

GATE: IN - 24.2023

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Question: The number of zeroes of the polynomial $P(s) = s^3 + 2s^2 + 5s + 80$ in the right side of the plane? (GATE IN 2023)

Solution:

The table below shows the Routh array of the n^{th} - order characteristic polynomial :

$$a_0 s^n + a_1 s^{n-1} + \dots + a_{n-1} s^1 + a_n s^0 \quad (1)$$

s^n	a_0	a_2	a_4	...
s^{n-1}	a_1	a_3	a_5	...
s^{n-2}	$b_1 = \frac{a_1 a_2 - a_3 a_0}{a_1}$	$b_2 = \frac{a_1 a_4 - a_5 a_0}{a_1}$
s^{n-3}	$c_1 = \frac{b_1 a_3 - b_2 a_1}{b_1}$	\vdots		
\vdots	\vdots	\vdots		
s^1	\vdots	\vdots		
s^0	a_n			

TABLE 1: Routh Array

Characteristic Equation:

$$s^3 + 2s^2 + 5s + 80 = 0 \quad (2)$$

From Table 1:

s^3	1	5
s^2	2	80
s^1	$\frac{2 \times 5 - 80 \times 1}{2} = -35$	
s^0	$\frac{-35 \times 80}{-35} = 80$	

TABLE 2

From Table 2:

Since there are 2 sign changes in the first column of the Routh tabulation. So, the number of zeros in the right half of the s-plane will be 2.

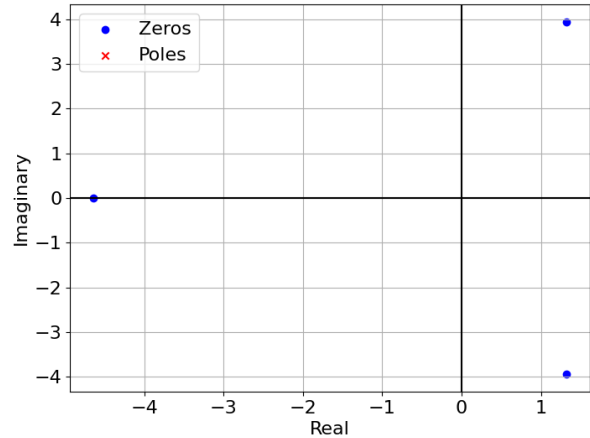


Fig. 1

From equation (2) and Appendix (??) - (??):

$$X(z) = \frac{z^{-1}(1 + 4z^{-1} + z^{-2})}{(1 - z^{-1})^4} + \frac{2z^{-1}(z^{-1} + 1)}{(1 - z^{-1})^3} + \frac{5z^{-1}}{(1 - z^{-1})^2} + \frac{80}{1 - z^{-1}}; |z| > 1 \quad (3)$$

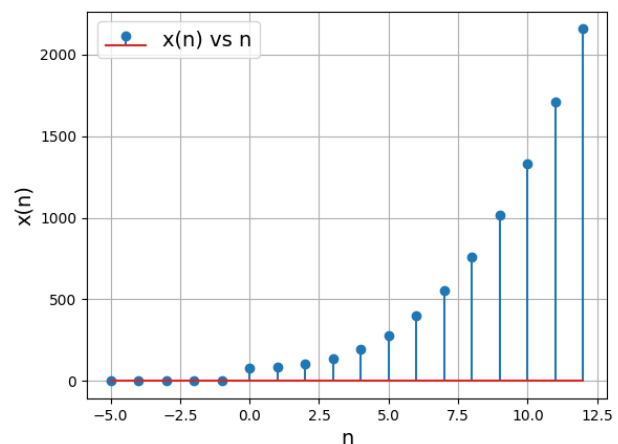


Fig. 2