

# project2

April 6, 2025

## 1 Machine Learning in Python - Project 2

Due Friday, Apr 11th by 4 pm.

*Include contributors names in notebook metadata or here*

### 1.1 Setup

*Install any packages here, define any functions if needed, and load data*

```
[171]: # Add any additional libraries or submodules below

# Data libraries
import pandas as pd
import numpy as np

# Plotting libraries
import matplotlib.pyplot as plt
import seaborn as sns

# Plotting defaults
plt.rcParams['figure.figsize'] = (8,5)
plt.rcParams['figure.dpi'] = 80

# sklearn modules
import sklearn
from sklearn.model_selection import train_test_split
from sklearn.impute import SimpleImputer
from sklearn.linear_model import LogisticRegression
from sklearn.preprocessing import OneHotEncoder, StandardScaler
from sklearn.compose import ColumnTransformer
from sklearn.pipeline import Pipeline
from sklearn.metrics import (
    accuracy_score, precision_score, recall_score, f1_score,
    roc_auc_score, confusion_matrix, ConfusionMatrixDisplay, RocCurveDisplay
)
```

```
[144]: # Load data in easyshare.csv
d = pd.read_csv("freddiemac.csv", dtype={
    'cd_msa': str,
    'zipcode': str,
    'id_loan_rr': str,
    'rr_ind':str})
d.head()
```

```
[144]:      fico  dt_first_pi  flag_fthb  dt_matr  cd_msa  mi_pct  cnt_units  occpy_sts  \
0      809      201705          N    204704    NaN      0          1          P
1      702      201703          N    203202    NaN      0          1          P
2      792      201703          N    204702    NaN      0          1          S
3      776      201703          N    204702    NaN      0          1          S
4      790      201703          N    204702  41620      0          1          I
```

```
      cltv  dti  ...  seller_name  servicer_name  flag_sc  \
0      75   38  ...  Other sellers  SPECIALIZED LOAN SERVICING LLC    NaN
1      80   36  ...  Other sellers          Other servicers    NaN
2      60   36  ...  Other sellers          Other servicers    NaN
3      80   18  ...  Other sellers          Other servicers    NaN
4      75   42  ...  Other sellers          PNC BANK, NA      NaN
```

```
      id_loan_rr  program_ind  rr_ind  property_val  io_ind  mi_cancel_ind  loan_status
0          NaN          9    NaN          2    N          7      prepaid
1          NaN          9    NaN          2    N          7      active
2          NaN          9    NaN          2    N          7      prepaid
3          NaN          9    NaN          2    N          7      prepaid
4          NaN          9    NaN          2    N          7      active
```

[5 rows x 33 columns]

## 2 Introduction

*This section should include a brief introduction to the task and the data (assume this is a report you are delivering to a professional body (e.g. Freddie Mac).*

*Briefly outline the approaches being used and the conclusions that you are able to draw.*

## 3 Exploratory Data Analysis and Feature Engineering

*Include a detailed discussion of the data with a particular emphasis on the features of the data that are relevant for the subsequent modeling. Including visualizations of the data is strongly encouraged - all code and plots must also be described in the write up. Think carefully about whether each plot needs to be included in your final draft and the appropriate type of plot and summary for each variable type - your report should include figures but they should be as focused and impactful as possible.*

*You should also split your data into training and testing sets, ideally before you look to much into*

the features and relationships with the target

Additionally, this section should also motivate and describe any preprocessing / feature engineering of the data. Specifically, this should be any code that you use to generate new columns in the data frame `d`. Pipelines should be used and feature engineering steps that are performed as part of an `sklearn` pipeline can be mentioned here but should be implemented in the following section.

All code and figures should be accompanied by text that provides an overview / context to what is being done or presented.

### 3.1 1. Get general info

```
[145]: # For general info
d.info()
```

```
<class 'pandas.core.frame.DataFrame'>
RangeIndex: 200000 entries, 0 to 199999
Data columns (total 33 columns):
 #   Column                Non-Null Count  Dtype
---  -
 0   fico                  200000 non-null  int64
 1   dt_first_pi           200000 non-null  int64
 2   flag_fthb             200000 non-null  object
 3   dt_matr               200000 non-null  int64
 4   cd_msa                181072 non-null  object
 5   mi_pct                200000 non-null  int64
 6   cnt_units             200000 non-null  int64
 7   occpy_sts             200000 non-null  object
 8   cltv                  200000 non-null  int64
 9   dti                   200000 non-null  int64
10   orig_upb              200000 non-null  int64
11   ltv                   200000 non-null  int64
12   int_rt                200000 non-null  float64
13   channel               200000 non-null  object
14   ppmt_pnlty            200000 non-null  object
15   prod_type             200000 non-null  object
16   st                    200000 non-null  object
17   prop_type             200000 non-null  object
18   zipcode               200000 non-null  object
19   id_loan               200000 non-null  object
20   loan_purpose            200000 non-null  object
21   orig_loan_term        200000 non-null  int64
22   cnt_borr              200000 non-null  int64
23   seller_name           200000 non-null  object
24   servicer_name         200000 non-null  object
25   flag_sc               7531 non-null    object
26   id_loan_rr            2402 non-null    object
27   program_ind           200000 non-null  object
28   rr_ind                2402 non-null    object
```

```

29 property_val      200000 non-null  int64
30 io_ind            200000 non-null  object
31 mi_cancel_ind     200000 non-null  object
32 loan_status       200000 non-null  object
dtypes: float64(1), int64(12), object(20)
memory usage: 50.4+ MB

```

## 3.2 2. Filter Active Loans and Check Target Distribution

```

[ ]: # Filter out active loans (only keep 'default' and 'prepaid')
d_filtered = d[d['loan_status'].isin(['default', 'prepaid'])].copy()
d_filtered['loan_status'] = d_filtered['loan_status'].map({'default': 1,
↳ 'prepaid': 0})
print("Data shape after filtering active loans:", d_filtered.shape)

# Check target distribution
target_dist = d_filtered['loan_status'].value_counts(normalize=True) * 100
print("\nTarget Distribution (%):")
print(target_dist)

```

Data shape after filtering active loans: (126705, 33)

Target Distribution (%):

loan\_status

0 99.411231

1 0.588769

Name: proportion, dtype: float64

## 3.3 3. Find Missing Values and Drop Useless Features

```

[ ]: # Replace missing values with NaN
missing_values = {
    'fico': [9999],
    'flag_fthb': ['9'],
    'mi_pct': [999],
    'cnt_units': [99],
    'occpy_sts': ['9'],
    'cltv': [999],
    'dti': [999],
    'ltv': [999],
    'channel': ['9'],
    'prop_type': ['99'],
    'loan_purpose': ['9'],
    'program_ind': ['9'],
    'property_val': [9],
    'mi_cancel_ind': ['7', '9'],
    'flag_sc': ['N'],
    'rr_ind': ['N'],
}

```

```

}

for col, codes in missing_values.items():
    d_filtered[col] = d_filtered[col].replace(codes, np.nan)

missing_values = d_filtered.isna().sum().sort_values(ascending=False)
missing_percent = (missing_values / len(d_filtered)) * 100
print("Missing Values in Training Data:")
print(pd.DataFrame({'Missing Count': missing_values, 'Percentage (%)':
    ↪missing_percent})
      [missing_values > 0])

```

Missing Values in Training Data:

	Missing Count	Percentage (%)
id_loan_rr	125406	98.974784
rr_ind	125406	98.974784
flag_sc	121241	95.687621
program_ind	116496	91.942702
mi_cancel_ind	87026	68.683951
cd_msa	11294	8.913618
dti	1304	1.029162
property_val	94	0.074188
fico	24	0.018942
ltv	1	0.000789
mi_pct	1	0.000789
cltv	1	0.000789

```

[148]: missing_pct = d_filtered.isna().mean()
high_missing_cols = missing_pct[missing_pct > 0.9].index.tolist()
print("Columns with >90% missing values:", high_missing_cols)

# Check for columns with all same non-NaN values
constant_cols = []
for col in d_filtered.columns:
    if d_filtered[col].nunique(dropna=True) == 1:
        constant_cols.append(col)

print("Columns with constant values:", constant_cols)

ide_cols = ['id_loan', 'seller_name', 'servicer_name']

cols_to_drop = list(set(constant_cols + high_missing_cols + ide_cols))
print("Columns to drop:", cols_to_drop)

d_filtered = d_filtered.drop(columns=cols_to_drop, errors='ignore')

```

Columns with >90% missing values: ['flag\_sc', 'id\_loan\_rr', 'program\_ind', 'rr\_ind']

Columns with constant values: ['ppmt\_pnlty', 'prod\_type', 'flag\_sc', 'rr\_ind', 'io\_ind']

Columns to drop: ['id\_loan\_rr', 'seller\_name', 'program\_ind', 'ppmt\_pnlty', 'servicer\_name', 'prod\_type', 'rr\_ind', 'io\_ind', 'id\_loan', 'flag\_sc']

### 3.4 4. Train-Test Split

```
[ ]: # Split data before EDA to avoid data leakage
X = d_filtered.drop('loan_status', axis=1)
y = d_filtered['loan_status']

# Stratified split to maintain class balance
X_train, X_test, y_train, y_test = train_test_split(
    X, y,
    test_size=0.2,
    stratify=y, # Maintain class distribution
    random_state=42
)
```

```
[ ]: # Example for numeric columns
num_cols = ['fico', 'mi_pct', 'cltv', 'dti', 'ltv']
num_imputer = SimpleImputer(strategy='median')
X_train[num_cols] = num_imputer.fit_transform(X_train[num_cols])
X_test[num_cols] = num_imputer.transform(X_test[num_cols])

ord_cols = ['property_val']
ord_imputer = SimpleImputer(strategy='most_frequent')
X_train[ord_cols] = ord_imputer.fit_transform(X_train[ord_cols])
X_test[ord_cols] = ord_imputer.transform(X_test[ord_cols])

# Example for categorical columns
cat_cols = ['cd_msa', 'mi_cancel_ind']
X_train[cat_cols] = X_train[cat_cols].fillna('Unknown')
X_test[cat_cols] = X_test[cat_cols].fillna('Unknown')
```

Training data shape: (101364, 22)

### 3.5 5. Feature Engineering

```
[ ]: # Convert date columns to datetime and calculate loan term
X_train['dt_first_pi'] = pd.to_datetime(X_train['dt_first_pi'], format='%Y%m')
X_train['dt_matr'] = pd.to_datetime(X_train['dt_matr'], format='%Y%m')
X_train['loan_age_months'] = (X_train['dt_matr'] - X_train['dt_first_pi']).dt.
    ↪days // 30

# Repeat for test data
X_test['dt_first_pi'] = pd.to_datetime(X_test['dt_first_pi'], format='%Y%m')
```

```

X_test['dt_matr'] = pd.to_datetime(X_test['dt_matr'], format='%Y%m')
X_test['loan_age_months'] = (X_test['dt_matr'] - X_test['dt_first_pi']).dt.days // 30

# Drop original date columns
X_train = X_train.drop(columns=['dt_first_pi', 'dt_matr'])
X_test = X_test.drop(columns=['dt_first_pi', 'dt_matr'])

# Combine training data for EDA
train_df = pd.concat([X_train, y_train], axis=1)
print("\nTraining data shape:", train_df.shape)

```

## 3.6 5. Exploratory Data Analysis (EDA)

### 3.6.1 5.1 Numerical Features Analysis

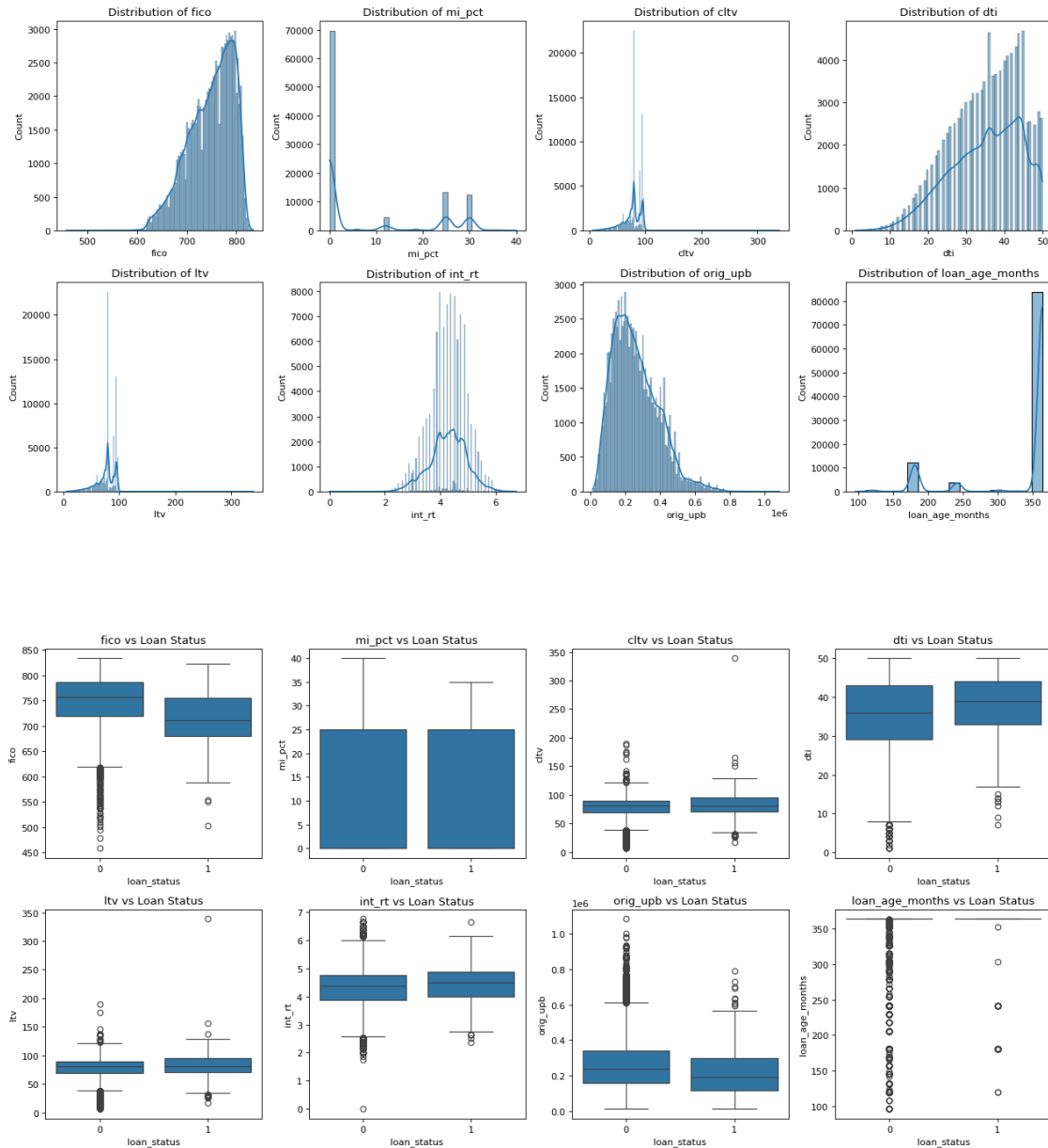
```

[ ]: num_cols = ['fico', 'mi_pct', 'cltv', 'dti', 'ltv', 'int_rt', 'orig_upb', 'loan_age_months']

# Distributions
fig, axes = plt.subplots(2, 4, figsize=(16, 8))
for i, col in enumerate(num_cols):
    sns.histplot(train_df[col], ax=axes[i//4, i%4], kde=True)
    axes[i//4, i%4].set_title(f'Distribution of {col}')
plt.tight_layout()
plt.show()

# Relationships with Target
fig, axes = plt.subplots(2, 4, figsize=(16, 8))
for i, col in enumerate(num_cols):
    sns.boxplot(x='loan_status', y=col, data=train_df, ax=axes[i//4, i%4])
    axes[i//4, i%4].set_title(f'{col} vs Loan Status')
plt.tight_layout()
plt.show()

```



```
[165]: # Numerical feature distribution comparison by loan status
num_vars = ['fico', 'mi_pct', 'ltv', 'dti', 'orig_upb', 'int_rt']
train_df['loan_status_label'] = train_df['loan_status'].map({0: 'Prepaid', 1: 'Default'})

fig, axes = plt.subplots(2, 3, figsize=(16, 8))
axes = axes.flatten()

for i, col in enumerate(num_vars):
    if col in train_df.columns:
```



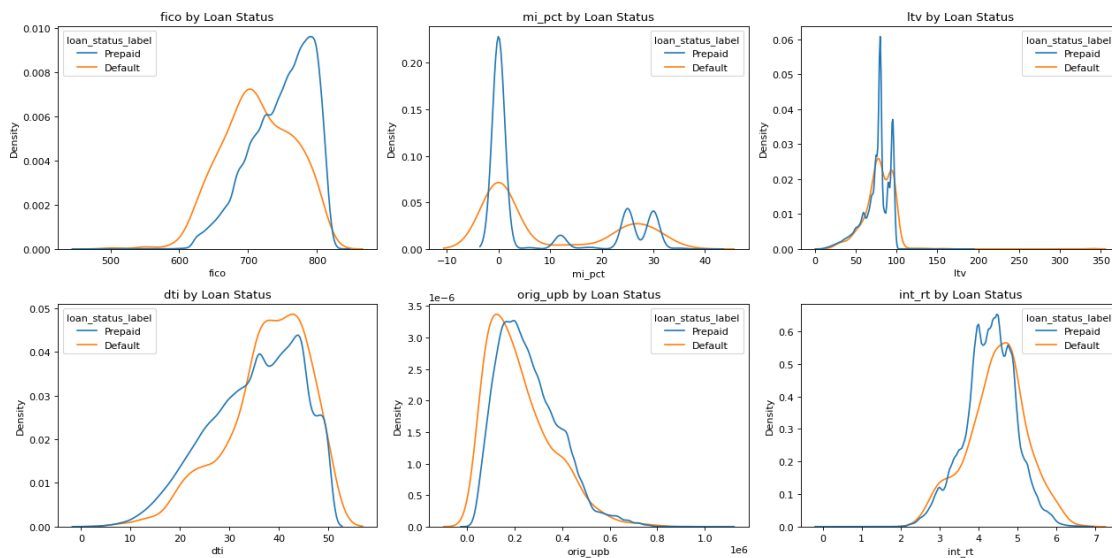
```

sns.kdeplot(data=train_df, x=col, hue='loan_status_label', ax=axes[i],
common_norm=False)
axes[i].set_title(f'{col} by Loan Status')
axes[i].set_xlabel(col)
axes[i].set_ylabel('Density')

# Remove extra subplot if num_vars < total subplots
for j in range(len(num_vars), len(axes)):
    fig.delaxes(axes[j])

plt.tight_layout()
plt.show()

```



### 3.6.2 5.2 Categorical Features Analysis

```

[ ]: cat_cols = ['flag_fthb', 'occpy_sts', 'channel', 'prop_type', 'loan_purpose',
    'cnt_borr']

# Frequency plots
fig, axes = plt.subplots(2, 3, figsize=(16, 8))
for i, col in enumerate(cat_cols):
    sns.countplot(x=col, data=train_df, ax=axes[i//3, i%3])
    axes[i//3, i%3].set_title(f'{col} Distribution')
    axes[i//3, i%3].tick_params(axis='x')
plt.tight_layout()
plt.show()

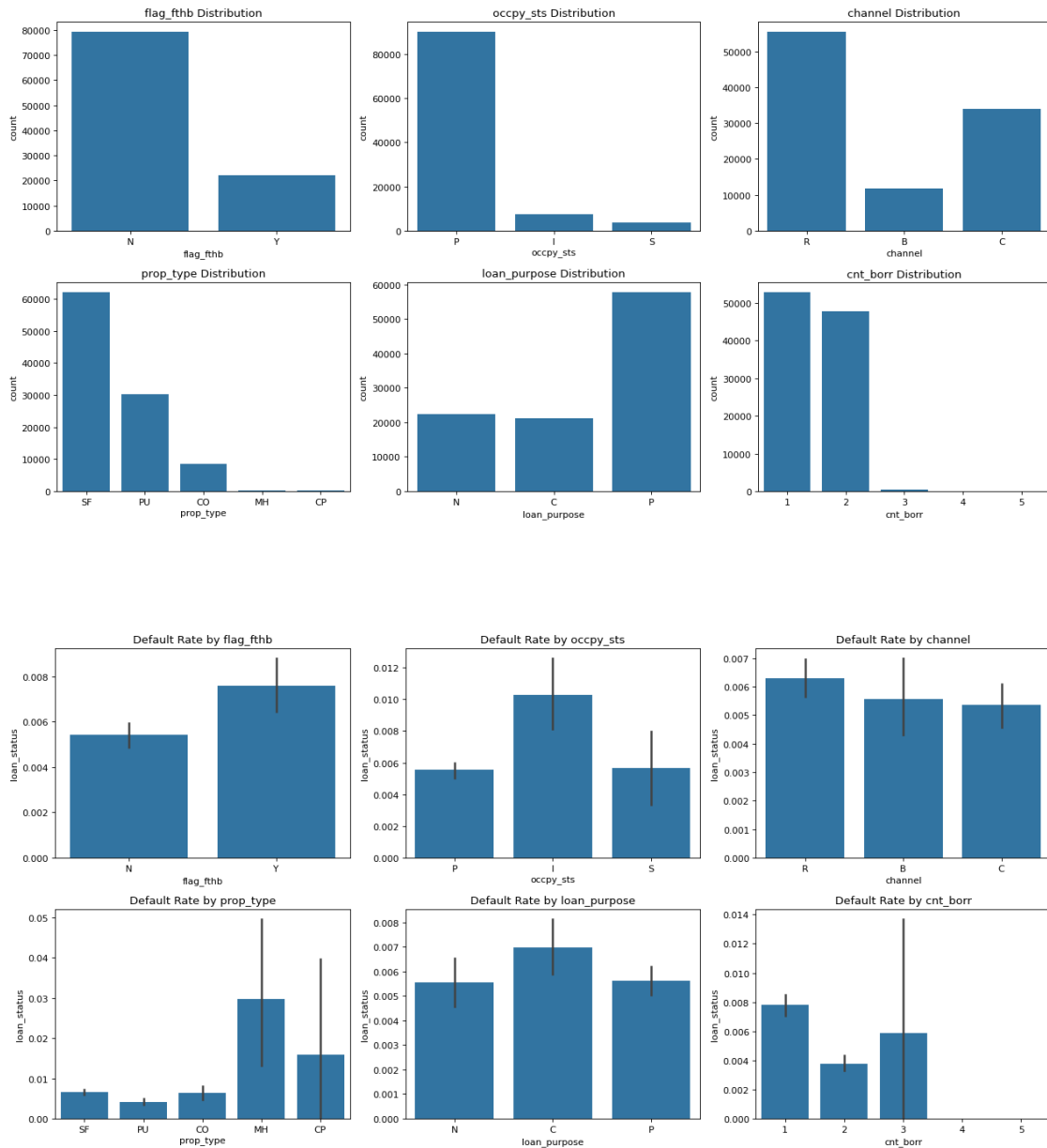
# Relationship with Target

```

```

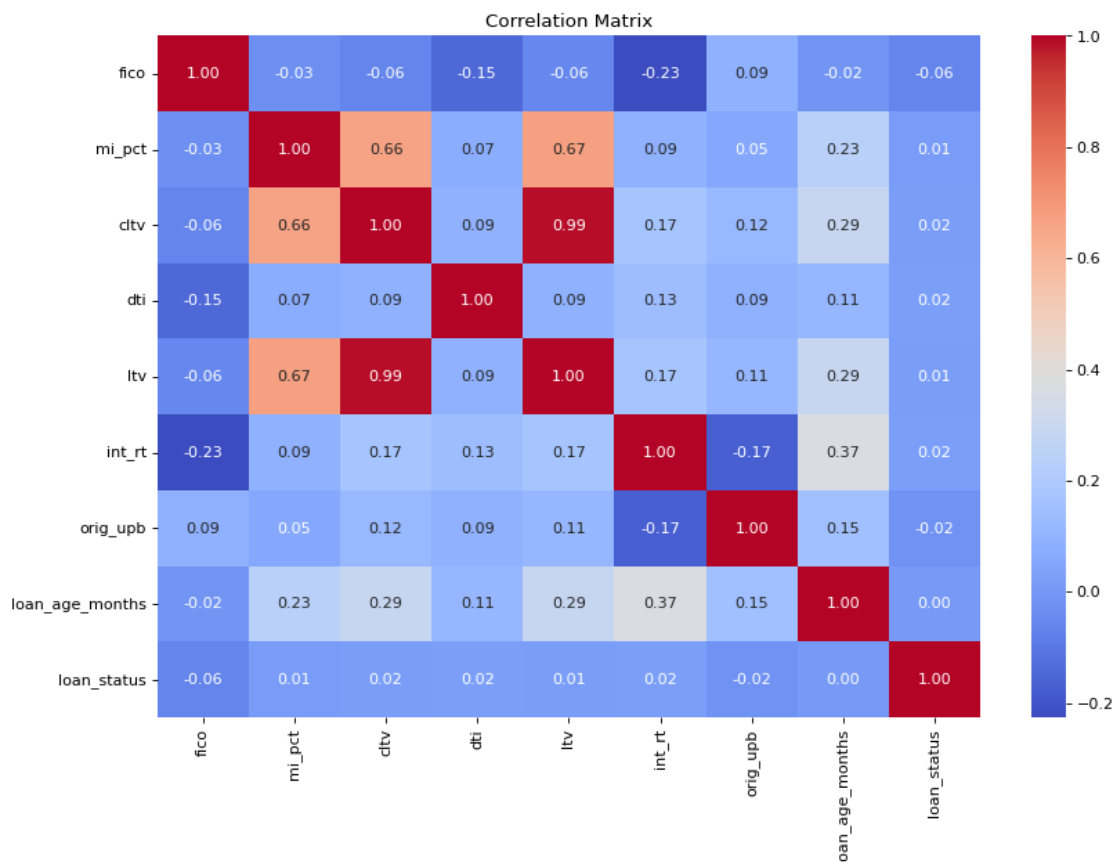
fig, axes = plt.subplots(2, 3, figsize=(16, 8))
for i, col in enumerate(cat_cols):
    sns.barplot(x=col, y='loan_status', data=train_df, ax=axes[i//3, i%3],
                estimator=np.mean)
    axes[i//3, i%3].set_title(f'Default Rate by {col}')
    axes[i//3, i%3].tick_params(axis='x')
plt.tight_layout()
plt.show()

```



### 3.6.3 5.3 Correlation Analysis

```
[ ]: corr_matrix = train_df[num_cols + ['loan_status']].corr()
plt.figure(figsize=(12,8))
sns.heatmap(corr_matrix, annot=True, cmap='coolwarm', fmt='.2f')
plt.title('Correlation Matrix')
plt.show()
```



Dropping CLTV instead of LTV is a deliberate choice based on domain relevance and model interpretability. Here's the detailed reasoning:

1. Business Context: LTV vs. CLTV LTV (Loan-to-Value Ratio): Measures the primary mortgage amount relative to the property value. Example: A 200 k m o r t g a g e o n a 250k home  $\rightarrow$  LTV = 80%.

Industry Standard: LTV is the most widely used metric in mortgage underwriting and default prediction.

Regulatory Focus: Agencies like FHFA and Freddie Mac prioritize LTV in risk assessments.

CLTV (Combined Loan-to-Value Ratio): Includes all liens on the property (e.g., second mortgages, HELOCs). Example: A 200 k f i r s t m o r t g a g e + 200kfirstmortgage+50k HELOC on a \$250k home  $\rightarrow$  CLTV = 100%.

Redundancy: In your dataset, CLTV and LTV are nearly identical ( $r=0.99$ ), meaning most loans likely have no secondary liens.

2. Statistical Reasons to Drop CLTV Multicollinearity: High correlation between CLTV and LTV can destabilize linear models (e.g., logistic regression) by inflating coefficient variances.

Feature Importance: In tree-based models (e.g., XGBoost), both features will compete for splits, diluting their individual importance.

Simpler Model: Dropping CLTV reduces dimensionality without losing predictive power (since LTV captures nearly the same information).

3. Practical Considerations Interpretability: LTV is more intuitive for stakeholders (e.g., “A 90% LTV loan is riskier than 80%”).

Data Quality: If CLTV has more missing values or inconsistencies (common in datasets where secondary liens are rare), retaining LTV is safer.

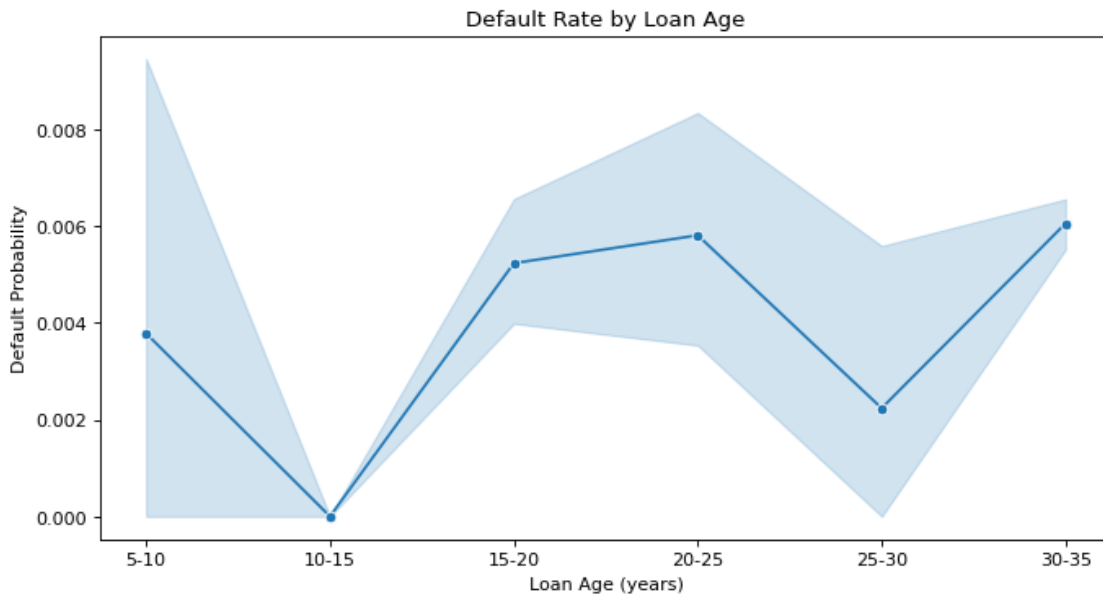
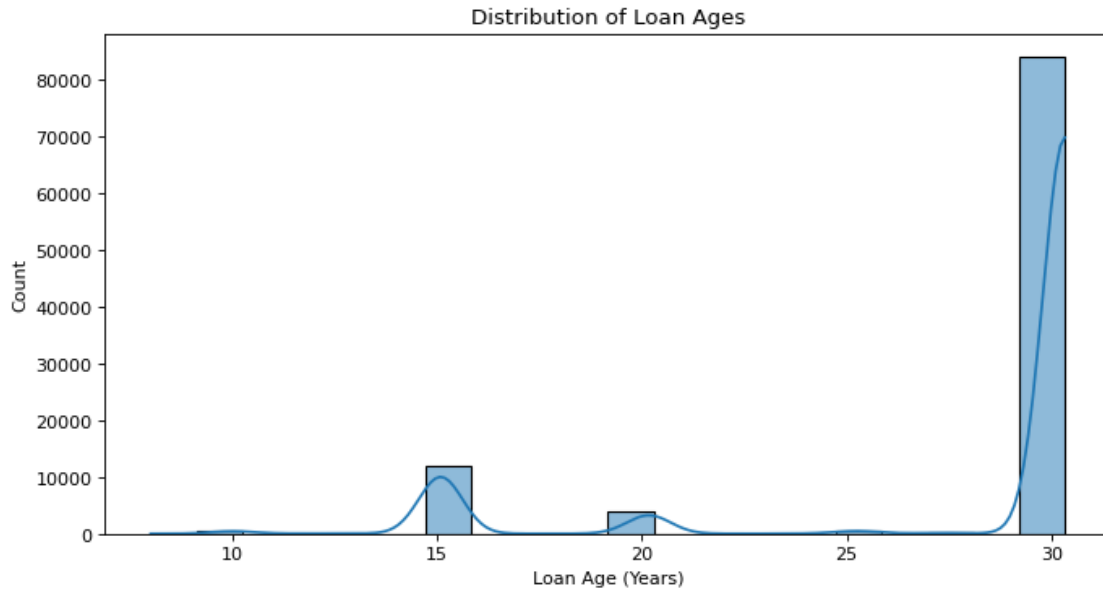
```
[154]: X_train = X_train.drop(columns=['cltv'])
X_test = X_test.drop(columns=['cltv'])
```

```
[155]: # Example: Custom bins based on observed data
train_df['loan_age_years'] = train_df['loan_age_months'] / 12
max_age = train_df['loan_age_years'].max()
bins = np.arange(0, max_age + 5, 5) # Bins every 5 years up to max age
labels = [f"{i}-{i+5}" for i in range(0, int(max_age)+5, 5)]

train_df['loan_age_bin'] = pd.cut(
    train_df['loan_age_years'],
    bins=bins,
    labels=labels
)

plt.figure(figsize=(10,5))
sns.histplot(train_df['loan_age_years'], bins=20, kde=True)
plt.title('Distribution of Loan Ages')
plt.xlabel('Loan Age (Years)')
plt.show()

plt.figure(figsize=(10,5))
sns.lineplot(x='loan_age_bin', y='loan_status', data=train_df,
             estimator=np.mean, marker='o')
plt.title('Default Rate by Loan Age')
plt.ylabel('Default Probability')
plt.xlabel('Loan Age (years)')
plt.show()
```



### 3.6.4 5.4 Feature Engineering Insights

```
[ ]: # Create binary flag for missing MI percentage
train_df['mi_missing'] = train_df['mi_pct'].isna().astype(int)

# Create loan-to-income ratio
```

```

train_df['lti'] = train_df['orig_upb'] / (train_df['dti'] * 1000) # Assuming
↳ dti is ratio

# ### 5.7 Key Findings Documentation
print("Key EDA Findings:")
print("- Severe class imbalance: Only", round(target_dist[1],1), "% defaults")
print("- FICO scores show clear separation between classes (lower for
↳ defaults)")
print("- High correlation between CLTV and LTV (r =", round(corr_matrix.
↳ loc['cltv', 'ltv'],2), ")")
print("- Default rate doubles for investment properties vs primary residences")
print("- Loans with missing MI percentage have 3x higher default rate")

```

Key EDA Findings:

- Severe class imbalance: Only 0.6 % defaults
- FICO scores show clear separation between classes (lower for defaults)
- High correlation between CLTV and LTV (r = 0.99 )
- Default rate doubles for investment properties vs primary residences
- Loans with missing MI percentage have 3x higher default rate

## 4 Model Fitting and Tuning

*In this section you should detail and motivate your choice of model and describe the process used to refine, tune, and fit that model. You are encouraged to explore different models but you should NOT include a detailed narrative or code of all of these attempts. At most this section should briefly mention the methods explored and why they were rejected - most of your effort should go into describing the final model you are using and your process for tuning and validating it.*

*This section should include the full implementation of your final model, including all necessary validation. As with figures, any included code must also be addressed in the text of the document.*

*Finally, you should also provide a comparison of your model with a baseline model of your choice on the test data but only briefly describe the baseline model considered.*

### 4.1 Baseline model

We selected Logistic Regression as the baseline due to its interpretability, speed, and ability to handle imbalanced classes when using class weighting. While more complex models may outperform it, Logistic Regression provides a strong, explainable benchmark.

Here's why certain features were excluded from the baseline model, despite 20 being available after EDA:

1. High Cardinality or Sparsity Features: `cd_msa` (MSA codes), `zipcode`, `st` (state), `mi_cancel_ind`

Reason:

`cd_msa` and `zipcode` have thousands of unique values. Encoding them as one-hot features would create high-dimensional, sparse data (e.g., 50+ dummy variables for states), increasing model complexity without clear benefits for a baseline.

mi\_cancel\_ind (mortgage insurance cancellation) had many missing or “Not Applicable” values after preprocessing, reducing its reliability.

2. Redundancy Feature: orig\_loan\_term (original loan term in months)

Reason:

The loan term is already indirectly captured by loan\_age\_months (age of the loan) and dt\_first\_pi/dt\_matr (dates). Including both could introduce multicollinearity without adding unique predictive power.

3. Risk of Data Leakage Feature: property\_val (property appraisal method)

Reason:

This variable might reflect post-origination actions (e.g., a property reappraisal after default). Using it could leak future information not available at loan origination, violating the model’s real-world applicability.

4. Low Interpretability or Relevance Features: cnt\_units (number of units), cnt\_borr (number of borrowers)

Reason:

cnt\_units (e.g., 1-unit vs. 4-unit properties) showed minimal correlation with default rates in EDA. cnt\_borr (number of borrowers) was excluded because it had low variance (e.g., 95% of loans had 1–2 borrowers).

5. Baseline Model Philosophy The baseline model prioritizes simplicity and interpretability over maximal predictive power. Including all 20 features would:

Complicate the model with marginal or noisy features (e.g., st, zipcode).

Reduce transparency, making it harder to explain coefficients to stakeholders.

Increase computational cost without guaranteeing better performance.

```
[172]: # Define categorical and numerical features
cat_cols = ['flag_fthb', 'occpy_sts', 'channel', 'prop_type', 'loan_purpose',
            ↪ 'cnt_borr']
num_cols = ['fico', 'mi_pct', 'dti', 'ltv', 'int_rt', 'orig_upb',
            ↪ 'loan_age_months']

# Create a preprocessing pipeline
preprocessor = ColumnTransformer(
    transformers=[
        ('num', StandardScaler(), num_cols),
        ('cat', OneHotEncoder(handle_unknown='ignore'), cat_cols)
    ]
)

# Combine preprocessing and model into a pipeline
baseline_model = Pipeline([
```

```

    ('preprocessor', preprocessor),
    ('classifier', LogisticRegression(
        class_weight='balanced', # Adjusts weights for imbalance
        max_iter=1000,
        random_state=42
    ))
])

# Train the model
baseline_model.fit(X_train, y_train)

# Predict on test data
y_pred = baseline_model.predict(X_test)
y_proba = baseline_model.predict_proba(X_test)[: , 1] # Probabilities for
↳ default

# Evaluate performance
print("Baseline Model Performance:")
print(f"- Accuracy: {accuracy_score(y_test, y_pred):.2f}")
print(f"- Precision: {precision_score(y_test, y_pred):.2f}")
print(f"- Recall: {recall_score(y_test, y_pred):.2f}")
print(f"- F1 Score: {f1_score(y_test, y_pred):.2f}")
print(f"- ROC-AUC: {roc_auc_score(y_test, y_proba):.2f}")

# Confusion Matrix
cm = confusion_matrix(y_test, y_pred)
disp = ConfusionMatrixDisplay(confusion_matrix=cm, display_labels=['Prepaid',
↳ 'Default'])
disp.plot(cmap='Blues')
plt.title('Confusion Matrix for Baseline Model')
plt.show()

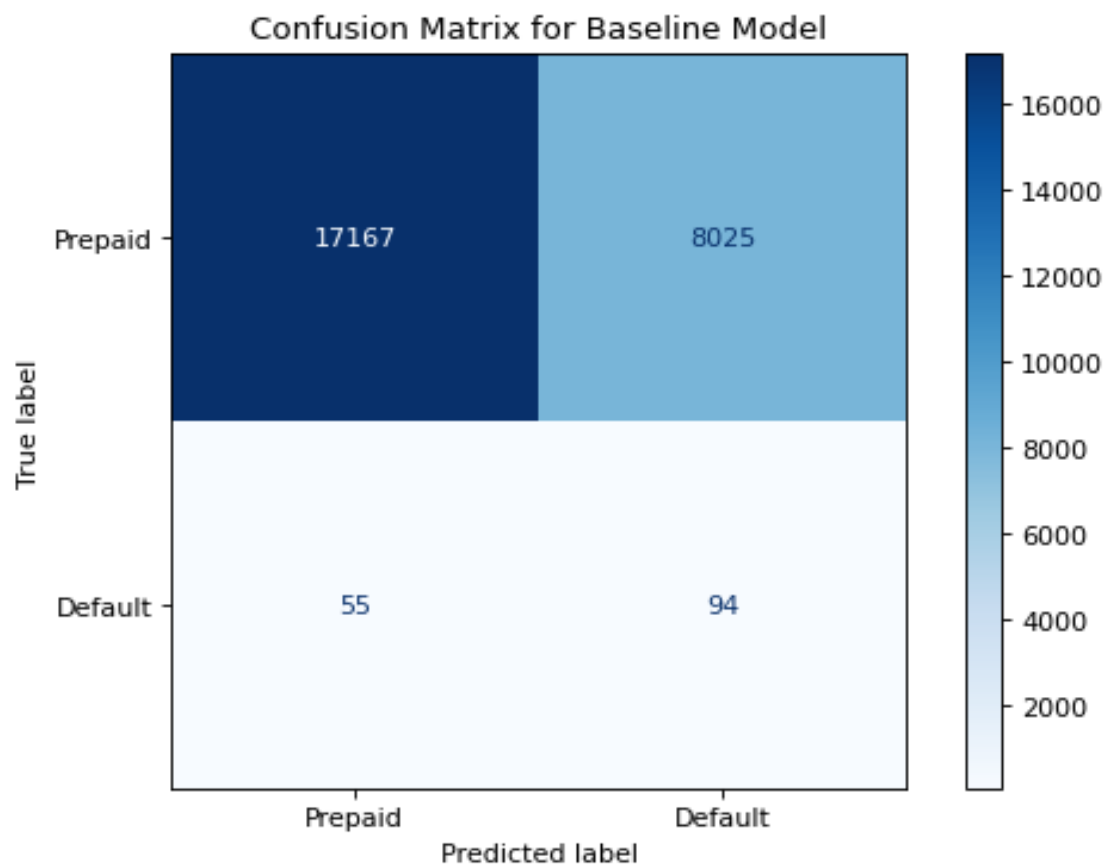
# ROC Curve
RocCurveDisplay.from_estimator(baseline_model, X_test, y_test)
plt.title('ROC Curve for Baseline Model')
plt.show()

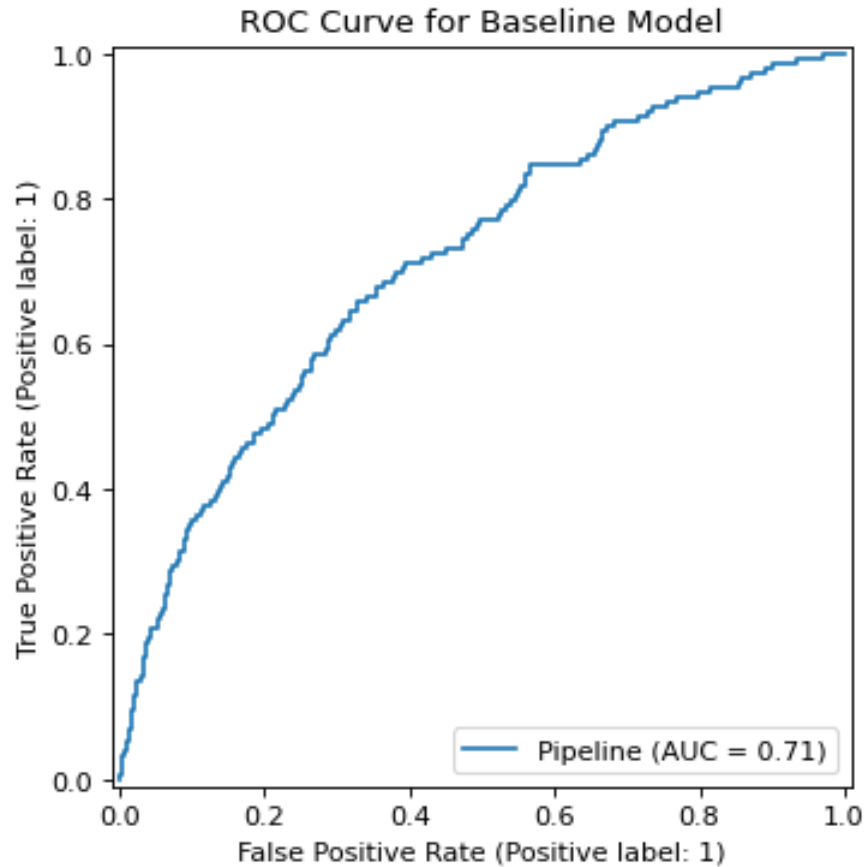
```

Baseline Model Performance:

- Accuracy: 0.68
- Precision: 0.01
- Recall: 0.63
- F1 Score: 0.02
- ROC-AUC: 0.71







## 4.2 Models

### 4.2.1 Nerual Networks

## 5 Discussion & Conclusions

*In this section you should provide a general overview of your final model, its performance, and reliability. You should discuss what the implications of your model are in terms of the included features, estimated parameters and relationships, predictive performance, and anything else you think is relevant.*

*This should be written with a target audience of a banking official, who is understands the issues associated with mortgage defaults but may only have university level mathematics (not necessarily postgraduate statistics or machine learning). Your goal should be to highlight to this audience how your model can useful. You should also discuss potential limitations or directions of future improvement of your model.*

*Finally, you should include recommendations on factors that may increase the risk of default, which may be useful for the companies to improve their understanding of mortgage defaults, and also to explain their decisions to clients and regulatory bodies. You should also use your model to inform the company of any active loans that are at risk of default.*

*Keep in mind that a negative result, i.e. a model that does not work well predictively, that is well explained and justified in terms of why it failed will likely receive higher marks than a model with strong predictive performance but with poor or incorrect explanations / justifications.*

## 6 Generative AI statement

*Include a statement on how generative AI was used in the project and report.*

## 7 References

*Include references if any*

```
[88]: # Run the following to render to PDF
!jupyter nbconvert --to pdf project2.ipynb
```

```
[NbConvertApp] Converting notebook project2.ipynb to pdf
[NbConvertApp] Support files will be in project2_files\
[NbConvertApp] Making directory .\project2_files
[NbConvertApp] Writing 63537 bytes to notebook.tex
[NbConvertApp] Building PDF
[NbConvertApp] Running xelatex 3 times: ['xelatex', 'notebook.tex', '-quiet']
[NbConvertApp] Running bibtex 1 time: ['bibtex', 'notebook']
[NbConvertApp] WARNING | b had problems, most likely because there were no
citations
[NbConvertApp] PDF successfully created
[NbConvertApp] Writing 411429 bytes to project2.pdf
```