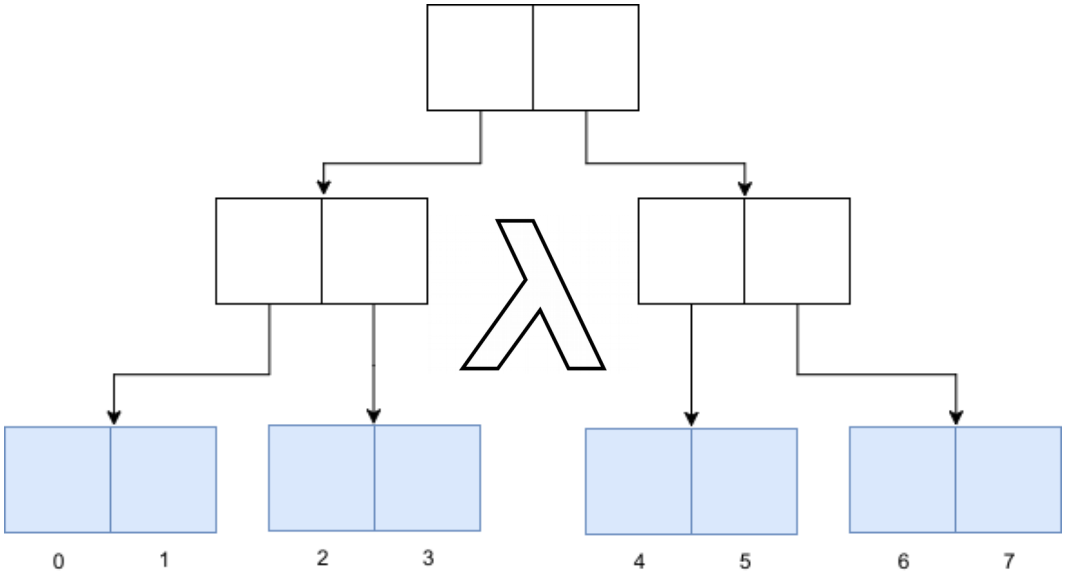
Marvellous Functional Datastructures: The Vector



Hello!

- Robert

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- Robert
- Scala & Clojure

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- Robert
- Scala & Clojure
- Obsessed with FP

Vectors: An Introduction

- What are Vectors?

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- **H**ash **A**rray **M**apped **T**ries (HAMT)

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  - Trie, Radix Tree, Prefix Tree

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  - Structured based on their contents

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  - tee, try, add, aid, map, see, sit

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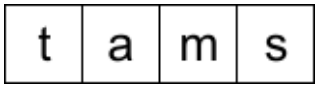

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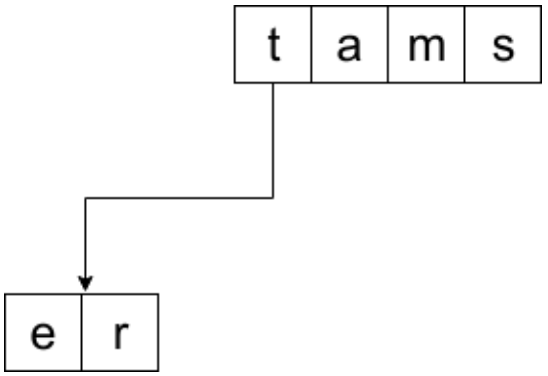

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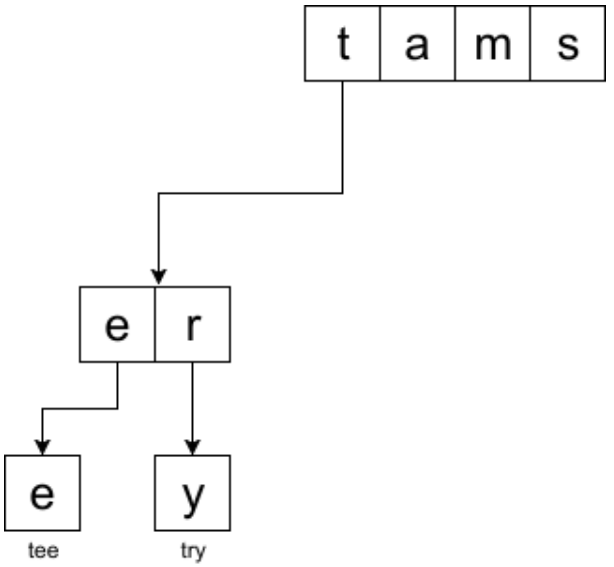

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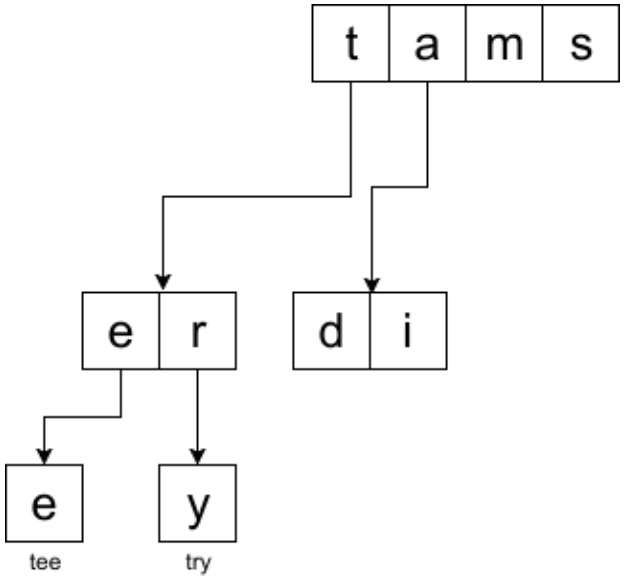

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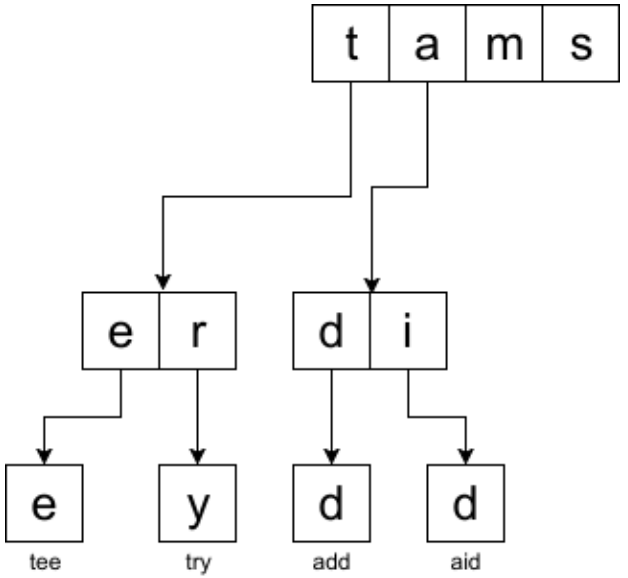

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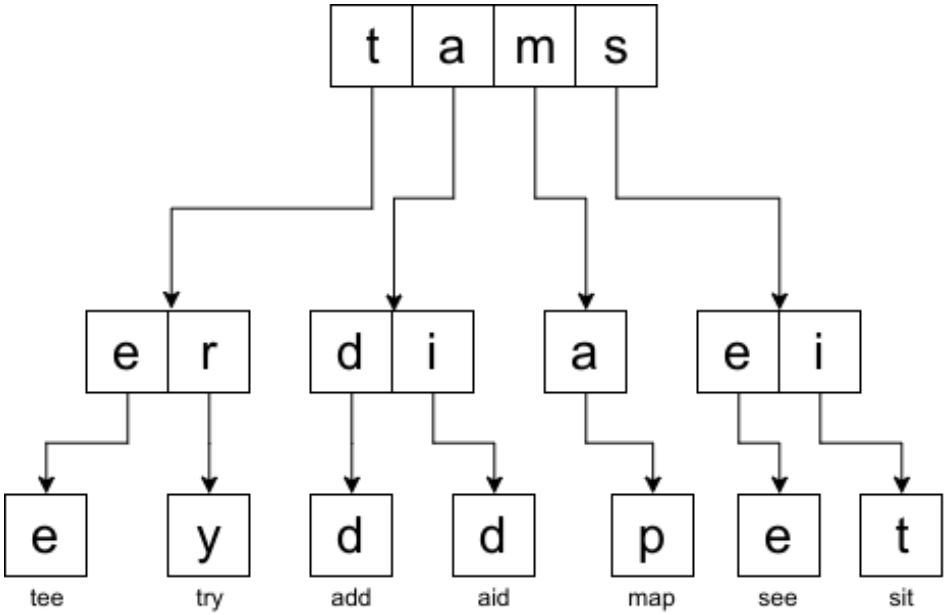

Vectors: An Introduction

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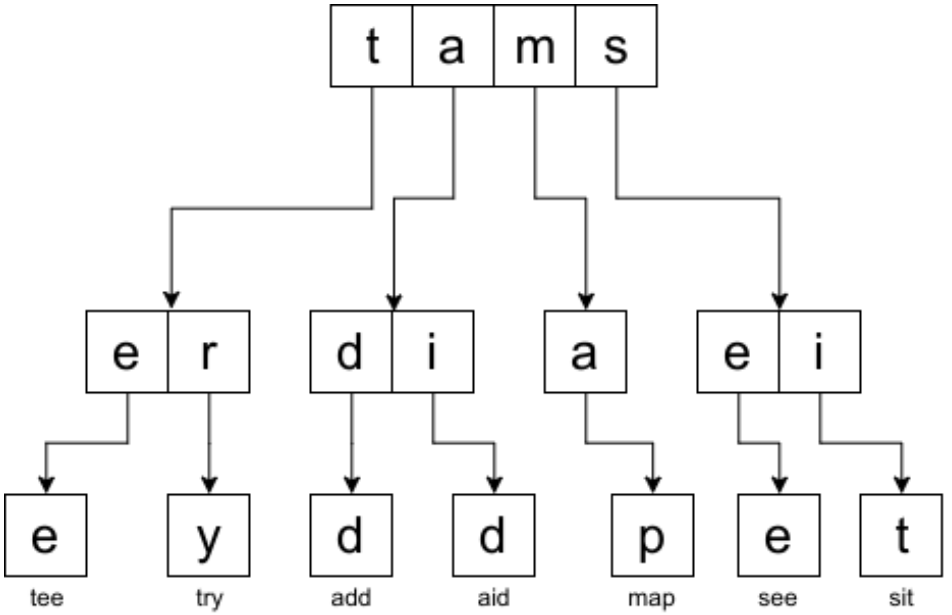

Vectors: An Introduction

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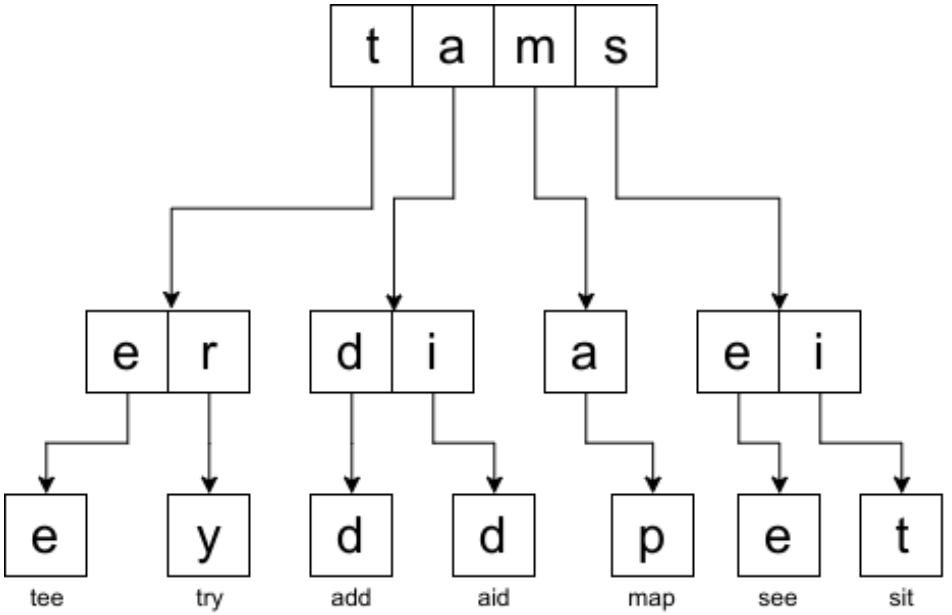

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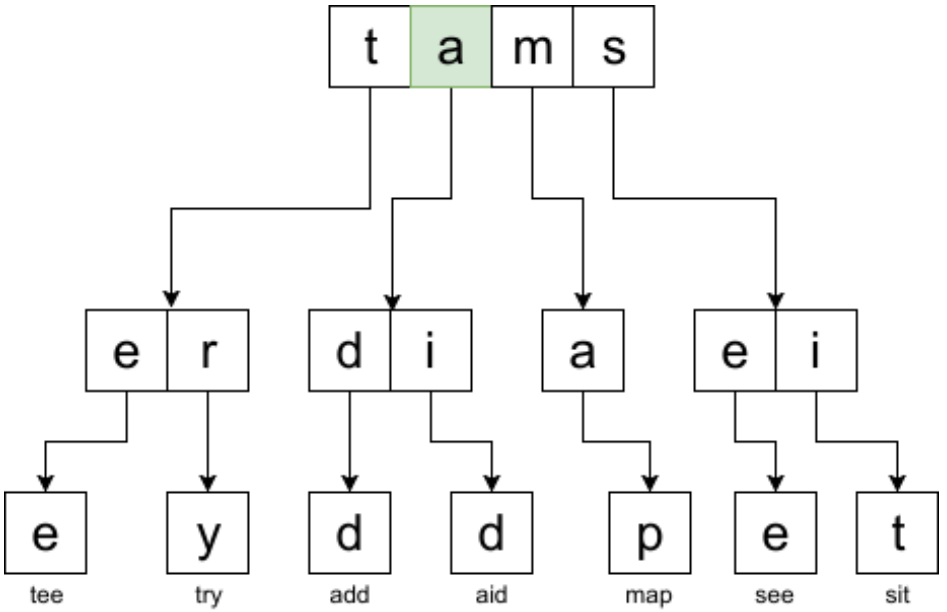

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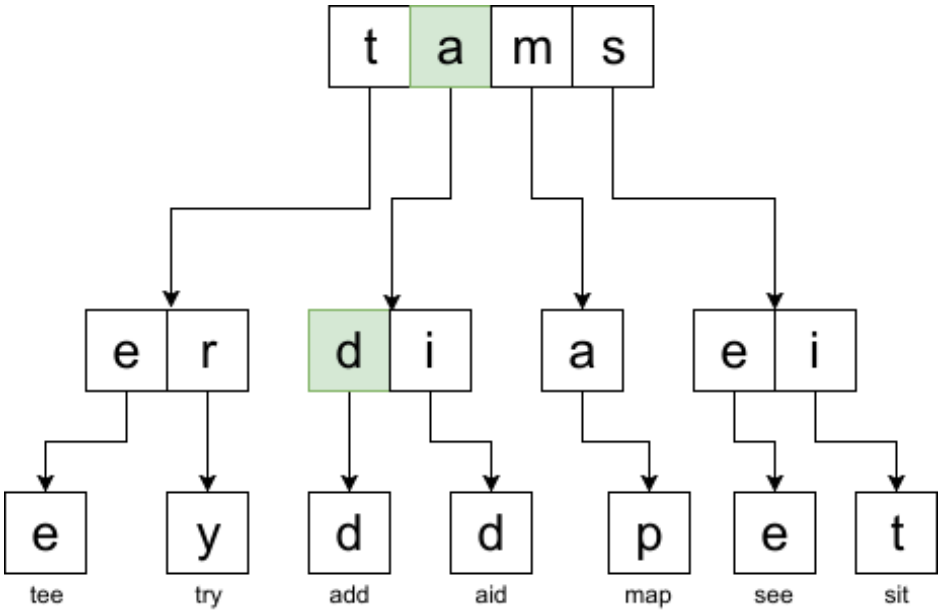

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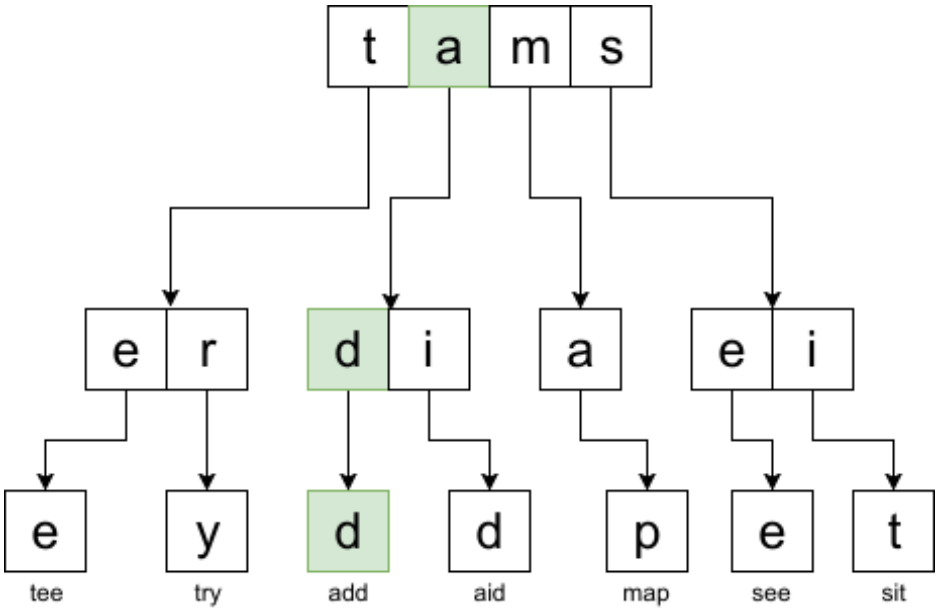
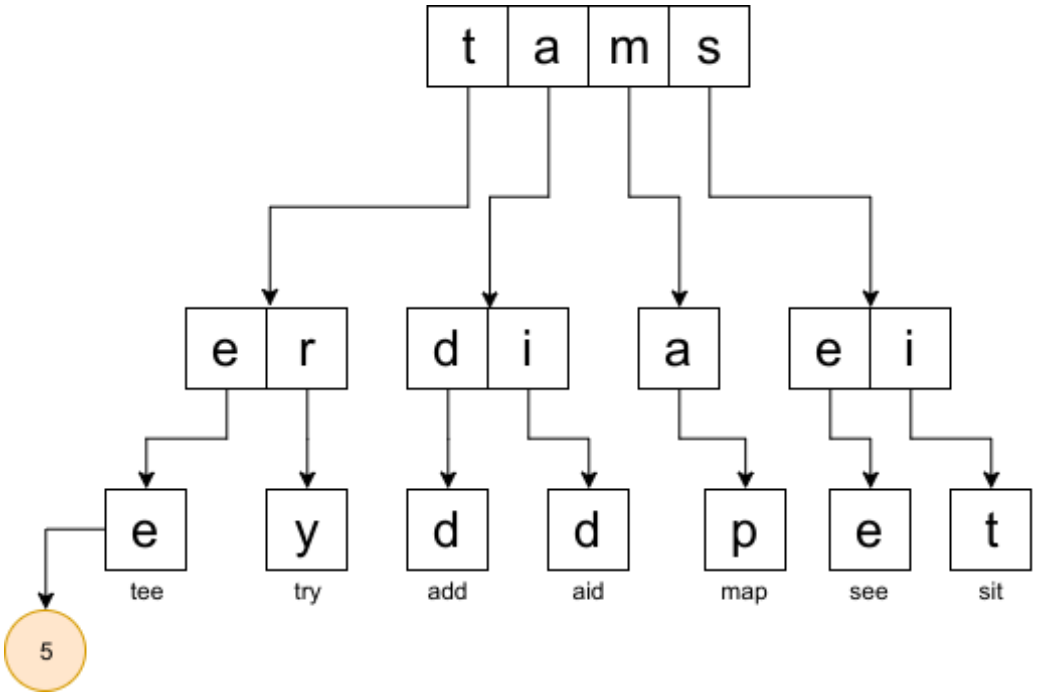


Vectors: An Introduction

- Trie Maps:
  - Associate value with leaf node



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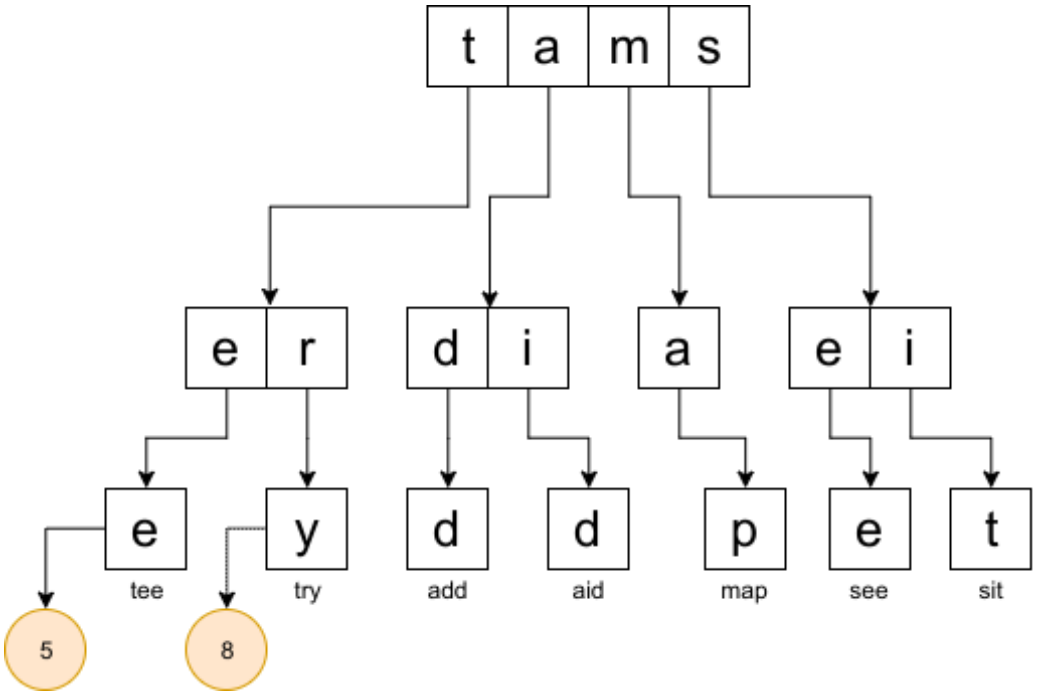

Vectors: An Introduction

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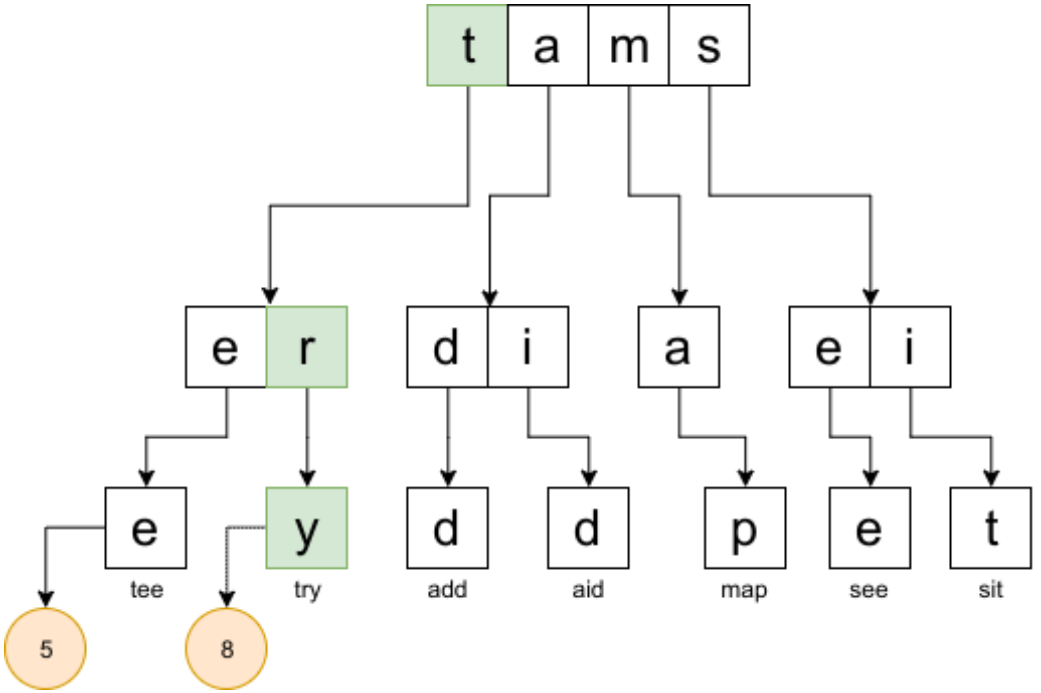

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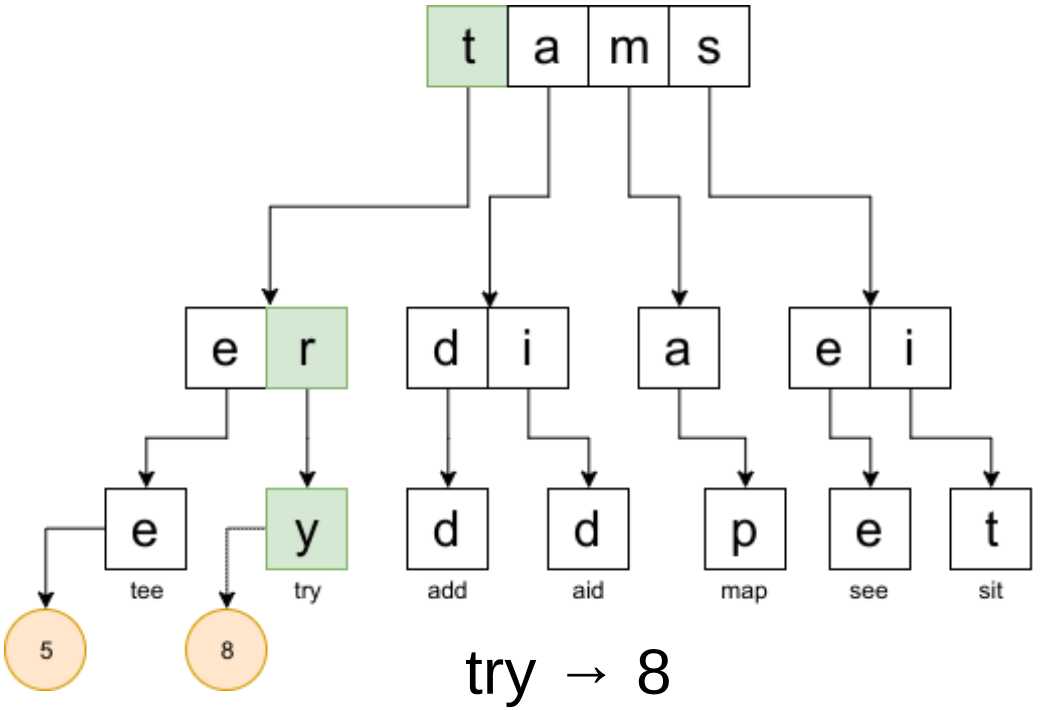

try → 8

Vectors: An Introduction

- Hash Array Mapped Tries:
  - Tries with hash ranges

Vectors: An Introduction

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  - Hash-Maps!

Vectors: An Introduction

- Hash Array Mapped Tries:
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  - Hash-Maps!
- Vectors:
  - HAMTs with ranges of integers

Vectors: An Introduction

- Indexing a trie:

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    1. Fixed branching factors (power of 2):

M = 2^b

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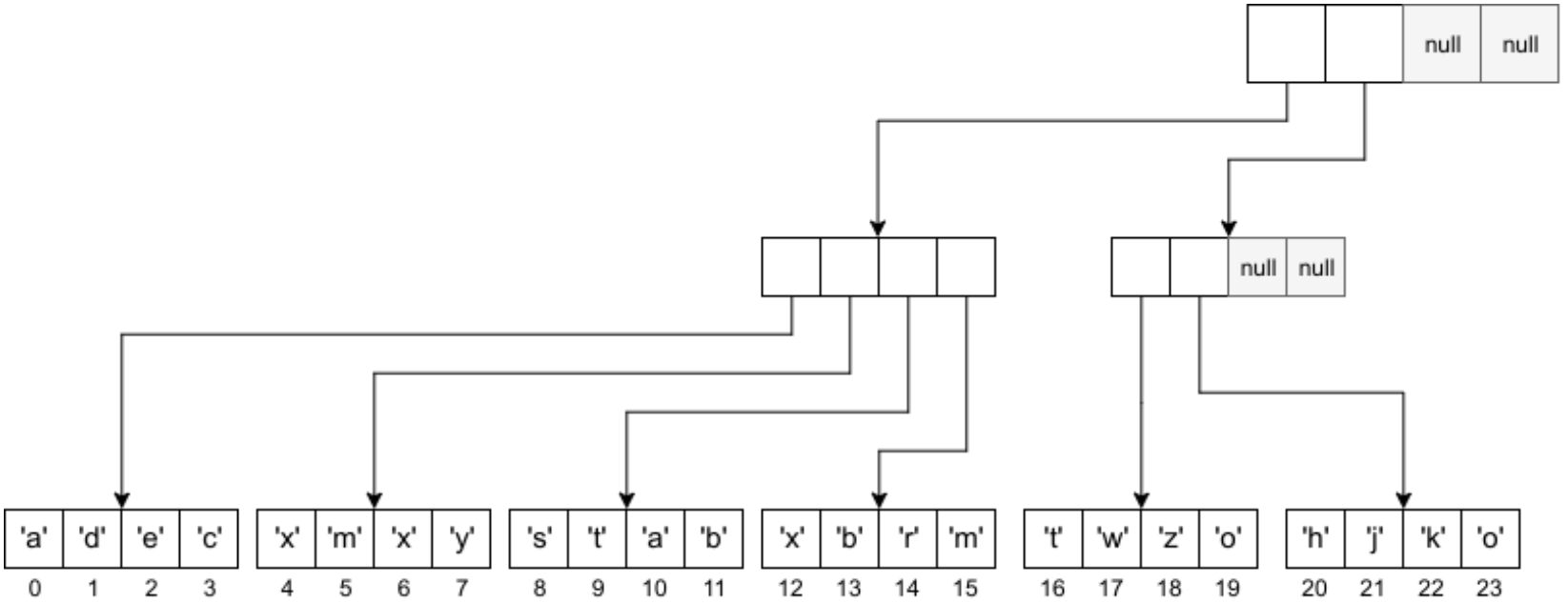
- Indexing a trie:
  1. Fixed branching factors (power of 2):

     M = 2^b

  2. Indexes are binary => Trie is bit-mapped

How to vector

Branching factor: 4
Height: 2



How to vector

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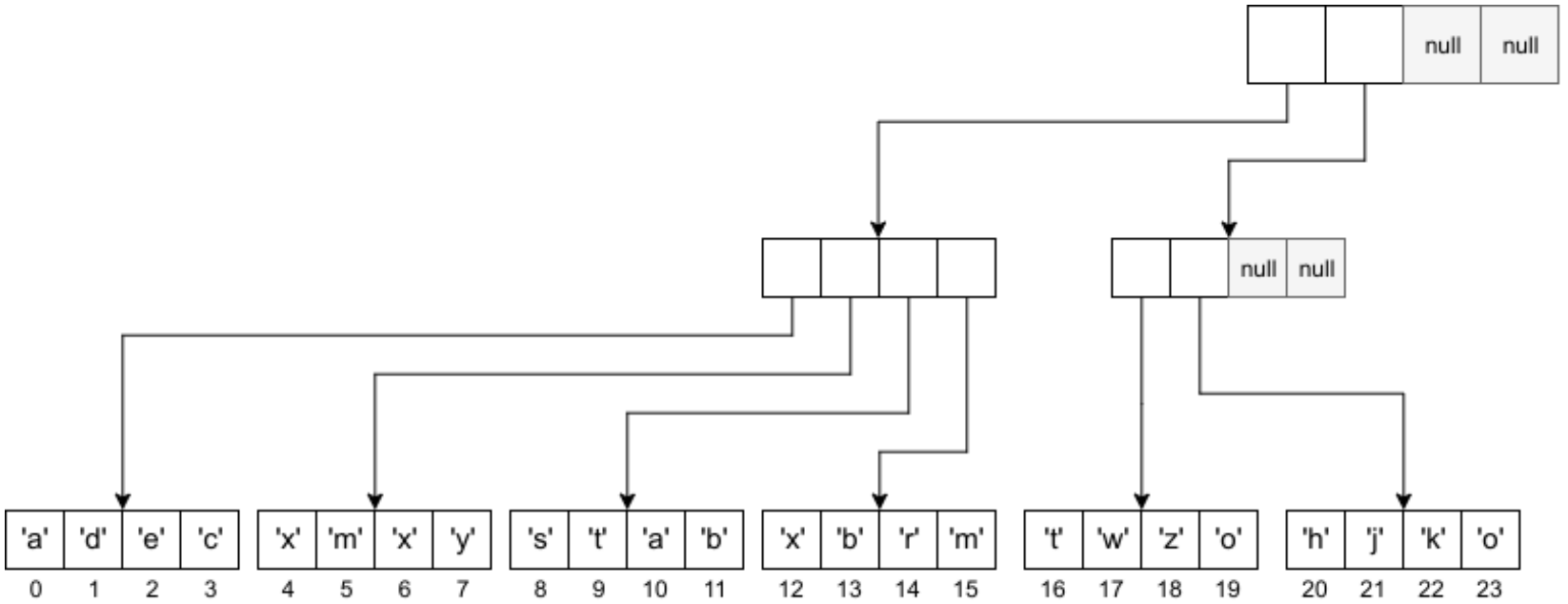
Look-up: 17



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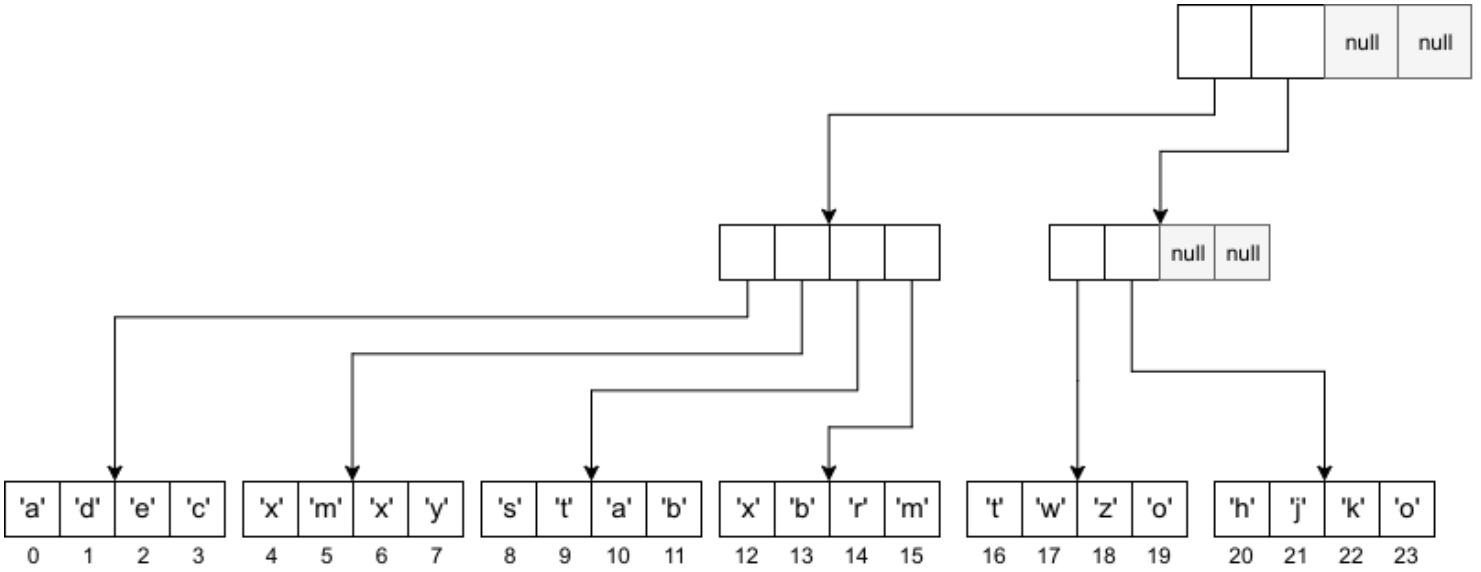

17 = | 0 | 1 | 0 | 0 | 0 | 1 |

How to vector

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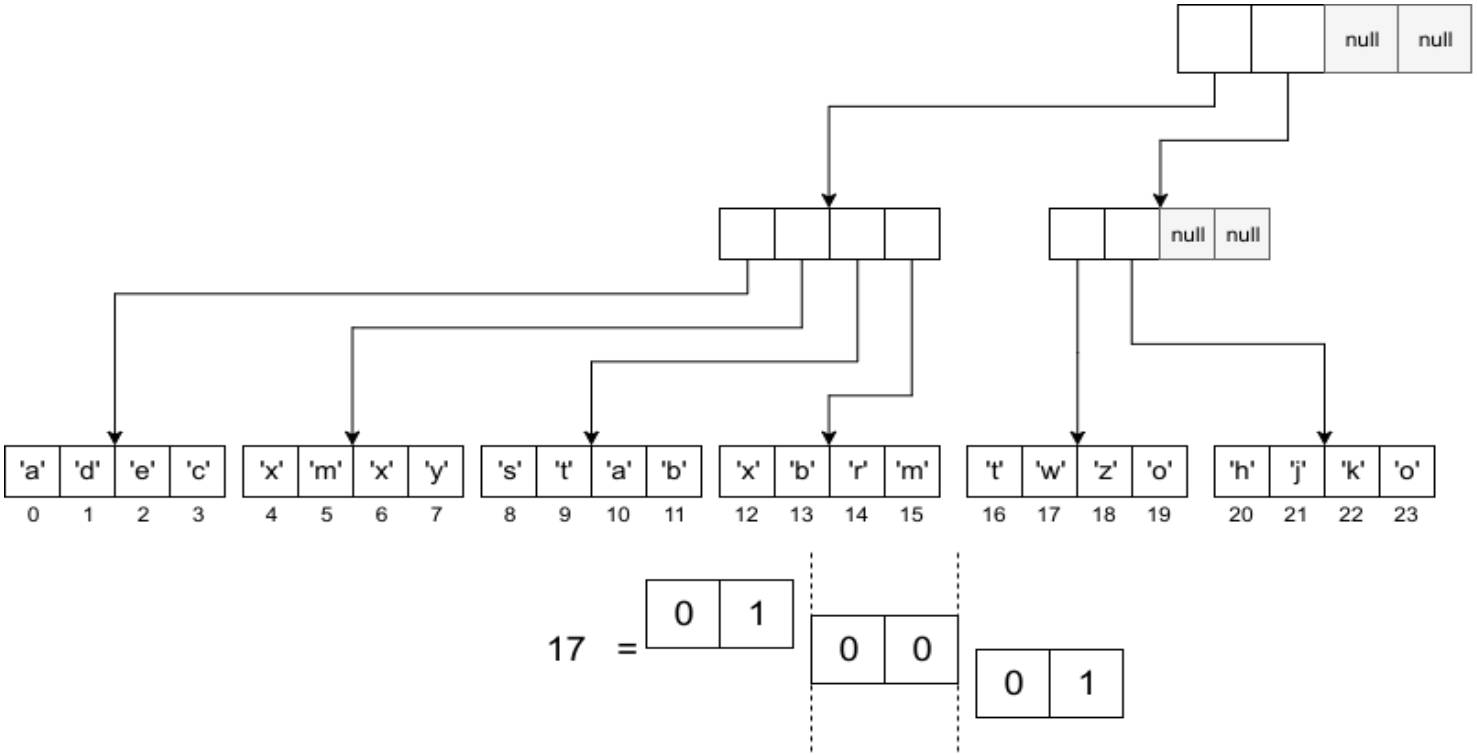

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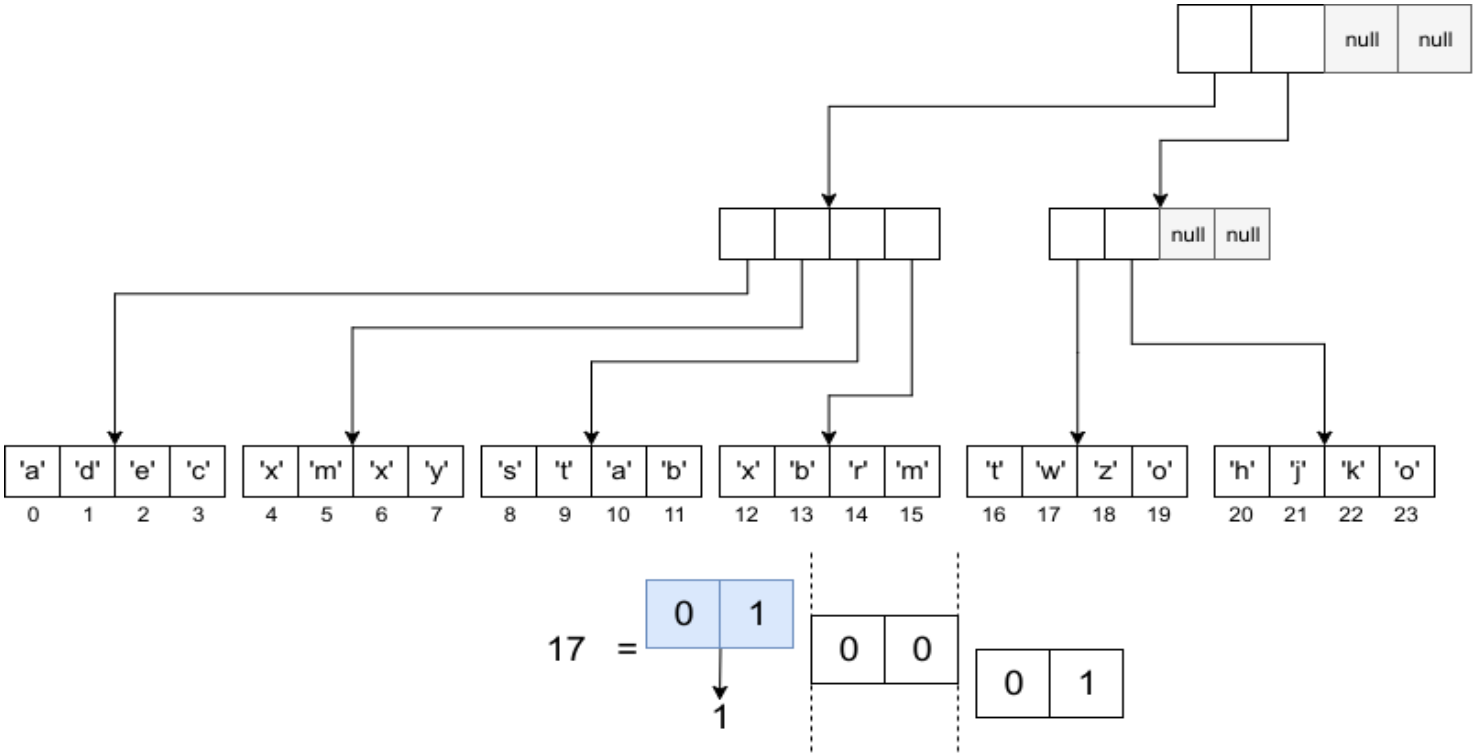

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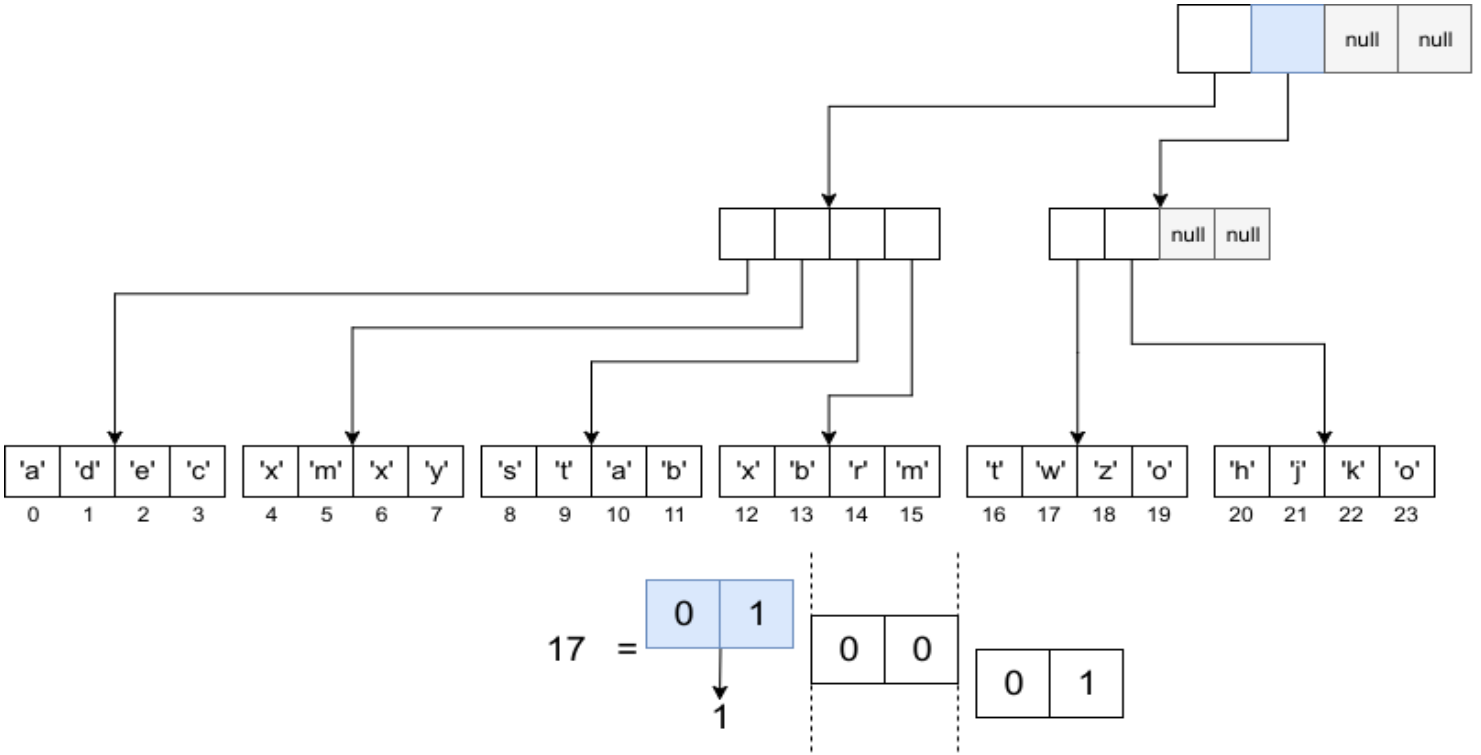

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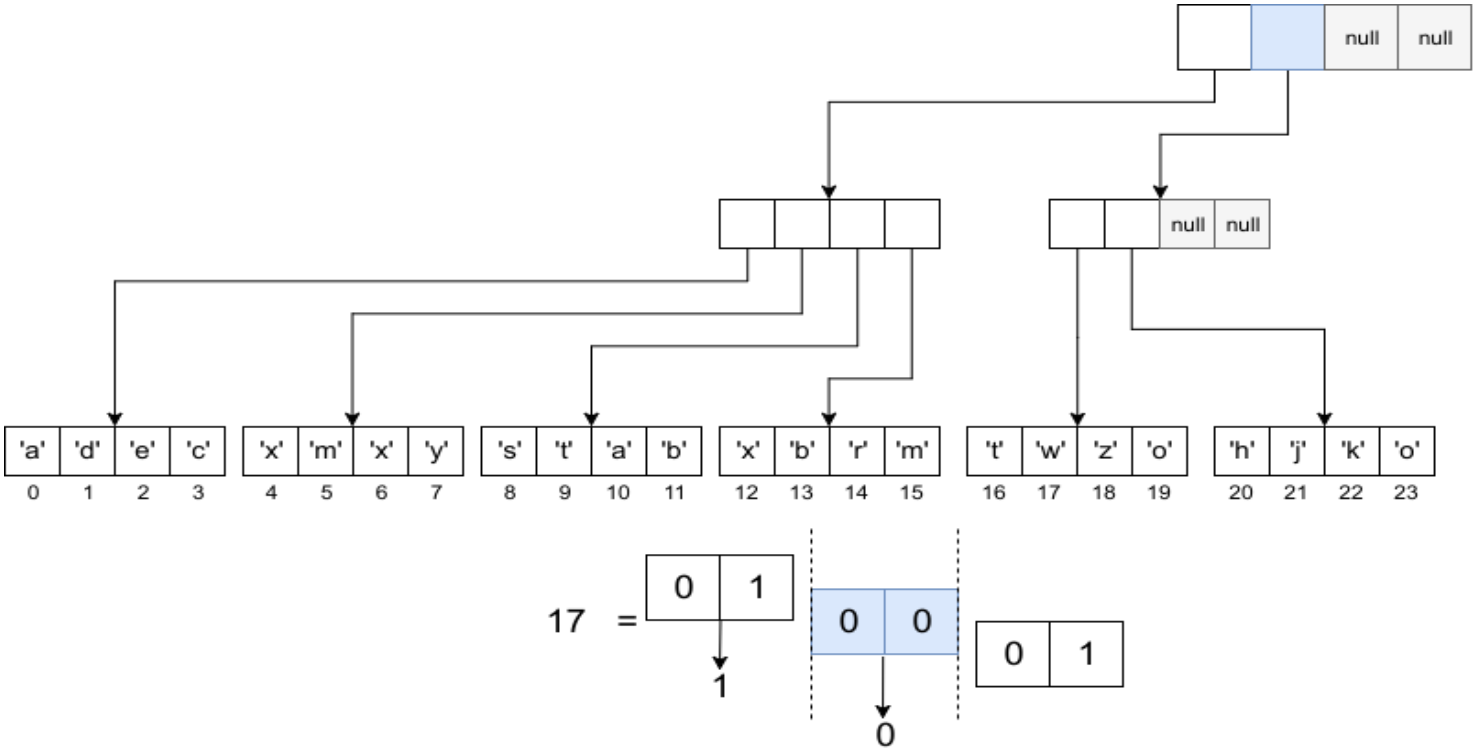

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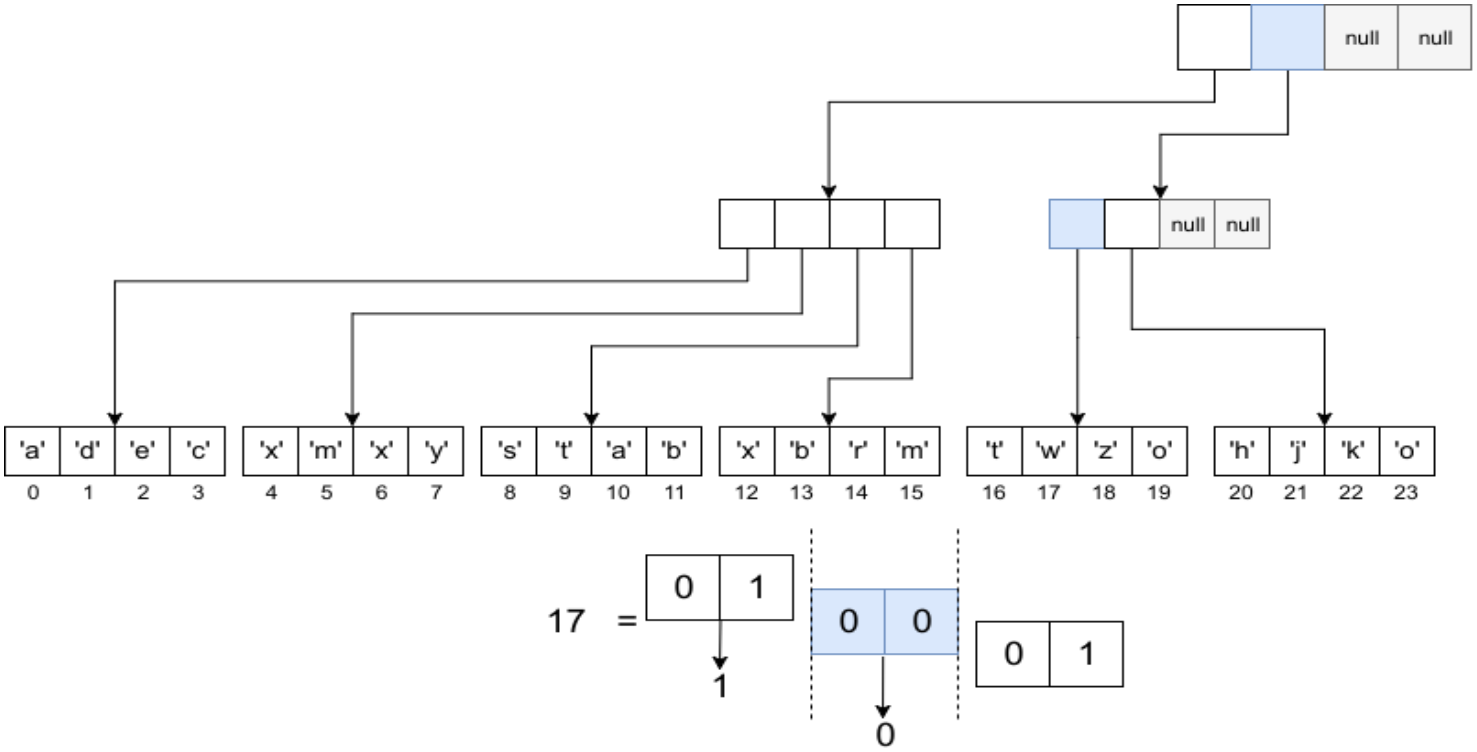

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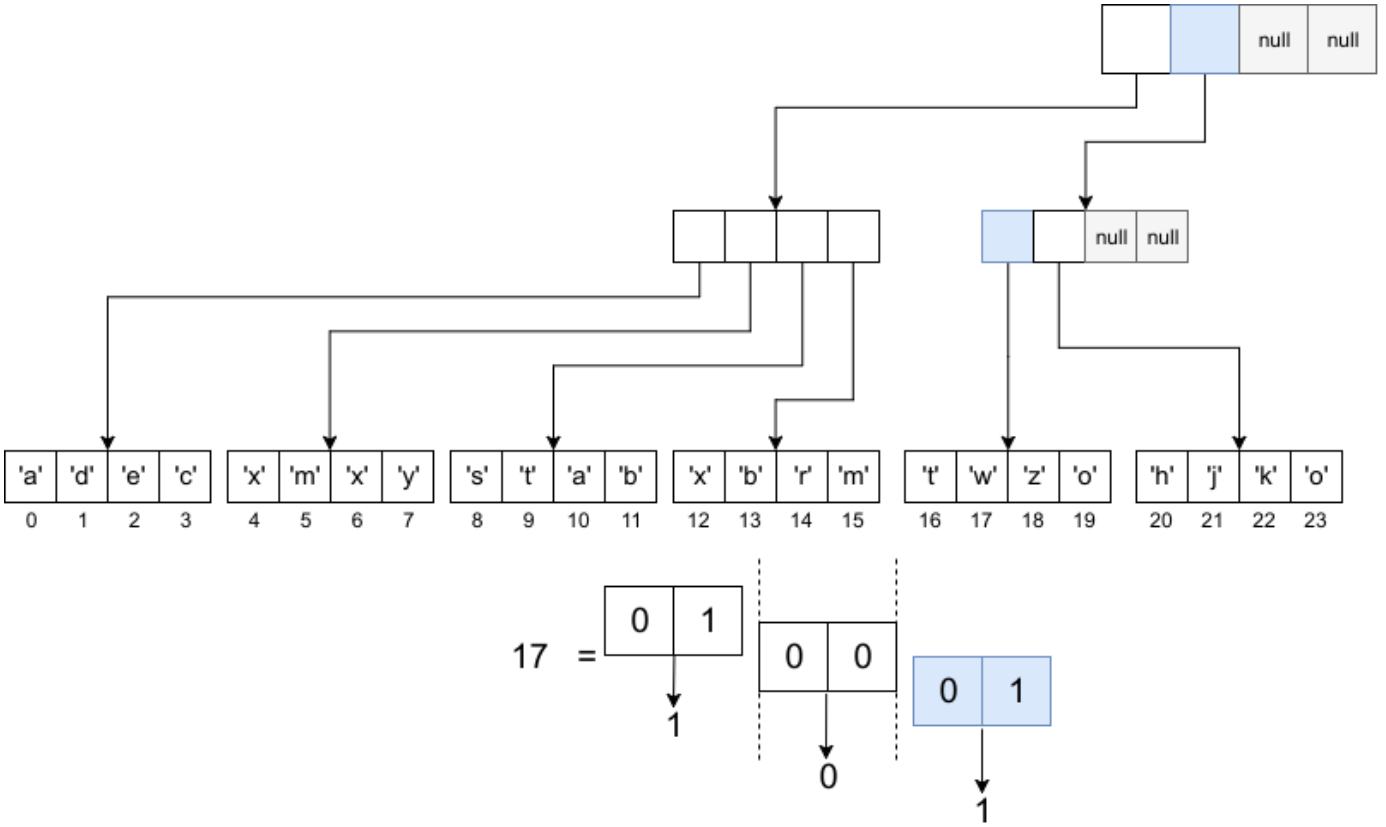

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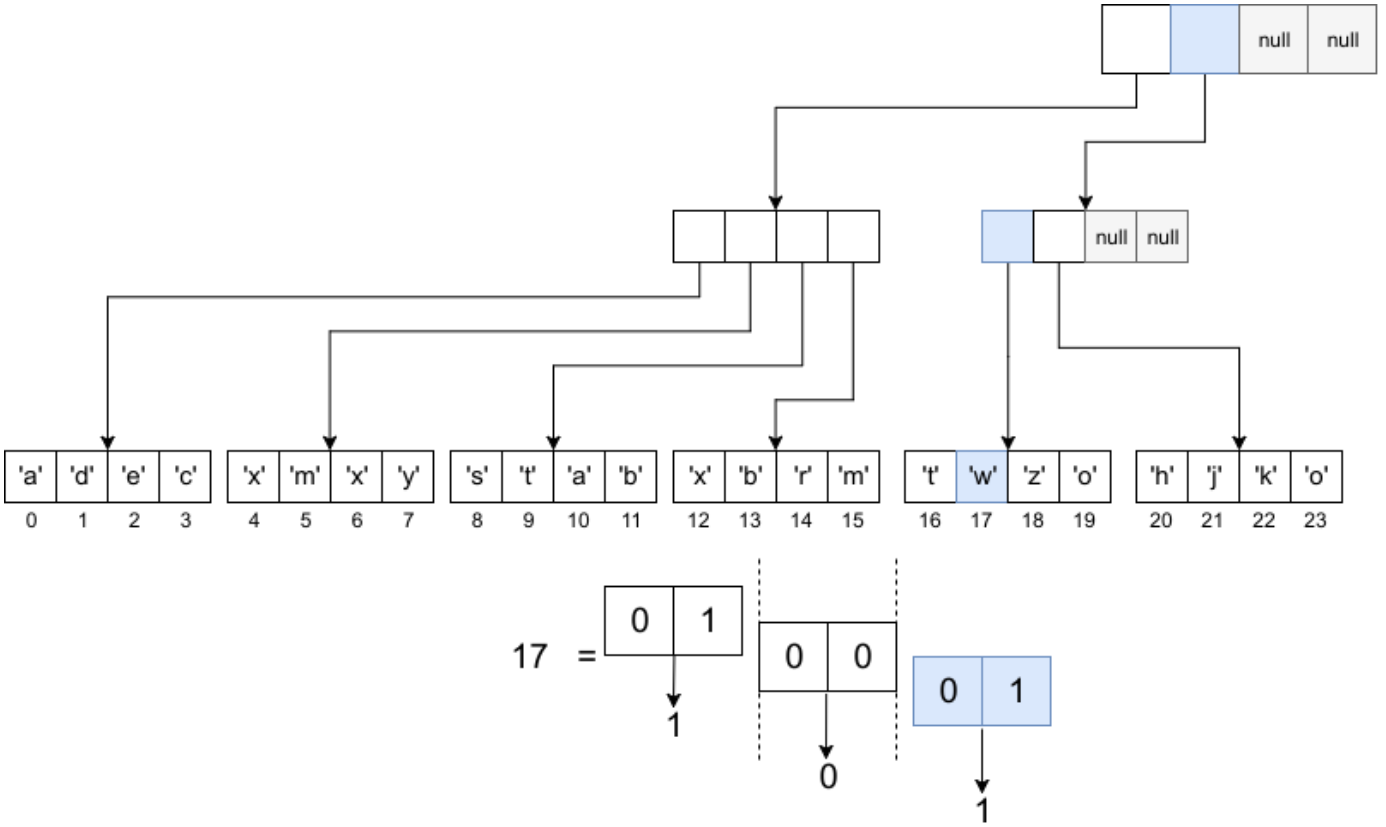
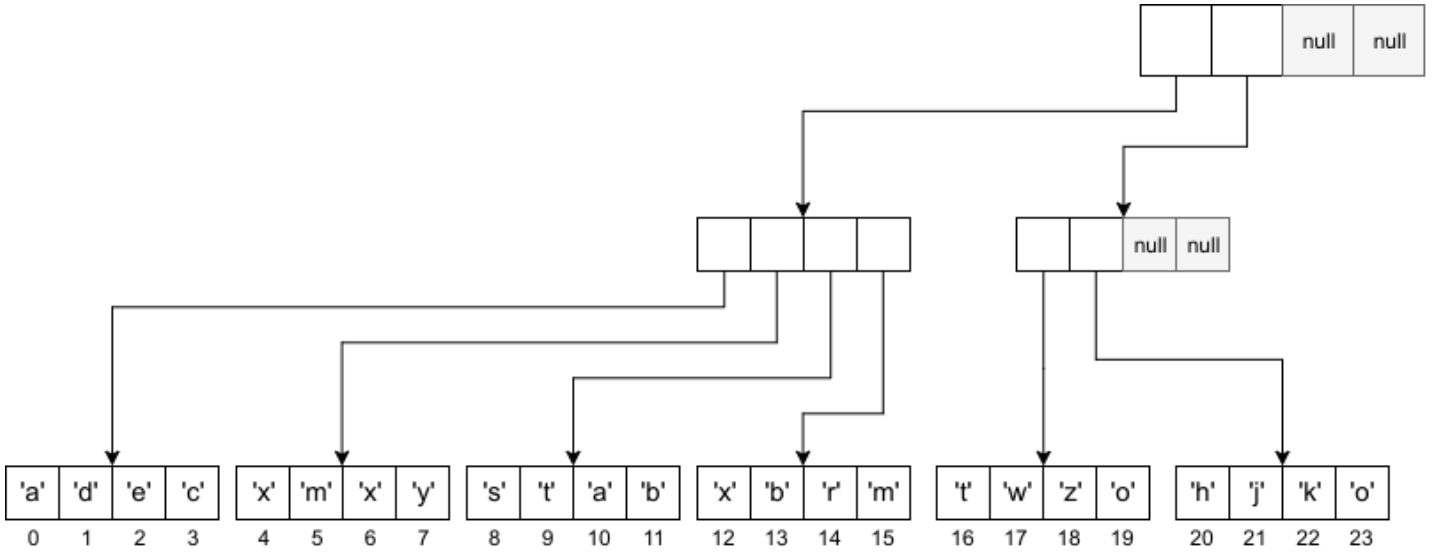


How to vector

Branching factor: 4
Height: 2

Append: ‘n’ → index 24



'n' = 24

How to vector

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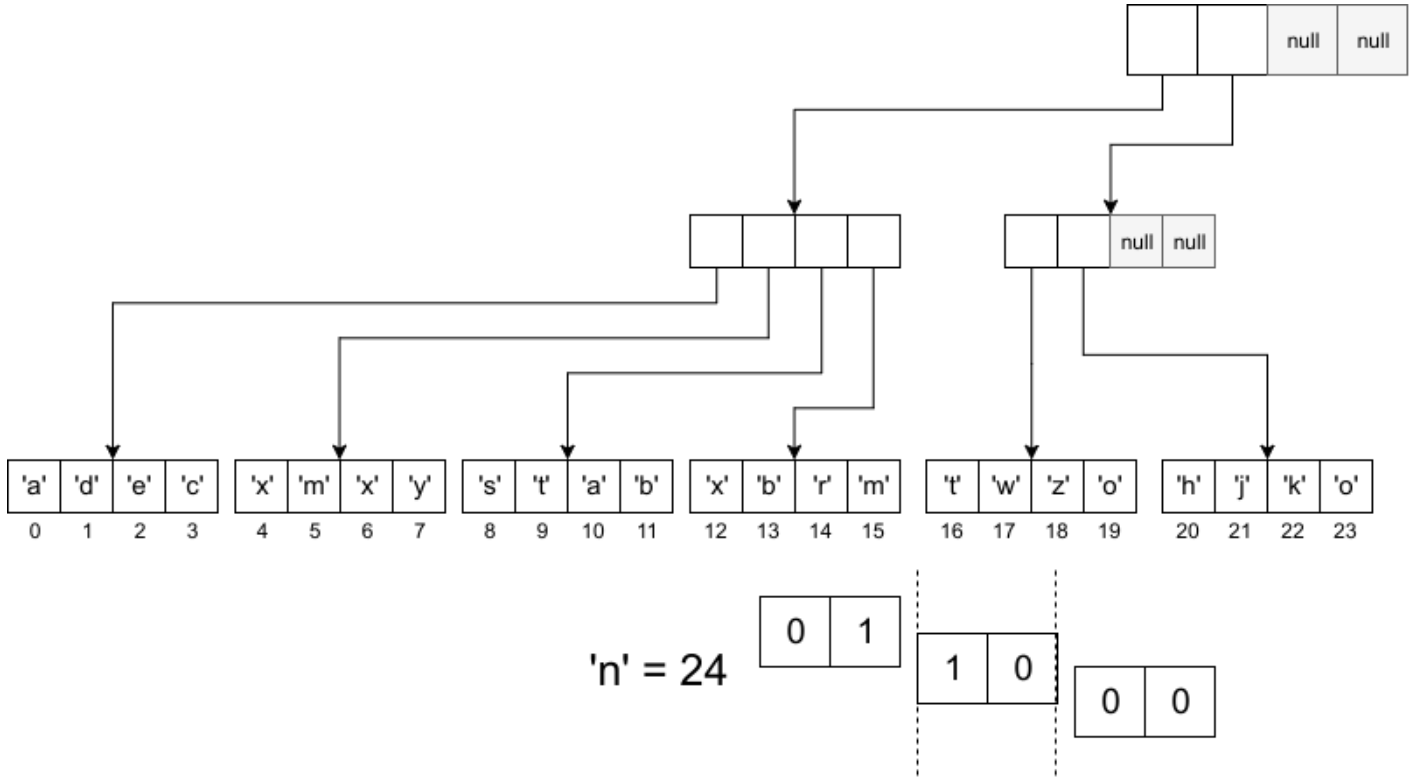
Height: 2

Append: ‘n’ → index 24



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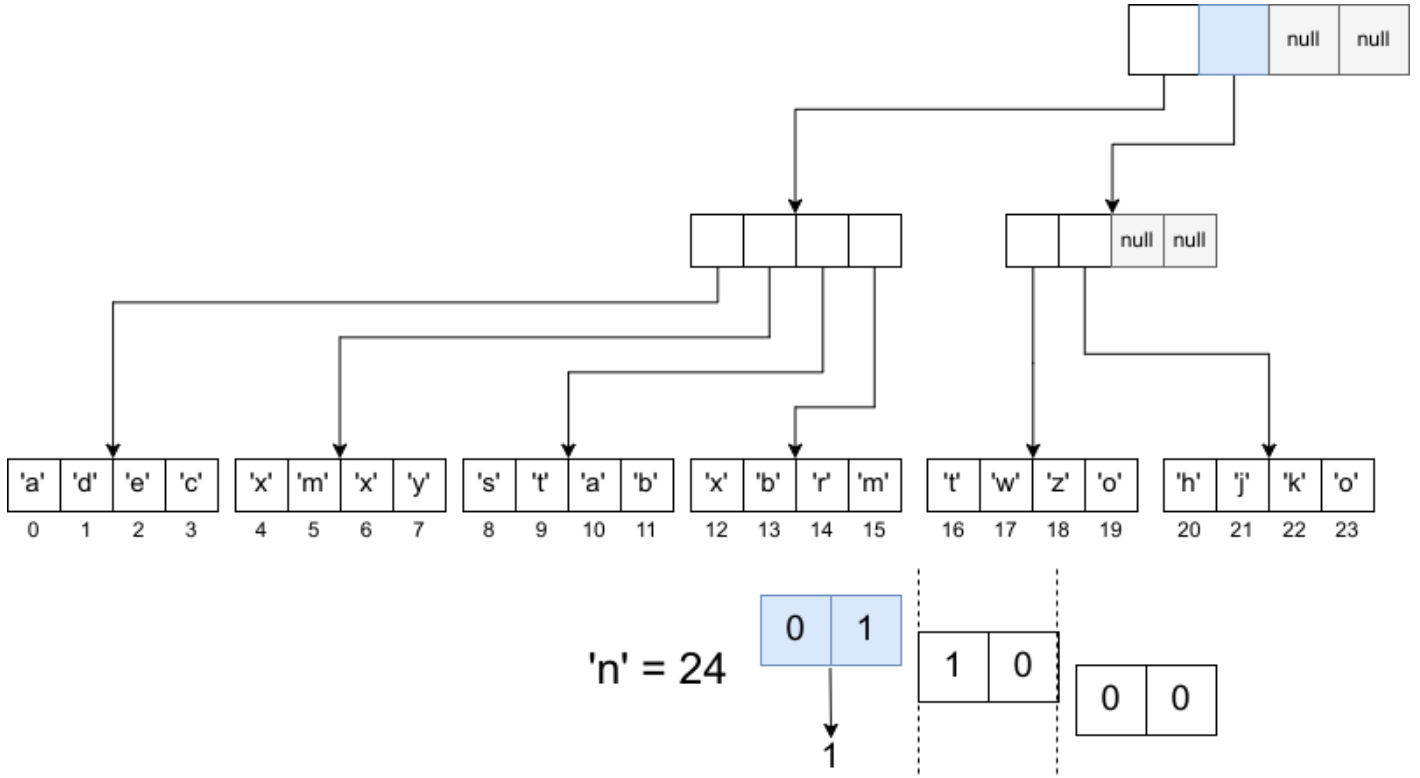

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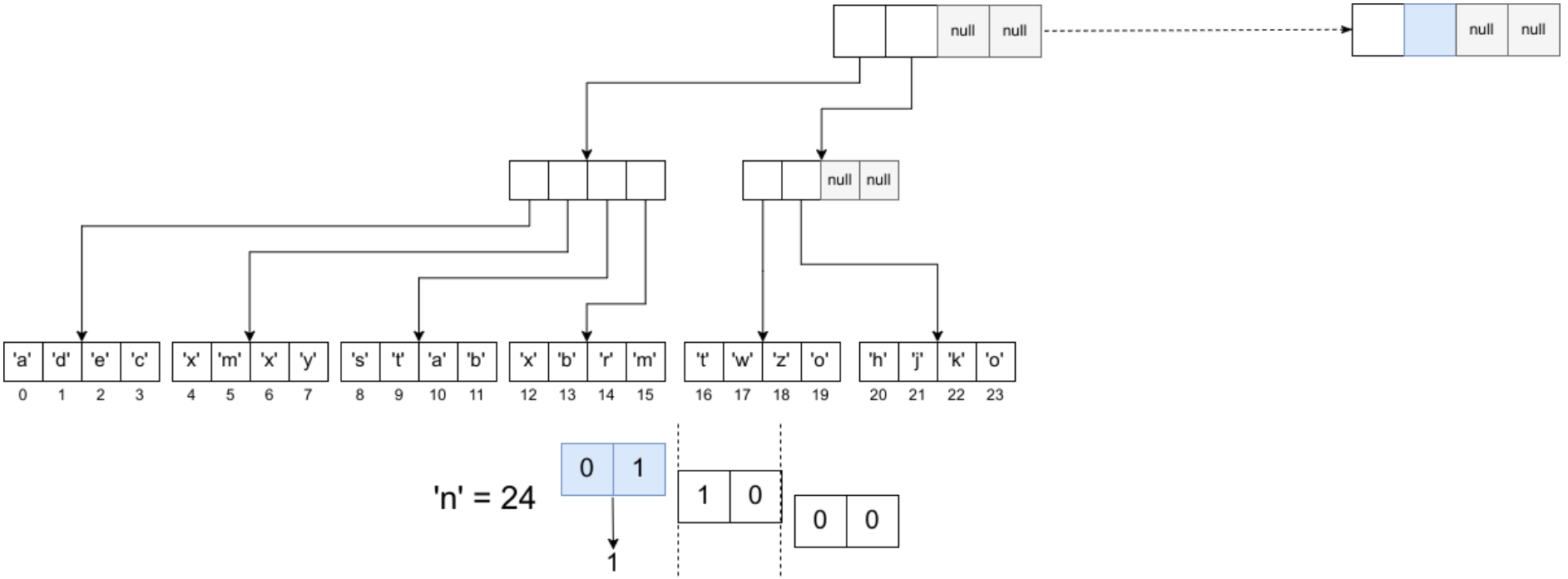

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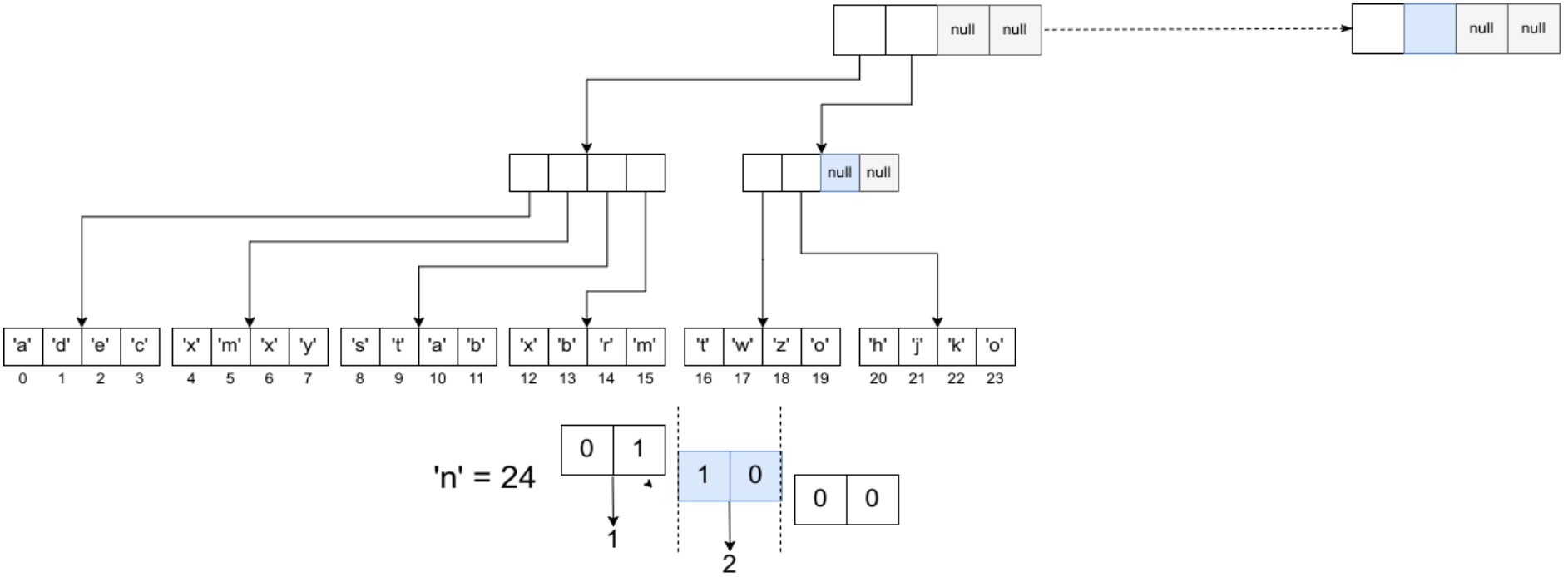

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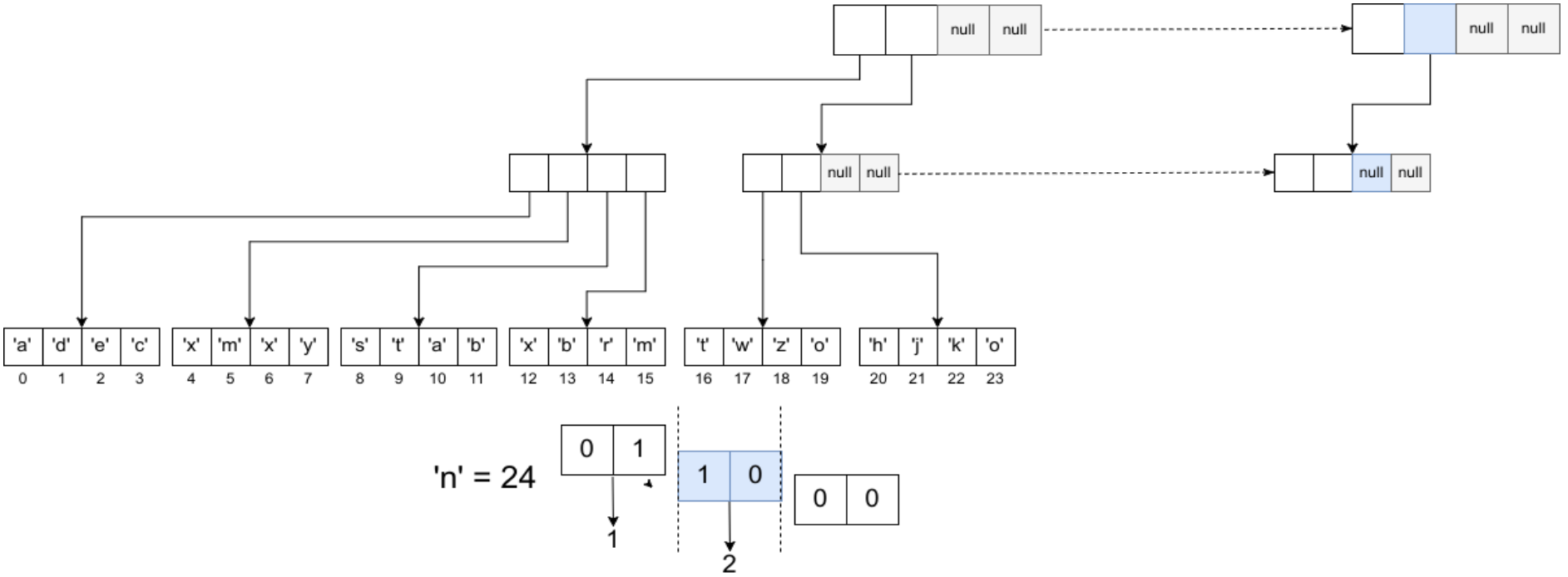

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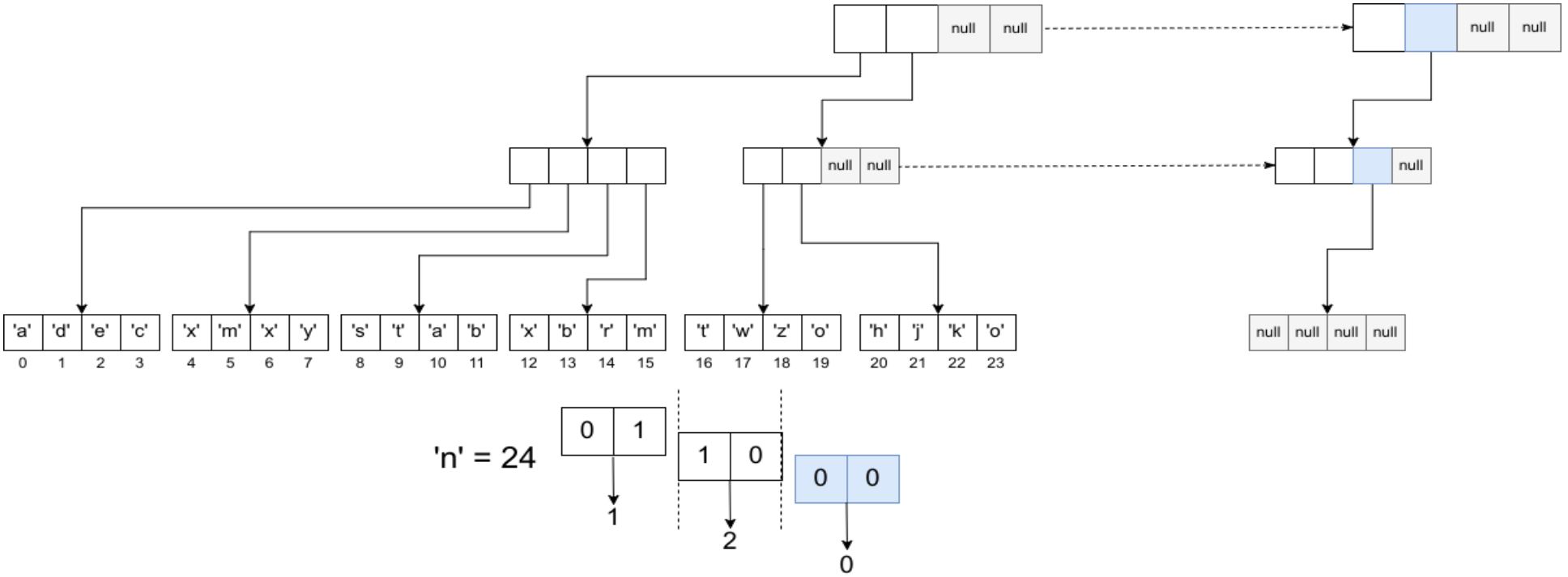

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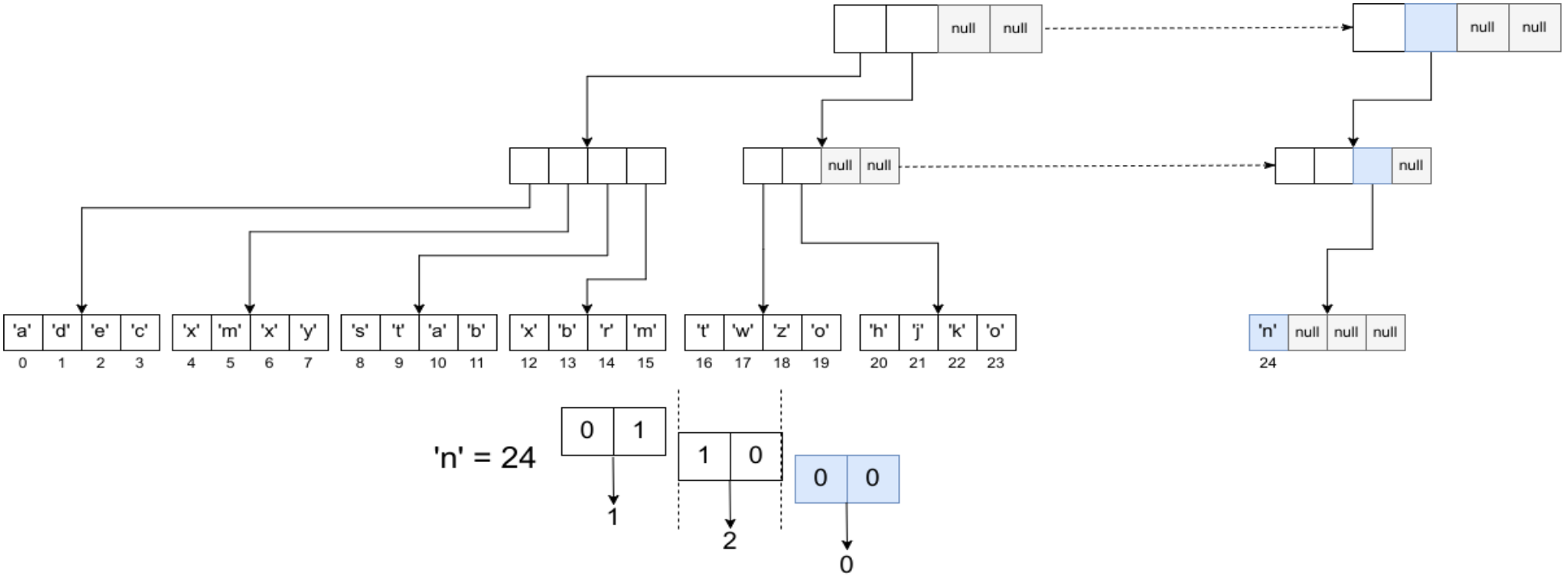

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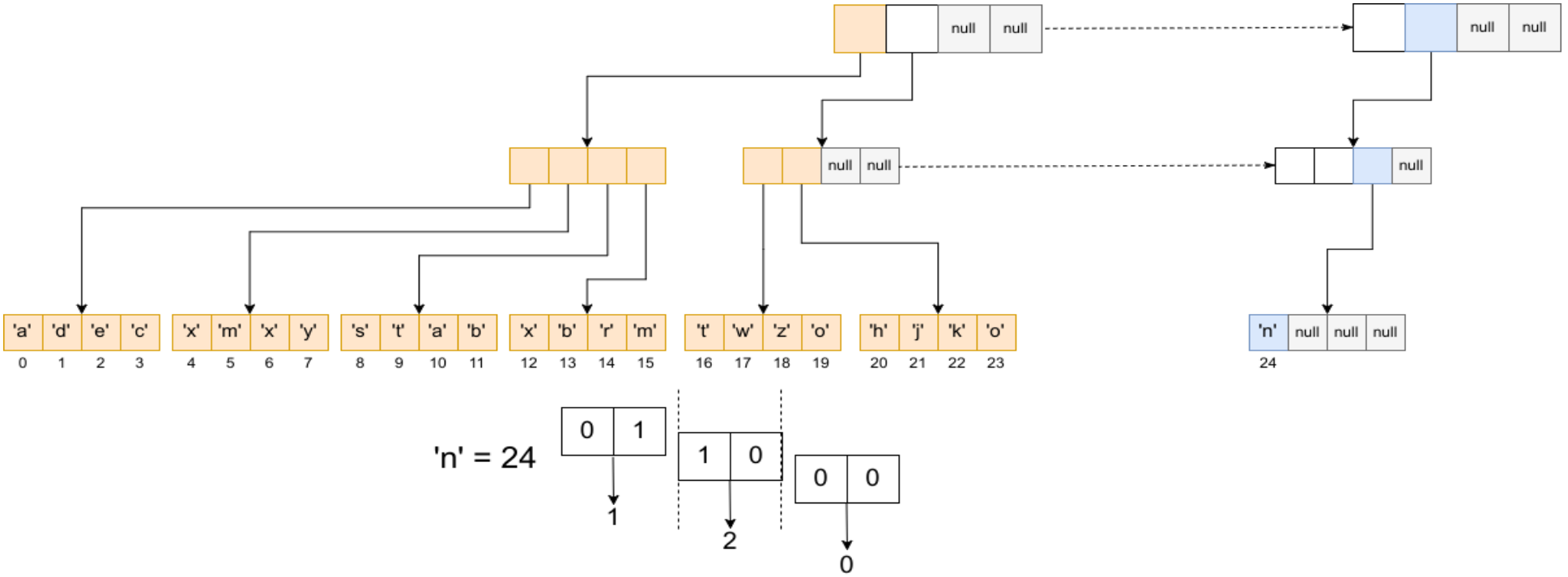

How to vector

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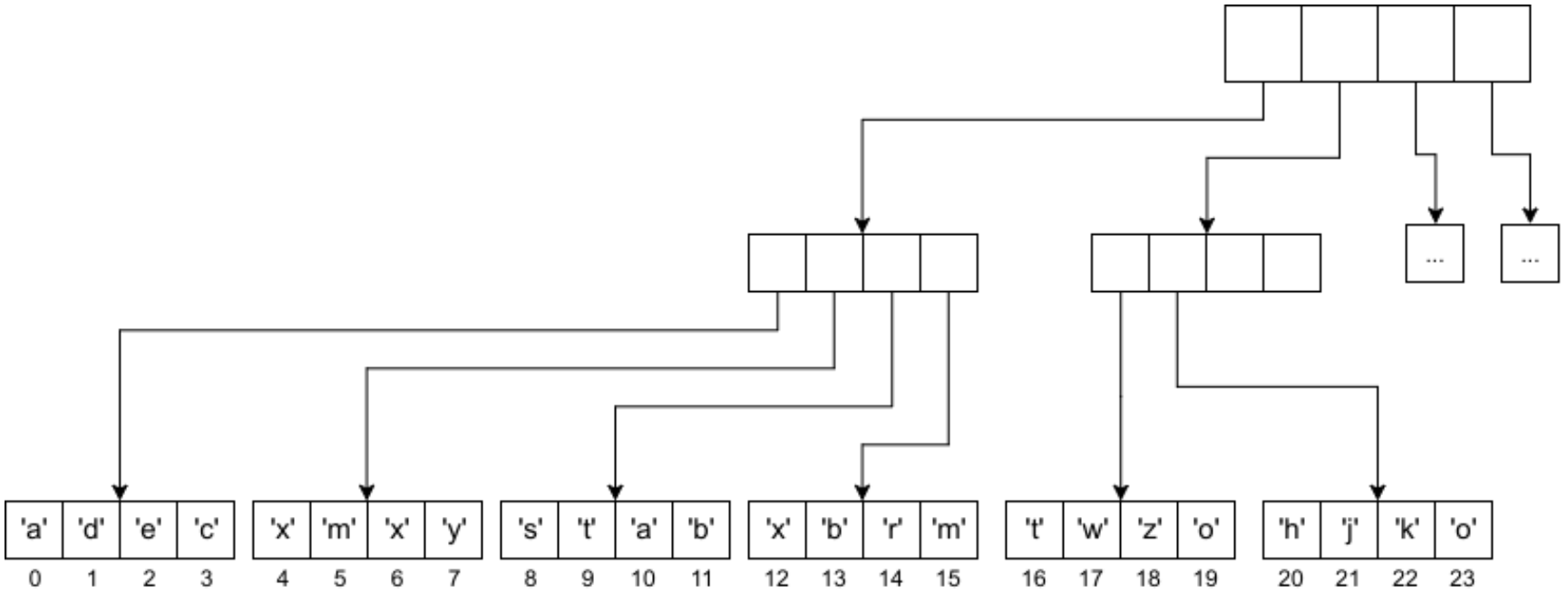
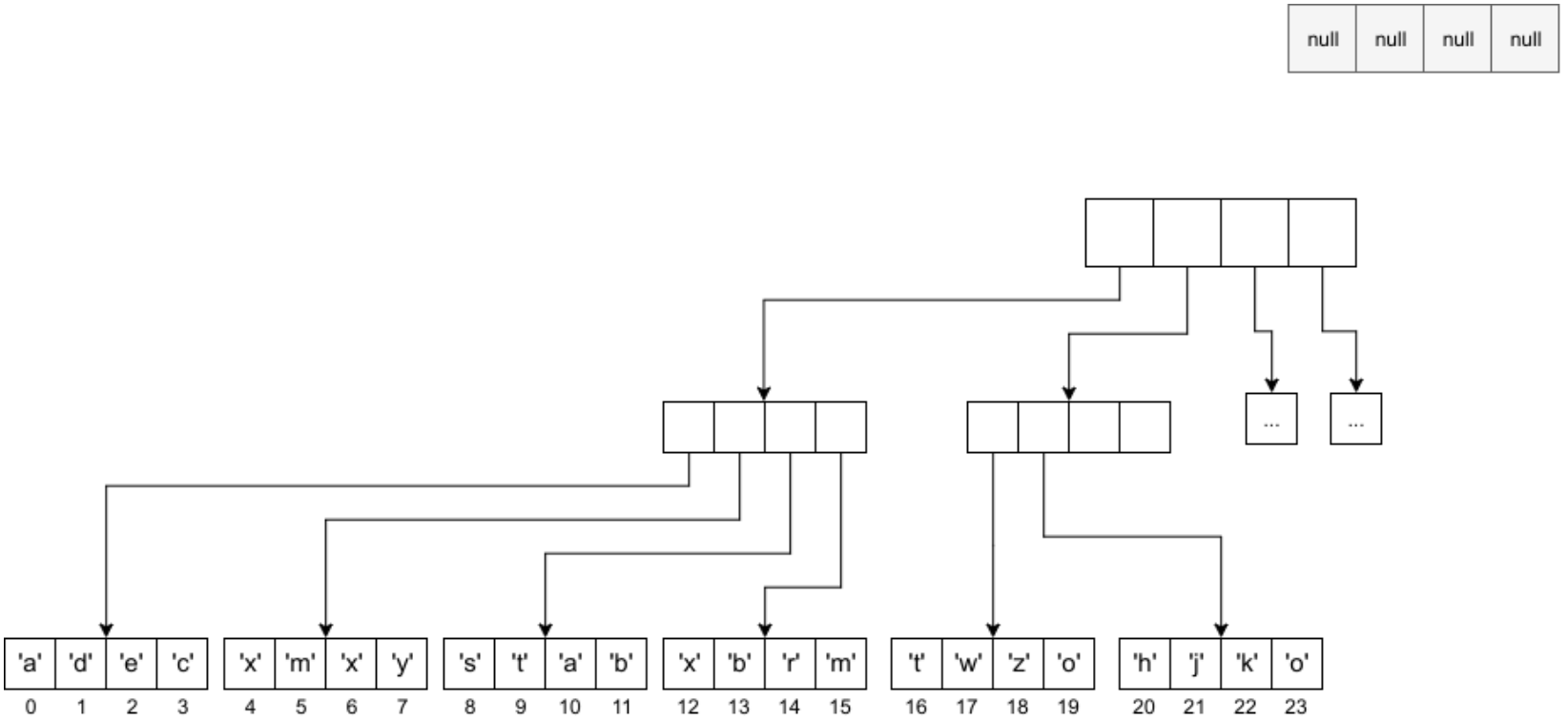
Append when full



How to vector

Branching factor: 4
Height: **3**

Append when full



How to vector

Branching factor: 4
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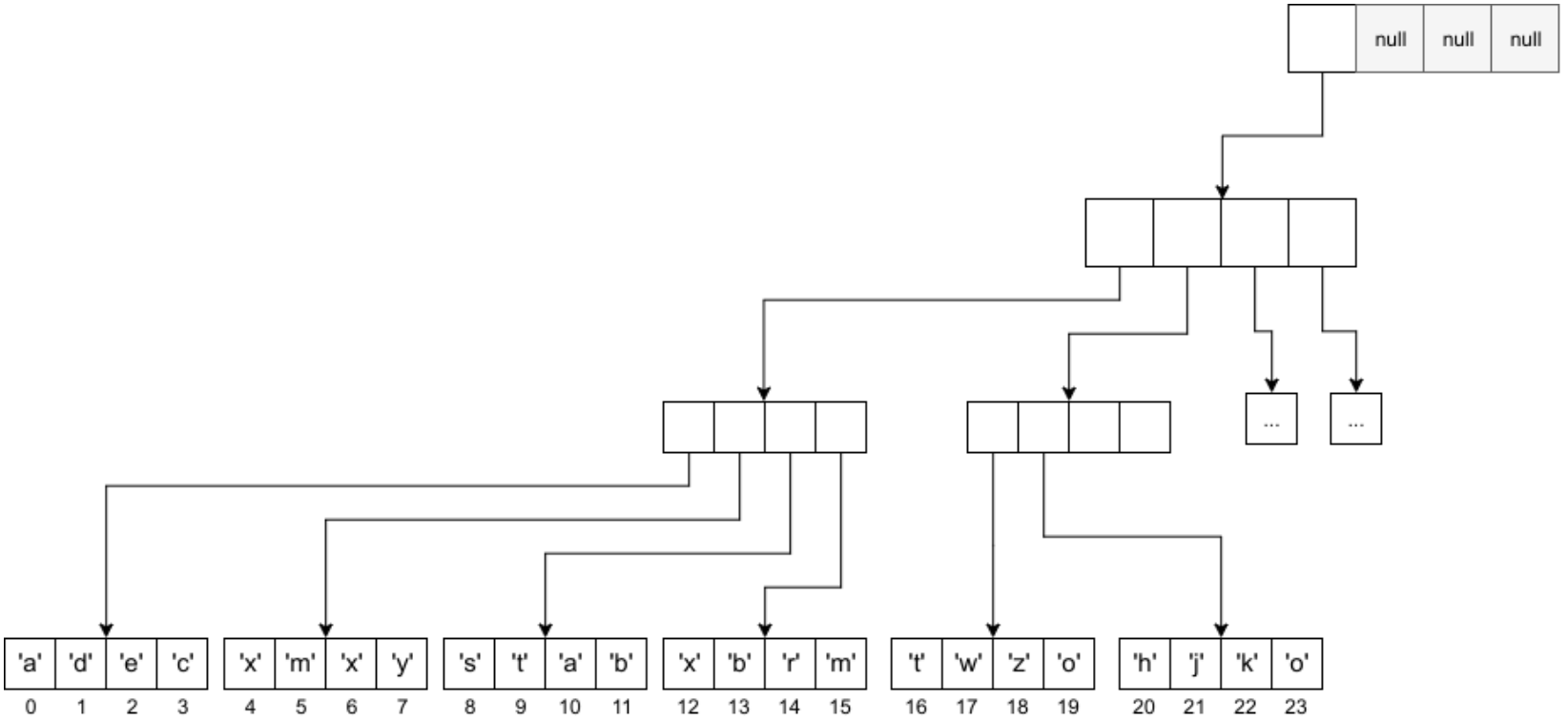

How to vector

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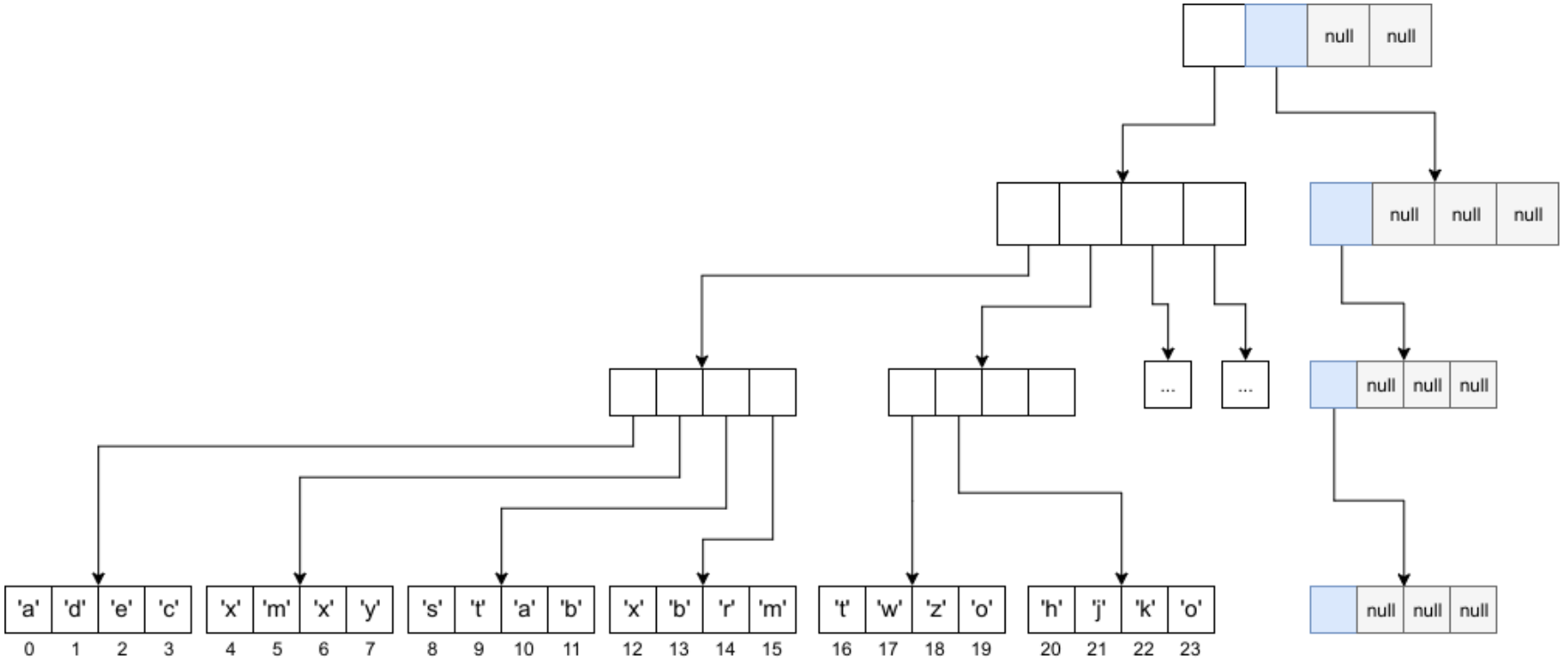
Height: **3**

Append when full



How to vector (properly this time)

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How to vector (properly this time)

- You don’t implement binary nonesense
- Calculate with bitwise operations
- Index with formula:

  f (i, h) = (i >> shift) & (M – 1)

  shift = h * **b** (M = 2^**b**)

  M = branching factor

Vectors: In the wild

- Why log32?

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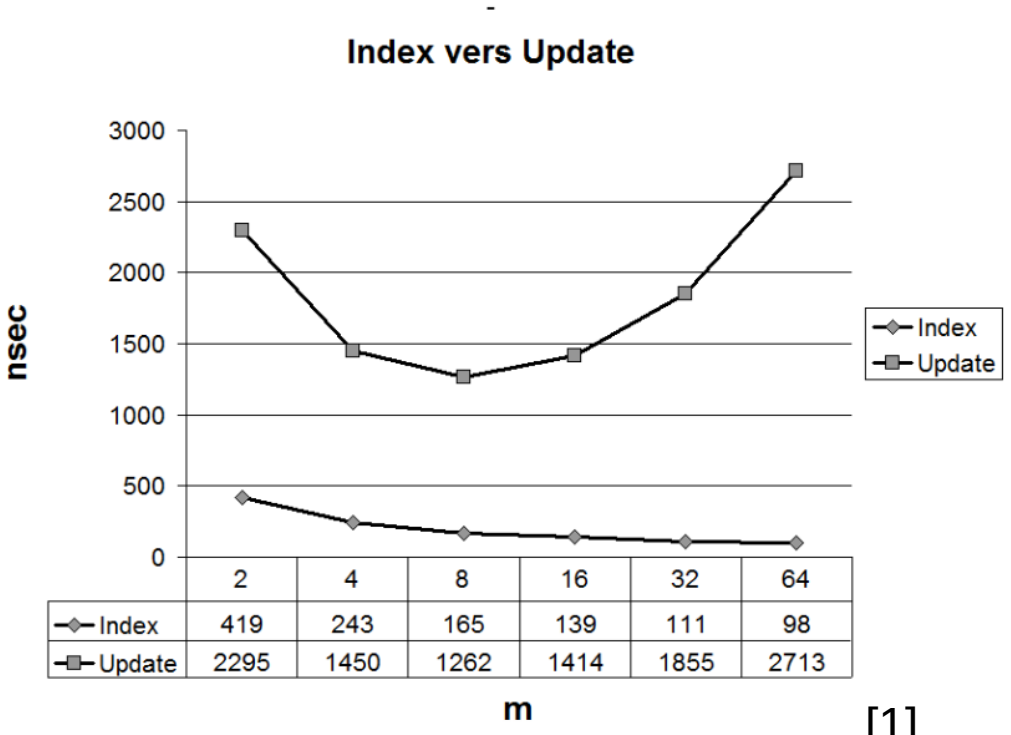


	2	4	8	16	32	64
Index	419	243	165	139	111	98
Update	2295	1450	1262	1414	1855	2713

[1]

Vectors: In the wild

- Scala Vector:
  - (on average) O(1) update
  - (on average) O(1) look-up

[1]

Vectors: In the wild

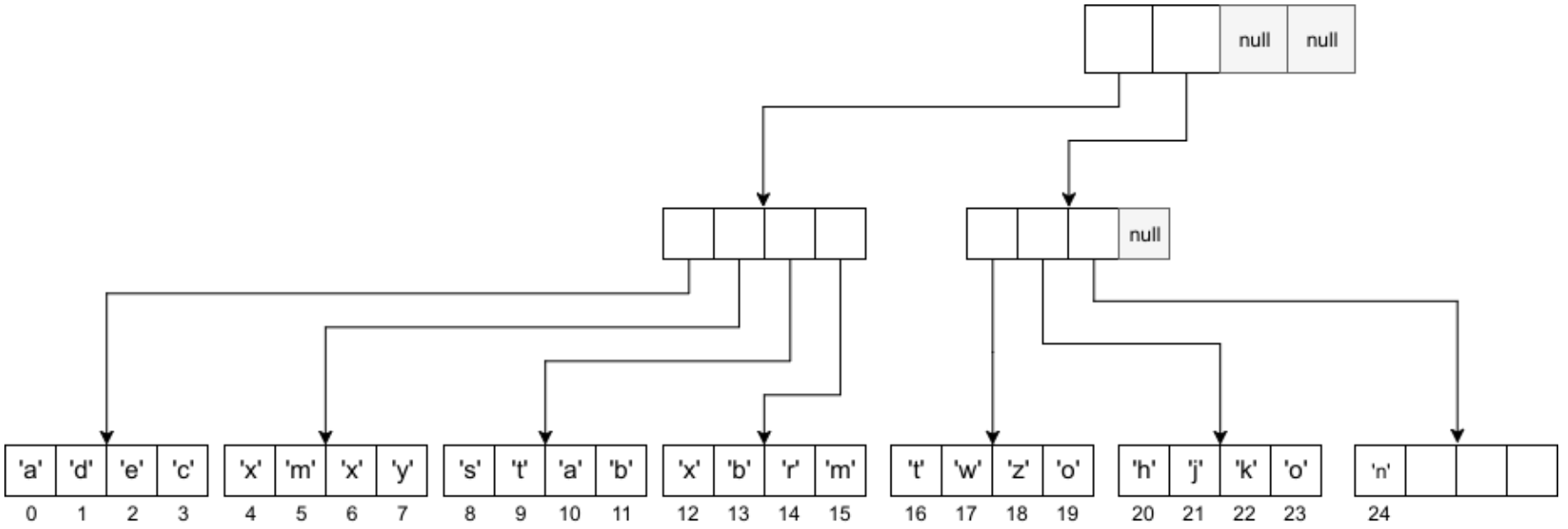
- Scala Vector:
  - (on average) O(1) update
  - (on average) O(1) look-up

- Clojure Vector:
  - O(1) appension
  - O(1) last
  - O(1) pop

[1]

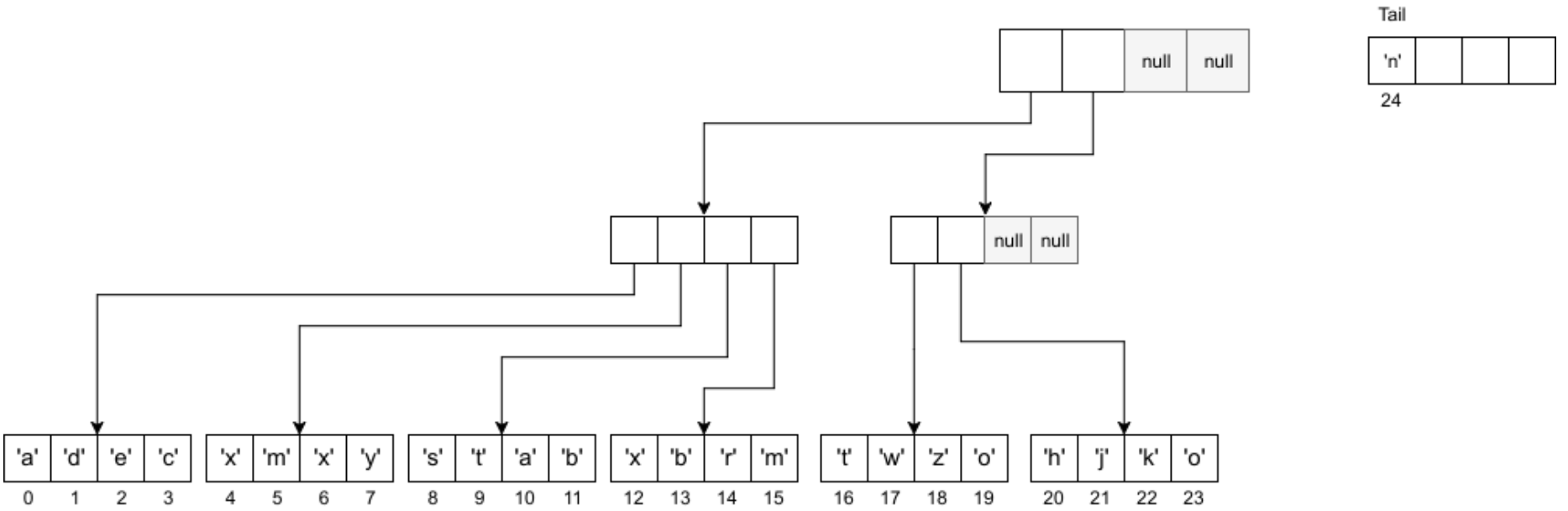
Clojure Vector

- Tail



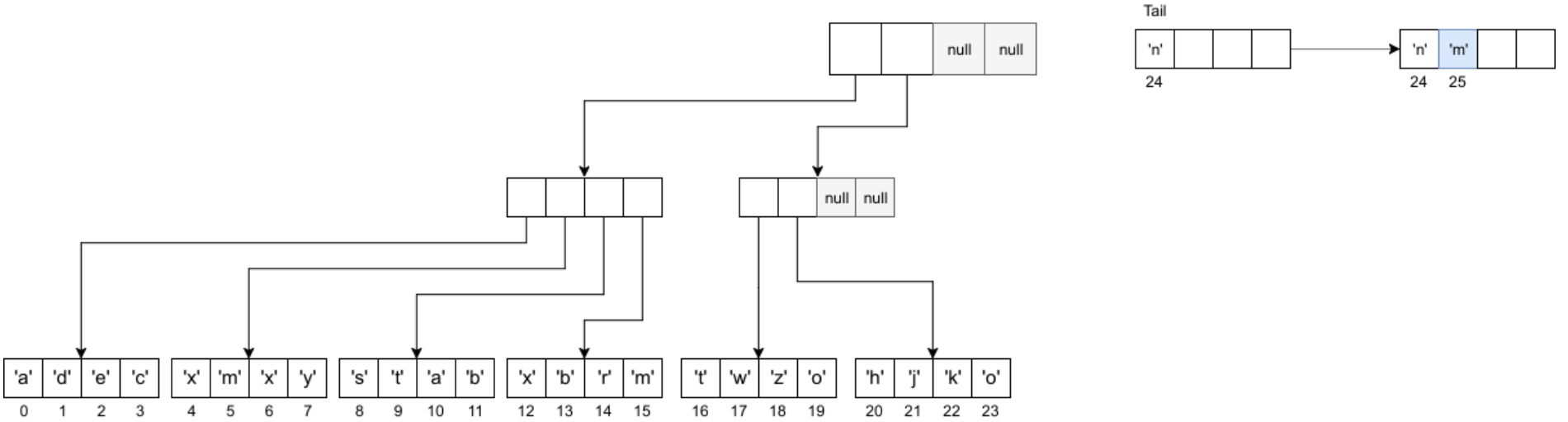
Clojure Vector

- Tail



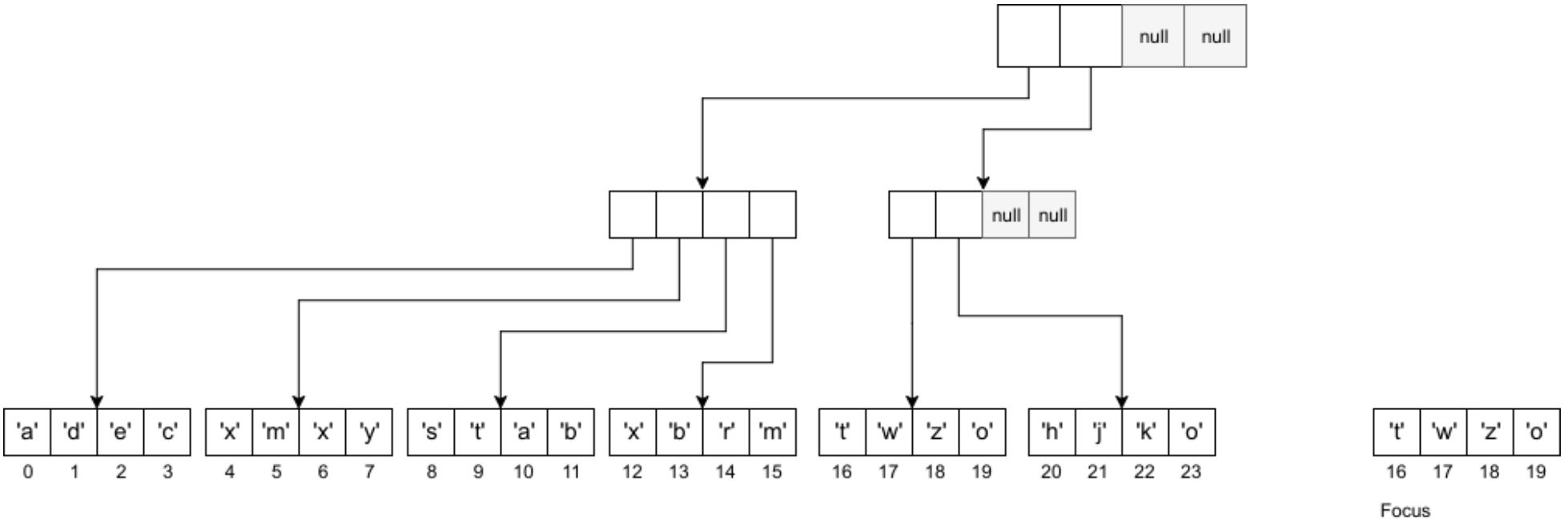
Clojure Vector

- Tail



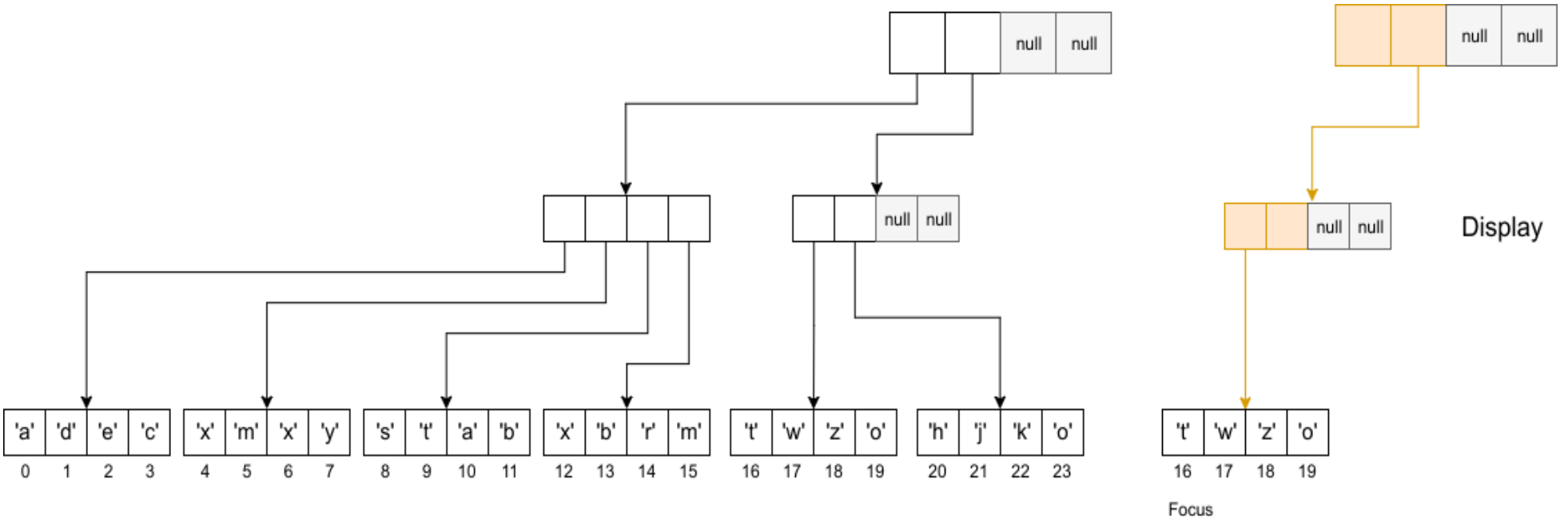
Scala Vector

- Focus



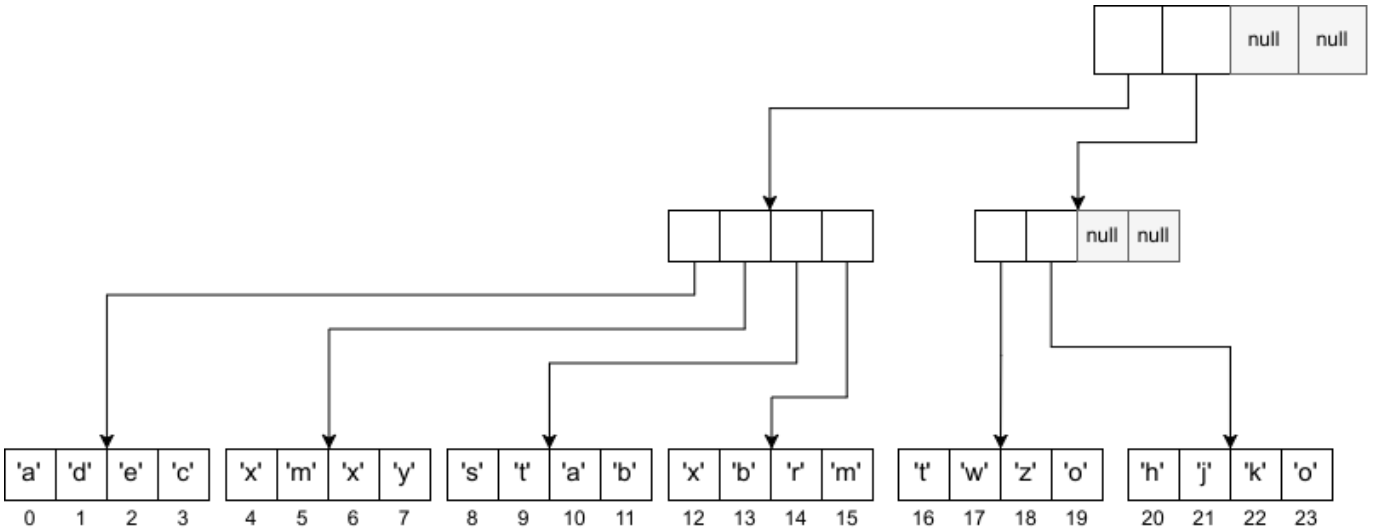
Scala Vector

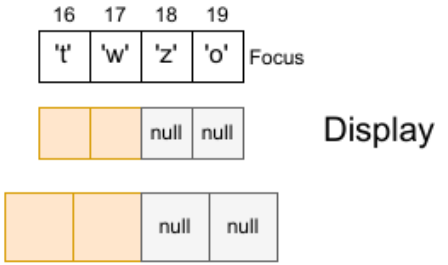
- Focus with Display



Scala Vector

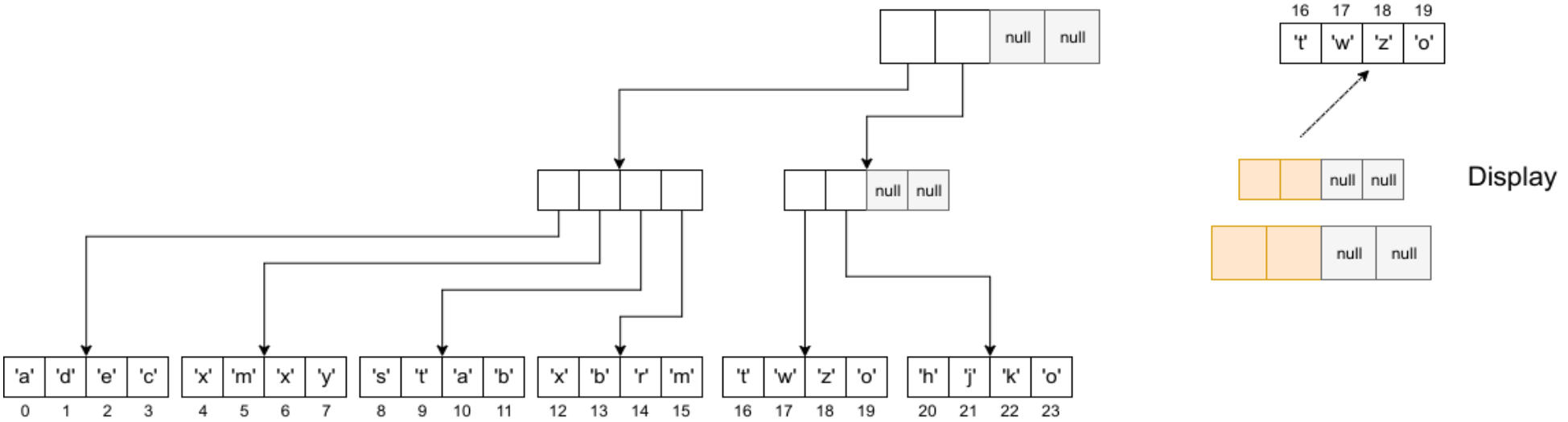
- Focus with Display





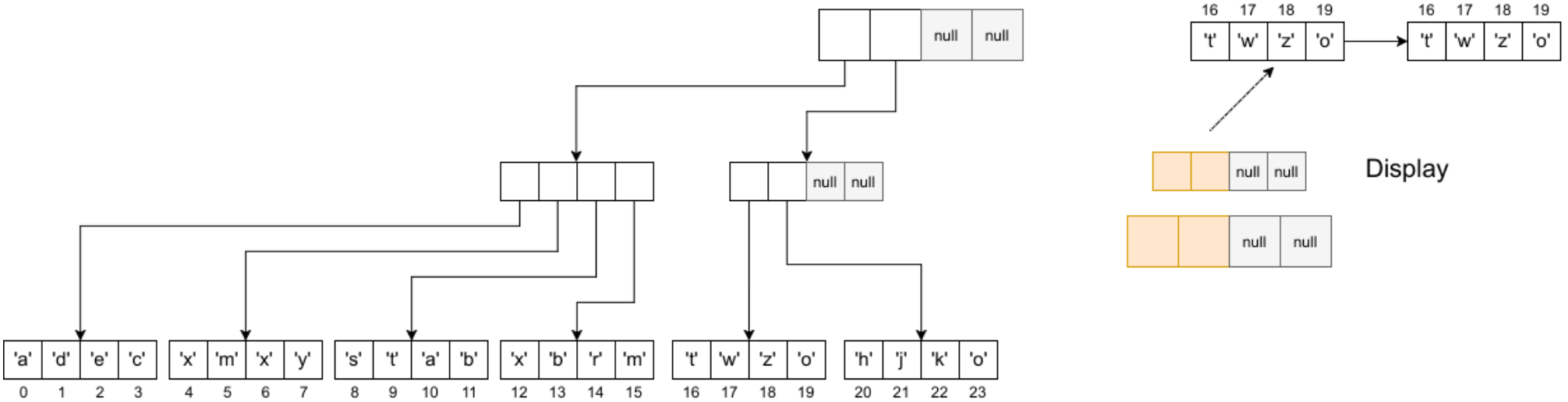
Scala Vector

- Focus with Display



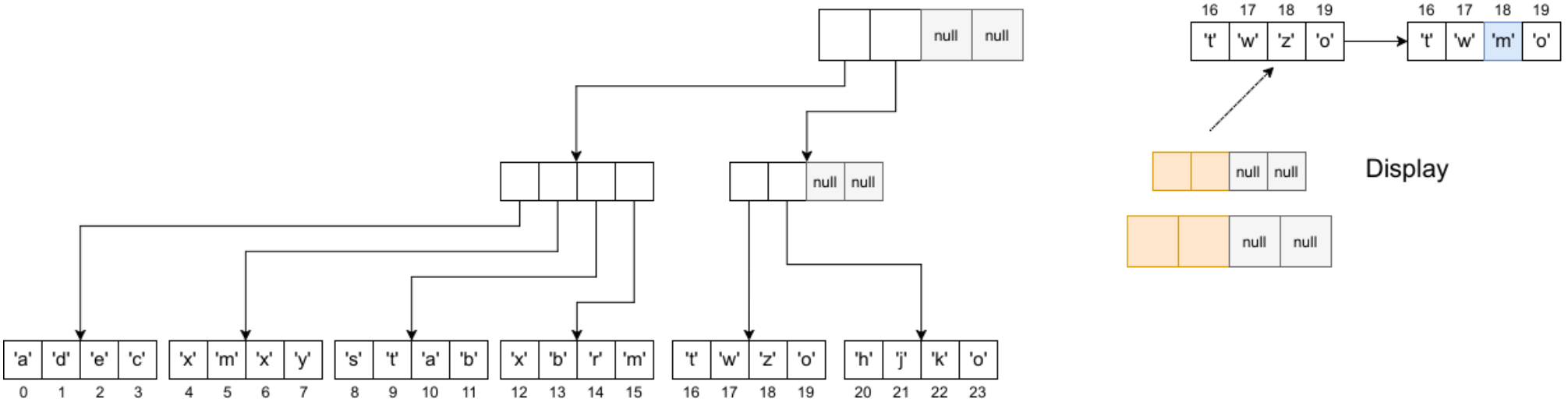
Scala Vector

- Focus with Display



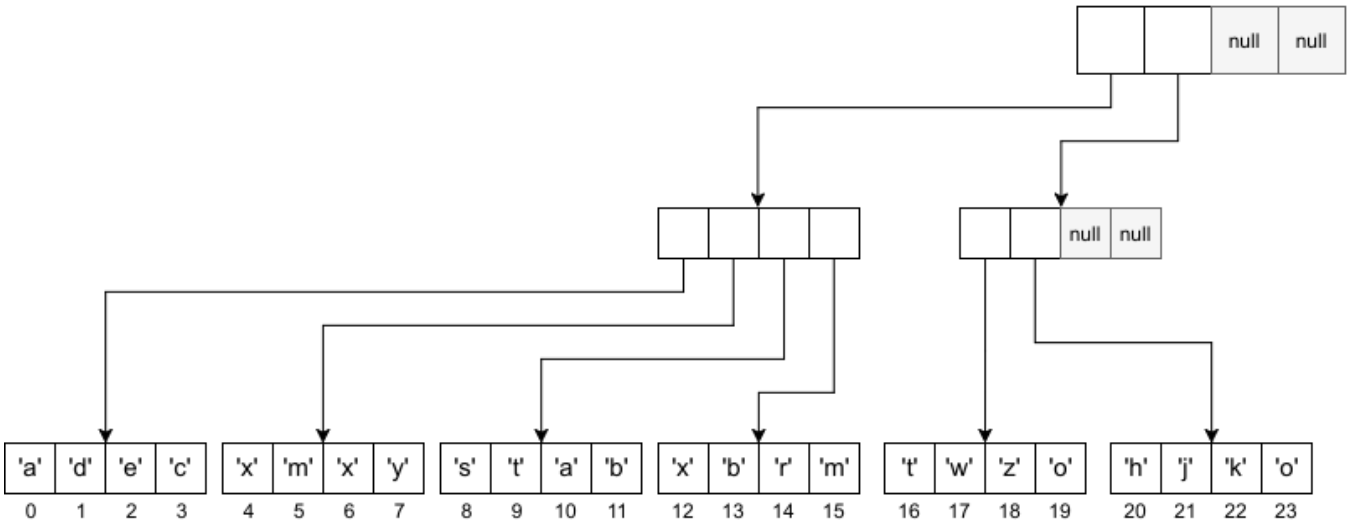
Scala Vector

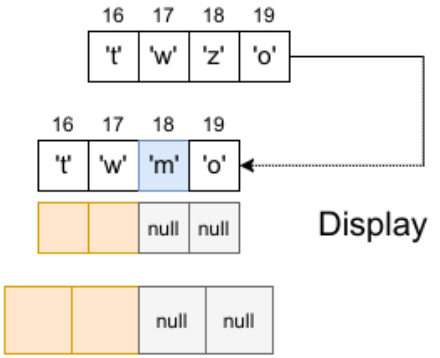
- Focus with Display



Scala Vector

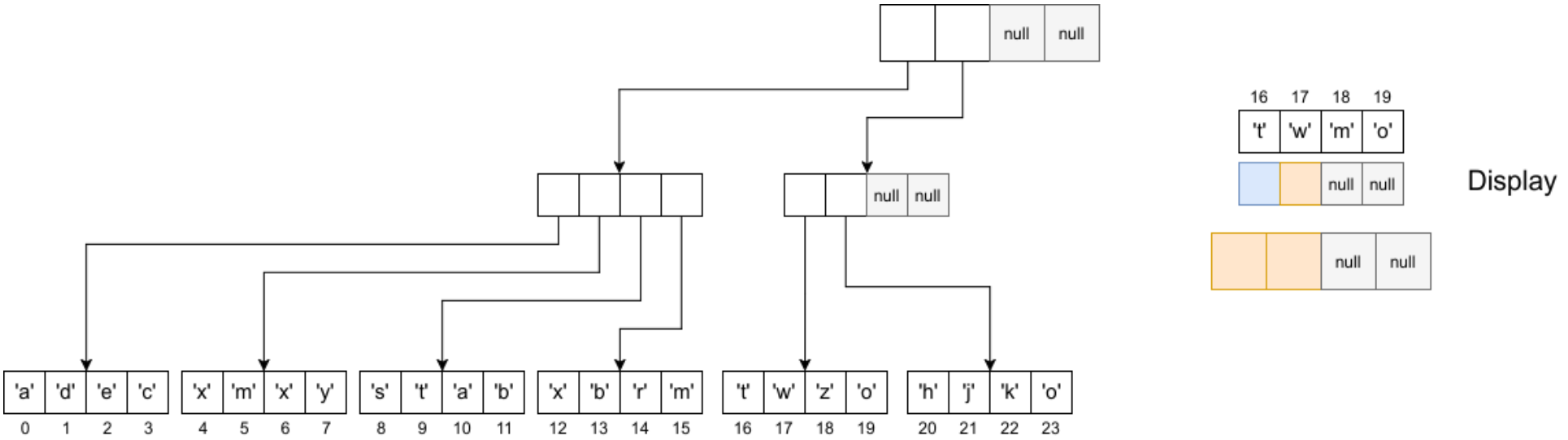
- Focus with Display





Scala Vector

- Focus with Display



Vectors: An Implementation

Thank you!

Presentation: https://github.com/AvramRobert/marvellous-functional-datastructures

[1] https://infoscience.epfl.ch/record/169879/files/RMTrees.pdf