

9. Compute the actual CD

$$CD = \frac{1}{4} \left[ LC - \frac{N_2 + N_1}{2} + \sqrt{\left( LC - \frac{N_2 + N_1}{2} \right)^2 - \frac{8(N_2 - N_1)^2}{4\pi^2}} \right]$$

10. Compute the angle of wrap for each sprocket. The minimum angle of wrap should be  $120^\circ$

$$\theta_1 = 180^\circ - 2 \sin^{-1} \left[ \frac{PD_2 - PD_1}{2CD} \right]$$

$$\theta_2 = 180^\circ + 2 \sin^{-1} \left[ \frac{PD_2 - PD_1}{2CD} \right]$$

11. Compute factor of safety

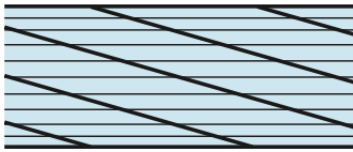
$$FS = P_{allowed} / P_{des}$$

$P_{allowed}$  is the number you got from the table in step 3 times the strand factor

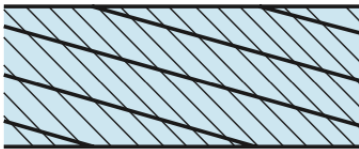
## 1.7 Wire Rope

### 1.7.1 Anatomy

There's two types of rope winding:



(a) Regular lay



(b) Lang lay

- Regular-lay ropes have the wires in the strand twisted in one direction and the strands in the rope twisted in the opposite direction
- Lang-lay ropes have the wires in the strand and the strands in the rope twisted in the same direction. Lang lay is more flexible than regular lay.

### 1.7.2 Nomenclature

$F$  = tensile force on rope (lbf)

$W$  = weight at the end of the rope (load) (lbf)

$m$  = number of ropes supporting load

$w$  = weight/foot supporting load (lbf/ft)

$l$  = maximum suspended length of rope (ft)  
 $a$  = maximum acceleration/deceleration ( $ft/s^2$ )  
 $g$  = acceleration of gravity ( $32.17 \text{ ft/s}^2$ )  
 $p/S_u$  = specified life  
 $S_u$  = ultimate tensile strength (psi)  
 $D$  = sheave or which drum diameter (in)  
 $d$  = nominal wire rope size (in)  
 $E_r$  = Young's modulus (psi)  
 $d_w$  = diameter of the wire (in)  
 $A_m$  = metal cross-sectional area ( $in^2$ )

### 1.7.3 Formulae

$$\text{rope tension: } F_t = \left( \frac{W}{m} + wl \right) \left( 1 + \frac{a}{g} \right)$$

$$\text{ultimate strength of wire: } S_u = \frac{2000F}{Dd}$$

$$\text{fatigue tension: } F_f = \frac{(p/S_u)S_u Dd}{2}$$

$$\text{equivalent bending load: } F_b = \frac{E_r d_w A_m}{D}$$

$$\text{fatigue factor of safety: } n_f = \frac{F_f - F_b}{F_t}$$

$$\text{factor of safety for static loading: } n_s = \frac{F_u - F_b}{F_t}$$

$$\text{bearing pressure: } P = \frac{2F}{dD}$$

### 1.7.4 Useful Tables

**Table 17–24** Wire-Rope Data

| Rope                     | Weight per Foot, lbf | Minimum Sheave Diameter, in | Standard Sizes $d$ , in         | Material                  | Size of Outer Wires | Modulus of Elasticity,* Mpsi | Strength, <sup>†</sup> kpsi |
|--------------------------|----------------------|-----------------------------|---------------------------------|---------------------------|---------------------|------------------------------|-----------------------------|
| 6 × 7 haulage            | $1.50d^2$            | $42d$                       | $\frac{1}{4}$ – $1\frac{1}{2}$  | Monitor steel             | $d/9$               | 14                           | 100                         |
|                          |                      |                             |                                 | Plow steel                | $d/9$               | 14                           | 88                          |
|                          |                      |                             |                                 | Mild plow steel           | $d/9$               | 14                           | 76                          |
| 6 × 19 standard hoisting | $1.60d^2$            | $26d$ – $34d$               | $\frac{1}{4}$ – $2\frac{3}{4}$  | Monitor steel             | $d/13$ – $d/16$     | 12                           | 106                         |
|                          |                      |                             |                                 | Plow steel                | $d/13$ – $d/16$     | 12                           | 93                          |
|                          |                      |                             |                                 | Mild plow steel           | $d/13$ – $d/16$     | 12                           | 80                          |
| 6 × 37 special flexible  | $1.55d^2$            | $18d$                       | $\frac{1}{4}$ – $3\frac{1}{2}$  | Monitor steel             | $d/22$              | 11                           | 100                         |
|                          |                      |                             |                                 | Plow steel                | $d/22$              | 11                           | 88                          |
| 8 × 19 extra flexible    | $1.45d^2$            | $21d$ – $26d$               | $\frac{1}{4}$ – $1\frac{1}{2}$  | Monitor steel             | $d/15$ – $d/19$     | 10                           | 92                          |
|                          |                      |                             |                                 | Plow steel                | $d/15$ – $d/19$     | 10                           | 80                          |
| 7 × 7 aircraft           | $1.70d^2$            | —                           | $\frac{1}{16}$ – $\frac{3}{8}$  | Corrosion-resistant steel | —                   | —                            | 124                         |
|                          |                      |                             |                                 | Carbon steel              | —                   | —                            | 124                         |
| 7 × 9 aircraft           | $1.75d^2$            | —                           | $\frac{1}{8}$ – $1\frac{3}{8}$  | Corrosion-resistant steel | —                   | —                            | 135                         |
|                          |                      |                             |                                 | Carbon steel              | —                   | —                            | 143                         |
| 19-wire aircraft         | $2.15d^2$            | —                           | $\frac{1}{32}$ – $\frac{5}{16}$ | Corrosion-resistant steel | —                   | —                            | 165                         |
|                          |                      |                             |                                 | Carbon steel              | —                   | —                            | 165                         |

**Table 17–27** Some Useful Properties of 6 × 7, 6 × 19, and 6 × 37 Wire Ropes

| Wire Rope | Weight per Foot $w$ , lbf/ft | Weight per Foot Including Core $w$ , lbf/ft | Minimum Sheave Diameter $D$ , in | Better Sheave Diameter $D$ , in | Diameter of Wires $d_w$ , in | Area of Metal $A_m$ , in <sup>2</sup> | Rope Young's Modulus $E_r$ , psi |
|-----------|------------------------------|---|----------------------------------|---------------------------------|------------------------------|---------------------------------------|----------------------------------|
| 6 × 7     | $1.50d^2$                    |   | $42d$                            | $72d$                           | $0.111d$                     | $0.38d^2$                             | $13 \times 10^6$                 |
| 6 × 19    | $1.60d^2$                    | $1.76d^2$                                   | $30d$                            | $45d$                           | $0.067d$                     | $0.40d^2$                             | $12 \times 10^6$                 |
| 6 × 37    | $1.55d^2$                    | $1.71d^2$                                   | $18d$                            | $27d$                           | $0.048d$                     | $0.40d^2$                             | $12 \times 10^6$                 |

**Table 17–26** Maximum Allowable Bearing Pressures of Ropes on Sheaves (in psi)

| Rope         | Sheave Material   |                        |                         |                                 |                              |
|--------------|-------------------|------------------------|-------------------------|---------------------------------|------------------------------|
|              | Wood <sup>a</sup> | Cast Iron <sup>b</sup> | Cast Steel <sup>c</sup> | Chilled Cast Irons <sup>d</sup> | Manganese Steel <sup>e</sup> |
| Regular lay: |                   |                        |                         |                                 |                              |
| 6 × 7        | 150               | 300                    | 550                     | 650                             | 1470                         |
| 6 × 19       | 250               | 480                    | 900                     | 1100                            | 2400                         |
| 6 × 37       | 300               | 585                    | 1075                    | 1325                            | 3000                         |
| 8 × 19       | 350               | 680                    | 1260                    | 1550                            | 3500                         |
| Lang lay:    |                   |                        |                         |                                 |                              |
| 6 × 7        | 165               | 350                    | 600                     | 715                             | 1650                         |
| 6 × 19       | 275               | 550                    | 1000                    | 1210                            | 2750                         |
| 6 × 37       | 330               | 660                    | 1180                    | 1450                            | 3300                         |

$S_u$  ranges:

|                               |                        |
|-------------------------------|------------------------|
| Improved plow steel (monitor) | $240 < S_u < 280$ kpsi |
| Plow steel                    | $210 < S_u < 240$ kpsi |
| Mild plow steel               | $180 < S_u < 210$ kpsi |

No idea how to use this but here it is in case it's relevant:

