The Digital Abstraction

Building Digital Systems in an Analog World

Reminders:

- Lab 1 due today
- Late day policy
- Sign up for Lab 1 checkoff meeting

6.004 Course Outline

Module 1: Assembly language

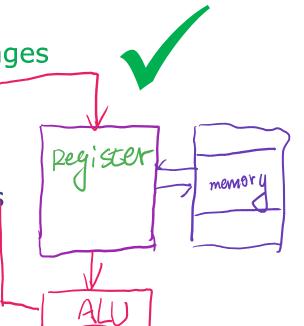
 From high-level programming languages to the language of the computer

Module 2: Digital design

Combinational and sequential circuits

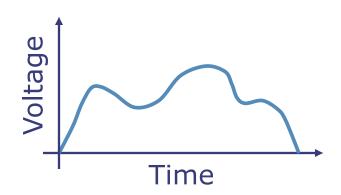
Module 3: Computer architecture

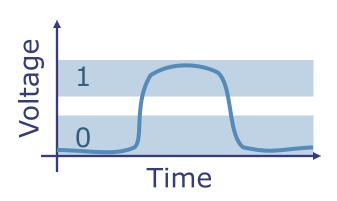
- Simple and pipelined processors
- Caches and the memory hierarchy
- Module 4: Computer systems
 - Operating system and virtual memory
 - Parallelism and synchronization



Analog vs. Digital Systems

- Analog systems represent and process information using continuous signals
 - e.g., voltage, current, temperature, pressure, ...
- Digital systems represent and process information using discrete symbols
 - Typically binary symbols (bits)
 - Encoded using ranges of a physical quantity (e.g., voltage)





Representing Information with Voltage

Representation of each point (x, y) on a B&W Picture:

0 volts: BLACK

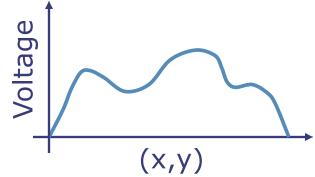
1 volt: WHITE

0.37 volts: 37% Gray

etc.



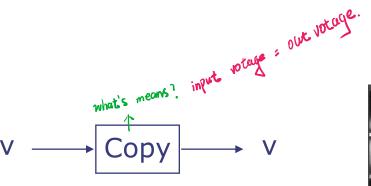
Representation of a picture:
Scan points in some prescribed order... generate voltage waveform



Information Processing = Computation

First let's introduce some processing blocks:





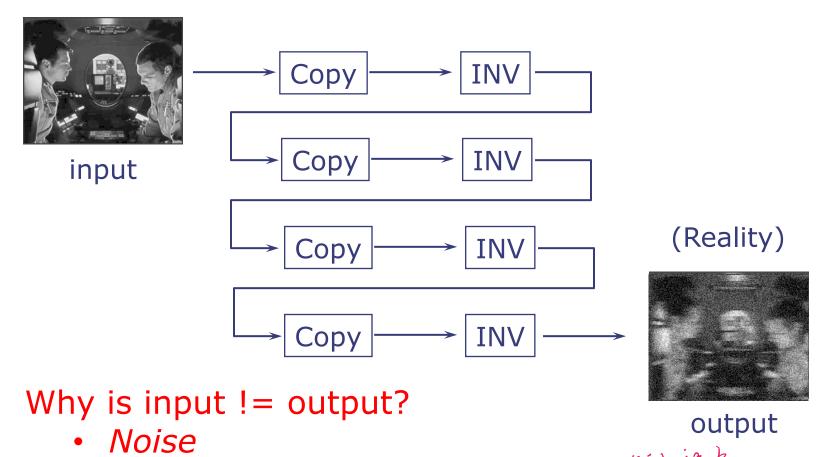








Let's Build a System!



· Manufacturing variations 处理代程的过程中

Components degrade over time 确件发化。

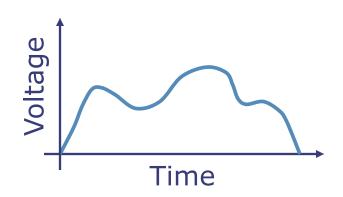
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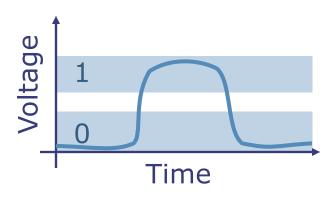
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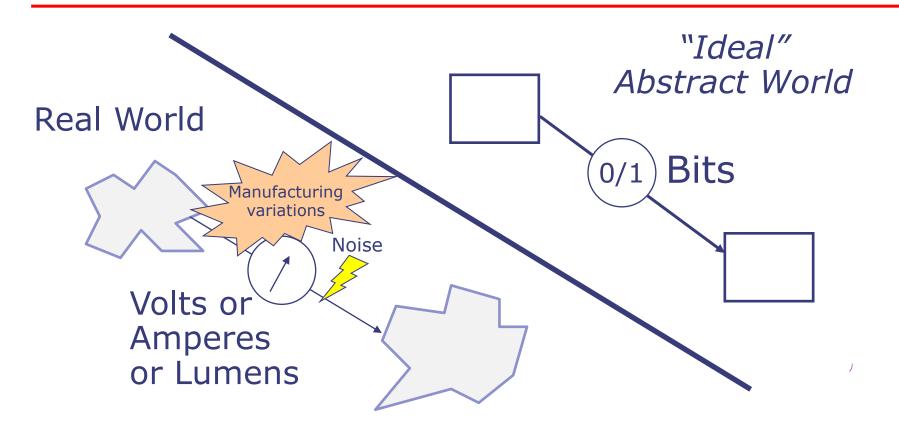
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Digital systems tolerate noise

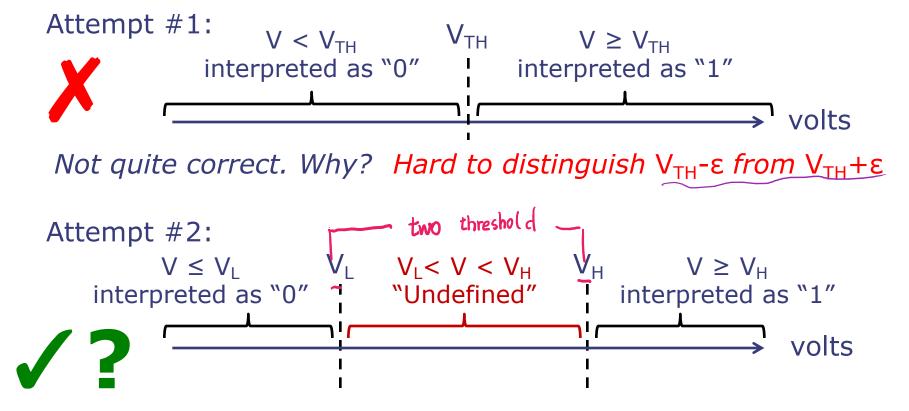
The Digital Abstraction



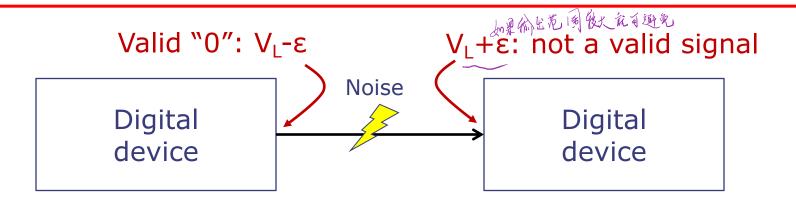
Keep in mind that the world is not digital, we would simply like to engineer it to behave that way. In the end we must use real physical phenomena to implement digital designs!

Using Voltages "Digitally"

- Key idea: Encode two symbols, "0" and "1" (1 bit)
- Use the same convention for every component and wire in our digital system



Will This System Work?



Upstream device transmits a signal at V_L - ϵ , a valid "0". Noise on the wire causes the downstream device to receive V_L + ϵ , which is undefined.

How can we address this?

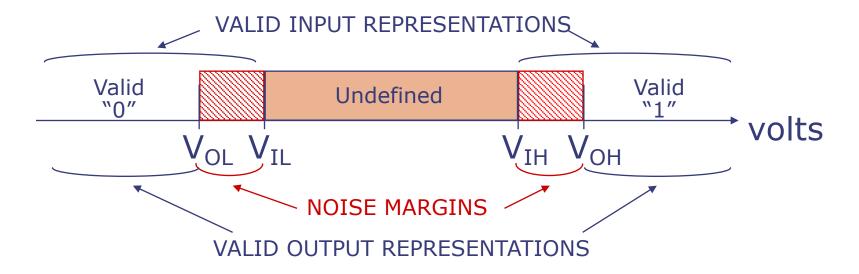
Output voltages should use narrower ranges, so that signal will still be valid when it reaches an input even if there is noise.

Noise Margins

提出

Proposed fix: Different specifications for inputs and outputs

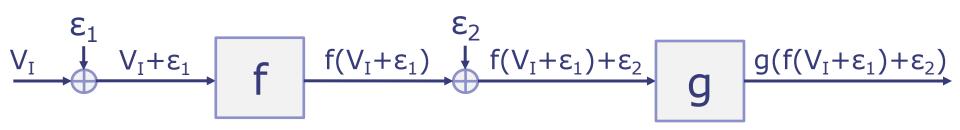
- Digital output: "0" ≤ V_{OL}, "1" ≥ V_{OH}
- Digital input: "0" \leq V_{IL}, "1" \geq V_{IH}
- $\cdot V_{OL} < V_{IL} < V_{IH} < V_{OH}$



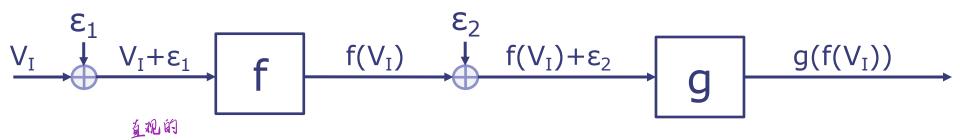
A digital device accepts marginal inputs and provides unquestionable outputs (to leave room for noise).

Digital Systems are Restorative

Analog systems: Noise accumulates



Digital systems: Noise is canceled at each stage

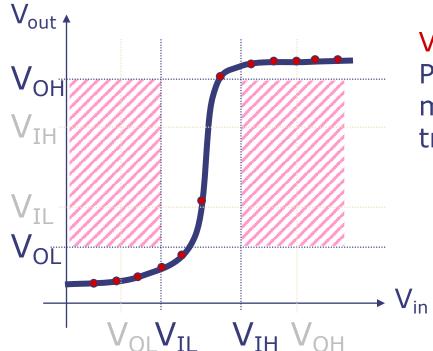


Intuitively, canceling noise requires active components, i.e., components that inject energy into the system

Voltage Transfer Characteristic

Buffer: A simple digital device that copies its input value to its output

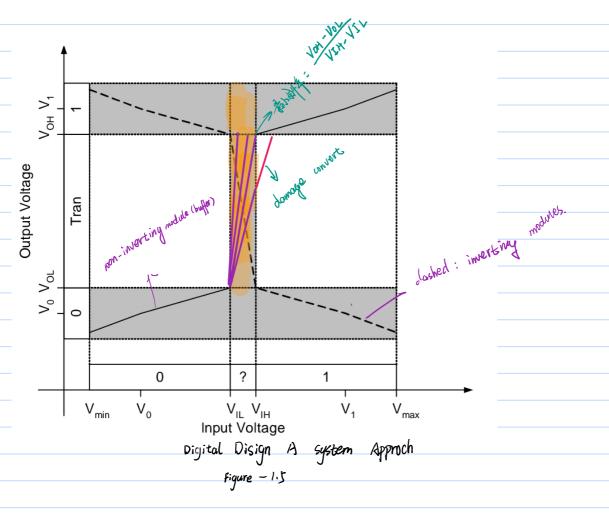




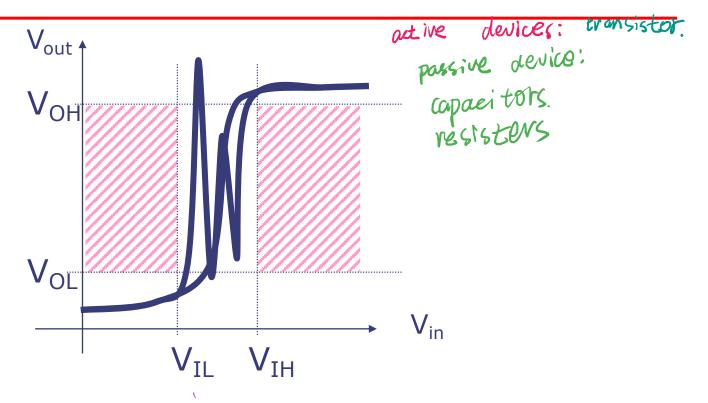
Voltage Transfer Characteristic (VTC): Plot of V_{out} vs. V_{in} where each measurement is taken after any transients have died out.

Note: VTC does not tell you anything about how fast a device is — it measures static behavior, not dynamic behavior.

VTC must avoid the shaded regions (aka "forbidden zones"), which correspond to valid inputs but invalid outputs.



Voltage Transfer Characteristic



- 1)Note the center white region is taller than it is wide $(V_{OH}-V_{OL} > V_{IH}-V_{IL})$. Net result: device must have GAIN > 1 and thus be ACTIVE
- 2) Note the VTC can do anything when $V_{\rm IL} < V_{\rm IN} < V_{\rm IH}$

Types of Digital Circuits



- Combinational circuits
 - Do not have memory
 - Each output is a function of current input values
 - Examples: Inverter 0
 1
 0
 1
 0
 0
 0
 0
 0
 0
 0
 0
 0
 0
 0
 0
 0
 0
 0
 0
 0
 0
 0
- Sequential circuits
 - Have memory, i.e., state
 - Each output depends on current state + current inputs

Digital Abstraction Problem

Suppose that you measured the voltage transfer curve of the device shown below. Can we find a signaling specification (V_{IL} , V_{IH} , V_{OL} , V_{OH}) that

would allow this device to

be a digital inverter?

$$V_{OL} < V_{IL} < V_{IH} < V_{OH}$$

$$V_{in} \leq V_{IL}$$
 $V_{IL} = 1$ 以什么不能能证。

$$V_{in} \ge V_{IH}$$

$$V_{IH} = 3$$

Low NM = 0.5

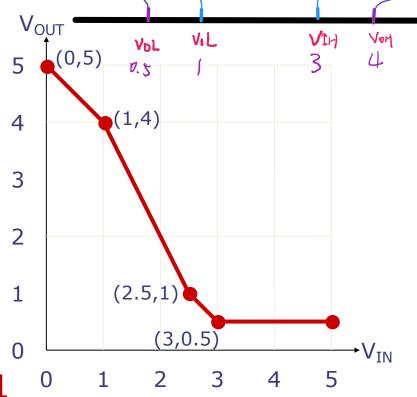
$$V_{out} \ge V_{OH}$$

$$V_{OH} = 4$$

$$V_{out} \le V_{OL}$$

$$V_{OL} = 0.5$$

High NM = 1

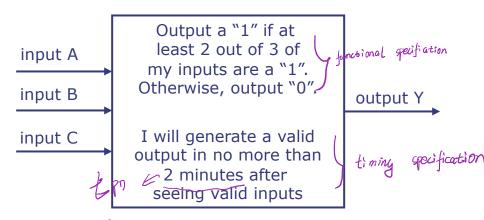


Introduction to Combinational Circuits

Combinational Devices

A <u>combinational device</u> is a circuit element that has

- one or more digital inputs
- one or more digital outputs
- a functional specification that details the value of each output for every possible combination of valid input values
- a timing specification consisting (at a minimum) of a propagation delay (t_{PD}): an upper bound on the required time to produce valid, stable output values from an arbitrary set of valid, stable input values



Static discipline

February 20, 2020

Composing Combinational Devices

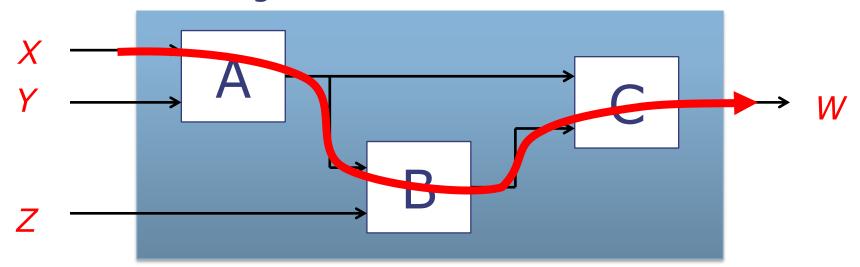
A set of interconnected elements is a combinational device if

- each circuit element is combinational
- every input is connected to exactly one output or to a constant (0 or 1)
- the circuit contains no directed cycles



Example: Is This a Combinational Device?

A, B, and C are combinational devices. Is the following circuit a combinational device?



Does it have digital inputs? Yes

Does it have digital outputs? Yes

Can you derive a functional description?

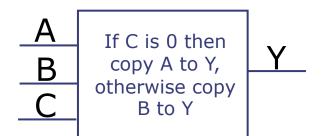
 $W = f_C(f_A(X, Y), f_B(f_A(X, Y), Z))$ Can you derive a t_{PD} ? $t_{PD} = t_{PD,A} + t_{PD,B} + t_{PD,C}$ February 20, 2020

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Functional Specifications

 There are many ways to specify the function of a combinational device



- We will use two systematic approaches:
 - Truth tables enumerate the output values for all possible combinations of input values
 - Boolean expressions are equations containing binary (0/1) variables and three operations: AND (⋅), OR (+), and NOT (overbar)

$$Y = \bar{C} \cdot A + C \cdot B$$

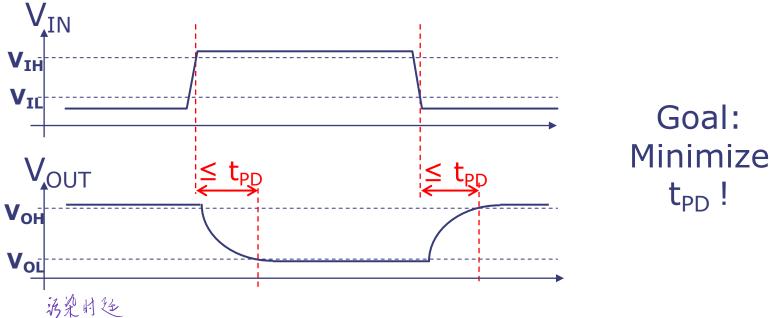
Truth Table

C	В	Α	Y
0	0	0	0
0	0	1	1
0	1	0	0
0	1	1	1
1	0	0	0
1	0	1	0
1	1	0	1
1	1	1	1

Any combinational function can be specified as a truth table or Boolean expression (next lecture)

Timing Specifications

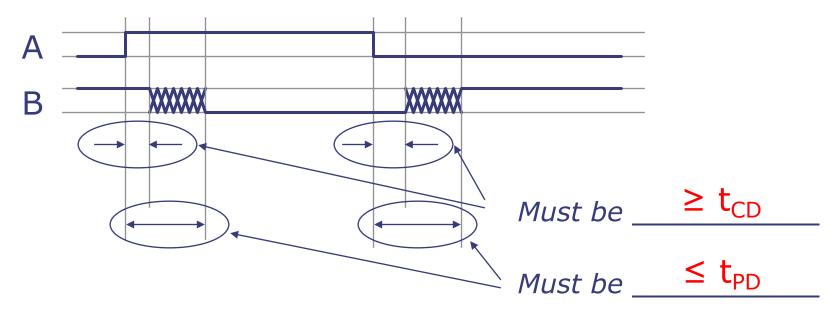
 Propagation delay (t_{PD}): An upper bound on the delay from valid inputs to valid outputs



- Contamination delay (t_{CD}): A lower bound on the delay from invalid inputs to invalid outputs
 - Used later (for sequential logic), can ignore for now

The Combinational Contract





No promises during XXXXX

Summary

- Digital systems tolerate noise
- Digital encoding
 - Valid voltage levels for representing "0" and "1"
 - Undefined range avoids mistaking "0" for "1" and vice versa
 - Noise margins require tougher standards for outputs than for inputs
- Combinational devices
 - Have Tinkertoy-set simplicity, modularity
 - Predictable composition: "parts work → whole thing works"
 - Must obey static discipline
 - Digital inputs & outputs: restores marginal input voltages
 - Complete functional specification
 - Valid inputs lead to valid outputs in bounded time

Thank you!

Next lecture: Boolean Algebra