

system 1

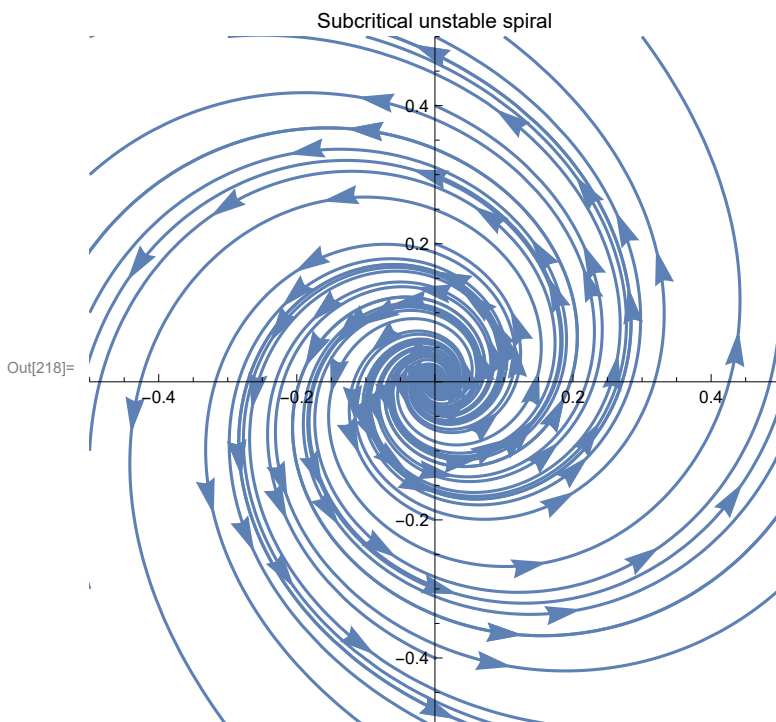
positive μ

```
In[208]:= Clear["Global`*"]
tEnd = -6;
tStart = 0;
xMin = -0.5;
xMax = 0.5;
yMin = -0.5;
yMax = 0.5;
systemSolver[x0_, y0_] =
  NDSolve[{x'[t] ==  $\mu$  * x[t] - 3 y[t] - x[t]^3, y'[t] == 3 x[t] +  $\mu$  * y[t] + 2 y[t]^3,
    x[0] == x0, y[0] == y0} /.  $\mu \rightarrow 1$ , {x, y}, {t, tStart, tEnd}];

table1 = Table[{0, y}, {y, yMin, yMax, 0.1}];
table2 = Table[{xMin, y}, {y, yMin, yMax, 0.2}];
table3 = Table[{xMax, y}, {y, yMin, yMax, 0.2}];
table4 = Table[{x, yMin}, {x, xMin, xMax, 0.2}];
table5 = Table[{x, yMax}, {x, xMin, xMax, 0.2}];
initialCondition = Join[table1, table2, table3, table4, table5];

Show[Table[ParametricPlot[Evaluate[
  {x[t], y[t]} /. systemSolver[initialCondition[[i, 1]], initialCondition[[i, 2]]],
  {t, tStart, tEnd}, PlotRange -> {{xMin, xMax}, {yMin, yMax}},
  {i, Length[initialCondition]}] /.
  Line[x_] -> {Arrowheads[{0., 0.04, 0.04, 0.04, 0.}], Arrow[x]}],
  PlotLabel -> "Subcritical unstable spiral"]
```

... NDSolve: Initial condition x0 is not a number or a rectangular array of numbers.



negative μ

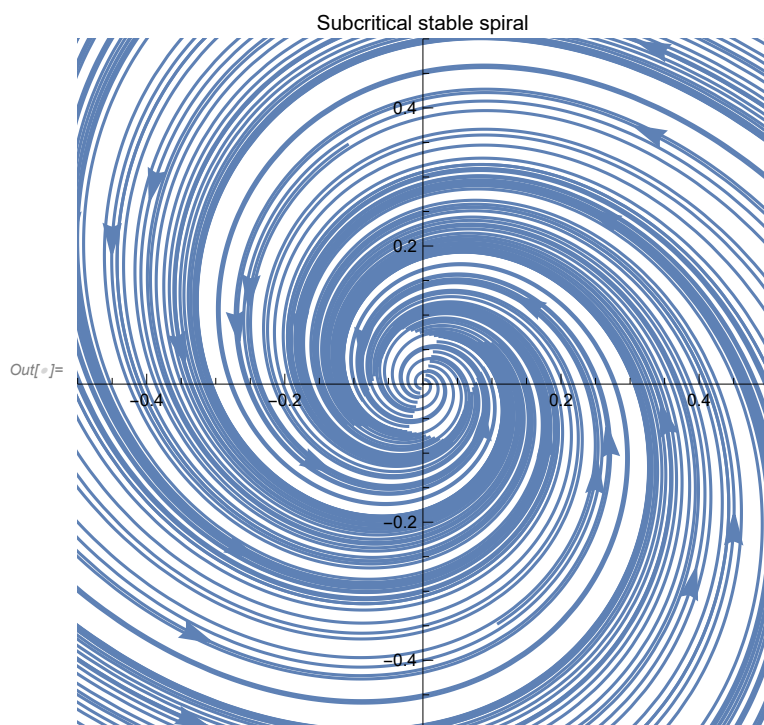
```

In[ ]:= Clear["Global`*"]
tEnd = -2;
tStart = 2;
xMin = -0.5;
xMax = 0.5;
yMin = -0.5;
yMax = 0.5;
systemSolver[x0_, y0_] =
  NDSolve[{x'[t] ==  $\mu$  * x[t] - 3 y[t] - x[t]^3, y'[t] == 3 x[t] +  $\mu$  * y[t] + 2 y[t]^3,
    x[0] == x0, y[0] == y0} /.  $\mu \rightarrow -1$ , {x, y}, {t, tStart, tEnd}];

table1 = Table[{0, y}, {y, yMin, yMax, 0.05}];
table2 = Table[{xMin, y}, {y, yMin, yMax, 0.05}];
table3 = Table[{xMax, y}, {y, yMin, yMax, 0.05}];
table4 = Table[{x, yMin}, {x, xMin, xMax, 0.05}];
table5 = Table[{x, yMax}, {x, xMin, xMax, 0.05}];
initialCondition = Join[table1, table2, table3, table4, table5];

Show[Table[ParametricPlot[Evaluate[
  {x[t], y[t]} /. systemSolver[initialCondition[[i, 1]], initialCondition[[i, 2]]],
  {t, tStart, tEnd}, PlotRange -> {{xMin, xMax}, {yMin, yMax}}],
  {i, Length[initialCondition]}] /.
  Line[x_] -> {Arrowheads[{0., 0.04, 0.04, 0.04, 0.}], Arrow[x]},
  PlotLabel -> "Subcritical stable spiral"]

```



(*We see that the above plot is stable since all the arrows move towards the center*)

system 2

Positive μ

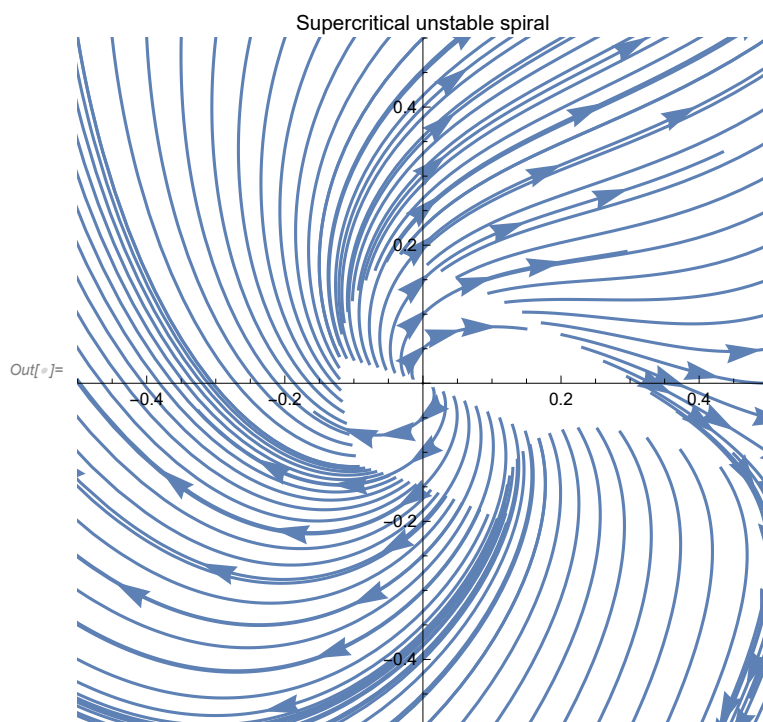
```

In[ ]:= Clear["Global`*"]
tEnd = -1.2;
tStart = 1.2;
xMin = -0.5;
xMax = 0.5;
yMin = -0.5;
yMax = 0.5;
systemSolver[x0_, y0_] =
  NDSolve[{x'[t] ==  $\mu$  * x[t] + y[t] - x[t]^2, y'[t] == -x[t] +  $\mu$  * y[t] + 2 x[t]^2,
    x[0] == x0, y[0] == y0} /.  $\mu \rightarrow 1$ , {x, y}, {t, tStart, tEnd}];
table1 = Table[{0, y}, {y, yMin, yMax, 0.05}];
table2 = Table[{xMin, y}, {y, yMin, yMax, 0.05}];
table3 = Table[{xMax, y}, {y, yMin, yMax, 0.05}];
table4 = Table[{x, yMin}, {x, xMin, xMax, 0.05}];
table5 = Table[{x, yMax}, {x, xMin, xMax, 0.05}];
initialCondition = Join[table1, table2, table3, table4, table5];

Show[Table[ParametricPlot[Evaluate[
  {x[t], y[t]} /. systemSolver[initialCondition[[i, 1]], initialCondition[[i, 2]]],
  {t, tStart, tEnd}, PlotRange -> {{xMin, xMax}, {yMin, yMax}}],
  {i, Length[initialCondition]}] /.
  Line[x_] -> {Arrowheads[{0., 0.04, 0.04, 0.04, 0.}], Arrow[x]},
  PlotLabel -> "Supercritical unstable spiral"]

```

⋯ NDSolve: Initial condition x0 is not a number or a rectangular array of numbers.

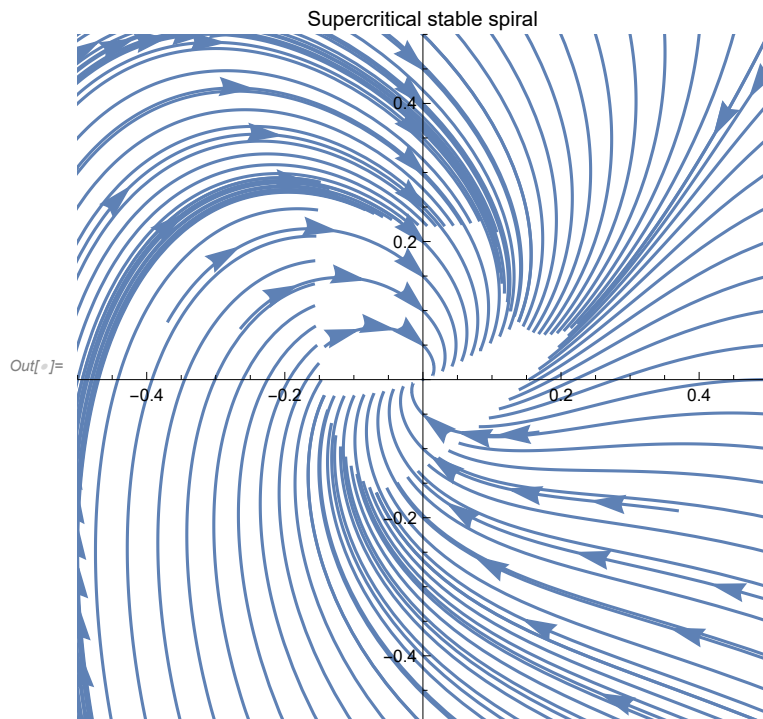


(*We see that the above plot is unstable since the arrows moves away from the center*)

negative μ

```
In[ ]:= Clear["Global`*"]
tEnd = -1.2;
tStart = 1.2;
xMin = -0.5;
xMax = 0.5;
yMin = -0.5;
yMax = 0.5;
systemSolver[x0_, y0_] =
  NDSolve[{x'[t] ==  $\mu$  * x[t] + y[t] - x[t]^2, y'[t] == -x[t] +  $\mu$  * y[t] + 2 x[t]^2,
    x[0] == x0, y[0] == y0} /.  $\mu \rightarrow -1$ , {x, y}, {t, tStart, tEnd}];
table1 = Table[{0, y}, {y, yMin, yMax, 0.05}];
table2 = Table[{xMin, y}, {y, yMin, yMax, 0.05}];
table3 = Table[{xMax, y}, {y, yMin, yMax, 0.05}];
table4 = Table[{x, yMin}, {x, xMin, xMax, 0.05}];
table5 = Table[{x, yMax}, {x, xMin, xMax, 0.05}];
initialCondition = Join[table1, table2, table3, table4, table5];

Show[Table[ParametricPlot[Evaluate[
  {x[t], y[t]} /. systemSolver[initialCondition[[i, 1]], initialCondition[[i, 2]]],
  {t, tStart, tEnd}, PlotRange -> {{xMin, xMax}, {yMin, yMax}}],
  {i, Length[initialCondition]}] /.
  Line[x_] -> {Arrowheads[{0., 0.04, 0.04, 0.04, 0.}], Arrow[x]},
  PlotLabel -> "Supercritical stable spiral"]
```



(*We see that it's stable since the arrows move towards the center*)
(*In conclusion, the plots agree with my answers in task c). I got that $a_1 > 0$ which means that all plots for system 1 should be subcritical which the plots show. And I got that $a_2 < 0$ which means that all the plots for system 2 should be supercritical*)