

4.2)

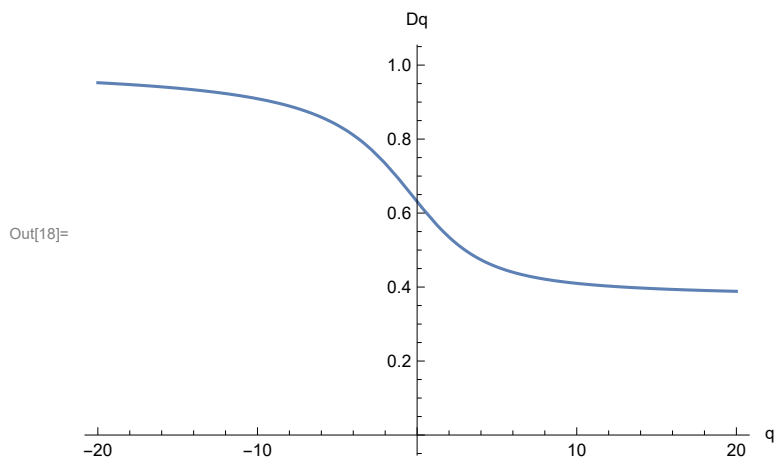
a)

```
In[5]:= (*The answer is derived by paper and pen,  
so it is attached in a seperate file in OpenTa*)  
Dq[q_] := 1 / (1 - q) * Log[(2 / 3) ^ q + (1 / 3) ^ q] / Log[3];  
Dq[q]
```

$$\text{Out[6]} = \frac{\text{Log}\left[\left(\frac{2}{3}\right)^q + 3^{-q}\right]}{(1 - q) \text{Log}[3]}$$

b)

```
In[17]:= DqPlot = Plot[Dq[q], {q, -20, 20}];  
Show[DqPlot, AxesLabel -> {"q", "Dq"},  
PlotRange -> {{-20, 20}, {0, 1}}, AxesOrigin -> {0, 0}]
```



c)

(*Just put in the values for q,
so q=1 and q=2! Need limit for q=1 otherwise it will be zero in the denominator*)

```
D1 = Limit[Dq[q], q -> 1]
```

```
D2 = Dq[2]
```

$$\text{Out[15]} = \frac{\text{Log}\left[\frac{27}{4}\right]}{\text{Log}[27]}$$

$$\text{Out[16]} = \frac{\text{Log}\left[\frac{9}{5}\right]}{\text{Log}[3]}$$

d)

```
In[22]:= (*Just make the q go to infinity and in the other case -infinity*)
```

```
DInf = Limit[Dq[q], q → Infinity]
```

```
DNegativeInf = Limit[Dq[q], q → -Infinity]
```

```
Out[22]= 
$$\frac{\text{Log}\left[\frac{3}{2}\right]}{\text{Log}[3]}$$

```

```
Out[23]= 1
```