

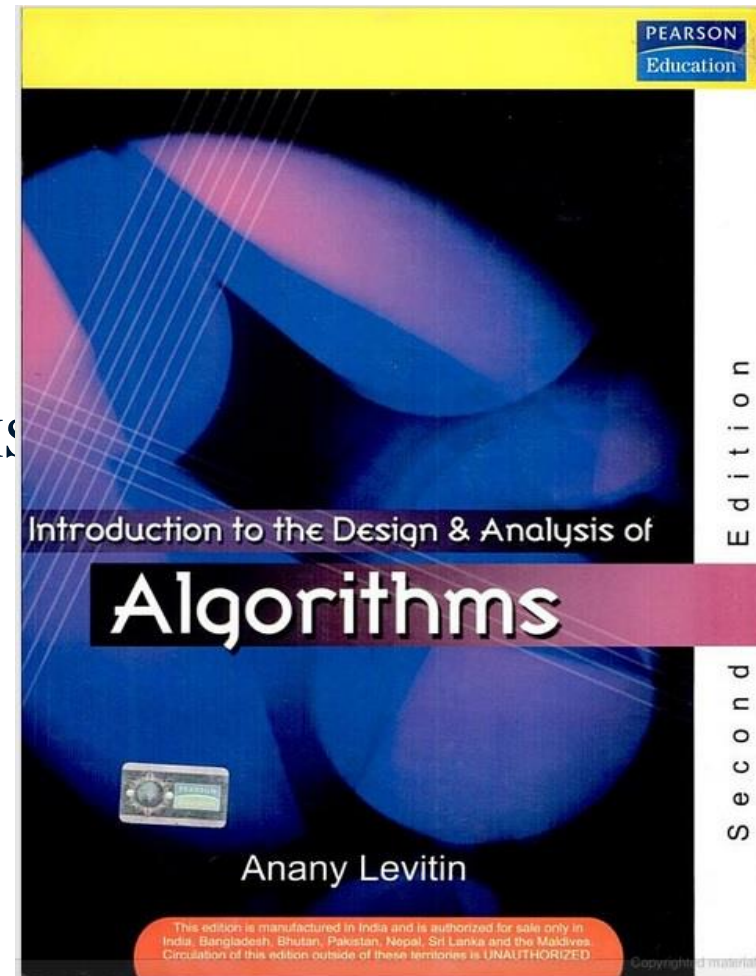


Zero Lecture on Design and Analysis of Algorithm CSE408

□ LTP – 3 0 0 [Three lectures/week]

□ Text Book

- INTRODUCTION TO THE DESIGN AND ANALYSIS OF ALGORITHMS
– ANANY LEVITIN,
PEARSON EDUCATION



Detail of Academic Tasks



- AT1: Test1 Lecture #11(Before MTE)
 - AT2: Test2 Lecture #19(Before MTE)
 - AT3: Test3 Lecture #33(After MTE)
- Best 2 will be considered with the conditions as :
- AT1 or AT2
 - AT3 will be mandatory

Weight age of AT,MTT,ETT



- Attendance: 5 Marks
- Academic Tasks(CA): 25 Marks
- MTT : 20 Marks
- ETT: 50 Marks



Need to study this course .



Why are we learning Design and analysis of algorithms?

- ❑ Algorithms are used in almost every program or software system.
- ❑ Once we design an algorithm we need to know how well it performs on any input.
- ❑ In particular we would like to know whether there are better algorithms for the problem, An answer to this first demands a way to analyze an algorithm in a machine-independent way.
- ❑ Some Specific design techniques are essential ingredients of many software applications.



- UNIT I - Foundations of algorithm
- UNIT II - String matching algorithms and computational geometry
- UNIT III - Divide and conquer and ordered statistics
- UNIT IV - Dynamic programming and greedy techniques
- UNIT V - Backtracking and approximation algorithms
- UNIT VI - Number-theoretic algorithms and complexity classes

CSE408:DESIGN AND ANALYSIS OF ALGORITHMS

Course Outcomes: Through this course students should be able to

CO1 :: explain the basic techniques of analyzing the algorithms using space and time complexity, asymptotic notations

CO2 :: analyse various string matching algorithms and understand brute force algorithm design technique

CO3 :: understand divide and conquer algorithm design technique using various searching and sorting algorithms

CO4 :: define dynamic programming and greedy algorithm design technique and solve various all pair and single source shortest path problems

CO5 :: apply the backtracking method to solve some classic problems and understand branch and bound algorithm design technique

CO6 :: define various number theory problems and understand the basics concepts of complexity classes

Unit I

Foundations of Algorithm : Algorithms, Fundamentals of Algorithmic Problem Solving:, Basic Algorithm Design Techniques, Analyzing Algorithm, Fundamental Data Structure:, Linear Data Structure, Graphs and Trees, Fundamentals of the Analysis of Algorithm Efficiency:, Measuring of Input Size, Units for Measuring Running Time, Order of Growth, Worst-Case, Best-Case, and Average-Case Efficiencies, Asymptotic Notations and Basic Efficiency Classes:, $O(\text{Big-oh})$ -notation, Big-omega notation, Big-theta notation, Useful Property Involving the Asymptotic Notations, Using Limits for Comparing Orders of Growth

Unit II

String Matching Algorithms and Computational Geometry : Sequential Search and Brute-Force String Matching, Closest-Pair and Convex-Hull Problem, Exhaustive Search, Voronoi Diagrams, Naive String-Matching Algorithm, Rabin-Karp Algorithm, Knuth-Morris-Pratt Algorithm

Unit III

Divide and Conquer and Order Statistics : Merge Sort and Quick Sort, Binary Search, Multiplication of Large Integers, Strassen's Matrix Multiplication, Substitution Method for Solving Recurrences, Recursion-Tree Method for Solving Recurrences, Master Method for Solving Recurrence, Closest-Pair and Convex-Hull Problems by Divide and Conquer, Decrease and Conquer: Insertion Sort, Depth-First Search and Breadth-First Search, Connected Components, Topological Sort, Transform and Conquer: Presorting, Balanced Search Trees, Minimum and Maximum, Counting Sort, Radix Sort, Bucket Sort, Heaps and Heapsort, Hashing, Selection Sort and Bubble Sort

Unit IV

Dynamic Programming and Greedy Techniques : Dynamic Programming: Computing a Binomial Coefficient, Warshall's and Floyd's Algorithm, Optimal Binary Search Trees, Knapsack Problem and Memory Functions, Matrix-Chain Multiplication, Longest Common Subsequence, Greedy Technique and Graph Algorithm: Minimum Spanning Trees, Prim's Algorithm, Kruskal's Algorithm, Dijkstra's Algorithm, Huffman Code, Single-Source Shortest Paths, All-Pairs Shortest Paths, Iterative Improvement: The Maximum-Flow Problem, Limitations of Algorithm Power: Lower-Bound Theory

Unit V

Backtracking and Approximation Algorithms : Backtracking: n-Queens Problem, Hamiltonian Circuit Problem, Subset-Sum Problem, Branch-and-Bound: Assignment Problem, Knapsack Problem, Traveling Salesman Problem, Vertex-Cover Problem and Set-Covering Problem, Bin Packing Problems

Unit VI

Number-Theoretic Algorithms and Complexity Classes : Number Theory Problems: Modular Arithmetic, Chinese Remainder Theorem, Greatest Common Divisor, Optimization Problems, Basic Concepts of Complexity Classes- P, NP, NP-hard, NP-complete Problems



CO1 :: Explain the basic techniques of analyzing the algorithms using space and time complexity, asymptotic notations

CO2 :: Analyze various string matching algorithms and understand brute force algorithm design technique

CO3 :: Understand divide and conquer algorithm design technique using various searching and sorting algorithms



- CO4 :: define dynamic programming and greedy algorithm design technique and solve various all pair and single source shortest path problems
- CO5 :: apply the backtracking method to solve some classic problems and understand branch and bound algorithm design technique
- CO6 :: define various number theory problems and understand the basics concepts of complexity classes

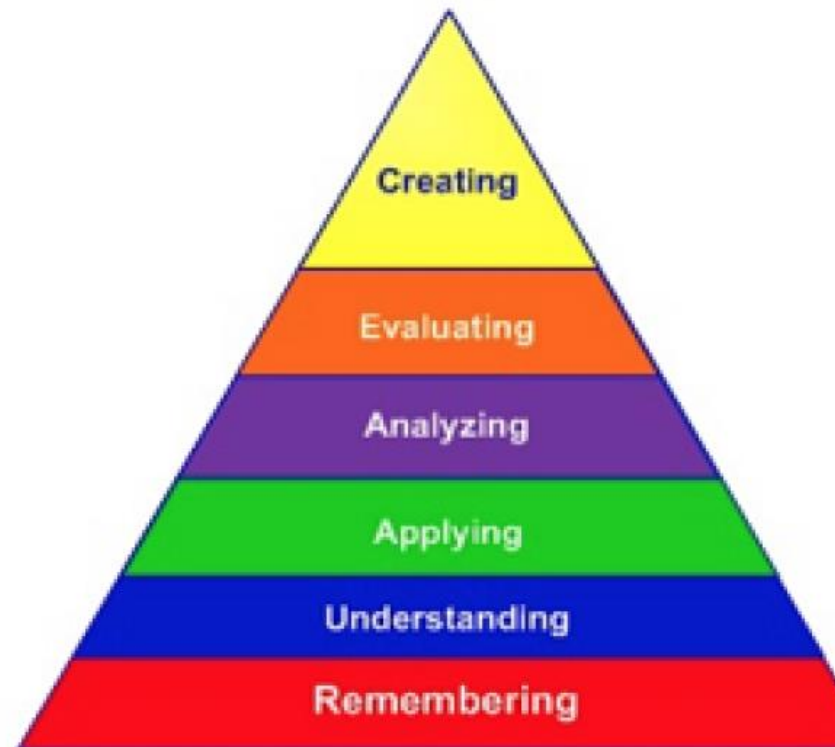
RBT– Revised Blooms Tax anomy



Blooms Taxonomy



Blooms Taxonomy - Revised



Creating

- The student can put elements together to form a functional whole, create a new product or point of view : **assemble, generate, construct, design, develop, formulate, rearrange, rewrite, organize, devise.**

Evaluating

- The student can make judgments and justify decisions: **appraise, argue, defend, judge, select, support, evaluate, debate, measure, select, test, verify**

Analyzing

- The student can distinguish between parts, how they relate to each other, and to the overall structure and purpose: **compare, contract, criticize, differentiate, discriminate, question, classify, distinguish, experiment**

Applying

- The student can use information in a new way: **demonstrate, dramatize, interpret, solve, use, illustrate, convert, discover, discuss, prepare**

Understanding

- The Student can construct meaning from oral, written and graphic messages: **interpret, exemplify, classify, summarize, infer, compare, explain, paraphrase, discuss**

Remembering

- The student can recognize and recall relevant knowledge from long-term memory: **define, duplicate, list, memorize, repeat, reproduce**

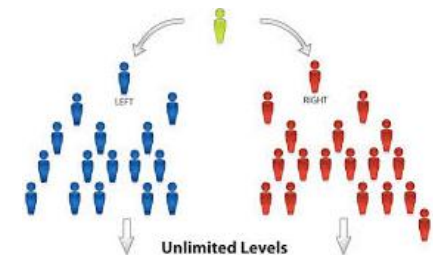


MOOC-Massive Open Online Course Approved (MOOC Course)

1. NPTEL

[https://nptel.ac.in/courses/106106131 /](https://nptel.ac.in/courses/106106131/)

Benefit to register the Approved MOOC is *All CAs*



String matching algorithms and computational geometry



Divide and conquer and ordered statistis



Dynamic programming and greedy technique

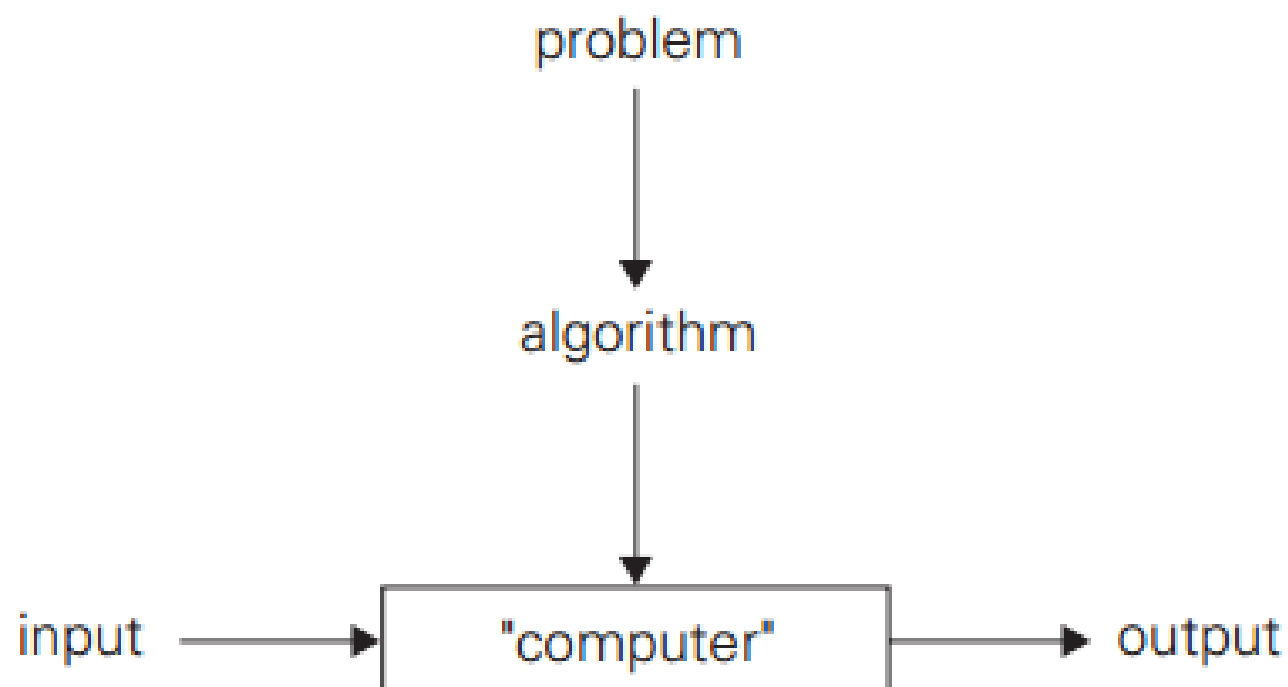


Which sweet should I have next?



An ***algorithm*** is a sequence of unambiguous instructions for solving a problem, i.e., for obtaining a required output for any legitimate input in a finite amount of time.

- The nonambiguity requirement for each step of an algorithm cannot be compromised.
- The range of inputs for which an algorithm works has to be specified carefully.
- The same algorithm can be represented in several different ways.
- There may exist several algorithms for solving the same problem.



Problem for Swapping 2 Numbers



Using Temporary Variable	Without using temporary variable
<pre>void swap(int a, int b) { int temp; temp = a; a = b; b = temp; }</pre>	<pre>void swap(int a, int b) { a = a + b; b = a - b; a = a - b; }</pre>

Fundamentals of algorithmic problem solving

- Understanding the problem
- Ascertaining the capabilities of a computational device.
- Choosing between exact and approximate problem solving.
- Deciding an appropriate Data Structure
- Algorithm design techniques.
- Methods of specifying an algorithm.
- Proving an algorithms correctness
- Analyzing an algorithm.
- Coding an algorithm

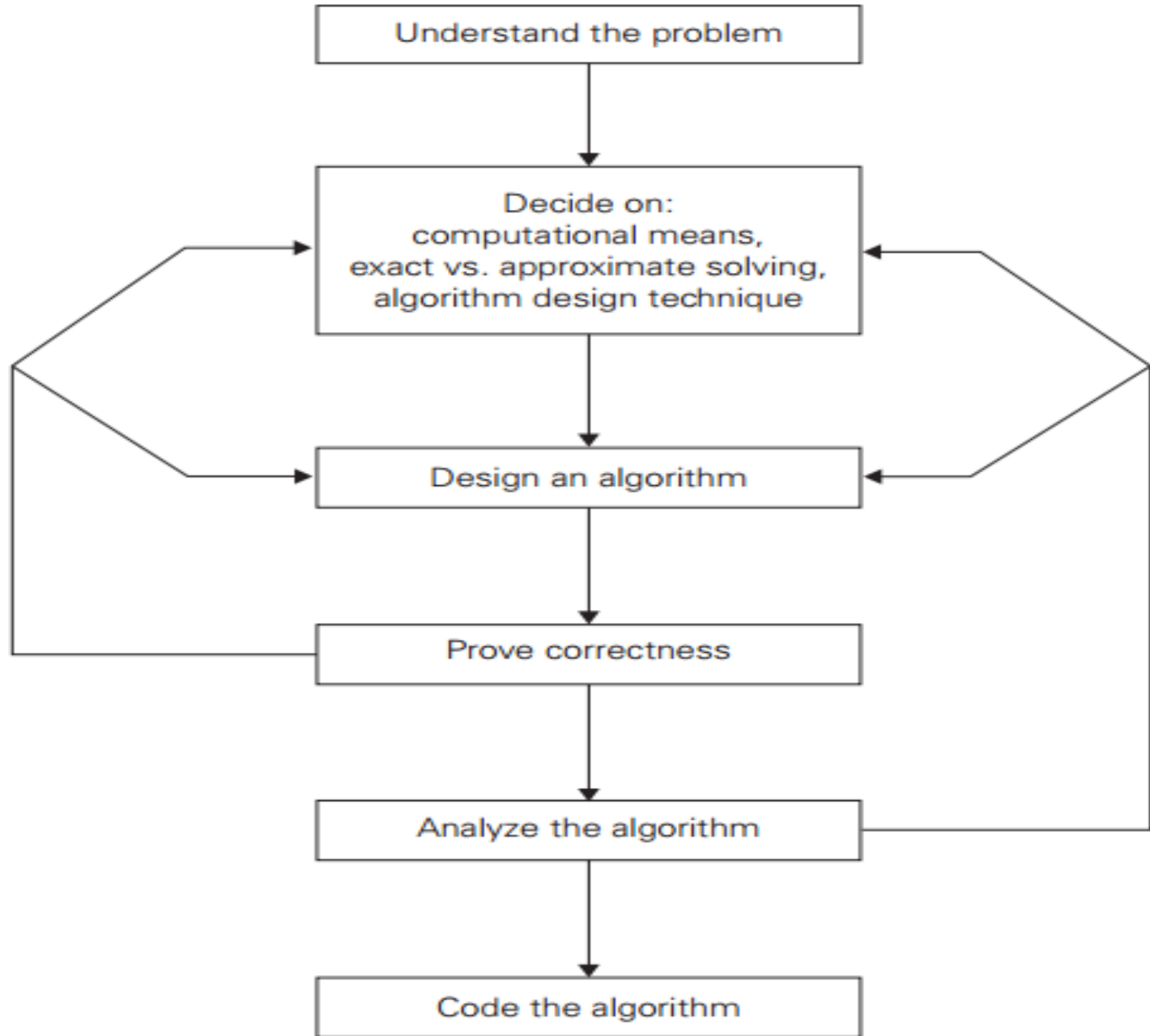


FIGURE 1.2 Algorithm design and analysis process.

Step 1- Understanding the problem



- ❑ Understand the given problem completely.
- ❑ Read the problem description carefully
- ❑ Ask doubts about the problem
- ❑ Do few examples
- ❑ Think about special cases like boundary value
- ❑ Know about the already known algorithms for solving that problem
- ❑ Clear about the input to an algorithm.



- Sequential Algorithms: Instructions are executed one after another and one operation at a time. Algorithms designed to be executed on such machine are called sequential algorithms
- Parallel Algorithms: Modern computers that can execute instructions in parallel. Algorithms designed to be executed on such machine are called parallel algorithms



- Exact Algorithm: Solving problem exactly
- Approx. Algm. : Solving problem approximately
- Why Approx. Algm.?
- Some problems cannot be solved exactly
- Solving problem exactly can be unacceptably slow because of the problem complexity.

Step 4- Deciding on appropriate Data Structures



- ❑ Decide on the suitable data structure
- ❑ A Data structure is defined as a particular scheme of organizing related data items.

Step 5- Algorithm Design techniques



- ▶ An algorithm design technique is a general approach to solve problems algorithmically.
- ▶ The various design techniques are:
- ▶ Brute force
- ▶ Divide and conquer
- Greedy approach
- Dynamic programming
- Backtracking

Step 6- Method of specifying an algorithm

- ❑ Natural language
- ❑ There are 3 methods:
 - Easy but ambiguous
- ❑ Pseudo code
 - Mixture of programming language and natural language
- ❑ Flow chart
 - It is pictorial representation of the algorithm.
 - Here symbols are used.

Step 7- Proving an algorithm's correctness

- ▶ Correctness: Prove that the algo. Yields the required result for every legitimate input in a finite amount of time.
- ▶ A common technique for proving correctness is to use mathematical induction
- ▶ In order to show the alg. Is incorrect, we have to take just one instance of its input for which the algm. Fails.
- ▶ If a algo. is found to be incorrect, then reconsider one or more those decisions
- ▶ For approx. algo. We should show that the error produced by the algo does not exceed the predefined limit.

Step 8- Analyzing an algorithm



- ▶ Analyze the following qualities of the algorithm
- ▶ Efficiency:
 - Time efficiency and Space efficiency
- ▶ Simplicity
 - Simple algorithms mean easy to understand and easy to program.
- ▶ Generality
 - Design an algm. for a problem in more general terms. In some cases, designing more general algm. Is unnecessary or difficult.
 - Optimality
 - The algorithm should produce optimal results.

Step 9- Coding an algorithm



- ❑ Algorithms are designed to be implemented as computer programs.
- ❑ Use code tuning technique. For eg., replacing costlier multiplication operation with cheaper addition operation.

Fundamental data structures

- list
 - array
 - linked list
 - string
- stack
- queue
- priority queue/heap
- **graph**
- **tree and binary tree**
- **set and dictionary**

TYPES OF DATA STRUCTURES

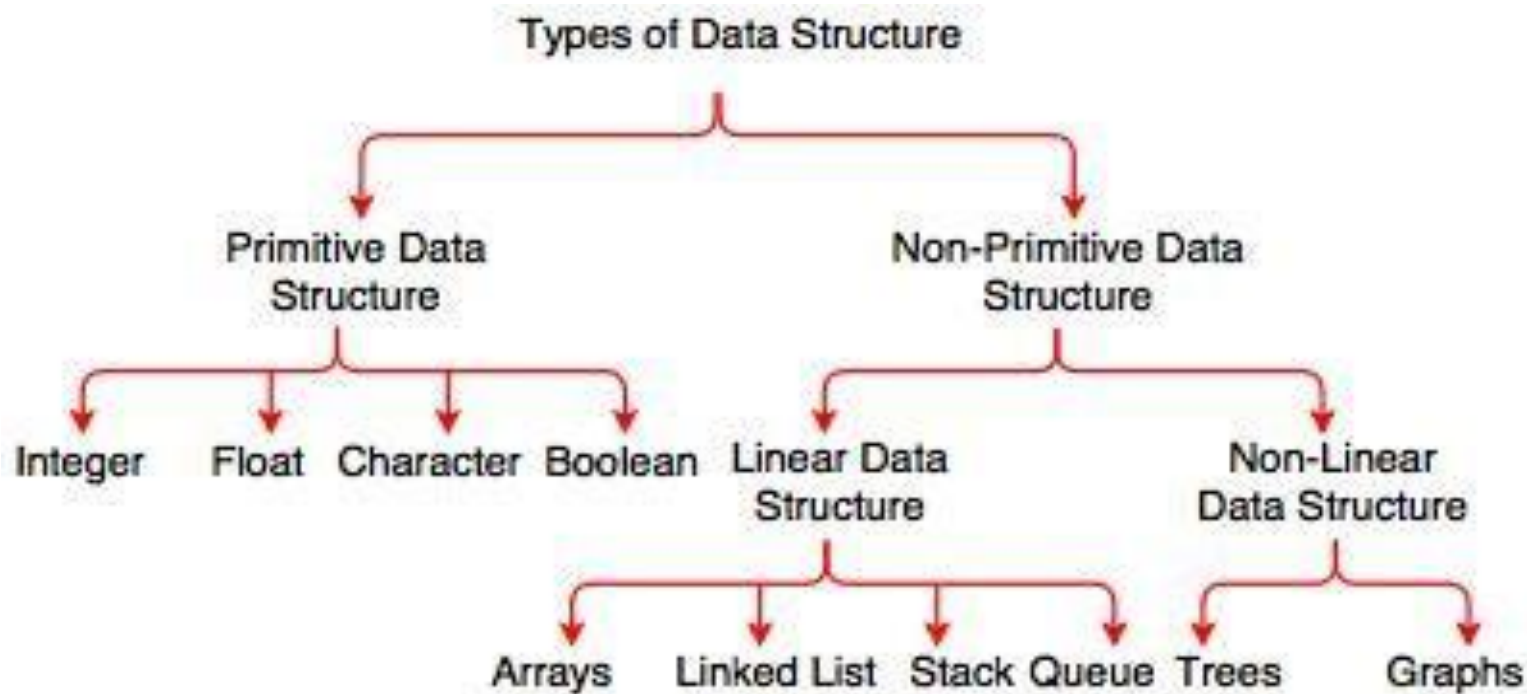


Fig. Types of Data Structure

□ Arrays

- A sequence of n items of the same data type that are stored contiguously in computer memory and made accessible by specifying a value of the array's index.

□ Linked List

- A sequence of zero or more nodes each containing two kinds of information: some data and one or more links called pointers to other nodes of the linked list.
- Singly linked list (next pointer)
- Doubly linked list (next + previous pointers)

□ Stacks

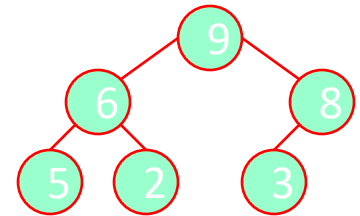
- A stack of plates
 - insertion/deletion can be done only at the top.
 - LIFO
- Two operations (push and pop)

□ Queues

- A queue of customers waiting for services
 - Insertion/enqueue from the rear and deletion/dequeue from the front.
 - FIFO
- Two operations (enqueue and dequeue)

■ Priority queues (implemented using heaps)

- A data structure for maintaining a set of elements, each associated with a key/priority, with the following operations
 - Finding the element with the highest priority
 - Deleting the element with the highest priority
 - Inserting a new element
- Scheduling jobs on a shared computer



Graphs

□ Formal definition

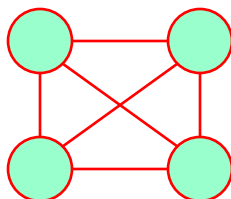
- A graph $G = \langle V, E \rangle$ is defined by a pair of two sets: a finite set V of items called **vertices** and a set E of vertex pairs called **edges**.

□ **Undirected** and **directed** graphs (**digraphs**).

□ maximum number of edges in an undirected graph with $|V|$ vertices

□ **Complete** graphs

- A graph with every pair of its vertices connected by an edge is called complete, $K_{|V|}$



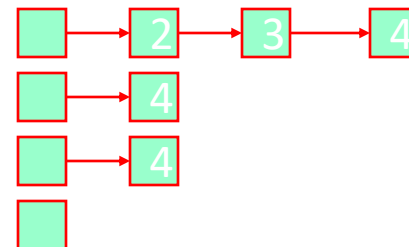
Graph Representation

□ Adjacency matrix

- $n \times n$ boolean matrix if $|V|$ is n .
- The element on the i th row and j th column is 1 if there's an edge from i th vertex to the j th vertex; otherwise 0.
- The adjacency matrix of an undirected graph is symmetric.

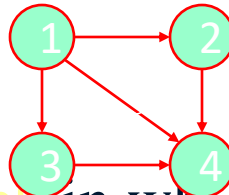
□ Adjacency linked lists

- A collection of linked lists, one for each vertex, that contain all the vertices adjacent to the list's vertex.
- Which data structure would you use if the graph is a 100-node star shape?



□ Weighted graphs

- Graphs or digraphs with numbers assigned to the edges.



- A dense graph is a graph in which the number of edges is close to the maximal number of edges. The opposite, a graph with only a few edges, is a sparse graph.

Graph Properties -- Paths and Connectivity

□ Paths

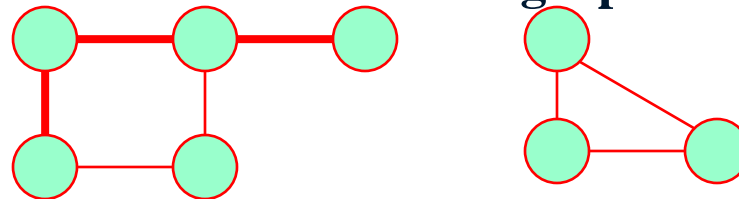
- A path from vertex u to v of a graph G is defined as a sequence of adjacent (connected by an edge) vertices that starts with u and ends with v .
- Simple paths: All edges of a path are distinct.
- Path lengths: the number of edges, or the number of vertices $- 1$.

□ Connected graphs

- A graph is said to be connected if for every pair of its vertices u and v there is a path from u to v .

□ Connected component

- The maximum connected subgraph of a given graph.



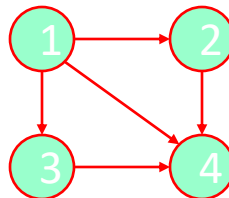
Graph Properties -- Acyclicity

□ **Cycle**

- A simple path of a positive length that starts and ends at the same vertex.

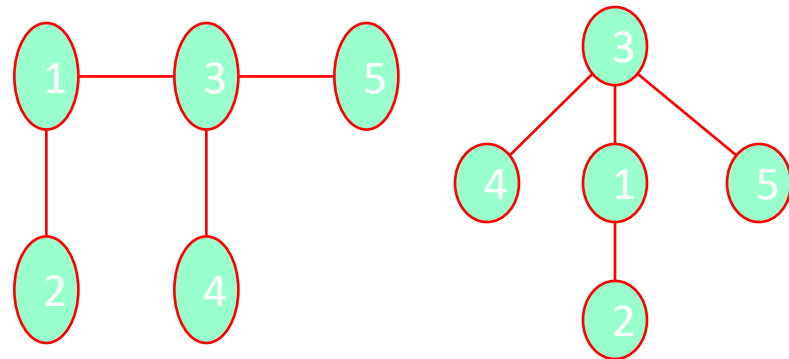
□ **Acyclic graph**

- A graph without cycles
- DAG (Directed Acyclic Graph)



Trees

- Trees
 - A tree (or free tree) is a connected acyclic graph.
 - Forest: a graph that has no cycles but is not necessarily connected.
- Properties of trees
 - For every two vertices in a tree there always exists exactly one simple path from one of these vertices to the other.
 - Rooted trees: The above property makes it possible to select an arbitrary vertex in a free tree and consider it as the root of the so called rooted tree.
 - Levels in a rooted tree.



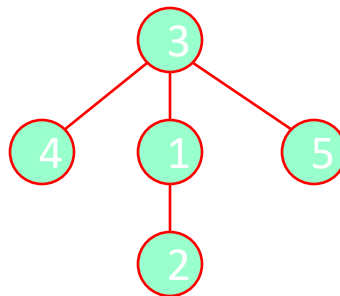
- Ancestors
 - For any vertex v in a tree T , all the vertices on the simple path from the root to that vertex are called ancestors.
- Descendants
 - All the vertices for which a vertex v is an ancestor are said to be descendants of v .
- Parent, child and siblings
 - If (u, v) is the last edge of the simple path from the root to vertex v , u is said to be the parent of v and v is called a child of u .
 - Vertices that have the same parent are called siblings.
- Leaves
 - A vertex without children is called a leaf.
- Subtree
 - A vertex v with all its descendants is called the subtree of T rooted at v .

□ Depth of a vertex

- The length of the simple path from the root to the vertex.

□ Height of a tree

- The length of the longest simple path from the root to a leaf.



Ordered Trees

- Ordered trees
 - An ordered tree is a rooted tree in which all the children of each vertex are ordered.
- Binary trees
 - A binary tree is an ordered tree in which every vertex has no more than two children and each children is designated s either a left child or a right child of its parent.
- Binary search trees
 - Each vertex is assigned a number.
 - A number assigned to each parental vertex is larger than all the numbers in its left subtree and smaller than all the numbers in its right subtree.
- $\lfloor \log_2 n \rfloor \leq h \leq n - 1$, where h is the height of a binary tree and n the size.

