Demographic Influences on Municipal Budget Allocation and Infrastructure Development in Toronto*

Population density influences larger budget allocations, while average household income determines the focus of construction projects

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This study examines the relationship between population density, average household income, and budget allocations across Toronto's 25 wards and investigates their combined influence on construction activity. Using data from the city's Capital Budget Plan, Ward Profiles, and Active Building Permits, we analyze spending patterns in key infrastructure-related areas. Employing a causal modeling approach, our findings reveal a negative association between population density and construction activity, despite some high-density wards receiving higher budget allocations. Additionally, average household income and total budget allocations exhibit a positive correlation with the number of building permits. These results underscore potential inequities in resource distribution, highlighting the need for data-driven and equitable urban budget planning to better address community needs.

Table of contents

1	Introduction					
	1.1	Estimand	4			
2	Data	ta				
	2.1	Ward Profiles (25-Ward Model)	5			
	2.2	Capital Budget and Plan Details	6			
	2.3	City Wards	7			

^{*}Code and data are available at: https://github.com/Aviral-03/InfrastructureCausalModel-TO.

	2.4	Building Permits - Active Permits	8					
	2.5	Trends in Budget Allocations (2021-2024)	10					
	2.6	Relationship between Variables of Interest and Budget Allocations	12					
		2.6.1 Relationship between Confounders and Budget Allocations (Service Im-						
		provement and Enhancement)	12					
		2.6.2 Relationship between Confounders and Budget Allocations (Growth-						
		Related and State of Good Repair)	13					
3	Mod	lel	14					
•	3.1	Model set-up	15					
	3.2	Model justification	16					
	0.2	Wiodel Justinearion	10					
4	Resi	ults	16					
	4.1	Distribution of Average Household Income and Population Density	16					
	4.2	Relationship between Confounders, Mediators and Budget Allocations	17					
	4.3	Model Results	18					
5	Disc	Discussion 19						
	5.1	Building Permits and Economic Well-Being	20					
	5.2	Investing in Higher-Income Areas vs. High-Density Areas	20					
	5.3	Budget Allocations and Construction Activity	21					
6	\ \/or	knesses and Future Work	21					
U			21					
	6.1	Future Work	22					
Α	Арр	endix	23					
	A.1	Survey Design for Construction Analysis	23					
	A.2	Sampling Methodology	23					
	A.3	Ensuring Robust Data Collection	23					
	A.4	Building Permits Status	24					
	A.5	Model Details	25					
	A.6	Posterior Predictive Check	25					
	A.7	Comparison of the Posterior and Prior	26					
	A.8	Markov Chain Monte Carlo Convergence	27					
	A.9	Credibility Intervals	29					
D-	.f		30					
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1 Introduction

In urban governance, the equitable allocation of municipal budgets is essential to meet a city's social, economic, and infrastructure needs. This challenge is especially pressing in Toronto,

where 25 wards compete for limited resources amid a growing population ("Ontario's Long-Term Report on the Economy 2024" 2024). Understanding how demographic factors influence budget decisions remains under-explored. Therefore, this study seeks to answer: How do demographic factors such as population and income affect budget allocations across Toronto's wards, and can we assess their combined impact on construction activity, a key indicator of infrastructure development?

Looking back, Toronto's historical budget data have shown uneven investment, particularly in high-density, lower-income areas, leading to disparities in infrastructure and services (Ferguson, Lisa 2024). However, following 2023 Mayor election, Mayor Olivia Chow promise to prioritize housing, transit, and equity-focused initiatives (City of Toronto 2024e). The 2024 budget prioritizes significant investments in affordable housing, transportation, and community safety, while also focusing on long-term infrastructure development through a 10-year capital plan. Notable projects, such as the *Ontario Line* subway expansion, are projected to drive economic growth and urban development (Navabi 2024). Similarly, the *Sidewalks to Skylines* 10-year plan aims to create jobs and enhance residents' quality of life (City of Toronto 2024f). As these initiatives progress, ensuring equitable infrastructure investments will be crucial for Toronto's sustainable growth. With the city's population increasingly distributed across its wards, it is imperative to assess whether current budget allocations effectively align with broader development objectives amidst shifting demographic trends.

This study analyzes data from the City of Toronto's Open Data Portal, incorporating demographic information from the 2021 Ward Profiles, budget details from the Capital Budget & Plan By Ward (10-Year Approved) 2021-2024, and construction data from Building Applications and Permits. Using a Bayesian multi-regression model guided by a causal framework, we found that both average household income and total budget allocations significantly influence the number of building permits. However, population density displayed an unexpected negative relationship with construction activity, suggesting the presence of unobserved factors affecting this link. To address this, we excluded population density as an explanatory variable and confirmed that higher-income wards receiving larger budget allocations corresponded to more construction activity. These findings highlight the importance of understanding how socioeconomic and budgetary factors shape urban development, emphasizing the need for equitable resource distribution to support balanced growth across Toronto's wards.

The paper is organized as follows: Section 2 outlines the data sources and methodology used in the analysis. Section 3 explains the Bayesian model applied to estimate the effects of demographic and economic factors, following the causal model (Figure 1). Section 4 presents key findings, including trends in budget allocations, the relationship between demographic factors and budget distribution, and the impact on construction projects. Section 5 explores the implications for urban governance and budget planning in Toronto. Finally, Section 6 addresses the study's limitations and suggests recommendations for future research. Additional details, including tables, figures, and methodology, are provided in the Section A.

1.1 Estimand

Our research investigates the causal relationships between population, income, budget allocation, and active construction projects, as illustrated in Figure 1. Population and income are key confounders, influencing both budget allocation and the number of construction projects. Budget allocation serves a dual role: as a mediator connecting population and income to construction projects and as an instrumental variable, helping to estimate their effects on construction activity. The outcome variable is the number of active construction projects, while population and income are the primary predictors. Our goal is to estimate the causal effect of budget allocation on construction activity, accounting for the confounding effects of population and income.

Population is a important demographic indicator, representing the number of residents in each ward, while average household income reflects economic well-being, influencing access to resources and quality of life (Schaeffer 2021). Therefore, these two variables of interest were chosen for the analysis. For budget allocations we choose these specific categories of interest, specifically Growth-Related expenditures, State of Good Repair, and Service Improvement and Enhancement.

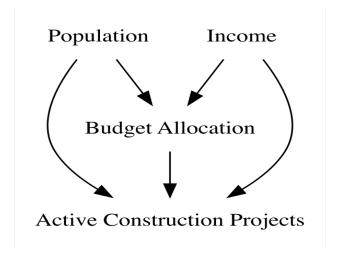


Figure 1: Causal model: Population and income influence budget allocation and construction projects

2 Data

The raw data was sourced from the City of Toronto's Open Data Portal using the opendatatoronto (Sharla Gelfand 2022) package. For the purpose of this analysis we used several data sets: 2023 Ward Profiles (25-Ward Model) (City of Toronto 2024b), Capital Budget and Plan Details from 2021-2024 (City of Toronto 2024d), City Wards (City of Toronto 2024c), and Building Permits - Active Permits (City of Toronto 2024a).

The data, provided in CSV formats, was cleaned and analyzed using R (R Core Team 2024) programming language. The readxl (Wickham and Bryan 2023) package was used for reading Excel files. Other R packages used includes tidyverse (Wickham et al. 2019), styler (Müller and Walthert 2024), and dplyr (Wickham et al. 2023) for creating tables. ggplot2 (Wickham 2016) and kableExtra (Zhu 2024) were used for data visualization and table formatting. The patchwork (Pedersen 2024) package was used for combining multiple plots, and sf (Venables and Ripley 2002) for spatial data analysis. For model estimation, the rstanarm (Brilleman et al. 2018) package was used for Bayesian modeling, and bayesplot (Gabry et al. 2019) for visualizing the results. The lintr (Hester et al. 2024) package was used for code linting.

2.1 Ward Profiles (25-Ward Model)

The 2021 Ward Profiles (City of Toronto 2024b), based on the 25-Ward model were provided by City Planning. These profiles included census data from the 2021, 2016, and 2011 Census of Population, covering demographic, social, and economic information for each ward in Toronto. These variables were collected through methods including online responses, mailed questionnaires, the Census Help Line, and enumerators ("National Household Survey (NHS)" 2023).

These questionnaires gathered information on various topics related to residents' demographic characteristics, such as education, household income, number of dependents, employment status and etc. Participation in the survey is voluntary, and data is collected directly from residents, including their postal codes, which are used to determine their respective wards. To ensure privacy and confidentiality, the data is subsequently aggregated and anonymized (Government of Canada 2023).

This data-set was included in this analysis to provide understanding into the population and average household income for each ward, providing understanding into the city's socioeconomic landscape. 25-Ward model was used instead of the 44-Ward model as it was the most recent data available at the time of analysis and matched the Capital Budget data.

The data was stored in an Excel workbook with multiple tabs, but for this analysis, we used the first tab, 2021 Census One variable, which contains data for all 25 wards (Ward 1, Ward 2, ..., Ward 25). After cleaning, the data was saved in CSV and Parquet formats, with the following columns:

• ward_id: unique identifier for each ward,

• ward: ward name,

• population: total population,

• income: average household income.

The ward names were manually entered into the cleaned data to match with ward_id. A sample of the data can be seen in Table 1.

Table 1: Sample of Cleaned Toronto Ward Profile Data

Ward ID	Ward Name	Population	Income
1	Etobicoke North	115120	95200
2	Etobicoke Centre	117200	146600
3	Etobicoke-Lakeshore	139920	127200
4	Parkdale-High Park	104715	127200
5	York South-Weston	115675	88700
6	York Centre	107355	107500

2.2 Capital Budget and Plan Details

Each year, the City of Toronto publishes the Capital Budget and Plan Details dataset (City of Toronto 2024d), which outlines a 10-year capital budget and plan. This dataset breaks down the capital budget across the city's 25 wards, allocating funds for infrastructure projects, equipment purchases, and other fixed assets. This budget is developed through a collaborative process, where city staff prepare an initial draft, which is then reviewed by the Budget Committee. Input is solicited from Toronto residents and businesses, and subsequently, the Mayor presents the finalized budget proposal by February 1. City Council reviews and considers this budget within 30 days (City of Toronto 2024e).

For the purpose of this analysis we selected the year 2021-2024 to align with the 2022 municipal elections and the subsequent relevance to planning efforts. Furthermore, the city's budgeting process underwent significant shifts after 2020 due to the impact of the COVID-19 pandemic, which altered spending priorities and resource allocation. Focusing on the 2021–2024 timeframe allows us to analyze the post-pandemic period, avoiding the uncertainties of the pandemic and ensuring the data remains consistent and reliable.

Each budget plan includes five primary categories under State of Good Repair, Growth Related, Health and Safety, Service Improvement and Enhancement, and Legislated. These categories define the main areas where capital expenditures are directed. For this analysis, however, we will focus on these three variables of interest: State of Good Repair, Growth Related, and Service Improvement and Enhancement.

Since our analysis aims to understand how budget allocations influence construction activity and infrastructure development, we selected these three categories as they are most relevant to capital expenditures and infrastructure projects. State of Good Repair focuses on maintaining and preserving existing infrastructure, Growth Related addresses the expansion and development of new infrastructure, and Service Improvement and Enhancement aims to enhance public services and amenities.

Raw data includes key columns such as Project Name, yearly budget allocations for each year, Ward Number, Ward, Category, and Total 10 Year (Sum of Year 1 to 10), where the budget is in thousands of dollars (e.g., 10 = \$10,000). Table 2 shows a sample of the cleaned data along with our variables of interest:

- Ward ID
- Ward Name
- Category of the Capital Budget
- Total 10-year capital budget allocated to each ward

Rows with CW (city-wide budget) were removed since they were applicable to all wards.

Ward Total 10-Year Budget (in Ward Name IDCategory 000s1 Etobicoke North Growth Related 37873.0 Etobicoke North Service Improvement and 6361.0 Enhancement Etobicoke Centre Growth Related 69025.0 Etobicoke Centre Service Improvement and 20116.0 Enhancement Etobicoke Centre State of Good Repair 5112.0 3 Etobicoke-Growth Related 85358.9 Lakeshore

Table 2: Sample of Cleaned Toronto Capital Budget Data

2.3 City Wards

The City Wards dataset (City of Toronto 2024c), published by the City Clerk's Office and last updated on July 22, 2024, contains geographical information about each ward, including the ward ID, ward name, and ward boundary. These ward boundaries were decided as a part of Bill 5, Better Local Government Act in 2018, reducing the number of wards from 47 to 25 (City of Toronto 2024c).

This dataset, effective January 1, 2024, was used to map the ward_id to the ward name in the cleaned data. Key columns include:

- ward_id: unique identifier for each ward,
- ward: ward name,
- ward_boundary: geographical boundary of the ward.

The ward names were mapped to the ward_id and integrated with the Ward Profiles Section 2.1 and Capital Budget data sets Section 2.2 to create the final data set for analysis. This dataset was not used directly in the analysis but was essential for mapping the ward names to the ward IDs in the cleaned data.

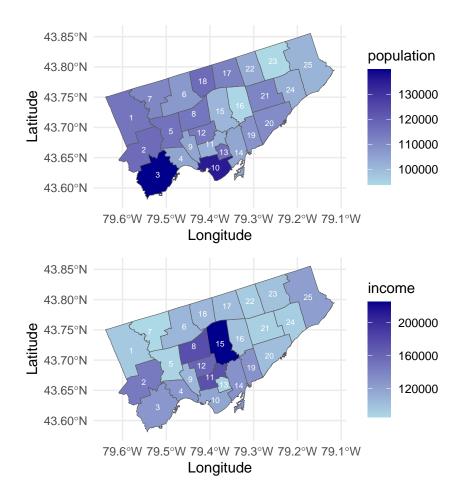


Figure 2: Map of Toronto highlighting the population and income densities by ward

2.4 Building Permits - Active Permits

The Building Permits - Active Permits dataset (City of Toronto 2024a), published by the City Planning Division and last updated on November 28, 2024, serves as an important record

of active building permits in Toronto. A building permit is a municipally issued document, mandated by the Building Code Act and enforced by the City of Toronto, regulating the construction or demolition of physical structures (City of Toronto 2024a).

The process of obtaining a building permit involves submitting an application to the City of Toronto, including necessary drawings, documents, and other forms based on the permit type. The Building Division reviews the application, and a Toronto Building Inspector ensures compliance with the Ontario Building Code, Zoning By-law, and other applicable regulations. Once approved, the permit is issued, allowing the applicant to commence construction or demolition, and thus data is saved in the system as an active permit.

Table 3 outlines detailed information about active building permits in Toronto, including key features such as Permit Number, Permit Type, Structure Type, Status, and more.

Table 3: Sample of the raw building permits data

				Postal	
ID	Permit Type	Structure Type	Work	Code	Status
1	Non-Residential	Office	Addition to	M2R	Permit
	Building Permit		Existing Building		Issued
2	Residential	SFD - Semi-Detached	Addition to	M4L	Inspection
	Building Permit		Existing Building		
3	Residential	Multiple Unit Building	Alteration to	M6R	Inspection
	Building Permit		Existing Building		
4	Residential	HVAC Alt. Boiler/Furn	HVAC	M6K	Inspection
	Building Permit	Rplmt. or A/C			
5	Mechanical(MS)	HVAC Alt. add on Sys.	Install/Alter	M6H	Inspection
	, ,	or Ductwork Alt.	HVAC - only		
6	Mechanical(MS)	Office	Install/Alter	M5C	Inspection
	,		HVAC - only		_

We selected this data-set to evaluate how our confounders, population and income, influence construction activity, and mediator, budget allocation, correlate with the number of building permits issued in each ward. The number of permits serves as a proxy for construction activity and development, highlighting the demand for infrastructure investment and capital expenditures. By examining the relationship between building permits and outlined variables, we can understand how construction activity influences resource distribution across the city's wards.

From the raw data, we selected key variables of interest: Postal Code, Status, and Work. The Postal Code was used to map building permits to their respective wards, while Status and Work were utilized to filter permits based on their current state and type of work. Table 7 lists 45 unique statuses assigned to each submitted permit. For this analysis, we focused on permits

with the following statuses: Approved, Application Accepted, Issuance Pending, Ready for Issuance, Permit Issued, and Permit Issued/Close File. These statuses indicate that the permit has been approved and that construction or demolition is either underway or completed.

The cleaned data was then saved in CSV and Parquet formats with the following columns:

- ward_id: Unique identifier for each ward.
- total_building_permits: Total number of building permits issued in each ward.

Figure 3 illustrates the total number of building permits by ward, providing understanding into construction activity and development patterns across Toronto's wards.

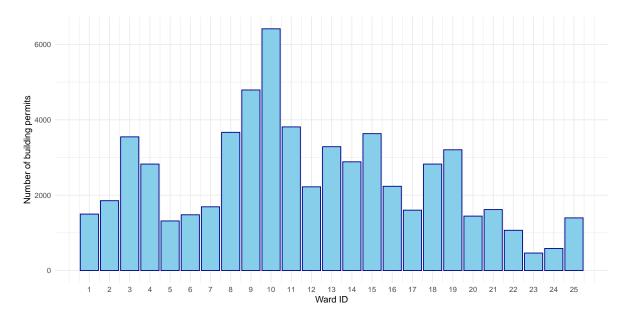


Figure 3: Total number of building permits by Ward

2.5 Trends in Budget Allocations (2021-2024)

The box plots in Figure 4 illustrate the trends in budget allocations across three categories—Growth Related, State of Good Repair, and Service Improvement and Enhancement—from 2021 to 2024. Each box plot represents the distribution of budget allocations for each year, with the median value indicated by the horizontal line inside the box. Outliers are labeled with the corresponding ward ID, highlighting wards with unusually high or low budget allocations.

Ward 10 (Spadina-Fort York) received the highest budget allocations across both *Growth Related* and *State of Good Repair* categories, indicating significant investment in infrastructure

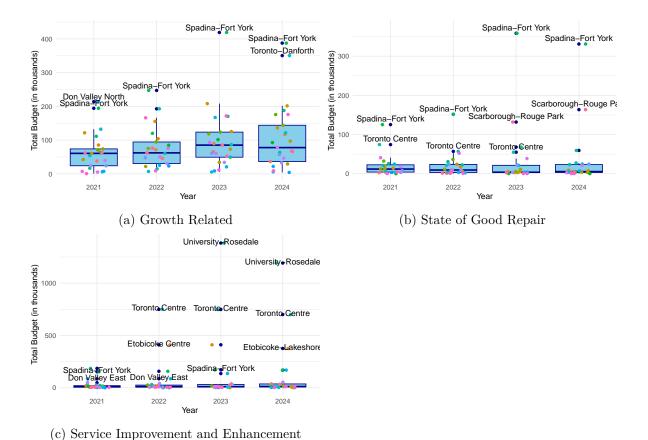


Figure 4: Trends in budget allocations (2021-2024) by category

development and maintenance to population-dense areas. Toronto Center (Ward 13), Don Valley East (Ward 16), and Etobicoke Center (Ward 2) also received notable budget allocations, some of these wards have higher average household incomes as well as higher population densities. The box plots presents that budget allocations for *Growth Related* projects have increased steadily over the years, with 75% of wards receiving higher allocations in 2024 compared to 2021. In contrast, budget allocations for *State of Good Repair* and *Service Improvement and Enhancement* projects have remained relatively consistent, with few outliers receiving higher budget allocations.

The box plots for *State of Good Repair* and *Service Improvement and Enhancement* projects however, are less varied as most of the wards received similar budget allocations across the years, with few outliers such as University-Rosedale, Toronto Centre and Don Valley West receiving higher budget allocations, who coincidentally have higher average household income.

2.6 Relationship between Variables of Interest and Budget Allocations

Our budget data spans three categories—Growth Related, State of Good Repair, and Service Improvement and Enhancement—for the years 2021-2024. As observed in Section 2.5, there has been a steady increase in budget allocations across these categories. To better understand the relationship between these budget categories and our variables of interest, we calculate the average budget allocation for each category across the years. The results are presented in Table 4.

Ward		Growth	State of Good	Service Improvement and
ID	Ward Name	Related	Repair	Enhancement
1	Etobicoke North	46497.25	2565.643	7279.627
2	Etobicoke	86651.25	5546.250	126011.750
	Centre			
3	Etobicoke-	112789.98	9572.525	205245.100
	Lakeshore			
4	Parkdale-High	171717.25	8373.225	7211.932
	Park			
5	York	73226.12	12362.250	11403.250
	South-Weston			
6	York Centre	31927.25	10725.475	3865.750

Table 4: Average 10-year budget allocations by category (2021-24)

2.6.1 Relationship between Confounders and Budget Allocations (Service Improvement and Enhancement)

Figure 5 illustrates the relationship between average household income, population, and the total budget allocation each year (2021-2024) for *Service Improvement and Enhancement* projects. These projects aim to enhance the quality of services provided to residents and improve the overall infrastructure of the city (City of Toronto 2018).

The linear regression lines for average household income and population shows a positive correlation with budget allocation for Service Improvement and Enhancement projects. Wards with higher average household incomes, such as Ward 11 (University-Rosedale) receive a larger share of the budget allocation for these projects, while wards with higher population densities, such as Ward 10 (Spadina-Fort York) and Ward 3 (Etobicoke-Lakeshore), also receive a proportionally larger share of the funds. This suggests that both income levels and population density play a significant role in determining funding levels for Service Improvement and Enhancement projects, with higher-income and more populous wards benefiting from increased allocations.

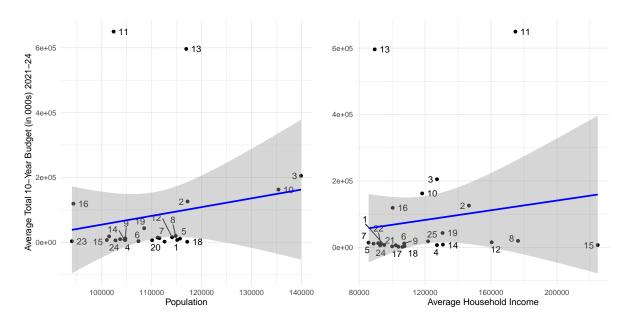


Figure 5: Service Improvement and Enhancement Budget by Ward

Other wards like Ward 15 which has the highest average household income, but is one of least populous wards, receives a lower budget allocation for Service Improvement and Enhancement projects, indicating that population density may be a more significant factor in determining funding levels than income levels.

Despite these outliers, the majority of wards received similar budget allocations for Service Improvement and Enhancement projects, underscoring a city-wide strategy to enhance services uniformly for all residents.

2.6.2 Relationship between Confounders and Budget Allocations (Growth-Related and State of Good Repair)

Figure 6a) illustrates the relationship between average household income, population, and the total budget allocation for *Growth-Related projects*. The linear regression line for average household income remains relatively flat, hovering around \$100,000. This suggests that budget allocations for Growth-Related projects are not significantly influenced by income levels, indicating a more uniform distribution of funds across wards regardless of household income. A similar lack of correlation is observed in Figure 6b), where budget allocations for State of Good Repair projects also show minimal dependence on average household income.

In contrast, the linear regression line for population shows a strong positive correlation with budget allocation for Growth-Related projects. Wards with higher population densities—such as Ward 10 (Spadina-Fort York) and Ward 3 (Toronto Centre)—receive a larger share of

the Growth-Related budget. This indicates that population density plays an important role in determining funding levels for these projects, with more populous wards benefiting from increased allocations. A similar trend is observed in the budget distribution for State of Good Repair projects, where wards with higher population densities receive a proportionally larger share of the funds.

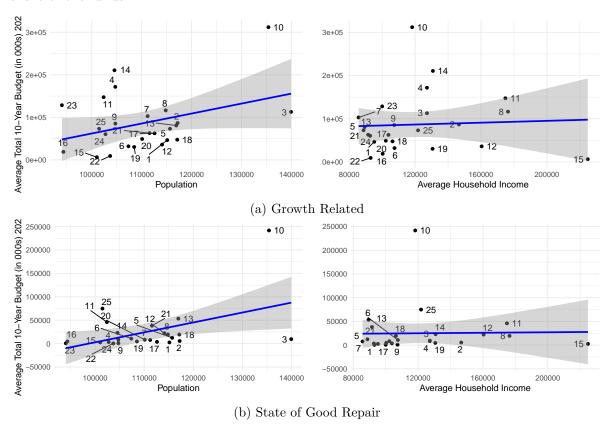


Figure 6: Growth and State of Good Repair Budget by Ward

3 Model

The purpose of this paper is to investigate the relationship between population density, average household income, and budget allocations across Toronto's 25 wards, and their potential impact on the economic well-being of each ward, as represented by the total_building_permits issued, a indicator of infrastructure development. To achieve this, we will fit a Bayesian regression model with varying intercepts to estimate the effect of these variables on the number of building permits issued in each ward.

3.1 Model set-up

The particular model we used is Bayesian multiple linear regression model with varying intercepts. The model includes the following variables:

$$\begin{split} y_i | \mu_i, \sigma &\sim \text{Normal}(\mu_i, \sigma) \\ \mu_i &= \beta_0 + \beta_1 x_{\text{income}} + \beta_2 x_{\text{budget}} + \gamma_i \\ \beta_0 &\sim \text{Normal}(0, 2.5) \\ \beta_1 &\sim \text{Normal}(0, 2.5) \\ \beta_2 &\sim \text{Normal}(0, 2.5) \\ \gamma_i &\sim \text{Normal}(0, 2.5) \\ \sigma &\sim \text{Exponential}(1) \end{split}$$

In the above model:

- μ_i is the expected number of building permits issued in ward i.
- β_0 is the intercept, representing the expected number of building permits issued in a ward with average values for all other variables.
- β_1 is the coefficient for the predicted change in the number of building permits issued in a ward given a one unit increase in the average household income of the ward.
- β_2 is the coefficient for the predicted change in the number of building permits issued in a ward given a one unit increase in the total budget allocation across three categories: Growth Related, State of Good Repair, and Service Improvement and Enhancement.

The model also includes a varying intercept γ_i for each ward, accounting for the unobserved heterogeneity between wards. The varying intercepts allow the model to capture the unique characteristics of each ward that may influence the number of building permits issued.

The model was fitted using the stan_glmer function from the rstanarm package (Brilleman et al. 2018) in R (R Core Team 2024) and modelsummary (Arel-Bundock 2022) for model summary tables. The prior distributions for the coefficients were set to normal distributions with a mean of 0 and a standard deviation of 2.5. The model also included a prior for the intercept, which was set to a normal distribution with a mean of 0 and a standard deviation of 2.5. The standard deviation of the likelihood was set to an exponential distribution with a rate parameter of 1.

3.2 Model justification

Table 5: Mean, Median, and Standard Deviation of Each Variable

Variable	Mean	Median	Standard Deviation
Population	110451.60	110095.0	10593.872
Average Household Income	120096.00	107300.0	33980.638
Total Budget	194355.34	113992.8	226896.460
Total Building Permits	2454.28	2221.0	1382.892

To ensure model stability and interpretability, we standardized predictor variables (population density, average household income, and budget allocations) by subtracting their means and dividing by their standard deviations, as detailed in Table 5. This step addressed differences in scale and prevented numerical instability during Bayesian multiple linear regression modeling.

The Bayesian multiple linear regression model was selected because the outcome variable—building permits—is continuous rather than count-based, making Poisson or negative binomial models unsuitable. The chosen predictors reflect demographic, economic, and infrastructural factors known to influence construction activity. Population density and average household income represent key socioeconomic indicators, while budget allocations for Growth-Related, State of Good Repair, and Service Improvement projects drive infrastructure investments.

During causal analysis, population density exhibited unexpected exclusion restriction characteristics, showing a negative relationship with building permits. To enhance interpretability, population density was excluded from the model, leaving average household income and budget allocations as the primary predictors. The refitted model focuses on understanding how economic and infrastructural factors shape construction activity.

4 Results

In this section, we visualize the relationships between population density, average household income, budget allocations with total number of building permits across Toronto's 25 wards. Additionally, we present our model results, highlighting how these variables influence the number of building permits issued in each ward.

4.1 Distribution of Average Household Income and Population Density

The City of Toronto is divided into 25 wards, and the 2021 census data highlights significant disparities in population and average household income among them. As shown in Figure 2,

Spadina-Fort York (Ward 10) and Etobicoke-Lakeshore (Ward 3) have the highest population densities, with 135,400 and 139,920 residents, respectively. In contrast, Don Valley West (Ward 15) has a lower population density of 101,025 but boasts the highest average household income at \$224,800.

Population distribution presents a concentration in the western part of the city and downtown areas. Notably, wards like Etobicoke Centre (Ward 2) and Etobicoke-Lakeshore (Ward 3), situated farther from downtown, have lower costs of living and correspondingly lower average household incomes, such as Etobicoke North (Ward 2) with \$95,200.

An interesting pattern emerges around Don Valley West (Ward 15), which has the highest average household income. Wards such as University-Rosedale (Ward 11), Toronto-St. Paul's (Ward 12), and Eglinton-Lawrence (Ward 8) are clustered together, indicating a geographical correlation among high-income areas. Conversely, the wards with the highest population densities do not overlap with those that have the highest average household incomes, highlighting distinct socioeconomic patterns within the city.

4.2 Relationship between Confounders, Mediators and Budget Allocations

We now examine the results of independent comparisons between the outcome variable (total number of building permits in Toronto's 25 wards) and the predictor variables: population density, average household income, and budget allocations for Growth-Related, State of Good Repair, and Service Improvement and Enhancement projects. As illustrated in Figure 7, most predictor variables demonstrate a strong positive correlation with the number of building permits, suggesting that higher population density, average household income, and budget allocations are generally associated with increased construction activity and urban development.

However, the role of population density presents a different narrative. Although Section 2.6 revealed a positive correlation between population density and building permits, a counterintuitive negative relationship emerged within the model, leading to its exclusion. This anomaly is largely explained by the influence of Ward 10 (Spadina-Fort York) and Ward 3 (Etobicoke-Lakeshore), which consistently exhibited high population densities, substantial budget allocations, and elevated building permit counts.

When these two wards are excluded, a clearer pattern emerges, Wards 8 (Eglinton-Lawrence), 11 (University-Rosedale), 2 (Etobicoke Centre), and 15 (Don Valley West) dominate in terms of building permits, average household income, and budget allocations. These findings suggest that, while population density plays a role in shaping construction activity, its effects are overshadowed by the more direct influence of income levels and budget distribution, warranting its exclusion to reduce model distortion and improve interpretability.

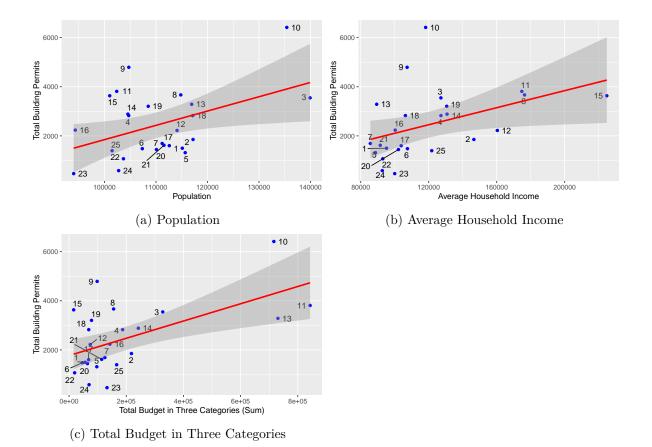


Figure 7: Relationship between Variables and Total Building Permits

4.3 Model Results

The Bayesian regression model results, summarized in Table 6, provide understanding into the relationship between budget allocations, average household income, and building permits across Toronto's wards. The model explains 59.1% of the variance in building permits, with significant positive coefficients for total budget (0.525) and average household income (0.365). This indicates that wards with higher budgets and income levels are more likely to experience construction activity.

Ward-specific random effects shows the influence of unobserved, ward-specific factors on permit issuance, while the adjusted (R^2) of 0.359 suggests moderate explanatory power after accounting for predictor complexity. With an RMSE of 0.57, the model achieves reasonable predictive accuracy.

While the assumption of linearity and additive effects simplifies the analysis, it may overlook variable interactions. The exclusion of population density, due to its counterintuitive negative relationship, reflects a trade-off between clarity and capturing complex dynamics. Despite

Table 6: Model Results

	Model
(Intercept)	-0.009
total_budget	0.525
$average_household_income$	0.365
$Sigma[ward_id \times (Intercept), (Intercept)]$	0.144
Num.Obs.	25
R2	0.594
R2 Adj.	0.359
R2 Marg.	0.459
Log.Lik.	-22.941
ELPD	-31.3
ELPD s.e.	5.0
LOOIC	62.6
LOOIC s.e.	10.0
WAIC	60.6
RMSE	0.57
r2.adjusted.marginal	0.359100614152714

these limitations, the findings highlight the critical role of economic resources—both income and budget—in driving urban development, emphasizing the need for equitable resource allocation in shaping infrastructure growth.

5 Discussion

In this section, we discuss the implications of our findings on urban development, economic well-being, and resource distribution in Toronto. We explore the role of budget allocations, average household income, and population density in shaping construction activity and infrastructure development across the city's 25 wards. Our analysis highlights the complex interplay between economic factors, demographic trends, and policy decisions, shedding light on the challenges and opportunities for equitable urban growth in Toronto.

5.1 Building Permits and Economic Well-Being

Construction plays a pivotal role in the economy, driving both job creation and economic growth (Building (CIOB) and Green 2023). One of the key indicators of construction activity is the number of building permits issued within a ward. Increased construction correlates with job opportunities, infrastructure development, and overall community well-being. For example, investment in residential and non-residential construction rose from 24.9% in 2021 to 29.5% in 2023, with projections indicating a further 1.5% increase in construction employment by 2024 (Canada and Development 2024).

As highlighted in Section 4.3 Bayesian regression model shows that average household income has a significant positive effect on the issuance of building permits. This suggests that construction activity tends to concentrate in higher-income areas, where demand for development is stronger. This finding underscores the role of income levels in driving construction and infrastructure development, emphasizing the need for targeted investments in lower-income areas to stimulate economic growth and enhance community well-being.

For potential property investors in Toronto, these understanding offer a strategic advantage. Investing in areas with higher average household incomes may be more profitable due to the increased likelihood of ongoing construction activity, which can drive property value appreciation and strengthen the local economy. While high-population-density areas are typically attractive for investment, our findings suggest that this may not always be the case.

5.2 Investing in Higher-Income Areas vs. High-Density Areas

The interplay between population density, average household income, and infrastructure investment in Toronto highlights a complex challenge in achieving equitable resource distribution. As seen in Section 2.6 high-income areas often attract more construction activity, driven by market forces and residents' ability to finance new developments. Whereas, only specific high-density areas like Ward 10 (Spadina-Fort York) and Ward 13 (Toronto Centre) receive substantial investment despite high population density, justifying the reason for population density exclusion in the model. Meanwhile, as discussed in Section 4.1, low-density and lower-income wards risk being underserved.

These findings underscore the importance of equity-based budgeting, where low-density and lower-income areas should receive targeted investments to meet infrastructure needs. This approach aligns with urban development strategies that prioritize inclusivity. Notable examples include transit expansions such as the Ontario Line and Crosstown extensions (Navabi 2024). The Ontario Line is expected to connect high-density areas like Ward 10 (Spadina-Fort York) and Ward 13 (Toronto Centre) to the broader transit network, which could stimulate further development and infrastructure investment in these wards, fostering a more balanced urban landscape and distributing population growth more evenly across the city.

For future policy, Toronto could enhance equity by expanding initiatives such as eliminating parking minimums. This policy reduces construction costs, making development in high-density areas more feasible. Such measures would promote a more balanced and sustainable urban environment, ensuring that population growth is accompanied by appropriate infrastructure investments.

5.3 Budget Allocations and Construction Activity

Our analysis shows a complex relationship between budget allocations and construction activity in Toronto's 25 wards. As discussed in Section 2.5 there has been a steady increases in budget allocations for key initiatives such as Growth-Related, State of Good Repair, and Service Improvement and Enhancement projects from 2021 to 2024, the distribution of building permits shows only a good correlation with these allocations Section 4.3. This finding suggests that budget allocations alone may not be the sole driver of construction activity, as other factors like market conditions, regulatory frameworks, and community priorities also play a significant role.

This discrepancy reflects broader challenges highlighted in Toronto's recent 10-year economic plan (Freeman 2024), which aims to tackle pressing issues such as housing, inequality, and congestion. The plan emphasizes the need for strategic investments that go beyond conventional infrastructure spending. For example, the city has committed \$35 million to cultural initiatives over the next decade, signaling a shift toward holistic urban development that prioritizes cultural and social well-being alongside physical infrastructure improvements. This shift may explain the weak correlation between budget allocations and building permits, as construction activity is influenced by a broader range of factors beyond traditional infrastructure spending.

Moreover, the Ford government's fall economic statement indicates a shrinking provincial deficit, suggesting a cautious fiscal environment that may limit how budgetary increases translate into tangible construction outputs ("2024 Fall Economic Statement" 2024). These dynamics suggest that other factors, such as regulatory frameworks, market conditions, or demographic shifts, may be playing a more significant role than budgetary allocations alone in shaping Toronto's construction landscape.

6 Weaknesses and Future Work

This analysis has several limitations that warrant consideration. As discussed in Section 2, the datasets used, sourced from the City of Toronto, presents city's demographics, budget allocations, and building permits. However, they may not fully capture the complexity of Toronto's infrastructure development and resource distribution.

For instance, in Section 2.4, all building *Work Types* were included in the analysis, which may not accurately represent construction activity in each ward. Many recorded work types, such as renovations, demolitions, and minor repairs (e.g., HVAC installations or pipework), are not indicative of significant construction projects. Future research could refine the analysis by focusing on specific types of construction projects to better reflect actual development activity.

Additionally, as noted in Section A, there are 45 unique statuses assigned to building permits, but this study analyzed only a subset of these statuses. This narrow focus may overlook important stages in the construction process. Expanding the analysis to include more permit statuses could offer a more in-depth understanding of construction activity.

Another limitation is the lack of detailed data on specific projects within each budget category, which restricts the paper's analysis into why certain wards receive more or less funding. Access to granular project-level data could provide deeper context and explanations for funding disparities.

Moreover, the analysis assumes linear relationships between population density, average household income, and budget allocations, which may oversimplify the underlying dynamics. Developing more complex models that account for non-linear relationships and interactions could yield a richer understanding of factors influencing construction activity.

Finally, the analysis assumes independence among wards, an assumption that may not hold true given shared infrastructure and resource dependencies. Future studies could incorporate spatial or network-based models to address interdependencies between wards.

6.1 Future Work

This analysis provides a foundation for future research on infrastructure development, resource distribution, and economic well-being in Toronto. Future studies could explore additional factors that influence budget allocations and building permit issuance, such as infrastructure needs, community priorities, and political considerations. By incorporating these variables into the analysis, researchers can gain a more in-depth understanding of how municipal budgets are allocated and how construction activity is distributed across the city's wards.

In terms of policy recommendations, the city should adopt equity-based budgeting to ensure underfunded, high-density wards receive adequate resources, particularly for essential services like health and safety. Toronto could also implement a baseline funding model for high-need areas and enhance public engagement in the budget process, ensuring that residents of under served wards have a voice in resource allocation. These actions would promote more transparent, balanced, and equitable urban governance.

A Appendix

The relationship between income levels, population density, and construction outcomes reflects complex interactions shaped by diverse socioeconomic and regional factors. Existing datasets, such as the NHS survey, provide a starting point but do not fully capture these dynamics. To address this, a well-structured survey methodology is outlined to ensure greater representativeness and reliability.

A.1 Survey Design for Construction Analysis

The survey seeks to understand how income levels influence construction investments, access to resources, regulatory challenges, and housing quality across geographic regions. This allows for a detailed assessment of regional and economic differences in construction outcomes.

A.2 Sampling Methodology

The proposed design prioritizes representativeness through the following methods:

- Stratified Sampling: Groups are categorized by income levels and ward classifications (high-income, populated, and etc.) to ensure diverse representation.
- Random Sampling Within Strata: This approach minimizes selection bias, ensuring participants across income groups are adequately represented.

A.3 Ensuring Robust Data Collection

- Sampling Bias: Using stratified random sampling ensures inclusion of marginalized groups, particularly those in remote wards or lower income brackets, often underrepresented in traditional data sources.
- Non-Response Bias: Offering multiple delivery modes—such as online forms, mailed surveys, and in-person interviews—accommodates varying levels of accessibility. To encourage participation, incentives like gift cards or small monetary rewards can be provided.
- Question Design: Survey questions must be neutrally worded to avoid influencing responses. Pilot testing and iterative feedback from participants will refine question clarity and relevance.

- Human-Centric Approach: Present the survey as an opportunity for participants to share their experiences and shape future construction planning.
- Visual Enhancements: Include infographics or interactive components to make participation more engaging and relatable.
- Validation Through Multiple Sources: To strengthen findings, the survey data should be cross-referenced with secondary sources, such as municipal reports, and supplemented with qualitative interviews where necessary.

This approach ensures a structured methodology that balances statistical rigor with participant-focused design, allowing for a meaningful exploration of how socioeconomic factors influence construction outcomes across regions.

A.4 Building Permits Status

Table 7: Building permit statuses

CIT	$\Gamma \Lambda$	\mathbf{T}	r	r
· O	I /		u	

Permit Issued

Inspection

Application Withdrawn

Revised

Pending Cancellation

Application Received

Revision Issued

Order Complied

Revocation Pending

Rescheduled

Examiner's Notice Sent

Issuance Pending

Inspection Request to Cancel

Under Review

Plan Review Complete

Not Accepted

Permit Issued/Close File

Ready for Issuance

Work Suspended

Abandoned

File Closed

VIOLATION Work Not Started Not Started Order Issued

Response Received Refusal Notice Forwarded for Issuance Application On Hold Application Acceptable

Follow-up Required Consultation Completed Extension Granted Request Received Active

Deficiency Notice Issued Refused Approved Agreement in Progress NA

Open Application Accepted Permit Revoked Forward to Inspector Revoked

A.5 Model Details

A.6 Posterior Predictive Check

We employ a posterior predictive check in Figure 8 to evaluate how well the model fits the data. By examining the distribution of the observed data against the simulated data, we can assess the model's predictive accuracy and identify any discrepancies. (Alexander 2024).

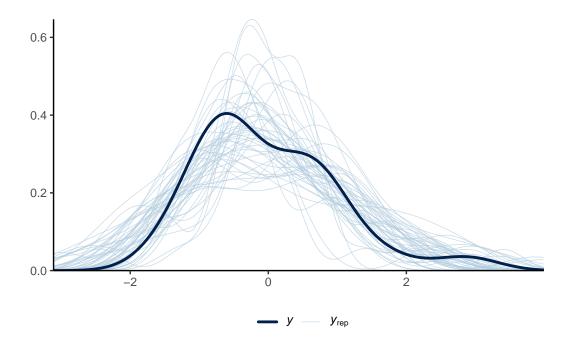


Figure 8: Examining how the model fits the data through a posterior predictive check

A.7 Comparison of the Posterior and Prior

We compare the posterior and prior in Figure 9 to examine how the estimates change once data is taken into account (Alexander 2024).

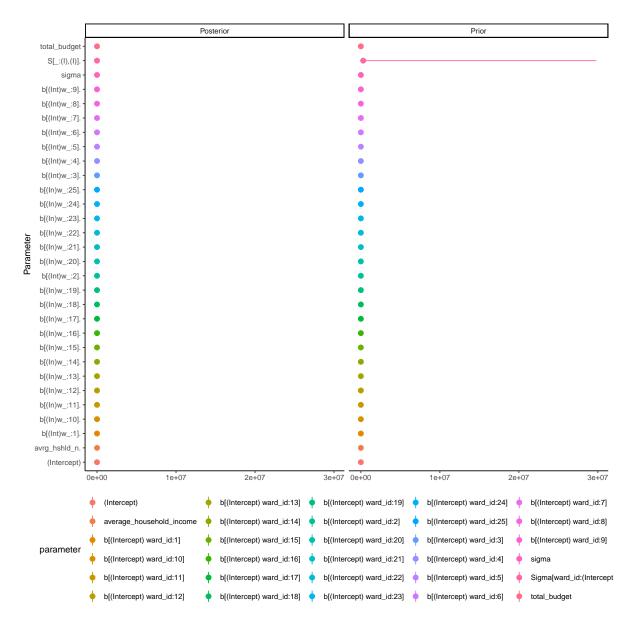


Figure 9: Examining how the model is affected by the data through a posterior-prior comparison

A.8 Markov Chain Monte Carlo Convergence

Since rstanarm uses the MCMC sampling algorithm (Alexander 2024), we assess whether the algorithm encountered any issues by reviewing the Rhat and trace plots, as shown in Figure 10. The Rhat plot shows no concerns, with values consistently close to 1, indicating that the

algorithm converged properly (Alexander 2024). Additionally, the trace plot appears normal, as the lines remain horizontal and fluctuate as expected, further supporting the adequacy of the sampling process (Alexander 2024).

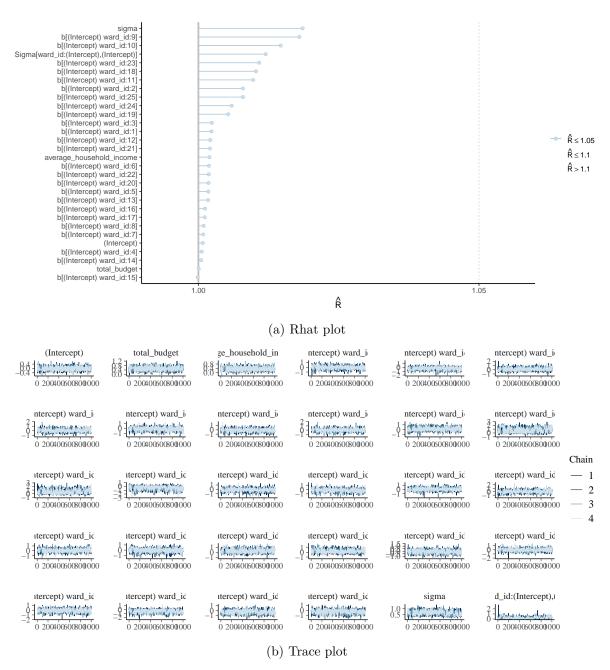


Figure 10: Checking the convergence of the MCMC algorithm

A.9 Credibility Intervals

Lastly, we employ a 95% credibility interval as showcased in Figure 11, to gain a better understanding of the probability distribution of our coefficients.

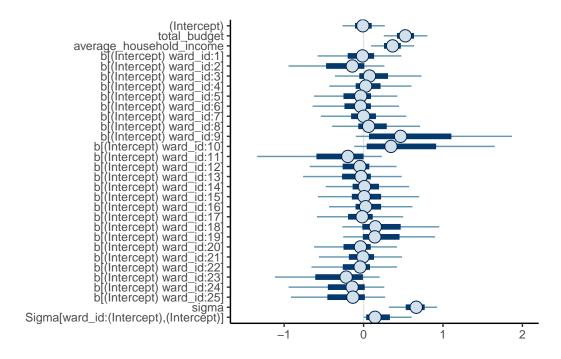


Figure 11: Credible intervals

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