Tutorial Sheet-9 (Hints and Answers)

MATHEMATICS-II (MA10002)

- 1. Hints: Compute the ranges of x, y and then calculate double integral accordingly.

 - (i) Ans: $\frac{a^4}{3}$ (ii) Ans: $\frac{e^4}{2} 2e$ (iii) Ans: $\frac{55}{156}$ (iv) Ans: $\frac{-935}{3}$
- 2. Hints: In change of order of integration, first integrate the integrand with respect to x and then integrate with respect to y under a suitable range.
 - (i) Ans: $\frac{16a^2}{3}$
 - (ii) Ans:1 $-\frac{1}{\sqrt{2}}$
 - (iii) Ans: $\frac{1}{12}(e^{729} 1)$
 - (iv) Ans: $\frac{1}{16}(17^{1.5} 1)$
- 3. Hints: Using the transformation T find jacobian and ranges of u and v and then integrate with respect to u and v. Ans: $\frac{1}{2}(e-1)$
- 4. (i) Ans: $\frac{-1}{2}$
 - (ii) Hints: Compute the ranges of u, v after using the transformation. Ans: $-\pi^3$
- 5. (i) Hints: Use the transformation x = 2u and y = 3v. Ans: 6π
 - (ii) Hints: Use the transformation $x = \frac{u^2}{v}$ and $y = \frac{v}{u}$. Ans: $\frac{3}{4}$
 - (iii) Hints: Use the transformation u = x + y and v = 2x y. Ans: $\frac{1}{3}$
- 6. Ans: $\frac{16}{3}a^2$
- 7. Ans: 16
- 8. Ans: $\frac{2}{3}\pi ab(2^{1.5}-1)$
- 9. Ans: 31.6