

**Tutorial Sheet 12: Systems of ODEs**

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(1) Solve the following systems of ODEs.

(a)  $x'_1 = x_1 + 2x_2$ ,  $x'_2 = \frac{1}{2}x_1 + x_2$

(b)  $x'_1 = -8x_1 - 2x_2$ ,  $x'_2 = 2x_1 - 4x_2$

(c)  $x'_1 = x_2$ ,  $x'_2 = -x_1 + x_3$ ,  $x'_3 = -x_2$

(2) Solve the following IVPs.

(a)  $x'_1 = 2x_1 + 2x_2$ ,  $x'_2 = 5x_1 - x_2$ ,  $x_1(0) = 0$ ,  $x_2(0) = 7$

(b)  $x'_1 = -14x_1 + 10x_2$ ,  $x'_2 = -5x_1 + x_2$ ,  $x_1(0) = -1$ ,  $x_2(0) = 1$

(3) Solve the following systems of ODEs.

(a)  $x'_1 = x_2 + e^{3t}$ ,  $x'_2 = x_1 - 3e^{3t}$

(b)  $x'_1 = -x_1 + x_2 + 10 \cos t$ ,  $x'_2 = -3x_1 - x_2 - 10 \sin t$

(c)  $x'_1 = x_1 + 4x_2 - 2 \cos t$ ,  $x'_2 = x_1 + x_2 - \cos t + \sin t$