

### 9.3.4 Other Shit

#### 9.3.4.1 Worm Gears *\*Using Mott*

Some useful Shit:

$N_G$  = Number of teeth on the gear

$N_W$  = Number of worm threads

$D_G$  = pitch diameter of the gear (in)

$D_W$  = Pitch diameter of the worm

$p$  = circular pitch (in)

$P_d$  = diametral pitch (teeth/inch)

$m$  = module

$L$  = Lead angle

$C$  = Center distance (in)

$\phi_n$  = Normal pressure angle

$\phi_t$  = transverse pressure angle

$a$  = addendum (in)

$h_t$  = whole depth (in)

$h_k$  = working depth (in)

$b$  = dedendum (in)

$D_{rW}$  = Root diameter of worm (in)

$D_{oW}$  = Outside diameter of worm (in)

$D_{rG}$  = Root Diameter of gear (in)

$F_G$  = Face width of wormgear (in)

$F_W$  = face length of worm (in)

$n_W$  = speed of worm (rpm)

$n_G$  = speed of gear (rpm)

$\nu_{tW}$  = Pitch line speed for worm (ft/min)

$\nu_{tG}$  = Pitch line speed for gear (ft/min)

$VR$  = Velocity ratio

Now for some of the formulae to solve for these values:

$$\text{circular pitch: } p = \frac{\pi D_G}{N_G}$$

$$\text{diametral pitch: } P_d = \frac{N_G}{D_G} \text{ or } P_d = \frac{\pi}{p}$$

$$\text{module: } m = \frac{D}{N}$$

$$\text{axial pitch: } P_x = p$$

$$\text{lead: } L = N_W P_x$$

$$\text{lead angle: } \tan(\lambda) = \frac{L}{\pi D_W}$$

$$\text{center distance: } C = \frac{D_W + D_G}{2} = \frac{N_W + N_G}{2 P_d}$$

$$\text{angle relationship: } \tan \phi_n = \tan(\phi_t) \cos(\lambda)$$

$$\text{addendum: } a = 0.318 P_x = \frac{1}{P_d}$$

$$\text{whole depth: } h_t = 0.6866 P_x = \frac{2.157}{P_d}$$

$$\text{working depth: } h_k = 2a$$

$$\text{dedendum: } b = h_t - a$$

$$\text{root diameter of worm: } D_{rW} = D_W - 2b$$

$$\text{outside diameter of worm: } D_oW = D_W + 2a = D_W + h_k$$

$$\text{root diameter of gear: } D_rG = D_G - 2b$$

$$\text{throat diameter of gear: } D_t = D_G + 2a$$

$$\text{face width of wormgear: } F_G = \sqrt{D_{oW}^2 - D_W^2} = 2p \approx \frac{6}{P_d}$$

$$\text{face length of worm: } F_W = 2\sqrt{\left(\frac{D_t}{2}\right)^2 - \left(\frac{D_G}{2-a}\right)^2}$$

**Speed:**

- pitch line speed for worm:  $\nu_{tW} = \frac{\pi D_W n_W}{12}$  lb-ft or  $\nu_{tW} = \frac{\pi D_W n_W}{60000}$  m/s
- pitch line speed for gear:  $\nu_{tG} = \frac{\pi D_G n_G}{12}$  lb-ft or  $\nu_{tW} = \frac{\pi D_G n_G}{60000}$  m/s
- Velocity Ratio:  $VR = \frac{n_W}{n_G} = \frac{N_G}{N_W}$
- Sliding speed:  $\nu_s = \frac{\nu_{tG}}{\sin(\lambda)} = \frac{\nu_{tW}}{\cos(\lambda)}$

**Forces:**

- Force relationship:  $W_{tG} = W_{xW}$ ,  $W_{xG} = W_{tW}$ ,  $W_{rG} = W_{rW}$
- output torque:  $T_o = \frac{63000 P_o}{n_G} = \frac{W_{tG} D_G}{2}$
- transmitted force:  $W_{tG} = \frac{2T_o}{D_G}$
- axial force:  $W_{xG} = W_{tG} \frac{\cos(\phi_n) \sin(\lambda) + \mu \cos(\lambda)}{\cos(\phi_n) \cos(\lambda) - \mu \sin(\lambda)}$
- radial force:  $W_{rG} = \frac{W_{tG} \sin(\phi_n)}{\cos(\phi_n) \cos(\lambda) - \mu \sin(\lambda)}$
- friction force:  $W_f = \frac{\mu W_{tG}}{\cos(\lambda) \cos(\phi_n) - \mu \sin(\lambda)}$
- power loss due to friction:  $P_L = \frac{\nu_s W_f}{33000}$
- input power:  $P_i = P_o + P_L$
- $\eta = \frac{P_o}{P_i} = \frac{\cos(\phi_n) - \mu \tan(\lambda)}{\cos(\phi_n) + \frac{\mu}{\tan(\lambda)}}$

**Now design selection for worm gears:**

1. Calculate the lead  $L$  and the lead angle  $\lambda$

$$p = \frac{\pi}{P_d} = \frac{\pi D_G}{N_G}$$

$$P_x = p$$

$$L = N_W P_x$$

$$\lambda = \arctan\left(\frac{L}{\pi D_W}\right)$$

2. Find Center Distance  $CD$

$$CD = \frac{D_G + D_W}{2}$$

3. Calculate the pitch line speed of the gear

$$\nu_{tG} = \frac{\pi D_G n_G}{12}$$

4. Calculate the sliding speed

$$\nu_s = \frac{\nu_{tG}}{\sin(\lambda)} = \frac{\nu_{tW}}{\cos(\lambda)}$$

5. Calculate the coefficient of friction:

$$\mu = \begin{cases} 0.15 & , \nu = 0 \\ 0.124e^{-0.074\nu_s^{0.645}} & , 0 < \nu_s < 10 \\ 0.103e^{-0.11\nu_s^{0.45}} + 0.012 & , \nu_s > 10 \end{cases}$$

6. Find the forces on the gear:

$$\begin{aligned} T_o &= \frac{63000P_o}{n_G} = \frac{W_{tG}D_G}{2} \\ W_{tG} &= \frac{2T_o}{D_G} \\ W_{xG} &= W_{tG} \frac{\cos(\phi_n) \sin(\lambda) + \mu \cos(\lambda)}{\cos(\phi_n) \cos(\lambda) - \mu \sin(\lambda)} \\ W_{rG} &= \frac{W_{tG} \sin(\phi_n)}{\cos(\phi_n) \cos(\lambda) - \mu \sin(\lambda)} \end{aligned}$$

7. Find the friction force:

$$W_f = \frac{\mu W_{tG}}{\cos(\lambda) \cos(\phi_n) - \mu \sin(\lambda)}$$

8. Find the power loss due to friction:

$$P_L = \frac{\nu_s W_f}{33000}$$

9. Compute the input power:

$$P_i = P_o + P_L$$

10. Calculate efficiency:

$$\eta = \frac{P_o}{P_i} = \frac{\cos(\phi_n) - \mu \tan(\lambda)}{\cos(\phi_n) + \frac{\mu}{\tan(\lambda)}}$$

11. Find the Lewis form factor  $y$  from the table below using your  $\phi_n$  value:

TABLE 10-5 Approximate Lewis Form Factor for Wormgear Teeth	
$\phi_n$	$y$
$14\frac{1}{2}^\circ$	0.100
$20^\circ$	0.125
$25^\circ$	0.150
$30^\circ$	0.175

12. Find the normal circular pitch:

$$p_n = p \cos(\lambda) = \frac{\pi \cos(\lambda)}{P_d}$$

13. Find the dynamic factor  $K_v$ :

$$K_v = \frac{1200}{1200 + \nu_{tG}}$$

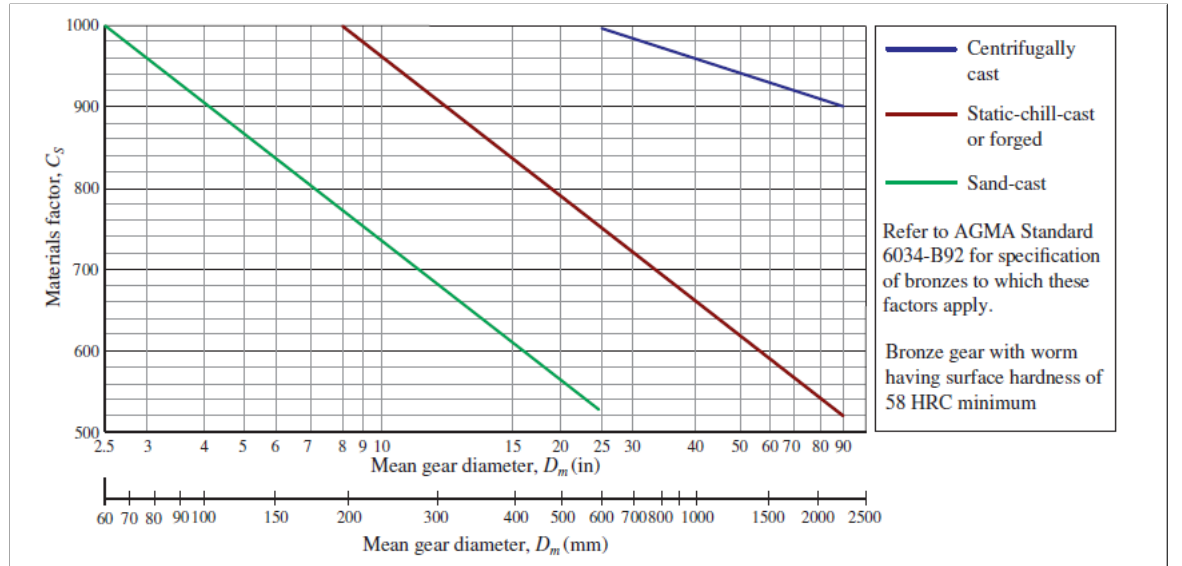
14. Find the dynamic load,  $W_d$ :

$$W_d = \frac{W_{tG}}{K_v}$$

15. Find the stress  $\sigma$  in the gear teeth:

$$\sigma = \frac{W_d}{y F p_n}$$

16. Find the materials factor  $C_s$  using this figure:



For sand-cast bronzes:

$$C_s = \begin{cases} 1189.636 - 476.545 \log_{10}(D_p) & D_G > 2.5 \\ 1000 & D_G < 2.5 \end{cases}$$

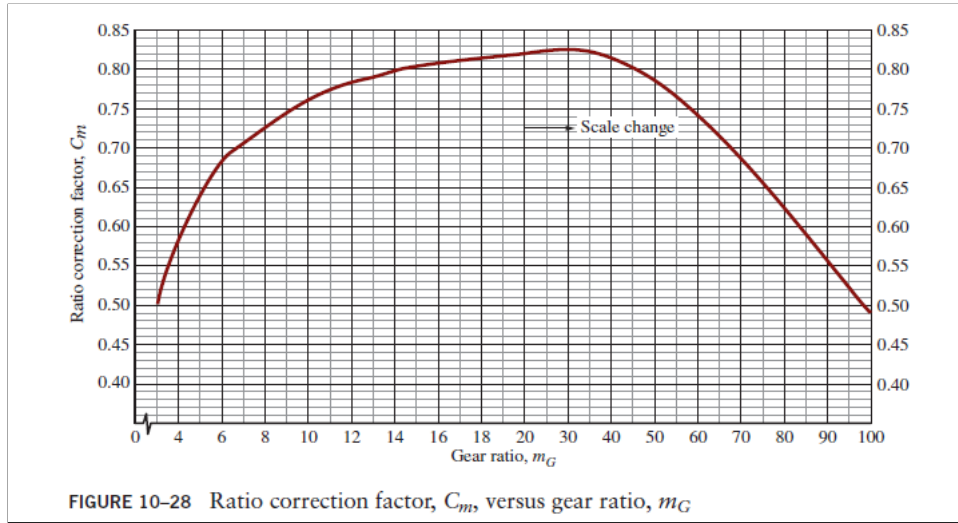
For static-chill-cast or forged bronze:

$$C_s = \begin{cases} 1411.651 - 455.825 \log_{10}(D_p) & D_G < 8 \\ 1000 & D_G > 8 \end{cases}$$

For centrifugally cast bronze:

$$C_s = \begin{cases} 1251.291 - 179.75 \log_{10}(D_p) & D_G < 25 \\ 1000 & D_G > 25 \end{cases}$$

17. Find the ration correction factor  $C_m$ :



Remember that  $m_G$  is the gear ratio which is  $m_G = \frac{N_G}{N_p}$

$$C_m = \begin{cases} 0.02\sqrt{-m_G^2 + 40m_G - 76} + 0.46 & 6 < m_g < 20 \\ 0.0107\sqrt{m_G^2 + 56m_G + 5146} & 20 < m_G < 76 \\ 1.1483 - 0.00658m_G & m_G > 76 \end{cases}$$

18. Find the Worm gear velocity factor  $C_v$ :

$$C_v = \begin{cases} 0.659e^{-0.0011\nu_s} & 0 < \nu_s < 700 \\ 13.31\nu_s^{-0.571} & 700 < m_G < 3000 \\ 65.52\nu_s^{-0.774} & \nu_s > 3000 \end{cases}$$

19. Find the effective face width  $F_e$ :

$$F_e = \begin{cases} F & , F < \frac{D_W}{3} \\ \frac{D_W}{3} & , F > \frac{D_W}{3} \end{cases}$$

20. Find the rated tangential load  $W_{tR}$ :

$$W_{tR} = C_s D_G^{0.8} F_e C_m C_v$$

21. Check if the design is satisfactory to resist pitting:

If  $W_{tR} > W_{tG}$  then the design is satisfactory