1. Considuter Following Sequen:

Assignment-1: Discrete Mathe.

Submission deadline: 15.2.18.

9,8,4,3,2,7,6,5,10,1.

find the nos. to as defined in the proof of Frdős-Szekeres
Theorem; and use these ti's to find a decreasing Subsequence of at least four terms.

- 2. A building înspertor hors 77 days to make his round. He wants to romane at least one inspection a day, and has 132 inspections to make. Is there a period of consecutive days in which he makes exactly 21
 - 3. There are 3 Slices of olive pizza, 5 Slices of plain pizza, 7 slices of pepperoni pizza and 8 slices of anchory pizza remaining at a pizza panty.
 - (a) How many elices need to be requested to assure that 3 of at least one kind of pizza are received?
 - (b) How many slices need to be requested to assure that 5 slices of anchory are received?
 - 4. The " second order" fibornacci sequence is defined by the rule!

 $U_0 = 0$, $U_1 = 1$, $U_{n+2} = U_{n+1} + U_n + F_n$

ahen frais the n-th fibonacci rumber.

Express Un intermed for and fort1

(Hint: Use generating functions).

5. Show that $\sum_{k} {n \choose k} F_{t}^{k} F_{t-1}^{n-k}$ from its always a fibonacci Mussker, ochen fin in the n-th fibonacci number.

6 .	What is the generating for for the Sequence (= \frac{2^m + 3^m}{2}).
	2,5,13,15,
7.	find ten generating for for { \frac{1}{\text{k(nk)}}, ozken { ozken } differentiate it and exposes the coefficients in terms differentiate it and exposes the coefficients in terms
	differentiate it and exposs the co-efficients in territories
.	of honoric numbers.
	$(11 - 1 + \frac{1}{2} + \frac{1}$

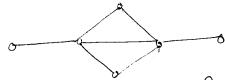
(Hn=1+++3+

8. The laplace transform of a fur. f(x) in the fur.

$$Lf(s) = \int_{0}^{\infty} e^{-st} f(t) dt$$

Civen that a, a, a2, ... in an infinite sequence having a convergent generating fun, let f(x) be the step fun. Express the Laplace transform of f(x)in terrors of the generating for a for this sequence.

- 9. If a in the graph of following figure, express P(a,x) in towns of folynomials P(Ik,x) for various k.
- find the chromatic polynomial for ten following graph using reduction theorem.



A fourt fly in classified as either dominant, hybrid or recessive for eye color. Ten fruit flies one to be chosen for an experiment. In how many different crays can the genetypes (classifications) do so i nant, hybrid, and recessive be chosen if you are interested only in the number of dominants, number of hybrids, and number of recessives?

- 12. Suppose that arother a in suitable for jobs 3,4,5, arother b in suitable for jobs 2,3, and arother c in suitable for jobs 1,5. Also, each worker can be assigned to almost one job, no more than one crocker per job, and a crocker only gets a job to which he or she in Suited. Set up a generating fur. and use it to answer the following questions.
 - a) In how many vaye can he assign one crosker to a job?
 - (b) In how many crays can ere assign two crockers to jobs?
 - (1) In how many crays can eve assign three crakers to jobs?
- 13. Professor Jones crants to teach Calculus I or linear algebra, Professor Smith Crante to teach linear Algebra or Combinatoring and Professor Creen wants to teach Calculus I or Combinatories. Each professor can be assigned to teach at onest one course, with no more than one professor at onest one course, with no more than one professor per course, and a professor only gets a course that he or she crants to teach. Set up a georerating fundance with the answer the following questions.
 - (a) In how many crays can we assign one professor to a course?
 - (b) In how many ways can we assign two professors to cours?
 - (c) In how many crays to can we assign three professors to courses?

 First the mumber of colored 10 10 11
- 14. Find the number of codewords of length k from an alphabet fa, 1, c, d, e 3 if b cerus an odd number of times.

- 15. In how many ways can 200 identical terminals be divided among four computer rooms So that each room will have 20 or 40 or 60 or 80 or 100 terminals?

 (Set up the appropriate generating fun, but do not
 - calculate De teu ansner. Indicate ahat you are looking for, for example, the coefficient of x!)
- 16. In a computer system overhaul, a bank compleyee mistakenly deleted records of soven "pin numbers" belonging to seven accounts. After recreating the records, he assigned those pins to the accounts at random. In how rowny ways could be do this so that at least one pin gets properly assigned.
- 17. Find tu number of devangements of \$1,2,3,4,5,6,7,8} in which the first four elements are mapped into:
 - (a) 1,2,3,4 in some order.
 - (b) 5,6,7,8 in some order.
- 18. A codeword from ten alphabet jo,1,27 is considered legitimate iff no tero 0's appear consecutively. Find a recurrence for ten ouronber on of legitimate codecrads of length n.
- 19. Vie tu onethod of characteristic roots to solve ten Following recurences
 - (a) $a_n = -2a_{n-1} a_{n-2}$, $a_0 = 2$, $a_1 = 2$
 - (b) an=gan-2, a0=4, a1=2.
- 20. Use generating fund to solve each of the recurrences in I(9).
- 21. Suppose that fant satisfies $ma_n = 2 (a_{n-1} + a_{n-2})$, m > 2, and $a_n = e$, $a_1 = 2e$. Let A(x) be the ordinary generating function for fant, (a) show that A'(x) = 2(1+x) A(x).

22. If	$C_{n+1} = 2\pi C_n + \pi C_n + 2$, $n > 0$, and	Co = 1,	find Cn
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23. Solve Simultaneously the recurrences

$$a_{n+1} = a_n + b_n + (n, h > 1)$$

$$b_{n+1} = a_n + b_n + (n, h > 1)$$

$$c_{n+1} = a_n + b_n + (n, h > 1)$$

Subject to the irritial conditions $q = b_1 = q = 1$.

24. Let Dn be the mo. of drevangements of \$1,2,.,n.

Derive a formula for Dn as follows:

(a)
$$u = \frac{Dn}{n!} = \frac{Dn-1}{(n-1)!}$$

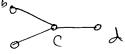
tind a recurrence relation for Cati in teress of Ca

- (b) Some the recurrence for Cn by iteration.
- (e) Use the formula for Cn to solve for Dn.
- 25. Suppose that A(x) is the ordinary generating fun for the sequence fant and B(x) is the ordinary generating fun for the Sequence ? bn?, and that

bn = an-r bo + an-r-1 b1+ · · + ao bn-ro, for n>, k, crha k>, r.

find a relation & involving A(x) and B(x).

26. Use the poinciple of inclusion and exclusion to find the Chromatic polynomial of the following graph.



27. Vie inclusion and exclusion to find the number of Solutions to the equ". 24+23=15

in ashich each xi in a nonnegative integer a and xi=15

28. Write an expression for the perborbility that in a sequence of Trandom digits chosen from 0,1,2,..., 9, exactly 2 of the digits will not appear.

The names on the files of 10 different jeb candidates appearing for an interview ever unfortunately lost, and a new receptist placed the names on the files at random. In how many crays could this be done so that exactly 3 candidates files were labeled properly.

30. Of 100 cars tested at an inspection Station, of had defective headlights, 8 defective breaks, 7 defective horns, 2 defective crindshield cripers, 4 defective headlights and breaks, 3 defective headlights and horns, 2 defective headlights and crindshield cripers, 3 defective breaks and crindshield cripers, 1 defective horn of crindshield cripers, 1 defective headlights, breaks and horn, 1 defective headlight, from and arindshield cripers, rome had any offer combinations of defects.

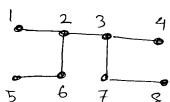
a) How many care have at least one of the defects in question

b) How many can have at least 2 of the defects in question?

() How many can have exactly 2 of the defects in question?

31. I find the number of onto functions from a set with 5 elements to a set with 3 elements.

32. Write down ten Prijfer code of the following Aree:



33. Draw the tree orhere Prinfer code in (1,7,5,7,7,1)

34. In cheeking the nork of a proofreader, we look for 5 kinds
of rosis prints in a textbook. In how many craye can we find
12 misprints.

35. In \$29), suppose ne de not distinguish ten types of sonis points but are do keep a second of ten page on arbich mis point or numed. In how many different arays can are find 25 mispoints in 75 pages.