



$$v_X \left(\frac{1}{R_1} + \frac{1}{R_2} + sC_2 + \frac{1}{R_3} \right) - \frac{1}{R_1} v_i - \frac{1}{R_2} v_o = 0 \quad (1)$$

$$\frac{1}{R_3} v_X = -sC_1 v_o \Rightarrow v_X = -sC_1 R_3 v_o \quad (2)$$

NOTA

② en ①

$$-(s c_1 R_3 v_0) \frac{R_2 R_3 + R_1 R_2 + R_3 R_1 + s R_1 R_2 R_3 c_2}{R_1 R_2 R_3} - \frac{1}{R_2} v_0 = \frac{1}{R_1} v_i$$

$$- \frac{[s^2 R_1 R_2 R_3 c_1 c_2 + s c_1 (R_1 R_2 + R_1 R_3 + R_2 R_3) + R_1] v_0}{R_1 R_2} = \frac{1}{R_1} v_i$$

$$T(s) = \frac{-R_2}{s^2 R_1 R_2 R_3 c_1 c_2 + s c_1 (R_1 R_2 + R_1 R_3 + R_2 R_3) + R_1}$$

$$T(s) = \frac{-R_2}{s^2 + s \frac{R_1 R_2 + R_1 R_3 + R_2 R_3}{R_1 R_2 R_3 c_2} + \frac{1}{R_2 R_3 c_1 c_2}}$$

ω_0^2 (above the constant term)
 $\frac{\omega_0}{Q}$ (below the coefficient of s)

$$T(s) = \frac{+K \omega_0^2}{s^2 + \frac{\omega_0}{Q} s + \omega_0^2}$$

$$\omega_0^2 = \frac{1}{R_2 R_3 c_1 c_2}$$

$$\left(\frac{\omega_0}{Q}\right)^2 = \left(\frac{R_1 R_2 + R_1 R_3 + R_2 R_3}{R_1 R_2 R_3 c_2}\right)^2$$

$$\frac{1}{R_2 R_3 c_1 c_2} = \frac{(R_1 R_2 + R_2 R_3 + R_1 R_3)^2}{R_1^2 R_2^2 R_3^2 c_2^2} \cdot Q^2 \quad | \quad K = R_2 / R_1$$

$$Q^2 = \frac{c_2 R_1^2 R_2 R_3}{c_1 (R_1 R_2 + R_2 R_3 + R_1 R_3)^2} \rightarrow Q = \frac{R_1 \sqrt{R_2 R_3 c_2}}{\sqrt{c_1} (R_1 R_2 + R_2 R_3 + R_1 R_3)}$$

NOTA

$$R_1 = R_2 = R_3 = 1\Omega ; C_1 = 0,01F ; C_2 = 1F$$

$$\omega_0^2 = \frac{1}{1\Omega \cdot 1\Omega \cdot 1F \cdot 0,01F} \Rightarrow \omega_0^2 = 100 s^{-2}$$

$$\omega_0 = 10 s^{-1}$$

$$Q = \frac{1\Omega \cdot \sqrt{1\Omega^2 \cdot 1F}}{\sqrt{0,01F} (1\Omega \cdot 1\Omega \cdot 3)} = 3,33 ; K = 1$$

$$T(s) = \frac{K \omega_0^2}{s^2 + \frac{\omega_0}{Q} s + \omega_0^2}$$

$$T(s) = \frac{100 s^{-2}}{s^2 + 3s + 100 \text{seg}^{-1}}$$

$$T(\omega) = T(s) \Big|_{s=j\omega} = \frac{100 \text{seg}^{-1}}{(100 \text{seg}^{-1} - \omega^2) + j\omega \cdot 3}$$

$$|T(\omega)| = \frac{100 \text{seg}^{-1}}{\sqrt{(100 \text{seg}^{-1} - \omega^2)^2 + (\omega \cdot 3)^2}}$$

b)

NORMALIZAMOS:

$$\omega_0 = 1 \Rightarrow \omega_0^2 = 1 = \frac{1}{R_2 R_3 C_1 C_2} \Rightarrow R_2 R_3 C_1 C_2 = 1 \quad ; \quad C_2 = \frac{1}{C_1} \\ R_1 = R_2 = R_3 = 1$$

$$K_{dB} = 10, \text{ dB} \rightarrow \text{GRÁFICO} \quad ; \quad C_1 = \frac{C_{1N}}{(\omega_0 \cdot R_2)} \\ \underbrace{4700 \text{ PF}} \quad \underbrace{1000}$$

$$K = \frac{R_2}{R_1}$$

$$C_2 = C_{2N} \left(\frac{\omega_0}{1000} \cdot R_2 \right) \\ \underbrace{47 \text{ PF}} \quad \underbrace{1000}$$

$$C_1 = \frac{1}{C_{2N}} \left(\omega_0 \cdot R_2 \right) \quad ; \quad C_{2N} = C_2 \omega_0 \cdot R_2$$

$$C_{2N} \cdot C_1 = \frac{1}{\omega_0 \cdot R_2} \quad ; \quad C_1 C_2 \omega_0 \cdot R_2 = \frac{1}{\omega_0 \cdot R_2}$$

$$R_2^2 = \frac{1}{\omega_0^2 \cdot C_1 C_2}$$

$$R_2 = 2,13 \text{ M}\Omega$$

$$\rightarrow R_1 = R_2 = R_3 = 1. \quad R_2 = 2,13 \text{ M}\Omega$$