speed processing logic. Figure 12-1 illustrates the components in a typical memory hierarchy. At the bottom of the hierarchy are the relatively slow magnetic tapes used to store removable files. Next are the magnetic disks used as backup storage. The main memory occupies a central position by being able to communicate directly with the CPU and with auxiliary memory devices through an I/O processor. When programs not residing in main memory are needed by the CPU, they are brought in from auxiliary memory. Programs not currently needed in main memory are transferred into auxiliary memory to provide space for currently used programs and data.

cache memory

A special very-high-speed memory called a *cache* is sometimes used to increase the speed of processing by making current programs and data available to the CPU at a rapid rate. The cache memory is employed in computer systems to compensate for the speed differential between main memory access time and processor logic. CPU logic is usually faster than main memory access time, with the result that processing speed is limited primarily by the speed of main memory. A technique used to compensate for the mismatch in operating speeds is to employ an extremely fast, small cache between the CPU and main memory whose access time is close to processor logic clock cycle time. The cache is used for storing segments of programs currently being executed in the CPU and temporary data frequently needed in the present calculations. By

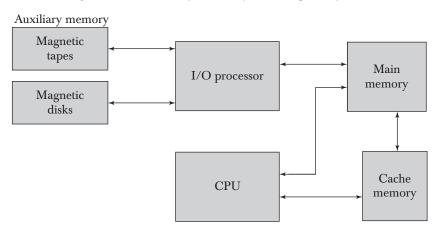


Figure 12-1 Memory hierarchy in a computer system.

making programs and data available at a rapid rate, it is possible to increase the performance rate of the computer.

While the I/O processor manages data transfers between auxiliary memory and main memory, the cache organization is concerned with the transfer of information between main memory and CPU. Thus each is involved with a different level in the memory hierarchy system. The reason for having two or three levels of memory hierarchy is economics. As the storage capacity of the memory increases, the cost per bit for storing binary information decreases and the access time of the memory becomes longer. The auxiliary memory has a large storage capacity, is relatively inexpensive, but has low access speed compared to main memory. The cache memory is very small, relatively expensive, and has very high access speed. Thus as the memory access speed increases, so does its relative cost. The overall goal of using a memory hierarchy is to obtain the highest-possible average access speed while minimizing the total cost of the entire memory system.

Auxiliary and cache memories are used for different purposes. The cache holds those parts of the program and data that are most heavily used, while the auxiliary memory holds those parts that are not presently used by the CPU. Moreover, the CPU has direct access to both cache and main memory but not to auxiliary memory. The transfer from auxiliary to main memory is usually done by means of direct memory access of large blocks of data. The typical access time ratio between cache and main memory is about 1 to 7. For example, a typical cache memory may have an access time of 100 ns, while main memory access time may be 700 ns. Auxiliary memory average access time is usually 1000 times that of main memory. Block size in auxiliary memory typically ranges from 256 to 2048 words, while cache block size is typically from 1 to 16 words.

multiprogramming

Many operating systems are designed to enable the CPU to process a number of independent programs concurrently. This concept, called *multiprogramming*, refers to the existence of two or more programs in different parts of the memory hierarchy at the same time. In this way it is possible to keep all parts of the computer busy by working with several programs in sequence. For example, suppose that a program is being executed in the CPU and an I/O transfer is required. The CPU initiates the I/O processor to start executing the transfer. This leaves the CPU free to execute another program. In a multiprogramming system, when one program is waiting for input or output transfer, there is another program ready to utilize the CPU.

With multiprogramming the need arises for running partial programs, for varying the amount of main memory in use by a given program, and for moving programs around the memory hierarchy. Computer programs are sometimes too long to be accommodated in the total space available in main memory. Moreover, a computer system uses many programs and all the programs cannot reside in main memory at all times. A program with its data normally resides in auxiliary memory. When the program or a segment of the program is to be