TECHNICAL NOTE

DiscoSnp++: Additional File

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Validation of predictions and precision/recall computations

Both on real datasets or synthetic ones, predicted polymorphisms can be compared to a reference set. In all the performed tests, one dispose from a reference genome that is used in the purpose of simulating and validating predictions. Whatever the tested method, the predicted polymorphisms are validated using the following process:

- All predicted sequences are fully mapped using Gassst [1] on the reference genome with a least 90% similarity.
- For SNPs:
 - For each couple of sequences predicting one or more SNPs: if one or the two sequence(s) map the reference genome: for each predicted SNP of the mapped sequence(s), if its position matches exactly a position on which a SNP was simulated, then this SNP is considered as a True Positive (TP).
- For indels:
 - If one or the two sequence(s) of a predicted indel matches a simulated indel position, then such a prediction is considered as a True Positive (TP).
- A predicted polymorphism that is not a True Positive is a False Positive (FP).
- A simulated polymorphism not mapped by a predicted polymorphism is a False Negative (FN).

The precision defined by

$$precision = \frac{numberTP}{numberTP + numberFP}$$

and the recall is defined by

$$recall = \frac{numberTP}{numberTP + numberFN}$$

Note that in the case of real datasets, the *precision* is meaningless as the reference sets are not exhaustive. The main manuscript does not provide *precision* for real read sets.

Simulation experiments

Two to n E. Coli datasets: simulations and experiments Simulations

We propose an experiment simulating more than two haploid bacterial individuals. For doing this, we created 30 copies (that we call individuals) of the E. coli K-12

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MG1655 strain. We then simulated SNPs with a uniform distribution such that \approx 4200 SNPs (\approx 0.1% of the genome length) are common to any pair of individuals, half this number is common to any trio of individuals, a third to any quadruplet, and so on. With this strategy, while considering all the 30 individuals together, 69 600 SNP sites were generated, covering \approx 1.5% of the genome. We also simulated indels following exactly the same process, with a ratio of one indel for ten SNPs.

We simulated a 40x sequencing of each of the 30 individuals, with 100-bp reads and 0.1% error rate. Thus, 1,855,870 reads were generated per read set.

Experiments

Experiments were made on subsets of two Coli individuals (the two first read sets), three individuals (the three first read sets), and so on up to 30 experiments. The command used are reported Table 1.

Two human read sets: simulations and experiments

Simulations

An experiment was performed on two human diploid read sets. This experiment applied on human chromosome 1, (GRCh37/hg19 reference assembly version), \approx 249 million base pairs. SNPs and indels were simulated following the 1000 genome project [2] predictions. Precisely, from the phase 1 vcf file [3], we extracted SNPs and indels of individuals HG00096 and HG00100. Variants having the same genotypes in both individuals were discarded. For each of the two individuals, two version of the chromosome were created. On each of these two versions, SNPs and indels were placed following the VCF file, i.e., 0|0: no modification of the chromosomes, 0|1: modification of one of the two chromosomes (randomly chosen), 1|1: modification of the two chromosomes.

For each individual, we simulated a 40x illumina sequencing with 0.1% error rate (20x per chromosome). Thus, 99,600,000 reads were generated per read set.

Experiments

Experiments were performed using DiscoSnp++, cortex and the hybrid approach using the commands indicated Table 2.

GATK parameters

As mentioned in the manuscript, we used GATK either simply calling SNPs and indel using the *UnifiedGenotyper* option as shown Table 2 or using the reads realignment and the *HaplotypeCaller*.

We decided not to present results using the reads realignment and the *Haplotype-Caller* as this does not improve significantly the prediction precision and recall (see Figure 1) and as the execution time is three times longer (from approximately 19h to 54h for this experiment).

Saccharomyces cerevisiae: experiment

We used reads provided by the Kvitek [4] study. The 24 read sets were downloaded from the NCBI Sequence Read Archive (with the accession number SRA054922), and processed to remove barcode and adapter sequences as in the initial study.

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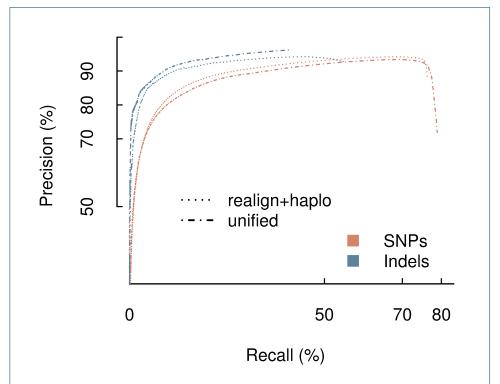


Figure 1 Comparison of the hybrid results on the human dataset depending on the GATK pipeline. "realign+haplo" stands for the using the GATK realigner and of the HaplotypeCaller, while "unified" stands for the *UnifiedGenotyper* only.

DiscoSnp++ was run independently on populations E1, E2 and E3. For each population, DiscoSnp++ was applied on the eight read sets corresponding to the eight time points, with the default parameters and c=11, D=60 (searching for indels of length at most 60) and P=4 (authorizing up to 4 close SNPs in a unique bubble).

```
The command were the following:
run_discoSnp++.sh -r "'ls data/E1_gen*'" -D 60 -P 4 -c 11
run_discoSnp++.sh -r "'ls data/E2_gen*'" -D 60 -P 4 -c 11
run_discoSnp++.sh -r "'ls data/E3_gen*'" -D 60 -P 4 -c 11
```

1 VCF creation

1.1 Mapping predictions on a reference genome

Depending on the user choice and the availability of a reference genome, DiscoSnp++ may map its predictions. We performed tests using BWA [5] and we provide an automatic pipeline based on this tool output.

The reference genome and the predictions may present differences due to distinct individuals, bad assembly of the reference or reference species distant from analyzed reads. Thus, errors (indel and mismatches) are authorized during the mapping. By default we use BWA authorizing at most t=3 errors and using a seed of length 10. Each prediction (each couple of sequence $\{S_A, S_B\}$) is considered as mapped at a unique genomic position if there exists a minimal distance $d \leq t$ for which either S_A and S_B have a unique match on the reference genome. In this case, the position of this match is indicated in the VCF file. Algorithm 1, presents how this unique position, if exists, is detected for each predicted variant.

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Algorithm 1 Mapping and validation of mapped variants

```
1: Map DiscoSnp++ output on the reference genome, authorizing at most t errors (indels and mis-
    matches)
   for each DiscoSnp++ prediction p (couple of sequence \{S_A,S_B\}) do
        for d (distance) in range 0:t do
 4:
           Compute U = \{\text{genomic positions where } S_A \text{ and/or } S_B \text{ mapped at distance } <= d\}
 5:
           if |U| == 1 then
               Set prediction p as Mapped at this unique position (within distance d)
 6:
 7:
               Break
 8:
           end if
 9:
           if |U| > 1 then
               Set prediction p Multiple Mapped
10:
11:
           end if
12.
13:
        end for
14:
        if p never set as "Mapped" (Unique position or Multiple Mapping) then
15
           set p as "Unmapped"
16.
17: end for
```

1.2 Detailed VCF content

The proposed VCF file contains the following fields:

- **CHROM**: Chromosome id where the prediction is mapped, or '.' if no reference genome provided or if no (unique) mapping of the variant
- POS:
 - If a reference genome is provided and if the couple is mapped on a unique position: position of the variant
 - If a reference genome is provided and if the couple is not uniquely mapped: one of the positions of the variant (the first reported by BWA)
 - Else (no reference genome provided or couple unmapped): '.'
- **ID**: identification of the SNP or the indel.
- REF:

For SNPs:

- If one of the two predictions is mapped on the genome: the nucleotide present on the reference genome at the variant position.
- Else, or if no reference genome provided: the lexicographically smallest of the two variants

For Indels: one of the two predictions is longer than the other.

- If the smallest prediction is mapped on the genome: the nucleotide present on the reference genome at the variant position-1.
- If the longest prediction is mapped on to the genome: the sequence of the reference genome from the variant position-1 to the variant position+size of the indel.
- Else, or if no reference genome provided: the lexicographically smallest of the two variants

Remark: the REF (and ALT) sequences are extracted from the reference genome is forward strand. If the reverse complement of the prediction is mapped, the reported REF and ALT sequences correspond to the reverse complement of the DiscoSnp++ predictions.

- ALT: The variant non reported as the "REF" variant
- QUAL: '*'
- FILTER:

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- PASS if the variant is mapped on a unique position
- MULTIPLE if the variant is mapped on multiple positions
- '.' if no reference genome provided

• INFO:

- **Ty**: Type of variant: 'INDEL' or 'SNP' XXX
- **Rk**: Rank of the prediction computed by *DiscoSnp++*
- DT: If the variant is mapped on a unique position: distance of the mapping (see Algorithm 1). If the variant is unmapped or mapped on multiple positions: '-1'
- GT: Genotype: TODO XXX
- **UL**: Length of the left unitig ('None' if not computed)
- UR: Length of the right unitig ('None' if not computed)
- **CL**: Length of the left contig ('None' if not computed)
- CR: Length of the right contig ('None' if not computed)
- **DP**: Combined depth across all samples (average)
- Genome: Applies only for SNPs when a reference genome is provided ('<INS>' or '' for indels and '.'when no reference genome provided). Nucleotide on the reference genome at the variant position. Important Remark: This is equal to the "REF" field only if one of the two prediction matches the reference.
- Sd: Applies only when a reference genome is provided ('.' if no reference genome provided or if the variant was not mapped). Strand of the prediction mapping. '1': Forward, '-1': Reverse. Important Remark: Fields "REF", "ALT" and "AR" are based on the mapped predictions.

2 Genotyping

 c_u : Coverage upper path

 c_l : Coverage lower path

err: Uniform error rate(0.01)

prior: heterozygous prior(0.33)

$$\begin{split} like_{0/0} &= -10 \log_{10} \left((1 - err)^{c_u} \times err^{c_l} \times C^{c_u}_{c_u + c_l} \times \frac{1 - prior}{2} \right) \\ like_{1/1} &= -10 \log_{10} \left(err^{c_u} \times (1 - err)^{c_l} \times C^{c_u}_{c_u + c_l} \times \frac{1 - prior}{2} \right) \\ like_{0/1} &= -10 \log_{10} \left(\left(\frac{1}{2} \right)^{c_u + c_l} \times prior \right) \\ min(like_{0/0}, like_{1/1}, like_{0/1}) &\Rightarrow 0/0, \text{ or } 1/1, \text{ or } 0/1 \end{split}$$

3 Algorithm: Bubble walking

References

- Rizk, G., Lavenier, D.: GASSST: global alignment short sequence search tool. Bioinformatics (Oxford, England) 26(20), 2534–40 (2010). doi:10.1093/bioinformatics/btq485
- Altshuler, D.M., Durbin, R.M., Abecasis, G.R., Bentley, D.R., Chakravarti, A., Clark, A.G., Donnelly, P., Eichler, E.E., Flicek, P., Gabriel, S.B., Gibbs, R.A., Green, E.D., Hurles, M.E., Knoppers, B.M., Korbel, J.O., Lander, E.S., Lee, C., Lehrach, H., Mardis, E.R., Marth, G.T., Mcvean, G.A., Nickerson, D.A., Schmidt, J.P., Sherry,

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Algorithm 2 SNP & Indels caller

```
1: #Search for SNPs
    for each couple of successor kmers kmer_1, kmer_2 do
       expand(kmer_1, kmer_2, 1 SNPs already detected up to P authorized close SNPs)
 3.
 4: end for
 5:
    #Search for Indels (whatever predicted SNPs)
 6:
   for each path selected as the <code>extended_path</code> do
        Breadth first extend the extended\_path (up to D nuc.)
 8:
       if Last character of the extension == last char. of the non expanded kmer then
 9:
           expand(kmer_1, kmer_2, 1) variant already detected up to 1 authorized variant)
10:
        end if
11: end for
```

Algorithm 3 Expand two kmers

```
1: Test branching kmer_1, kmer_2. Exit if necessary
 2: Get kmer_1^+ and kmer_2^+ the unique possible extensions of kmer_1 and kmer_2 with the same \alpha.
     Note that with branching=2: there may exist several couple kmer_1^+, kmer_2^+, both extended with
     the same lpha
 3: if kmer_1^+ == kmer_2^+ then
         Finish the bubble & stop the expand
 4:
 5:
        Expand(kmer_1^+, kmer_2^+, 0 \text{ new SNP detected up to } P \text{ authorized close SNPs})
 6:
 7:
    end if
 8:
    if Number detected close SNPs < P then
         for kmer_1^+ and kmer_2^+ two kmers extending kmer_1 and kmer_2 with distinct \alpha,\beta do
 9:
             \begin{array}{c} \text{if } kmer_1^+ == kmer_2^+ \text{ then} \\ \text{Finish the bubble \& stop the expand} \end{array}
10:
11:
12:
                 Expand(kmer_1^+, kmer_2^+, 1 \text{ new SNP detected up to } P \text{ authorized close SNPs})
13:
14:
             end if
         end for
15
16: end if
```

S.T., Wang, J., Wilson, R.K., Dinh, H., Kovar, C., Lee, S., Lewis, L., Muzny, D., Reid, J., Wang, M., Fang, X.D., Guo, X.S., Jian, M., Jiang, H., Jin, X., Li, G.Q., Li, J.X., Li, Y.R., Li, Z., Liu, X., Lu, Y., Ma, X.D., Su, Z., Tai, S.S., Tang, M.F., Wang, B., Wang, G.B., Wu, H.L., Wu, R.H., Yin, Y., Zhang, W.W., Zhao, J., Zhao, M.R., Zheng, X.L., Zhou, Y., Gupta, N., Clarke, L., Leinonen, R., Smith, R.E., Zheng-Bradley, X., Grocock, R., Humphray, S., James, T., Kingsbury, Z., Sudbrak, R., Albrecht, M.W., Amstislavskiy, V.S., Borodina, T.A., Lienhard, M., Mertes, F., Sultan, M., Timmermann, B., Yaspo, M.L., Fulton, L., Fulton, R., Weinstock, G.M., Balasubramaniam, S., Burton, J., Danecek, P., Keane, T.M., Kolb-Kokocinski, A., McCarthy, S., Stalker, J., Quail, M., Davies, C.J., Gollub, J., Webster, T., Wong, B., Zhan, Y.P., Auton, A., Yu, F., Bainbridge, M., Challis, D., Evani, U.S., Lu, J., Nagaswamy, U., Sabo, A., Wang, Y., Yu, J., Coin, L.J.M., Fang, L., Li, Q.B., Li, Z.Y., Lin, H.X., Liu, B.H., Luo, R.B., Qin, N., Shao, H.J., Wang, B.Q., Xie, Y.L., Ye, C., Yu, C., Zhang, F., Zheng, H.C., Zhu, H.M., Garrison, E.P., Kural, D., Lee, W.P., Leong, W.F., Ward, A.N., Wu, J.T., Zhang, M.Y., Griffin, L., Hsieh, C.H., Mills, R.E., Shi, X.H., von Grotthuss, M., Zhang, C.S., Daly, M.J., DePristo, M.A., Banks, E., Bhatia, G., Carneiro, M.O., del Angel, G., Genovese, G., Handsaker, R.E., Hartl, C., McCarroll, S.A., Nemesh, J.C., Poplin, R.E., Schaffner, S.F., Shakir, K., Yoon, S.C., Lihm, J., Makarov, V., Jin, H.J., Kim, W., Kim, K.C., Rausch, T., Beal, K., Cunningham, F., Herrero, J., McLaren, W.M., Ritchie, G.R.S., Gottipati, S., Keinan, A., Rodriguez-Flores, J.L., Sabeti, P.C., Grossman, S.R., Tabrizi, S., Tariyal, R., Cooper, D.N., Ball, E.V., Stenson, P.D., Barnes, B., Bauer, M., Cheetham, R.K., Cox, T., Eberle, M., Kahn, S., Murray, L., Peden, J., Shaw, R., Ye, K., Batzer, M.A., Konkel, M.K., Walker, J.A., MacArthur, D.G., Lek, M., Herwig, R., Shriver, M.D., Bustamante, C.D., Byrnes, J.K., De la Vega, F.M., Gravel, S., Kenny, E.E., Kidd, J.M., Lacroute, P., Maples, B.K., Moreno-Estrada, A., Zakharia, F., Halperin, E., Baran, Y., Craig, D.W., Christoforides, A., Homer, N., Izatt, T., Kurdoglu, A.A., Sinari, S.A., Squire, K., Xiao, C.L., Sebat, J., Bafna, V., Burchard, E.G., Hernandez, R.D., Gignoux, C.R., Haussler, D., Katzman, S.J., Kent, W.J., Howie, B., Ruiz-Linares, A., Dermitzakis, E.T.: An integrated map of genetic variation from 1,092 human genomes. Nature 491, 56-65 (2012). doi:10.1038/nature11632

- 3. 1000 genome phase 1 vcf file.
 - $\mathsf{ftp://ftp.1000} \\ \mathsf{genomes.ebi.ac.uk/vol1/ftp/release/20110521/ALL.chr1.phase} \\ 1_release_v \\ 3.20101123.snps_indels_svs.genotypes.vcf.gz \\ \mathsf{genotypes.vcf.gz} \\ \mathsf{genot$
- Kvitek, D.J., Sherlock, G.: Whole genome, whole population sequencing reveals that loss of signaling networks is the major adaptive strategy in a constant environment. PLoS genetics 9(11), 1003972 (2013). doi:10.1371/journal.pgen.1003972
- Li, H., Durbin, R.: Fast and accurate short read alignment with Burrows-Wheeler transform. Bioinformatics 25(14), 1754–1760 (2009). doi:10.1093/bioinformatics/btp324

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```
DiscoSnp++
 for ((i=2;i<=31;i++)); do
 #Prepare input parameters
   \label{list="""} ist = ""; for((j=0;j<i;j++)); do list = list ""coli_muted_n_30_genome_$j\_reads.fasta; done = list = list ""; for((j=0;j<i;j++)); do list = list
 #Run discoSnp++
   run_discoSnp++.sh -r "$list" -p dsc_$i\_genomes -P 4 -D 10
 #(needs a compilation per number of input read sets):
for ((i=1;i<31;i++)); do make MAXK=31 NUM_COLS=$i cortex_var; done
 #Prepare input parameters
for ((i=0;i<30;i++)); do echo coli_muted_n_30_genome_$i\_reads.fasta > ind$i; done
for ((i=2;i<31;i++)); do
  for ((j=0;j<i;j++)); do echo -e "IND$j\tind$j\t.\t." >> INDEX$i; done;
 done
 #Prepare data
 for ((i=0;i<30;i++)); do
   cortex_var_31_c2 --se_list ind$i --kmer_size 31 --mem_height 20 --mem_width 75 \
       --dump_binary genome_$i\_reads.ctx --sample_id sample$i --remove_low_coverage_supernodes 3
 done
 for ((i=0;i<30;i++)); do
 #Prepare input parameters
   echo "genome_$i\_reads.ctx" > ind$i\_ctx
   for ((i=0;i<$nb;i++));
     do echo ind$i\_ctx >> my_cortex_list_ctx_$nb
   done
 #Detect variants
   cortex_var_31_c$nb --colour_list my_cortex_list_ctx_$nb --kmer_size 31 --mem_height 22 --mem_width 75 \
      --detect_bubbles1 0/1 --output_bubbles1 my_res_cortex_$nb --remove_low_coverage_supernodes 3
 done
                                                                                                          Hybrid approach
 #Assemblv
 SOAPdenovo-63mer pregraph -s soap.config -o soapNAR30A -K $k -d 5
 SOAPdenovo-63mer contig -g soapNAR30A
 \#remove contigs whose size is < 100:
python ./filter_fasta_by_length.py soapNAR30A.contig NAR30A_ref.contigs.fa 100
mv soapNAR3OA.contig NAR3OA_ref.contigs.fa
bowtie2-build -f NAR3OA_ref.contigs.fa NAR3OA_ref.contigs_index ;
 #Map reads
basen=coli_muted_n_30_genome_
 suffixn=_reads.fasta
 for i in $(seq 0 30); do
   bowtie2 -f --non-deterministic --threads 8 --rg-id "read$i" --rg "SM:read$i" \
     --rg "PL:Illumina" --rg "LB:simumima" -x NAR3OA_ref.contigs_index -U ${basen}${i}${suffixn} \ | samtools view -bS -> NAR3OA_${i}_bw2.bam;
   \verb|samtools| sort -m 25000000000 NAR30A_$\{i\}_bw2.bam NAR30A_$\{i\}_bw2.sorted.bam| | banda | ba
   \label{local_norm} \verb"mv NAR30A_${i}_bw2.sorted.bam.bam NAR30A_${i}_bw2.bam"
   samtools index NAR30A_${i}_bw2.bam
   samtools flagstat NAR30A_${i}_bw2.bam > NAR30A_${i}_bw2.flagstat
 #Variant calling
 samtools faidx coli_muted_ref.contigs.fa
 java -Xmx4g -jar ./CreateSequenceDictionary.jar R=coli_muted_ref.contigs.fa O=coli_muted_ref.contigs.dict
 gpar="-I coli_muted_0_bw2.bam"
 for i in $(seq 1 30); do
   gpar="$gpar -I coli_muted_${i}_bw2.bam"
   java -Xmx8g -jar /softs/local/GATK/2.8.1/GenomeAnalysisTK.jar -R coli_muted_ref.contigs.fa -T UnifiedGenotyper \
    -glm BOTH ${gpar} -o coli_muted_both_${i}.vcf
 done
```

Table 1 Commands used for calling SNPs and indels from 2 to 30 E. Coli read sets (coli_muted_n_30_genome_i_reads.fasta for i in [1,30]) with DiscoSnp++, cortex or the hybrid approach.

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```
DiscoSnp++
{\tt run\_discoSnp++.sh-r"humch1\_00096\_reads.fasta~humch1\_00100\_reads.fasta"-P~4~-D~10}
                                                              cortex
#Prepare data
for i in 096 100; do
 cortex_var_31_c2 --se_list data$i.txt --kmer_size 31 --mem_height 25 --mem_width 100 \
   --dump_binary genome_$i\_reads.ctx --sample_id sample$i --remove_low_coverage_supernodes 3
#Prepare parameters
for i in 096 100: do
 echo "genome_$i\_reads.ctx" > ind$i\_ctx
 echo ind$i\_ctx >> my_cortex_list_ctx
done
#Detect variants
cortex_var_31_c2 --colour_list my_cortex_list_ctx --kmer_size 31 --mem_height 25 --mem_width 100 \
 --detect_bubbles1 0,1/0,1 --output_bubbles1 my_res_cortex --remove_low_coverage_supernodes 3
                                                     Hybrid approach
#Assembly
SOAPdenovo-63mer pregraph -s soap.config -o soaphum -K $k -d 5
SOAPdenovo-63mer contig -g soaphum
#Remove contigs whose size is < 100:
./filter_fasta_by_length.py soaphum.contig hum_ref.contigs.fa 100
mv soaphum.contig hum_ref.contigs.fa
#Align reads
${path_bw2}bowtie2-build -f hum_ref.contigs.fa hum_ref.contigs_index
for i in 096 100; do
 bowtie2 -f --non-deterministic --threads 8 --rg-id "read$i" --rg "SM:read$i" --rg "PL:Illumina" \
--rg "LB:simumima" -x hum_ref.contigs_index -U /WORKS/tests_human/data/humch1_00$i\_reads.fasta \
 | ${path_sam}samtools view -bS - > hum_${i}_bw2.bam;
 samtools sort -m 25000000000 hum_${i}_bw2.bam hum_${i}_bw2.sorted.bam
 \label{local_norm_norm} \verb|mv hum_${i}_bw2.sorted.bam.bam hum_${i}_bw2.bam| \\
 \verb|samtools| index hum_${i}_bw2.bam|
 samtools flagstat hum_${i}_bw2.bam > hum_${i}_bw2.flagstat
done
#Variant calling
samtools faidx hum_ref.contigs.fa
java -Xmx4g -jar ./CreateSequenceDictionary.jar R=${ref} O=hum_ref.contigs.dict
\label{local_GATK_2.8.1} time~ \texttt{`grizk/bin/memusage java -Xmx62g -jar /softs/local/GATK/2.8.1/GenomeAnalysisTK.jar \setminus \texttt{`grizk/bin/memusage java -Xmx62g -jar /softs/local/GATK/2.8.1/GenomeAnalysisTK.jar \} \\
-R ${ref} \
-T HaplotypeCaller \
-I ${prefix}_096_bw2.bam -I ${prefix}_100_bw2.bam \
-o ${prefix}_both_HaplotypeCaller.vcf
Table 2 Commands used for calling SNPs and indels from two human chromosome 1 read sets
```

Table 2 Commands used for calling SNPs and indels from two human chromosome 1 read sets (humch1_00096_reads.fasta humch1_00100_reads.fasta) with DiscoSnp++, cortex or the hybrid approach.