A numerical study of fixation probabilities for strategies in the Iterated Prisoner's Dilemma

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Abstract

The Iterated Prisoner's Dilemma is a well established framework for the study of emergent behaviour. In this paper an extensive numerical study of the evolutionary dynamics of this framework are presented.

Fixation probabilities for Moran processes are obtained for 172 different strategies. This is done in both a standard 200 turn interaction and a noisy setting.

To the authors knowledge this is the largest such study. It allows for insights about the behaviour and performance of strategies with regard to their survival in an evolutionary setting.

1 Introduction

Since the formulation of the Moran Process in [9], this model of evolutionary population dynamics has been used to gain insights about the evolutionary stability of strategies in a number of settings. Similarly since the first Iterated Prisoner's Dilemma (IPD) tournament described in [2] the Prisoner's dilemma has been used to understand the evolution of cooperative behaviour in complex systems.

The analytical models of a Moran process are based on the relative fitness between two strategies and take this to be a fixed value r [11]. This is a valid model for simple strategies of the Prisoner's Dilemma such as to always cooperate or always defect. This manuscript provides a detailed numerical analysis of 172 complex and adaptive strategies for the IPD. In this case the relative fitness of a strategy is dependent on the population distribution.

Further deviations from the analytical model occur when interactions between players are subject to uncertainty. This is referred to as noise and has been considered in the IPD setting in [4, 10, 14]. Noise is also considered here.

This work provides answers to the following questions:

- 1. What strategies are good invaders?
- 2. What strategies are good at resisting invasion?
- 3. How does the population size affect these findings?

Figure 1 shows a diagrammatic representation of the Moran process. The Moran process is a stochastic birth death process on a finite population in which the population size stays constant over time. Individuals are **selected** according to a given fitness landscape. Once selected, a given individual is reproduced and similarly another individual is chosen to be removed from the population. In some settings mutation is also considered but without mutation (the case considered in this work) this process will arrive at an absorbing state where the population is entirely made up of a single individual. The probability with which a given strategy is the survivor is called the absorption probability. A more detailed analytic description of this is given in Section 3.

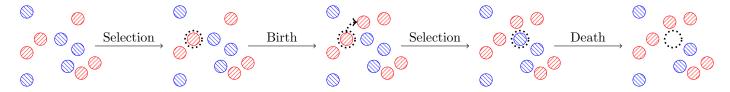


Figure 1: A diagrammatic representation of a Moran process

The Moran process was initially introduced in [9] in a genetic setting. It has sine been used in a variety of settings including the understanding of the spread of cooperative behaviour. However, as stated before, these mainly consider non sophisticated strategies. Some work has looked at evolutionary stability of strategies within the Prisoner's Dilemma [7]

but this is not done in the more widely used setting of the Moran process but in terms of infinite population stability. In [3] Moran processes are looked at in a theoretic framework for a small subset of strategies. In [6] machine learning techniques are used to train a strategy capable of resisting invasion and also invade any memory one strategy. Recent work [Hilbe2017] has investigated the effect of memory length on strategy performance and the emergence of cooperation but this is not done in Moran process context and only considers specific cases of memory 2 strategies.

The contribution of this work is a detailed and extensive analysis of absorption probabilities for 172 strategies. These strategies and the numerical simulations are from [12] which is an open source research library written for the study of the IPD. The strategies and simulation frameworks are automatically tested in accordance to best practice. The large number of strategies are available thanks to the open source nature of the project with over 40 contributions made by different programmers. Thus by considering Moran processes with population size greater than 2 we are taking in to account the effect of complex population dynamics. By considering sophisticated strategies we are taking in to effect the reputation of a strategy during each interaction.

Section 2 will explain the methodological approach used, Section 3 will validate the methodology by comparing simulated results to analytical results. The main results of this manuscript are presented in Section 4 which will present a detailed analysis of all the data generated. Finally, Section 5 will conclude and offer future avenues for the work presented here.

2 Methodology

To carry out this large numerical experiment 172 strategies are used from [12]. These include 169 default strategies in the library at the time (excluding strategies classified as having a long run time) as well as the following 3 finite state machine machine strategies [1]:

Appendix A shows all the players in question. More information about each player can be obtained in the documentation for [12]. The memory depth of the used strategies is shown in Table 1a.

Memory Depth	0	1	2	3	4	5	6	9	10	11	12	16	20	40	200	∞
Count	3	31	12	8	2	6	1	1	5	1	1	2	2	2	1	94

(a) Memory depth

Stochastic	Count
False	123
True	49

(b) Stochastic versus deterministic

Table 1: Summary of properties of used strategies

All strategies are paired and these pairs are used in 2000 repetitions of a Moran process assuming a starting population of (N/2, N/2). This is repeated for even N between 2 and 14. The fixation probability is then estimated for each value of N.

Note that due to the high computational cost of these experiments, for any given interaction between two players within the Moran process the outcome is sampled from a pre computed cache of 1000 match outcomes. This is carried out using the approximate Moran process implemented in [12].

As an example, Figure 2 shows the scores between two players that over the 1000 outcomes gives 971 different scores. A variety of software libraries have been used in this work:

- The Axelrod library (IPD strategies and Moran processes) [12].
- The matplotlib library (visualisation) [5].
- The pandas and numpy libraries (data manipulation) [8, 13].

Section 3 will validate this approach against theoretic results.

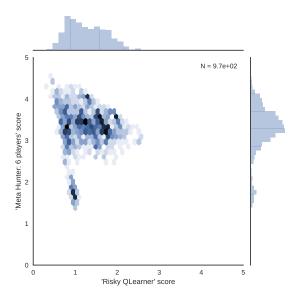


Figure 2: All possible scores for the pair of strategies that have the most different number of match outcomes

3 Validation

As described in [11] Consider the payoff matrix:

$$M = \begin{pmatrix} a, b \\ c, d \end{pmatrix} \tag{1}$$

The expected payoffs of i players of the first type in a population with N-i players of the second type are given by:

$$F_i = \frac{a(i-1) + b(N-i)}{N-1} \tag{2}$$

$$G_i = \frac{ci + d(N - i - 1)}{N - 1} \tag{3}$$

With an intensity of selection ω the fitness of both strategies is given by:

$$f_i = 1 - \omega + \omega F_i \tag{4}$$

$$g_i = 1 - \omega + \omega G_i \tag{5}$$

The transitions within the birth death process that underpins the Moran process are then given by:

$$p_{i,i+1} = \frac{if_i}{if_i + (N-i)g_i} \frac{N-i}{N}$$
 (6)

$$p_{i,i-1} = \frac{(N-i)g_i}{if_i + (N-i)g_i} \frac{i}{N}$$
 (7)

$$p_{ii} = 1 - p_{i,i+1} - p_{i,i-1} \tag{8}$$

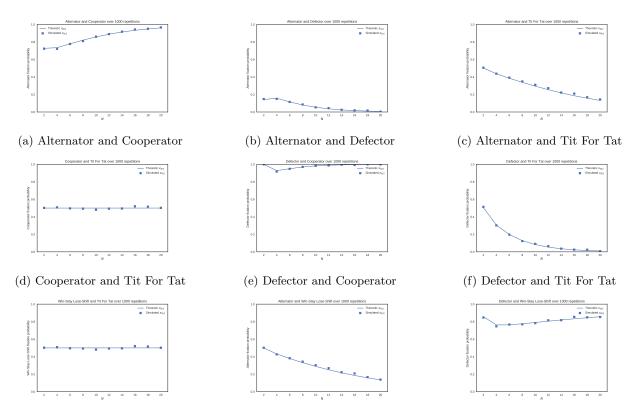
Using this it is a known result that the fixation probability of the first strategy in a population of i individuals of the first type (and N-i individuals of the second. We have:

$$x_{i} = \frac{1 + \sum_{j=1}^{i-1} \prod_{k=1}^{j} \gamma_{j}}{1 + \sum_{j=1}^{N-1} \prod_{k=1}^{j} \gamma_{j}}$$
(9)

where:

$$\gamma_j = \frac{p_{j,j-1}}{p_{j,j+1}}$$

Using this comparisons of $x_{N/2}$ are shown in Figure 3. Note that these are all deterministic strategies and show a perfect match up between the expected value of (9) and the actual Moran process for all strategies pairs.



(g) Win Stay Lose Shift and Tit For Tat (h) Alternator and Win Stay Lose Shift (i) Defector and Win Stay Lose Shift

Figure 3: Comparison of theoretic and actual Moran Process fixation probabilities for **deterministic** strategies

Figure 4 shows the fixation probabilities for stochastic strategies. These are no longer a good match which highlights the weakness of the analytical formulae that relies on the average payoffs. A detailed analysis of the 172 strategies considered will be shown in the next Section.

4 Numerical results

Figures 6 and ?? shows the fixation rates of each player on the y axis against each player on the x axis.

Figure ?? and ?? show the distribution of the fixation rates for all strategies.

Figure ?? and ?? show the distribution of the median fixation rates for all strategies.

Figures 13a and 13b show the median rank of each strategy against population size in the standard and noisy settings. Note that these ranks are not necessarily integers as group ties are given the average rank.

Tables 2, 3, 4 and 5 show the rankings across population size based for the top on bottom performers across the extreme population sizes.

Table 6 shows the performance based on memory length.

5 Conclusion

Further work:

• Spatial structure;

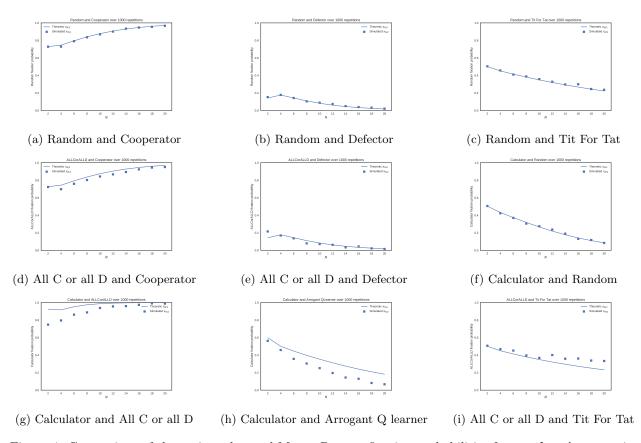


Figure 4: Comparison of theoretic and actual Moran Process fixation probabilities for stochastic strategies

Player			2	4	6	8	1	0 12	14
ZD-Extort-4: 0.23529411764	705882, 0.5	25, 1 1	.0 107	7.0 1	22.0	127.0	136.	0 138.0	136.0
Meta Winner Memory One:	31 players	2	2.0 113	3.5 1	20.5	126.0	126.	0 132.0	134.0
Feld: 1.0, 0.5, 200		3	3.0 106	6.0 1	16.0	121.0	123.	0 127.0	128.0
ZD-Extort-2: 0.1111111111111	1111, 0.5	4	1.0 123	3.0 1	36.0	147.0	148.	5 148.0	148.0
ZD-Extort-2 v2: 0.125, 0.5, 1		5	$5.0 ext{ } 121$	1.0	33.0	146.0	150.	0 146.0	146.5
Player	2	4	6	8	8	10	12	14	
Cycler CCCCCD	168.0	153.0	149.0	144.0	0 13	37.0 1	35.0	131.0	
e	169.0	171.0	158.0	156.0	0 15	56.0 1	62.0	163.0	
Cycler CCCD	170.0	157.0	150.0	149.0	0 14	45.0 1	43.0	143.5	
Tricky Cooperato	r 171.0	158.5	152.0	150.0	0 14	16.0 1	61.0	160.0	
π	172.0	172.0	159.0	159.0	0 15	57.0 1	55.0	159.0	

Table 2: Performance across population sizes of top and bottom performing strategies in population size N=2

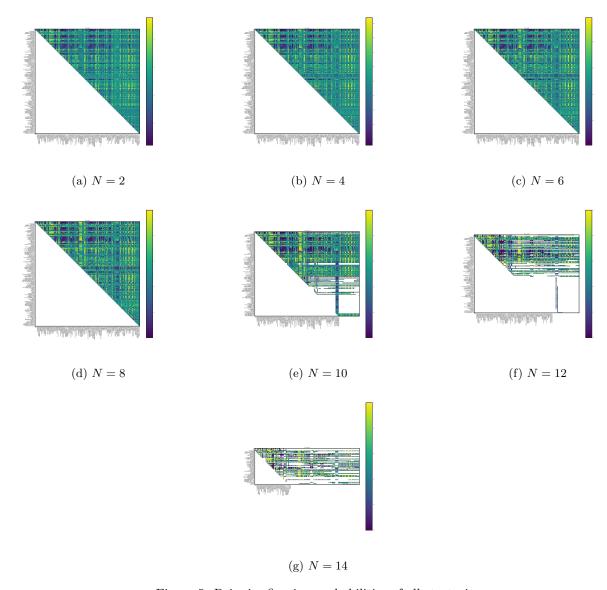


Figure 5: Pairwise fixation probabilities of all strategies

Player		2 4	6	8	10	12	14	
Predator	11.	0 2.0	2.0	2.0	2.0	2.0	1.0	
Handshake	13.	0 4.0	4.0	4.0	4.0	4.0	2.0	
CollectiveStrateg	gy 6.	0 1.0	1.0	1.0	1.0	1.0	3.0	
Prober 4	15.	0 3.0	3.0	3.0	3.0	3.0	4.0	
Hard Prober	82.	5 6.0	7.0	8.0	7.0	7.0	5.0	
Player	2	4	6		8	10	12	14
Hard Go By Majority	32.0	163.5	169.0	16	7.5	167.5	167.5	168.0
Hard Go By Majority: 5	32.0	163.5	165.5	16	7.5	167.5	167.5	169.0
Suspicious Tit For Tat	38.0	163.5	165.5	16	7.5	167.5	170.0	170.0
Opposite Grudger	140.0	167.0	171.0	17	1.0	171.0	170.0	171.0
SolutionB1	150.0	170.0	172.0	17	2.0	172.0	172.0	172.0

Table 3: Performance across population sizes of top and bottom performing strategies in population size N=14

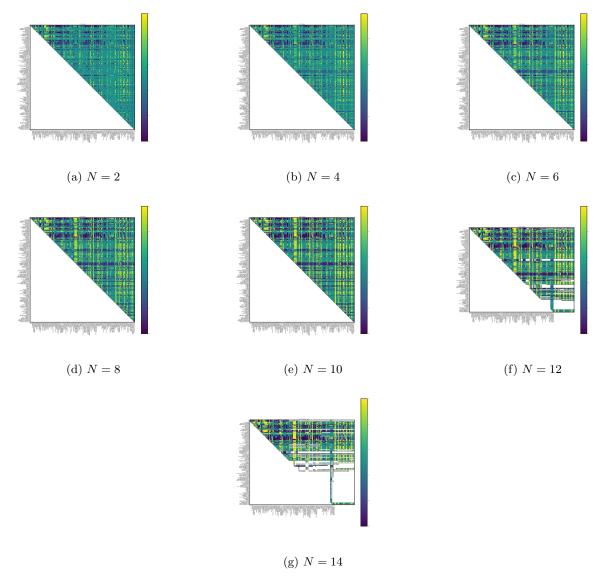


Figure 6: Pairwise fixation probabilities of all strategies (with noise)

Player				2	4	6	8	10	12	14
MEM2		1.0	16.0	23.5	30.0	30.0	9.0	10.0		
FSM P	Player: $[(0, 'C', 0, 'C'),$	(0, D',	3, 'C'	2.0	28.0	46.0	72.0	69.0	95.5	4.0
Retalia	ite 2: 0.08			3.5	19.5	44.0	44.5	39.0	42.5	56.5
Retalia	ite: 0.1			3.5	23.0	40.0	49.5	62.0	72.5	105.0
Predat	or			5.0	34.0	51.5	55.5	50.0	31.0	25.0
	Player	2	4	6		8	10	12	14	
	Arrogant QLearner	168.0	162.0	163.0	156.	.0 15	5.0 1	49.0	147.0	
	Cautious QLearner	170.0	158.0	165.0	157.	.0 157	7.0 1	58.0	143.0	
	Cooperator Hunter	170.0	157.0	146.0	144.	.0 144	4.0 13	36.0	160.0	
	Hesitant QLearner	170.0	162.0	164.0	158.	.0 158	8.0 14	45.0	144.0	
	Cycler CCCCCD	172.0	172.0	167.0	164.	.0 162	2.0 1	62.0	151.5	

Table 4: Performance across population sizes of top and bottom performing strategies in population size N=2 (with noise)

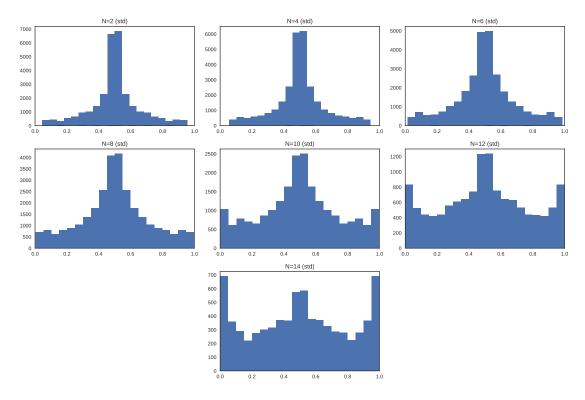


Figure 7: Distribution of fixation rates for all players

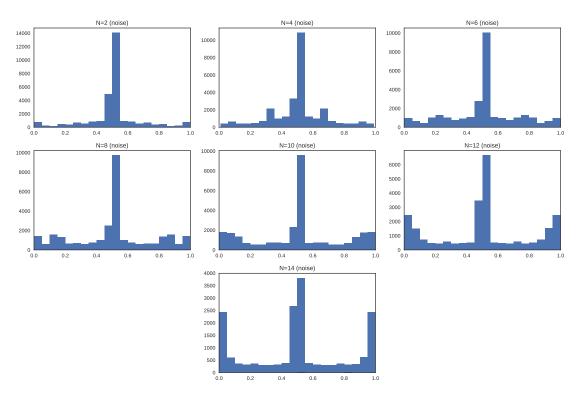


Figure 8: Distribution of fixation rates for all players (noise)

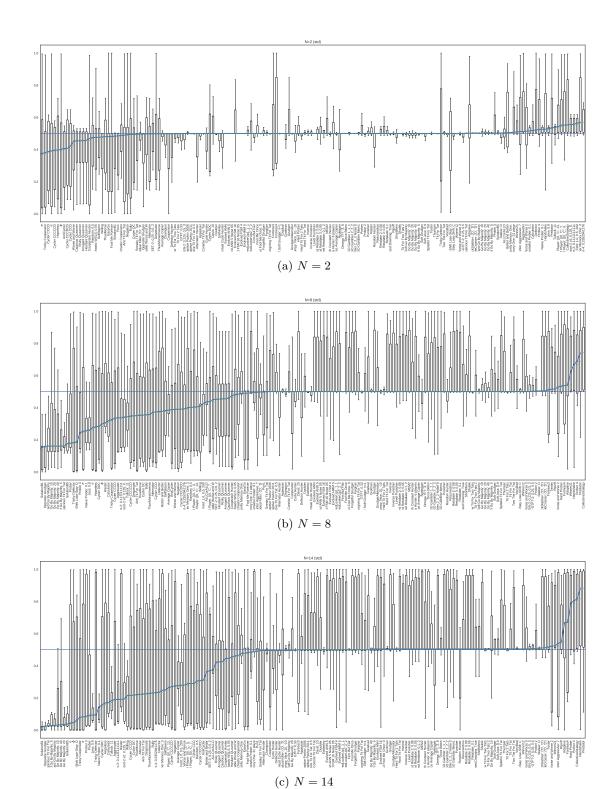


Figure 9: Fixation probabilities of all strategies

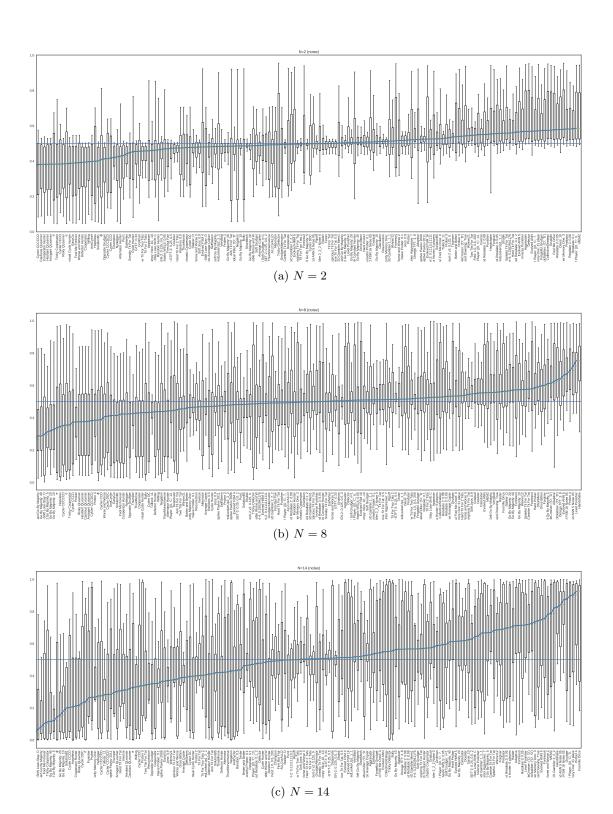


Figure 10: Fixation probabilities of all strategies (with noise) $\,$

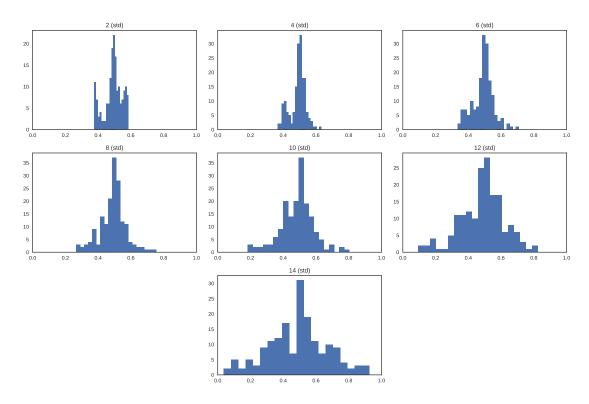


Figure 11: Distribution of median fixation rates for all players

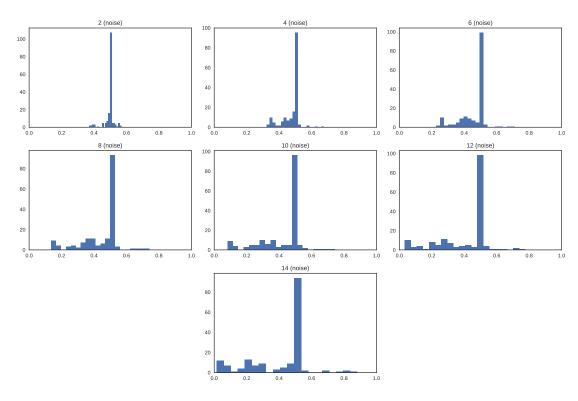


Figure 12: Distribution of median fixation rates for all players (noise)

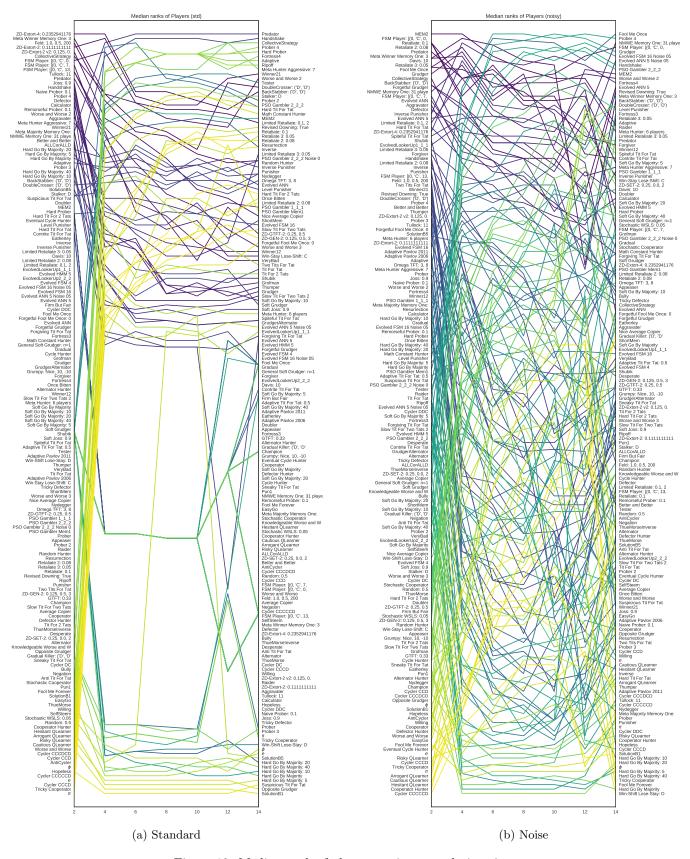


Figure 13: Median rank of players against population size

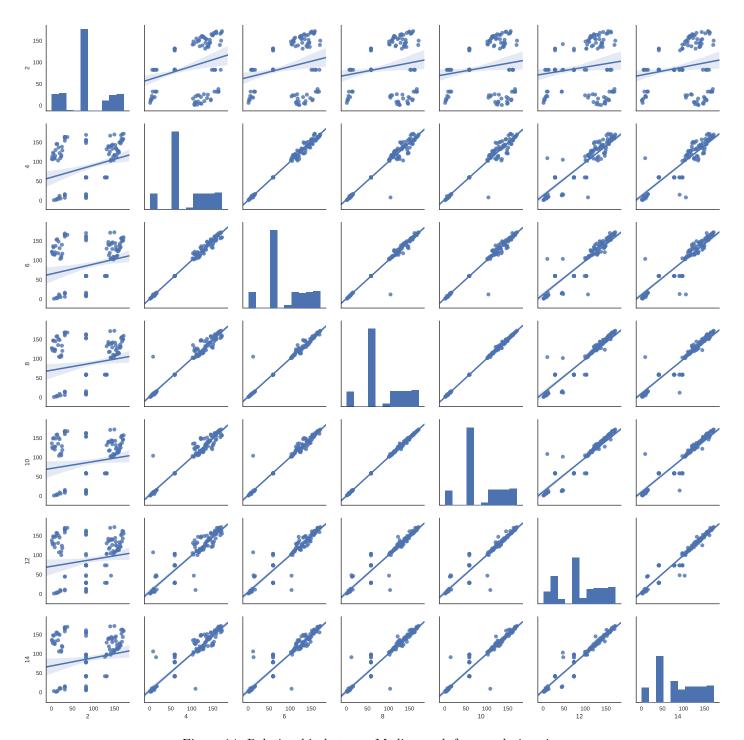


Figure 14: Relationship between Median rank for population size

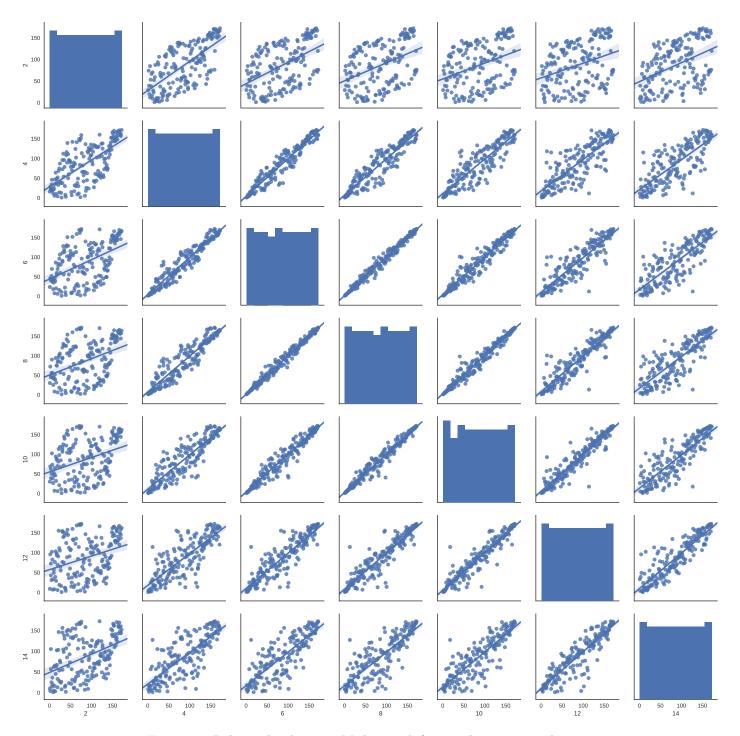


Figure 15: Relationship between Median rank for population size with noise

Play	ver			2	4	6	8	10	12	14
Fool	Me Once			9.0	11.5	18.0	25.0	26.5	33.0	1.0
Pro	per 4			39.0	3.0	3.0	4.0	5.0	4.0	2.0
NM	WE Memory One: 31 player	'S		14.0	47.0	38.5	39.0	46.0	39.0	3.0
FSN	I Player: [(0, 'C', 0, 'C'), (0.	, 'D', 3,	'C'	2.0	28.0	46.0	72.0	69.0	95.5	4.0
Gru	dger			10.5	21.5	41.0	41.0	52.0	49.0	5.0
•	Player	2	4		6	8	10	12	14	-
-	Hard Go By Majority: 40	71.0	149.0	169	.5 17	70.5	172.0	171.0	168.0	
	Tricky Cooperator	166.5	167.0	157	.0 16	62.0	163.0	167.0	169.0	
	Fool Me Forever	160.5	156.0	150	.0 14	16.0	141.0	153.0	170.0	
	Hard Go By Majority	76.0	159.0	172	.0 17	72.0	171.0	172.0	171.0	
	Win-Shift Lose-Stay: D	119.5	160.0	171	.0 17	70.5	170.0	166.0	172.0	

Table 5: Performance across population sizes of top and bottom performing strategies in population size N = 14 (with noise)

- More than two types in the population;
- Modified Moran processes (Fermi selection);
- Mutation;

Acknowledgements

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Memory Depth	2	4	6	8	10	12	14
9	11.00	2.00	2.00	2.00	2.00	2.00	1.00
$\frac{3}{2}$	82.50	59.50	59.50	58.50	58.50	28.50	41.50
6	82.50	59.50	59.50	58.50	58.50	28.50	41.50
12	82.50	59.50	59.50	58.50	58.50	73.50	41.50
4	82.50	35.25	33.75	32.75	31.75	39.25	42.00
16	82.50	59.50	59.50	58.50	58.50	73.50	59.75
∞	82.50	59.50	59.50	58.50	58.50	73.50	78.00
10	82.50	59.50	59.50	58.50	58.50	73.50	78.00
3	82.50	59.50	59.50	58.50	58.50	73.50	84.50
40	57.25	111.50	112.50	113.00	113.00	119.75	122.00
0	131.50	103.00	118.00	125.00	124.00	123.00	123.00
5	82.50	151.50	140.50	136.00	133.50	128.50	126.50
200	3.00	106.00	116.00	121.00	123.00	127.00	128.00
1	82.50	119.00	120.50	123.00	127.50	126.00	130.00
20	57.25	111.50	112.50	113.00	113.00	119.25	131.25
11	10.00	130.00	137.00	145.00	148.50	149.00	150.00
		(:	a) Standar	rd			
Memory Depth	2	4	6	8	10	12	14
9	5.00	34.00	51.50	55.50	50.00	31.0	25.00
16	57.75	51.25	51.50	37.50	44.25	31.5	39.50
4	89.25	60.50	65.50	63.00	63.75	73.0	43.75
6	103.00	85.00	74.00	68.00	60.00	41.0	52.00
10	106.00	40.50	47.00	52.00	64.50	76.5	70.00
∞	77.00	77.50	77.25	79.50	74.50	69.5	72.00
1	100.00	102.00	103.00	102.00	100.50	103.0	92.50
200	34.00	54.00	55.50	53.00	71.50	75.0	98.00
20	89.25	94.25	96.00	95.50	91.75	99.5	102.00
40	91.50	96.50	96.50	96.25	94.75	97.0	105.00
0	126.50	125.00	125.00	118.00	100.50	97.5	109.50
2	85.25	76.50	90.25	87.00	84.50	98.0	113.00
3	110.75	63.00	64.00	67.25	68.50	93.0	116.50
12	70.00	11.50	12.00	13.00	17.50	114.0	127.00
5	89.00	134.50	127.75	131.25	135.50	136.5	133.00
11	44.50	111.00	129.00	136.00	149.00	144.0	151.50

(b) Noisy

Table 6: Median rank by memory length

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A List of players

28. Cycler DC

1.	Adaptive	29. Cycler DDC	57.	Fortress3	
2.	Adaptive Tit For Tat: 0.5	30. Cycler CCCDCD	58.	Fortress4	
3.	Aggravater	31. Davis: 10	59.	GTFT: 0.33	
4.	ALLCorALLD	32. Defector	60.	General Soft $n=1,d=4,c=2$	Grudger:
5.	Alternator	33. Defector Hunter	61	Soft Go By Majority	
6.	Alternator Hunter	34. Desperate		Soft Go By Majority: 10	1
7.	AntiCycler	35. DoubleCrosser: ('D', 'D	')	Soft Go By Majority: 20	
8.	Anti Tit For Tat	36. Doubler		Soft Go By Majority: 40	
9.	Adaptive Pavlov 2006	37. EasyGo		Soft Go By Majority: 5	
10.	Adaptive Pavlov 2011	38. Eatherley	66.	, , , , , , , , , , , , , , , , , , ,	
11.	Appeaser	39. Eventual Cycle Hunter		Gradual	
12.	Arrogant QLearner	40. Evolved ANN	68.	Gradual Killer: ('D', 'D',	'D', 'D',
13.	Average Copier	41. Evolved ANN 5		'D', 'C', 'C')	
14.	Better and Better	42. Evolved ANN 5 Noise 0	6 9.	Grofman	
15.	BackStabber: ('D', 'D')	43. Evolved FSM 4	70.	Grudger	
16.	Bully	44. Evolved FSM 16	71.	GrudgerAlternator	
17.	Calculator	45. Evolved FSM 16 Noise ()5	Grumpy: Nice, 10, -10	
18.	Cautious QLearner	46. EvolvedLookerUp1_1_1		Handshake	
19.	Champion	47. EvolvedLookerUp2_2_2		Hard Go By Majority	
	CollectiveStrategy	48. Evolved HMM 5		Hard Go By Majority: 1	
	Contrite Tit For Tat	49. Feld: 1.0, 0.5, 200		Hard Go By Majority: 2	
	Cooperator	50. Firm But Fair		Hard Go By Majority: 4	
	Cooperator Hunter	51. Fool Me Forever		Hard Go By Majority: 5	
	Cycle Hunter	52. Fool Me Once		Hard Prober	
	Cycler CCCCCD	53. Forgetful Fool Me Once	0.05	Hard Tit For 2 Tats	
	Cycler CCCD	54. Forgetful Grudger	01.	Hard Tit For Tat	
	Cycler CCD	55. Forgiver		Hesitant QLearner	
41.	Cyclei COD	55. TOISIVEI	83.	Hopeless	

84. Inverse

56. Forgiving Tit For Tat

85.	Inverse Punisher	120. Retaliate 3:	0.05 155.	Worse and Worse	
86.	Joss: 0.9	121. Revised Dow	vning: True	Worse and Worse 2	
87.	Knowledgeable Worse and Worse	122. Ripoff	100.	Worse and Worse 2	
88.	Level Punisher	123. Risky QLear	rner 157.	Worse and Worse 3	
89.	Limited Retaliate: 0.1, 20	124. SelfSteem	158.	ZD-Extort-2: 0.1111111111111111,	
90.	Limited Retaliate 2: 0.08, 15	125. ShortMem		0.5	
91.	Limited Retaliate 3: $0.05, 20$	126. Shubik	159.	ZD-Extort-2 v2: 0.125, 0.5, 1	
92.	Math Constant Hunter	127. Slow Tit For			
93.	Naive Prober: 0.1	128. Slow Tit For	Two Tats 2 160.	ZD-Extort-4: 0.23529411764705882, 0.25, 1	
94.	MEM2	129. Sneaky Tit l			
95.	Negation	130. Soft Grudge	r 161.	ZD-GTFT-2: 0.25, 0.5	
96.	Nice Average Copier	131. Soft Joss: 0.	9 162.	ZD-GEN-2: 0.125, 0.5, 3	
97.	Nydegger	132. SolutionB1	163	ZD-SET-2: 0.25, 0.0, 2	
98.	Omega TFT: 3, 8	133. SolutionB5	103.	ZD-SE1-2. 0.20, 0.0, 2	
99.	Once Bitten	134. Spiteful Tit	For Tat 164.	e	
100.	Opposite Grudger	135. Stalker: D	165.	Meta Hunter: 6 players	
101.	π	136. Stochastic C	-		
102.	Predator	137. Stochastic W	VSLS: 0.05 166.	Meta Hunter Aggressive: 7 players	
103.	Prober	138. Suspicious T			
104.	Prober 2	139. Tester	167.	Meta Majority Memory One: 31 players	
105.	Prober 3	140. ThueMorse		pas, era	
106.	Prober 4	141. ThueMorseI	nverse 168.	Meta Winner Memory One: 31 players	
107.	Pun1	142. Thumper		F	
108.	PSO Gambler 1_1_1	143. Tit For Tat	169.	NMWE Memory One: 31 players	
109.	PSO Gambler 2_2_2	144. Tit For 2 Ta	its 170.	FSM Player: [(0, 'C', 7, 'C'), (0,	
110.	PSO Gambler 2_2_2 Noise 05	145. Tricky Coop	erator	'D', 1, 'C'), (1, 'C', 11, 'D'), (1, 'D', 11, 'D'), (2, 'C', 8, 'D'), (2,	
111.	PSO Gambler Mem1	146. Tricky Defec	etor	'D', 8, 'C'), (3, 'C', 3, 'C'), (3, 'D',	
112.	Punisher	147. Tullock: 11		12, 'D'), (4, 'C', 6, 'C'), (4, 'D', 3, 'C'), (5, 'C', 11, 'C'), (5, 'D',	
113.	Raider	148. Two Tits Fo	r Tat	8, 'D'), (6, 'C', 13, 'D'), (6, 'D', 14, 'C'), (7, 'C', 4, 'D'), (7, 'D',	
114.	Random: 0.5	149. VeryBad		2, 'D'), (8, 'C', 14, 'D'), (8, 'D',	
115.	Random Hunter	150. Willing		8, 'D'), (9, 'C', 0, 'C'), (9, 'D', 10, 'D'), (10, 'C', 8, 'C'), (10, 'D', 15,	
116.	Remorseful Prober: 0.1	151. Winner12		'C'), (11, 'C', 6, 'D'), (11, 'D', 5, 'D'), (12, 'C', 6, 'D'), (12, 'D', 9,	
117.	Resurrection	152. Winner21		'D'), (13, 'C', 9, 'D'), (13, 'D', 8,	
118.	Retaliate: 0.1	153. Win-Shift Lo	ose-Stay: D	'D'), (14, 'C', 8, 'D'), (14, 'D', 13, 'D'), (15, 'C', 4, 'C'), (15, 'D', 5,	
119.	Retaliate 2: 0.08	154. Win-Stay Lo	ose-Shift: C	'C')], 1, C	

- 171. FSM Player: [(0, 'C', 13, 'D'), (0, 'D', 12, 'D'), (1, 'C', 3, 'D'), (1, 'D', 4, 'D'), (2, 'C', 14, 'D'), (2, 'D', 9, 'D'), (3, 'C', 0, 'C'), (3, 'D', 1, 'D'), (4, 'C', 1, 'D'), (4, 'D', 2, 'D'), (5, 'C', 12, 'C'), (5, 'D', 6, 'C'), (6, 'C', 1, 'C'), (6, 'D', 14, 'D'), (7, 'C', 12, 'D'), (7, 'D', 2, 'D'), (8, 'C', 7, 'D'), (8, 'D', 9, 'D'), (8, 'C', 7, 'D'), (8, 'D', 9, 'D', 12, 'D', 12, 'D'), (8, 'D', 9, 'D', 12, 'D', 12, 'D'), (8, 'D', 9, 'D', 12, 'D', 12, 'D'), (8, 'D', 9, 'D', 12, 'D', 12, 'D'), (8, 'D', 9, 'D', 12, 'D', 12, 'D', 12, 'D'), (8, 'D', 9, 'D', 12, 'D', 12, 'D', 12, 'D', 12, 'D', 12, 'D', 12, 'D', 'D', 12, 'D', 12
- 'D'), (9, 'C', 8, 'D'), (9, 'D', 0, 'D'), (10, 'C', 2, 'C'), (10, 'D', 15, 'C'), (11, 'C', 7, 'D'), (11, 'D', 13, 'D'), (12, 'C', 3, 'C'), (12, 'D', 8, 'D'), (13, 'C', 7, 'C'), (13, 'D', 10, 'D'), (14, 'C', 10, 'D'), (14, 'D', 7, 'D'), (15, 'C', 15, 'C'), (15, 'D', 11, 'D')], 1, C
- 172. FSM Player: [(0, 'C', 0, 'C'), (0, 'D', 3, 'C'), (1, 'C', 5, 'D'), (1, 'D', 0, 'C'), (2, 'C', 3, 'C'), (2, 'D', 2, 'D'), (3, 'C', 4, 'D'), (3, 'D', 6, 'D'), (4, 'C', 3, 'C'), (4, 'D', 1, 'D'), (5, 'C', 6, 'C'), (5, 'D', 3, 'D'), (6, 'C', 6, 'D'), (6, 'D', 6, 'D'), (7, 'C', 7, 'D'), (7, 'D', 5, 'C')], 1, C