HW6

- \bullet pages 114–119, problems 1,2,4,5.
- $\bullet\,$ Find the limits

$$\lim_{x \to +\infty} x^3 \left(\sin(x^{-1}) - x^{-1} \right), \quad \lim_{x \to 1} \frac{1 - \cos(x - 1)}{\tan^2(x - 1)}.$$

1

• Suppose f is continuously differentiable on $[0, \infty)$ (that is, it is differentiable and the derivative is continuous at every point of $[0, \infty)$) and $|f'(x)| \leq 1$ for all $x \geq 0$. Is f bounded on $[0, \infty)$? Is it uniformly continuous on $[0, \infty)$?