



Faculty of Engineering & Technology  
Electrical & Computer Engineering Department  
ENCS4310: Digital Signal Processing  
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Section.no : 2

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**Question#1:** For the following Signal  $x[n]$ :

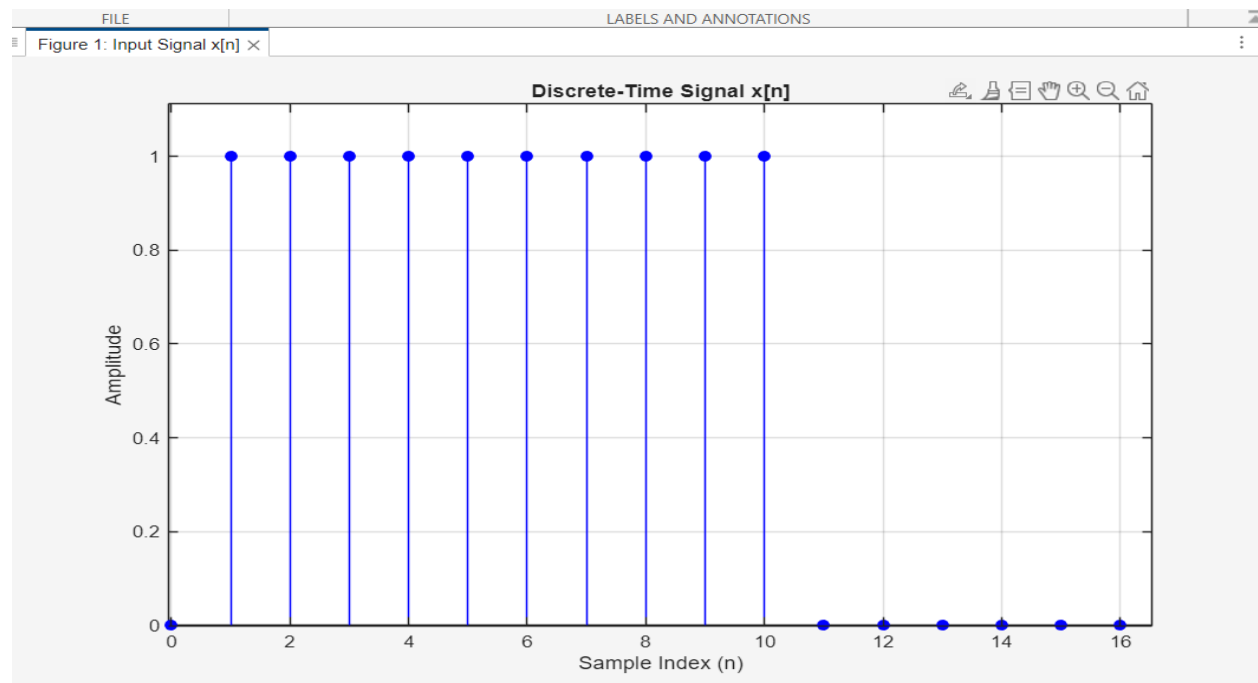
$$x[n] = \begin{cases} 1, & n = 1 \dots 10 \\ 0, & \text{Otherwise} \end{cases}$$

$x[n]$  Signal and its plot in MATLAB:

MATLAB code :

```
spProj.m x +  
I:\Users\Lenovo\OneDrive\Documents\MATLAB\DspProj.m  
  
n = 0:255;  
x = zeros(size(n));  
x(n >= 1 & n <= 10) = 1;  
  
figure('Name', 'Input Signal x[n]');  
stem(n, x, 'b', 'filled');  
title('Discrete-Time Signal x[n]');  
xlabel('Sample Index (n)');  
ylabel('Amplitude');  
grid on;  
axis([0 25 -0.5 1.5]);
```

Plot of  $x[n]$  :

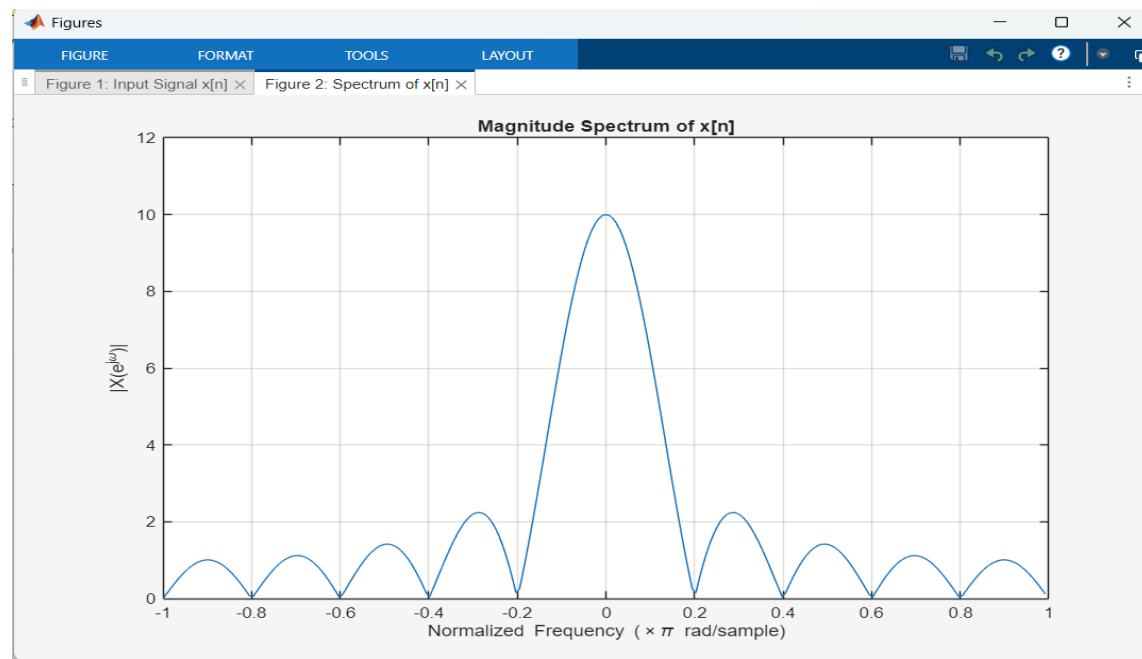


## Part 1: Calculate and plot the Spectrum.

MATLAB code :

```
ive > Dokumente > MATLAB
DspProj.m * x
C:\Users\Lenovo\OneDrive\Dokumente\MATLAB\DspProj.m
20 % Q1.1:
21 % Calculate Spectrum
22
23 N_fft = 256;
24 X_fft = fft(x, N_fft);
25
26 freq_axis = (-N_fft/2 : N_fft/2-1) * (2*pi/N_fft);
27 MagX = abs(fftshift(X_fft));
28
29 % Plot the Spectrum :
30 figure('Name', 'Spectrum of x[n]');
31 plot(freq_axis/pi, MagX);
32 title('Magnitude Spectrum of x[n]');
33 xlabel('Normalized Frequency (\times\pi rad/sample)');
34 ylabel('|X(e^{j\omega})|');
35 grid on;
36 axis([-1 1 0 12]);
37
```

Plot of  $x[n]$  :



## Part 2:

Compute the output  $y[n]$  for the length-4 filter ( $M=3$ ) whose coefficients are  $\{b_k\} = \{3, -1, 2, 1\}$ . The causal running average is a special case of the general causal difference equation

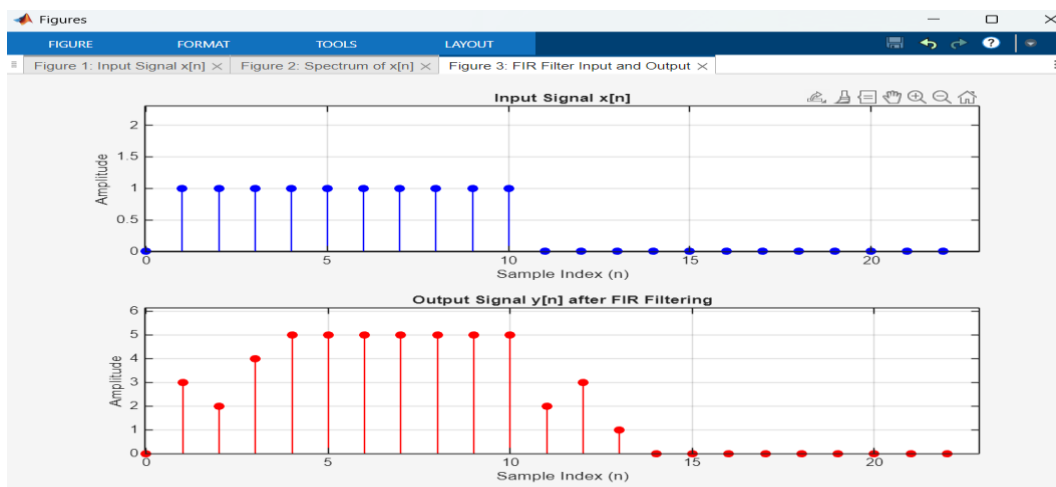
$$y[n] = \sum b x[n - k] \text{ ---(1)}$$

where the coefficients  $b_k$  are fixed numbers, usually the  $b_k$  coefficients are not all the same, and then we say that Equation (1) defines a weighted running average of  $M + 1$  samples.

MATLAB code :

```
DspProj.m * x
C:\Users\Lenovo\OneDrive\Dokumente\MATLAB\DspProj.m
39
40 %filter coefficients {bk}
41 b_fir = [3, -1, 2, 1];
42 a_fir = 1;
43
44 y = filter(b_fir, a_fir, x); %Output y[n] using the filter function
45
46 % Input Plot for comparing:
47 figure('Name', 'FIR Filter Input and Output');
48 subplot(2,1,1);
49 stem(n, x, 'b', 'filled');
50 title('Input Signal x[n]');
51 xlabel('Sample Index (n)');
52 ylabel('Amplitude');
53 grid on;
54 axis([0 30 -1 2]);
55
56 % output Plot:
57 subplot(2,1,2);
58 stem(n, y, 'r', 'filled');
59 title('Output Signal y[n] after FIR Filtering');
60 xlabel('Sample Index (n)');
61 ylabel('Amplitude');
62 grid on;
63 axis([0 30 -2 6]);
64
```

Plot of  $x[n]$  :



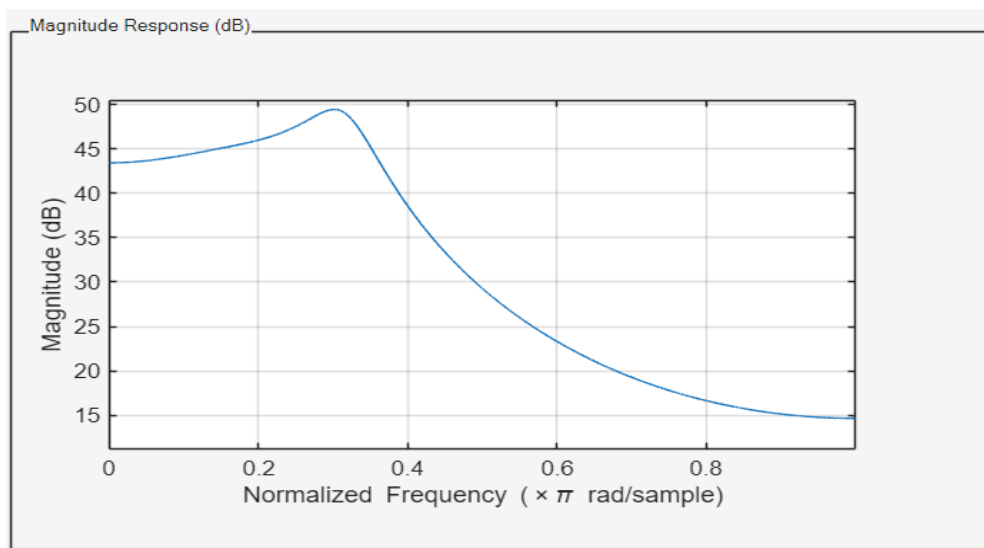
## Question 2: Exploring Minimum-Phase and All-Pass Systems in MATLAB

Using the MATLAB filter design tool, design your own example of

Part 1. A minimum phase system

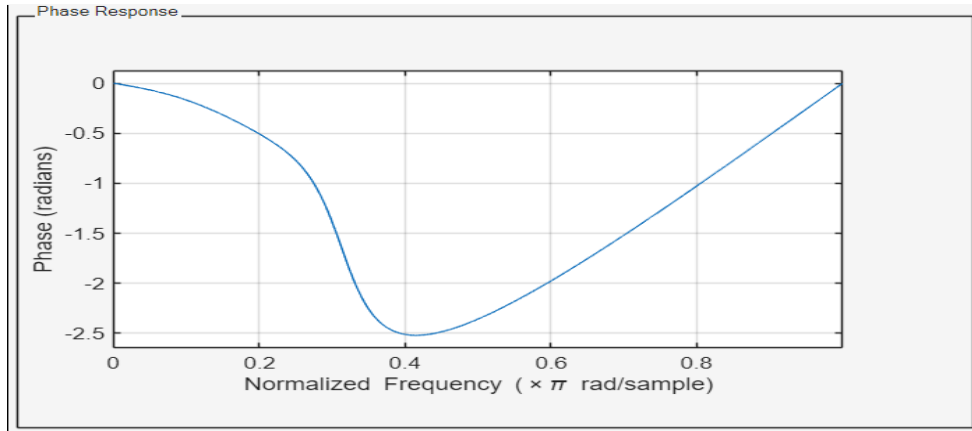
Use the tool to generate:

### 1. magnitude response



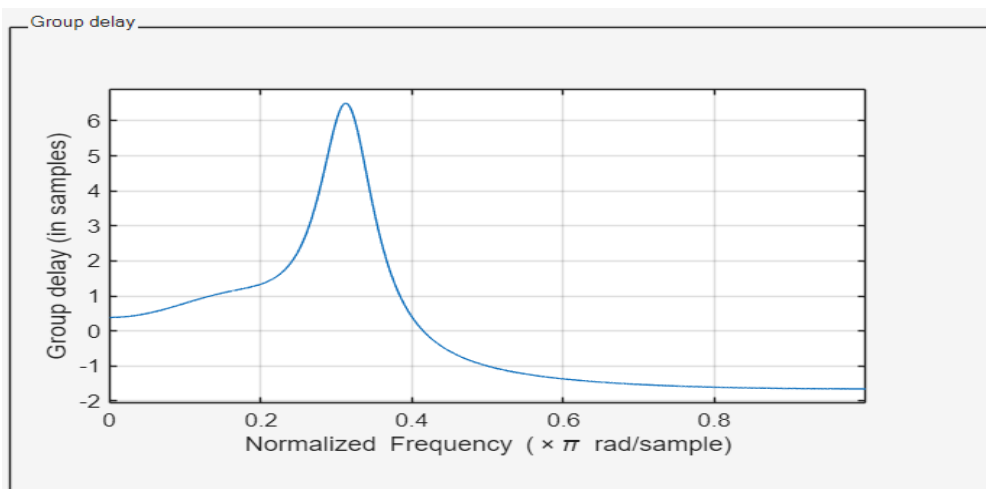
- The plot shows a low-pass filter behavior.
- The gain is high in the lower frequencies (below  $\sim 0.3\pi$  rad/sample), with a peak near  $0.3\pi$ .
- Beyond that, the response decreases steadily, reaching strong attenuation at higher frequencies.
- This confirms that the filter is frequency-selective.

## 2. phase response



- The phase curve is nonlinear across frequency.
- Unlike a linear-phase FIR, the slope is not constant.
- but, since this is a minimum-phase filter, the phase distortion is reduced compared to other realizations, and the group delay is minimized for this given magnitude response.

## 3. group delay



- The group delay is not flat (unlike linear-phase filters).
- It peaks around the transition band ( $\approx 0.3\pi$  rad/sample), indicating extra delay there.
- In the passband (low frequencies), the delay is relatively small, confirming the minimum-phase property (minimum possible delay for the same magnitude response).

#### 4. difference equation

```
>> B_Min
```

```
B_Min =
```

```
35.7143    0.0530    0.0710    0.0530    0.0280
```

```
>> A_Min
```

```
A_Min =
```

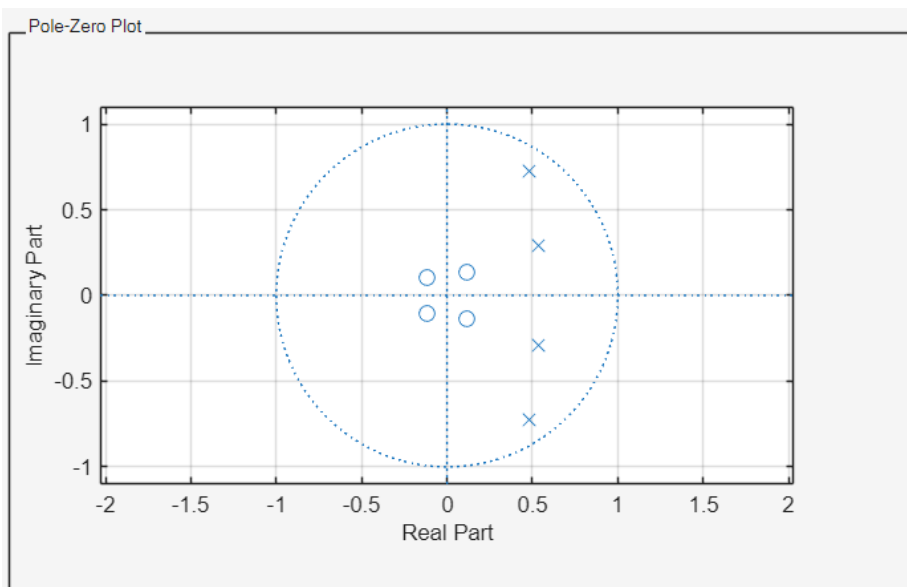
```
1.0000   -2.0260    2.1480   -1.1590    0.2790
```

➤ From your coefficients (B\_Min and A\_Min):

➤ The system equation is:

$$y[n] - 2.0260 y[n-1] + 2.1480 y[n-2] - 1.1590 y[n-3] + 0.2790 y[n-4] = 35.7143 x[n] + 0.0530 x[n-1] + 0.0710 x[n-2] + 0.0530 x[n-3] + 0.0280 x[n-4]$$

#### 5. Pole-Zero diagram

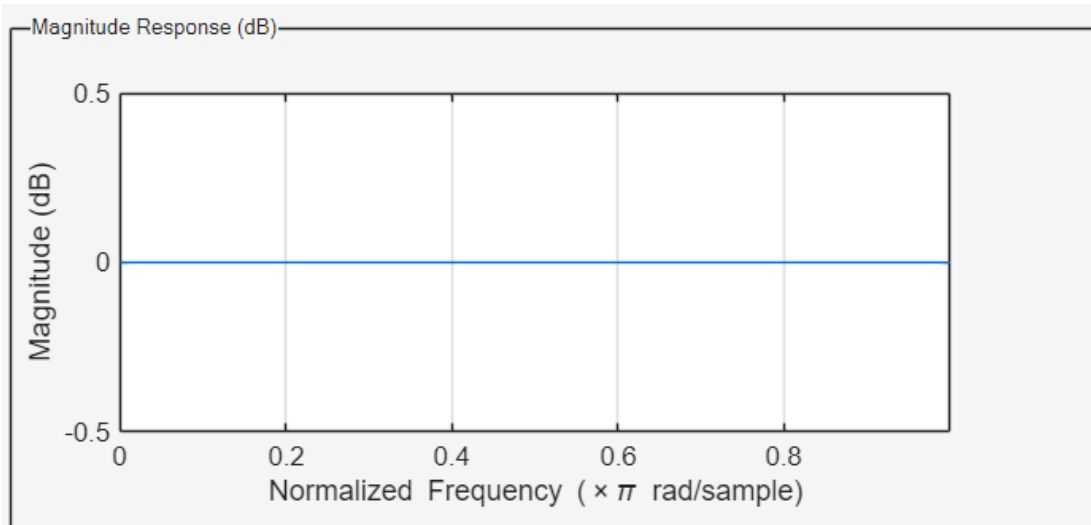


all zeros are inside the unit circle (ensuring causality & stability with minimal phase).

## Part 2. An all-pass system

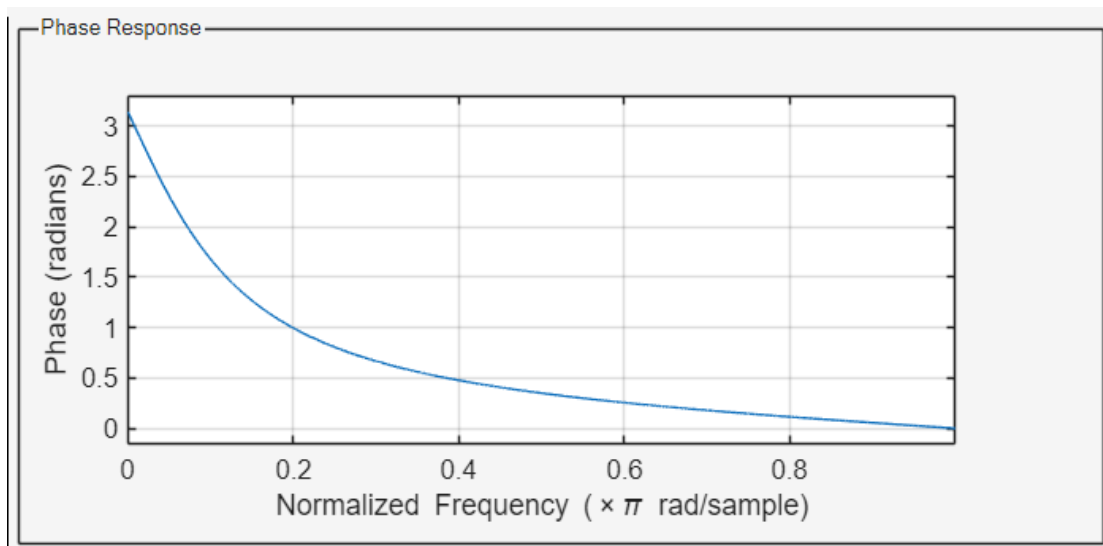
Use the tool to generate:

### 1. magnitude response



- Completely flat at 0 dB across all frequencies → confirms the all-pass property (no amplitude change).

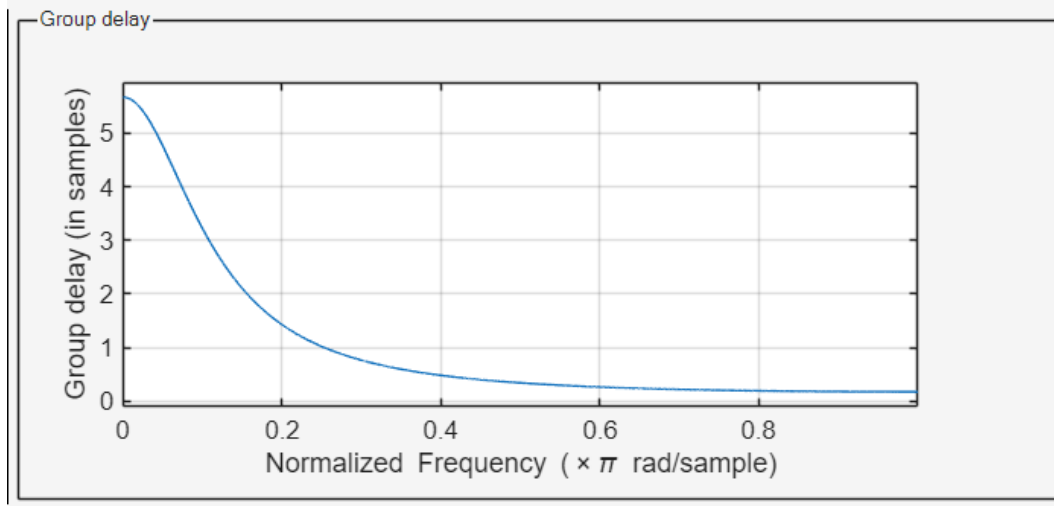
### 2. phase response



- Strongly nonlinear phase shift across frequency.
- The filter only affects phase, not magnitude.



### 3. group delay



- The plot is not a flat horizontal line. It has a distinct peak at the transition band, meaning different frequencies are delayed by different amounts.
- This non-linear phase response is characteristic of IIR filters, which are efficient but can introduce phase distortion.
- In contrast, a linear-phase filter would have a constant group delay (a flat line), meaning all frequencies are delayed by the same amount, thus avoiding phase distortion.

### 4. difference equation

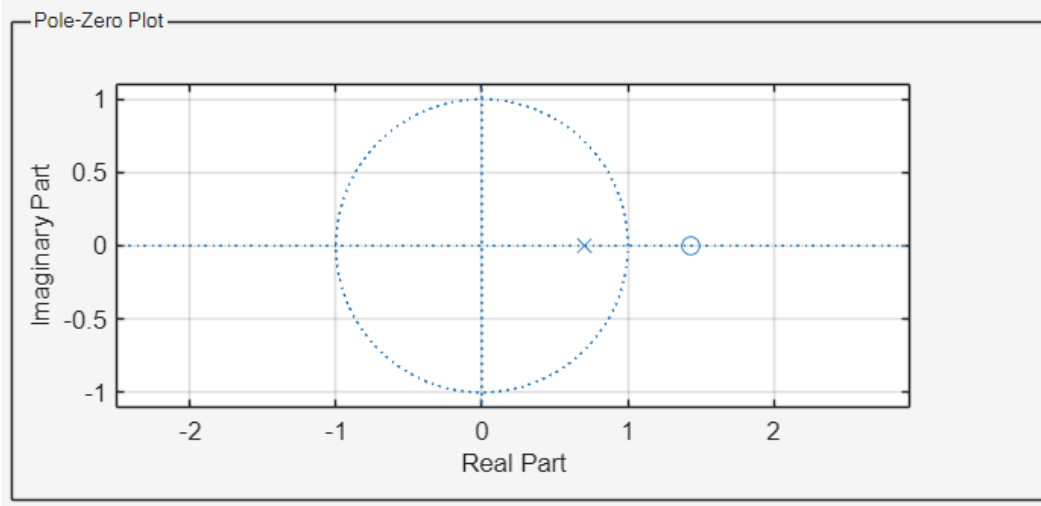
#### Command Window

```
A_All =  
    1.0000    -0.7000  
  
>> A_All  
A_All =  
    1.0000    -0.7000  
  
>> B_All  
B_All =  
    0.7000    -1.0000
```

The system equation is:

$$y[n] + 0.7000 y[n-1] = 0.7000 x[n] - 1.0000 x[n-1]$$

## 5. Pole-Zero diagram



every pole inside the unit circle has a reciprocal zero outside (mirror symmetry), which enforces unity magnitude.

What do you observe about the magnitude responses?

- **Minimum-phase system:**

The magnitude response shows a low-pass shape — it has higher gain at lower frequencies and attenuates as frequency increases. This is typical for a designed IIR filter.

- **All-pass system:**

The magnitude response is completely flat at 0 dB across all frequencies. This is the defining property of an all-pass filter: it does not alter signal amplitude, only phase.

How do the phase responses differ?

- **Minimum-phase system:**

The phase response is nonlinear, but it is associated with a reduced group delay compared to a linear-phase FIR of the same magnitude response. This means it still distorts phase, but with minimum possible delay for that magnitude response.

- **All-pass system:**

The phase response is highly nonlinear and varies strongly with frequency. Even though the magnitude is flat, the filter introduces frequency-dependent phase shifts and dispersion. This causes the group delay to vary across frequencies.