

PRACTICAL 1

Title: Random Variable

find the mean and variance for the following

a)

x	-1	0	1	2
$p(x)$	0.1	0.2	0.3	0.4

solution:

x	$p(x)$	$x.p(x)$	$E(x)^2$	$[E(x)]^2$
-1	0.1	-0.1	0	0.01
0	0.2	0	0	0
1	0.3	0.3	0.3	0.09
2	0.4	0.8	1.6	0.64
Total		$\sum x = 1$	$\sum x.p(x) = 1$	$\sum E(x)^2 = 2$
				$\sum [E(x)]^2 = 0.74$

$\therefore \text{Mean} = E(x) = \sum x_i \cdot p(x) = 1$

$$\begin{aligned}\therefore \text{Variance} &= V(x) = \sum E(x)^2 - \sum [E(x)]^2 \\ &= 2 - 0.74 \\ &= 1.24\end{aligned}$$

$\therefore \text{Mean } E(x) = 1 \text{ and Variance } V(x) = 1.24$

x	-1	0	1	2
$p(x)$	$1/8$	$1/8$	$1/4$	$1/2$

Solution :

x	$p(x)$	$x \cdot p(x)$	$E(x)^2$	$[E(x)]^2$
-1	$1/8$	$-1/8$	$1/8$	$1/64$
0	$1/8$	0	0	0
1	$1/4$	$1/4$	$1/4$	$1/16$
2	$1/2$	1	2	1
Total	$\Sigma = 1$	$\Sigma = 9/8$	$\Sigma = 19/8$	$\Sigma = 69/64$

$$\therefore \text{Mean} = E(x) = \sum x \cdot p(x) = 9/8$$

$$\therefore \text{variance } v(x) = \sum E(x)^2 - \sum [E(x)]^2$$

$$= \frac{19}{8} - \frac{69}{64}$$

$$= \frac{152 - 69}{64}$$

$$= \frac{83}{64}$$

$$\therefore \text{Mean } E(x) = 9/8 \text{ and variance } v(x) = 83/64$$

x	-3	10	15
$p(x)$	0.4	0.35	0.25

Solution :

x	$p(x)$	$x \cdot p(x)$	$E(x)^2$	$[E(x)]^2$
-3	0.4	-1.2	3.6	1.44
10	0.35	3.5	35	12.25
15	0.25	3.75	56.25	14.0625
Total	$\Sigma = 1$	$\Sigma = 6.05$	$\Sigma = 94.85$	$\Sigma = 27.7525$

$$\therefore \text{Mean} = E(x) = \Sigma x \cdot p(x) = 6.05$$

$$\begin{aligned}\therefore \text{Variance } v(x) &= \Sigma E(x)^2 - \Sigma [E(x)]^2 \\ &= 94.85 - 27.7525 \\ &= 67.0975\end{aligned}$$

$$\therefore \text{Mean } E(x) = 6.05 \text{ and Variance } v(x) = 67.0975$$

- Q2. If $p(x)$ is pmf of a random variable x . If $p(x)$ represents pmf for random variable x . find value of k . Then evaluate mean and variance.

Solution : As $p(x_i)$ is a pmf it should satisfy the properties

of pmf which are

- a). $p(x_i) > 0$ for all sample space
- b). $\sum p(x_i) = 1$

PRACTICAL 1:

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Solution :

x	p(x)	x.p(x)	$E(x)^2$	$[E(x)]^2$
-1	0.1	-0.1	0	0.01
0	0.2	0	0	0
1	0.3	0.3	0.3	0.09
2	0.4	0.8	1.6	0.64
Total	$\sum p = 1$	$\sum x = 1$	$\sum E(x)^2 = 2$	$\sum [E(x)]^2 = 0.74$

∴ Mean = $E(x) = \sum x_i p(x) = 1$

$$\begin{aligned} \therefore \text{Variance } V(x) &= \sum E(x)^2 - [E(x)]^2 \\ &= 2 - 0.74 \\ &= 1.24 \end{aligned}$$

∴ Mean $E(x) = 1$ and Variance $V(x) = 1.24$

EE

x	-1	0	1	2
$P(x)$	$1/8$	$1/8$	$1/4$	$1/2$

Solution :

x	$P(x)$	$x \cdot P(x)$	$E(x)^2$	$[E(x)]^2$
-1	$1/8$	$-1/8$	$1/8$	$1/64$
0	$1/8$	0	0	0
1	$1/4$	$1/4$	$1/4$	$1/16$
2	$1/2$	1	2	1
Total	$\Sigma = 1$	$\Sigma = 9/8$	$\Sigma = 19/8$	$\Sigma = 69/64$

$$\therefore \text{Mean} = E(x) = \sum x \cdot P(x) = 9/8$$

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$P(x)$	0.4	0.35	0.25

Solution :

x	$P(x)$	$x \cdot P(x)$	$E(x)^2$	$[E(x)]^2$
-3	0.4	-1.2	3.6	1.44
10	0.35	3.5	35	12.25
15	0.25	3.75	56.25	14.0625
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$$\therefore \text{Mean } E(x) = 6.05 \text{ and Variance } v(x) = 67.0975$$

~~If $P(x)$ is pmf of a random variable x . If $P(x)$ represents pmf for random variable x . find value of k . Then evaluate mean and variance.~~

Solution : As $P(x_i)$ is a pmf it should satisfy the properties of pmf which are

$$\begin{aligned}P(x_i) &> 0 \text{ for all sample space} \\ \Sigma P(x_i) &= 1\end{aligned}$$

7.6

x	-1	0	1	2
$P(x)$	$k+1/13$	$k/13$	$1/13$	$k-4/13$

$$\therefore \sum P(x_i) = 1 = \frac{k+1}{13} + \frac{k}{13} + \frac{1}{13} + \frac{k-4}{13}$$

$$\frac{1}{13} = k+1+k+1+k-4$$

$$13 = 3k - 2$$

$$15 = 3k$$

$$k = 5$$

x	$P(x)$	$x \cdot P(x)$	$E(x)^2$	$[E(x)]^2$
-1	$6/13$	$-6/13$	$6/13$	$36/169$
0	$5/13$	0	0	0
1	$1/13$	$1/13$	$1/13$	$1/169$
2	$1/13$	$2/13$	$4/13$	$4/169$
Total	$\Sigma = 1$	$\Sigma = -3/13$	$\Sigma = 11/13$	$\Sigma = 41/169$

$$\text{Mean} = E(x) = \sum x \cdot P(x) = \frac{-3}{13}$$

$$\therefore \text{Variance} = V(x) = \sum E(x)^2 - \sum [E(x)]^2$$

$$= \frac{11}{13} - \frac{41}{169}$$

$$= \frac{143 - 41}{169}$$

$$= \frac{102}{169}$$

$$\therefore \text{Mean} = -3/13 \text{ & variance} = 102/169$$

Q2. The P.M.F of random variable X is given by ...

x	-3	-1	0	1	2	3	5	8
$p(x)$	0.1	0.2	0.15	0.2	0.1	0.15	0.05	0

Solution :

x	-3	-1	0	1	2	3	5	8
$p(x)$	0.1	0.2	0.15	0.2	0.1	0.15	0.05	0.05
$F(x)$	0.1	0.3	0.45	0.65	0.85	0.90	0.95	1.0

$$\begin{aligned}
 \text{Q1 } P(-1 \leq x < 2) &= P(2 \leq x) - P(x < -1) + P(x = -1) \\
 &= F(x_b) - F(x_a) + p(a) \\
 &= F(2) - F(-1) + p(-1) \\
 &= 0.75 - 0.3 + 0.2 \\
 &= 0.25
 \end{aligned}$$

$$\begin{aligned}
 \text{Q2 } P(1 \leq x \leq 5) &= F(x_b) - F(x_a) + p(a) \\
 &= F(5) - F(1) + p(1) \\
 &= 0.95 - 0.65 + 0.2 \\
 &= 0.15
 \end{aligned}$$

$$\begin{aligned}
 \text{Q3 } P(x \leq 2) &= P(x = -3) + P(x = -1) + P(x = 0) + P(x = 1) + P(x = 2) \\
 &= 0.1 + 0.2 + 0.15 + 0.2 + 0.1 \\
 &= 0.75
 \end{aligned}$$

$$\begin{aligned}
 \text{Q4 } P(x \geq 0) &= 1 - F(0) + p(0) \\
 &= 1 - 0.45 + 0.15 \\
 &= 0.40
 \end{aligned}$$

58.

Let f be continuous random variable with PDF

$$\therefore f(x) = \frac{x+1}{2} \quad -1 < x < 1$$

Obtain CDF of x

Solution: By definition of CDF
we have

$$\begin{aligned} F(x) &= \int_{-1}^{x+1} t dt \\ &= \int_{-1}^x \frac{u+1}{2} du \\ &= \frac{1}{2} \left(\frac{1}{2} x^2 + x \right) \text{ for } -1 \leq x \leq 1 \end{aligned}$$

Hence the CDF is

$$\begin{aligned} F(x) &= 0 \quad \text{for } x < -1 \\ &= \frac{1}{4} x^2 + \frac{1}{2} x \quad \text{for } -1 \leq x \leq 1 \\ &= 1 \quad \text{for } x > 1 \end{aligned}$$

Q5. let F be continuous random variable with P.d.f

$$\therefore f(x) = \begin{cases} \frac{x+2}{18} & -2 \leq x < 4 \\ 0 & \text{otherwise} \end{cases}$$

Calculate c.d.f

Solution: By definition of c.d.f we have

$$F(x) = \int_{-2}^x t dt$$

$$= \int_2^x \frac{x+2}{18} dx$$

$$= \frac{1}{18} \left(\frac{1}{2} x^2 + 2x \right)$$

Hence c.d.f is

$$F(x) = 0 \quad \text{for } x < -2$$

$$= \frac{1}{18} \left(\frac{1}{2} x^2 + 2x \right)$$

$$\text{for } -2 \leq x < 4$$

$$= 1 \quad \text{for } x \geq 4$$

G.F.

Practical 2

Title: Binomial Distribution

An unbiased coin is tossed 4 times calculate
of obtaining no head, atleast one head and
one tail.

No HEAD :

```
> dbinom(0, 4, 0.5)
```

```
[1] 0.0625
```

ATLEAST ONE HEAD

```
> 1 - dbinom(0, 4, 0.5)
```

```
[1] 0.9375
```

More than one tail :

```
pbinom(1, 4, 0.5, lower.tail = F)
```

```
[1] 0.9375
```

The probability that student is accepted to a college is 0.3. If 5 students supply, what's probability of atleast 2 are accepted.

```
> pbinom(2, 5, 0.3)
```

```
[1] 0.83692
```

- Q3. An unbiased coin is tossed 6 times the probability of head at any toss = 0.3. let n be no of heads that comes up. Calculate $P(X=2)$, $P(X=3)$, $P(1 < X < 5)$

> $\text{dbinom}(2, 6, 0.3)$

[1] 0.324135

> $\text{dbinom}(3, 6, 0.3)$

[1] 0.18522

> $\text{dbinom}(2, 6, 0.3) + \text{dbinom}(3, 6, 0.3) + \text{dbinom}(4, 6, 0.3)$

[1] 0.74373

- Q4. For $n=10$, $p=0.6$, evaluate binomial probabilities and plot the graphs of pmf and cdf.

> $x = \text{seq}(0, 10)$

> $y = \text{dbinom}(x, 10, 0.6)$

? y

[1]	0.0001048	0.0015728640	0.0106168320
	0.042473280	0.1114767360	0.2006581248
	0.2598226560	0.2149908480	0.1209323520
	0.0403107840	0.0060466176	

> Plot $(x, y, x\text{lab} = "Sequence", y\text{lab} = "probabilities", "D")$

> $x = \text{seq}(0, 10)$

> $y = \text{dbinom}(x, 10, 0.6)$

> plot(x, y, xlab = "Sequence", ylab = "probabilities", "c")

pch = 1()

Q.

5. Generate a random sample of size 10 for $B(8, 0.3)$. Find the mean and the variance of the sample.

```
> rbinom(8, 10, 0.3)
[1] 2 2 3 4 3 4 2 3
> mean(rbinom(8, 10, 0.3))
[1] 2.375
> var(rbinom(8, 10, 0.3))
[1] 1.696469.
```

26. The probability of men hitting the target if he shoots 10 times what is the probability he hits the target exactly 3 times, probability he hits target atleast one time

```
> dbinom(3, 10, 0.25)
[1] 0.2502829
> 1 - dbinom(1, 10, 0.25)
[1] 0.8122883
```

27. Bits are sent for communication channel in packets of 12. If the probability of bit being corrupted what is the probability of no more than 2 bits corrupted in a packet?

```
> pbinom(2, 12, 0.1, lower.tail = F) + dbinom(2, 12, 0.1, 1)
[1] 0.3409977.
```

Practical 3 - Normal Distribution. 43

- Q1 A normal distribution of 100 students with mean marks 40 and s.deviation 15. find the no. of students whose marks are
 ① Less than 30 ② 40 and 70 ③ 25 and 35
 ④ more than 60.

$$\text{mean} = 40$$

$$s.d = 15$$

$$0.5 - \text{pnorm}(5.0, 40, 15)$$

$$0.2524725$$

$$\text{pnorm}(10, 40, 15) - \text{pnorm}(40, 40, 15)$$

$$0.4839377$$

$$\text{pnorm}(35, 40, 15) - \text{pnorm}(25, 40, 15)$$

$$0.2107861$$

more than 60

$$\text{pnorm}(60, 40, 15, \text{lower.tail} = F)$$

$$0.09121122$$

- Q2 If the random variable 'x' follows to the normal distribution with mean 10, variance 100, s.deviation 10.
 Find ① $P(x < 70)$ ② $P(x > 65)$, ③ $P(x < 30)$
 ④ $P(35 < x < 60)$ ⑤ $P(20 < x < 32)$

~~$\text{pnorm}(70, 50, 10)$~~

~~0.1772499~~

~~$\text{pnorm}(65, 50, 10, \text{lower.tail} = F)$~~

~~0.0008072~~

~~$\text{pnorm}(30, 50, 10)$~~

~~0.0224013~~

$$\text{pnorm}(60, 50, 10) - \text{pnorm}(35, 50, 10) \Rightarrow 0.9745$$

Ex

$$\text{pnorm}(31, 50, 10) = \text{pnorm}(20, 50, 10)$$
$$0.05482120$$

Let $x \sim (60, 400)$, find k_1 and k_2 such that $P(x < k_1) = 0.1$ and $P(x > k_2) = 0.8$

$$\text{qnorm}(0.1, 160, 20)$$
$$165.0669$$

$$\text{qnorm}(0.2, 160, 20)$$
$$143.1671$$

A random variable x follows normal distribution with $\mu = 10$, $\sigma^2 = 2$. Generate 100 observations and find mean, median and variance.

$$\text{rnorm}(100, 10, 2)$$

$$\text{mean} = 9.911$$

$$\text{median} = 9.979$$

$$\text{variance} = 4.132851$$

Write a command to generate 10 random nos normally distribution with mean 50 std dev 10.

v. find sample mean and median.

$$\text{rnorm}(10, 50, 10)$$

$$\text{mean} = 51.45702$$

$$\text{median} = 51.70231$$

$$\text{variance} = 14.68388$$

PRACTICAL 4

Sample mean and std. deviation given single population

Suppose the load level on the cookie bags states that it has almost 2 gms of saturated fat in a single cookie. In a sample of 35 cookies, it was found that mean and saturated fat per cookie = 2.1 gm. Assume that the sample std. deviation is 0.3 at 1% level of significance can be rejected the claim on food label.

$$\sigma = 0.3$$

$$n = 35$$

$$\bar{x} = 2.1$$

$$N = 2$$

$$H_0 \text{ (null hypothesis)} = \mu < 2$$

$$H_1 \text{ (alt-hypothesis)} = \mu > 2$$

$$z = \frac{2.1 - 2}{\frac{0.3}{\sqrt{35}}} = 1.972027$$

$$p\text{-value} = 1 - \text{pnorm}(z)$$

$$= 0.0243$$

Reject the null hypothesis : p-value < 0.05

\therefore Accepted alternate hypothesis.

Q2. A sample of 100 customers was randomly selected and was found that average spending was \$45. The SD = 30 using 0.05 level of significance you conclude that the avg. spent by the customer is more than 250/- whereas the restaurant thinks it is not > 250/-

$$\bar{x} = 275, \mu = 250, \sigma = 30, n = 100$$

$$H_0: \mu < 250$$

$$H_1: \mu > 250$$

$$Z = \frac{\bar{x} - \mu}{\sigma}$$

$$= \frac{275 - 250}{30} = 8.33$$

$$\Rightarrow P(Z > 8.33) = F$$

$$\therefore \text{p-value} = 2.305236e-13$$

\Rightarrow Reject the null hypothesis : p-value < 0.05
 \therefore Accept the alternate hypothesis ($\mu > 250$)

Q3. A quality control engineer finds that sample of 100 have average life of 470 hours. Assuming population whether the population mean is 480 hours. population mean < 480 hours. at $\alpha \rightarrow 0.05$.

$$n = 100, \bar{x} = 470, \mu_0 < 480, \sigma = 25, \mu = 480$$

$$Z = \frac{\bar{x} - \mu}{\sigma/\sqrt{n}} = -4$$

$$P(Z < -4) = 1$$

$$= 6.11257 \approx .05$$

Reject all null hypothesis $\therefore p < 0.05$

Accept the alternate hypothesis ($\mu < 180$)

Q4. A principal at school claiming that the IQ is 100 of the students. A random sample of 30 students whose IQ was found to be 112. The SD of population is 15. Test claim of principal.

Method 1 tail test

$$H_0 = \mu = 100$$

$$H_1 = \mu > 100$$

$$\bar{x} = 112, SD = 15, \mu = 100, n = 30$$

$$Z = \frac{\bar{x} - \mu}{\frac{\sigma}{\sqrt{n}}}$$

$$= 112 - 100$$

$$\frac{15}{\sqrt{30}}$$

~~$$Z = 4.38179$$~~

$$P \text{ value} = 5.885 \text{ Re-act}$$

Reject the null hypothesis = claims of principal ($\mu = 100$)

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Method 2 = 2 tail test

$$H_0 = \mu = 100$$

$$H_1 = \mu \neq 100$$

$$\rightarrow \text{pvalue} = 2 \times (1 - \text{norm}(\text{abs}(z))) = 1.172134$$

\rightarrow Reject the null hypothesis if pvalue < 0.05

* Single population portion :

If it is believed that coin is fair. The coin is tossed 40 times; 25 times - Head occurs. Whether the coin is fair or not at 95%

>> $2 = \rho - \rho_0 \rightarrow$ probability of population

$$\sqrt{\frac{\rho_0(1-\rho_0)}{n}}$$

$$\rho_0 = 0.5$$

$$\rho_0 = 1 - \rho_0 = 0.5$$

$$\rho = \frac{2S}{n} = 0.7$$

$$n = 40$$

$$\Rightarrow z = 0.7 - 0.5$$

$$\sqrt{\frac{0.5 \times 0.5}{40}}$$

$$H_0 = \mu = 0.5$$

$$H_1 = \mu \neq 0.5$$

>> pvalue = $2 \times (1 - \text{norm}(\text{abs}(z)))$

$$\therefore \text{pvalue} = 0.01141204$$

\rightarrow Reject the null hypothesis if $p < 0.05$

Accept the alternate hypothesis,

Practical - 5

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Title : Chi Square Test.

Use following data to test whether the attribute conditions of home and child are independent.

Condition of Home.	
	dirty
Clean	70
F. clean	20
dirty	35

H_0 = Both are independent, H_1 = Both are dependant

- > $x = c(70, 35)$
- > $y = c(50, 20, 45)$
- > $z = \text{data.frame}(x, y)$
- > z

[1]	x	y
1	70	50
2	80	20
3	35	45

> `chisq.test(z)`

Pearson's chi squared' test

~~data.z~~

$$\chi^2 - \text{squared} = 25.646, \text{ df} = 2, \text{ p-value} = 2.998$$

∴ Reject the null hypothesis
Both are dependent.

Q2. A dice is tossed 120 times and following results are obtained.

No: of terms	Frequency
1	30
2	25
3	18
4	10
5	22
6	15

Test the hypothesis that dice is unbiased

$\therefore H_0 = \text{dice is tossed}$

$H_1 = \text{dice is biased}$

$\rightarrow \text{Obs} = c(30, 25, 18, 10, 22, 15)$

$\rightarrow \chi^2 = \sum (\text{obs})^2 / \text{length(Obs)}$

$\rightarrow \text{exp}$

$c]$ 20

$\rightarrow \chi^2 = \text{sum}((\text{obs} - \text{exp})^2 / \text{exp}))$

$\rightarrow \text{pchisq}(\chi^2, \text{df} = \text{length(Obs)} - 1)$

$c]$ 0.956659

$\therefore \text{Accept the null hypothesis}$

$\therefore \text{dice is unbiased}$

Q3. An IQ test was conducted and the students were observed before and after training the result are followed:

before	after
110	120
120	118
123	125
132	134
125	121

Test whether there is change in the IQ after the training.

$H_0 = \text{no change in IQ}$
 $H_1 = \text{IQ increased after training}$

```
> a = c(120, 118, 125, 134, 121)
> b = c(110, 120, 123, 132, 125)
> 2 = sum((b - a)^2) / a
> pchisq(2, df = length(b) - 1)
```

```
[1] 0.1135959
```

Accept the null hypothesis

~~There is change in IQ after training.~~

Q4.

80

graduate
online
face to face

Undergrad
20
5

40

Is there any association
for type of education

i. H_0 : Independent

ii. H_1 : Dependent

> $x = c(20, 40, 25, 15)$

> $z = \text{matrix}(x, \text{nrow} = 2)$

> $\text{chisq.test}(z)$

Pearson's Chi squared test with
Yates continuity correction

data: z

X: squared = 18.05, df = 1, p-value = 2.157e-05

∴ Reject null hypothesis

∴ Both are dependent

A dice is tossed 180 times

No of terms frequency

1 20

2 30

3 35

4 40

5 12

6 43

Test the hypothesis that dice is unbiased

H_0 : dice is biased
 H_1 : dice is unbiased

$x = c(20, 30, 35, 40, 12, 43)$

χ^2 -test(x)
 Chi squared test for given probabilities

data: x

χ^2 -squared = 23.933, df = 5, p-value = 0.000223,

\therefore Reject null hypothesis
 \therefore Dice is unbiased.

~~Next~~

Ques. let $\mathbf{x} = 3366, 3337, 3361, 3410, 3316, 3355, 3348, 3356, 3324, 3382, 3377, 3355, 3408, 3401, 3398, 3424, 3383, 3374, 3384, 3374$.

Write R command for following to test hypo.

1. $H_0: \mu = 3400, H_1: \mu \neq 3400$
2. $H_0: \mu = 3400, H_1: \mu > 3400$
3. $H_0: \mu = 3400, H_1: \mu < 3400$
at 95% level of confidence. Also check at 94% level of confidence.

→ ① $H_0: \mu = 3400$

$H_1: \mu \neq 3400$

> $\mathbf{x} = c(3366, 3337, 3361, 3410, 3316, 3357, 3356, 3326, 3382, 3323, 3355, 3408, 3401, 3398, 3424, 3383, 3374, 3384, 3374)$

> $t.test(x, mu = 3400, alter = "two.sided", conf.level = 0.95)$

onc sample t-test.

data: \mathbf{x}

~~t = -4.48 (S, df = 19, P value = 0.000222
alternative hypothesis: true mean is not equal to 3400)~~

95 percent confidence level: 3961.717 3316.117

Sample

mean of $y = 3373.95$

: Reject H_0

: Accept H_1

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> $t \cdot \text{test}(x, \text{no} = 3400, \text{alter} = \text{"two.side"})$

conf.level = 0.97)

one sample t-test

data : x

$t = -4.4865$, $df = 19$, $p\text{-value} = 0.002528$ alternative

hypothesis : true mean is not equal to 3400

97 percent confidence level 3360.33

sample estimate

Mean of $x = 3373.95$

: Reject H_0

: Accept H_1

(2) $\text{t-test}(x, \mu_0 = 3400, \text{alter} = \text{"greater"}, \text{conf.level} = 0.95)$

one sample t-test.

data : x

$t = 4.4865$, $df = 19$, $p\text{-value} = 0.9999$

sample estimate

Mean of $x: 3373.95$

: Accept H_0



Q3

t-test (x, nu = 3400, alter = "greater", Sent, 1e 1
one sided t-test)

data: x

t = 4.4865, df = 19, p-value = 0.9999 alternative hypothesis: true mean is greater than 3400
3397.337 Inf

Sample estimates:

mean of x: 3393.98

Accept H₀

H₀ = M = 3400

H₁ = M < 3400

> t.test(x, mu = 3400, alter = "less", conf.level = 0.95)
one sided t-test

data x

t2 = 4.4865, 15, p-value = 0.0001256

alternative hypothesis: true mean is less than

95 percent confidence level

Int 3383.99

Reject H₀

Sample estimate

mean of x:

Reject H₁

One sided t-test

data : x

$$4.4865 = 7$$

$= 4.4265$, $df = 19$, $p\text{value} = 0.0001264$ alternative hypothesis : True mean is less than 47;. confidence level.

INT 338.5563

Sample estimates

Mean of \bar{X} 3373.95

∴ Reject H_0

.. Accept H₁

Below use the data of given width of 2 different data

DATA (A) :- 25, 32, 30, 43, 24, 14, 32, 24, 31, 31, 35
 DATA (B) :- 44, 34, 22, 10, 47, 51, 40, 30, 30, 32, 35, 18

$$H_0: -a \cdot b = 0$$

$$\begin{aligned} & a = c(25, 33, \dots, \dots, \dots, 31, 35) \\ & b = c(44, \cancel{39}, 24, \dots, \dots, 38, 18) \end{aligned}$$

~~t.test(a, b paired = T, alter = "two.sided", cat~~

$$\text{level} = 0.98$$

paired t-test

alternate hypothesis : true difference in mean is not equal to 0.

95% confidence level

$$-14.247330 \pm 0.033947$$

Sample estimate

$$-3.166660$$

\therefore Accept H_0

\therefore there is no difference in weight.

Q3. 2 student gave the test, after 1 month, they again gave the test after coaching so the marks given show that students are benefited by coaching.

$$E_1 : (23, 20, 19, 21, 28, 20, 19, 17, 23, 16, 19)$$

$$E_2 : (24, 19, 22, 20, 22, 20, 20, 31, 20, 17)$$

$$E_1 = (23, 20, 19, 21, \dots, 10, 19)$$

$$E_2 = (24, 19, 22, \dots, 20, 17)$$

t. test (E_1, E_2 , paired T. alter alter "are confron-

Paired t-test

data = f, and β

$t = 1.4832$, df = 10 P-value = 0.08441

alternative hypothesis true difference is less than

99% confidence level

Int 0.863333

Sample estimate

Mean of the difference
 -1

Accept No.

④ Two days of BP was given and data was collected

$D_1 = 0.3, -1.8, -0.2, -1.2, -0.1, -3.2, 0.2$

$D_2 = 1.9, 0.8, 1.1, -0.1, 4.4, 5.5, 0.2$

check which 2 days have the two days have same effect

$H_0: D_1 = D_2$

$H_1: D_1 \neq D_2$

$D_1 = c(0.3, -1.8, \dots, -0.8, 0.3)$

$D_2 = c(1.9, 0.8, \dots, 4.4)$

. test

D₂

df=9, pvalue = 0.95238

hesis :- the difference

confidence level

t difference

1.58

H₀

H₁

difference in Salaries for the same job
different Companies

49958, 41997, 44310, 44310, 45740, 5644

58840, 4095, 522213, 47134, 43552

(A-B, Paired.T.alter = "two.sided")

(conf.level = 0.95)

data = LA and RB

t = 4.4569, df = 5, pvalue = 0.00666.

Practical No : 7.

Q1. Life expectancy in 10 region of Indian
2000 are given below. See whether the values
the 2 times are same.

1990 :- 37, 39, 46, 42, 45, 44, 46, 40, 50, 51

2000 :- 44, 45, 48, 43, 42, 49, 50, 41, 48, 52, 42, 51

$$H_0 = \sigma_1^2 = \sigma_2^2$$

$$H_1 = \sigma_1^2 \neq \sigma_2^2$$

$$S_1 = \{32, 34, 46, \dots, 50, 51\}$$

$$S_2 = \{44, 45, \dots, 52, 42\}$$

var. test(51, 52)

$$P. \text{ value} = 0.9176$$

17 005 ✓

Accept H_0 .

I :- (25, 28, 26, 22, 24, 31, 31, 26, 31)

II :- (30, 35, 21, 32, 23, 36, 25, 36, 32, 27).

~~$$H_0 = \sigma_1^2 = \sigma_2^2$$~~

~~$$H_1 = \sigma_1^2 \neq \sigma_2^2$$~~

~~$S_1 = \{25, 28, 26, 22, 24, 31, 31, 26, 31\}$~~

~~$S_2 = \{30, 35, 21, 32, 23, 36, 25, 36, 32, 27\}$~~

~~$$H_0 = \sigma_1^2 = \sigma_2^2$$~~

~~$$H_1 = \sigma_1^2 \neq \sigma_2^2$$~~

$$S_1 = c(25, 28, 24, 31, \dots, 31)$$

$$S_2 = c(30, 25, 31, \dots, 24)$$

pvalue = 0.5541

Accept H₀.

For the Roll. data the hypothesis for equality of 2 population mean "population variance".

$$H_0: \sigma_1^2 = \sigma_2^2$$

$$H_1: \sigma_1^2 \neq \sigma_2^2$$

$$H = c(173, 148, 145, 140, 181, 185, 125, 200)$$

$$u = c(180, 130, 120, 183, 187, 205)$$

v.value = 0.2259

t.test(x, y)

p.value = 0.8214

Accept H.

The foll. are the price of countries in the sample from recommended cities.

~~of shop Selected~~ from recommended cities.

$$\text{city A} = c(24, 10, 27, \dots, 26, 100)$$

$$\text{city B} = c(20, 20, 24, \dots, 81, 80)$$

$$x = c(24, 10, 27, \dots, 26, 100)$$

$$y = c(20, 20, 24, 20, 22, 20, 44, 20, 81, 20)$$

s.hapiro.test(x)

pvalue = 0.1559

18

$$p\text{ value} = 0.9304$$

$$H_0 = \sigma_1^2 = \sigma_2^2$$

$$\omega_1 = \sigma_1^2 \neq \sigma_2^2$$

$$r\text{ value} = 0.54249.$$

2 variance are not equal object H_0 Accept H_1

$$H_0 \bar{x}_1 = \bar{x}_2$$

$$x_1 \neq s_{x_2}$$

t. text $x_1, \text{var.equal=}\text{F}$)

t. test (y, var.equal = F)

Accept H_0 .

Q. Prepare a csv file in excel Import the file in and Apply the ttest cldscr the equality of variance or 2 data.

Obs : 01 : - (10, 15, 17, 11, ..., ..., 20)

Obs : 02 : (15, 14, 16, ..., ..., 19)

Data.

Obs : 01

10

15

14

16

11

12

19

20

Obs : 02

15

14

16

11

12

19

```
> attach(data)
> mean(bbs)
14.8333
```

```
> var.test(ohs1, ohs2)
```

$$p\text{-value} = 0.571$$

Accept H_0 .

Mean

Practical 8.

Non parametric Test

1. The times of failures in hrs of 10 random selected 9 volt battery of a certain company is as follows

28.9, 15.2, 28.7, 72.5, 48.6, 52.4, 32.1, 49.5, 62

Test the hypothesis that the population median is 63

$\therefore H_0: \text{median} = 63$

$\therefore H_1: \text{median} < 63$

$n = c(28.9, 15.2, 28.7, 72.5, 48.6, 52.4, 32.1, 49.5,$

62.1, 54.5)

$> SP = \text{length}(which(n) < 63)$)

$> SN = \text{length}(\text{which}(n \geq 63))$

$> SP$

$> SN$

$_1$

$> n = SP + SN$

$> 2 \text{binom}(0.5, n, 0.5)$

$\therefore 2 \text{binom} < SN$

$\therefore \text{Accept } H_0$

$\therefore \text{Median} = 63.$

The following data gives the weight of 40 students in random sample 41, 48, 57, 64, 46, 67, 54, 48, 69, 56

61, 57, 54, 50, 48, 65, 61, 66, 54, 50

48, 49, 62, 44, 49, 47, 55, 59, 63, 53

51, 67, 49, 60, 64, 53, 50, 48, 51, 52, 54

> SP = length(which(x>50))

> SP

> 25

> SN = length(which(x<50))

> SN

> 12

> n=SP+SN

> qbinom(0.05, n, 0.5)

14

$\therefore \cancel{qbinom} > SN$

\therefore Reject H₀.

38

- 23: The median age of tourist visiting a certain place is claim to had 41 yrs. A random sample of 40 tourists have the age.

$25, 29, 52, 48, 57, 34, 45, 36, 30, 49, 45, 31, 33, 55, 42$

> $s_p =$

$$\therefore H_0 = \text{median} = 41$$

$$H_1 = \text{median} \neq 41$$

> $x = c(25, 29, 52, 48, 57, 34, 45, 36, 31, 33, 55, 42)$

> $s_p = \text{length}(\text{which}(x < 41))$

> s_p

9

> $s_n = \text{length}(\text{which}(x < 41))$

> s_n

8

> $n = s_p + s_n$

> $\text{qbinom}(0.05, n, 0.5)$

5

2 binom Sn

Accept H_0 median ≈ 1

57

the times in numeric that has to wait until solution is given. Check whether the weight increases or stop using wilcox. That p & s.v. of sign pcat.

Solution $H_0 = \text{median} = 41$ you keep solving.
 $H_1 = \text{weight don't change}$

a = $c(25, 29, 52, 48, 57, 34, 45, 36, 31, 33, 55, 42)$

b = $c(72, 82, 72, 62, 73)$

> a.b-a

> x

-7, -7, 3, -4, -1

> wilcox.test(x, Mv=0)

p.value = 0.1786

pair, pValue > 0.05

H0

Accept H_0 .

58

Practical 8.

1. The times of failure in his, + 10 randomly selected 9 volt battery of a certain company is as follows
 $(28.9, 18.4, 28.4, 72.5, 48.6, 52.4, 37.6, 49.5, 62.1, 54.5)$

Test the hypothesis that the population median is 63 against alternative is then 63 at 5% of level of significance.

$$\therefore H_0 = \text{Median} = 63$$

$$H_1 = \text{Median} \neq 63$$

$$n = c(28.9, 18.2, 28.7, 72.5, 48.6, 52.4, 37.6, 49.7, 62.1, 54.5)$$

$$> S.P = \text{length} (\text{which } (x > 63))$$

$$> S.A = \text{length} (\text{which } (x < 63))$$

$$> S.P$$

$$> 2$$

$$> S.H$$

$$1$$

$$> Q = S.P + S.H$$

$$> Q \sim \text{binom}(0.08, n, 0.5)$$

$$\therefore Q \sim \text{binom} < S.H$$

Accept H_0

$$\text{Median} = 63$$

The following data gives the weight of 40 students in random sample.

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46, 44, 57, 64, 46, 54, 48, 69, 61, 57, 54, 50, 48, 65, 61, 66, 84, 50, 48, 44, 62, 47, 44, 47, 33, 34, 63, 53, 56, 67, 44, 60, 64, 33, 30, 48, 31, 32, 34

Use the sign test to test whether the median rate of population is 50 kg against alternative it is 150 kg.

$$\therefore H_0 = \text{median} = 50$$

$$H_1 = \text{median} \neq 50$$

$$x = c(46, 44, 57, 64, 46, 67, 54, 50, 48, 61, 57, 54, 50, 48, 65, 61, 66, 84, 50, 48, 44, 62, 47, 44, 47, 33, 34, 63, 53, 56, 67, 44, 60, 64, 33, 30, 48, 31, 32, 34)$$

$$> S.P = \text{length which } (x > 50)$$

$$> S.P$$

is

$$> S.H = \text{length which } (x < 50)$$

$$S.H$$

$$12$$

$$> n = S.P + S.H$$

$$> Q \sim \text{binom}(0.05, n, 0.5)$$

$$\therefore Q \sim \text{binom} > S.H$$

∴ Reject H_0 .

88) The median age of tourist visiting a certain place is claim to be 41 yrs. A random sample of 20 tourists have the age.

25, 24, 52, 48, 57, 34, 45, 36, 30, 49, 28, 39, 44, 46, 22, 45, 29, 42. Use the sign test to check the claim.

$$H_0: \text{median} = H_1$$

$$H_1: \text{median} \neq H_1$$

$\Rightarrow x = c(25, 29, 52, 48, 57, 39, 45, 36, 30, 44, 25, 44, 63, 32, 45, 28, 42)$

$\Rightarrow SP = \text{length}(\text{which}(x > 41))$

$\Rightarrow SP$

$\Rightarrow Sn = \text{length}(\text{which}(x > 41))$

$\Rightarrow Sn$

8

$$\Rightarrow n = SP + Sn$$

$$\Rightarrow \text{binom}(0.05, n, 0.5)$$

$$\begin{matrix} S \\ \text{binom} < Sn \end{matrix}$$

Accept H_0

$$\therefore \text{Median} = H_1$$

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The time in minutes that a patient has to wait to consultation is recommended as following is
24, 25, 20, 21, 32, 28, 12, 25, 24, 26.

We will use sign test to check whether median waiting test more than 20 or not.

Q. The following data gives the effects of 3 treatments.

$$T_1 : 2, 3, 3, 2, 6$$

$$T_2 : 10, 8, 7, 5, 10$$

$$T_3 : 10, 13, 14, 13, 15$$

Test the hypothesis that all treatments are equally effective.

$$H_0 = T_1 = T_2 = T_3$$

$$H_1 = T_1 \neq T_2 \neq T_3$$

$$a = c(2, 3, 7, 2, 6)$$

$$b = c(10, 8, 7, 5, 10)$$

$$c = c(10, 13, 14, 13, 15)$$

$$d = \text{data.frame}(a, b, c)$$

d

$$x = \text{as.matrix}(d)$$

$$e = \text{stack}(d)$$

$$\text{var}(\text{value} - \text{ind}, \text{data} = e)$$

$$\text{var}(\text{value} - \text{ind}, \text{data} = e)$$

$$p\text{-value} = 0.00062$$

\therefore Reject H_0 .

The life cycle of different brands of tyres is given. Test whether the driving test of all tyres is the same.

H_0 = life of all brands of tyres is same
 H_1 = life of all brands of tyres is not same.

$$a = c(20, 23, 18, 17, 22, 24)$$

$$b = c(19, 15, 11, 20, 15, 17)$$

$$c = c(21, 29, 22, 17, 20)$$

$$d = c(15, 14, 16, 18, 14, 16)$$

$$m = \text{list}(a, b, c, d)$$

m

$$e = \text{stack}(m)$$

$$m = \text{list}(p = a, q = b, r = c, s = d)$$

m

$$e = \text{stack}(m)$$

e

$$\text{var}(\text{value} - \text{ind}, \text{data} = e, \text{var.equal} = \text{TRUE})$$

$$p\text{-value} = 0.00438$$

\therefore Reject H_0 .

Q3
23. Three types of wax is applied for the protection of ears and no. of days of protection were noted. Test whether these are equally effective.

H₀ :- Equally effective.

H₁ :- Not equally effective.

$$a = c(44, 45, 46, 47, 48, 49)$$

$$b = c(40, 42, 41, 42, 43)$$

$$c = c(50, 53, 58, 59)$$

$$m = \text{list}(a=n, g=b, rs=c)$$

$$m
e = \text{stack}(m)$$

$$e
e = \text{oveway.test}(values = \text{ind}, data = e)$$

p. value :- 0.03822

∴ Reject H₀.

An experiment was concluded on 8 persons the observation were noted. Test the hypothesis that all groups have equal results on their health.

H₀ - equal result on their health.

H₁ - Not equal result.

$$a = c(23, 26, 51, 48, 58, 34, 29, 44)$$

$$b = c(22, 27, 29, 38, 46, 48, 49, 53)$$

$$c = c(84, 10, 38, 49, 56, 60, 56, 62)$$

$$d = \text{data.frame}(a, b, c)$$

$$x = \text{as.matrix}(x = d)$$

$$e = \text{stack}(d)$$

$$\text{aov(values ~ ind, data = e)}$$

$$\text{oveway.test(values ~ ind, data = e)}$$

$$p.value = 0.01633$$

∴ Reject H₀.