

9.3.3 Stress Calculations

Stress Analysis (This guide Follows Mott)

- Typically design using pinion values as the gear will be the same material
- Always use 4 decimal places for your values

9.3.3.1 Spur Gears *using Mott

Here is the bending stress formulas for a pinion and a gear.

$$s_{tP} = \frac{W_t P_d}{F J_p} K_o K_s K_m K_B K_v$$

$$s_{tG} = s_{tP} \frac{J_P}{J_G}$$

The contact stress formula is:

$$s_c = C_p \sqrt{\frac{W_t K_o K_s K_m K_B K_v}{F D_p I}}$$

The allowable bending stress formulas are:

$$s_{at,P} > s_{tP} \frac{K_R(SF)}{Z_{NP}}$$

$$s_{at,G} > s_{tG} \frac{K_R(SF)}{Z_{NP}}$$

Follow steps 1 - 24 to calculate the bending stress values and to specify a material and SF for it.

Follow steps 25 - 30 to calculate the contact stress value and to specify a material and SF for it.

Let the fun begin!

- Find your shock for the input and output using the following:

| |
|--|
| <i>Uniform:</i> Electric motor or constant-speed gas turbine |
| <i>Light shock:</i> Water turbine, variable-speed drive |
| <i>Moderate shock:</i> Multicylinder engine |
| Examples of the roughness of driven machines include the following: |
| <p><i>Uniform:</i> Continuous-duty generator, paper, and film winders.</p> <p><i>Light shock:</i> Fans and low-speed centrifugal pumps, liquid agitators, variable-duty generators, uniformly loaded conveyors, rotary positive displacement pumps, and metal strip processing.</p> <p><i>Moderate shock:</i> High-speed centrifugal pumps, reciprocating pumps and compressors, heavy-duty conveyors, machine tool drives, concrete mixers, textile machinery, meat grinders, saws, bucket elevators, freight elevators, escalators, concrete mixers, plastics molding and processing, sewage disposal equipment, winches, and cable reels.</p> <p><i>Heavy shock:</i> Rock crushers, punch press drives, pulverizers, processing mills, tumbling barrels, wood chippers, vibrating screens, railroad car dumpers, log conveyors, lumber handling equipment, metal shears, hammer mills, commercial washers, heavy-duty hoists and cranes, reciprocating feeders, dredges, rubber processing, compactors, and plastics extruders.</p> |

- Find your overload factor (K_o) based on the shocks for the driven machine and the power source using Table 9-1 below

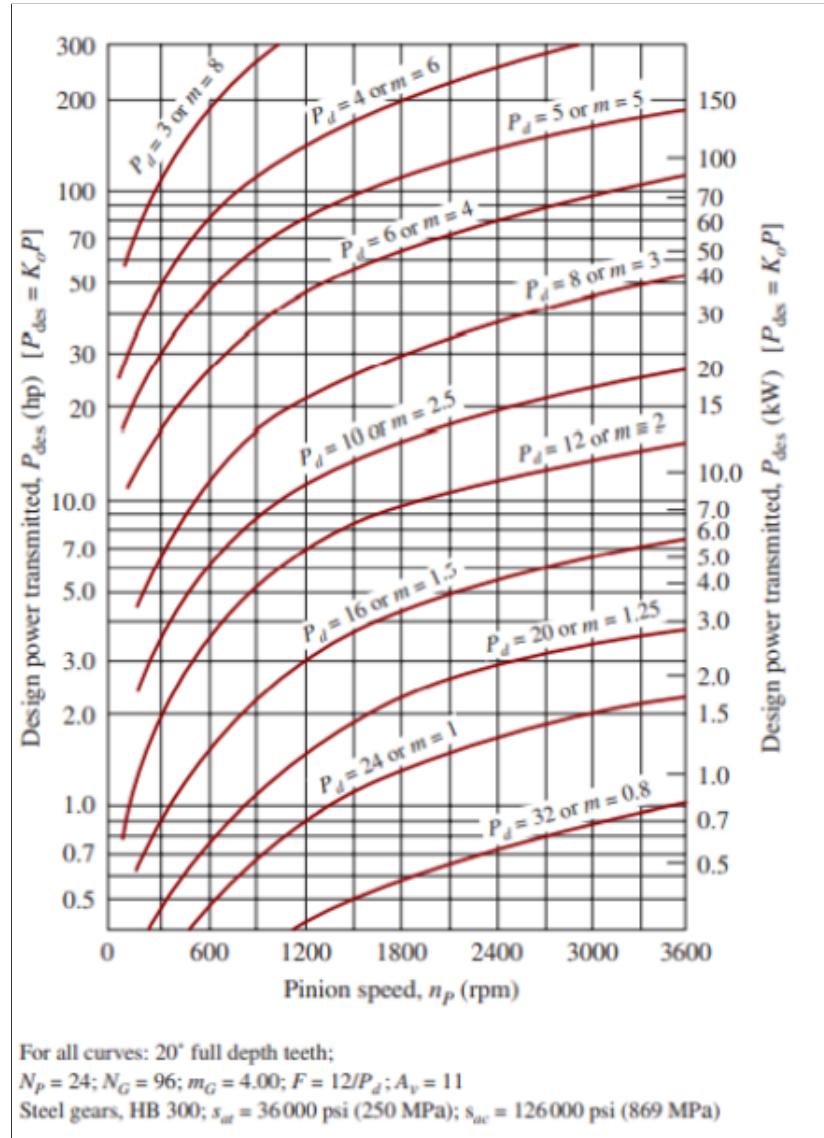
TABLE 9-1 Suggested Overload Factors, K_o

| Driven Machine | | | | |
|----------------|---------|-------------|----------------|-------------|
| Power source | Uniform | Light shock | Moderate shock | Heavy shock |
| Uniform | 1.00 | 1.25 | 1.50 | 1.75 |
| Light shock | 1.20 | 1.40 | 1.75 | 2.25 |
| Moderate shock | 1.30 | 1.70 | 2.00 | 2.75 |

3. Using your K_o and your input power, calculate your design power (HP) using the following formula:

$$P_{design} = PK_o$$

4. Using your design power and the pinion speed, find your diametral pitch (P_d) using the following figure 9-11)⁵³



⁵³Round to the smallest number!

5. Now, choose the number of teeth for the pinion (N_P), using the following range:

$$17 < N_P < 20$$

6. Choose the speed of the gear based on the range given in the problem. Typically want to assume a value that is in the middle of the range.

7. Calculate the velocity ratio using the following formula:

$$VR = \frac{n_P}{n_G}$$

Where " n_P " is the rotational speed of the pinion given in the question and " n_G " is the rotational speed of the gear

8. Calculate the number of teeth in the output gear (N_G) using the following formula:

$$N_G = N_P(VR)$$

Round to the nearest integer

9. Now recalculate your velocity ratio using the number of teeth in the pinion and gear:

$$VR = \frac{N_G}{N_P}$$

10. Calculate the actual output speed (n_G) using this formula:

$$n_G = n_P \left(\frac{N_P}{N_G} \right)$$

Make sure this value is within the specified range given in the question, if not, test a new value for N_P .

11. Find the pitch diameters in inches for the two gears:

$$D_P = \frac{N_P}{P_d}$$

$$D_G = \frac{N_G}{P_d}$$

12. Calculate the Centre Distance (CD in inches), pitch line speed, v_t [ft/min], transmitted load W_t [lbs], and radial load W_r (lbs) using the following formulas:

$$C = \frac{N_P + N_G}{2P_d}$$

$$v_t = \frac{\pi}{12} D_P n_P$$

$$W_t = \frac{33,000P}{v_t}$$

$$W_r = W_t \tan \phi$$

13. Calculate your face width value, F (inches), given the following ranges:

- (a) Lower Limit $F = \frac{8}{P_d}$
- (b) Nominal $F = \frac{12}{P_d}$
- (c) Upper Limit $F = \frac{16}{P_d}$

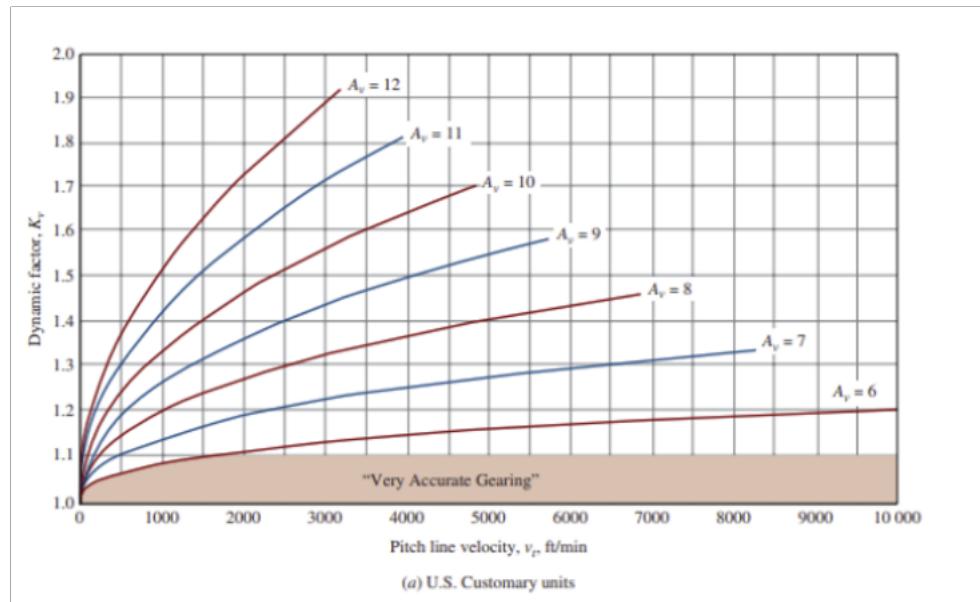
Just go for the nominal value if the question doesn't mention anything specific

14. If the quality number A_v is not given you can calculate it using this table:

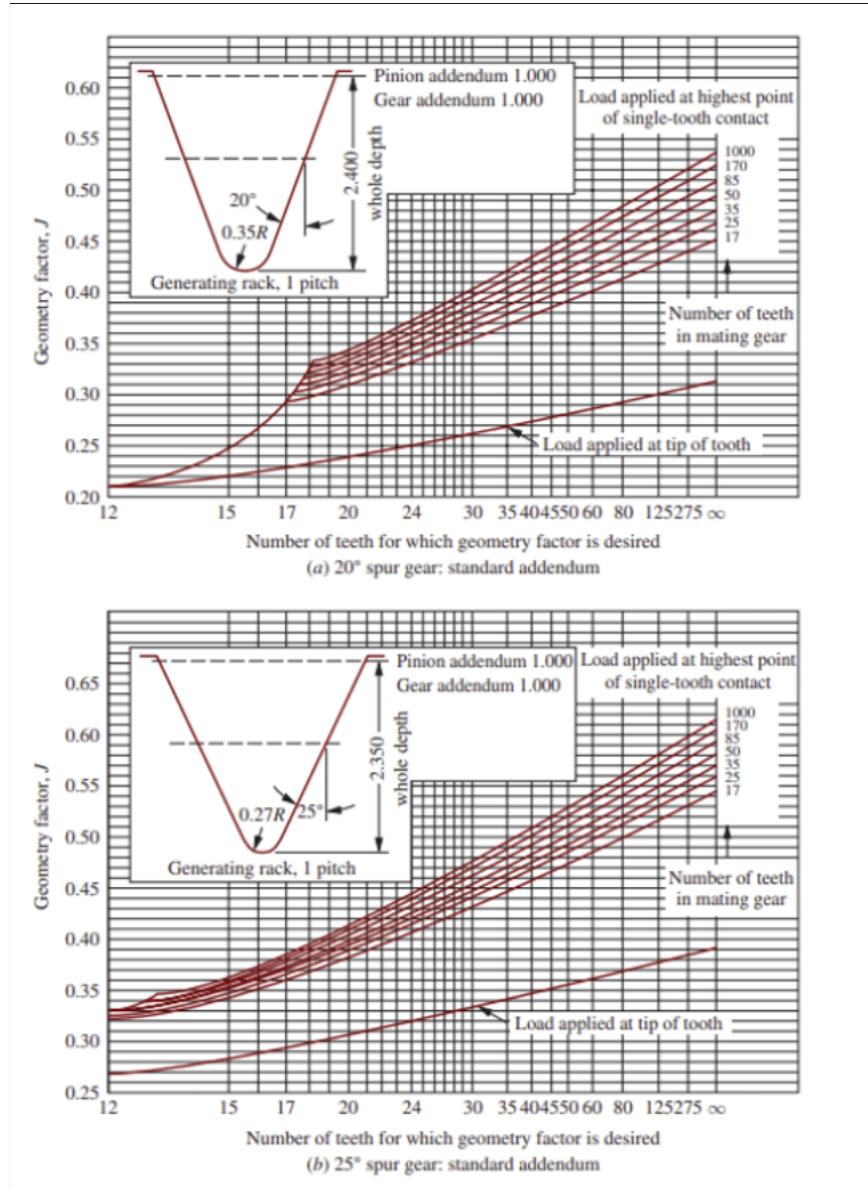
TABLE 9-5 Recommended AGMA Quality Numbers

| Application | Quality number | Application | Quality number |
|---|----------------|-------------------------|----------------|
| Cement mixer drum drive | A11 | Small power drill | A9 |
| Cement kiln | A11 | Clothes washing machine | A8 |
| Steel mill drives | A11 | Printing press | A7 |
| Grain harvester | A10 | Computing mechanism | A6 |
| Cranes | A10 | Automotive transmission | A6 |
| Punch press | A10 | Radar antenna drive | A5 |
| Mining conveyor | A10 | Marine propulsion drive | A5 |
| Paper-box-making machine | A9 | Aircraft engine drive | A4 |
| Gas meter mechanism | A9 | Gyroscope | A2 |
| Machine tool drives and drives for other high-quality mechanical systems | | | |
| Pitch line speed (fpm) | Quality number | Pitch line speed (m/s) | |
| 0–800 | A10 | 0–4 | |
| 800–2000 | A8 | 4–11 | |
| 2000–4000 | A6 | 11–22 | |
| Over 4000 | A4 | Over 22 | |

15. Find the the dynamic factor K_v in the following figure using A_v and v_t :



16. Using N_P and N_G , Find the geometry factor "J" using the following graphs. Typically we assume a 20 degree pressure angle spur gear so use that graph and don't dog it too much.



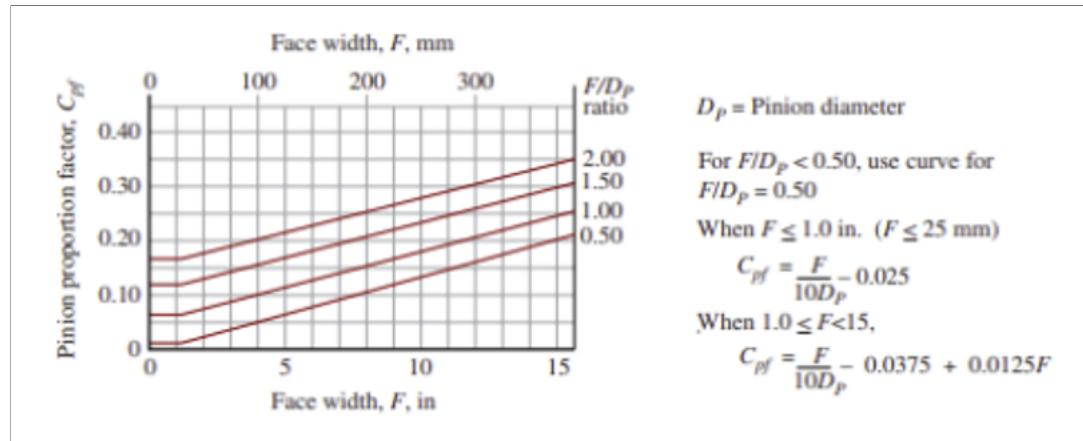
17. Now to find the size factor, K_s , using the following table using your diametral pitch value⁵⁴

| TABLE 9-2 Suggested Size Factors, K_s | | |
|---|--------------------|--------------------|
| Diametral pitch, P_d | Metric module, m | Size factor, K_s |
| ≥ 5 | ≤ 5 | 1.00 |
| 4 | 6 | 1.05 |
| 3 | 8 | 1.15 |
| 2 | 12 | 1.25 |
| 1.25 | 20 | 1.40 |

18. In order to find your load-distribution factor, K_m , perform the following steps given this formula for K_m .

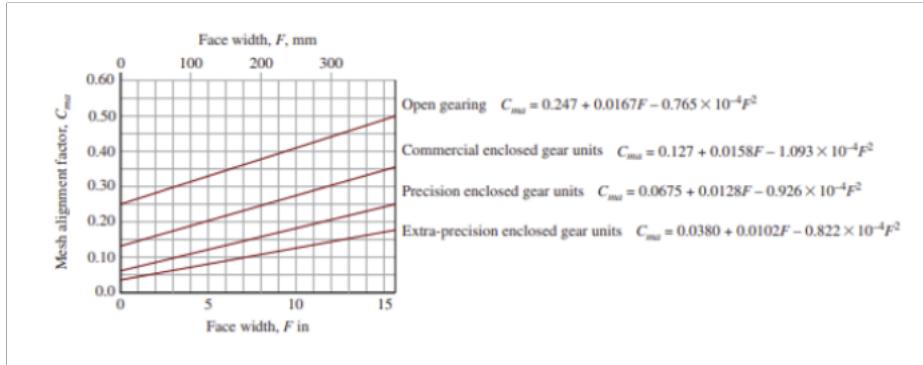
$$K_m = 1 + C_{pf} + C_{ma}$$

Using your face width value and $\frac{F}{D_p}$ ratio, find the pinion proportion factor (C_{pf}) using figure 9-12 below:



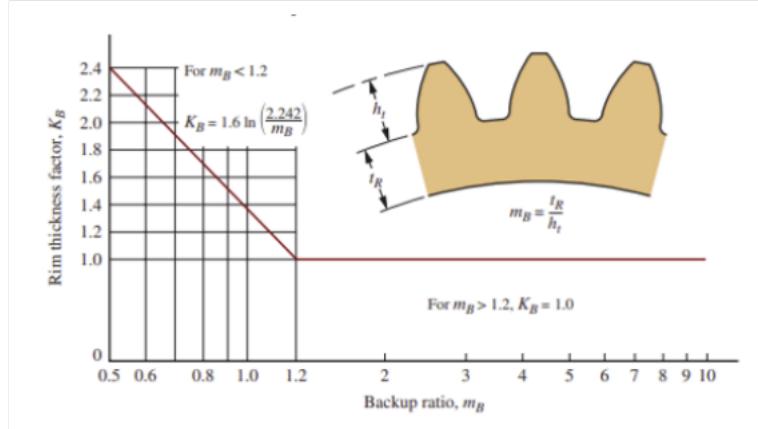
Now we need to find the mesh alignment factor, C_{ma} , using figure 9-13 below. Typically assume that the gears are "Commercial Enclosed Gear Units"

⁵⁴or if you're enough of a dog, you can check the module



Finally find K_m using the formula given in this step.

19. **Find the rim thickness factor, K_b .** Typically this value is 1 for commercially made gears. If this is not the case then use the following figure 9-14 below:



20. **We now have all the factors needed to calculate the bending stress.** Plug everything back into the formula we initially introduced:

$$s_{t,P} = \frac{W_t P_d}{F J_p} K_o K_s K_m K_B K_v$$

$$s_{t,G} = s_{t,P} \frac{J_P}{J_G}$$

21. You can also calculate the allowable bending stress using the following formula:

$$s_{at\ P} > s_{tP} \frac{K_R(SF)}{Y_{NP}}$$

$$s_{at\ G} > s_{tG} \frac{K_R(SF)}{Y_{NG}}$$

- (a) In order to find the Reliability factor, K_R , use this table:

| TABLE 9-11 Reliability Factor, K_R | |
|--------------------------------------|-------|
| Reliability | K_R |
| 0.90, one failure in 10 | 0.85 |
| 0.99, one failure in 100 | 1.00 |
| 0.999, one failure in 1000 | 1.25 |
| 0.9999, one failure in 10 000 | 1.50 |

Typically, Jon tell us to assume 99% Reliability, so use $K_R = 1$

- (b) For the safety factor (SF), assume 1 for now. General range is between 1 and 1.5
- (c) To find the stress cycle factor Y_N , we need to first calculate the number of loading cycles, N_c using this formula:

$$N_{cP} = 60 \times \text{lifetime} \times n_P$$

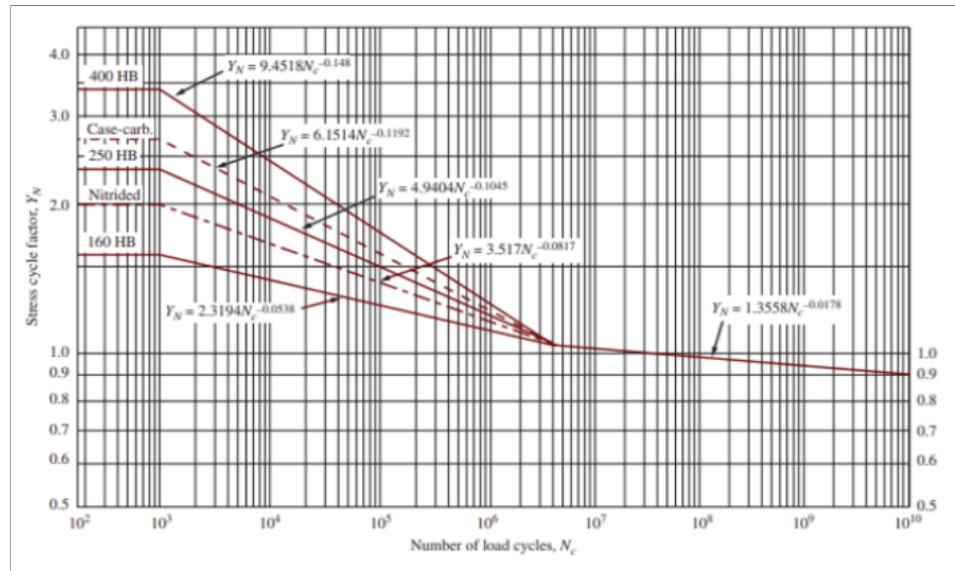
$$N_{cP} = 60 \times \text{lifetime} \times n_G$$

- (d) The lifetime could be specified in the question in hours, or can be found using the following table:

| TABLE 9-12 Recommended Design Life | |
|--|-----------------|
| Application | Design life (h) |
| Domestic appliances | 1000–2000 |
| Aircraft engines | 1000–4000 |
| Automotive | 1500–5000 |
| Agricultural equipment | 3000–6000 |
| Elevators, industrial fans, multipurpose gearing | 8000–15 000 |
| Electric motors, industrial blowers, general industrial machines | 20 000–30 000 |
| Pumps and compressors | 40 000–60 000 |
| Critical equipment in continuous 24-h operation | 100 000–200 000 |

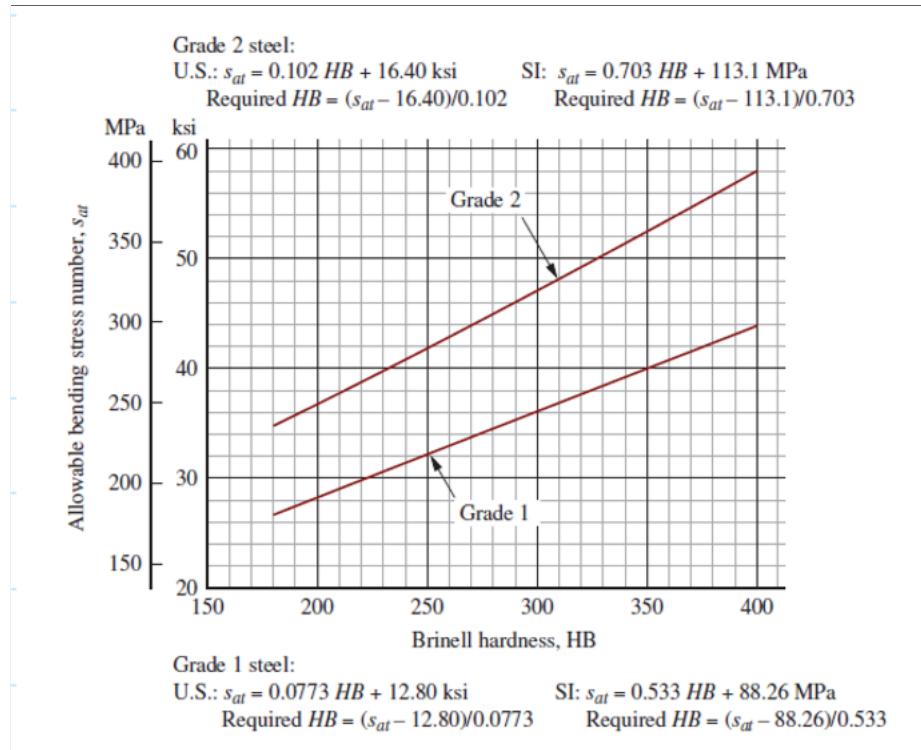
Source: Eugene A. Avallone and Theodore Baumeister III, eds. Marks' Standard Handbook for Mechanical Engineers. 9th ed. New York: McGraw-Hill, 1986.

(e) Now use N_c to calculate Y_N using figure 9-21:



22. Now you can plug everything in to get your allowable bending stress, S_{at} .

23. We now have to choose a material. Use figure 9-18 below to find the required Brinell Hardness (HB) for the material.



We typically use grade 1 steel values. Use ksi for every calculation here.

Now that we have the required hardness, look at appendix 3 or 5 in the textbook and choose any material that has a hardness above the required one. We normally use Appendix 3.

APPENDIX 3 Design Properties of Carbon and Alloy Steels

| Material designation (SAE number) | Condition | Tensile strength | | Yield strength | | Ductility (percent elongation in 2 in) | Brinell hardness (HB) |
|--------------------------------------|------------|------------------|-------|----------------|-------|---|--------------------------|
| | | (ksi) | (MPa) | (ksi) | (MPa) | | |
| 1020 | Hot-rolled | 55 | 379 | 30 | 207 | 25 | 111 |
| 1020 | Cold-drawn | 61 | 420 | 51 | 352 | 15 | 122 |
| 1020 | Annealed | 60 | 414 | 43 | 296 | 38 | 121 |
| 1040 ¹ | Hot-rolled | 72 | 496 | 42 | 290 | 18 | 144 |
| 1040 | Cold-drawn | 80 | 552 | 71 | 490 | 12 | 160 |
| 1040 | OQT 1300 | 88 | 607 | 61 | 421 | 33 | 183 |
| 1040 | OQT 400 | 113 | 779 | 87 | 600 | 19 | 262 |
| 1050 | Hot-rolled | 90 | 620 | 49 | 338 | 15 | 180 |
| 1050 | Cold-drawn | 100 | 690 | 84 | 579 | 10 | 200 |
| 1050 | OQT 1300 | 96 | 662 | 61 | 421 | 30 | 192 |
| 1050 | OQT 400 | 143 | 986 | 110 | 758 | 10 | 321 |
| 1117 | Hot-rolled | 65 | 448 | 40 | 276 | 33 | 124 |
| 1117 | Cold-drawn | 80 | 552 | 65 | 448 | 20 | 138 |
| 1117 | WQT 350 | 89 | 614 | 50 | 345 | 22 | 178 |
| 1137 | Hot-rolled | 88 | 607 | 48 | 331 | 15 | 176 |
| 1137 | Cold-drawn | 98 | 676 | 82 | 565 | 10 | 196 |
| 1137 | OQT 1300 | 87 | 600 | 60 | 414 | 28 | 174 |
| 1137 | OQT 400 | 157 | 1083 | 136 | 938 | 5 | 352 |
| 1144 ¹ | Hot-rolled | 94 | 648 | 51 | 352 | 15 | 188 |
| 1144 | Cold-drawn | 100 | 690 | 90 | 621 | 10 | 200 |
| 1144 | OQT 1300 | 96 | 662 | 68 | 469 | 25 | 200 |
| 1144 | OQT 400 | 127 | 876 | 91 | 627 | 16 | 277 |
| 1213 | Hot-rolled | 55 | 379 | 33 | 228 | 25 | 110 |
| 1213 | Cold-drawn | 75 | 517 | 58 | 340 | 10 | 150 |
| 12L13 | Hot-rolled | 57 | 393 | 34 | 234 | 22 | 114 |
| 12L13 | Cold-drawn | 70 | 483 | 60 | 414 | 10 | 140 |
| 1340 ¹ | Annealed | 102 | 703 | 63 | 434 | 26 | 207 |
| 1340 | OQT 1300 | 100 | 690 | 75 | 517 | 25 | 235 |
| 1340 | OQT 1000 | 144 | 993 | 132 | 910 | 17 | 363 |
| 1340 | OQT 700 | 221 | 1520 | 197 | 1360 | 10 | 444 |
| 1340 | OQT 400 | 285 | 1960 | 234 | 1610 | 8 | 578 |
| 3140 | Annealed | 95 | 655 | 67 | 462 | 25 | 187 |
| 3140 | OQT 1300 | 115 | 792 | 94 | 648 | 23 | 233 |
| 3140 | OQT 1000 | 152 | 1050 | 133 | 920 | 17 | 311 |
| 3140 | OQT 700 | 220 | 1520 | 200 | 1380 | 13 | 461 |
| 3140 | OQT 400 | 280 | 1930 | 248 | 1710 | 11 | 555 |
| 4130 | Annealed | 81 | 558 | 52 | 359 | 28 | 156 |
| 4130 | WQT 1300 | 98 | 676 | 89 | 614 | 28 | 202 |
| 4130 | WQT 1000 | 143 | 986 | 132 | 910 | 16 | 302 |
| 4130 | WQT 700 | 208 | 1430 | 180 | 1240 | 13 | 415 |
| 4130 | WQT 400 | 234 | 1610 | 197 | 1360 | 12 | 461 |
| 4140 ¹ | Annealed | 95 | 655 | 54 | 372 | 26 | 197 |
| 4140 | OQT 1300 | 117 | 807 | 100 | 690 | 23 | 235 |
| 4140 | OQT 1000 | 168 | 1160 | 152 | 1050 | 17 | 341 |
| 4140 | OQT 700 | 231 | 1590 | 212 | 1460 | 13 | 461 |
| 4140 | OQT 400 | 290 | 2000 | 251 | 1730 | 11 | 578 |
| 4150 | Annealed | 106 | 731 | 55 | 379 | 20 | 197 |
| 4150 | OQT 1300 | 127 | 880 | 116 | 800 | 20 | 262 |
| 4150 | OQT 1000 | 197 | 1360 | 181 | 1250 | 11 | 401 |
| 4150 | OQT 700 | 247 | 1700 | 229 | 1580 | 10 | 495 |
| 4150 | OQT 400 | 300 | 2070 | 248 | 1710 | 10 | 578 |

(Continued)

APPENDIX 3 (Continued)

| Material designation (SAE number) | Condition | Tensile strength | | Yield strength | | Ductility (percent elongation in 2 in) | Brinell hardness (HB) |
|--------------------------------------|-----------|------------------|-------|----------------|-------|---|-----------------------|
| | | (ksi) | (MPa) | (ksi) | (MPa) | | |
| 4340 ¹ | Annealed | 108 | 745 | 68 | 469 | 22 | 217 |
| 4340 | OQT 1300 | 140 | 965 | 120 | 827 | 23 | 280 |
| 4340 | OQT 1000 | 171 | 1180 | 158 | 1090 | 16 | 363 |
| 4340 | OQT 700 | 230 | 1590 | 206 | 1420 | 12 | 461 |
| 4340 | OQT 400 | 283 | 1950 | 228 | 1570 | 11 | 555 |
| 5140 | Annealed | 83 | 572 | 42 | 290 | 29 | 167 |
| 5140 | OQT 1300 | 104 | 717 | 83 | 572 | 27 | 207 |
| 5140 | OQT 1000 | 145 | 1000 | 130 | 896 | 18 | 302 |
| 5140 | OQT 700 | 220 | 1520 | 200 | 1380 | 11 | 429 |
| 5140 | OQT 400 | 276 | 1900 | 226 | 1560 | 7 | 534 |
| 5150 | Annealed | 98 | 676 | 52 | 359 | 22 | 197 |
| 5150 | OQT 1300 | 116 | 800 | 102 | 700 | 22 | 241 |
| 5150 | OQT 1000 | 160 | 1100 | 149 | 1030 | 15 | 321 |
| 5150 | OQT 700 | 240 | 1650 | 220 | 1520 | 10 | 461 |
| 5150 | OQT 400 | 312 | 2150 | 250 | 1720 | 8 | 601 |
| 5160 | Annealed | 105 | 724 | 40 | 276 | 17 | 197 |
| 5160 | OQT 1300 | 115 | 793 | 100 | 690 | 23 | 229 |
| 5160 | OQT 1000 | 170 | 1170 | 151 | 1040 | 14 | 341 |
| 5160 | OQT 700 | 263 | 1810 | 237 | 1630 | 9 | 514 |
| 5160 | OQT 400 | 322 | 2220 | 260 | 1790 | 4 | 627 |
| 6150 ¹ | Annealed | 96 | 662 | 59 | 407 | 23 | 197 |
| 6150 | OQT 1300 | 118 | 814 | 107 | 738 | 21 | 241 |
| 6150 | OQT 1000 | 183 | 1260 | 173 | 1190 | 12 | 375 |
| 6150 | OQT 700 | 247 | 1700 | 223 | 1540 | 10 | 495 |
| 6150 | OQT 400 | 315 | 2170 | 270 | 1860 | 7 | 601 |
| 8650 | Annealed | 104 | 717 | 56 | 386 | 22 | 212 |
| 8650 | OQT 1300 | 122 | 841 | 113 | 779 | 21 | 255 |
| 8650 | OQT 1000 | 176 | 1210 | 155 | 1070 | 14 | 363 |
| 8650 | OQT 700 | 240 | 1650 | 222 | 1530 | 12 | 495 |
| 8650 | OQT 400 | 282 | 1940 | 250 | 1720 | 11 | 555 |
| 8740 | Annealed | 100 | 690 | 60 | 414 | 22 | 201 |
| 8740 | OQT 1300 | 119 | 820 | 100 | 690 | 25 | 241 |
| 8740 | OQT 1000 | 175 | 1210 | 167 | 1150 | 15 | 363 |
| 8740 | OQT 700 | 228 | 1570 | 212 | 1460 | 12 | 461 |
| 8740 | OQT 400 | 290 | 2000 | 240 | 1650 | 10 | 578 |
| 9255 | Annealed | 113 | 780 | 71 | 490 | 22 | 229 |
| 9255 | Q&T 1300 | 130 | 896 | 102 | 703 | 21 | 262 |
| 9255 | Q&T 1000 | 181 | 1250 | 160 | 1100 | 14 | 352 |
| 9255 | Q&T 700 | 260 | 1790 | 240 | 1650 | 5 | 534 |
| 9255 | Q&T 400 | 310 | 2140 | 287 | 1980 | 2 | 601 |

Notes: Properties common to all carbon and alloy steels:

Poisson's ratio: 0.27.

Shear modulus: 11.5×10^6 psi; 80 GPa.

Coefficient of thermal expansion: 6.5×10^{-6} F⁻¹.

Density: 0.283 lb/in³; 7680 kg/m³.

Modulus of elasticity: 30×10^6 psi; 207 GPa.

¹See Appendix 4 for graphs of properties versus heat treatment.

APPENDIX 5 Properties of Carburized Steels

| Material designation (SAE number) | Condition | Core properties | | | | | |
|--------------------------------------|-----------|------------------------------------|----------------------------------|--|-----------------------------|---------------------------|-----|
| | | Tensile strength (ksi) (MPa) | Yield strength (ksi) (MPa) | Ductility (percent elongation in 2 in) | Brinell hardness (HB) | Case hardness (HRC) | |
| 1015 | SWQT 350 | 106 | 731 | 60 | 414 | 15 | 217 |
| 1020 | SWQT 350 | 129 | 889 | 72 | 496 | 11 | 255 |
| 1022 | SWQT 350 | 135 | 931 | 75 | 517 | 14 | 262 |
| 1117 | SWQT 350 | 125 | 862 | 66 | 455 | 10 | 235 |
| 1118 | SWQT 350 | 144 | 993 | 90 | 621 | 13 | 285 |
| 4118 | SOQT 300 | 143 | 986 | 93 | 641 | 17 | 293 |
| 4118 | DOQT 300 | 126 | 869 | 63 | 434 | 21 | 241 |
| 4118 | SOQT 450 | 138 | 952 | 89 | 614 | 17 | 277 |
| 4118 | DOQT 450 | 120 | 827 | 63 | 434 | 22 | 229 |
| 4320 | SOQT 300 | 218 | 1500 | 178 | 1230 | 13 | 429 |
| 4320 | DOQT 300 | 151 | 1040 | 97 | 669 | 19 | 302 |
| 4320 | SOQT 450 | 211 | 1450 | 173 | 1190 | 12 | 415 |
| 4320 | DOQT 450 | 145 | 1000 | 94 | 648 | 21 | 293 |
| 4620 | SOQT 300 | 119 | 820 | 83 | 572 | 19 | 277 |
| 4620 | DOQT 300 | 122 | 841 | 77 | 531 | 22 | 248 |
| 4620 | SOQT 450 | 115 | 793 | 80 | 552 | 20 | 248 |
| 4620 | DOQT 450 | 115 | 793 | 77 | 531 | 22 | 235 |
| 4820 | SOQT 300 | 207 | 1430 | 167 | 1150 | 13 | 415 |
| 4820 | DOQT 300 | 204 | 1405 | 165 | 1140 | 13 | 415 |
| 4820 | SOQT 450 | 205 | 1410 | 184 | 1270 | 13 | 415 |
| 4820 | DOQT 450 | 196 | 1350 | 171 | 1180 | 13 | 401 |
| 8620 | SOQT 300 | 188 | 1300 | 149 | 1030 | 11 | 388 |
| 8620 | DOQT 300 | 133 | 917 | 83 | 572 | 20 | 269 |
| 8620 | SOQT 450 | 167 | 1150 | 120 | 827 | 14 | 341 |
| 8620 | DOQT 450 | 130 | 896 | 77 | 531 | 22 | 262 |
| E9310 | SOQT 300 | 173 | 1190 | 135 | 931 | 15 | 363 |
| E9310 | DOQT 300 | 174 | 1200 | 139 | 958 | 15 | 363 |
| E9310 | SOQT 450 | 168 | 1160 | 137 | 945 | 15 | 341 |
| E9310 | DOQT 450 | 169 | 1170 | 138 | 952 | 15 | 352 |

Notes: Properties given are for a single set of tests on 1/2-in round bars.

SWQT: single water-quenched and tempered.

SOQT: single oil-quenched and tempered.

DOQT: double oil-quenched and tempered.

300 and 450 are the tempering temperatures in °F. Steel was carburized for 8 h. Case depth ranged from 0.045 to 0.075 in.

Anything that has a hardness over 400 should use flame or induction hardening techniques over through hardening, since they provide the strength required for high contact stress because their inside is still ductile to prevent failure.

TABLE 9–8 Examples of Gear Materials

| Heat treatment | Typical alloys (SAE numbers) |
|---|------------------------------------|
| Through-hardened or Case-hardened by flame or induction hardening | 1045, 4140, 4150, 4340, 4350 |
| Carburizing, case-hardened | 1020, 4118, 4320, 4820, 8620, 9310 |

24. **We now calculate our actual safety factor.** Use the formula in figure 9-18 to calculate the allowable bending stress value using the hardness for the material you chose. This formula is also what you will use to calculate your Safety factor in the end:

$$SF = \frac{s_{at}Y_n}{s_tK_r}$$

25. **Now we move to calculating the contact stress** using the following formula:

$$s_c = C_p \sqrt{\frac{W_t K_o K_s K_m K_B K_v}{FD_p I}}$$

We have most of these constants from the bending stress calculations. Key differences are C_p and I , which will be shown below

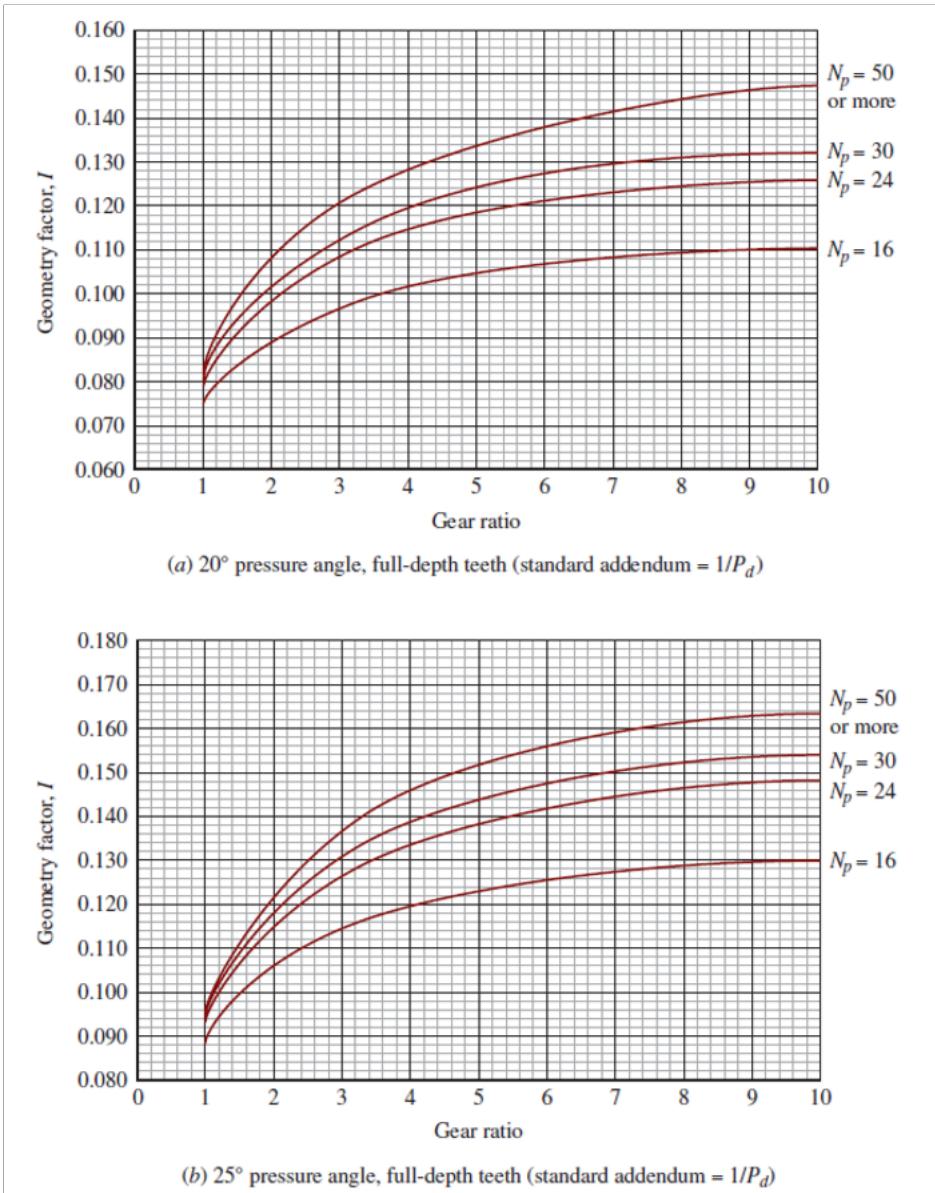
26. **For the elastic coefficient, C_p ,** we generally assume a material of steel which has a C_p of 2300. There are other materials shown here as well:

TABLE 9-7 Elastic Coefficient, C_p

| Pinion material | Modulus of elasticity, E_p , lb/in ² (MPa) | Gear material and modulus of elasticity, E_b , lb/in ² (MPa) | | | | | |
|-----------------|---|---|---|---------------------------------------|------------------------------------|--|-------------------------------------|
| | | Steel (2×10^6) | Malleable iron (1.7×10^6) | Nodular iron (1.7×10^6) | Cast iron (1.5×10^6) | Aluminum bronze (1.2×10^6) | Tin bronze (1.1×10^6) |
| Steel | 30×10^6 (2×10^5) | 2300 (191) | 2180 (181) | 2160 (179) | 2100 (174) | 1950 (162) | 1900 (158) |
| Mall. iron | 25×10^6 (1.7×10^5) | 2180 (181) | 2090 (174) | 2070 (172) | 2020 (168) | 1900 (158) | 1850 (154) |
| Nod. iron | 24×10^6 (1.7×10^5) | 2160 (179) | 2070 (172) | 2050 (170) | 2000 (166) | 1880 (156) | 1830 (152) |
| Cast iron | 22×10^6 (1.5×10^5) | 2100 (174) | 2020 (168) | 2000 (166) | 1960 (163) | 1850 (154) | 1800 (149) |
| Al. bronze | 1.75×10^6 (1.2×10^5) | 1950 (162) | 1900 (158) | 1880 (156) | 1850 (154) | 1750 (145) | 1700 (141) |
| Tin bronze | 16×10^6 (1.1×10^5) | 1900 (158) | 1850 (154) | 1830 (152) | 1800 (149) | 1700 (141) | 1650 (137) |

Source: Extracted from AGMA Standard 2001-D04, *Fundamental Rating Factors and Calculation Methods for Involute Spur and Helical Gear Teeth*, with the permission of the publisher, American Gear Manufacturers Association, 1001 North Fairfax Street, 5th floor, Alexandria, VA 22314.
Note: Poisson's ratio = 0.30; units for C_p are (lb/in²)^{0.5} or (MPa)^{0.5}.

27. **Using the actual gear ratio and N_p , Find the pitting geometry factor, I , using the following graphs.** Again, assume a 20 degree pressure angle, so use that graph. Figure 9-17



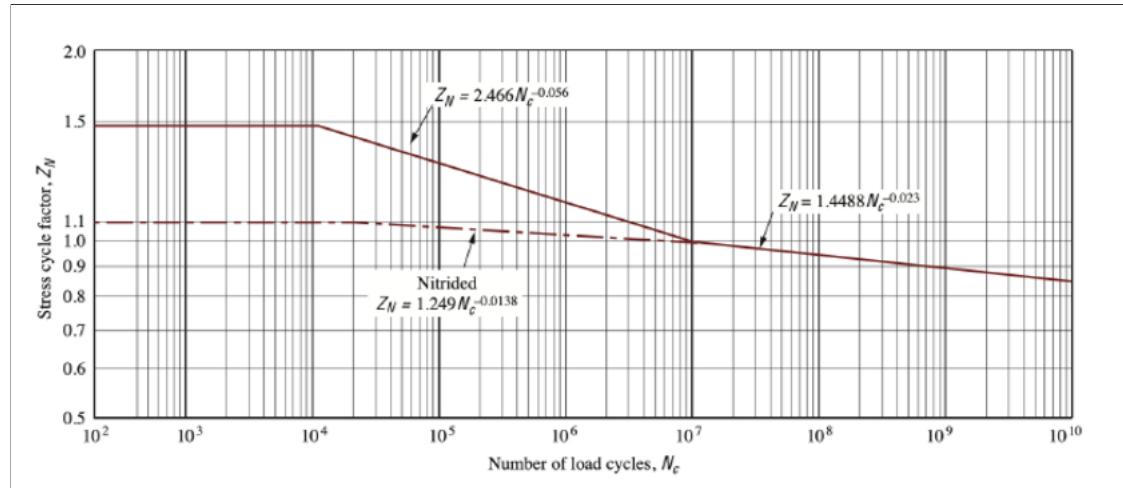
28. We can now plug everything in to find the contact stress, s_c

29. In order to find the allowable contact stress, s_{ac} , we use this formula:

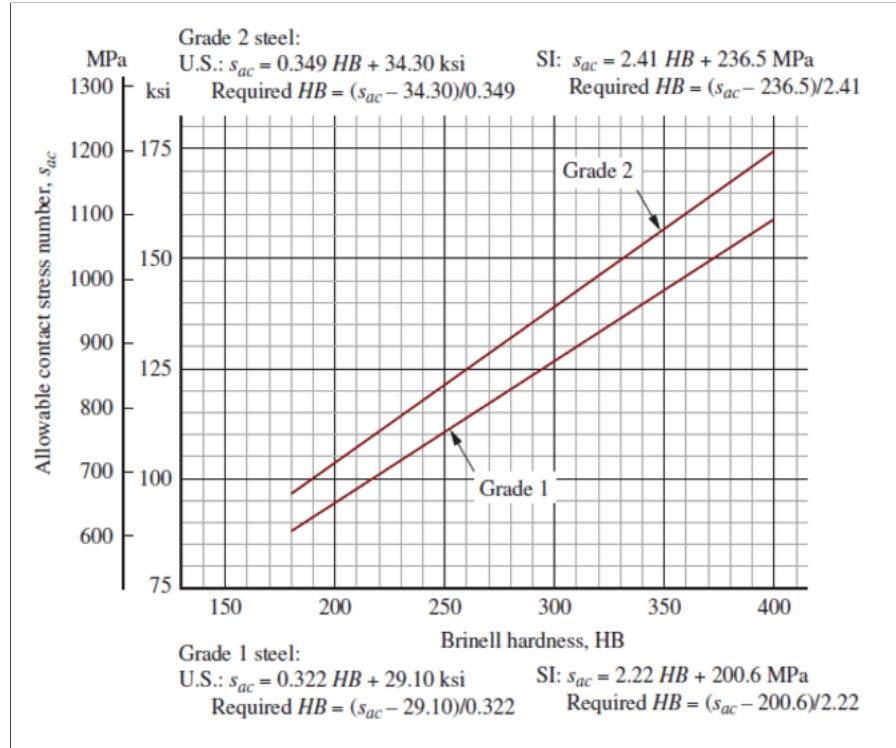
$$s_{ac,P} > s_{cP} \frac{K_R(SF)}{Z_{NP}}$$

$$s_{ac,G} > s_{cG} \frac{K_R(SF)}{Z_{NG}}$$

We already assumed a K_R of 1 and a safety factor of 1 in step 21. Now we need to find Z_N which is the stress cycle factor. We use the following figure 9-22:



30. We follow a similar procedure to specify the material and to find the safety factor using the contact stresses. Although the formulas change slightly, use figure 9-19 below



Follow the same procedure for bending stress material specification and safety factor calculations. This is what you will use to calculate your Safety factor in the end:

$$SF = \frac{s_{ac} Z_n}{s_c K_r}$$

9.3.3.2 Helical Gears *using Mott

The process for calculating helical gear stress is very similar to spur gears, with the key differences being that J and I change!. Here's how it goes:

1. Find your shock for the input and output using the following:
2. Find your overload factor (K_o) based on the shocks for the driven machine and the power source using Table 9-1 below
3. Using your K_o and your input power, calculate your design power (HP) using the following formula:

$$P_{des} = P K_o$$

4. In order to find the normal diametrical pitch and number of teeth in the pinion, just use these random numbers $P_{nd} = 12$ and $N_p = 24$
5. Calculate the diametrical pitch using this formula:

$$P_d = P_{nd} \cos(\psi)$$

Use the helix angle given in the question

6. Calculate the axial pitch p_x using this formula:

$$p_x = \frac{\pi}{P_d \tan(\psi)}$$

7. Assume that n_G is given, if not then use a similar process in the spur gear section to find it. Use the gear ratio to get the number of teeth in the gear, N_G

$$VR = \frac{N_G}{N_P} = \frac{n_p}{n_G}$$

8. Calculate the tangential pressure angle or the normal pressure angle:

$$\phi_t = \arctan\left(\frac{\tan(\phi_n)}{\cos(\psi)}\right)$$

$$\phi_t = \arctan(\tan(\phi_t) \cos(\psi))$$

9. Calculate the diameters of the gears cause fuck it why not:

$$D_p = \frac{N_P}{P_d}$$

$$D_G = \frac{N_G}{P_d}$$

Look the P_d we are using is not the Normal one its the new one just keep that in mind

10. Find the nominal face width:

$$F_{nom} = 2p_x$$

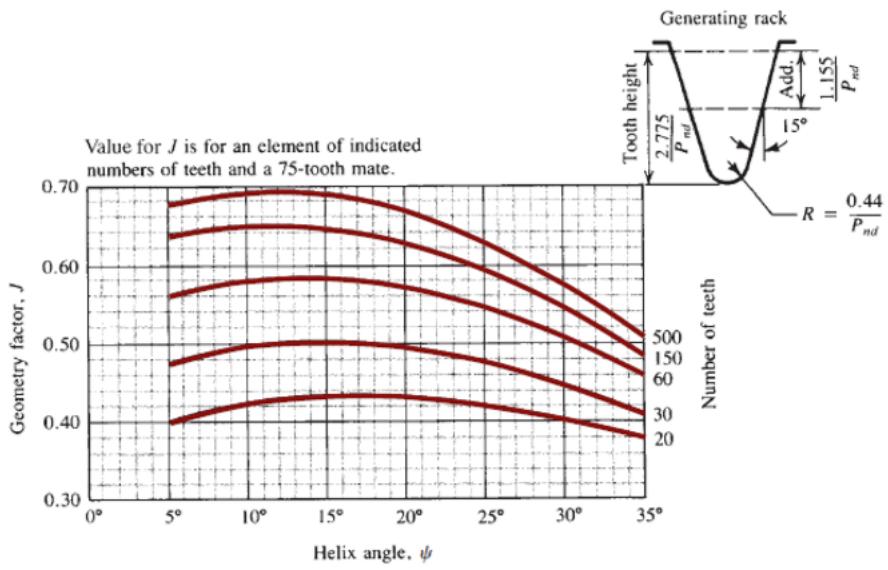
11. Find Center distance (inch), pitch line speed (feet/min), and transmitted load (lbs):

$$C = \frac{N_P + N_G}{2P_d}$$

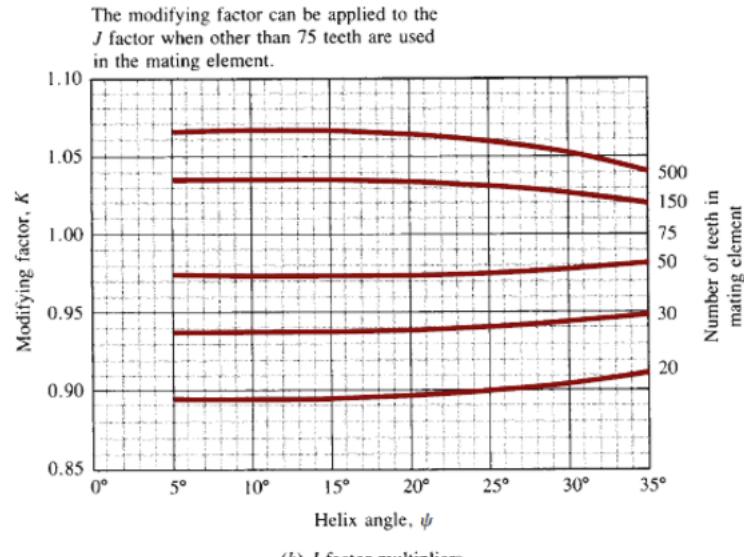
$$v_t = \frac{\pi}{12} D_p n_p$$

$$W_t = \frac{33000P}{v_t}$$

12. Now follow the same procedure as the spur gears to find the stresses, J and I will be different though.
13. Choose J from the graphs below depending on the normal pressure angle



(a) Geometry factor (J) for 15° normal pressure angle and indicated addendum



(b) J factor multipliers

FIGURE 10–5 Geometry factor (J) for 15° normal pressure angle

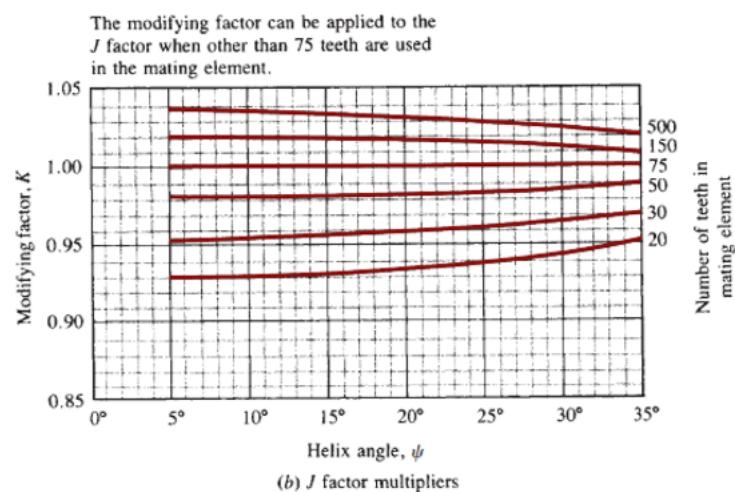
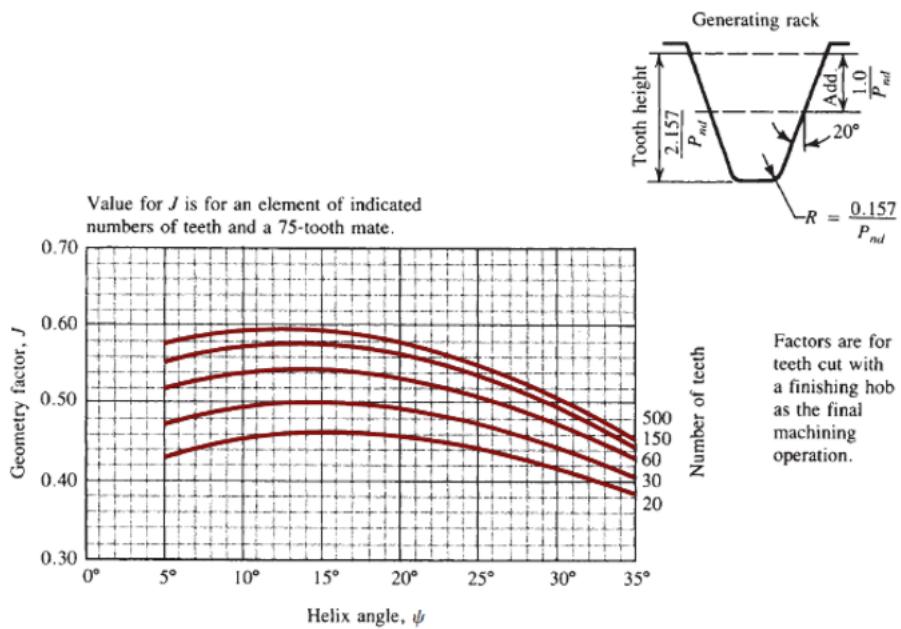
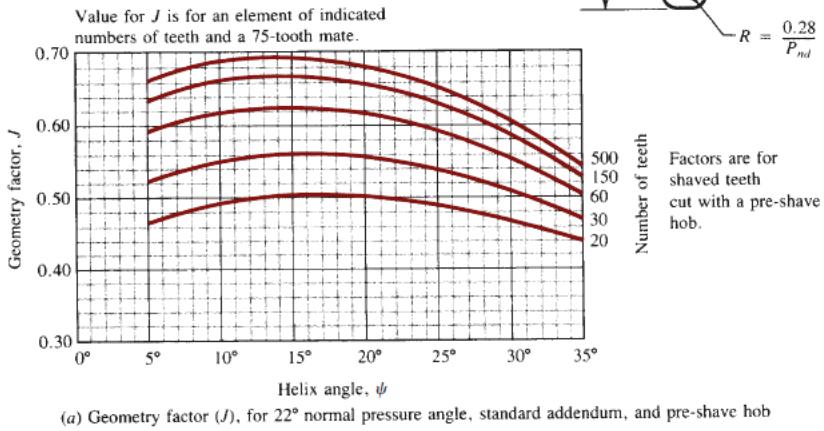
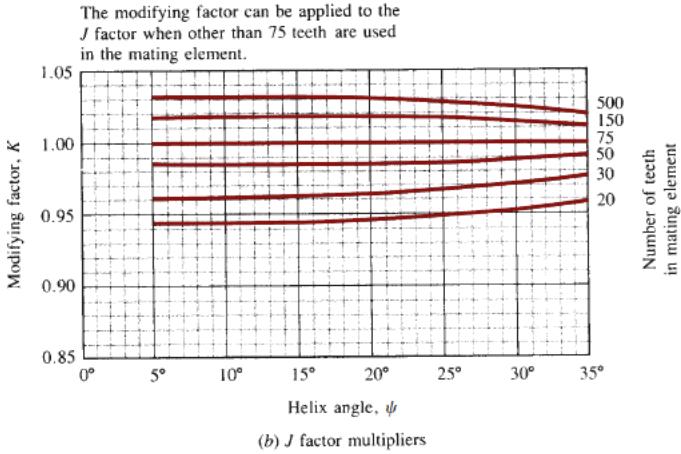


FIGURE 10-6 Geometry factor (J) for 20° normal pressure angle



(a) Geometry factor (J), for 22° normal pressure angle, standard addendum, and pre-shave hob



(b) J factor multipliers

FIGURE 10–7 Geometry factor (J) for 22° normal pressure angle

I swear he will never give you a 22° one but if he does it is what it is.

14. Now calculate I using the tables below:

TABLE 10-1 Geometry Factors for Pitting Resistance, I , for Helical Gears with 20° Normal Pressure Angle and Standard Addendum

A. Helix angle $\psi = 15.0^\circ$

| Gear teeth | Pinion teeth | | | | |
|------------|--------------|-------|-------|-------|-------|
| | 17 | 21 | 26 | 35 | 55 |
| 17 | 0.124 | | | | |
| 21 | 0.139 | 0.128 | | | |
| 26 | 0.154 | 0.143 | 0.132 | | |
| 35 | 0.175 | 0.165 | 0.154 | 0.137 | |
| 55 | 0.204 | 0.196 | 0.187 | 0.171 | 0.143 |
| 135 | 0.244 | 0.241 | 0.237 | 0.229 | 0.209 |

B. Helix angle $\psi = 25.0^\circ$

| Gear teeth | Pinion teeth | | | | |
|------------|--------------|-------|-------|-------|-------|
| | 14 | 17 | 21 | 26 | 35 |
| 14 | 0.123 | | | | |
| 17 | 0.137 | 0.126 | | | |
| 21 | 0.152 | 0.142 | 0.130 | | |
| 26 | 0.167 | 0.157 | 0.146 | 0.134 | |
| 35 | 0.187 | 0.178 | 0.168 | 0.156 | 0.138 |
| 55 | 0.213 | 0.207 | 0.199 | 0.189 | 0.173 |
| 135 | 0.248 | 0.247 | 0.244 | 0.239 | 0.230 |

Source: Extracted from AGMA Standard 908-B89 (R 1999), *Geometry Factors for Determining the Pitting Resistance and Bending Strength of Spur, Helical and Herringbone Gear Teeth*, with the permission of the publisher, American Gear Manufacturers Association, 1001 North Fairfax Street, 5th floor, Alexandria, VA 22314.

TABLE 10-2 Geometry Factors for Pitting Resistance, I , for Helical Gears with 25° Normal Pressure Angle and Standard Addendum

A. Helix angle $\psi = 15.0^\circ$

| Gear teeth | Pinion teeth | | | | |
|------------|--------------|-------|-------|-------|-------|
| | 14 | 17 | 21 | 26 | 35 |
| 14 | 0.130 | | | | |
| 17 | 0.144 | 0.133 | | | |
| 21 | 0.160 | 0.149 | 0.137 | | |
| 26 | 0.175 | 0.165 | 0.153 | 0.140 | |
| 35 | 0.195 | 0.186 | 0.175 | 0.163 | 0.143 |
| 55 | 0.222 | 0.215 | 0.206 | 0.195 | 0.178 |
| 135 | 0.257 | 0.255 | 0.251 | 0.246 | 0.236 |

B. Helix angle $\psi = 25.0^\circ$

| Gear teeth | Pinion teeth | | | | |
|------------|--------------|-------|-------|-------|-------|
| | 12 | 14 | 17 | 21 | 26 |
| 12 | 0.129 | | | | |
| 14 | 0.141 | 0.132 | | | |
| 17 | 0.155 | 0.146 | 0.135 | | |
| 21 | 0.170 | 0.162 | 0.151 | 0.138 | |
| 26 | 0.185 | 0.177 | 0.166 | 0.154 | 0.141 |
| 35 | 0.203 | 0.197 | 0.188 | 0.176 | 0.163 |
| 55 | 0.227 | 0.223 | 0.216 | 0.207 | 0.196 |
| 135 | 0.259 | 0.258 | 0.255 | 0.251 | 0.246 |

Source: Extracted from AGMA Standard 908-B89, *Geometry Factors for Determining the Pitting Resistance and Bending Strength of Spur, Helical and Herringbone Gear Teeth*, with the permission of the publisher, American Gear Manufacturers Association, 1001 North Fairfax Street, 5th floor, Alexandria, VA 22314.