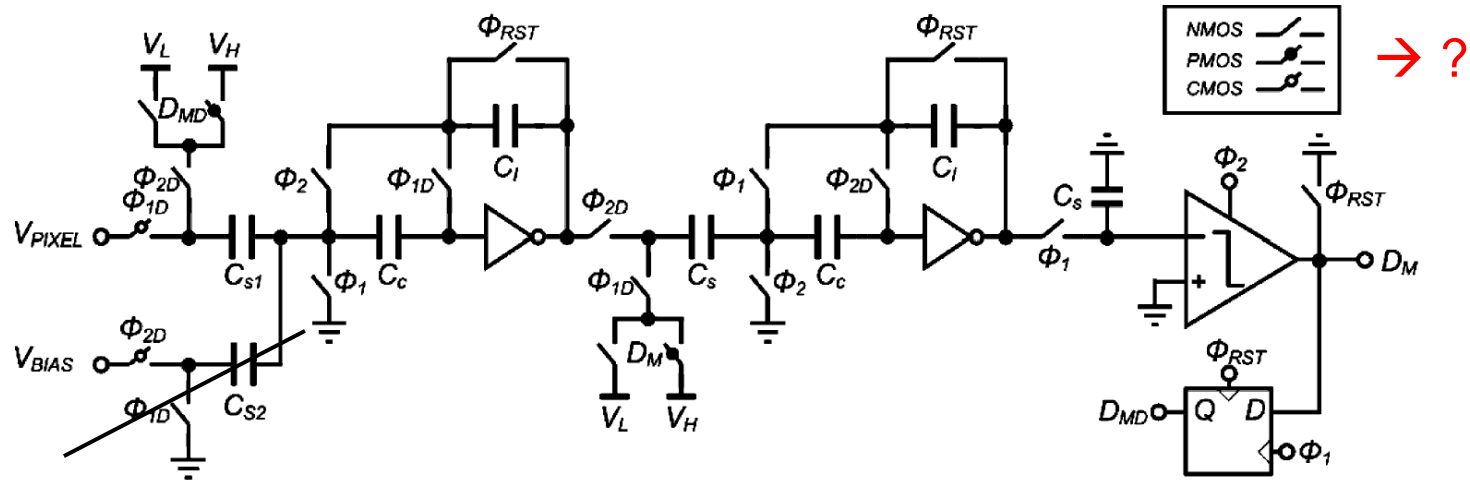


# Switches

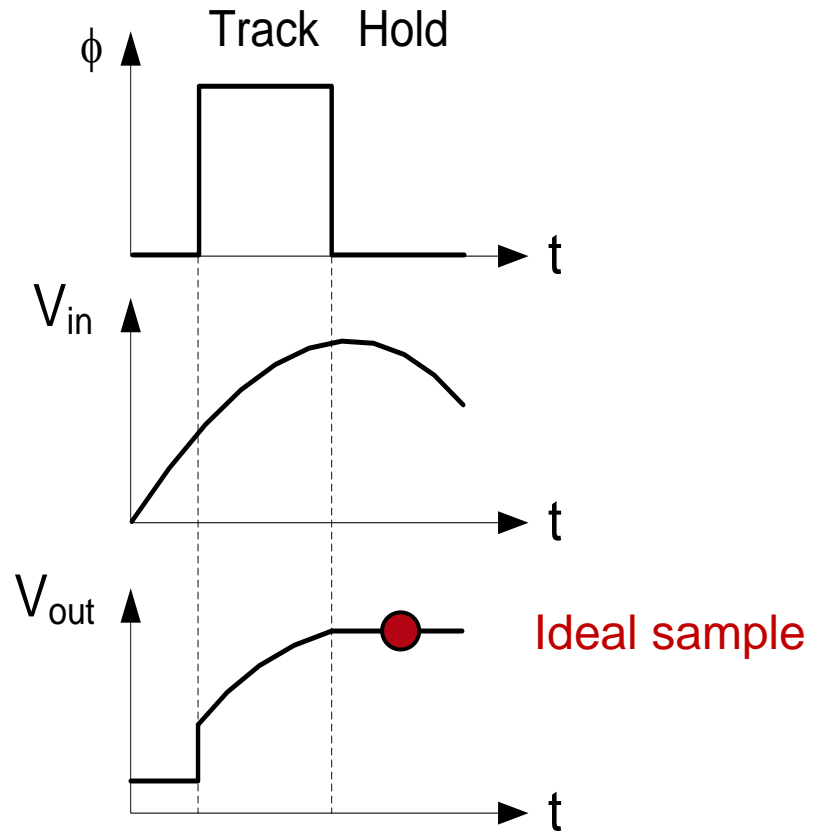
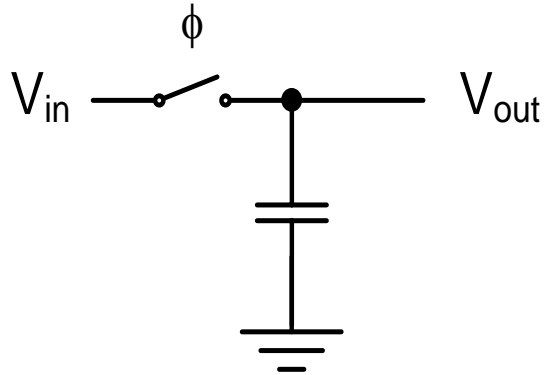
**Boris Murmann**  
**[bmurmann@hawaii.edu](mailto:bmurmann@hawaii.edu)**

# Motivation



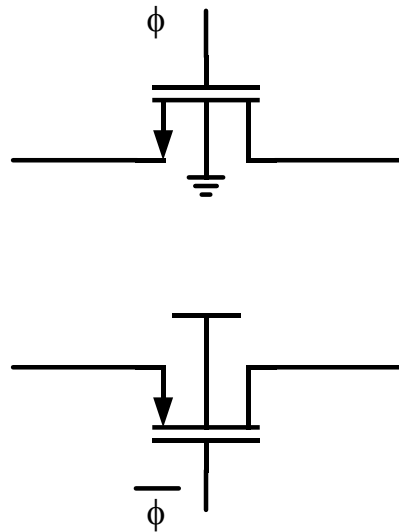
- The last piece of our circuit that needs to be transistorized are the switches and the clock generator

# Ideal Switch Operation

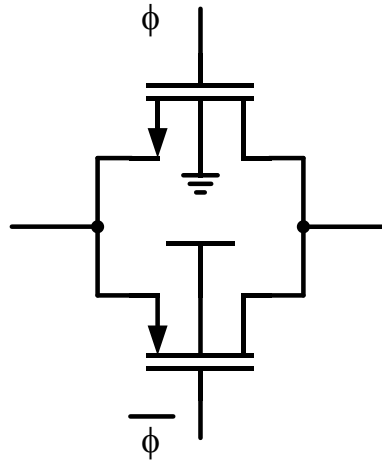


# Common Switch Implementation Options

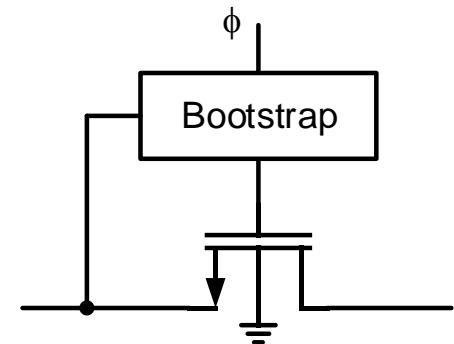
NMOS or PMOS



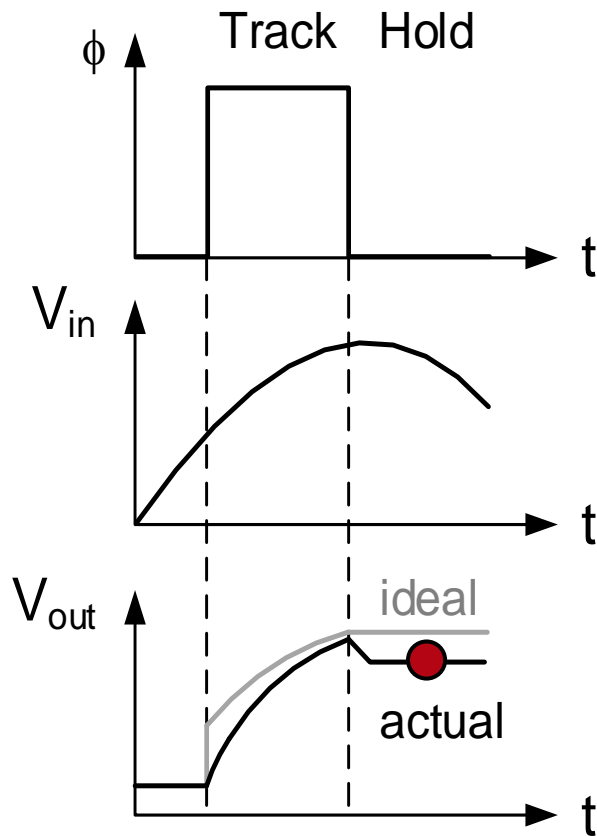
CMOS  
(transmission gate)



Bootstrapped NMOS  
(advanced concept)



# Long List of Nonidealities



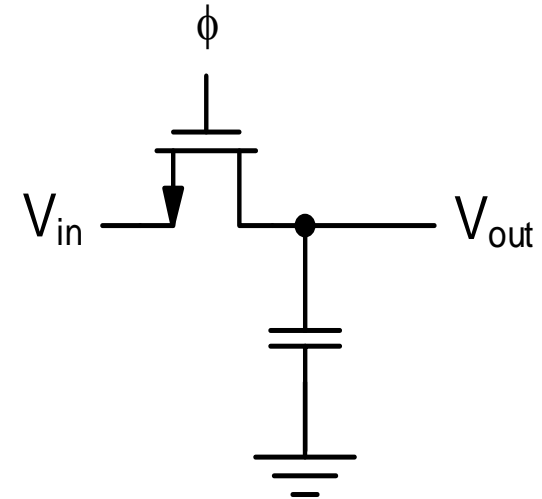
- Sampling noise ( $kT/C$ )
  - Finite on resistance
  - Charge injection and clock feedthrough
  - Clock jitter
  - Tracking nonlinearity
  - Hold-mode feedthrough and leakage
- 
- As a result, samples contain
    - Offset
    - Noise
    - Nonlinear errors (distortion)

# On-Resistance of NMOS Switch

$$I_D \approx \mu C_{ox} \frac{W}{L} \left( V_{GS} - V_t - \frac{V_{DS}}{2} \right) V_{DS}$$

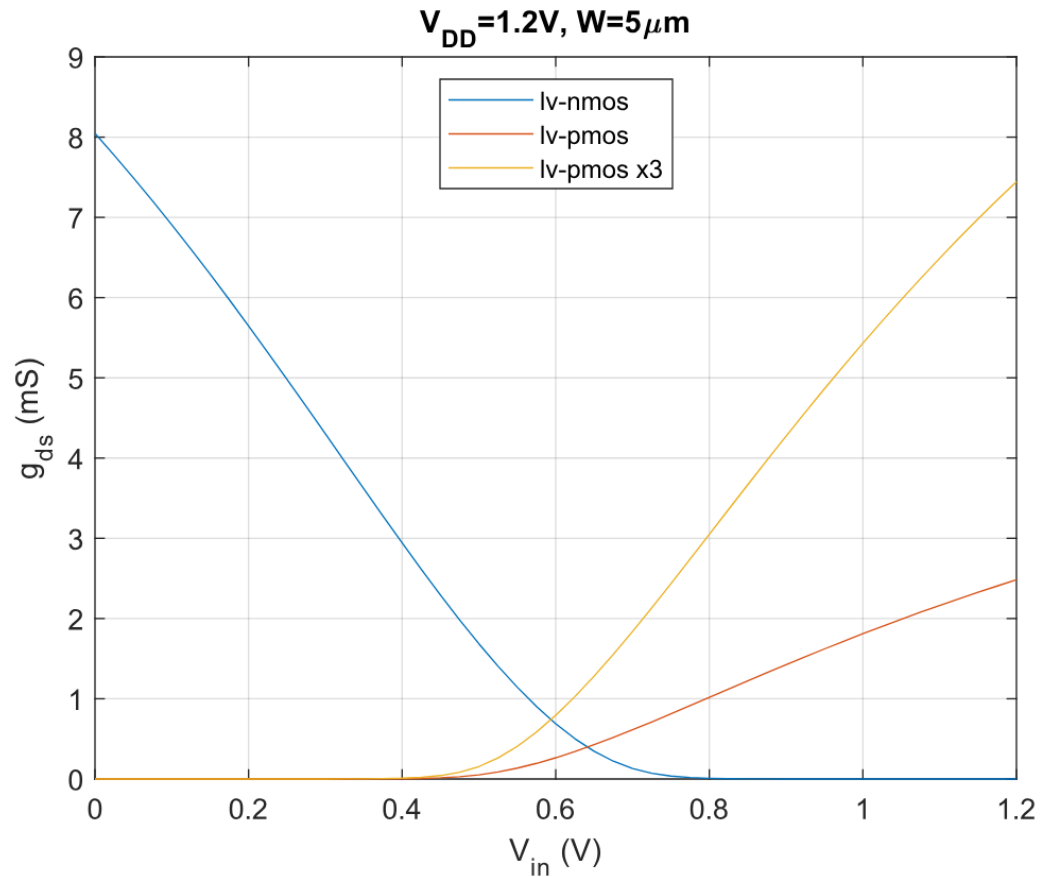
$$r_{ds} \approx \left[ \frac{dI_D}{dV_{DS}} \Big|_{V_{DS} \rightarrow 0} \right]^{-1} = \frac{1}{\mu C_{ox} \frac{W}{L} (V_{GS} - V_t)}$$

$$r_{ds} \approx \frac{1}{\mu C_{ox} \frac{W}{L} (\phi - \mathbf{V_{in}} - V_t)} \quad g_{ds} = \frac{1}{r_{ds}}$$



- The on-resistance varies with  $V_{in}$ 
  - NMOS switch works well for low  $V_{in}$
  - PMOS switch works well for high  $V_{in}$

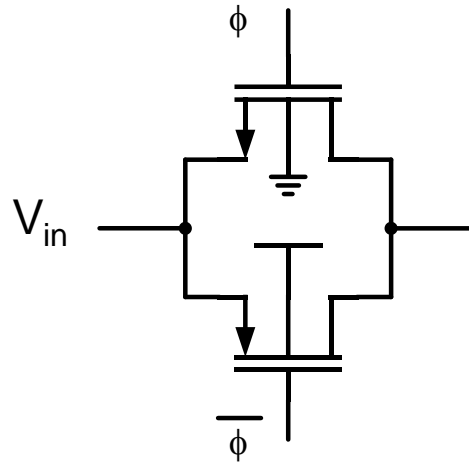
# Simulation of NMOS/PMOS Switches in IHP Technology



[https://github.com/bmurmnn/EE628/tree/main/4\\_Technology/6\\_ron\\_tgate](https://github.com/bmurmnn/EE628/tree/main/4_Technology/6_ron_tgate)

# CMOS Switch (Transmission Gate)

- For increasing  $V_{in}$ , NMOS resistance increases, but PMOS resistance decreases → sounds great!



In the on-state:

$$V_{GSn} = V_{DD} - V_{in}$$

$$V_{SGp} = V_{IN}$$

$$r_{on} = \frac{1}{\mu_n C_{ox} \frac{W_n}{L_n} (V_{GSn} - V_{tn})} \parallel \frac{1}{\mu_n C_{ox} \frac{W_n}{L_n} (V_{SGp} - |V_{tp}|)}$$



- Assuming “equal strength” sizing, such that

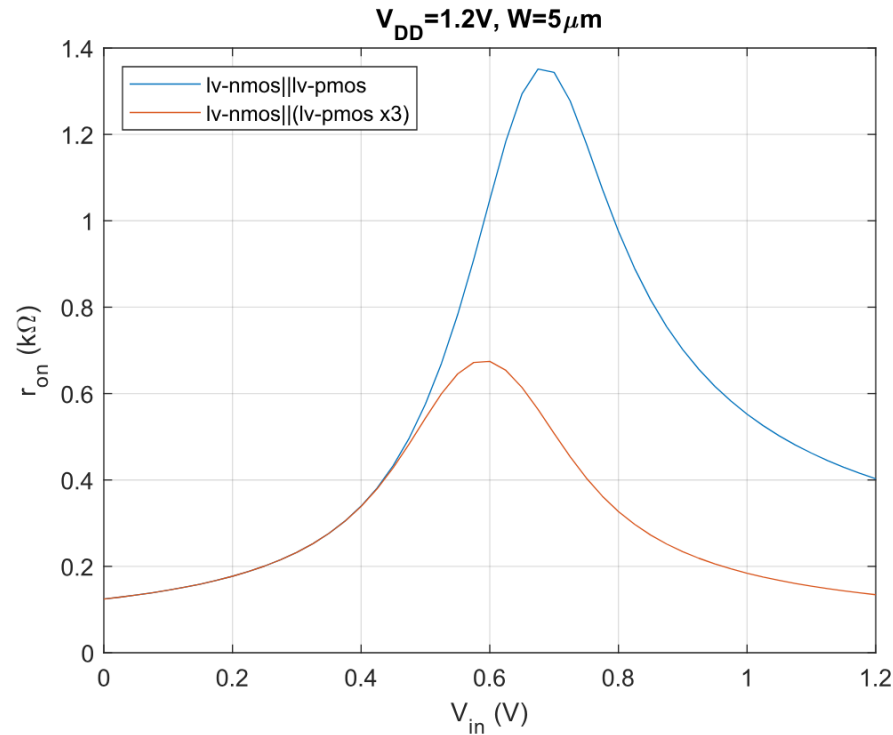
$$\mu_n C_{ox} \frac{W_n}{L_n} = \mu_p C_{ox} \frac{W_p}{L_p}$$

we find

$$r_{on} = \frac{1}{\mu_n C_{ox} \frac{W_n}{L_n} (V_{DD} - V_{tn} - |V_{tp}|)}$$

- Independent of  $V_{in} \rightarrow$  too good to be true!
- Missing factors
  - Backgate effect
  - Short channel effects

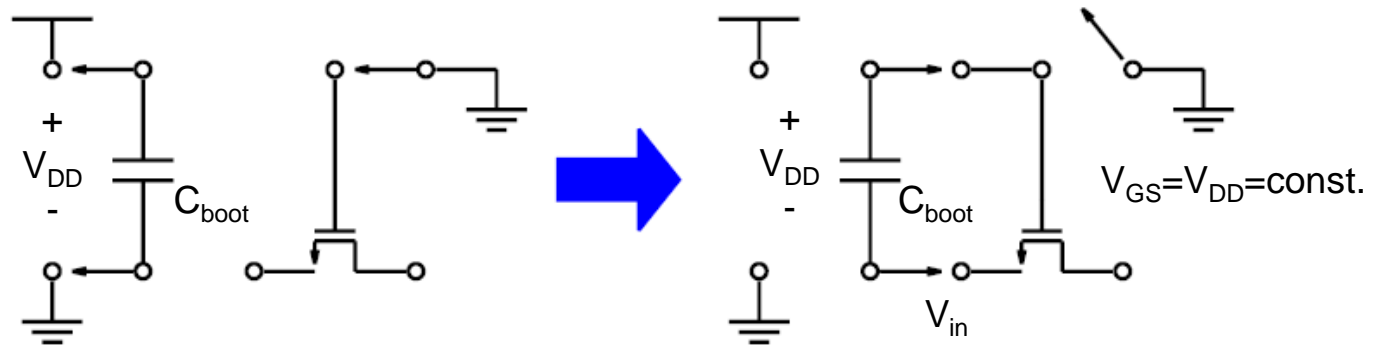
# Simulation CMOS Switch in IHP Technology



[https://github.com/bmurmnn/EE628/tree/main/4\\_Technology/6\\_ron\\_tgate](https://github.com/bmurmnn/EE628/tree/main/4_Technology/6_ron_tgate)

- Design
  - Size P/N ratio to minimize curvature
  - Size P and N simultaneously to meet  $r_{on}$  requirement

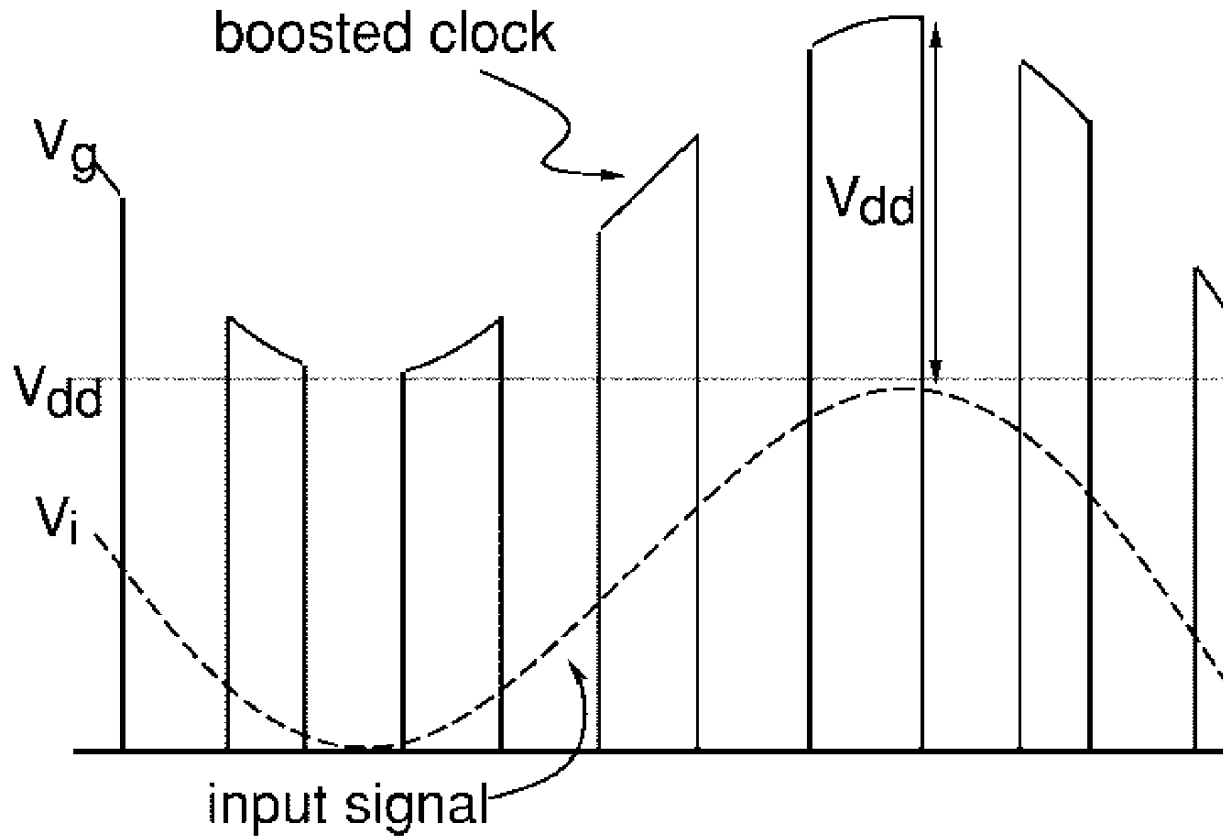
## Aside: Clock Bootstrapping



A. Abo, "Design for Reliability of Low-voltage, Switched-capacitor Circuits," PhD Thesis, UC Berkeley, 1999.

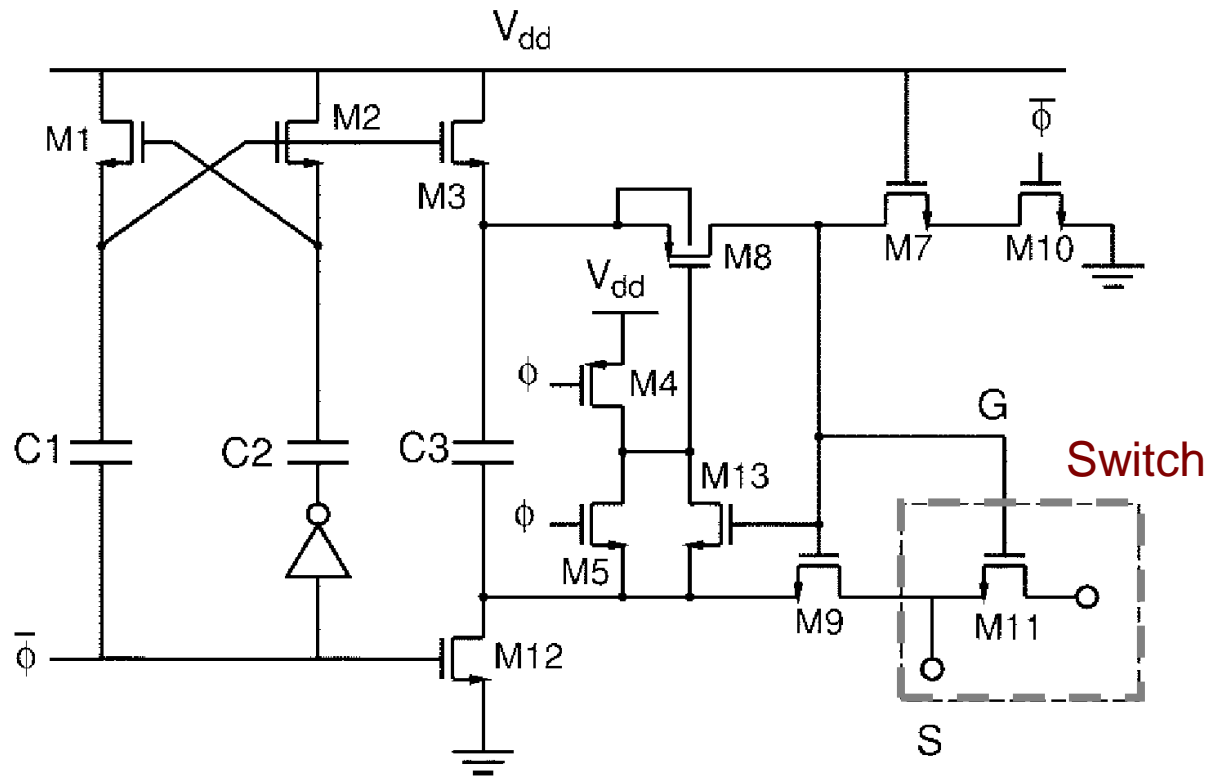
- Phase 1
  - $C_{boot}$  is precharged to  $V_{DD}$
  - Sampling switch is off
- Phase 2
  - Sampling switch is on with  $V_{GS}=V_{DD}=\text{const.}$
  - To first order,  $r_{on}$  is signal independent

## Waveforms



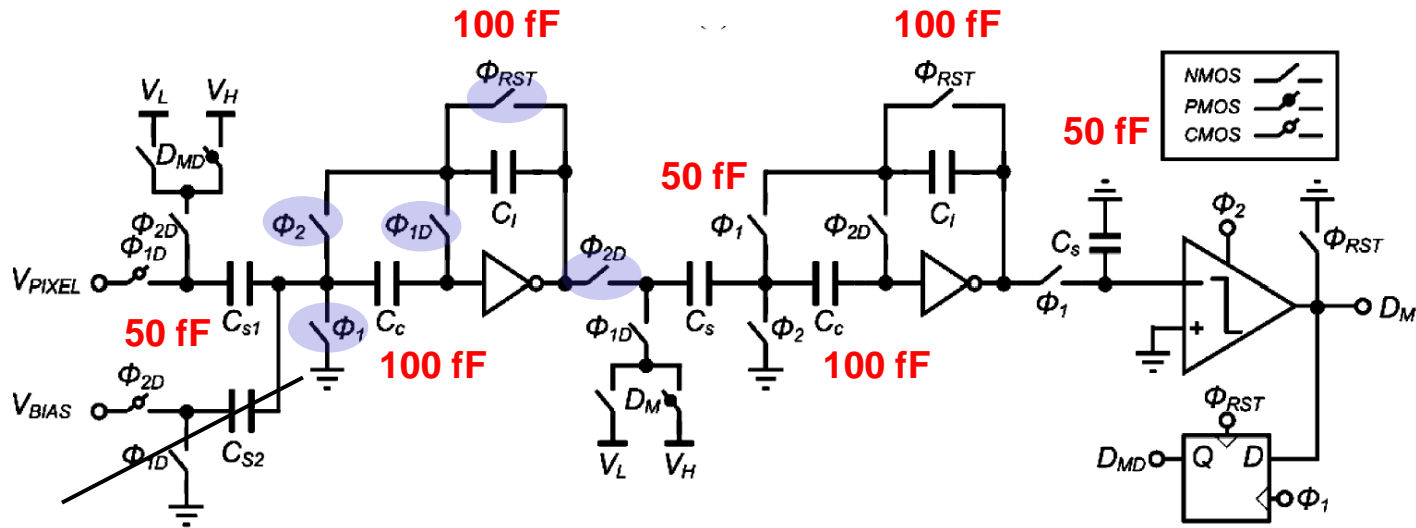
A. Abo, "Design for Reliability of Low-voltage, Switched-capacitor Circuits," PhD Thesis, UC Berkeley, 1999.

# Circuit Implementation



A. Abo et al., "A 1.5-V, 10-bit, 14.3-MS/s CMOS Pipeline Analog-to-Digital Converter," IEEE J. Solid-State Circuits, pp. 599, May 1999

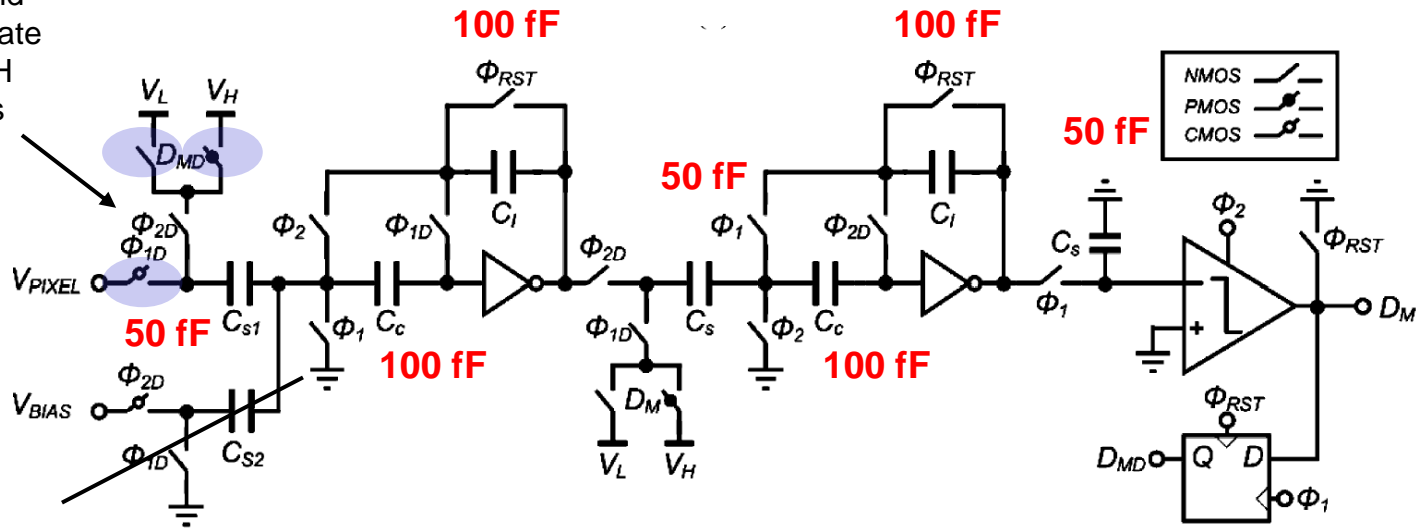
# How Large Should the Switch Devices Be?



- Highlighted above are NMOS switches operating around 0.6 V
- For a 5-um device,  $g_{ds} \sim 0.6 \text{ mS}$ ,  $r_{on} \sim 1.5 \text{ k}\Omega$
- With  $C \sim 150 \text{ fF}$ , the time constant is 0.225 ns
- Half clock period at  $\sim 50 \text{ MHz}$  is 10 ns, i.e.,  $\sim 44$  time constants
- We can reduce the switch size by about 4x, so  $W > 1.25 \text{ um}$ 
  - $W = 2 \text{ um}$  is a safe choice (process variation, parasitics, ...)

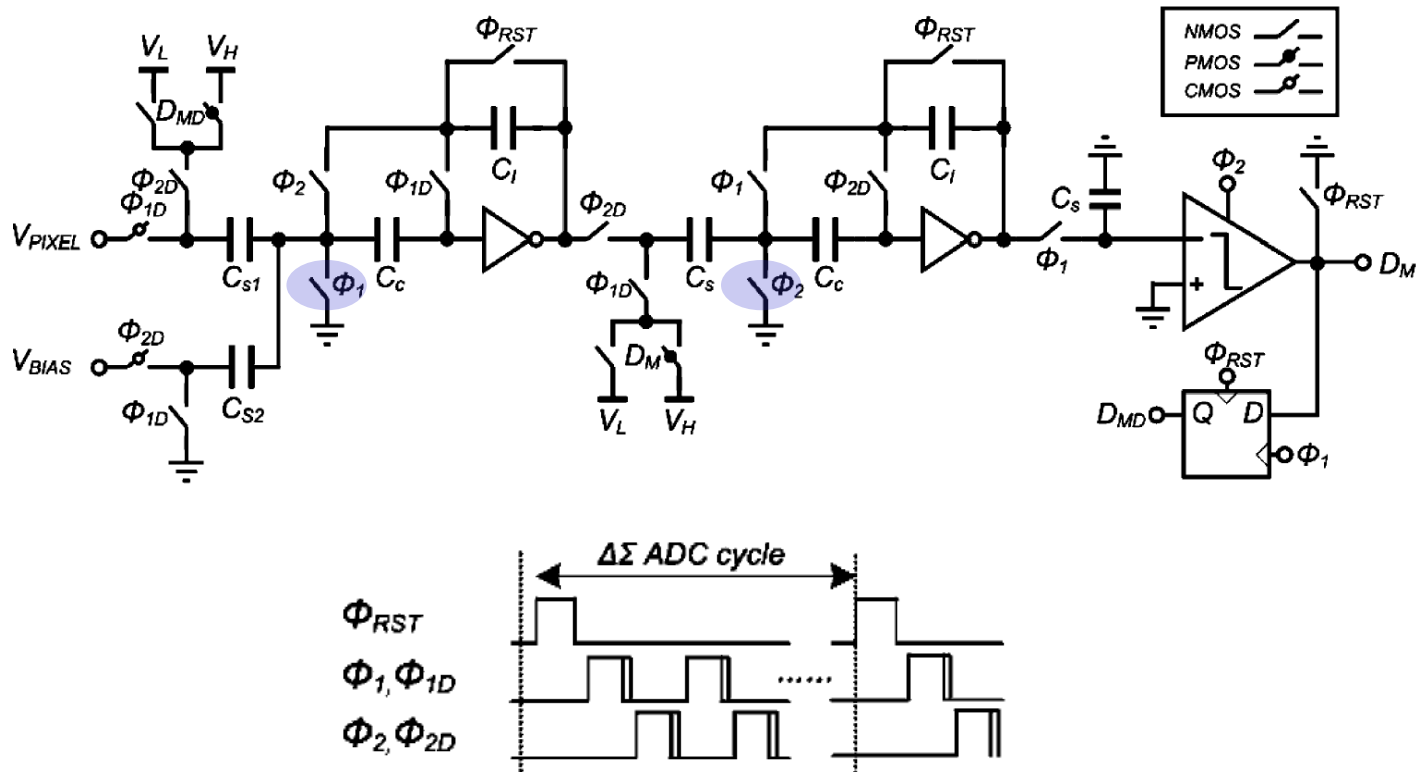
## How Large Should the Switch Devices Be?

Don't need  
this; should  
use AND gate  
for VL/VH  
switches



- VL switch can be smaller since  $g_{ds}$  at  $\sim 0.3$  V is 4 mS
  - $W = 0.5$   $\mu\text{m}$  should be fine
- VH switch should be about 3x wider (low PMOS mobility)
- CMOS input switch can be sized like switch on previous slide
  - NMOS  $\sim 2$   $\mu\text{m}$ , PMOS  $\sim 6$   $\mu\text{m}$

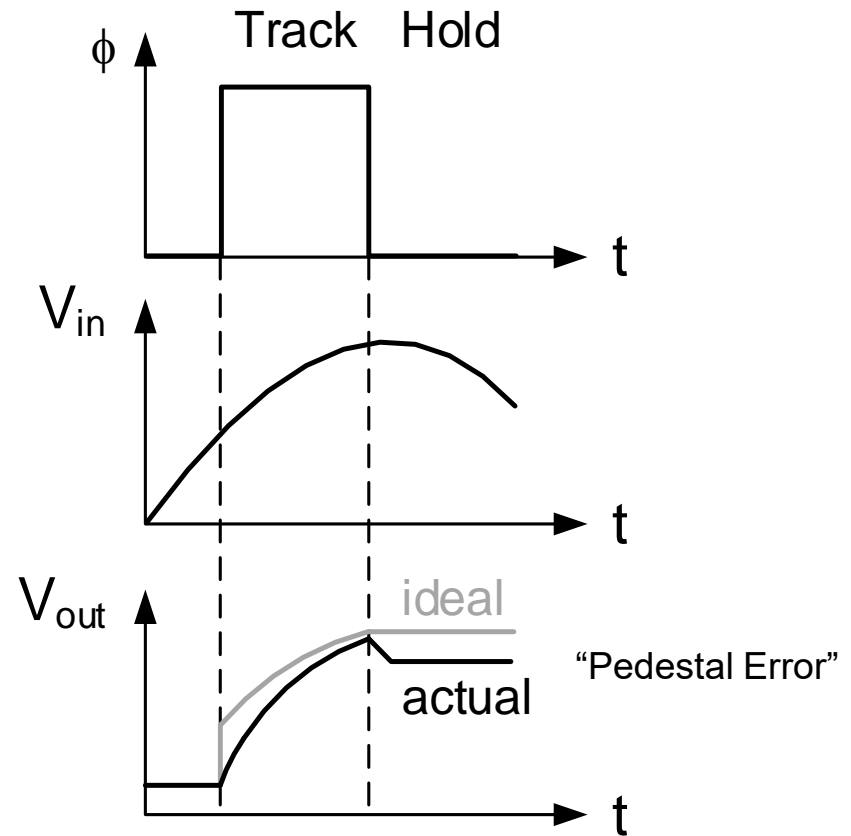
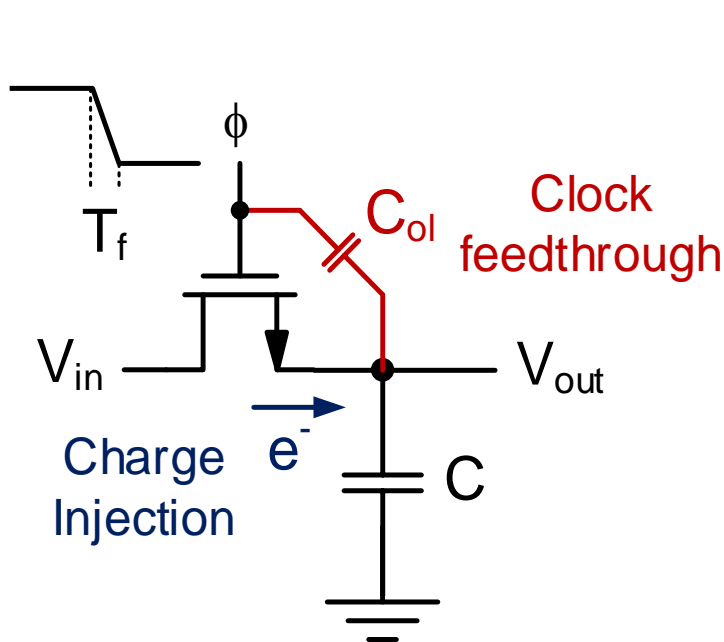
# Switch Timing



- Highlighted switches turn off early. Why?

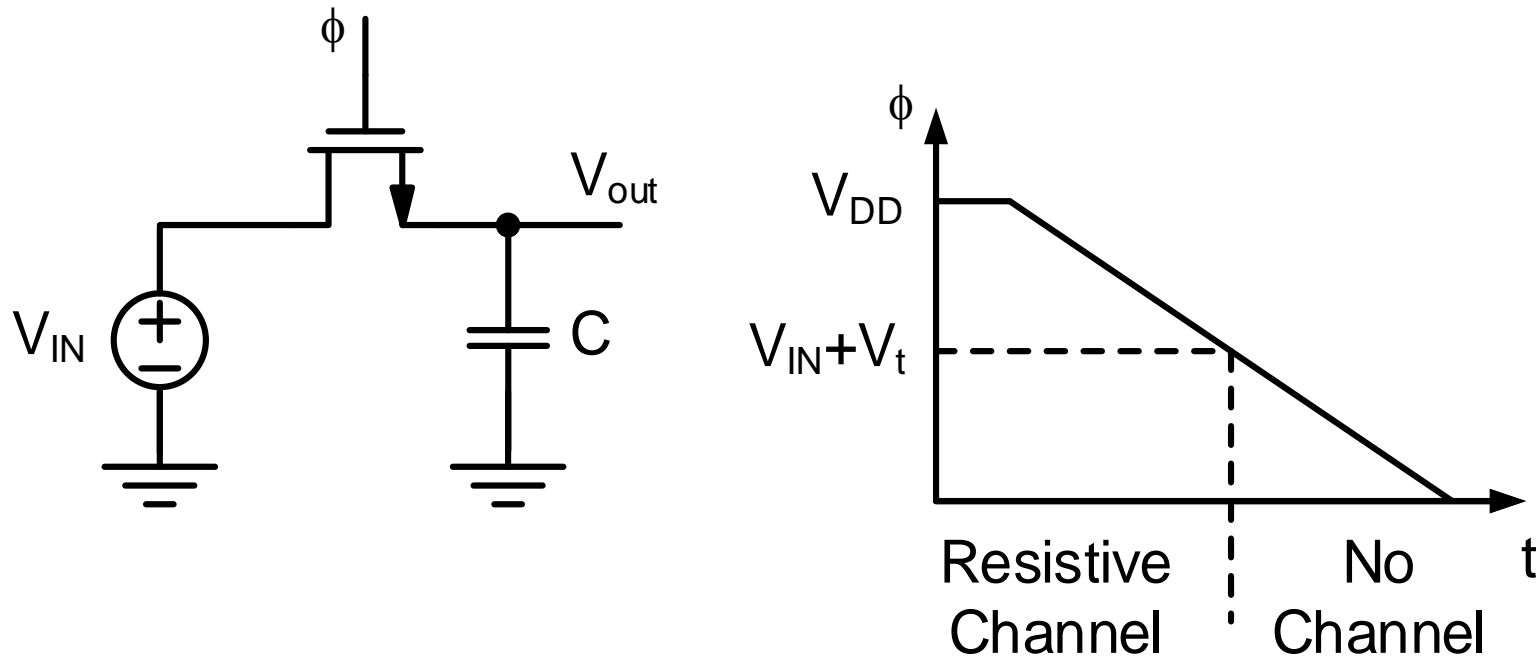


# Charge Injection and Clock Feedthrough



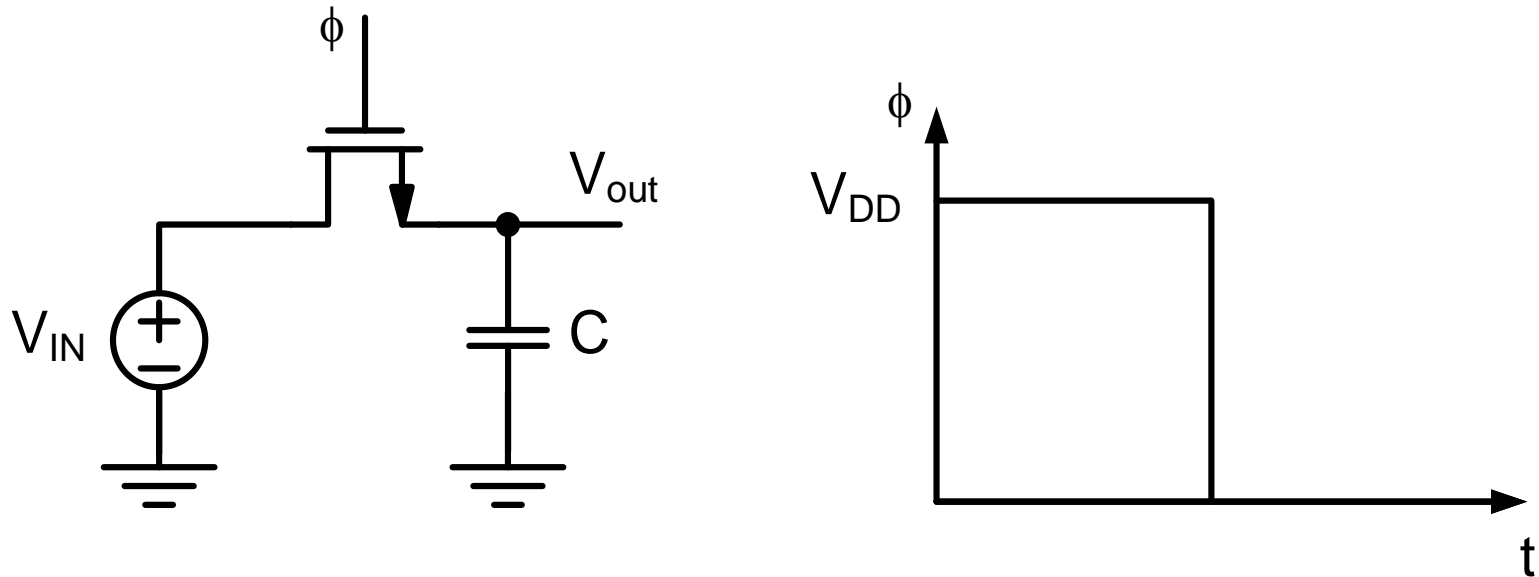
- Focus on charge injection first and analyze two extreme cases
  - Very large  $T_f$  ("slow gating")
  - Very small  $T_f$  ("fast gating")

## Slow Gating



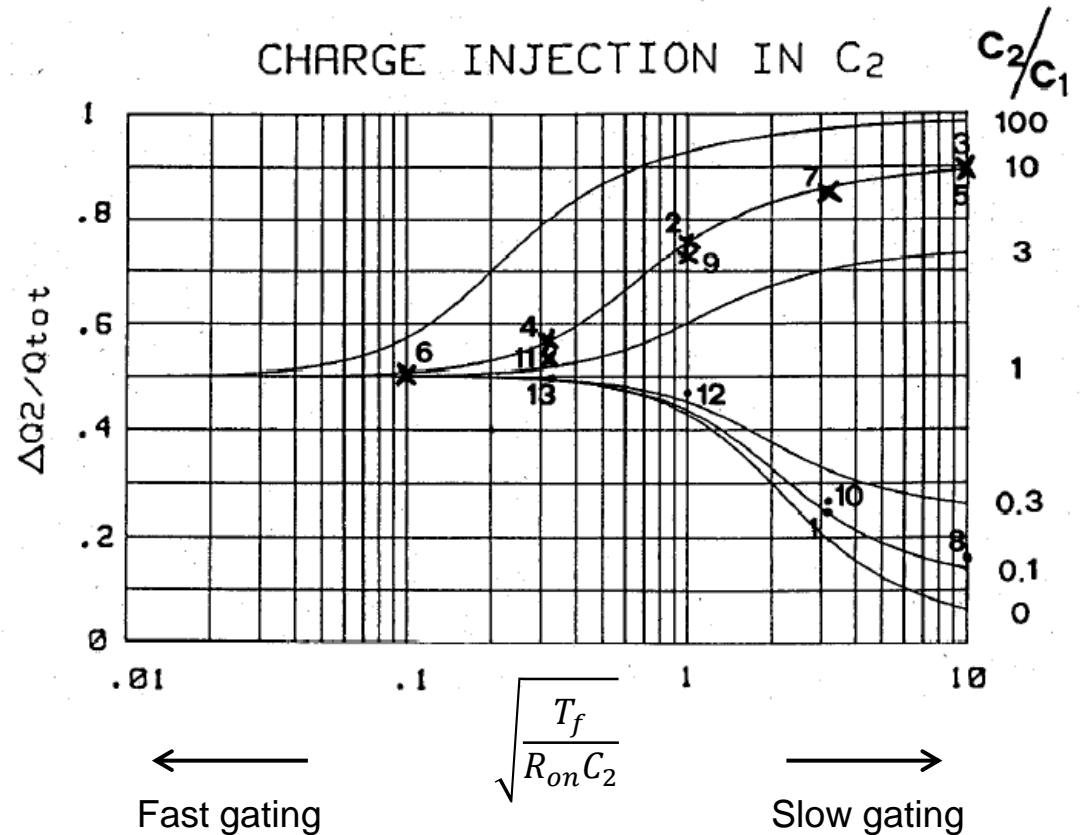
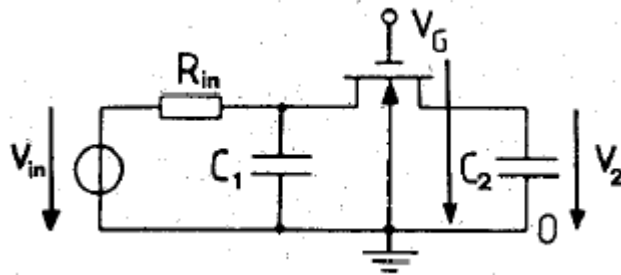
- All channel charge is absorbed by the input source, none of it goes to  $C$
- This is because the MOSFET can manage to equalize  $V_{IN}$  and  $V_{out}$  during the slow turn-off transient

## Fast Gating



- Assuming “infinitely” fast gating, there is no time for the transistor’s on-resistance to play a role in the transient
- With  $V_{GS,D} < V_t$  at the source and drain side of the channel, pinch-off occurs at both sides
- Roughly speaking, we see a current source looking into both sides of the MOSFET and the charge splits 50/50 (independent of termination impedance)

# Charge Split Ratio Data



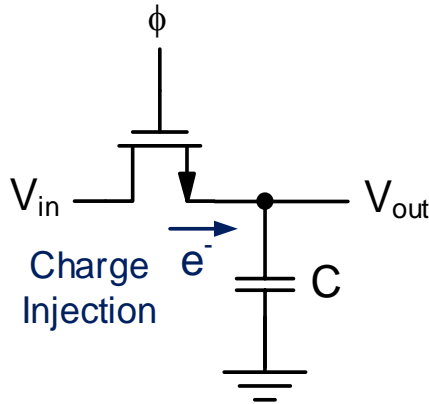
G. Wegmann et al., "Charge injection in analog MOS switches," JSSC, June 1987

Y. Ding and R. Harjani, "A universal analytic charge injection model," Proc. ISCAS, May 2000

# What Happens in Practical Circuits?

- We tend to drive the switch gate as fast as the technology allows
- $R_{on}C_2$  and  $T_f$  are thus usually comparable (same order of magnitude)
  - This brings us into the x-axis range  $<1$  on the chart by Wegmann
  - Means that the charge split may in practice still have “some” dependence on the termination impedances
- Trying to predict the charge split accurately is somewhat hopeless
- We typically use the fast-gating approximation (50/50 split) to get an estimate of the injected charge
  - But we know that slightly more charge will go to the side with lower impedance (perhaps 60...80%)

# Fast Gating Estimate of Charge Injection Error



$$V_{out} = V_{in} + \frac{1}{2} \frac{Q_{ch}}{C} \quad Q_{ch} \approx -WLC_{ox}(V_{DD} - V_{in} - V_t)$$

$$V_{out} = V_{in} - \frac{1}{2} \frac{WLC_{ox}}{C} (V_{DD} - V_{in} - V_t)$$

$$V_{out} = V_{in}(1 + \epsilon) + V_{os}$$

$$\epsilon = \frac{1}{2} \frac{WLC_{ox}}{C}$$

**Gain error**

$$V_{os} = \frac{1}{2} \frac{WLC_{ox}}{C} (V_{DD} - V_t)$$

**Offset error**

Example:  $\epsilon = \frac{1}{2} \frac{20\mu m \cdot 2fF/\mu m}{1pF} = +2\%$

$$V_{os} = 2\%(1.8V - 0.5V) = -26mV$$

## Impact of Technology Scaling

$$\left. \begin{aligned} \Delta V &= \frac{1}{2} \frac{Q_{ch}}{C} & Q_{ch} &\approx -WLC_{ox}(V_{GS} - V_t) \\ R &= \frac{1}{\mu C_{ox} \frac{W}{L} (V_{GS} - V_t)} = \frac{L^2}{\mu Q_{ch}} \\ NRC &= \frac{T_s}{2} = \frac{1}{2f_s} \end{aligned} \right\} \boxed{\frac{\Delta V}{Nf_s} \approx \frac{L^2}{\mu}}$$

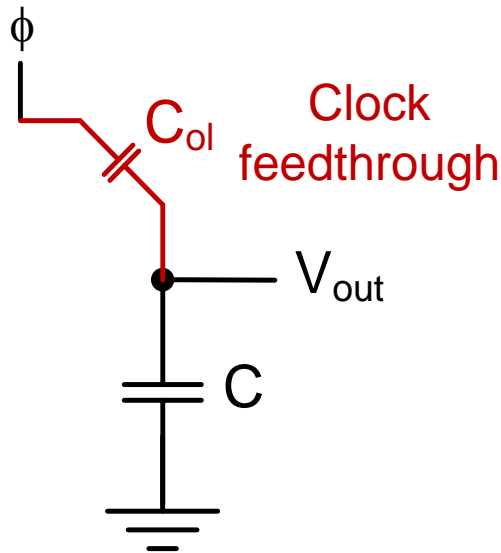
- Ratio of charge injection error and speed benefits from shorter channels and increases in mobility (e.g., due to strain)

## Note On Gain Error

- Our simplistic analysis assumed that the channel charge is linearly related to  $V_{in}$  and hence we see a linear gain error
- This is of course true only to first order (consider backgate effect, etc.)
  - There will always be nonlinear errors in the injected charge
- Computing these nonlinear error terms is analytically difficult and tedious
  - Typically need to rely on simulations to get a feel
- Simulation that the nonlinear portion of the injected charge can be on the order of 0.05...0.1%
- As a rule of thumb, one can assume that signal-dependent charge injection errors limit the sampling linearity to ~10-11 bits



## Clock Feedthrough (Assuming Fast Gating)



$$V_{out} = V_{in} - V_{DD} \frac{C_{ol}}{C_{ol} + C} = V_{in} + V_{os}$$

$$V_{os} = -V_{DD} \frac{C_{ol}}{C_{ol} + C}$$

**Offset error**

Example:  $C_{ol} = 20\mu m \cdot 0.2 \frac{fF}{\mu m} = 4fF$

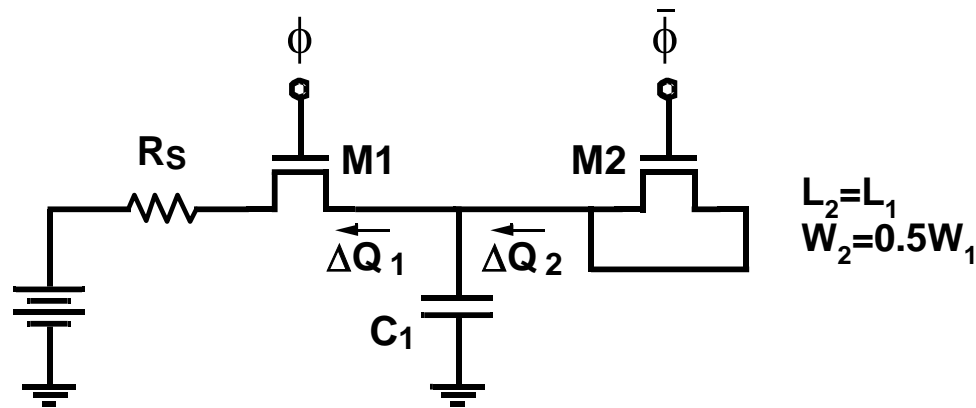
$$V_{os} = -1.8V \frac{4fF}{4fF + 1pF} = -7.1mV$$

- The total offset error is found by adding the charge injection and clock feedthrough components

# Combatting Charge Injection Errors

- Bootstrapped switch
  - Keeps  $V_{GS}$  relatively constant, but channel charge is still signal dependent due to backgate effect, etc.
- Charge cancelation
  - Inject a charge packet with opposite sign
- Transmission gate
  - Achieves partial cancellation between NMOS and PMOS
- Bottom plate sampling
  - The ultimate solution for mitigating signal dependent charge injection

# Charge Cancellation

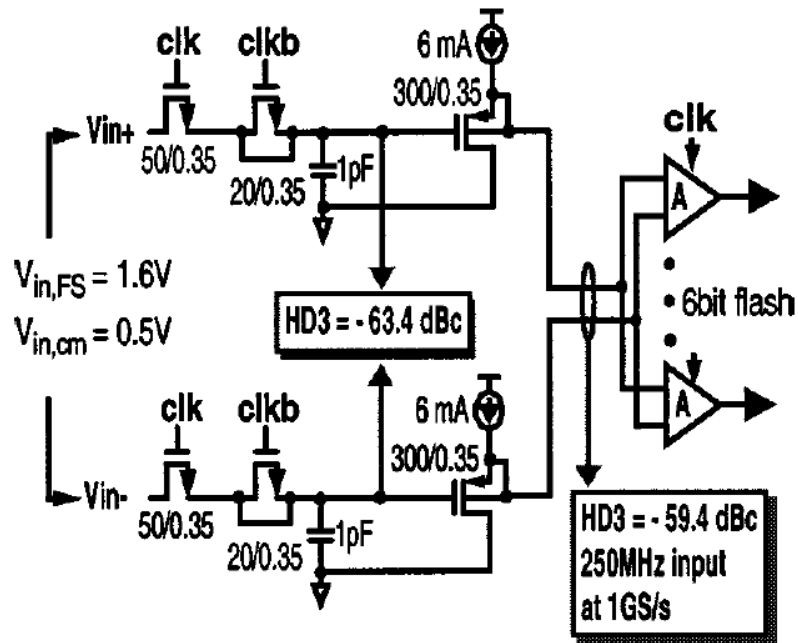


Suarez, Gray and Hodges, JSSC 12/75

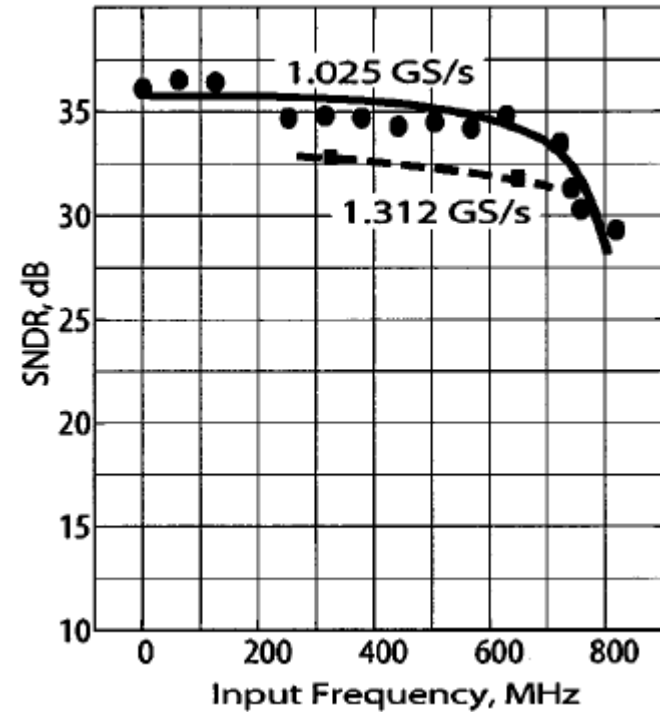
Eichenberger and Guggenbühl, JSSC 8/89

- Cancellation is not perfect, since the channel charge of M1 will not exactly split 50/50 (a larger fraction tends to go the low-impedance input)
- Not a precision technique, just an attempt to do a partial clean-up
  - For example, mitigate a large common mode bounce

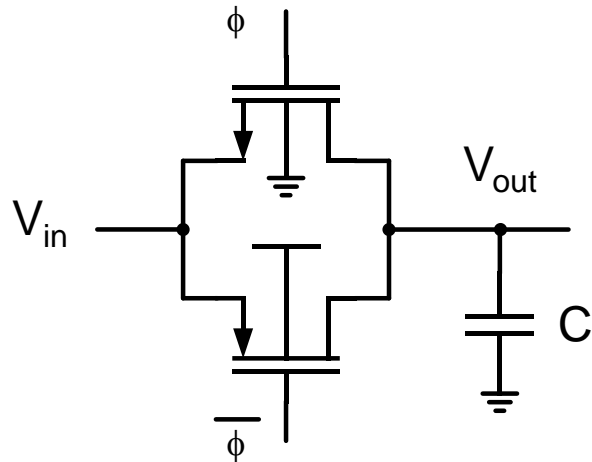
# Application Example



Choi and Abidi, JSSC 12/2001



# Transmission Gate



$$Q_{chn} \approx -W_n L_n C_{ox} (V_{DD} - V_{in} - V_{tn})$$

$$Q_{chp} \approx +W_p L_p C_{ox} (V_{in} - |V_{tp}|)$$

- Assuming  $W_n L_n = W_p L_p$

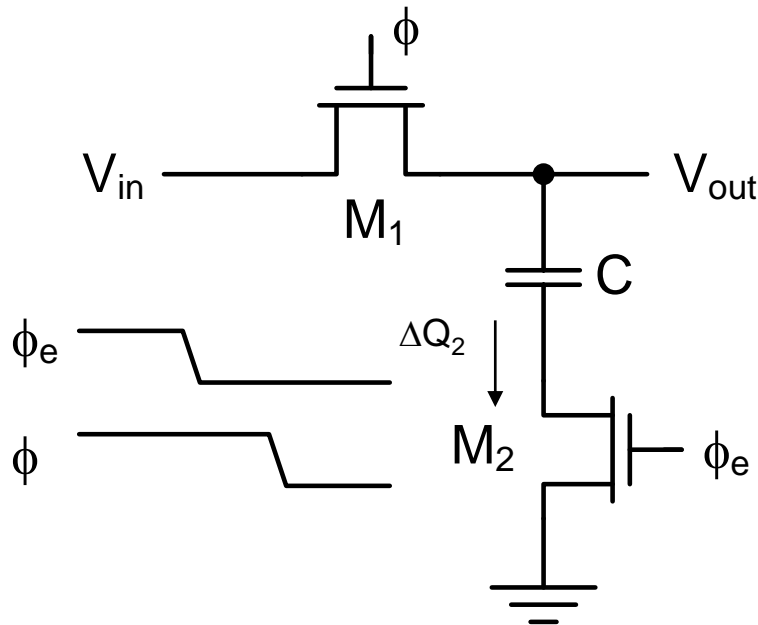
$$\Delta V_{out} \approx \frac{1}{2} \frac{Q_{chn}}{C} + \frac{1}{2} \frac{Q_{chp}}{C} = \frac{W_n L_n C_{ox}}{C} \left( V_{in} - \frac{V_{DD}}{2} + \frac{V_{tn} - |V_{tp}|}{2} \right)$$

- Charges fully cancel e.g. for  $V_{in} = V_{DD}/2$ , and  $V_{tn} = |V_{tp}|$ , but there is still signal-dependent residual injection

# Bottom Plate Sampling

- How to overcome nonlinear charge injection for high-fidelity designs?
  - For example, DR  $\sim 100$  dB
- Basic idea
  - Sample signal at the "grounded" side of the capacitor to achieve signal-independent sampling
- Original reference
  - D. G. Haigh and B. Singh, "A switching scheme for SC filters which reduces the effect of parasitic capacitances associated with switch control terminals," Proc. ISCAS, 1983, pp. 586–589

# Bottom Plate Sampling Analysis (1)



- Turn  $M_2$  off slightly before  $M_1$ 
  - Typically, a few hundred ps delay between falling edges of  $\phi_e$  and  $\phi$
- During turn off,  $M_2$  injects charge

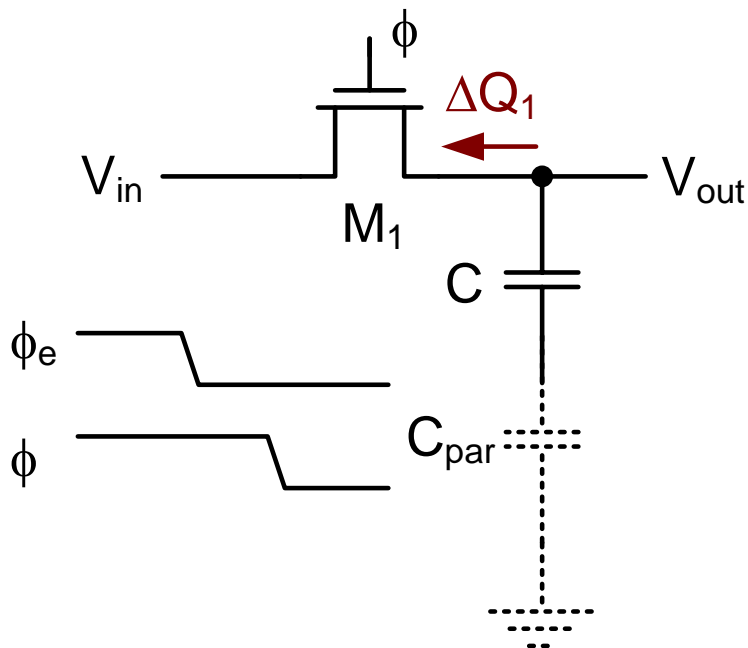
$$\Delta Q_2 \approx \frac{1}{2} W L C_{ox} (V_{DD} - V_t)$$

- To first order, the charge injected by  $M_2$  is signal independent
- Voltage across  $C$

$$V_C = V_{in} + \frac{\Delta Q_2}{C}$$

## Bottom Plate Sampling Analysis (2)

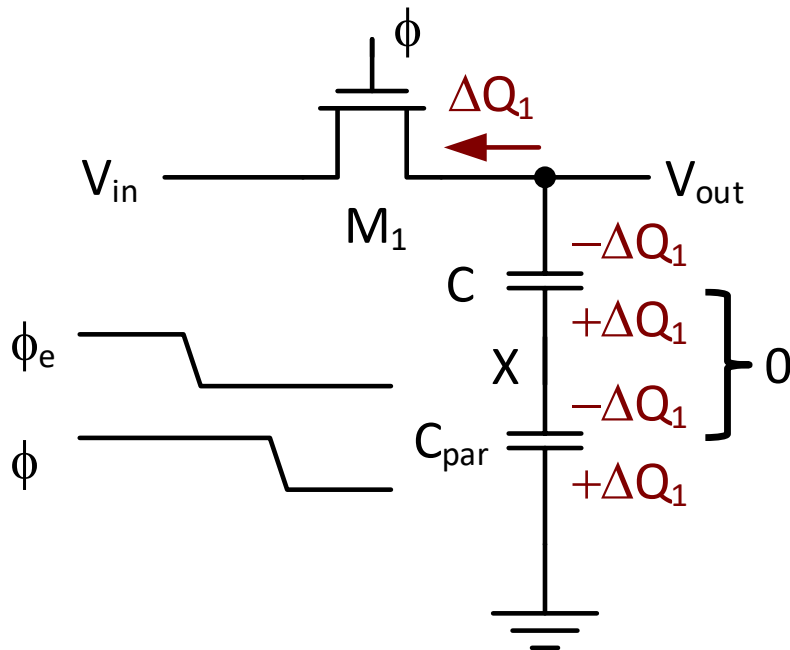
$$\Delta Q_1 \approx \frac{1}{2} W L C_{ox} (V_{DD} - V_{in} - V_t)$$



- Next, turn off M1
- M1 injects signal-dependent charge into series combination of C and bottom plate parasitic capacitance ( $C_{par}$ )
- Voltage across C contaminated with error due to signal dependent charge injection
- Looks like, this is not much different from conventional sampling?
  - But wait...



## Bottom Plate Sampling Analysis (3)

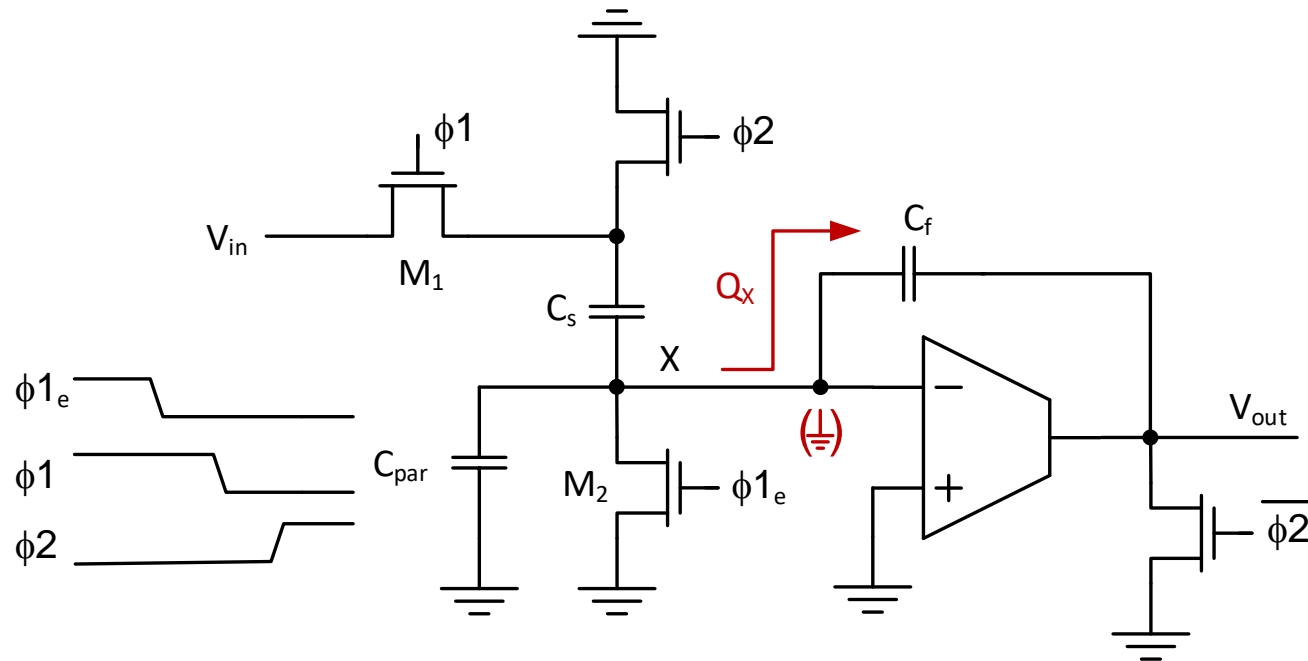


$$Q_X = -CV_{in} - \underbrace{\Delta Q_2}$$

Charge injected by  $M_2$   
(signal independent)

- Interesting observation
  - Even though  $M_1$  injects charge, total charge at node X cannot change!
  - Gaussian surface around node X
- Idea
  - Process total charge at node X instead of looking at voltage across C

# Charge Redistribution



- Amplifier forces voltage at node X to “zero”
  - Charge at node X must redistribute onto feedback capacitor  $C_f$

# Charge Conservation Analysis

Charge at node X during  $\phi_1$ :  $Q_{X1} = -C_s V_{in} - \Delta Q_2 + 0 \cdot C_f$

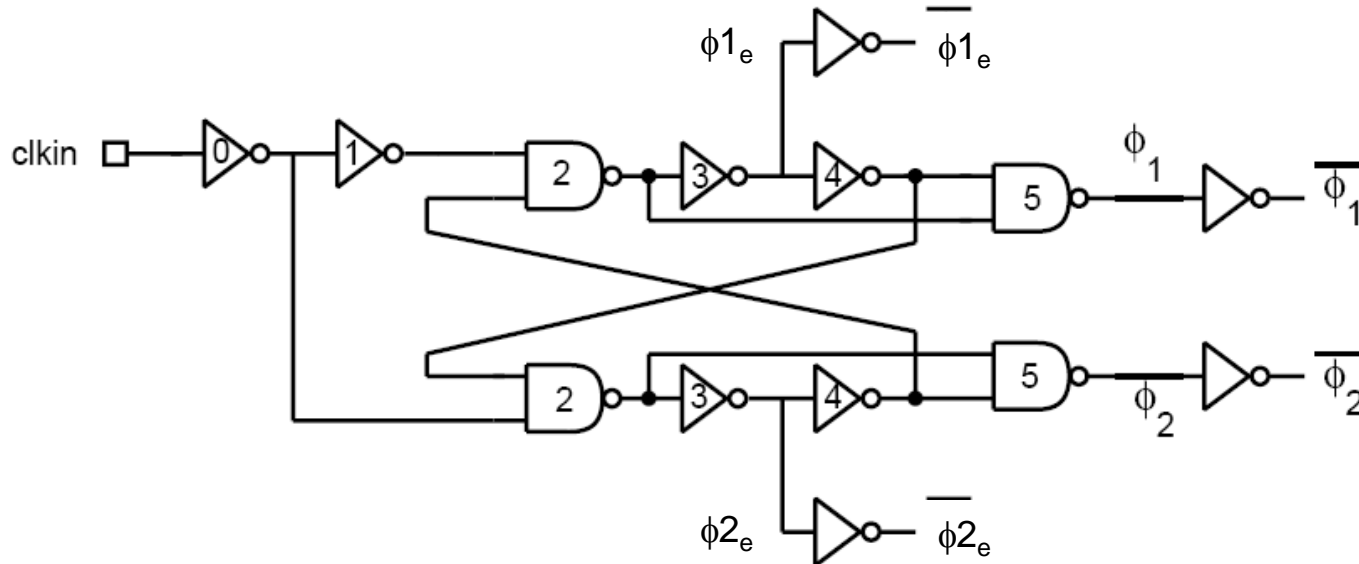
Charge at node X during  $\phi_2$ :  $Q_{X2} = -C_f V_{out}$

Charge Conservation:  $Q_{X1} = Q_{X2}$

$$V_{out} = \frac{C_s}{C_f} V_{in} + \frac{\Delta Q_2}{C_f}$$

- Key point:  $\Delta Q_2$  is signal independent, just a constant offset error
- The offset can be removed using a differential architecture

## Clock Generation Example



[A. Abo, "Design for Reliability of Low-voltage, Switched-capacitor Circuits," PhD Thesis, UC Berkeley, 1999]