Problem Statement 1:

In each of the following situations, state whether it is a correctly stated hypothesis testing problem and why?

1.
$$H$$
0: μ = **25**, H **1**: $\mu \neq$ **25**

2. *H***0**:
$$\sigma$$
 > **10**, *H***1**: σ = **10**

3.
$$H$$
0: x **= 50,** H **1:** x **≠ 50**

4.
$$H$$
0: p **= 0.1**, H **1:** p **= 0.5**

5.
$$H$$
0: S **= 30,** H **1:** S **> 30**

- 1. Yes, because values in both are statement about population or distribution, have equal values and has inequality in ull hypothesis.
- 2. No, because null hypothesis has an eqaulity claim and alternate hypothesis has inequality.
- 3. No, because hypothesis is stated in terms of statistics and not sample data 4. No, because values in both hypothesis is different and has equal sign.
- 4. No, because hypothesis are always statements about population or distribution and not about sample

Problem Statement 2:

The college bookstore tells prospective students that the average cost of its textbooks is Rs. 52 with a standard deviation of Rs. 4.50. A group of smart statistics students thinks that the average cost is higher. To test the bookstore's claim against their alternative, the students will select a random sample of size 100. Assume that the mean from their random sample is Rs. 52.80. Perform a hypothesis test at the 5% level of significance and state your decision.

```
In [1]:
    from scipy.stats import norm
    import numpy as np
    import scipy.stats as stats
    from scipy.stats import chi2_contingency

    p_mean = 52
    p_std = 4.50
    n = 100
    sample_mean = 52.80

SE = p_std/n**0.5
    Z = (sample_mean-p_mean)/SE
    print(f"Z score is:{Z}")
    alpha=0.05  #test_significance
    print(f"Critical region is {norm.ppf(alpha/2)}, {-norm.ppf(alpha/2)}")

Z score is:1.77777777777775
```

Z score is:1.777777777777715 Critical region is -1.9599639845400545, 1.9599639845400545

* From above we can conclude we can accept null hypothesis since z_score<critical region

Problem Statement 3:

A certain chemical pollutant in the Genesee River has been constant for several years with mean μ = 34 ppm (parts per million) and standard deviation σ = 8 ppm. A group of factory representatives whose companies discharge liquids into the river is now claiming that they have lowered the average with improved filtration devices. A group of environmentalists will test to see if this is true at the 1% level of significance. Assume \ that their sample of size 50 gives a mean of 32.5 ppm. Perform a hypothesis test at the 1% level of significance and state your decision.

```
In [2]: p_mean = 34
p_std = 8
n = 50
sample_mean = 32.5

SE = p_std/n**0.5  #standard Error
Z = (sample_mean-p_mean)/SE
print(f"Z score is:{Z}")
alpha=0.01
print(f"Critical region is {norm.ppf(alpha/2)}, {-norm.ppf(alpha/2)}")

Z score is:-1.3258252147247767
Critical region is -2.575829303548901, 2.575829303548901
```

* From above we can conclude we can accept null hypothesis since critical_region<Z_score

Problem Statement 4:

Based on population figures and other general information on the U.S. population, suppose it has been estimated that, on average, a family of four in the U.S. spends about \$1135 annually on dental expenditures. Suppose further that a regional dental association wants to test to determine if this figure is accurate for their area of country. To test this, 22 families of 4 are randomly selected from the population in that area of the country and a log is kept of the family's dental expenditure for one year. The resulting data are given below. Assuming, that dental expenditure is normally distributed in the population, use the data and an alpha of 0.5 to test the dental association's hypothesis.

• 1008, 812, 1117, 1323, 1308, 1415, 831, 1021, 1287, 851, 930, 730, 699, 872, 913, 944, 954, 987, 1695, 995, 1003, 994

```
In [3]: given_data=[1008, 812, 1117, 1323, 1308, 1415, 831, 1021, 1287, 851, 930, 730, 69
p_mean =1135
sample_std = np.std(given_data)
n=22
sample_mean = np.sum(given_data,axis=0)/len(given_data)
SE = sample_std/n**0.5
alpha = 0.5
test_1 = (sample_mean-p_mean)/SE
print(f"t_Score is{test_1}")
print(f"Critical Region is {stats.t.ppf((alpha/2),df=21)} {stats.t.ppf(1-(alpha/2),df=21)}

**T_Score is-2.070747228595759
Critical Region is -0.6863519891164291 0.6863519891164291
```

* We reject null hypothesis alpha=0.5 since it lies within critical region

Problem Statement 5:

In a report prepared by the Economic Research Department of a major bank the Department manager maintains that the average annual family income on Metropolis is 48432.

What do you conclude about the validity of the report if a random sample of 400 families shows and average income of 48,574 with a standard deviation of 2000?

Critical region is -1.9599639845400545 1.9599639845400545

*We accept null hypothesis at alpha=0.05 since z_score<critical_region

Problem Statement 6:

Suppose that in past years the average price per square foot for warehouses in the United States has been 32.28. A national real estate investor wants to determine whether that figure has changed now. The investor hires a researcher who randomly samples 19 warehouses that are for sale across the United States and finds that the mean price per square foot is 31.67, with a standard deviation of 1.29. assume that the prices of warehouse footage are normally distributed in population. If the researcher uses a 5% level of significance, what statistical conclusion can be reached? What are the hypotheses?

```
In [5]: p_mean =32.28
n=19
sample_mean =31.67
sample_std =1.29
alpha =0.05

SE=sample_std/(n**0.5)
t=(sample_mean-p_mean)/SE
print(f"t_score is {round((t),1)}")
print(f"Critical region is {round(stats.t.ppf((alpha/2),df=18),1)} {-round(stats.t.ppf((alpha/2),df=18),1)} {-round(stats.t.ppf(calpha/2),df=18),1}
```

*we can reject null hypothesis at alpha=0.05 since it lies within critical region

Problem Statement 7:

Fill in the blank spaces in the table and draw your conclusions from it.

Acceptance region	Sample size	α	$\beta at \mu = 52$	$\beta at \mu = 50.5$
$48.5 < \bar{x} < 51.5$	10			
$48 < \bar{x} < 52$	10			
$48.81 < \bar{x} < 51.9$	16			
$48.42 < \bar{x} < 51.58$	16			

i) Acceptance region 48.5 < x < 51.5

```
In [6]: # Calculate Beta at Mu1 = 52
        n1 = 10
        Sig = 2.5
        Mu1 = 52
        p11 = (48.5 - Mu1)/(Sig/math.sqrt(n1))
        print(p11)
        p12 = (51.5 - Mu1)/(Sig/math.sqrt(n1))
        print(p12)
        # As p12 > p11, so our z score lies in between these two p12 < z < p11.
        # Find probability at these z score
        P11 = 0
        P12 = 0.2643
        # now Beta = p12 - p11
        Beta11 = P12 - P11
        print(f"Beta at Mu1 = 52 is : {Beta11}")
        -4.427188724235731
        -0.6324555320336759
        Beta at Mu1 = 52 is : 0.2643
In [7]: # Calculate Beta at Mu2 = 50.5
        n1 = 10
        Sig = 2.5
        Mu2 = 50.5
        p13 = (48.5 - Mu2)/(Sig/math.sqrt(n1))
        print(p13)
        p14 = (51.5 - Mu2)/(Sig/math.sqrt(n1))
        print(p14)
        # so our z score lies in between these two p13 < z < p14.
        # Find probability at these z score
        P13 = 0.0057
        P14 = 0.8962
        \# now Beta = p13 +(1 - p14)
        Beta12 = P13 +(1-P14)
        print(f"Beta at Mu2 = 50.5 is : {Beta12}")
        -2.5298221281347035
        1.2649110640673518
        Beta at Mu2 = 50.5 is : 0.1095
        ii) 48 < x < 51
```

```
In [8]: # Calculate Beta at Mu1 = 52
        n2 = 10
        Sig = 2.5
        Mu1 = 52
        p21 = (48.0 - Mu1)/(Sig/math.sqrt(n2))
        print(p21)
        p22 = (51.0 - Mu1)/(Sig/math.sqrt(n2))
        print(p22)
        # As p22 > p21, so our z score lies in between these two p22 < z < p21.
        # Find probability at these z score
        P21 = 0
        P22 = 0.1038
        # now Beta = p22 - p21
        Beta21 = P22 - P21
        print(f"Beta at Mu2 = 52 is : {Beta21}")
        -5.059644256269407
        -1.2649110640673518
        Beta at Mu2 = 52 is : 0.1038
In [9]: # Calculate Beta at Mu2 = 50.5
        n2 = 10
        Sig = 2.5
        Mu2 = 50.5
        p23 = (48 - Mu2)/(Sig/math.sqrt(n2))
        print(p23)
        p24 = (51 - Mu2)/(Sig/math.sqrt(n2))
        print(p24)
        # so our z score lies in between these two p13 < z < p14.
        # Find probability at these z score
        P23 = 0.0008
        P24 = 0.7357
        \# now Beta = p13 +(1 - p14)
        Beta22 = P23 + (1 - P24)
        print(f"Beta at Mu2 = 50.5 is : {Beta22}")
        -3.1622776601683795
        0.6324555320336759
        Beta at Mu2 = 50.5 is : 0.2651
        iii) 48.81 < x < 51.9
```

```
In [10]: |# Calculate Beta at Mu1 = 52
         n3 = 16
         Sig = 2.5
         Mu1 = 52
         p31 = (48.81 - Mu1)/(Sig/math.sqrt(n3))
         print(p31)
         p32 = (51.9 - Mu1)/(Sig/math.sqrt(n3))
         print(p32)
         # so our z score lies in between these two p31 < z < p32.
         # Find probability at these z score
         P31 = 0.4364
         P32 = 0
         # now Beta = p31 - p32
         Beta31 = P31 - P32
         print(f"Beta at Mu2 = 52 is : {Beta31}")
         -5.103999999999965
         -0.160000000000000228
         Beta at Mu2 = 52 is : 0.4364
In [11]: | # Calculate Beta at Mu2 = 50.5
         n3 = 16
         Sig = 2.5
         Mu2 = 50.5
         p33 = (48.81 - Mu2)/(Sig/math.sqrt(n3))
         print(p33)
         p34 = (51.9 - Mu2)/(Sig/math.sqrt(n3))
         print(p34)
         # so our z score lies in between these two p33 < z < 1- p34.
         # Find probability at these z score
         P33 = 0.0032
         P34 = 0.9875
         # now Beta = P33 + 1 - P34
         Beta32 = P33 +1 - P34
         print(f"Beta at Mu2 = 50.5 is : {Beta32}")
         -2.70399999999996
         2.239999999999975
         Beta at Mu2 = 50.5 is : 0.015700000000000047
         iv) 48.42 <x < 51.58
```

```
In [12]: # Calculate Beta at Mu1 = 52
         n4 = 16
         Sig = 2.5
         Mu1 = 52
         p41 = (48.42 - Mu1)/(Sig/math.sqrt(n4))
         print(p41)
         p42 = (51.58 - Mu1)/(Sig/math.sqrt(n4))
         print(p42)
         # As P42> P41, so our z score lies in between these two p42 < z < p41.
         # Find probability at these z score
         P41 = 0.0
         P42 = 0.2514
         # now Beta = p31 - p32
         Beta41 = P42 - P41
         print(f"Beta at Mu2 = 52 is : {Beta41}")
         -5.727999999999997
         -0.67200000000000027
         Beta at Mu2 = 52 is : 0.2514
In [13]: # Calculate Beta at Mu2 = 50.5
         n4 = 16
         Sig = 2.5
         Mu2 = 50.5
         p43 = (48.42 - Mu2)/(Sig/math.sqrt(n4))
         print(p33)
         p44 = (51.58 - Mu2)/(Sig/math.sqrt(n4))
         print(p34)
         # so our z score lies in between these two p33 < z < 1- p34.
         # Find probability at these z score
         P43 = 0.0035
         P44 = 0.9875
         # now Beta = P43 + 1- P44
         Beta42 = P43 + (1 - P44)
         print(f"Beta at Mu2 = 50.5 is : {Beta42}")
         -2.70399999999996
         2.239999999999975
         Beta at Mu2 = 50.5 is : 0.0159999999999955
```

Problem Statement 8:

Find the t-score for a sample size of 16 taken from a population with mean 10 when the sample mean is 12 and the sample standard deviation is 1.5.

```
In [14]: #t_score = ?
    n = 16
    p_mean = 10
    sample_mean =12
    sample_std =1.5

SE = sample_std/(n**0.5)
    t = (sample_mean-p_mean)/SE
    print(f"t_score is {round((t),1)}")
```

t_score is 5.3

Problem Statement 9:

Find the t-score below which we can expect 99% of sample means will fall if samples of size 16 are taken from a normally distributed population.

Problem Statement 10:

If a random sample of size 25 drawn from a normal population gives a mean of 60 and a standard deviation of 4, find the range of t-scores where we can expect to find the middle 95% of all sample means. Compute the probability that (-t0.05 < t < t0.10).

Problem Statement 11:

Two-tailed test for difference between two population means is there evidence to conclude that the number of people travelling from Bangalore to Chennai is different from the number of people travelling from Bangalore to Hosur in a week, given the following:

Population 1:--- Bangalore to Chennai

```
n1 = 1200
x1 = 452
s1 = 212
```

• Population 2:---- Bangalore to Hosur

```
n2 = 800
x2 = 523
s2 = 185
```

```
Z_Score is -7.926428526759299
Critical region is -1.9599639845400545 1.9599639845400545
```

*We reject null hypothesis since it lies within critical region at alpha=5%.So,number of people travelling from Bangalore to Chennai is different from the number of people travelling from Bangalore to Hosur in a week

Problem Statement 12:

Is there evidence to conclude that the number of people preferring Duracell battery is different from the number of people preferring Energizer battery, given the following:

Population 1:---- Duracell

```
n1 = 100
x1 = 308
s1 = 84
```

• Population 2:---- Energizer

```
n2 = 100
x2 = 254
s2 = 67
```

```
Z_Score is 5.025702668336442
Critical region is -1.9599639845400545 1.9599639845400545
```

*We reject null hypothesis since it lies within critical region at alpha=5%.So, number of people preferring Duracell battery is different from the number of people preferring Energizer battery

Problem Statement 13:

Pooled estimate of the population variance Does the data provide sufficient evidence to conclude that average percentage increase in the price of sugar differs when it is sold at two different prices?

• ---Population 1: -----

```
Price of sugar=Rs. 27.50
n1 = 14
x1 = 0.317%
s1 = 0.12%
```

-----Population 2: ------

```
Price of sugar=Rs. 20.00
n2 = 9
x2 = 0.21%
s2 = 0.11%
```

T_score is 0.3931089218182991 Critical Region is 1.7207429028118775

*We accept null hypothesis at alpha=5%.So,average price do not increase

Problem Statement 14:

The manufacturers of compact disk players want to test whether a small price reduction is enough to increase sales of their product. Is there evidence that the small price reduction is enough to increase sales of compact disk players?

· Population 1: Before reductionli>

```
n1 = 15
x1 = Rs. 6598
s1 = Rs. 844
```

· Population 2: After reduction

```
n2 = 12
x2 = RS. 6870
s2 = Rs. 669
```

T_score is -0.1364745051598569 Critical Region is -1.708140761251899

*We accept null hypothesis at alpha=5%. So average price remains same

Problem Statement 15:

Comparisons of two population proportions when the hypothesized difference is zero Carry out a two-tailed test of the equality of banks' share of the car loan market in 1980 and 1995.

• Population 1: 1980

```
n1 = 1000

x1 = 53

p = 0.53
```

• Population 2: 1985

```
n2 = 100

x2 = 43

p = 0.53
```

```
Z_score is 0.0
Critical region is -1.6448536269514729
```

*We can't reject null hypothesis at alpha=10%

Problem Statement 16:

Carry out a one-tailed test to determine whether the population proportion of traveler's check buyers who buy at least \$2500 in checks when sweepstakes prizes are offered as at least 10% higher than the proportion of such buyers when no sweepstakes are on.

· Population 1: With sweepstakes

```
n1 = 300

x1 = 120

p = 0.40
```

· Population 2: No sweepstakes

```
n2 = 700

x2 = 140

p = 0.20
```

Z_score is 3.303749523611152 Critical region is 1.6448536269514729

*We reject null hypothesis at alpha=5%

Problem Statement 17:

A die is thrown 132 times with the following results:

Number turned up: 1, 2, 3, 4, 5, 6 Frequency: 16, 20, 25, 14, 29, 28

Is the die unbiased? Consider the degrees of freedom as p – 1.

```
In [24]: f_obs= [16, 20, 25, 14, 29, 28]
    f_exp= [22,22,22,22,22]
    result=stats.chisquare(f_obs,f_exp)
    print(f"Chi square value is {result[0]} and p-value is {result[1]}")
    print('Dias is unbiased.')
```

Chi square value is 9.0 and p-value is 0.1090641579497725 Dias is unbiased.

Problem Statement 18: ¶

In a certain town, there are about one million eligible voters. A simple random sample of 10,000 eligible voters was chosen to study the relationship between gender and participation in the last election. The results are summarized in the following 2X2 (read two by two) contingency table:

	Men	Women
Voted	2792	3591
Not voted	1486	2131

We would want to check whether being a man or a woman (columns) is independent of having voted in the last election (rows). In other words, is "gender and voting independent"?

```
In [25]: observed voted men=2792
         observed voted women=3591
         observed_not_voted_men=1486
         observed not voted women=2131
         total voted=2792+3591
         total not voted=1486+2131
         total men=2792+1486
         total women=3591+2131
         expected voted men=(total voted*total men)/10000
         expected voted women=(total voted*total women)/10000
         expected not voted men=(total not voted*total men)/10000
         expected not voted women=(total not voted*total women)/10000
         chisquare1=(((observed voted women-expected voted women)**2)/expected voted women
         chisquare2=(((observed voted men-expected voted men)**2)/expected voted men)
         chisquare3=(((observed not voted men-expected not voted men)**2)/expected not vot
         chisquare4=(((observed_not_voted_women-expected_not_voted_women)**2)/expected_not
         chisquare=chisquare1+chisquare2+chisquare3+chisquare4
         print(f"Chi Square value is {chisquare}")
         print(f"Critical region with alpha=0.05 is 3.84")
         print("We reject null hypothesis.It is not gender and voting independent")
```

Chi Square value is 6.660455899328067 Critical region with alpha=0.05 is 3.84 We reject null hypothesis.It is not gender and voting independent

Problem Statement 19:

A sample of 100 voters are asked which of four candidates they would vote for in an election. The number supporting each candidate is given below:

Higgins	Reardon	White	Charlton	
41	19	24	16	

Do the data suggest that all candidates are equally popular? [Chi-Square = 14.96,with 3 df, p 0.05 .]

We reject null hypothesis. All candidates are not equally popular

Problem Statement 20:

Children of three ages are asked to indicate their preference for three photographs of adults. Do the data suggest that there is a significant relationship between age and photograph preference? What is wrong with this study? [Chi-Square = 29.6, with 4 df: p < 0.05].

###		Photogra	Photograph		
		Α	В	С	
Age of child	5 – 6 years	18	22	20	
	7 – 8 years	2	28	40	
	9 – 10 years	20	10	40	

```
In [27]: obs=([[18,22,20],[2,28,40],[20,10,40]])
    result=chi2_contingency(obs)
    print(f"Chi Square value is {result[0]}")
    print(f"Critical region with 4df and alpha=0.001 is 18.47")
    print("We reject null hypothesis.There is significant relationship between age ar
```

Chi Square value is 29.603174603174608 Critical region with 4df and alpha=0.001 is 18.47 We reject null hypothesis. There is significant relationship between age and pho tograph preference

Problem Statement 21:

A study of conformity using the Asch paradigm involved two conditions: one where one confederate supported the true judgement and another where no confederate gave the correct response.

	Support	No support
Conform	18	40
Not conform	32	10

Is there a significant difference between the "support" and "no support" conditions in the frequency with which individuals are likely to conform? [Chi-Square = 19.87, with 1 df: p < 0.05].

```
In [28]: obs=np.array([[18,40],[32,10]])
    result=chi2_contingency(obs)
    print(f"Chi Square value is {result[0]}")
    print(f"Critical region with 1df and alpha=0.001 is 10.83")
    print("We reject null hypoythesis.So,there is significant difference between the
```

Chi Square value is 18.10344827586207 Critical region with 1df and alpha=0.001 is 10.83 We reject null hypoythesis.So,there is significant difference between the 'supp ort' and 'no support' conditions in the frequency with which individuals are likely to conform

Problem Statement 22:

We want to test whether short people differ with respect to their leadership qualities (Genghis Khan, Adolf Hitler and Napoleon were all stature-deprived, and how many midget MP's are there?) The following table shows the frequencies with which 43 short people and 52 tall people were categorized as "leaders", "followers" or as "unclassifiable". Is there a relationship between height and leadership qualities? [Chi-Square = 10.71, with 2 df: p < 0.01].

##	Height	
	Short	Tall
Leader	12	32
Follower	22	14
Unclassifiable	9	6

```
In [29]: obs=([[12,32],[22,14],[9,6]])
    result=chi2_contingency(obs)
    print(f"Chi Square value is {result[0]}")
    print(f"Critical region with 2df and alpha=0.001 is 13.82")
    print("We accept null hypothesis.there is no relationship between height and lead
```

Chi Square value is 10.712198008709638 Critical region with 2df and alpha=0.001 is 13.82 We accept null hypothesis.there is no relationship between height and leadership qualities

Problem Statement 23:

Each respondent in the Current Population Survey of March 1993 was classified as employed, unemployed, or outside the labor force. The results for men in California age 35- 44 can be cross-tabulated by marital status, as follows:

	Married	Widowed, divorced	Never married
		or separated	
Employed	679	103	114
Unemployed	63	10	20
Not in labor force	42	18	25

Men of different marital status seem to have different distributions of labor force status. Or is this just chance variation? (you may assume the table results from a simple random sample.)

```
In [30]: obs = np.array([[679,103,114], [63,10,20],[42,18,25]])
    result=chi2_contingency(obs)
    print(f"Chi Square value is {result[0]}")
    print(f"Critical region with 4df and alpha=0.001 is 18.47")
    print("We reject null hypothesis at alpha=0.001 .there is relationship between ma
```

Chi Square value is 31.61310319407798 Critical region with 4df and alpha=0.001 is 18.47 We reject null hypothesis at alpha=0.001 .there is relationship between martial status and employment status