Note: Deadline: 22.10.20 upto 11:59 PM. Please submit in a single pdf file and write it properly. I want detailed solutions.

- 1. Find all the linear transformations f from  $\mathbb{M}_n(\mathbb{R})$  to  $\mathbb{R}$  such that f(AB) = f(BA) for all matrices  $A, B \in \mathbb{M}_n(\mathbb{R})$ .
- 2. Let  $\mathbb{V}$  be a finite dimensional vector space and let  $\mathbb{W}$  is a subspace of  $\mathbb{V}$ . Then prove that  $\mathbb{W}$  has unique complement if and only if  $\mathbb{S} = \{0\}$  or  $\mathbb{S} = \mathbb{V}$ .