

Problem Set 5, Part I

Problem 1: Sorting practice

1-1) {3, 4, 18, 24, 33, 40, 8, 10, 12}

1-2) {4, 10, 18, 24, 33, 40, 8, 3, 12}

1-3) {4, 10, 18, 8, 3, 12, 24, 33, 40}

1-4) {10, 18, 4, 24, 12, 3, 8, 40, 33}

1-5) {10, 18, 4, 8, 12, 3, 24, 40, 33}

1-6) {4, 10, 18, 24, 33, 40, 8, 3, 12}

Problem 2: Practice with big-O

2-1)

function	big-O expression
$a(n) = 5n + 1$	$a(n) = O(n)$
$b(n) = 5 - 10n - n^2$	$b(n) = O(n^2)$
$c(n) = 4n + 2\log(n)$	$c(n) = O(n)$
$d(n) = 6n\log(n) + n^2$	$d(n) = O(n^2)$
$e(n) = 2n^2 + 3n^3 - 7n$	$e(n) = O(n^3)$

2-2)

$O(n^2)$

This is because there are three nested for loops which depend on the previous for loop for their length. However, the first for loop only repeats three times regardless of n and hence does not really matter in the context of Big O.

2-3)

$O(n^2)$

Technically, the nested for loops should give you a $O(n * n/2)$ due to the second loop only iterating for half of the n elements. However, this simplifies to $O(n^2)$ since the expression above is closer to $O(n^2)$ than to $O(n)$. You can see this more clearly in a graphing software where $n*n/2$ is a lot closer to n^2 than to n .

Problem 3: Comparing two algorithms

worst-case time efficiency of algorithm A: $O(n^2)$

Explanation: Since the outer for loop can traverse from 0 to $n-1$, the inner loop can go from $i+1$ to n , and the inner loop is nested within the outer loop, then we can get the expression of $O(n \cdot n)$ which can then just be simplified to $O(n^2)$.

worst-case time efficiency of algorithm B: $O(n \log n)$

Explanation: The first mergesort call has a worst case scenario of running at $O(n \log n)$. The loop after that runs from 1 to n which yields a running time of $O(n)$. Combining these we get the expression $O(n + n \log n)$ which can then be simplified to $O(n \log n)$.

Problem 4: Practice with references

4-1)

Expression	Address	Value
n	0x100	0x712
n.ch	0x712	'n'
n.prev	0x718	0x064
n.prev.prev	0x070	0x360
n.prev.next.next	0x714	null
n.prev.prev.next	0x362	0x064

4-2)

```
n.prev = x;  
n.prev.next = x;  
x.next = n;  
x.prev = n.prev
```

4-3)

```
public static void initPrevs(DNode one){  
    DNode trav = one;  
    DNode trail = null;  
    while (trav != null && trav.ch < ch) {  
        trav.prev = trail;  
        trail = trav;  
        trail = trail.next;  
    }  
}
```