An open reproducible framework for the study of the iterated prisoner's dilemma

Owen Campbell Marc Harper Vincent Knight Karol Languer

October 11, 2015

1 Introduction

As stated in [4]: "few works in social science have had the general impact of [Axelrod's study of the evolution of cooperation]". In 1980, Axelrod wrote two papers: [1, 2] which described a computer tournament that has been at the origin of a majority of game theoretic work [3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 15, 16, 17, 18, 19, 20]. As described in [4] this work has not only had mathematical impact but has also led to insights in biology (for example in [6], a real tournament where Blu Jays are the participants is described) and in particular to the study of evolution.

The tournament is based on an iterated game (see [14] or similar for details) where two players repeatedly play the normal form game of (1) in full knowledge of each others playing history to date. An excellent description of the *one shot* game is given in [10] which is paraphrased below:

Two players must choose between Cooperate(C) and Defect(D):

- If both choose C, they receive a payoff of R (Reward);
- If both choose D, they receive a payoff of P (Ppunishment);
- If one chooses C and the other D, the defector receives a payoff of T (Temptation) and the cooperator a payoff of S (Sucker).

$$\begin{pmatrix} R, R & S, T \\ S, S & P, P \end{pmatrix} \quad \text{such that } T > R > P > S \text{ and } 2R > T + S \tag{1}$$

The game of (1) is called the Prisoner's Dilemma. Numerical values of (R, S, T, P) = (3, 0, 5, 1) are often used in the literature.

Axelrod's tournaments (and further implementations of these) are sometimes referred to as Iterated Prisoner's Dilemma tournaments.

- Review of the tournament itself; Original paper by Axelrod and Hamilton [1981-Axelrod-Hamilton]. Some recent discussion of memory one strategies [press2012iterated, stewart2012extortion].
- Discussion about open reproducible science (there are some reference around) (Python, git, github etc...)
- Overview of the library (what it can do, what has been done with it)
- Point at Sections 2 and 3.

2 Reproducing previous tournaments

3 New strategies, tournaments and implications

4 Conclusion

References

- [1] R. Axelrod. "Effective Choice in the Prisoner's Dilemma". In: Journal of Conflict Resolution 24.1 (1980), pp. 3–25 (cit. on p. 1).
- [2] R. Axelrod. "More Effective Choice in the Prisoner's Dilemma". In: *Journal of Conflict Resolution* 24.3 (1980), pp. 379–403. ISSN: 0022-0027. DOI: 10.1177/002200278002400301 (cit. on p. 1).
- [3] J. S. Banks and R. K. Sundaram. "Repeated games, finite automata, and complexity". In: Games and Economic Behavior 2.2 (1990), pp. 97–117. ISSN: 08998256. DOI: 10.1016/0899-8256(90)90024-0 (cit. on p. 1).
- [4] J. Bendor, R. M. Kramer, and S. Stout. "When in doubt . . .: Cooperation in a noisy prisoner's dilemma". In: *Journal of Conflict Resolution* 35.4 (1991), pp. 691–719. ISSN: 0022-0027. DOI: 10.1177/0022002791035004007 (cit. on p. 1).
- [5] R. Boyd and J. P. Lorberbaum. "No pure strategy is evolutionarily stable in the repeated Prisoner's Dilemma game". In: *Nature* 327 (1987), pp. 58–59. ISSN: 0028-0836. DOI: 10.1006/jtbi.1994.1092 (cit. on p. 1).
- [6] K. Chellapilla and D. B. Fogel. "Evolution, neural networks, games, and intelligence". In: Proceedings of the Ieee 87.9 (1999), pp. 1471–1496. ISSN: 00189219. DOI: Doi:10.1109/5.784222. URL: "3CGo"/20to"/20ISI%3E://WOS:000082176700004 (cit. on p. 1).
- [7] F. David B. "Evolving Behaviors in the Iterated Prisoner's Dilemma". In: Evol. Comput. 1.1 (1993), pp. 77-97. ISSN: 1063-6560. DOI: 10.1162/evco.1993.1.1.77. URL: http://dx.doi.org/10.1162/evco.1993.1.1.77\$%5Cbackslash\$nhttp://dl.acm.org/ft%5C_gateway.cfm?id=1326628%5C&type=pdf\$%5Cbackslash\$nhttp://www.mitpressjournals.org/action/cookieAbsent (cit. on p. 1).
- [8] M. Doebeli and C. Hauert. "Models of cooperation based on the Prisoner's Dilemma and the Snowdrift game". In: *Ecology Letters* 8.7 (2005), pp. 748–766. ISSN: 1461023X. DOI: 10.1111/j.1461-0248. 2005.00773.x (cit. on p. 1).
- [9] G. Ellison. "Cooperation in the prisoner's dilemma with anonymous random matching". In: Review of Economic Studies 61.3 (1994), pp. 567–588. ISSN: 00346527. DOI: 10.2307/2297904 (cit. on p. 1).
- [10] N. Gotts, J. Polhill, and A. Law. "Agent-based simulation in the study of social dilemmas". In: Artificial Intelligence Review 19 (2003), pp. 3–92. ISSN: 0269-2821. DOI: 10.1023/A:1022120928602. URL: http://dl.acm.org/citation.cfm?id=608970 (cit. on p. 1).
- [11] a.G. Isaac. "Simulating Evolutionary Games: A Python-Based Introduction". In: *Journal of Artificial Societies and Social Simulation* 11.3 (2008), p. 8. ISSN: 14607425. URL: http://jasss.soc.surrey.ac.uk/11/3/8.html (cit. on p. 1).
- [12] D. Kraines and V. Kraines. "Pavlov and the prisoner's dilemma". In: *Theory and Decision* 26.1 (1989), pp. 47–79. ISSN: 00405833. DOI: 10.1007/BF00134056 (cit. on p. 1).
- [13] J. P. Lorberbaum. "No strategy is evolutionarily stable in the repeated Prisoner's Dilemma game". In: Journal of Theoretical Biology 168.2 (1994), pp. 117–130 (cit. on p. 1).

- [14] M. Maschler, E. Solan, and S. Zamir. *Game theory*. Cambridge University Press, 2013, p. 1003. ISBN: 9781107005488. DOI: http://dx.doi.org/10.1017/CB09780511794216. URL: http://www.cambridge.org/gb/academic/subjects/economics/economics-general-interest/game-theory (cit. on p. 1).
- [15] P. Milgrom, J. Roberts, and R. Wilson. "Rational Cooperation in the Finitely Repeated Prisoners' Dilemma". In: *Journal of Economic Theory* 252 (1982), pp. 245–252 (cit. on p. 1).
- [16] P. Molander. "The optimal level of generosity in a selfish, uncertain environment". In: *The Journal of Conflict Resolution* 29.4 (1985), pp. 611–618. ISSN: 0022-0027. DOI: 10.1177/0022002785029004004 (cit. on p. 1).
- [17] J. K. Murnighan et al. "Expecting Continued Play in Prisoner's Dilemma Games". In: 27.2 (1983), pp. 279–300 (cit. on p. 1).
- [18] W. H. Press and F. J. Dyson. "Iterated Prisoner's Dilemma contains strategies that dominate any evolutionary opponent". In: *Proceedings of the National Academy of Sciences* 109.26 (2012), pp. 10409–10413. ISSN: 0027-8424. DOI: 10.1073/pnas.1206569109 (cit. on p. 1).
- [19] D. W. Stephens, C. M. McLinn, and J. R. Stevens. "Discounting and reciprocity in an Iterated Prisoner's Dilemma." In: Science (New York, N.Y.) 298.5601 (2002), pp. 2216–2218. ISSN: 00368075. DOI: 10.1126/science.1078498 (cit. on p. 1).
- [20] a. J. Stewart and J. B. Plotkin. "Extortion and cooperation in the Prisoner's Dilemma". In: Proceedings of the National Academy of Sciences 109.26 (2012), pp. 10134–10135. ISSN: 0027-8424. DOI: 10.1073/ pnas.1208087109 (cit. on p. 1).