Assignment - 4

- 1. Using Fourier transform (FT) express the solution of the following initial value problem in terms of difference of two error functions, Ut = C2NXX; - QCX (Q); t>0 $\mathcal{U}(\alpha,0) = \begin{cases} 0, \alpha < \alpha \\ 1, \alpha \leq \alpha \leq \lambda \\ 0, \alpha > \lambda. \end{cases}$
- 2. Solve by applying FT, $u_t = t^2 u_{22}$; $-\infty C \times C \times C \times (t, t)$; $u(2,0) = t(2); -\infty C \times C \times (t, t)$
- 3. Use (FT to solve the equation $\frac{\partial u}{\partial t} = \frac{\partial u}{\partial z}$; O(x < 0), t>0, where u(2,t) satisfies the conditions.
 - 1) $u_{x}(0,t) = 0$, $t \neq 0$ 2) $u(x,0) = \begin{cases} \alpha, 0 < x < 1 \\ 0, x > 1 \end{cases}$ 3) u(x,t) is bounded.
- 4. Using Laplace transform (LT) solve Wtt = uzz; OCZCI, t>0; N(2,0) = Sin TIZ; ux (2,0) = - sin TIX; 0 (2(1.
- 5. Using LT solve una = Lz utt cos wtz 0 < x < 0, $0 \le t < \infty$; u(0,t) = 0, u(x,0) = 0, $u_{\pm}(x,0) = 0$.
- 6. Solve using LT, utt = auxx; 270, t>0; u(2,0)=0, x>0; ux(x,0)=0; x>0; u(0,t)=smut, $\lim_{x\to\infty}\left(\operatorname{ex}(x,t)\right)=0.$

P. T.O.

- 7. Solve by applying FT, $u_{22} + u_{yy} = 0$, $-\infty \in \mathbb{Z} \times \mathbb{Z} \times \mathbb{Z}$, $y \neq 0$. $u(x_10) = \begin{cases} 1, & \alpha \in \mathbb{Z} \times \mathbb{Z$
- 8. Solve, employing appropriate transform technique w. r. to y, the following BVP: Wax + Uyy = 0; 0 (2 (1, 470. $u(0, \forall) = e^{-2 \forall}, u(l, \forall) = 0; \forall > 0; u_{\gamma}(2, 0) = 0.$
- 9. Solve the simultaneous PDE's

 $\frac{\partial u}{\partial x} = -2v, \quad \frac{\partial v}{\partial x} = \frac{1}{2} \frac{\partial u}{\partial t}.$

Here u = u(x,t), v = v(x,t): given conditions · α · α

10. Solve xyx+yt-y=x2, x70, t70; Y= Y(x,t). subject to the boundary conditions y(0, t)=0, 4(7,0)=0,