# A numerical study of fixation probabilities for strategies in the Iterated Prisoner's Dilemma

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#### Abstract

The Iterated Prisoner's Dilemma is a well established framework for the study of emergent behaviour. In this paper an extensive numerical study of the evolutionary dynamics of this framework are presented.

Fixation probabilities for Moran processes are obtained for 172 different strategies. This is done in both a standard 200 turn interaction and a noisy setting.

To the authors knowledge this is the largest such study. It allows for insights about the behaviour and performance of strategies with regard to their survival in an evolutionary setting.

## 1 Introduction

Since the formulation of the Moran Process in [10], this model of evolutionary population dynamics has been used to gain insights about the evolutionary stability of strategies in a number of settings. Similarly since the first Iterated Prisoner's Dilemma (IPD) tournament described in [2] the Prisoner's dilemma has been used to understand the evolution of cooperative behaviour in complex systems.

The analytical models of a Moran process are based on the relative fitness between two strategies and take this to be a fixed value r [12]. This is a valid model for simple strategies of the Prisoner's Dilemma such as to always cooperate or always defect. This manuscript provides a detailed numerical analysis of 172 complex and adaptive strategies for the IPD. In this case the relative fitness of a strategy is dependent on the population distribution.

Further deviations from the analytical model occur when interactions between players are subject to uncertainty. This is referred to as noise and has been considered in the IPD setting in [4, 11, 15]. Noise is also considered here.

This work provides answers to the following questions:

- 1. What strategies are good invaders?
- 2. What strategies are good at resisting invasion?
- 3. How does the population size affect these findings?

Figure 1 shows a diagrammatic representation of the Moran process. The Moran process is a stochastic birth death process on a finite population in which the population size stays constant over time. Individuals are **selected** according to a given fitness landscape. Once selected, a given individual is reproduced and similarly another individual is chosen to be removed from the population. In some settings mutation is also considered but without mutation (the case considered in this work) this process will arrive at an absorbing state where the population is entirely made up of a single individual. The probability with which a given strategy is the survivor is called the absorption probability. A more detailed analytic description of this is given in Section 3.

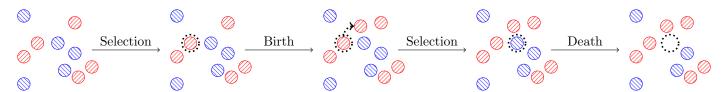


Figure 1: A diagrammatic representation of a Moran process

The Moran process was initially introduced in [10] in a genetic setting. It has sine been used in a variety of settings including the understanding of the spread of cooperative behaviour. However, as stated before, these mainly consider non sophisticated strategies. Some work has looked at evolutionary stability of strategies within the Prisoner's Dilemma [8]

but this is not done in the more widely used setting of the Moran process but in terms of infinite population stability. In [3] Moran processes are looked at in a theoretic framework for a small subset of strategies. In [7] machine learning techniques are used to train a strategy capable of resisting invasion and also invade any memory one strategy. Recent work [5] has investigated the effect of memory length on strategy performance and the emergence of cooperation but this is not done in Moran process context and only considers specific cases of memory 2 strategies.

The contribution of this work is a detailed and extensive analysis of absorption probabilities for 172 strategies. These strategies and the numerical simulations are from [13] which is an open source research library written for the study of the IPD. The strategies and simulation frameworks are automatically tested in accordance to best practice. The large number of strategies are available thanks to the open source nature of the project with over 40 contributions made by different programmers. Thus by considering Moran processes with population size greater than 2 we are taking in to account the effect of complex population dynamics. By considering sophisticated strategies we are taking in to effect the reputation of a strategy during each interaction.

Section 2 will explain the methodological approach used, Section 3 will validate the methodology by comparing simulated results to analytical results. The main results of this manuscript are presented in Section 4 which will present a detailed analysis of all the data generated. Finally, Section 5 will conclude and offer future avenues for the work presented here.

## 2 Methodology

To carry out this large numerical experiment 172 strategies are used from [13]. These include 169 default strategies in the library at the time (excluding strategies classified as having a long run time) as well as the following 3 finite state machine machine strategies [1]:

Appendix A shows all the players in question. More information about each player can be obtained in the documentation for [13]. The memory depth of the used strategies is shown in Table 1a.

Memory Depth	0	1	2	3	4	5	6	9	10	11	12	16	20	40	200	$\infty$
Count	3	31	12	8	2	6	1	1	5	1	1	2	2	2	1	94

(a) Memory depth

Stochastic	Count
False	123
True	49

(b) Stochastic versus deterministic

Table 1: Summary of properties of used strategies

All strategies are paired and these pairs are used in 2000 repetitions of a Moran process assuming a starting population of (N/2, N/2). This is repeated for even N between 2 and 14. The fixation probability is then estimated for each value of N.

Note that due to the high computational cost of these experiments, for any given interaction between two players within the Moran process the outcome is sampled from a pre computed cache of 1000 match outcomes. This is carried out using the approximate Moran process implemented in [13].

As an example, Figure 2 shows the scores between two players that over the 1000 outcomes gives 971 different scores. A variety of software libraries have been used in this work:

- The Axelrod library (IPD strategies and Moran processes) [13].
- The matplotlib library (visualisation) [6].
- The pandas and numpy libraries (data manipulation) [9, 14].

Section 3 will validate this approach against theoretic results.

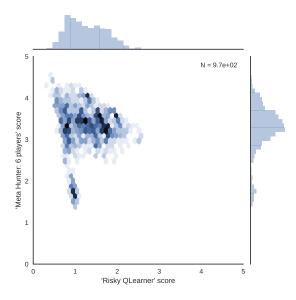


Figure 2: All possible scores for the pair of strategies that have the most different number of match outcomes

### 3 Validation

As described in [12] Consider the payoff matrix:

$$M = \begin{pmatrix} a, b \\ c, d \end{pmatrix} \tag{1}$$

The expected payoffs of i players of the first type in a population with N-i players of the second type are given by:

$$F_i = \frac{a(i-1) + b(N-i)}{N-1} \tag{2}$$

$$G_i = \frac{ci + d(N - i - 1)}{N - 1} \tag{3}$$

With an intensity of selection  $\omega$  the fitness of both strategies is given by:

$$f_i = 1 - \omega + \omega F_i \tag{4}$$

$$g_i = 1 - \omega + \omega G_i \tag{5}$$

The transitions within the birth death process that underpins the Moran process are then given by:

$$p_{i,i+1} = \frac{if_i}{if_i + (N-i)g_i} \frac{N-i}{N}$$
 (6)

$$p_{i,i-1} = \frac{(N-i)g_i}{if_i + (N-i)g_i} \frac{i}{N}$$
 (7)

$$p_{ii} = 1 - p_{i,i+1} - p_{i,i-1} \tag{8}$$

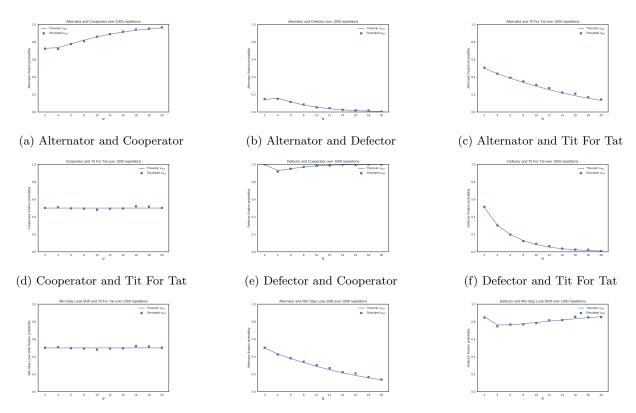
Using this it is a known result that the fixation probability of the first strategy in a population of i individuals of the first type (and N-i individuals of the second. We have:

$$x_{i} = \frac{1 + \sum_{j=1}^{i-1} \prod_{k=1}^{j} \gamma_{j}}{1 + \sum_{j=1}^{N-1} \prod_{k=1}^{j} \gamma_{j}}$$
(9)

where:

$$\gamma_j = \frac{p_{j,j-1}}{p_{j,j+1}}$$

Using this comparisons of  $x_{N/2}$  are shown in Figure 3. Note that these are all deterministic strategies and show a perfect match up between the expected value of (9) and the actual Moran process for all strategies pairs.



(g) Win Stay Lose Shift and Tit For Tat (h) Alternator and Win Stay Lose Shift (i) Defector and Win Stay Lose Shift

Figure 3: Comparison of theoretic and actual Moran Process fixation probabilities for **deterministic** strategies

Figure 4 shows the fixation probabilities for stochastic strategies. These are no longer a good match which highlights the weakness of the analytical formulae that relies on the average payoffs. A detailed analysis of the 172 strategies considered will be shown in the next Section.

#### 4 Numerical results

Figures 6 and ?? shows the fixation rates of each player on the y axis against each player on the x axis.

Figure ?? and ?? show the distribution of the fixation rates for all strategies.

Figure ?? and ?? show the distribution of the median fixation rates for all strategies.

Figures 13a and 13b show the median rank of each strategy against population size in the standard and noisy settings. Note that these ranks are not necessarily integers as group ties are given the average rank.

Tables 2a and 2b show the coefficients and  $R^2$  value of the linear model relating the rank in a particular sized population to the ranks in other populations sizes.

Tables 3, 4, 5 and 6 show the rankings across population size based for the top on bottom performers across the extreme population sizes.

Table 7 shows the performance based on memory length.

### 5 Conclusion

Further work:

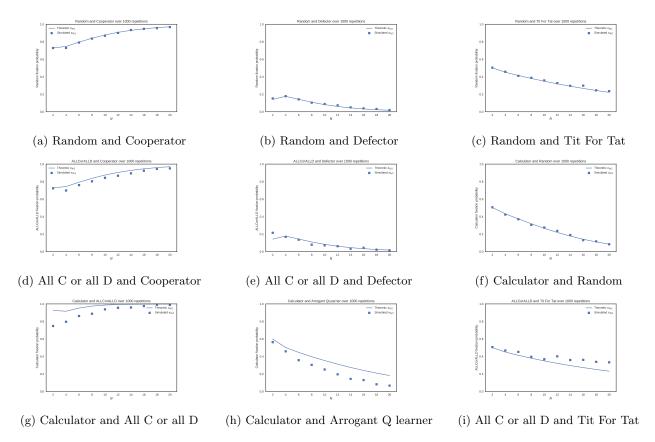


Figure 4: Comparison of theoretic and actual Moran Process fixation probabilities for stochastic strategies

	2	4	6	8	10	12	14	$R^2$		2	4	6	8	10	12	14	$R^2$
2	1.00	0.31	0.25	0.19	0.18	0.16	0.21	0.18	2	1.00	0.68	0.50	0.42	0.37	0.37	0.45	0.34
4	0.30	1.00	0.99	0.98	0.97	0.95	0.95	0.81	4	0.68	1.00	0.96	0.92	0.87	0.82	0.77	0.75
6	0.25	0.99	1.00	0.99	0.98	0.96	0.96	0.81	6	0.50	0.96	1.00	0.99	0.95	0.90	0.82	0.79
8	0.19	0.98	0.99	1.00	1.00	0.98	0.98	0.82	8	0.42	0.92	0.99	1.00	0.97	0.92	0.82	0.78
10	0.17	0.97	0.98	1.00	1.00	0.98	0.98	0.82	10	0.37	0.87	0.95	0.97	1.00	0.95	0.86	0.77
12	0.14	0.87	0.88	0.89	0.89	1.00	0.95	0.77	12	0.37	0.82	0.90	0.92	0.95	1.00	0.90	0.74
14	0.19	0.86	0.87	0.88	0.88	0.94	1.00	0.76	14	0.45	0.77	0.82	0.82	0.86	0.90	1.00	0.67

(a) Linear model coefficients for ranks without noise

(b) Linear model coefficients for ranks with noise

Table 2: Linear coefficients

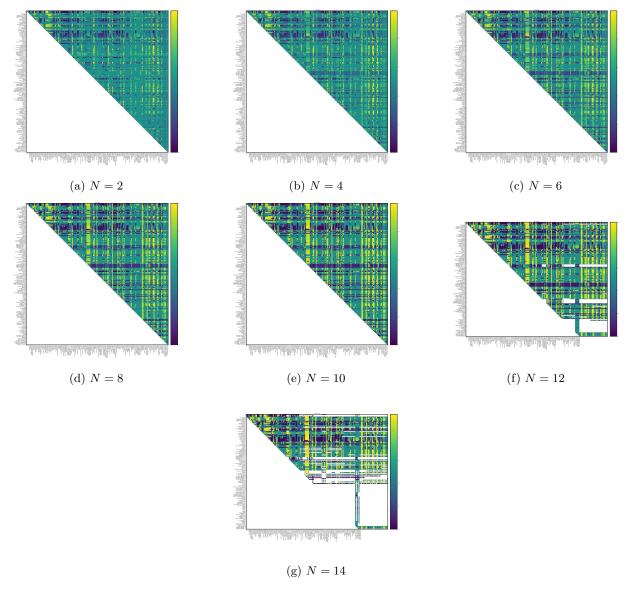
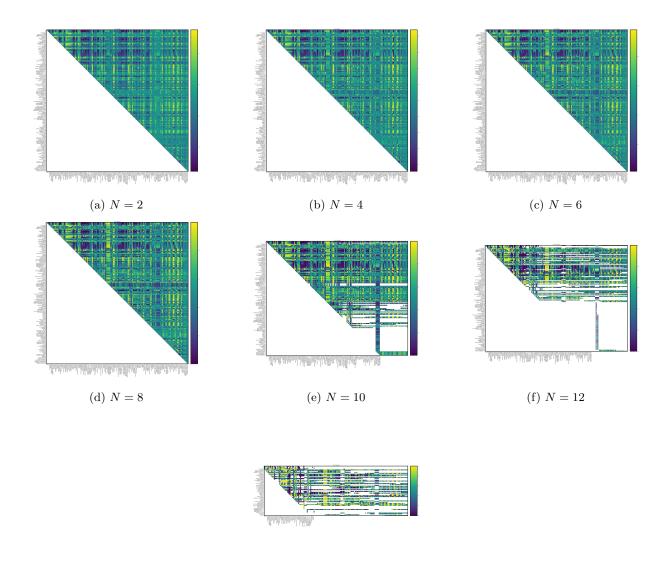


Figure 5: Pairwise fixation probabilities of all strategies

Player				2	4	6	8	3 1	10 12	14
ZD-Extor	ZD-Extort-4: 0.23529411764705882, 0.25, 1					122.0	127.0	136	.0 141.0	129.0
Meta Winner Memory One: 31 players				2.0 113	3.5	120.5	126.0	126	.0 133.0	132.0
Feld: 1.0,	0.5, 200		3	3.0 10	6.0	116.0	121.0	123	.0 127.0	128.0
ZD-Extor	rt-2: 0.1111111111111	111, 0.5	4	1.0	3.0	136.0	147.0	148	.5 148.0	146.0
ZD-Extor	ZD-Extort-2 v2: 0.125, 0.5, 1			5.0 12	1.0	133.0	146.0	150	.0 149.0	147.0
	Player	2	4	6		8	10	12	14	
	Cycler CCCCCD	168.0	153.0	149.0	14	4.0 1	37.0	135.0	133.0	
	$e^{}$	169.0	171.0	158.0	150	6.0 1	56.0	161.0	163.0	
	Cycler CCCD 170.0 Tricky Cooperator 171.0		157.0	150.0	14	9.0 1	45.0	143.0	144.5	
			158.5	152.0	150	0.0 - 1	46.0	156.0	155.0	
	$\pi$	172.0	172.0	159.0	159	9.0 1	57.0	155.0	152.0	

Table 3: Performance across population sizes of top and bottom performing strategies in population size N=2



(g) N = 14

Figure 6: Pairwise fixation probabilities of all strategies (with noise)

Player	2	2 4	6	8	10	12	14	
Predator	11.0	2.0	2.0	2.0	2.0	2.0	1.0	
Handshake	13.0	4.0	4.0	4.0	4.0	4.0	2.0	
CollectiveStrates	gy 6.0	1.0	1.0	1.0	1.0	1.0	3.0	
Prober 4	15.0	3.0	3.0	3.0	3.0	3.0	4.0	
Hard Prober	82.5	6.0	7.0	8.0	7.0	7.0	5.0	
Player	2	4	(	3	8	10	12	14
Hard Go By Majority: 10	32.0	163.5	165.5	5 16	7.5	167.5	164.0	168.0
Hard Go By Majority: 5	32.0	163.5	165.5	5 16	7.5	167.5	167.5	169.0
Suspicious Tit For Tat	38.0	163.5	165.5	5 16	7.5	167.5	170.0	170.0
Opposite Grudger	140.0	167.0	171.0	) 17	1.0	171.0	170.0	171.0
SolutionB1	150.0	170.0	172.0	) 17	2.0	172.0	172.0	172.0

Table 4: Performance across population sizes of top and bottom performing strategies in population size N=14

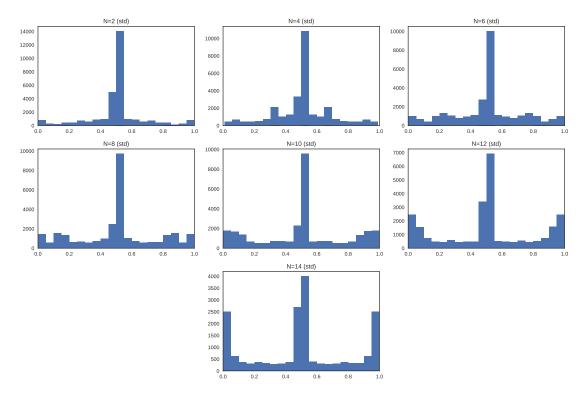


Figure 7: Distribution of fixation rates for all players

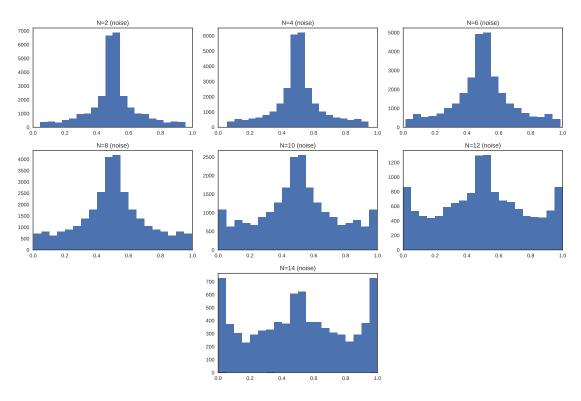


Figure 8: Distribution of fixation rates for all players (noise)

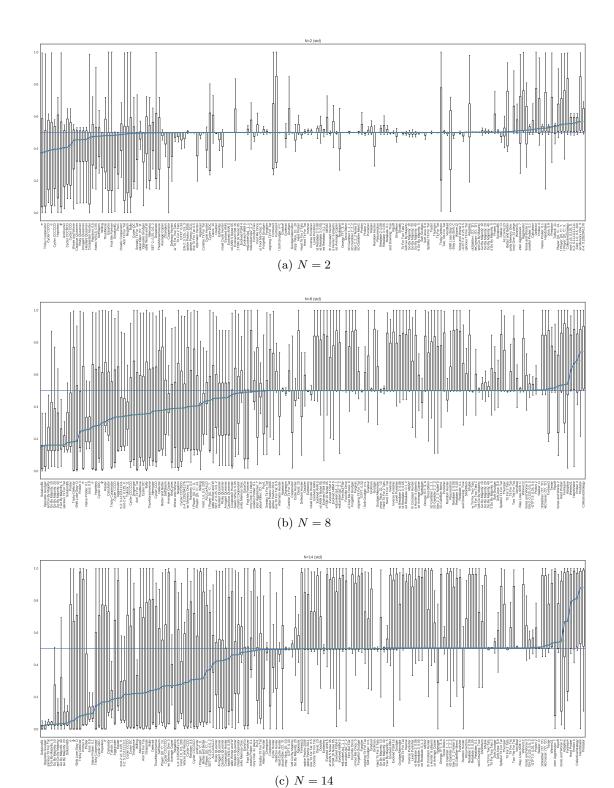


Figure 9: Fixation probabilities of all strategies

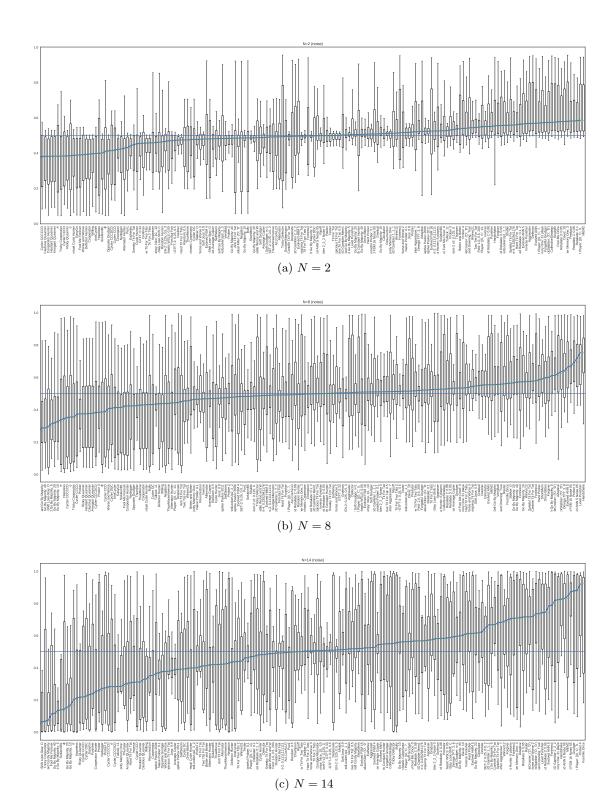


Figure 10: Fixation probabilities of all strategies (with noise)

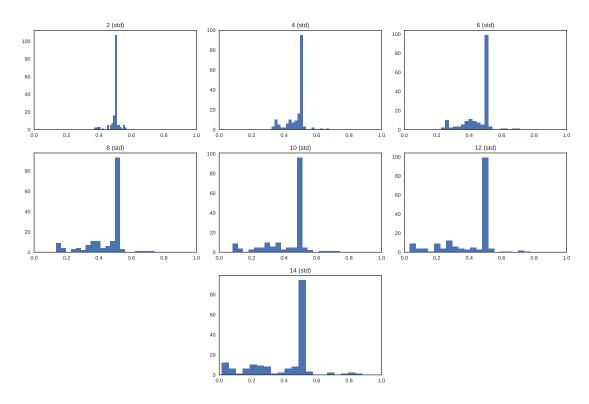


Figure 11: Distribution of median fixation rates for all players

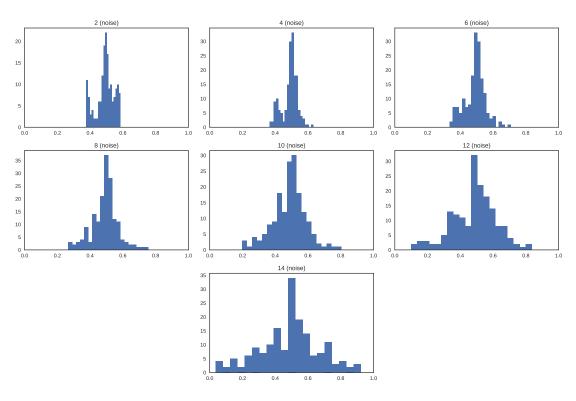


Figure 12: Distribution of median fixation rates for all players (noise)

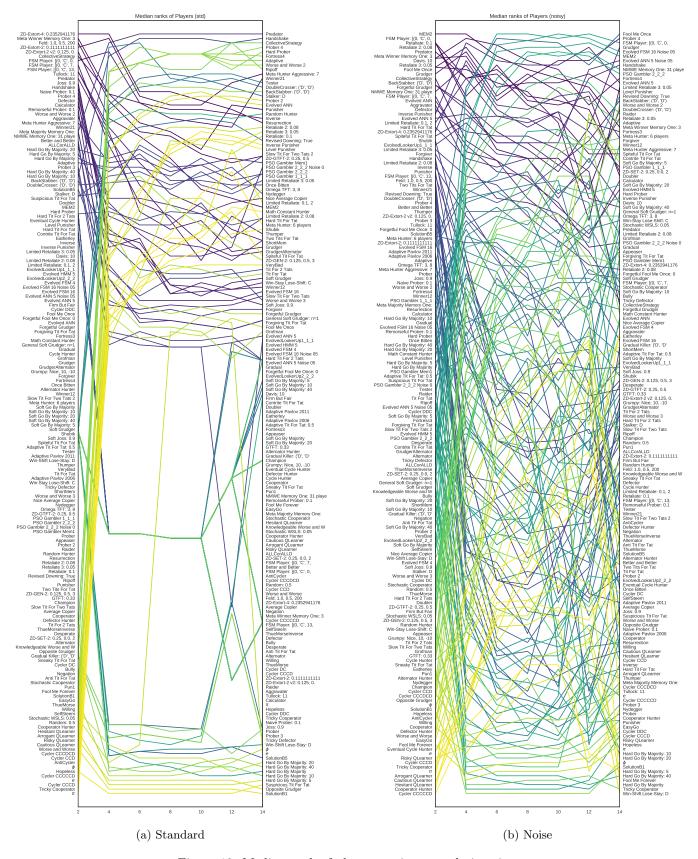


Figure 13: Median rank of players against population size

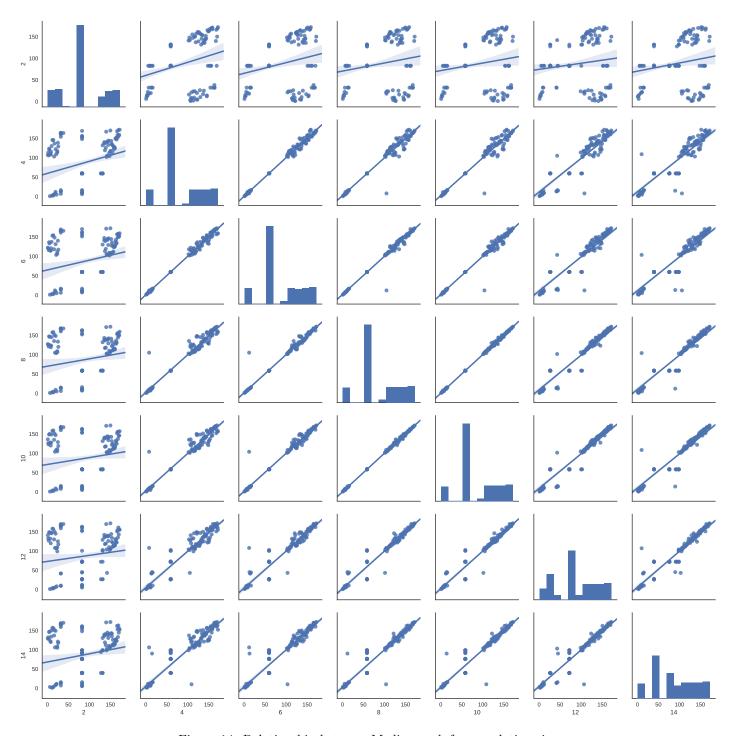


Figure 14: Relationship between Median rank for population size

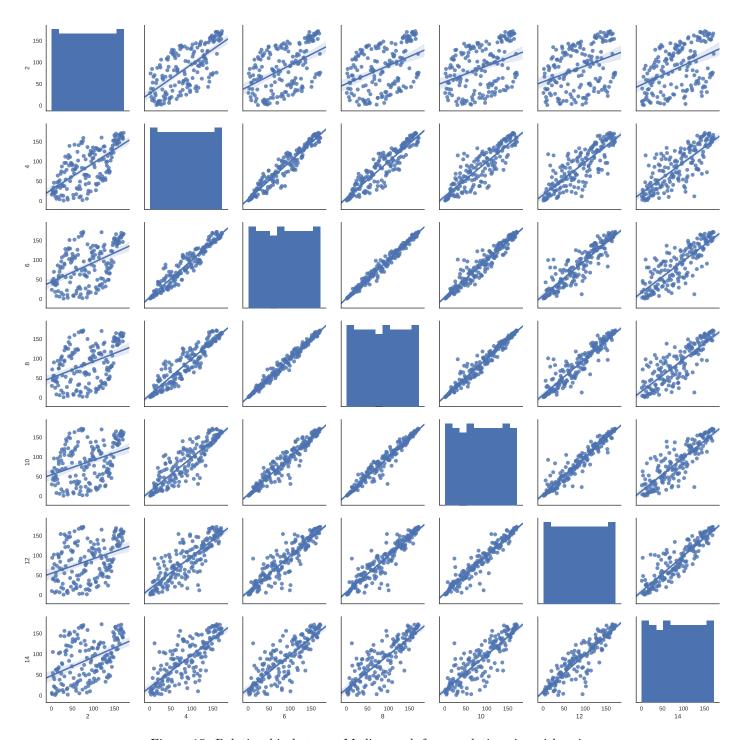


Figure 15: Relationship between Median rank for population size with noise

Player				2	4	6	8	10	12	14
MEM2				1.0	16.0	23.5	30.0	30.0	10.0	6.0
FSM Player: [(0, 'C', 0, 'C'), (0, 'D', 3, 'C'					28.0	46.0	72.0	63.0	94.0	3.0
Retalia	Retaliate 2: 0.08					44.0	44.5	42.0	40.0	54.0
Retalia	Retaliate: 0.1					40.0	49.5	61.0	68.0	105.0
Predate	Predator					51.5	55.5	47.5	42.0	45.0
	Player	2	4	6		8	10	12	14	
	Arrogant QLearner	168.0	162.0	163.0	156.	.0 15	3.0 1	45.0	145.0	
	Cautious QLearner	170.0	158.0	165.0	157.	.0 150	3.0   1	58.0	140.0	
	Cooperator Hunter	Cooperator Hunter 170.0 157.0		146.0	144.	0 - 144	4.0 1	37.0	155.0	
	Hesitant QLearner	170.0	162.0	164.0	158.	0 - 15	7.0   1	55.0	141.0	
	Cycler CCCCCD	172.0	172.0	167.0	164.	.0 165	2.0 1	60.0	151.0	

Table 5: Performance across population sizes of top and bottom performing strategies in population size N=2 (with noise)

Player			2	4	6	8	10	12	14
Fool Me Once			9.0	11.5	18.0	25.0	27.5	36.0	1.0
Prober 4			39.0	3.0	3.0	4.0	4.0	5.0	2.0
FSM Player: $[(0, 'C', 0, 'C'), (0, 'C')]$	'D', 3,	$^{\prime}\mathrm{C}^{\prime}$	2.0	28.0	46.0	72.0	63.0	94.0	3.0
Grudger			10.5	21.5	41.0	41.0	52.5	48.0	4.0
Evolved FSM 16 Noise 05			66.5	9.0	5.0	5.0	5.0	3.0	5.0
Player	2	4		6	8	10	12	14	-
Hard Go By Majority: 40	71.0	149.0	169	.5 17	0.5	172.0	171.0	168.0	_
Fool Me Forever	160.5	156.0	150	.0 14	6.0	141.0	151.0	169.0	
Hard Go By Majority	76.0	159.0	172	.0 17	2.0	171.0	172.0	170.0	
Tricky Cooperator	166.5	167.0	157	.0 16	32.0	166.0	166.0	171.0	
Win-Shift Lose-Stay: D	119.5	160.0	171	.0 17	0.5	170.0	165.0	172.0	

Table 6: Performance across population sizes of top and bottom performing strategies in population size N=14 (with noise)

Memory Depth	2	4	6	8	10	12	14
9	11.00	2.00	2.00	2.00	2.00	2.0	1.00
2	82.50	59.50	59.50	58.50	58.50	26.5	39.50
6	82.50	59.50	59.50	58.50	58.50	26.5	39.50
12	82.50	59.50	59.50	58.50	58.50	72.0	39.50
4	82.50	35.25	33.75	32.75	31.75	38.5	41.00
16	82.50	59.50	59.50	58.50	58.50	72.0	57.75
$\infty$	82.50	59.50	59.50	58.50	58.50	72.0	76.00
10	82.50	59.50	59.50	58.50	58.50	72.0	76.00
3	82.50	59.50	59.50	58.50	58.50	72.0	83.00
40	57.25	111.50	112.50	113.00	113.00	119.0	121.00
0	131.50	103.00	118.00	125.00	124.00	121.0	125.50
200	3.00	106.00	116.00	121.00	123.00	127.0	128.00
5	82.50	151.50	140.50	136.00	133.50	129.0	128.50
20	57.25	111.50	112.50	113.00	113.00	118.5	128.75
1	82.50	119.00	120.50	123.00	127.50	126.0	129.00
11	10.00	130.00	137.00	145.00	148.50	147.0	150.00
		(:	a) Standa	rd			
Memory Depth	2	4	6	8	10	12	14
16	57.75	51.25	51.50	37.50	45.00	31.00	37.75
4	89.25	60.50	65.50	63.00	65.00	59.50	38.75
9	5.00	34.00	51.50	55.50	47.50	42.00	45.00
6	103.00	85.00	74.00	68.00	58.50	41.00	56.00
10	106.00	40.50	47.00	52.00	66.50	74.00	72.00
$\infty$	77.00	77.50	77.25	79.50	74.75	68.00	73.50
1	100.00	102.00	103.00	102.00	101.50	103.00	95.00
200	34.00	54.00	55.50	53.00	71.00	73.00	99.00
20	89.25	94.25	96.00	95.50	93.50	101.00	99.50
0	126.50	125.00	125.00	118.00	90.00	99.00	101.50
40	91.50	96.50	96.50	96.25	96.00	97.00	104.00
2	85.25	76.50	90.25	87.00	83.25	99.00	108.00
3	110.75	63.00	64.00	67.25	68.00	106.25	116.00
12	70.00	11.50	12.00	13.00	23.00	92.00	126.00
5	89.00	134.50	127.75	131.25	135.00	136.00	133.25
11	44.50	111.00	129.00	136.00	147.50	147.00	148.50

(b) Noisy

Table 7: Median rank by memory length

- Spatial structure;
- More than two types in the population;
- Modified Moran processes (Fermi selection);
- Mutation;

## Acknowledgements

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## A List of players

1. Adaptive 36. Doubler 69. Grofman 70. Grudger 2. Adaptive Tit For Tat: 0.5 37. EasyGo 71. GrudgerAlternator 3. Aggravater 38. Eatherlev 72. Grumpy: Nice, 10, -10 4. ALLCorALLD 39. Eventual Cycle Hunter 73. Handshake 5. Alternator 40. Evolved ANN 74. Hard Go By Majority 6. Alternator Hunter 41. Evolved ANN 5 75. Hard Go By Majority: 10 7. AntiCycler 42. Evolved ANN 5 Noise 05 76. Hard Go By Majority: 20 8. Anti Tit For Tat 43. Evolved FSM 4 77. Hard Go By Majority: 40 9. Adaptive Pavlov 2006 44. Evolved FSM 16 78. Hard Go By Majority: 5 10. Adaptive Pavlov 2011 45. Evolved FSM 16 Noise 05 79. Hard Prober 11. Appeaser 46. EvolvedLookerUp1\_1\_1 80. Hard Tit For 2 Tats 12. Arrogant QLearner 47. EvolvedLookerUp2\_2\_2 81. Hard Tit For Tat 13. Average Copier 48. Evolved HMM 5 82. Hesitant QLearner 14. Better and Better 83. Hopeless 49. Feld: 1.0, 0.5, 200 15. BackStabber: ('D', 'D') 84. Inverse 50. Firm But Fair 16. Bully 85. Inverse Punisher 51. Fool Me Forever 17. Calculator 86. Joss: 0.9 52. Fool Me Once 87. Knowledgeable Worse and Worse 18. Cautious QLearner 53. Forgetful Fool Me Once: 0.05 88. Level Punisher 19. Champion 54. Forgetful Grudger 89. Limited Retaliate: 0.1, 20 20. CollectiveStrategy 55. Forgiver 90. Limited Retaliate 2: 0.08, 15 21. Contrite Tit For Tat 56. Forgiving Tit For Tat 91. Limited Retaliate 3: 0.05, 20 22. Cooperator 57. Fortress3 92. Math Constant Hunter 23. Cooperator Hunter 58. Fortress4 93. Naive Prober: 0.1 24. Cycle Hunter 59. GTFT: 0.33 94. MEM2 25. Cycler CCCCCD 95. Negation 60. General Soft Grudger: 26. Cycler CCCD n=1,d=4,c=296. Nice Average Copier 27. Cycler CCD 61. Soft Go By Majority 97. Nydegger 28. Cycler DC 62. Soft Go By Majority: 10 98. Omega TFT: 3, 8 29. Cycler DDC 63. Soft Go By Majority: 20 99. Once Bitten 30. Cycler CCCDCD 64. Soft Go By Majority: 40 100. Opposite Grudger 31. Davis: 10 101.  $\pi$ 65. Soft Go By Majority: 5 32. Defector 102. Predator  $66. \phi$ 33. Defector Hunter 103. Prober 67. Gradual 34. Desperate 104. Prober 2 68. Gradual Killer: ('D', 'D', 'D', 'D', 35. DoubleCrosser: ('D', 'D') 'D', 'C', 'C') 105. Prober 3

- 106. Prober 4
- 107. Pun1
- 108. PSO Gambler  $1_{-}1_{-}1$
- 109. PSO Gambler 2\_2\_2
- 110. PSO Gambler 2\_2\_2 Noise 05
- 111. PSO Gambler Mem1
- 112. Punisher
- 113. Raider
- 114. Random: 0.5
- 115. Random Hunter
- 116. Remorseful Prober: 0.1
- 117. Resurrection
- 118. Retaliate: 0.1
- 119. Retaliate 2: 0.08
- 120. Retaliate 3: 0.05
- 121. Revised Downing: True
- 122. Ripoff
- 123. Risky QLearner
- 124. SelfSteem
- 125. ShortMem
- 126. Shubik
- 127. Slow Tit For Two Tats
- 128. Slow Tit For Two Tats 2
- 129. Sneaky Tit For Tat
- 130. Soft Grudger
- 131. Soft Joss: 0.9
- 132. SolutionB1
- 133. SolutionB5
- 134. Spiteful Tit For Tat
- 135. Stalker: D
- 136. Stochastic Cooperator
- 137. Stochastic WSLS: 0.05

- 138. Suspicious Tit For Tat
- 139. Tester
- 140. ThueMorse
- 141. ThueMorseInverse
- 142. Thumper
- 143. Tit For Tat
- 144. Tit For 2 Tats
- 145. Tricky Cooperator
- 146. Tricky Defector
- 147. Tullock: 11
- 148. Two Tits For Tat
- 149. VeryBad
- 150. Willing
- 151. Winner12
- 152. Winner21
- 153. Win-Shift Lose-Stay: D
- 154. Win-Stay Lose-Shift: C
- 155. Worse and Worse
- 156. Worse and Worse 2
- 157. Worse and Worse 3
- 158. ZD-Extort-2: 0.1111111111111111, 0.5
- 159. ZD-Extort-2 v2: 0.125, 0.5, 1
- 160. ZD-Extort-4: 0.23529411764705882, 0.25, 1
- 161. ZD-GTFT-2: 0.25, 0.5
- 162. ZD-GEN-2: 0.125, 0.5, 3
- 163. ZD-SET-2: 0.25, 0.0, 2
- 164. e
- 165. Meta Hunter: 6 players
- 166. Meta Hunter Aggressive: 7 players

- 167. Meta Majority Memory One: 31 players
- 168. Meta Winner Memory One: 31 players
- 169. NMWE Memory One: 31 players
- 170. FSM Player: [(0, 'C', 7, 'C'), (0, 'D', 1, 'C'), (1, 'C', 11, 'D'), (1, 'D', 11, 'D'), (2, 'C', 8, 'D'), (2, 'D', 8, 'C'), (3, 'C', 3, 'C'), (3, 'D', 12, 'D'), (4, 'C', 6, 'C'), (4, 'D', 3, 'C'), (5, 'C', 11, 'C'), (5, 'D', 8, 'D'), (6, 'C', 13, 'D'), (6, 'D', 14, 'C'), (7, 'C', 4, 'D'), (7, 'D', 2, 'D'), (8, 'C', 14, 'D'), (8, 'D', 8, 'D'), (9, 'C', 0, 'C'), (9, 'D', 10, 'D'), (10, 'C', 8, 'C'), (10, 'D', 15, 'C'), (11, 'C', 6, 'D'), (11, 'D', 5, 'D'), (12, 'C', 6, 'D'), (12, 'D', 9, 'D'), (13, 'C', 9, 'D'), (13, 'D', 8, 'D'), (14, 'C', 8, 'D'), (14, 'D', 13, 'D'), (15, 'C', 4, 'C'), (15, 'D', 5, 'C')], 1, C
- 171. FSM Player: [(0, 'C', 13, 'D'), (0, 'D', 12, 'D'), (1, 'C', 3, 'D'), (1, 'D', 4, 'D'), (2, 'C', 14, 'D'), (2, 'D', 9, 'D'), (3, 'C', 0, 'C'), (3, 'D', 1, 'D'), (4, 'C', 1, 'D'), (4, 'D', 2, 'D'), (5, 'C', 12, 'C'), (5, 'D', 6, 'C'), (6, 'C', 1, 'C'), (6, 'D', 14, 'D'), (7, 'C', 12, 'D'), (7, 'D', 2, 'D'), (8, 'C', 7, 'D'), (8, 'D', 9, 'D'), (9, 'C', 8, 'D'), (9, 'D', 0, 'D'), (10, 'C', 2, 'C'), (10, 'D', 15, 'C'), (11, 'C', 7, 'D'), (11, 'D', 13, 'D'), (12, 'C', 3, 'C'), (12, 'D', 8, 'D'), (13, 'C', 7, 'C'), (13, 'D', 10, 'D'), (14, 'C', 10, 'D'), (14, 'D', 7, 'D'), (15, 'C', 15, 'C'), (15, 'D', 11, 'D')], 1, C
- 172. FSM Player: [(0, 'C', 0, 'C'), (0, 'D', 3, 'C'), (1, 'C', 5, 'D'), (1, 'D', 0, 'C'), (2, 'C', 3, 'C'), (2, 'D', 2, 'D'), (3, 'C', 4, 'D'), (3, 'D', 6, 'D'), (4, 'C', 3, 'C'), (4, 'D', 1, 'D'), (5, 'C', 6, 'C'), (5, 'D', 3, 'D'), (6, 'C', 6, 'D'), (6, 'D', 6, 'D'), (7, 'C', 7, 'D'), (7, 'D', 5, 'C')], 1, C