

# My First Steps in Neuronal Networks (Beginners Guide)

Axel Roth

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# Chapter 1

## About

### 1.1 Me

Hello, my name is Axel Roth, and I'm pursuing a master's degree in mathematics in Germany while working part-time in finance as something between a data analyst and a full stack developer. I have a lot of experience with R and all of its features, but I have never written a line of Python code or worked with Neuronal Networks before. So, why am I writing a Python Beginner's Guide to Neuronal Networks in the first place? It's simple. I'm currently attending a lecture in which we're learning how to program a Neuronal Network from scratch using basic Python packages, and I'd like to share my experience. Furthermore, I learned everything I know from free internet sources, which is why I want to give something back. It's also a good use-case for me to write my first things in English.

### 1.2 The Book

This book will essentially be a transcript of my lecture, in which we will learn to program a simple Perceptron (the most basic Neuronal Network), then progress to a multilayer Perceptron, and finally to a brief overview of decision trees. On this journey, we'll put the Neuronal Network to the test in a variety of scenarios that are simple to replicate. Because these are my first steps in this field, I apologize for my terrible spelling and cannot guarantee the highest quality, but this may be the best way to educate and attract uninitiated readers to take a look.

### 1.3 How it works

I'm writing this book in the R-Studio IDE, using the Bookdown framework, and using the reticulate package to embed python code. This is why I need to load the Python interpreter in the R-chunk below:

```
library(reticulate)
Sys.setenv(RETICULATE_PYTHON =
  ↪ "D:\\WinPython2\\WPy64-3950\\python-3.9.5.amd64\\")
```

In addition, I use R-Studio, R, and Python in a portable manner. It comes in handy when you need to switch between university and home computers, for example. Python can be downloaded through WinPython to be fully portable, and R-Studio supports it. I created all of the Neural Network images using the free website draw.io and im using QuillBot to compensate for my poor spelling skills. I would recommend jupyter lab or PyCharm if you are new to Python and have never used R.

## Chapter 2

# Single Perceptron

Throughout this chapter, I will show you how to program a single Perceptron in Python using only the numpy package. Numpy uses a vectorizable math structure, which allows you to easily perform normal matrix multiplications with just an expression (i always interpret vectors as one dimensional matrices!). In most cases, it is just a matter of translating mathematical formulas into python code without altering their structure. Before we begin, let's identify the necessary parameters, which will be explained later:

Number of iterations over all the training dataset := **epochs**

Learning rate :=  $\alpha$  = **alpha**

Bias value :=  $\beta$  = **bias** and the activation function:

$$step(s) = \begin{cases} 1, & s \geq \beta \\ 0, & s < \beta \end{cases}$$

This function is named the heavyside-function and should be the easiest activation function to understand. If the weighted sum is smaller than the bias  $\beta$ , it will send the value zero to the next neuron. It is the same in the brain. If there is not enough electricity, the neuron will not activate, and the next does not receive electricity.

The training dataset is the following:

$$\left[ \begin{array}{cc|c} x_{i,1} & x_{i,2} & y_i \end{array} \right]$$
$$\left[ \begin{array}{cc|c} 0 & 0 & 0 \\ 0 & 1 & 1 \\ 1 & 0 & 1 \\ 1 & 1 & 1 \end{array} \right]$$

The provided training dataset contains the X matrix with two inputs for each scenario and the Y matrix with the correct output (each row contains the input

and output of one scenario). If your looking closely, you can see that this is the OR-Gate. Later you will understand, why these type of problems are the only suitable things to do with a single neuron.

The needed python imports are the following:

```
import numpy as np
import matplotlib.pyplot as pyplot
```

( Do you see more imports than only the numpy package? Yes or No )

Now that we have all the needed parameters and settings, i can give you a quick overview of the algorithm.

## 2.1 Neural Network Basics

The forward pass and the backward pass are the two primary parts of a NN. To calculate the output, we calculate the weighted sum of each input neuron with the layer's weights and evaluate the activation function with in the forward pass. We analyze the inaccuracy in the backward pass and modify the weights accordingly. That's it! That is exactly what a Neuronal Network is doing. Everything was explained to you. Enjoy your life... No, no, no, we'll take a closer look:)

In a single Perceptron, what is the forward pass? It's just like I mentioned, evaluating the activation function using the weighted sum, so for one scenario of the training dataset, you have:

$$\text{step}(W \cdot x_i^T) = y_i$$

Using this formula to iterate over all scenarios in the training dataset is the standard approach... But I don't think that's the best way to put it because it's difficult to interpret it for all scenarios at the same time.

My next strategy is to use a single formula to account for all scenarios in the training dataset. If your data isn't too large, this is also a much faster method. First and foremost, we must interpret the new  $W$  and  $X$  dimensions. We have  $X$  as:

$$X = \begin{bmatrix} 0 & 0 \\ 0 & 1 \\ 1 & 0 \\ 1 & 1 \end{bmatrix}$$

each row describes the inputs for each neuron in the scenario  $i$ . For the weights  $W$  do we have for example:

$$W = \begin{bmatrix} 0.1 \\ 0.2 \end{bmatrix}$$



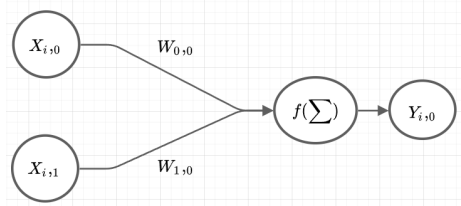
The new formula looks like this:

$$\text{step}(X * W) = Y$$

The  $*$  symbol defines a matrix to matrix multiplication. For example if you take a look at the  $i$ -th row (scenario) of  $X$  you will see the following:

$$Y_{i,0} = \text{step}([X_{i,0} \cdot W_{0,0} + X_{i,1} \cdot W_{1,0}])$$

and  $Y_{i,0}$  is the approximated output of the  $i$ -th scenario. Now can we look at the NN and compare the formula with it:



Yes it is the same, its the weighted sum of the inputs and evaluated the activation function with it, to calculate the output of the scenario  $i$ .

## 2.2 Forward pass

Now can we create the so called `forward()` function in python:

```
def forward(x, w):
    return( step(x @ w) )
```

(Numpy provides us with the `@` symbol to make a matrix to matrix multiplication and the `.T` to transpose)

Because we want to put one dimensional matrices into the `step()` function, its necessary to use numpy for the if-else statement:

```
def step(s):
    return( np.where(s >= bias, 1, 0) )
```

In the next step will we create an small example for the forward pass:

```
X = np.array([
    [0,0],
    [0,1],
    [1,0],
```

```

    [1,1],
  ])
  W = np.array([
    [0.1],
    [0.2]
  ])
  bias = 1
  Y_approx = forward(X, W)
  print(Y_approx)

```

```

## [[0]
##  [0]
##  [0]
##  [0]]

```

And these are all the generated outputs of our NN over all scenarios. Now do we need to calculate the error and adjust the weights accordingly.

## 2.3 Backward pass

We need the Delta-Rule to adjust the weights in a single Perceptron:

$$W(t+1) = W(t) + \Delta W(t)$$

with

$$\Delta W(t) = \alpha \cdot X^T * (Y - \hat{Y})$$

and  $\hat{Y}$  is the output of the NN. Translated to code it is:

```

def backward(W, X, Y, alpha, Y_approx):
    return(W + alpha * X.T @ (Y - Y_approx))

```

With the result of the forward pass and the correct outputs, do we have the following:

```

Y = np.array([
    [0],
    [1],
    [1],
    [1]
])
alpha = 0.01
W = backward(W, X, Y, alpha, Y_approx)
print(W)

```

```
## [[0.12]
##  [0.22]]
```

and these are the new weight.

## 2.4 Single Perceptron

Now do we want to do the same process multiple times, to train the NN:

```
X = np.array([
    [0,0],
    [0,1],
    [1,0],
    [1,1],
])
Y = np.array([
    [0],
    [1],
    [1],
    [1]
])
W = np.array([
    [0.1],
    [0.2]
])
alpha = 0.01
bias = 1
epochs = 100

errors = []
for i in range(epochs):
    Y_approx = forward(X, W)
    errors.append(Y - Y_approx)
    W = backward(W, X, Y, alpha, Y_approx)
```

The KNN is trained. In the next step, we will analyze the errors of each epoch. The best way to do so is to measure the mean-square-error with the following formula:

$$Errors = \frac{1}{2} \cdot \sum (Y - \hat{Y})^2$$

or as python code:

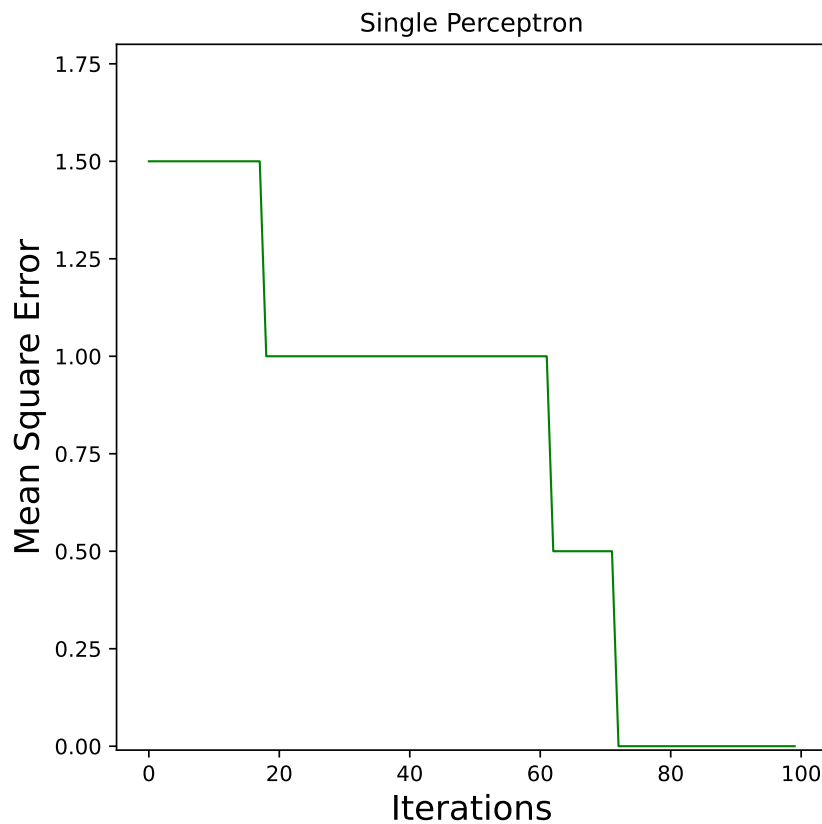
```
def mean_square_error(error):  
    return( 0.5 * np.sum(error ** 2) )
```

Now do we need to calculate the mean-square-error for each element in the list `errors` which can be performed with `map()`:

```
mean_square_errors = np.array(list(map(mean_square_error,  
↪ errors)))
```

To plot the errors, im using the following function:

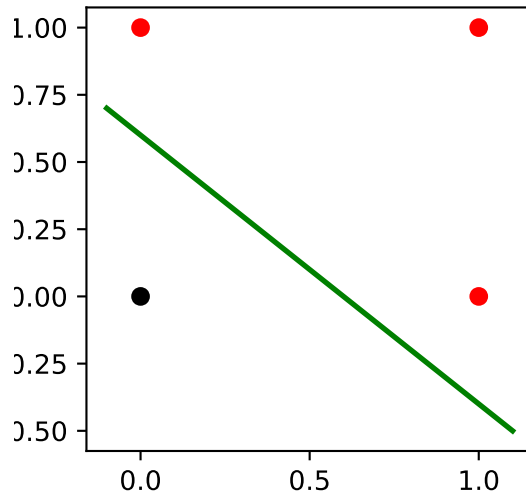
```
def plot_error(errors, title):  
    x = list(range(len(errors)))  
    y = np.array(errors)  
    pyplot.figure(figsize=(6,6))  
    pyplot.plot(x, y, "g", linewidth=1)  
    pyplot.xlabel("Iterations", fontsize = 16)  
    pyplot.ylabel("Mean Square Error", fontsize = 16)  
    pyplot.title(title)  
    pyplot.ylim(-0.01,max(errors)*1.2)  
    pyplot.show()  
  
plot_error(mean_square_errors, "Single Perceptron")
```



If you survived until now, you have learned how to program a single Perceptron!

## 2.5 Why does it work?

A single Perceptron with the heavyside activationfunction defines a classifier with the outputs 0 and 1. To find the correct solution, it needs to define a combination of weights and bias so that the inputs can be transferred to the groups  $X \cdot W \geq \beta$  or  $X \cdot W < \beta$ . The single Perceptron only converges to the given results, if the inputs could be splitted into groups by a straight line in the graph. For example the OR-Gate:



The red points (equals  $Y_i = 1$ ) and the black points (equals  $Y_i = 0$ ) can be split up with a straight line. If this isn't possible, as in the XOR-Gate, the single Perceptron will never find a combination of bias and weights to perform well. This explains why we need atleast multiple layers, as described in the chapter on multilayer Perceptrons. Here can you find a good source with more explanation.

## 2.6 Appendix (complete code)

```
import numpy as np
import matplotlib.pyplot as pyplot

X = np.array([
    [0,0],
    [0,1],
    [1,0],
    [1,1],
])
Y = np.array([
    [0],
    [1],
    [1],
    [1]
])
```

```

W = np.array([
    [0.1],
    [0.2]
])
alpha = 0.01
bias = 1
train_n = 100

def step(s):
    return( np.where(s >= bias, 1, 0) )

def forward(X, W):
    return( step(X @ W) )

def backward(W, X, Y, alpha, Y_approx):
    return(W + alpha * X.T @ (Y - Y_approx))

errors = []
for i in range(train_n):
    Y_approx = forward(X, W)
    errors.append(Y - Y_approx)
    W = backward(W, X, Y, alpha, Y_approx)

def mean_square_error(error):
    return( 0.5 * np.sum(error ** 2) )

mean_square_errors = np.array(list(map(mean_square_error,
↵ errors)))

def plot_error(errors, title):
    x = list(range(len(errors)))
    y = np.array(errors)
    pyplot.figure(figsize=(6,6))
    pyplot.plot(x, y, "g", linewidth=1)
    pyplot.xlabel("Iterations", fontsize = 16)
    pyplot.ylabel("Mean Square Error", fontsize = 16)
    pyplot.title(title)
    pyplot.ylim(-0.01,max(errors)*1.2)
    pyplot.show()

```

```
plot_error(mean_square_errors, "Single Perceptron")
```



## Chapter 3

# Adding trainable Bias

The single Perceptron, you saw in the previews chapter had the following activation function:

$$step(s) = \begin{cases} 1, & s \geq \beta \\ 0, & s < \beta \end{cases}$$

with  $\beta = 1$ . It is the perfect  $\beta$  for the given training dataset. But what happens if you shift the training data for example adding  $-5$  to the  $X$  matrix? Now it will never find the correct answer. That is because you need to select the  $\beta$  accordingly. But this wouldn't be intelligent to search for each dataset the optimal  $\beta$  by hand.

### 3.1 Generalising the Bias

First of all do we need to generalise the use of the bias, stating with the generalization of the activation function:

$$step(s) = \begin{cases} 1, & s \geq 0 \\ 0, & s < 0 \end{cases}$$

Now can we list it in the weighted sum:

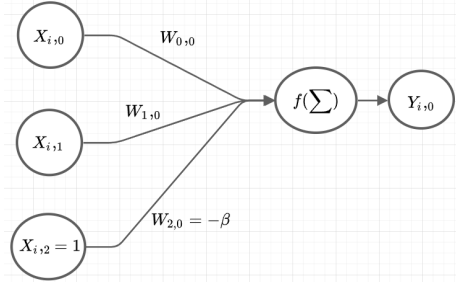
$$step(X * W - \beta) = Y$$

But we have the same problem as previews, because we need to specify the  $\beta$  explicit. Adding the bias to the training process is done by adding ones on the right side of the  $X$  matrix and adding the negative bias to the last row of  $W$ . The output of one scenario is calculated as the following:

$$Y_{i,0} = step([X_{i,0} \cdot W_{0,0} + X_{i,1} \cdot W_{1,0} + X_{i,2} \cdot W_{2,0}]) = step([X_{i,0} \cdot W_{0,0} + X_{i,1} \cdot W_{1,0} - \beta])$$

The resulting NN includes the bias into the re-adjusting process of the backward pass, because of that we will generate a random number for the bias that will be corrected anyway.

Now we have a NN that looks like all the other pictures of a single Perceptron in the internet:



The same step can be made with the following python code:

```
X = np.array([
    [0,0],
    [0,1],
    [1,0],
    [1,1],
])-5
X = np.append(X, np.array([np.ones(len(X))]).T, axis=1)

W = np.array([
    [0.1],
    [0.2]
])
W = np.append(W, -np.array([np.random.random(len(W[0]))]).T,
    ↪ axis=0)

print("X: \n", X)
print("W: \n", W)
```

We added  $-5$  to the  $X$  matrix to simulate the problem of shifted data, added ones on the left side of  $X$  and added negative random numbers in  $(0, 1)$  to the weights. Yes, if you would have a clue, what  $\beta$  would be great for the given problem, its better to choose it explicit. The new NN is slower, because it needs to find a good  $\beta$  by it self.

### 3.2 Appendix (complete code)

The complete code is the following:

```

np.random.seed(0)

X = np.array([
    [0,0],
    [0,1],
    [1,0],
    [1,1],
]) - 5
X = np.append(X, np.array([np.ones(len(X))]).T, axis=1)

W = np.array([
    [0.1],
    [0.2]
])
W = np.append(W, -np.array([np.random.random(len(W[0]))]).T,
    ↪ axis=0)

Y = np.array([
    [0],
    [1],
    [1],
    [1]
])

alpha = 0.01
epochs = 1000

def step(s):
    return( np.where(s >= 0, 1, 0) )

def forward(X, W):
    return( step(X @ W) )

def backward(W, X, Y, alpha, Y_approx):
    return(W + alpha * X.T @ (Y - Y_approx))

errors = []
for i in range(epochs):
    Y_approx = forward(X, W)
    errors.append(Y - Y_approx)
    W = backward(W, X, Y, alpha, Y_approx)

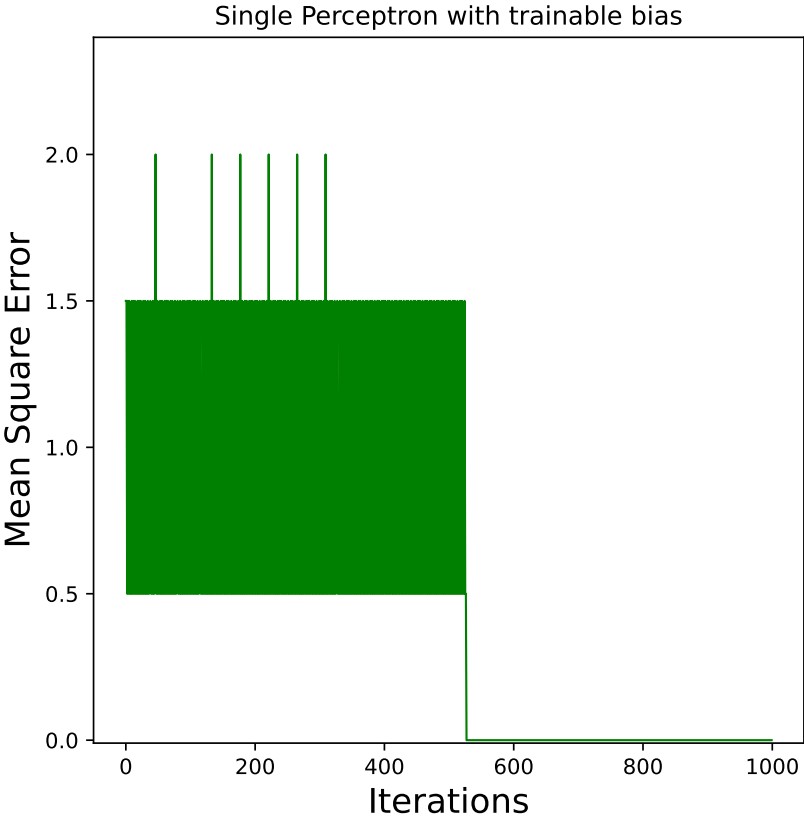
```

```
def mean_square_error(error):
    return( 0.5 * np.sum(error ** 2) )

mean_square_errors = np.array(list(map(mean_square_error,
↪ errors)))

def plot_error(errors, title):
    x = list(range(len(errors)))
    y = np.array(errors)
    pyplot.figure(figsize=(6,6))
    pyplot.plot(x, y, "g", linewidth=1)
    pyplot.xlabel("Iterations", fontsize = 16)
    pyplot.ylabel("Mean Square Error", fontsize = 16)
    pyplot.title(title)
    pyplot.ylim(-0.01,max(errors)*1.2)
    pyplot.show()

plot_error(mean_square_errors, "Single Perceptron with trainable
↪ bias")
```

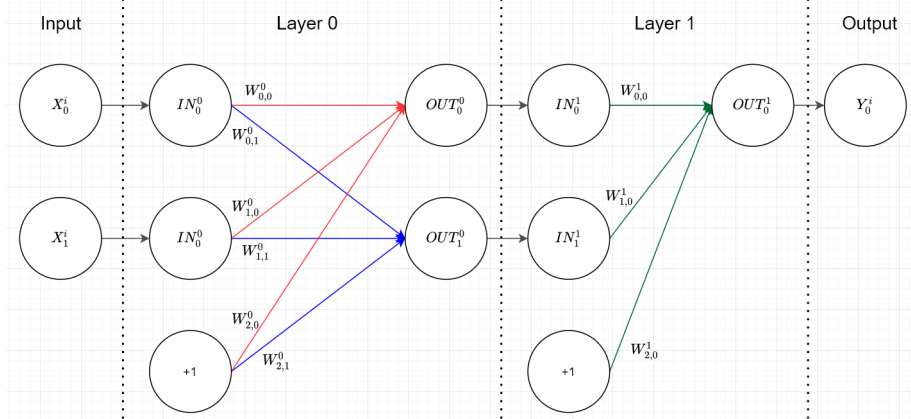




## Chapter 4

# Multilayer Perceptrons (MLP)

Multiple layers of neurons make up a multilayer Perceptron. As a result, we must calculate the forward pass several times, as well as the backward pass. First and foremost, do we need to broaden some definitions in order to support this behavior? The NN of the following image is what we want to do:



It's my own definition of layers since I believed it would be easier to transition from  $n$  to  $n + 1$  hidden layers if they were displayed as indicated in the image. By evaluating  $f(IN^{layer} \cdot W^{layer}) = OUT^{layer}$  and just transferring the result to the next layer like  $OUT^{layer} = IN^{layer+1}$ , with  $f$  as the chosen activation function, you can see that each layer has the identical procedure in the forward pass. We'll choose the sigmoid function as the activation function  $f$  because it has a simple deviation  $f'$  which is used for the backward pass and behaves similarly to the heavyside function with an output between 0 and 1.

```
def sigmoid(x):
    return 1.0 / (1.0 + np.exp(-x))

def deriv_sigmoid(x):
    return x * (1 - x)
```

Additionally will we choose the XOR-Gate as training dataset and generate random weights in a very generic approach:

```
X = np.array([
    [0,0],
    [0,1],
    [1,0],
    [1,1],
])

Y = np.array([
    [0],
    [1],
    [1],
    [0]
])

n_input = len(X[0])
n_output = len(Y[0])
hidden_layer_neurons = [2] # the 2 means that there is one hidden
    ↪ layer with 2 neurons

def generate_weights(n_input, n_output, hidden_layer_neurons):
    W = []
    for i in range(len(hidden_layer_neurons)+1):
        if i == 0: # first layer
            W.append(np.random.random((n_input+1,
    ↪ hidden_layer_neurons[i]))))
        elif i == len(hidden_layer_neurons): # last layer
            W.append(np.random.random((hidden_layer_neurons[i-1]+1,
    ↪ n_output)))
        else: # middle layers
            W.append(np.random.random((hidden_layer_neurons[i-1]+1,
    ↪ hidden_layer_neurons[i]))))

    return(W)

W = generate_weights(n_input, n_output, hidden_layer_neurons)
```



```
print("W[0]: \n", W[0])
print("W[1]: \n", W[1])

## W[0]:
## [[0.5488135  0.71518937]
##  [0.60276338 0.54488318]
##  [0.4236548  0.64589411]]
## W[1]:
## [[0.43758721]
##  [0.891773  ]
##  [0.96366276]]
```

The neurons for the hidden layers are generated using the `hidden_layer_neurons` list, while the input and output layer neurons are calculated from the training dataset. `hidden_layer_neurons = [4,2]`, for example, can construct two hidden layers with 4 and 2 neurons. I didn't choose the bias because it is automatically rectified. Is it now necessary to construct a helper function to add the biases to the last column of the inputs, like follows:

```
def add_ones_to_input(x):
    return(np.append(x, np.array([np.ones(len(x))]).T, axis=1))
```

## 4.1 Forward pass

The structure of the new forward function looks exactly like in the single Perceptron:

```
def forward(x, w):
    return( sigmoid(x @ w) )
```

Now we have everything to calculate the forward pass of the NN from above with the generated weights step by step:

```
IN = []
OUT = []

# layer 0
i = 0
IN.append( add_ones_to_input(X) )
OUT.append( forward(IN[i], W[i]) )
```

```

# layer 1
i = 1
IN.append( add_ones_to_input(OUT[i-1]) )
OUT.append( forward(IN[i], W[i]) )

# error
Y-OUT[-1]

## array([[ -0.85974823],
##        [ 0.12242041],
##        [ 0.12015376],
##        [-0.89115202]])

```

Thats all! We calculated the forward pass in a very generic way for the NN with 2 input neurons, 2 hidden neurons and 1 output neuron for all 4 scenarios at the same time. Sadly is the forward pass the easiest part of the multilayer Perceptron :)

## 4.2 Backward pass

The weights will be adjusted using the backpropagation algorithm, which is a variant of the descent gradient algorithm. Calculating the sensitives of the outputs according to the activation function multiplied by the error that occurred is done in the output layer. On all other layers, it's calculated by reversing the previously calculated gradient, splitting it up on each neuron by the previews weights, and multiplying the sensitivity of that layer's outputs by the activation function's sensitivity. The following is the formula:

$$grad^i = \begin{cases} f'(OUT^i) \cdot (Y - OUT^i), & i = \text{last layer} \\ f'(OUT^i) \cdot (grad^{i+1} * \widetilde{W}^{i+1\ T}), & \text{else} \end{cases}$$

with  $\widetilde{W}$  as the weights of the layer  $i$ , without the connection to the bias neuron. You can calculate  $\widetilde{W}$  in our datastructure by removing the last row. The gradients for the backward pass are calculated using the following code:

```

grad = [None] * 2

# layer 1
i = 1
grad[i] = deriv_sigmoid(OUT[i]) * (Y-OUT[i])

# layer 0

```

```
i = 0
grad[i] = deriv_sigmoid(OUT[i]) *(grad[i+1] @
↳ W[i+1][0:len(W[i+1])-1].T) # without bias weights
```

You can now examine the gradient of the last layer and the direction in which it is displayed:

```
print("Y: \n",Y)
print("OUT: \n",OUT[1])
print("grad: \n",grad[1])
```

```
## Y:
## [[0]
## [1]
## [1]
## [0]]
## OUT:
## [[0.85974823]
## [0.87757959]
## [0.87984624]
## [0.89115202]]
## grad:
## [[-0.10366948]
## [ 0.01315207]
## [ 0.01270227]
## [-0.08644184]]
```

The gradient appears to be pointing in the direction of drifting the output *OUT* closer to the desired output *Y*. The gradient descent algorithm accomplishes exactly that. The weights with the gradients and the learningrate  $\alpha$  must then be adjusted according to the direction of the gradients using the following formula:

$$W_{new}^i = W_{old}^i + \alpha \cdot (IN^i{}^T * grad^i)$$

After the first epoch, we get the following results for the adjusted weights in the example above:

```
alpha = 0.03

W[1] = W[1] + alpha * (IN[1].T @ grad[1])
W[0] = W[0] + alpha * (IN[0].T @ grad[0])
```

This was the forward and backward pass process in a multilayer Perceptron with two input neurons, two hidden layer neurons, and one output neuron for

one epoch. It's simple to use the above code to make a more generic NN with a variable number of hidden layers and variable training datasets for a given number of epochs, as shown in the appendix below.

### 4.3 Appendix (complete code)

```
import numpy as np
import matplotlib.pyplot as pyplot
np.random.seed(0)

X = np.array([
    [1,1],
    [0,1],
    [1,0],
    [0,0],
])

Y = np.array([
    [0],
    [1],
    [1],
    [0]
])

n_input = len(X[0])
n_output = len(Y[0])
hidden_layer_neurons = [2]

def generate_weights(n_input, n_output, hidden_layer_neurons):
    W = []
    for i in range(len(hidden_layer_neurons)+1):
        if i == 0: # first layer
            W.append(np.random.random((n_input + 1,
↪ hidden_layer_neurons[i])))
        elif i == len(hidden_layer_neurons): # last layer
            W.append(np.random.random((hidden_layer_neurons[i-1]+1,
↪ n_output)))
        else: # middle layers
            W.append(np.random.random((hidden_layer_neurons[i-1]+1,
↪ hidden_layer_neurons[i])))
    return(W)
```

```

def add_ones_to_input(x):
    return(np.append(x, np.array([np.ones(len(x))]).T, axis=1))

W = generate_weights(n_input, n_output, hidden_layer_neurons)

def sigmoid(x):
    return 1.0 / (1.0 + np.exp(-x))

def deriv_sigmoid(x):
    return x * (1 - x)

def forward(x, w):
    return( sigmoid(x @ w) )

def backward(IN, OUT, W, Y, grad, k):
    if k == len(grad)-1:
        grad[k] = deriv_sigmoid(OUT[k]) * (Y-OUT[k])
    else:
        grad[k] = deriv_sigmoid(OUT[k]) *(grad[k+1] @
↪ W[k+1][0:len(W[k+1])-1].T)
    return(grad)

alpha = 0.03
errors = []
for i in range(40000):
    IN = []
    OUT = []
    grad = [None]*len(W)
    for k in range(len(W)):
        if k==0:
            IN.append(add_ones_to_input(X))
        else:
            IN.append(add_ones_to_input(OUT[k-1]))
            OUT.append(forward(x=IN[k], w=W[k]))

    errors.append(Y - OUT[-1])

    for k in range(len(W)-1,-1, -1):
        grad = backward(IN, OUT, W, Y, grad, k)

    for k in range(len(W)):
        W[k] = W[k] + alpha * (IN[k].T @ grad[k])

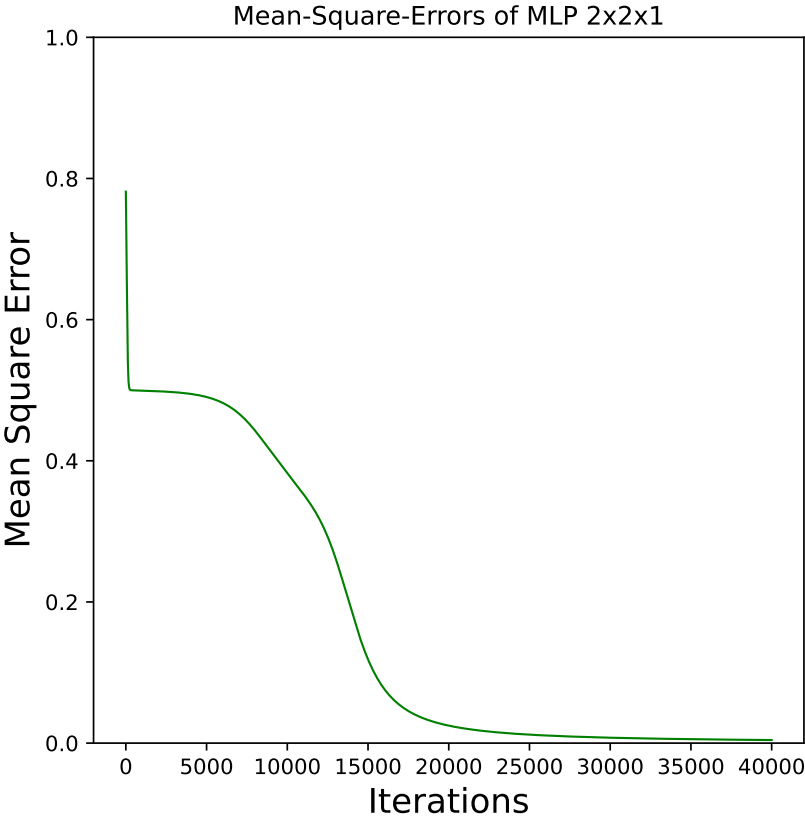
```

```
def mean_square_error(error):
    return( 0.5 * np.sum(error ** 2) )

mean_square_errors = np.array(list(map(mean_square_error,
↪ errors)))

def plot_error(errors, title):
    x = list(range(len(errors)))
    y = np.array(errors)
    pyplot.figure(figsize=(6,6))
    pyplot.plot(x, y, "g", linewidth=1)
    pyplot.xlabel("Iterations", fontsize = 16)
    pyplot.ylabel("Mean Square Error", fontsize = 16)
    pyplot.title(title)
    pyplot.ylim(0,1)
    pyplot.show()

plot_error(mean_square_errors, "Mean-Square-Errors of MLP 2x2x1")
```







## Chapter 5

# MLP example (Credit Default)

Now can we use our generic MLP model from the previews chapter to forecast real life credit defaults. The csv can be downloaded from Kaggle Data Source or from my github repo in the example\_data folder.

### 5.1 Loading and analysing the data

First all do we need to load the csv via pandas and analyse it:

```
import numpy as np
import pandas as pd
import matplotlib.pyplot as pyplot
pd.set_option('display.float_format', '{:.2f}'.format)
np.random.seed(0)

data =
↪ pd.read_csv("example_data/credit_risk_dataset.csv").fillna(0)

data.shape
data.head()
```

```
## (32581, 12)
##   person_age  person_income  person_home_ownership  person_emp_length  loan_intent  loan_grade
## 0          22         59000             RENT          123.00      PERSONAL             D
## 1          21          9600              OWN           5.00      EDUCATION             B
```

## 2	25	9600	MORTGAGE	1.00	MEDICAL
## 3	23	65500	RENT	4.00	MEDICAL
## 4	24	54400	RENT	8.00	MEDICAL

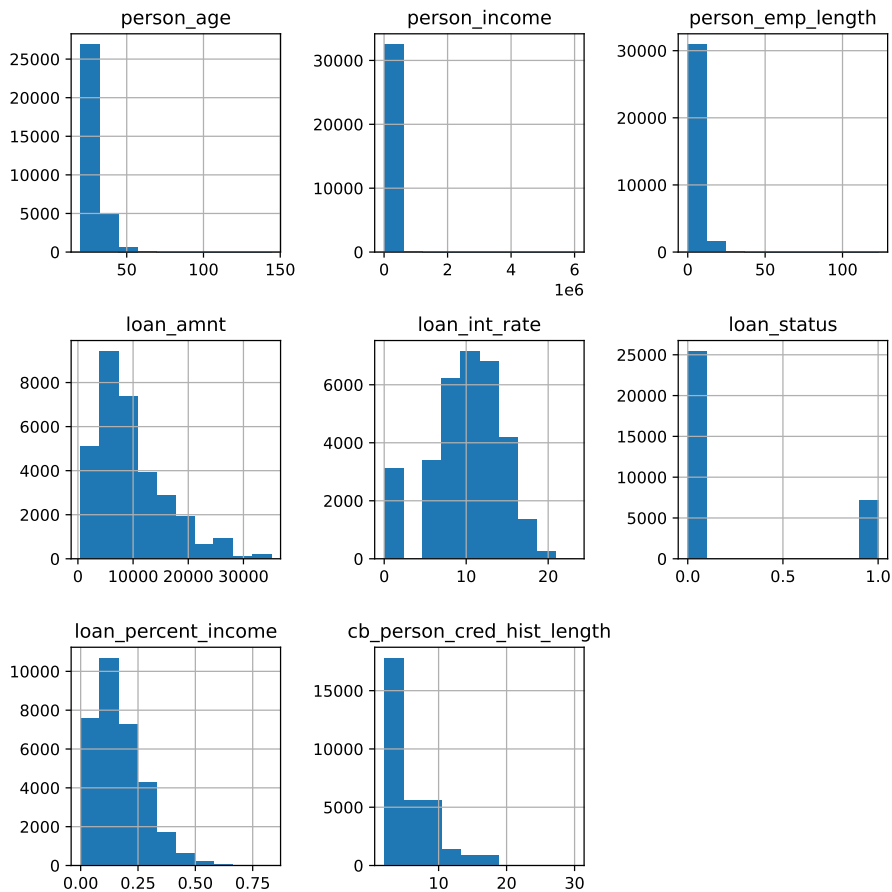
You can find the more details about the columns on kaggle, additionally to the next table:

Feature Name	Description
person_age	Age
person_income	Annual Income
person_homeownership	Home ownership
person_emp_length	Employment length (in years)
loan_intent	Loan intent
loan_grade	Loan grade
loan_amnt	Loan amount
loan_int_rate	Interest rate
loan_status	Loan status (0 is non default 1 is default)
loan_percent_income	Percent income
cb_person_default_on_file	Historical default
cb_person_cred_hist_length	Credit history length

The important column is `loan_status` that determinates the customers credit default and is used as the correct outputs  $Y$ . All other columns are considered as the input matrix  $X$ . First of all do we need to analyse the underlying data a little bit more. The columns with numerical data are visualized in the following charts:

```
l = ["person_age", "person_income", "person_emp_length",
    ↪ "loan_amnt", "loan_int_rate", "loan_status",
    ↪ "loan_percent_income", "cb_person_cred_hist_length"]
data[l].hist(bins=10,figsize=(8,8))
pyplot.tight_layout()
pyplot.show()
```

```
## array([[<AxesSubplot:title={'center':'person_age'}>,
##         <AxesSubplot:title={'center':'person_income'}>,
##         <AxesSubplot:title={'center':'person_emp_length'}>],
##        [<AxesSubplot:title={'center':'loan_amnt'}>,
##         <AxesSubplot:title={'center':'loan_int_rate'}>,
##         <AxesSubplot:title={'center':'loan_status'}>],
##        [<AxesSubplot:title={'center':'loan_percent_income'}>,
##         <AxesSubplot:title={'center':'cb_person_cred_hist_length'}>],
##        [<AxesSubplot:>]], dtype=object)
```



All other input columns are categorical that can't be processed by Neuronal Networks. Luckily there exist some methods to convert the categories to numbers for example with Ordinal Encoding, One hot Encoding or Embedding (more information can be found here). I will choose the Ordinal Encoding for our dataset, because it is the simplest method. Ordinal Encoding just maps numbers to the categories. The best would be to arrange the categories as good as possible and just map numbers to it like in the following code:

All other input columns are categorical, and Neuronal Networks cannot process them. Fortunately, there are some methods for converting categories to numbers, such as Ordinal Encoding, One-hot Encoding, and Embedding (more information can be found here). Because it is the easiest way, I will use Ordinal Encoding for our dataset. Ordinal Encoding simply converts numbers into categories. The best technique would be to organize each column's categories in a meaningful way before assigning numbers to them, as seen in the code below:

```

data = data.replace({"Y": 1, "N":0})
data["person_home_ownership"] =
↳ data["person_home_ownership"].replace({'OWN':1, 'RENT':2,
↳ 'MORTGAGE':3, 'OTHER':4})
data["loan_intent"] = data["loan_intent"].replace({'PERSONAL':1,
↳ 'EDUCATION':2, 'MEDICAL':3, 'VENTURE':4,
↳ 'HOMEIMPROVEMENT':5, 'DEBTCONSOLIDATION':6})
data["loan_grade"] = data["loan_grade"].replace({'A':1, 'B':2,
↳ 'C':3, 'D':4, 'E':5, 'F':6, 'G':7})

data.head()

```

	person_age	person_income	person_home_ownership	person_emp_length	loan_intent
## 0	22	59000	2	123.00	1
## 1	21	9600	1	5.00	2
## 2	25	9600	3	1.00	3
## 3	23	65500	2	4.00	3
## 4	24	54400	2	8.00	3

It's not the most precise method for encoding categorical data, but it's the simplest and doesn't add to the input matrix's size.

It's also crucial to standardize the data, which improves the learning process's stability and speed (for more information). Because we're using the sigmoid function, we'll normalize the data to the interval  $[0, 1]$ . The following function will work for the entire numpy array you've entered:

```

def NormalizeData(np_arr):
    for i in range(np_arr.shape[1]):
        np_arr[:,i] = (np_arr[:,i] - np.min(np_arr[:,i])) /
↳ (np.max(np_arr[:,i]) - np.min(np_arr[:,i]))
    return np_arr

```

Now we must divide the data into a training and a test dataset, convert the pandas dataframe to a numpy array, and normalize it:

```

training_n = 2000
X_train = NormalizeData( data.loc[0:(training_n-1), data.columns
↳ != 'loan_status'].to_numpy() )
Y_train = data.loc[0:(training_n-1), data.columns ==
↳ 'loan_status'].to_numpy()

X_test = NormalizeData( data.loc[training_n:, data.columns !=
↳ 'loan_status'].to_numpy() )
Y_test = data.loc[training_n:, data.columns ==
↳ 'loan_status'].to_numpy()

```

It's now time to load the functions that were created in the preview chapters.

```
def generate_weights(n_input, n_output, hidden_layer_neurons):
    W = []
    for i in range(len(hidden_layer_neurons)+1):
        if i == 0: # first layer
            W.append(np.random.random((n_input+1,
↪ hidden_layer_neurons[i])))
        elif i == len(hidden_layer_neurons): # last layer
            W.append(np.random.random((hidden_layer_neurons[i-1]+1,
↪ n_output)))
        else: # middle layers
            W.append(np.random.random((hidden_layer_neurons[i-1]+1,
↪ hidden_layer_neurons[i])))
    return(W)

def add_ones_to_input(x):
    return(np.append(x, np.array([np.ones(len(x))]).T, axis=1))

def sigmoid(x):
    return 1.0 / (1.0 + np.exp(-x))

def deriv_sigmoid(x):
    return x * (1 - x)

def forward(x, w):
    return( sigmoid(x @ w) )

def backward(IN, OUT, W, Y, grad, k):
    if k == len(grad)-1:
        grad[k] = deriv_sigmoid(OUT[k]) * (Y-OUT[k])
    else:
        grad[k] = deriv_sigmoid(OUT[k]) *(grad[k+1] @
↪ W[k+1][0:len(W[k+1])-1].T)
    return(grad)
```

## 5.2 Train and test phase

For the training and testing phases, we're making a simple wrapper:

```

def train(X, Y, hidden_layer_neurons, alpha, epochs):
    n_input = len(X_train[0])
    n_output = len(Y_train[0])
    W = generate_weights(n_input, n_output, hidden_layer_neurons)
    errors = []
    for i in range(epochs):
        IN = []
        OUT = []
        grad = [None]*len(W)
        for k in range(len(W)):
            if k==0:
                IN.append(add_ones_to_input(X))
            else:
                IN.append(add_ones_to_input(OUT[k-1]))
            OUT.append(forward(x=IN[k], w=W[k]))

        errors.append(Y - OUT[-1])

        for k in range(len(W)-1,-1, -1):
            grad = backward(IN, OUT, W, Y, grad, k)

        for k in range(len(W)):
            W[k] = W[k] + alpha * (IN[k].T @ grad[k])

    return W, errors

def test(X_test, W):
    for i in range(len(W)):
        X_test = forward(add_ones_to_input(X_test), W[i])
    return(X_test)

```

The `train()` function is just a simple wrapper around the things done in the last chapter and will fit the weights to the given `X_train` and `Y_train`. The `test()` function only contains the forward pass to calculate the output without adjusting the weights of the NN. Its used to evaluate the quality of the results. Its time to train the NN with the first 2000 rows of the given data, 20000 epochs, alpha of 0.01 and two hidden layers with 11 and 4 neurons:

```

W_train, errors_train = train(X_train, Y_train,
    ↪ hidden_layer_neurons = [11,4], alpha = 0.01, epochs = 10000)

```

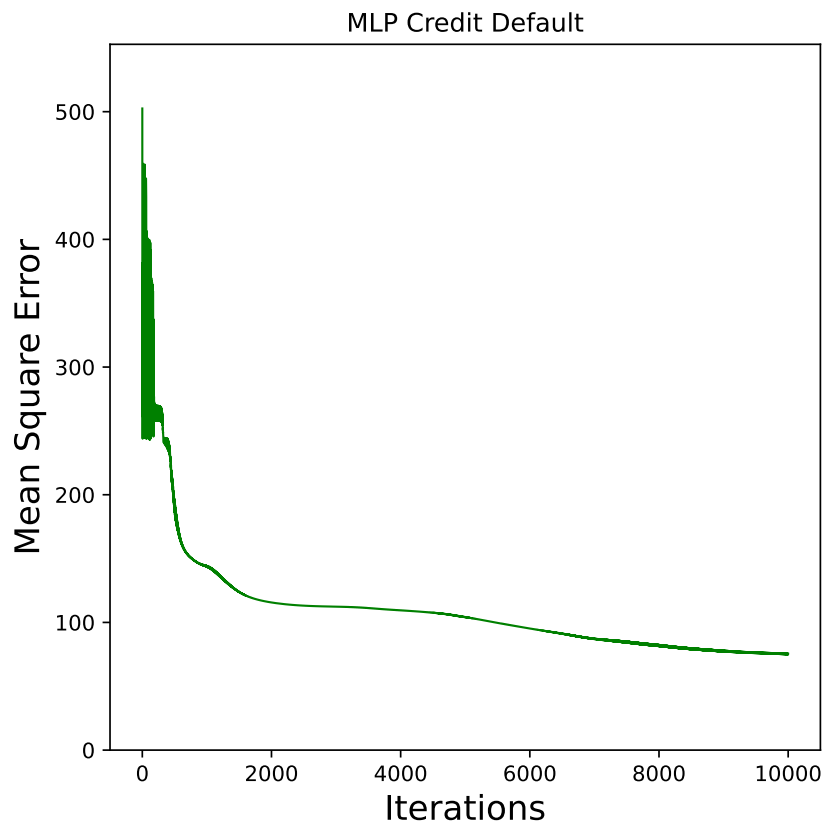
The return contains multiple values, that are assigned with the `a, b = fun_that_returns_2_vals()` pattern. We can visualize the learning process by calculating the mean-square-error and plotting it with the familiar line-chart:

```
def mean_square_error(error):
    return( 0.5 * np.sum(error ** 2) )

ms_errors_train = np.array(list(map(mean_square_error,
↪ errors_train)))

def plot_error(errors, title):
    x = list(range(len(errors)))
    y = np.array(errors)
    pyplot.figure(figsize=(6,6))
    pyplot.plot(x, y, "g", linewidth=1)
    pyplot.xlabel("Iterations", fontsize = 16)
    pyplot.ylabel("Mean Square Error", fontsize = 16)
    pyplot.title(title)
    pyplot.ylim(0,max(errors)*1.1)
    pyplot.show()

plot_error(ms_errors_train, "MLP Credit Default")
```



In the next step its time to test the NN on the never seen  $X_{\text{test}}$  and  $Y_{\text{test}}$  dataset.

```
result_test = test(X_test, W_train)
print("Mean Square error over all testdata: ",
      ↪ mean_square_error(Y_test - result_test))
```

```
## Mean Square error over all testdata: 2012.1713984629632
```

Because the Mean Square Error is hard to interpret, we will classify the output of the NN to be 1 or 0 and analyze the given answer for the credit defaults.

```
def classify(Y_approx):
    return( np.round(Y_approx,0) )
```



```

classified_error = Y_test - classify(result_test)
print("Mean Square error over all classified testdata: ",
      ↪ mean_square_error(classified_error))

print("Probability of a wrong output: ",
      ↪ np.round(np.sum(np.abs(classified_error)) /
      ↪ len(classified_error) * 100, 2), "%" )
print("Probability of a correct output: ", np.round((1 -
      ↪ np.sum(np.abs(classified_error)) /
      ↪ len(classified_error))*100,2), "%" )

```

```

## Mean Square error over all classified testdata: 2457.0
## Probability of a wrong output: 16.07 %
## Probability of a correct output: 83.93 %

```

An incredible tool to qualify the result is the confusion matrix from the sklearn package. It splits the results into 4 categories that can be used to qualify the

Actual class \ Predicted class	P	N
P	TP	FN
N	FP	TN

results with the following table:

For instance, ‘TP’ stands for True-Positiv, which means that the prediction was True=1 and the actual result was Positiv=1, indicating that the prediction was correct. For the classified result of the test phase, we have the following confusion matrix in our example:

```

from sklearn.metrics import confusion_matrix
confusion_matrix(Y_test, classify(result_test))

```

```

## array([[21164, 3142],
##        [ 1772, 4503]], dtype=int64)

```

### 5.3 Appendix (complete code)

```

import numpy as np
import matplotlib.pyplot as pyplot
import pandas as pd
from sklearn.metrics import confusion_matrix
np.random.seed(0)

data =
    ↪ pd.read_csv("example_data/credit_risk_dataset.csv").fillna(0)
data = data.replace({"Y": 1, "N":0})

data["person_home_ownership"] =
    ↪ data["person_home_ownership"].replace({'OWN':1, 'RENT':2,
    ↪ 'MORTGAGE':3, 'OTHER':4})
data["loan_intent"] = data["loan_intent"].replace({'PERSONAL':1,
    ↪ 'EDUCATION':2, 'MEDICAL':3, 'VENTURE':4,
    ↪ 'HOMEIMPROVEMENT':5, 'DEBTCONSOLIDATION':6})
data["loan_grade"] = data["loan_grade"].replace({'A':1, 'B':2,
    ↪ 'C':3, 'D':4, 'E':5, 'F':6, 'G':7})

def NormalizeData(np_arr):
    for i in range(np_arr.shape[1]):
        np_arr[:,i] = (np_arr[:,i] - np.min(np_arr[:,i])) /
    ↪ (np.max(np_arr[:,i]) - np.min(np_arr[:,i]))
    return(np_arr)

training_n = 2000
X_train = NormalizeData( data.loc[0:(training_n-1), data.columns
    ↪ != 'loan_status'].to_numpy() )
Y_train = data.loc[0:(training_n-1), data.columns ==
    ↪ 'loan_status'].to_numpy()

X_test = NormalizeData( data.loc[training_n:, data.columns !=
    ↪ 'loan_status'].to_numpy() )
Y_test = data.loc[training_n:, data.columns ==
    ↪ 'loan_status'].to_numpy()

def generate_weights(n_input, n_output, hidden_layer_neurons):
    W = []
    for i in range(len(hidden_layer_neurons)+1):
        if i == 0: # first layer
            W.append(np.random.random((n_input+1,
    ↪ hidden_layer_neurons[i])))

```

```

    elif i == len(hidden_layer_neurons): # last layer
        W.append(np.random.random((hidden_layer_neurons[i-1]+1,
↪ n_output)))
    else: # middle layers
        W.append(np.random.random((hidden_layer_neurons[i-1]+1,
↪ hidden_layer_neurons[i])))
    return(W)

def add_ones_to_input(x):
    return(np.append(x, np.array([np.ones(len(x))]).T, axis=1))

def sigmoid(x):
    return 1.0 / (1.0 + np.exp(-x))

def deriv_sigmoid(x):
    return x * (1 - x)

def forward(x, w):
    return( sigmoid(x @ w) )

def backward(IN, OUT, W, Y, grad, k):
    if k == len(grad)-1:
        grad[k] = deriv_sigmoid(OUT[k]) * (Y-OUT[k])
    else:
        grad[k] = deriv_sigmoid(OUT[k]) *(grad[k+1] @
↪ W[k+1][0:len(W[k+1])-1].T)
    return(grad)

def train(X, Y, hidden_layer_neurons, alpha, epochs):
    n_input = len(X[0])
    n_output = len(Y[0])
    W = generate_weights(n_input, n_output, hidden_layer_neurons)
    errors = []
    for i in range(epochs):
        IN = []
        OUT = []
        grad = [None]*len(W)
        for k in range(len(W)):
            if k==0:
                IN.append(add_ones_to_input(X))
            else:
                IN.append(add_ones_to_input(OUT[k-1]))

```

```

        OUT.append(forward(x=IN[k], w=W[k]))

    errors.append(Y - OUT[-1])

    for k in range(len(W)-1,-1, -1):
        grad = backward(IN, OUT, W, Y, grad, k)

    for k in range(len(W)):
        W[k] = W[k] + alpha * (IN[k].T @ grad[k])

    return W, errors

W_train, errors_train = train(X_train, Y_train,
    ↪ hidden_layer_neurons = [11,4], alpha = 0.01, epochs = 10000)

def mean_square_error(error):
    return( 0.5 * np.sum(error ** 2) )

ms_errors_train = np.array(list(map(mean_square_error,
    ↪ errors_train)))

def plot_error(errors, title):
    x = list(range(len(errors)))
    y = np.array(errors)
    pyplot.figure(figsize=(6,6))
    pyplot.plot(x, y, "g", linewidth=1)
    pyplot.xlabel("Iterations", fontsize = 16)
    pyplot.ylabel("Mean Square Error", fontsize = 16)
    pyplot.title(title)
    pyplot.ylim(0,max(errors)*1.1)
    pyplot.show()

plot_error(ms_errors_train, "MLP Credit Default")

def test(X_test, W):
    for i in range(len(W)):
        X_test = forward(add_ones_to_input(X_test), W[i])
    return(X_test)

```

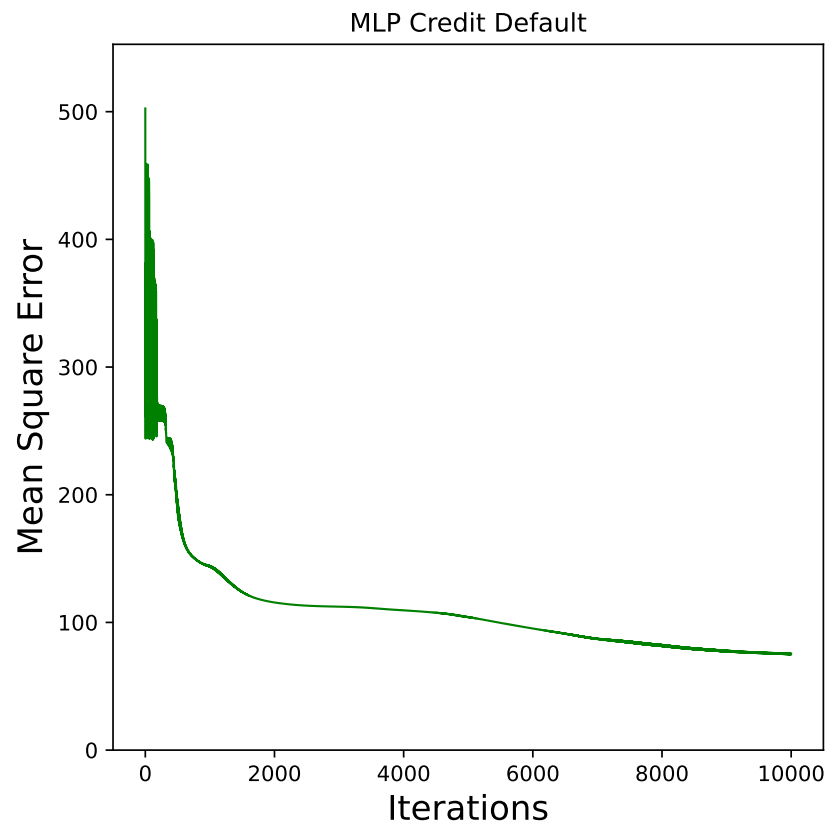
```
result_test = test(X_test, W_train)
print("Mean Square error over all testdata: ",
      ↪ mean_square_error(Y_test - result_test))

def classify(Y_approx):
    return( np.round(Y_approx,0) )

classified_error = Y_test - classify(result_test)
print("Mean Square error over all classified testdata: ",
      ↪ mean_square_error(classified_error))

print("Probability of a wrong output: ",
      ↪ np.round(np.sum(np.abs(classified_error)) /
      ↪ len(classified_error) * 100, 2), "%" )
print("Probability of a right output: ", np.round((1 -
      ↪ np.sum(np.abs(classified_error)) /
      ↪ len(classified_error))*100,2), "%" )

confusion_matrix(Y_test, classify(result_test))
```



```
## Mean Square error over all testdata: 2012.1713984629632
## Mean Square error over all classified testdata: 2457.0
## Probability of a wrong output: 16.07 %
## Probability of a right output: 83.93 %
## array([[21164, 3142],
##        [ 1772, 4503]], dtype=int64)
```

## Chapter 6

# Effect of batch size

First and foremost, do we need to distinguish between the following definitions that I discovered here:

- one epoch := one forward pass and backward pass of all the training examples.
- batch size := the number of training scenarios in one forward/backward pass. The higher the batch size, the more memory space will be needed.
- number of iterations := number of passes, each pass using [batch size] number of scenarios. To be clear, one pass = forward pass + backward pass (we do not count the forward pass and backward pass as two different passes).

I noted in the first chapter that the standard method for defining a NN is to cycle over all training data by selecting a random scenario until all possibilities have been used, resulting in one epoch. To make it easier, I changed it to pick all scenarios at once (full batch size). But what happens if the batch size is equal to the number of rows in the training dataset?

Unfortunately, there is no solid proof for the differences, but I did find a neat post that tries to explain it here. As a result, optimizing with the full batch size yields sharper minimax, whereas optimizing with a lesser batch size yields to flatter minimax. More information about the issue of speed vs. accuracy via batch size selection may be found here. He clearly outlines the issues and how switching to a dynamically growing batch size could be a smart option.

The underlying data determines the ideal hyperparameters like as bias, alpha, batch size, hidden neurons, and so on, according to what I've found so far. As a result, modifying the underlying dataset affects all of the ideal hyperparameters. Perhaps it would be more useful to test some hyperparameters on our Credit Default dataset and compare the outcomes.

## 6.1 Impact of different hyperparameters

First of all do we add a `batch_size` parameter to the previous `train()` function and generate random batches that all contain distinct random integers in each batch. We will use the following function to generate the random batches:

```
import numpy as np
import matplotlib.pyplot as pyplot
import pandas as pd
from sklearn.metrics import confusion_matrix
import math as ma
import time
np.warnings.filterwarnings('ignore',
    ↳ category=np.VisibleDeprecationWarning)

def generate_random_batches(batch_size, full_batch_size):
    batches = np.arange(full_batch_size)
    np.random.shuffle(batches)
    return(np.array_split(batches,
    ↳ ma.ceil(full_batch_size/batch_size)))

generate_random_batches(3, 10)

## [array([0, 8, 9]), array([4, 1, 5]), array([6, 2]), array([3, 7])]
```

Now do we need to adjust the `train()` function to iterate over all batches:

```
def train(X, Y, hidden_layer_neurons, alpha, epochs, batch_size):
    n_input = len(X[0])
    n_output = len(Y[0])
    W = generate_weights(n_input, n_output, hidden_layer_neurons)
    errors = []
    batches = generate_random_batches(batch_size, full_batch_size =
    ↳ len(X))
    for i in range(epochs):
        error_temp = np.array([])
        for z in range(len(batches)):
            IN = []
            OUT = []
            grad = [None]*len(W)
            for k in range(len(W)):
                if k==0:
                    IN.append(add_ones_to_input(X[batches[z],:]))
                else:
```



```

        IN.append(add_ones_to_input(OUT[k-1]))
        OUT.append(forward(x=IN[k], w=W[k]))

        error_temp = np.append(error_temp, Y[batches[z],:] -
↪ OUT[-1])

        for k in range(len(W)-1,-1, -1):
            grad = backward(IN, OUT, W, Y[batches[z],:], grad, k)

        for k in range(len(W)):
            W[k] = W[k] + alpha * (IN[k].T @ grad[k])
            errors.append(error_temp)

    return W, errors

```

And all the previes created functions, dataloading and transformations are:

```

data =
↪ pd.read_csv("example_data/credit_risk_dataset.csv").fillna(0)
data = data.replace({"Y": 1, "N":0})
data["person_home_ownership"] =
↪ data["person_home_ownership"].replace({'OWN':1, 'RENT':2,
↪ 'MORTGAGE':3, 'OTHER':4})
data["loan_intent"] = data["loan_intent"].replace({'PERSONAL':1,
↪ 'EDUCATION':2, 'MEDICAL':3, 'VENTURE':4,
↪ 'HOMEIMPROVEMENT':5, 'DEBTCONSOLIDATION':6})
data["loan_grade"] = data["loan_grade"].replace({'A':1, 'B':2,
↪ 'C':3, 'D':4, 'E':5, 'F':6, 'G':7})

def NormalizeData(np_arr):
    for i in range(np_arr.shape[1]):
        np_arr[:,i] = (np_arr[:,i] - np.min(np_arr[:,i])) /
↪ (np.max(np_arr[:,i]) - np.min(np_arr[:,i]))
    return(np_arr)

training_n = 2000
X_train = NormalizeData( data.loc[0:(training_n-1), data.columns
↪ != 'loan_status'].to_numpy() )
Y_train = data.loc[0:(training_n-1), data.columns ==
↪ 'loan_status'].to_numpy()

X_test = NormalizeData( data.loc[training_n:, data.columns !=
↪ 'loan_status'].to_numpy() )
Y_test = data.loc[training_n:, data.columns ==
↪ 'loan_status'].to_numpy()

```

```

def generate_weights(n_input, n_output, hidden_layer_neurons):
    W = []
    for i in range(len(hidden_layer_neurons)+1):
        if i == 0: # first layer
            W.append(np.random.random((n_input+1,
↪ hidden_layer_neurons[i])))
        elif i == len(hidden_layer_neurons): # last layer
            W.append(np.random.random((hidden_layer_neurons[i-1]+1,
↪ n_output)))
        else: # middle layers
            W.append(np.random.random((hidden_layer_neurons[i-1]+1,
↪ hidden_layer_neurons[i])))
    return(W)

def add_ones_to_input(x):
    return(np.append(x, np.array([np.ones(len(x))]).T, axis=1))

def sigmoid(x):
    return 1.0 / (1.0 + np.exp(-x))

def deriv_sigmoid(x):
    return x * (1 - x)

def forward(x, w):
    return( sigmoid(x @ w) )

def backward(IN, OUT, W, Y, grad, k):
    if k == len(grad)-1:
        grad[k] = deriv_sigmoid(OUT[k]) * (Y-OUT[k])
    else:
        grad[k] = deriv_sigmoid(OUT[k]) *(grad[k+1] @
↪ W[k+1][0:len(W[k+1])-1].T)
    return(grad)

def mean_square_error(error):
    return( 0.5 * np.sum(error ** 2) )

def plot_error(errors, title):
    x = list(range(len(errors)))
    y = np.array(errors)

```

```

pyplot.figure(figsize=(6,6))
pyplot.plot(x, y, "g", linewidth=1)
pyplot.xlabel("Iterations", fontsize = 16)
pyplot.ylabel("Mean Square Error", fontsize = 16)
pyplot.title(title)
pyplot.ylim(0,max(errors)*1.1)
pyplot.show()

def test(X_test, W):
    for i in range(len(W)):
        X_test = forward(add_ones_to_input(X_test), W[i])
    return(X_test)

def classify(Y_approx):
    return( np.round(Y_approx,0) )

```

Everything is loaded and set up. Now can we compare the time and the error for different `batch_size`:

```

# full batch size
np.random.seed(0)

start = time.time()
W_train, errors_train = train(X = X_train, Y = Y_train,
    ↪ hidden_layer_neurons = [11,4], alpha = 0.01, epochs = 5000,
    ↪ batch_size = 2000)
time_diff = time.time() - start
print("Time to train the NN: ", time_diff)

ms_errors_train = np.array(list(map(mean_square_error,
    ↪ errors_train)))
plot_error(ms_errors_train, "MLP Credit Default")
result_test = test(X_test, W_train)
print("Mean Square error over all testdata: ",
    ↪ mean_square_error(Y_test - result_test))

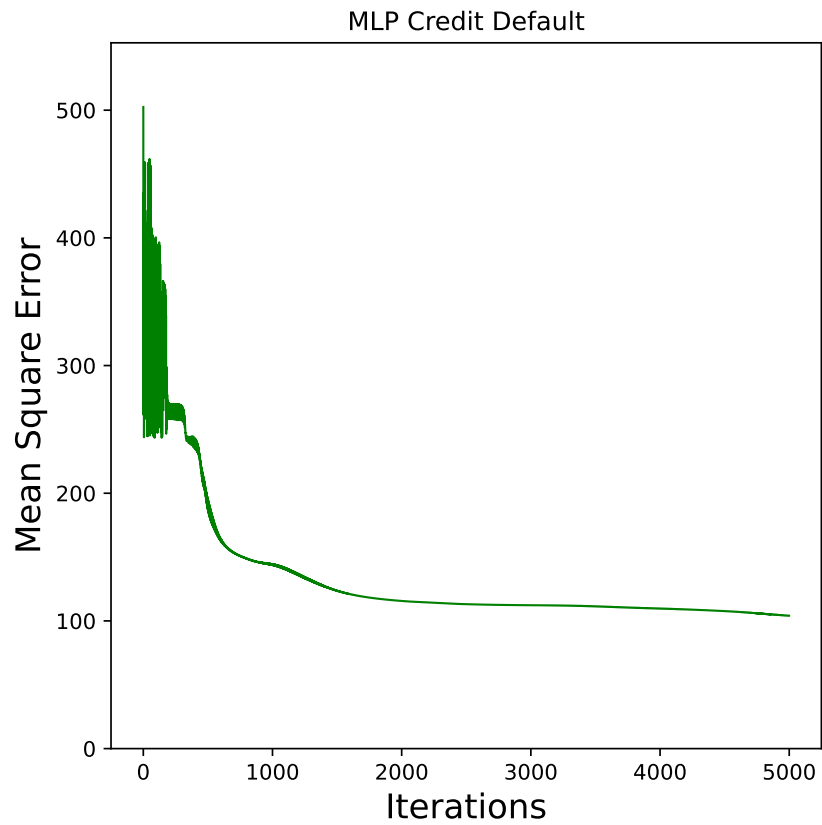
classified_error = Y_test - classify(result_test)
print("Mean Square error over all classified testdata: ",
    ↪ mean_square_error(classified_error))

print("Probability of a wrong output: ",
    ↪ np.round(np.sum(np.abs(classified_error)) /
    ↪ len(classified_error) * 100, 2), "%" )
print("Probability of a right output: ", np.round((1 -
    ↪ np.sum(np.abs(classified_error)) /
    ↪ len(classified_error))*100,2), "%" )

```

```
confusion_matrix(Y_test, classify(result_test))
```

```
## Time to train the NN: 8.31972336769104
```



```
## Mean Square error over all testdata: 2402.2283244767077
## Mean Square error over all classified testdata: 2932.0
## Probability of a wrong output: 19.18 %
## Probability of a right output: 80.82 %
## array([[20193, 4113],
##        [1751, 4524]], dtype=int64)
```

```

# batch size = 100
np.random.seed(0)

start = time.time()
W_train, errors_train = train(X = X_train, Y = Y_train,
    ↪ hidden_layer_neurons = [11,4], alpha = 0.01, epochs = 5000,
    ↪ batch_size = 100)
time_diff = time.time() - start
print("Time to train the NN: ", time_diff)

ms_errors_train = np.array(list(map(mean_square_error,
    ↪ errors_train)))
plot_error(ms_errors_train, "MLP Credit Default")
result_test = test(X_test, W_train)
print("Mean Square error over all testdata: ",
    ↪ mean_square_error(Y_test - result_test))

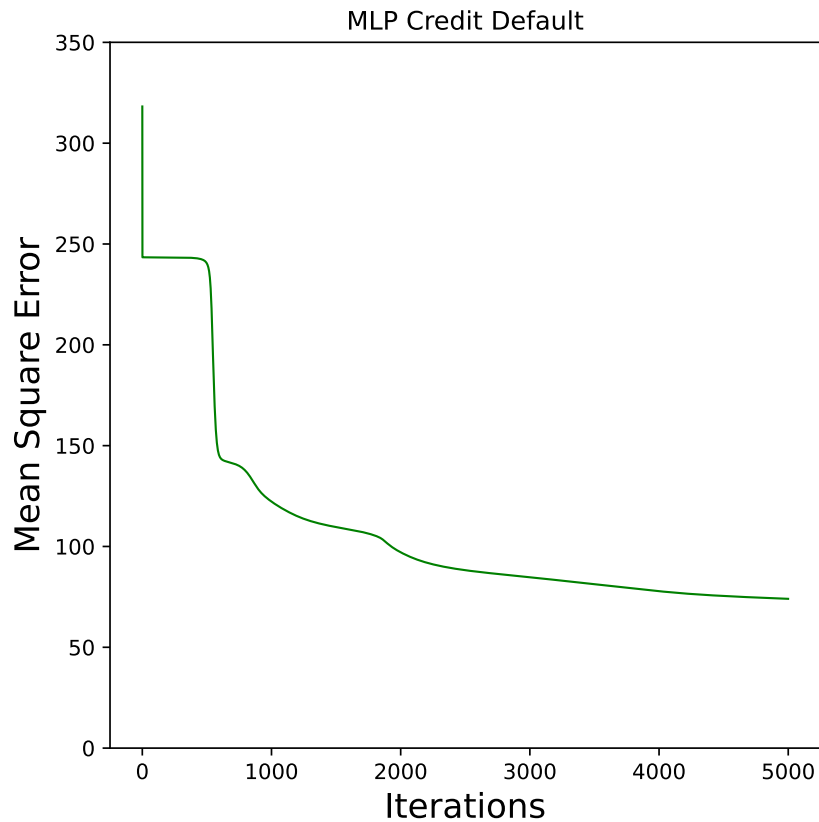
classified_error = Y_test - classify(result_test)
print("Mean Square error over all classified testdata: ",
    ↪ mean_square_error(classified_error))

print("Probability of a wrong output: ",
    ↪ np.round(np.sum(np.abs(classified_error)) /
    ↪ len(classified_error) * 100, 2), "%" )
print("Probability of a right output: ", np.round((1 -
    ↪ np.sum(np.abs(classified_error)) /
    ↪ len(classified_error))*100,2), "%" )

confusion_matrix(Y_test, classify(result_test))

```

```
## Time to train the NN: 22.19215226173401
```



```
## Mean Square error over all testdata: 2210.3693145823286
## Mean Square error over all classified testdata: 2559.5
## Probability of a wrong output: 16.74 %
## Probability of a right output: 83.26 %
## array([[21396, 2910],
##        [ 2209, 4066]], dtype=int64)
```

The full batch size is clearly faster than the smaller batch size, yet the smaller batch size has a lower error. Perhaps the ideal batch size is determined by the problem itself. If you have a low-dimensional input matrix and need a quick answer, full batch size is the way to go. If your dimensional input is large, you won't be able to use a complete batch size since your RAM will jump off. I believe it is important to study the underlying data and choose a batch size that is appropriate for it. For example, in the blog article I cited at the beginning of the chapter, some situations may require a dynamic batch size that lowers over time to provide the best outcomes.

## 6.2 Appendix (complete code)

```

import numpy as np
import matplotlib.pyplot as pyplot
import pandas as pd
from sklearn.metrics import confusion_matrix
import math as ma
np.random.seed(0)
np.warnings.filterwarnings('ignore',
    ↪ category=np.VisibleDeprecationWarning)

data =
    ↪ pd.read_csv("example_data/credit_risk_dataset.csv").fillna(0)
data = data.replace({"Y": 1, "N":0})

data["person_home_ownership"] =
    ↪ data["person_home_ownership"].replace({'OWN':1, 'RENT':2,
    ↪ 'MORTGAGE':3, 'OTHER':4})
data["loan_intent"] = data["loan_intent"].replace({'PERSONAL':1,
    ↪ 'EDUCATION':2, 'MEDICAL':3, 'VENTURE':4,
    ↪ 'HOMEIMPROVEMENT':5, 'DEBTCONSOLIDATION':6})
data["loan_grade"] = data["loan_grade"].replace({'A':1, 'B':2,
    ↪ 'C':3, 'D':4, 'E':5, 'F':6, 'G':7})

def NormalizeData(np_arr):
    for i in range(np_arr.shape[1]):
        np_arr[:,i] = (np_arr[:,i] - np.min(np_arr[:,i])) /
    ↪ (np.max(np_arr[:,i]) - np.min(np_arr[:,i]))
    return(np_arr)

training_n = 2000
X_train = NormalizeData( data.loc[0:(training_n-1), data.columns
    ↪ != 'loan_status'].to_numpy() )
Y_train = data.loc[0:(training_n-1), data.columns ==
    ↪ 'loan_status'].to_numpy()

X_test = NormalizeData( data.loc[training_n:, data.columns !=
    ↪ 'loan_status'].to_numpy() )
Y_test = data.loc[training_n:, data.columns ==
    ↪ 'loan_status'].to_numpy()

```

```

def generate_weights(n_input, n_output, hidden_layer_neurons):
    W = []
    for i in range(len(hidden_layer_neurons)+1):
        if i == 0: # first layer
            W.append(np.random.random((n_input+1,
↪ hidden_layer_neurons[i])))
        elif i == len(hidden_layer_neurons): # last layer
            W.append(np.random.random((hidden_layer_neurons[i-1]+1,
↪ n_output)))
        else: # middle layers
            W.append(np.random.random((hidden_layer_neurons[i-1]+1,
↪ hidden_layer_neurons[i])))
    return(W)

def add_ones_to_input(x):
    return(np.append(x, np.array([np.ones(len(x))]).T, axis=1))

def sigmoid(x):
    return 1.0 / (1.0 + np.exp(-x))

def deriv_sigmoid(x):
    return x * (1 - x)

def forward(x, w):
    return( sigmoid(x @ w) )

def backward(IN, OUT, W, Y, grad, k):
    if k == len(grad)-1:
        grad[k] = deriv_sigmoid(OUT[k]) * (Y-OUT[k])
    else:
        grad[k] = deriv_sigmoid(OUT[k]) *(grad[k+1] @
↪ W[k+1][0:len(W[k+1])-1].T)
    return(grad)

def generate_random_batches(batch_size, full_batch_size):
    batches = np.arange(full_batch_size)
    np.random.shuffle(batches)
    return(np.array_split(batches,
↪ ma.ceil(full_batch_size/batch_size)))

def train(X, Y, hidden_layer_neurons, alpha, epochs, batch_size):
    n_input = len(X[0])

```



```

n_output = len(Y[0])
W = generate_weights(n_input, n_output, hidden_layer_neurons)
errors = []
batches = generate_random_batches(batch_size, full_batch_size =
↪ len(X))
for i in range(epochs):
    error_temp = np.array([])
    for z in range(len(batches)):
        IN = []
        OUT = []
        grad = [None]*len(W)
        for k in range(len(W)):
            if k==0:
                IN.append(add_ones_to_input(X[batches[z],:]))
            else:
                IN.append(add_ones_to_input(OUT[k-1]))
                OUT.append(forward(x=IN[k], w=W[k]))

        error_temp = np.append(error_temp, Y[batches[z],:] -
↪ OUT[-1])

        for k in range(len(W)-1,-1, -1):
            grad = backward(IN, OUT, W, Y[batches[z],:], grad, k)

        for k in range(len(W)):
            W[k] = W[k] + alpha * (IN[k].T @ grad[k])
        errors.append(error_temp)

    return W, errors

W_train, errors_train = train(X = X_train, Y = Y_train,
↪ hidden_layer_neurons = [11,4], alpha = 0.01, epochs = 2000,
↪ batch_size = 2000)

def mean_square_error(error):
    return( 0.5 * np.sum(error ** 2) )

ms_errors_train = np.array(list(map(mean_square_error,
↪ errors_train)))

def plot_error(errors, title):
    x = list(range(len(errors)))

```

```

y = np.array(errors)
pyplot.figure(figsize=(6,6))
pyplot.plot(x, y, "g", linewidth=1)
pyplot.xlabel("Iterations", fontsize = 16)
pyplot.ylabel("Mean Square Error", fontsize = 16)
pyplot.title(title)
pyplot.ylim(0,max(errors)*1.1)
pyplot.show()

plot_error(ms_errors_train, "MLP Credit Default")

def test(X_test, W):
    for i in range(len(W)):
        X_test = forward(add_ones_to_input(X_test), W[i])
    return(X_test)

result_test = test(X_test, W_train)
print("Mean Square error over all testdata: ",
      ↪ mean_square_error(Y_test - result_test))

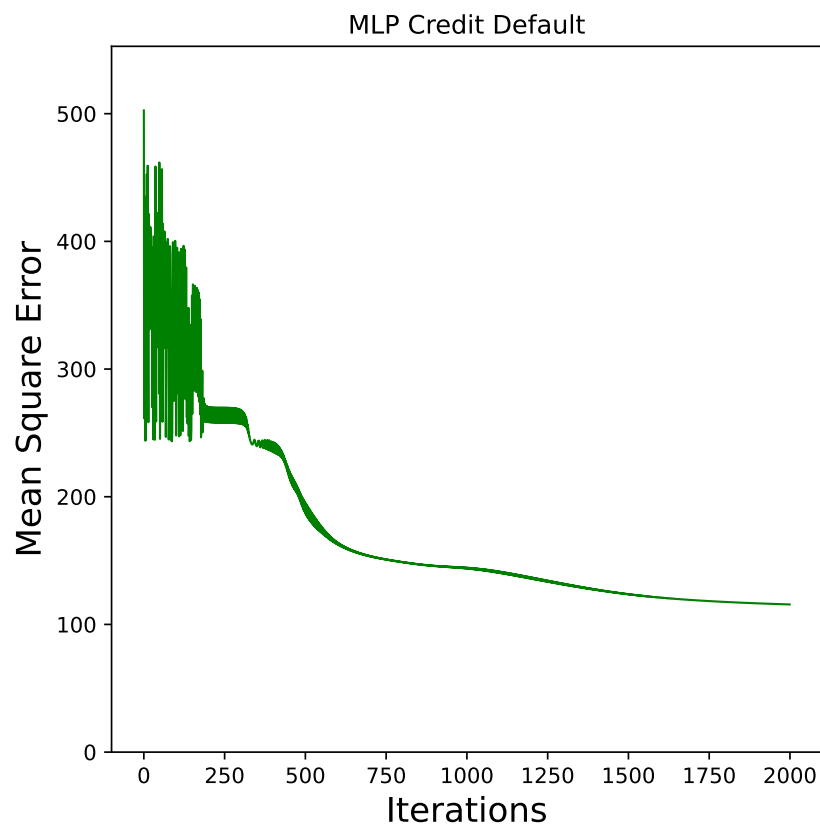
def classify(Y_approx):
    return( np.round(Y_approx,0) )

classified_error = Y_test - classify(result_test)
print("Mean Square error over all classified testdata: ",
      ↪ mean_square_error(classified_error))

print("Probability of a wrong output: ",
      ↪ np.round(np.sum(np.abs(classified_error)) /
      ↪ len(classified_error) * 100, 2), "%" )
print("Probability of a right output: ", np.round((1 -
      ↪ np.sum(np.abs(classified_error)) /
      ↪ len(classified_error))*100,2), "%" )

confusion_matrix(Y_test, classify(result_test))

```



```
## Mean Square error over all testdata: 2330.8698549481937
## Mean Square error over all classified testdata: 2940.0
## Probability of a wrong output: 19.23 %
## Probability of a right output: 80.77 %
## array([[20516, 3790],
##        [ 2090, 4185]], dtype=int64)
```



## Chapter 7

# Class MLP

Finally, can we create a ‘MLP’ class that contains all of the functions from the preview chapters. You can use this class to play around with different settings and learn new things about the datasets you’ve chosen.

```
import numpy as np
import matplotlib.pyplot as pyplot
import pandas as pd
from sklearn.metrics import confusion_matrix
import math as ma
import time
np.warnings.filterwarnings('ignore',
    ↪ category=np.VisibleDeprecationWarning)

class MLP:
    def __init__(self, X_train, Y_train, X_test, Y_test,
    ↪ hidden_layer_neurons, alpha, epochs, batch_size):
        self.X_train = X_train
        self.Y_train = Y_train
        self.X_test = X_test
        self.Y_test = Y_test
        self.hidden_layer_neurons = hidden_layer_neurons
        self.alpha = alpha
        self.epochs = epochs
        self.batch_size = batch_size

    def generate_weights(self):
        W = []
        for i in range(len(self.hidden_layer_neurons)+1):
            if i == 0: # first layer
```

```

        W.append(np.random.random((len(self.X_train)+1,
↪ self.hidden_layer_neurons[i])))
        elif i == len(self.hidden_layer_neurons): # last layer

↪ W.append(np.random.random((self.hidden_layer_neurons[i-1]+1,
↪ len(self.Y_train))))
        else: # middle layers

↪ W.append(np.random.random((self.hidden_layer_neurons[i-1]+1,
↪ self.hidden_layer_neurons[i])))
        return(W)

    @staticmethod
    def add_ones_to_input(x):
        return(np.append(x, np.array([np.ones(len(x))]).T, axis=1))
    @staticmethod
    def sigmoid(x):
        return 1.0 / (1.0 + np.exp(-x))
    @staticmethod
    def deriv_sigmoid(x):
        return x * (1 - x)

    @staticmethod
    def forward(x, w):
        return( sigmoid(x @ w) )

    @staticmethod
    def backward(IN, OUT, W, Y, grad, k):
        if k == len(grad)-1:
            grad[k] = deriv_sigmoid(OUT[k]) * (Y-OUT[k])
        else:
            grad[k] = deriv_sigmoid(OUT[k]) *(grad[k+1] @
↪ W[k+1][0:len(W[k+1])-1].T)
        return(grad)

    def generate_random_batches(self):
        batches = np.arange(len(self.X_train))
        np.random.shuffle(batches)
        return(np.array_split(batches,
↪ ma.ceil(len(self.X_train)/self.batch_size)))

    def train(self):
        W = self.generate_weights()
        errors = []
        batches = self.generate_random_batches()

```

```

for i in range(self.epochs):
    error_temp = np.array([])
    for z in range(len(batches)):
        IN = []
        OUT = []
        grad = [None]*len(W)
        for k in range(len(W)):
            if k==0:
                IN.append(self.add_ones_to_input(x =
↪ self.X_train[batches[z],:]))
            else:
                IN.append(self.add_ones_to_input(x = OUT[k-1]))
                OUT.append(self.forward(IN[k], W[k]))

        error_temp = np.append(error_temp,
↪ self.Y_train[batches[z],:] - OUT[-1])

        for k in range(len(W)-1,-1, -1):
            grad = self.backward(IN, OUT, W,
↪ self.Y_train[batches[z],:], grad, k)

        for k in range(len(W)):
            W[k] = W[k] + self.alpha * (IN[k].T @ grad[k])
        errors.append(error_temp)
    self.W = W
    self.errors = errors
    @staticmethod
    def mean_square_error(error):
        return( 0.5 * np.sum(error ** 2) )
    @staticmethod
    def plot_error(errors, title):
        x = list(range(len(errors)))
        y = np.array(errors)
        pyplot.figure(figsize=(6,6))
        pyplot.plot(x, y, "g", linewidth=1)
        pyplot.xlabel("Iterations", fontsize = 16)
        pyplot.ylabel("Mean Square Error", fontsize = 16)
        pyplot.title(title)
        pyplot.ylim(0,max(errors)*1.1)
        pyplot.show()

    def test(self):
        X_test = self.X_test
        for i in range(len(self.W)):
            X_test = self.forward(self.add_ones_to_input(X_test),
↪ self.W[i])

```

```

        return(X_test)
    @staticmethod
    def classify(Y_approx):
        return( np.round(Y_approx,0) )

data =
↳ pd.read_csv("example_data/credit_risk_dataset.csv").fillna(0)
data = data.replace({"Y": 1, "N":0})

data["person_home_ownership"] =
↳ data["person_home_ownership"].replace({'OWN':1, 'RENT':2,
↳ 'MORTGAGE':3, 'OTHER':4})
data["loan_intent"] = data["loan_intent"].replace({'PERSONAL':1,
↳ 'EDUCATION':2, 'MEDICAL':3, 'VENTURE':4,
↳ 'HOMEIMPROVEMENT':5, 'DEBTCONSOLIDATION':6})
data["loan_grade"] = data["loan_grade"].replace({'A':1, 'B':2,
↳ 'C':3, 'D':4, 'E':5, 'F':6, 'G':7})

def NormalizeData(np_arr):
    for i in range(np_arr.shape[1]):
        np_arr[:,i] = (np_arr[:,i] - np.min(np_arr[:,i])) /
↳ (np.max(np_arr[:,i]) - np.min(np_arr[:,i]))
    return(np_arr)

training_n = 2000
X_train = NormalizeData( data.loc[0:(training_n-1), data.columns
↳ != 'loan_status'].to_numpy() )
Y_train = data.loc[0:(training_n-1), data.columns ==
↳ 'loan_status'].to_numpy()

X_test = NormalizeData( data.loc[training_n:, data.columns !=
↳ 'loan_status'].to_numpy() )
Y_test = data.loc[training_n:, data.columns ==
↳ 'loan_status'].to_numpy()

# mlp = MLP(X_train, Y_train, X_test, Y_test,
↳ hidden_layer_neurons = [11,4], alpha = 0.01, epochs = 2000,
↳ batch_size = 2000)
# mlp.train()

```



## Chapter 8

# Decision Tree

The goal of Decision Trees (DT) and Neuronal Networks (NN) is the same: to analyze data and provide answers to previously unknown data. Nonetheless, there are significant differences in working with each of these methods. As a result, I've included a link to a thorough comparison of these two approaches. As a result, Decision Trees are much simpler than Neuronal Networks, with the added benefit of being easier to interpret the way a certain answer is given. In comparison, Neuronal Networks can easily process large datasets, and you can fine-tune the learning behavior using the hyper-parameter you choose, resulting in high accuracy. If you consider everything, it's better to consider Decision Trees before creating a Neuronal Network because it's a simpler approach. If your data is more complicated or large, Neuronal Networks are the way to go. They frequently use hybrids of Decision Trees and Neuronal Networks to archive understandable results with high accuracy in very complex situations (for example Neural-Backed Decision Trees).

### 8.1 Entropy

The impurity of the data is measured by entropy. Low impurity results in improved classification and accuracy. The goal of Decision Trees is to split the data with the highest purity gain at each node. The concave Entropy-Formula can be used to calculate the purity of a dataset:

$$E = -p \cdot \log_2(p) - (1 - p) \cdot \log_2(1 - p)$$

with  $p$  as the probability of having no default in the credit default dataset. If the dataset contains 50% defaults and 50% no defaults, the Entropy increases to 1, and it decreases to 0 if the dataset contains only defaults or only no defaults. The following is the python function:

```
def calc_entropy(df, decision_on = "loan_status"):
    if len(df)==0:
        return(0)
    p = np.sum(df[decision_on] == 0)/len(df)
    if p == 0 or p == 1:
        return(0)
    result = -p * ma.log(p,2) - (1-p)*ma.log(1-p,2)
    return result
```

Now can we calculate the initial Entropy of the credit default dataset as shown in the next code snippet:

```
import numpy as np
import math as ma
import pandas as pd

data =
↳ pd.read_csv("example_data/credit_risk_dataset.csv").fillna(0)
data = data.replace({"Y": 1, "N":0})

entropy_of_data = calc_entropy(df=data)
print("Initial Inpurity/Entropy of data: ", entropy_of_data)
```

```
## Initial Inpurity/Entropy of data: 0.7568007498467375
```

Unfortunately, do we face the same problem with categorical data as we had with the NN. We could convert categorical data to numerical as shown in the Credit Default chapter, but I'd like to remove these columns to make things easier. We'll also limit it to four columns plus the answer to make it more readable and understandable.

```
data = data.loc[:, ["person_age", "loan_percent_income",
↳ "loan_int_rate", "cb_person_default_on_file", "loan_status"]]
```

Now we must create the tree's nodes based on the decisions that result in the lowest Entropy. The purity obtained by splitting the data into two subsets by a single column condition (value  $z$ ) can be calculated as follows:

$$p_1(z) = \text{proportion of column-value} > z \quad p_2(z) = \text{proportion of no default and column-value} > z \quad p_3(z) = p$$

and in python can we use the `calc_entropy` function to make it even simpler:

```
def calcSplittedEntropy(df, col, val, decision_on =
↳ "loan_status"):
    w = np.sum(df[col] > val)/len(df)
    result = w * calc_entropy(df.loc[df[col] > val], decision_on) +
↳ (1-w) * calc_entropy(df.loc[df[col] <= val], decision_on)
    return result
```

For example can we split the dataset by column `loan_percent_income` and value  $z = 0.3$  to archive an decrease in Entropy:

```
entropy_ofSplittedData = calcSplittedEntropy(df=data,
↳ col="loan_percent_income", val=0.3, decision_on =
↳ "loan_status")
print("Splitted Inpurity/Entropy of data: ",
↳ entropy_ofSplittedData)
```

```
## Splitted Inpurity/Entropy of data: 0.648938734265563
```

This split results in a decrease of python `round(entropy_of_data-entropy_ofSplittedData,5)` in the overall Entropy.

## 8.2 Constructing the Tree

First of all do we need to find the column and the value that results in the highest decrease of Entropy and splitt the dataset by it. Afterwards do we pass the resulting subsets into the same function (recursion). We will save the given conditions for the splitting. If the given subset contains less than `min_size` of rows or reached the `max_depth` it will turn into a leaf. We need to analyze the function properties to find the minimal value for the optimal splitting. The `calcSplittedEntropy` function is concave ("The Entropy is concave in the probability mass function"). We can use this property to write a simple minimiza that checks if the next evaluation is smaller than the previous and steps along the input value. If the evaluation is bigger, it will change the direction and decrease the step distance. It repeats this process until the change in the evaluation is stagnating.

```
def find_minima(df, col, decision_on = "loan_status", round_at =
↳ 5):
    direction = 1
    step = (df[col].max()-df[col].min()) * 0.1
    val = df[col].min() + step
    best_entropy = 1
```

```

stagnation = 0

while stagnation <= 15:
    temp = calcSplittedEntropy(df, col, val)
    if temp > best_entropy:
        direction = -direction
        step = 0.5 * step
        stagnation += 1
    elif round(temp, round_at) < round(best_entropy, round_at):
        stagnation = 0
    else:
        stagnation += 1
    best_entropy = temp
    val = val + direction * step

return best_entropy, val

```

This minimizer is written by my self and it only works for convex functions. I dont know if there do exist better approaches, but this one works.

Now do we need to find the best decrease in Entropy of all columns with the next function:

```

def find_best_col(df, decision_on = "loan_status", round_at = 5):
    cols = list(df.columns[df.columns != decision_on])
    entropys = np.ones(len(cols))
    vals = np.ones(len(cols))

    for i in range(len(cols)):
        entropys[i], vals[i] = find_minima(df, col=cols[i],
        ↪ decision_on = "loan_status", round_at = 5)

    best_i = int(np.where(entropys == min(entropys))[0][0])
    return cols[best_i], entropys[best_i], vals[best_i]

```

The following is an example of the output for the initial dataste:

```
find_best_col(data)
```

```
## ('loan_percent_income', 0.6564119496913492, 0.29990234374999997)
```

It's now time to build the tree and save everything that ends in a leaf:

```

def make_node_and_leafs(df, decision_on = "loan_status", round_at
↪ = 5, path = "I", condition = "", min_size = 1000, max_depth =
↪ 4, leafs = pd.DataFrame(columns=["path", "condition", "rows",
↪ "P_of_no_default", "entropy"])):
    if len(df) < min_size or (path.count("-")-1) >= max_depth or
↪ len(df.columns) <= 1:
        leafs = leafs.append({"path":path+""},
↪ "condition":condition[0:(len(condition)-5)], "rows":len(df),
↪ "P_of_no_default":np.sum(df[decision_on] == 0)/len(df),
↪ "entropy":calc_entropy(df)}, ignore_index=True)
    else:
        col, entropy, val = find_best_col(df, decision_on, round_at)
        print("path:", path, " entropy:", entropy, " col:", col, "
↪ val:", val, " rows:", len(df))
        leafs = make_node_and_leafs( df.loc[df[col] > val, df.columns
↪ != col], decision_on, round_at, path+"-R", condition+col+" >
↪ "+str(float(round(val,5)))+ " and ", min_size, max_depth,
↪ leafs)
        leafs = make_node_and_leafs( df.loc[df[col] <= val,
↪ df.columns != col], decision_on, round_at, path + "-L",
↪ condition+col+" <= "+str(float(round(val,5)))+ " and ",
↪ min_size, max_depth, leafs)
    return(leafs)

leafs = make_node_and_leafs(df=data, decision_on = "loan_status",
↪ round_at = 5, min_size = 1000, max_depth = 4)
leafs["entropy"] = (leafs["entropy"]*leafs["rows"])/len(data)

print("Entropy in data: ", calc_entropy(data))
print("Entropy in all leafs: ", np.sum(leafs["entropy"]))

```

```

## path: I      entropy: 0.6564119496913492   col: loan_percent_income   val: 0.29990234374999997
## path: I-R    entropy: 0.9103981172376336   col: loan_int_rate      val: 14.01635546875   rows: 4
## path: I-R-L  entropy: 0.9607335396537932   col: cb_person_default_on_file   val: 0.14999999
## path: I-R-L-L  entropy: 0.9648046914552115   col: person_age      val: 34.296875   rows: 2977
## path: I-L    entropy: 0.531844917392527   col: loan_int_rate      val: 14.280073242187505   rows: 4
## path: I-L-R  entropy: 0.998669387657678   col: person_age      val: 22.3046875   rows: 4057
## path: I-L-R-R  entropy: 0.9992350724472542   col: cb_person_default_on_file   val: 0.14999999
## path: I-L-L  entropy: 0.44498607709157834   col: cb_person_default_on_file   val: 0.14999999
## path: I-L-L-R  entropy: 0.704963233218175   col: person_age      val: 33.9921875   rows: 2838
## path: I-L-L-L  entropy: 0.40973705382045866   col: person_age      val: 21.840624999999967   r
## Entropy in data:  0.7568007498467375
## Entropy in all leafs:  0.574488597974446

```

We can observe that the Entropy of all leafs is significantly smaller than the

initial Entropy.

### 8.3 Forecast Credit Defaults with DT

We must set a limit that divides all leafs by default and none default. We've set the restriction at 0.65, which indicates that leaves with a chance of none default of less than 65 percent are considered as defaults. The conditions column in the `leafs` table can be used to acquire these rows. The following analysis demonstrates the forecast's accuracy:

```
data_temp = data.copy()
data_temp["ID"] = list(range(len(data_temp)))
conditions = "(" + " | "
↳  (".".join(list(leafs.loc[leafs["P_of_no_default"] < 0.65,
↳  leafs.columns ==
↳  "condition"] ["condition"].replace("and", "&")) + ")")
data_temp = data_temp.query(conditions)
X = np.zeros(len(data))
X[list(data_temp["ID"])] = 1

Y = data.loc[:, data.columns == 'loan_status'].to_numpy()[:,0]

print("Wrong answers of the decission tree:
↳  ", np.sum(np.abs(Y-X))/len(Y) * 100, "%")
confusion_matrix(Y,X)
```

```
## Wrong answers of the decission tree: 17.94911144532089 %
## array([[21932, 3541],
##        [ 2307, 4801]], dtype=int64)
```

We can compare the results to the previews created NN (with `hidden_layer_neurons = [4,4]`, `alpha = 0.01`, `epochs = 500`, `batch_size = 2000`):

### 8.4 Extern Packages

There do exist some packages to create DTs for example `sklearn`, but i wasnt able to get the conditions out of it like in my own code:

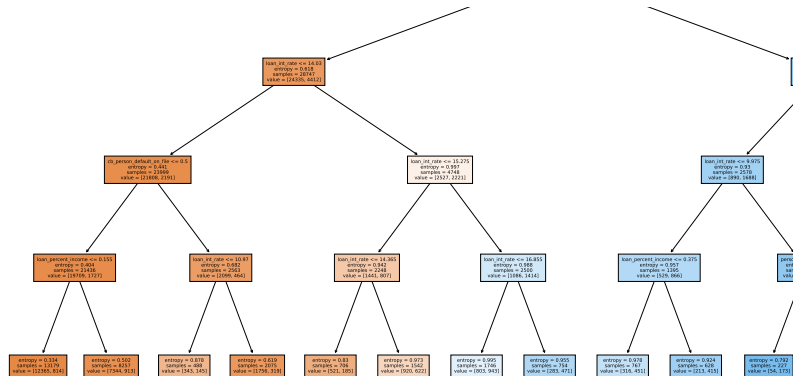
```
from sklearn.tree import DecisionTreeClassifier, plot_tree,
↳  export_graphviz, export_text
X = data.drop('loan_status', axis=1)
```

```

y = data['loan_status']
clf =
↳ DecisionTreeClassifier(criterion='entropy',max_depth=4,min_samples_split=1000,min_samples_leaf=10)
clf = clf.fit(X,y)
pyplot.figure(figsize=(16,8))
plot_tree(clf, filled=True, feature_names=X.columns,
↳ proportion=False, fontsize=6)
pyplot.show()

r = export_text(clf, feature_names=list(X.columns))
print(r)

```



```

## |--- loan_percent_income <= 0.31
## |   |--- loan_int_rate <= 14.03
## |   |   |--- cb_person_default_on_file <= 0.50
## |   |   |   |--- loan_percent_income <= 0.16
## |   |   |   |   |--- class: 0
## |   |   |   |   |--- loan_percent_income > 0.16
## |   |   |   |   |   |--- class: 0
## |   |   |   |--- cb_person_default_on_file > 0.50
## |   |   |   |   |--- loan_int_rate <= 10.97
## |   |   |   |   |   |--- class: 0
## |   |   |   |   |   |--- loan_int_rate > 10.97
## |   |   |   |   |   |   |--- class: 0
## |   |--- loan_int_rate > 14.03
## |   |   |--- loan_int_rate <= 15.28
## |   |   |   |--- loan_int_rate <= 14.37
## |   |   |   |   |--- class: 0
## |   |   |   |   |--- loan_int_rate > 14.37

```

```

## |   |   |   |   |--- class: 0
## |   |   |--- loan_int_rate > 15.28
## |   |   |   |--- loan_int_rate <= 16.85
## |   |   |   |   |--- class: 1
## |   |   |   |--- loan_int_rate > 16.85
## |   |   |   |   |--- class: 1
## |--- loan_percent_income > 0.31
## |   |--- loan_int_rate <= 12.76
## |   |   |--- loan_int_rate <= 9.97
## |   |   |   |--- loan_percent_income <= 0.38
## |   |   |   |   |--- class: 1
## |   |   |   |--- loan_percent_income > 0.38
## |   |   |   |   |--- class: 1
## |   |   |--- loan_int_rate > 9.97
## |   |   |   |--- person_age <= 22.50
## |   |   |   |   |--- class: 1
## |   |   |   |--- person_age > 22.50
## |   |   |   |   |--- class: 1
## |   |--- loan_int_rate > 12.76
## |   |   |--- loan_int_rate <= 14.31
## |   |   |   |--- class: 1
## |   |   |--- loan_int_rate > 14.31
## |   |   |   |--- class: 1

```

## 8.5 Appendix (complete code)

```

import numpy as np
import pandas as pd
from sklearn.metrics import confusion_matrix
import matplotlib.pyplot as pyplot
import math as ma

data =
↳ pd.read_csv("example_data/credit_risk_dataset.csv").fillna(0)
data = data.replace({"Y": 1, "N": 0})
data = data.loc[:, ["person_age", "loan_percent_income",
↳ "loan_int_rate", "cb_person_default_on_file", "loan_status"]]

def calc_entropy(df, decision_on = "loan_status"):
    if len(df)==0:

```



```

    return(0)
p = np.sum(df[decision_on] == 0)/len(df)
if p == 0 or p == 1:
    return(0)
result = -p * ma.log(p,2) - (1-p)*ma.log(1-p,2)
return result

def calcSplitted_entropy(df, col, val, decision_on =
↳ "loan_status"):
    w = np.sum(df[col] > val)/len(df)
    result = w * calc_entropy(df.loc[df[col] > val], decision_on) +
↳ (1-w) * calc_entropy(df.loc[df[col] <= val], decision_on)
    return result

def find_minima(df, col, decision_on = "loan_status", round_at =
↳ 5):
    direction = 1
    step = (df[col].max()-df[col].min()) * 0.1
    val = df[col].min() + step
    best_entropy = 1
    stagnation = 0

    while stagnation <= 15:
        temp = calcSplitted_entropy(df, col, val)
        if temp > best_entropy:
            direction = -direction
            step = 0.5 * step
            stagnation += 1
        elif round(temp,round_at) < round(best_entropy,round_at):
            stagnation = 0
        else:
            stagnation += 1
            best_entropy = temp
            val = val + direction * step

    return best_entropy, val

def find_best_col(df, decision_on = "loan_status", round_at = 5):
    cols = list(df.columns[df.columns != decision_on])
    entropys = np.ones(len(cols))
    vals = np.ones(len(cols))

    for i in range(len(cols)):
        entropys[i], vals[i] = find_minima(df, col=cols[i],
↳ decision_on = "loan_status", round_at = 5)

```

```

best_i = int(np.where(entropys == min(entropys))[0][0])
return cols[best_i], entropys[best_i], vals[best_i]

def make_node_and_leafs(df, decision_on = "loan_status", round_at
↪ = 5, path = "I", condition = "", min_size = 1000, max_depth =
↪ 4, leafs = pd.DataFrame(columns=["path", "condition", "rows",
↪ "P_of_no_default", "entropy"])):
    if len(df) < min_size or (path.count("-")-1) >= max_depth or
    ↪ len(df.columns) <= 1:
        leafs = leafs.append({"path":path+""},
    ↪ "condition":condition[0:(len(condition)-5)], "rows":len(df),
    ↪ "P_of_no_default":np.sum(df[decision_on] == 0)/len(df),
    ↪ "entropy":calc_entropy(df)}, ignore_index=True)
    else:
        col, entropy, val = find_best_col(df, decision_on, round_at)
        print("path:", path, " entropy:", entropy, " col:", col, "
    ↪ val:", val, " rows:", len(df))
        leafs = make_node_and_leafs( df.loc[df[col] > val, df.columns
    ↪ != col], decision_on, round_at, path+"-R", condition+col+" >
    ↪ "+str(float(round(val,5)))+ " and ", min_size, max_depth,
    ↪ leafs)
        leafs = make_node_and_leafs( df.loc[df[col] <= val,
    ↪ df.columns != col], decision_on, round_at, path + "-L",
    ↪ condition+col+" <= "+str(float(round(val,5)))+ " and ",
    ↪ min_size, max_depth, leafs)
    return(leafs)

leafs = make_node_and_leafs(df=data, decision_on = "loan_status",
↪ round_at = 5, min_size = 1000, max_depth = 4)
leafs["entropy"] = (leafs["entropy"]*leafs["rows"])/len(data)

print("Entropy in data: ", calc_entropy(data))
print("Entropy in all leafs: ", np.sum(leafs["entropy"]))

data_temp = data.copy()
data_temp["ID"] = list(range(len(data_temp)))

```

```

conditions = "(" + " |
↳ (".join(list(leafs.loc[leafs["P_of_no_default"] < 0.65,
↳ leafs.columns ==
↳ "condition"]["condition"].replace("and", "&")) + ")"
data_temp = data_temp.query(conditions)
X = np.zeros(len(data))
X[list(data_temp["ID"])] = 1

Y = data.loc[:, data.columns == 'loan_status'].to_numpy()[:,0]

print("Wrong answers of the decission tree:
↳ ", np.sum(np.abs(Y-X))/len(Y) * 100, "%")
confusion_matrix(Y,X)

```

```

## path: I      entropy: 0.6564119496913492   col: loan_percent_income   val: 0.29990234374999997
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## path: I-R-L-L entropy: 0.9648046914552115   col: person_age        val: 34.296875   rows: 2977
## path: I-L    entropy: 0.531844917392527   col: loan_int_rate      val: 14.280073242187505   rows:
## path: I-L-R  entropy: 0.998669387657678   col: person_age        val: 22.3046875   rows: 4057
## path: I-L-R-R entropy: 0.9992350724472542   col: cb_person_default_on_file   val: 0.149999
## path: I-L-L  entropy: 0.44498607709157834   col: cb_person_default_on_file   val: 0.149999
## path: I-L-L-R entropy: 0.704963233218175   col: person_age        val: 33.9921875   rows: 2838
## path: I-L-L-L entropy: 0.40973705382045866   col: person_age        val: 21.840624999999967   r
## Entropy in data: 0.7568007498467375
## Entropy in all leafs: 0.574488597974446
## Wrong answers of the decission tree: 17.94911144532089 %
## array([[21932, 3541],
##        [ 2307, 4801]], dtype=int64)

```