Submission Date: 10.09.2017

ASSIGNMENT - 2

Numerical Solutions of Ordinary and Partial Differential Equations

1. Determine the interval by absolute stability of the following implicit method when applied to the test equation $y' = \lambda y, \lambda < 0$;

$$u_{n+1} = u_n + \frac{h}{4}(K_1 + 3K_2); \quad K_1 = f(t_n, u_n); \quad K_2 = f\left(t_n + \frac{h}{3}, u_n + \frac{h}{3}(K_1 + K_2)\right)$$

- 2. Determine the interval of absolute stability of the following implicit method when applied to the test equation $y' = \lambda y, \lambda < 0$;
 - $u_{n+1} = u_n + \frac{1}{4}(3K_1 + K_2); \quad K_1 = hf(t_n + \frac{h}{3}, u_n + \frac{K_1}{3}); \quad K_2 = hf(t_n + h, u_n + K_1).$

Using this method, find y(1.1) from $y' = t^2 + y^2$, y(1.0) = 2, h = 0.1 (use Newton-Raphson iteration wherever required).

- 3. Solve numerically the equation y' = x + y with the initial conditions x(0) = 0, y(0) = 1 by Milne's method for x = 0.4 with h = 0.1.
- 4. Solve the differential equation $y' = x^3 y^2 2$ using Milne's method for x = 0.3(0.1)(0.6). Initial value x = 0, y = 1. The values of y for x = -0.1, 0.1 and 0.2 are to be computed by third order Taylor series expansion .
- 5. Use Milne's method to solve $\frac{dy}{dx} = y + x$, with initial condition y(0) = 1, from x = 0.20 to x = 0.30 with h = 0.1.
- 6. Given $y' = 2 xy^2$ and y(0) = 10. Show by Milne's method, that y(1) = 1.6505 taking h = 0.2.
- 7. Solve y' = -y with y(0) = 1 by using Milne's method from x = 0.5 to x = 0.8 with h = 0.1
- 8. Solve the initial value problem $\frac{dy}{dx} = x y^2$, y(0) = 1 to find y(0.4) by Adams-Moulton method. With y(0.1) = 0.9117, y(0.2) = 0.8494, y(0.3) = 0.8061.
- 9. Using the Adams-Bashforth formula, determine y(0.4) given the differential equation $\frac{dy}{dx} = \frac{1}{2}xy$, and the data

ux = z = 0				
X	0	0.1	0.2	0.3
У	1	1.0025	1.0101	1.0228

10. Find the value of α with which the linear multistep method

$$u_{n+1} = u_n + \frac{h}{2}(5u'_n + \alpha u'_{n-1})$$

is consistent.