# (A bit of) Advanced R

Part 2 - faster R programming

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### Outline I

- 1 Benchmark
- 2 Vectorize
- 3 Parallelize
- 4 Prefer simple objects
- **5** Use Rcpp and C++ code
- 6 Mind your vocabulary: R fast built in function, an others

### References I

Advanced R (Wickham, 2014), http://adv-r.had.co.nz/



Efficient R programming (Gillespie & Lovelace, 2016), https://bookdown.org/csgillespie/efficientR/



### References II

Seamless R and C++ integration with Rcpp (Eddelbuettel, 2013), for sale but see http://dirk.eddelbuettel.com



The R inferno (Burns, 2012), http://www.burns-stat.com/documents/books/the-r-inferno/



## Prerequisites

#### Data Structure in base R

- 1 Atomic vector (integer, double, logical, character)
- Recursive vector (list)
- 6 Factors
- Matrices and array
- 6 Data Frame
- → Creation, Basic Operation, Manipulation, Representation

### Basic R programming

- Control Statements
- 2 Functions
- Basics on Functionals
- → Advanced R, Chapters I.6, II.10, II.11

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# Quick (and dirty) benchmarking with system.time()

One usually relies on the command system.time(expr) to evaluate the timings:

```
func.two <- function(n) {return(rpois(n,1))}

n <- 1000
system.time(replicate(100, func.one(n)))

## user system elapsed
## 0.008 0.000 0.011
system.time(replicate(100, func.two(n)))</pre>
```

```
## user system elapsed
## 0.008 0.000 0.009
```

func.one <- function(n) {return(rnorm(n,0,1))}</pre>

#### Exercice

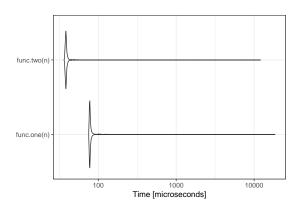
Write functions to compute the variance of a real vector, with an without loops. Benchmark them.

# Quick benchmarking with microbenchmark

```
func.one <- function(n) {return(rnorm(n,0,1))}
func.two <- function(n) {return(rpois(n,1))}

library(microbenchmark)

n <- 1000
res <- microbenchmark(func.one(n), func.two(n), times=1000)
ggplot2::autoplot(res)</pre>
```



## Profile your code

### Suppose you want to evaluate which part of the following function is hot:

```
## generate data, center/scale and perform ridge regression
my_func <- function(n,p) {</pre>
  require (MASS)
  ## draw data
  x <- matrix(rnorm(n*p),n,p)
  v <- rnorm(n)
  ## center/scale
  xs <- scale(x)
  vs \leftarrow v - mean(v)
  ## return ridge's coefficients
  ridge <- lm.ridge(ys~xs+0,lambda=1)
  return(ridge$coef)
```

# Profile your code with base Rprof I

### One can rely on the default Rprof function, with somewhat technical outputs

```
Rprof(file="profiling.out", interval=0.05)
res <- my_func(1000,500)
Rprof(NULL)
summaryRprof("profiling.out")$by.self</pre>
```

```
##
               self.time self.pct total.time total.pct
## "La.svd"
                   1.25
                          64.10
                                    1.30
                                           66.67
## "matrix"
                   0.20 10.26
                                    0.20 10.26
                  0.15 7.69
  "aperm.default"
                                   0.15
                                          7.69
## "FUN"
                   0.10 5.13
                                   1.95 100.00
## ".External2"
                 0.10 5.13
                                   0.15
                                           7.69
## "t.default"
                 0.10
                           5.13
                                    0.10
                                            5.13
## "na.omit"
                   0.05
                           2.56
                                    0.05
                                            2.56
```

summaryRprof("profiling.out")\$by.total

# Profile your code with base Rprof II

##		total.time	total.pct	self.time	self.pct
##	"FUN"	1.95		0.10	5.13
##	"block_exec"	1.95	100.00	0.00	0.00
##	"call_block"	1.95	100.00	0.00	0.00
##	"eval"	1.95	100.00	0.00	0.00
##	"evaluate"	1.95	100.00	0.00	0.00
##	"evaluate_call"	1.95	100.00	0.00	0.00
##	"evaluate::evaluate"	1.95	100.00	0.00	0.00
##	"handle"	1.95	100.00	0.00	0.00
##	"in_dir"	1.95	100.00	0.00	0.00
##	"knit"	1.95	100.00	0.00	0.00
##	"knitr::knit"	1.95	100.00	0.00	0.00
##	"lapply"	1.95	100.00	0.00	0.00
##	"my_func"	1.95	100.00	0.00	0.00
##	"process_file"	1.95	100.00	0.00	0.00
##	"process_group"	1.95	100.00	0.00	0.00
##	"process_group.block"	1.95	100.00	0.00	0.00
##	"rmarkdown::render"	1.95	100.00	0.00	0.00
##	"timing_fn"	1.95	100.00	0.00	0.00
##	"withCallingHandlers"	1.95	100.00	0.00	0.00
##	"withVisible"	1.95	100.00	0.00	0.00
##	"lm.ridge"	1.55	79.49	0.00	0.00
##	"La.svd"	1.30	66.67	1.25	64.10
##	"svd"	1.30	66.67	0.00	0.00
##	"scale"	0.25	12.82	0.00	0.00
##	"scale.default"	0.25	12.82	0.00	0.00
##	"matrix"	0.20	10.26	0.20	10.26

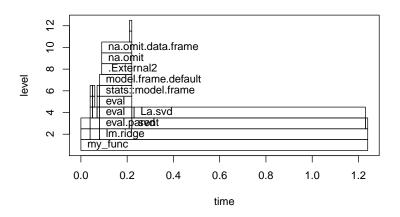
# Profile your code with base Rprof III

##	"aperm.default"	0.15	7.69	0.15	7.69
##	".External2"	0.15	7.69	0.10	5.13
##	"aperm"	0.15	7.69	0.00	0.00
##	"sweep"	0.15	7.69	0.00	0.00
##	"t.default"	0.10	5.13	0.10	5.13
##	"apply"	0.10	5.13	0.00	0.00
##	"model.matrix"	0.10	5.13	0.00	0.00
##	"model.matrix.default"	0.10	5.13	0.00	0.00
##	"t"	0.10	5.13	0.00	0.00
##	"na.omit"	0.05	2.56	0.05	2.56
##	"eval.parent"	0.05	2.56	0.00	0.00
##	"model.frame.default"	0.05	2.56	0.00	0.00
##	"stats::model.frame"	0.05	2.56	0.00	0.00

# Profile your code with profr

The *profr* package is maybe a little easier to understand. . .

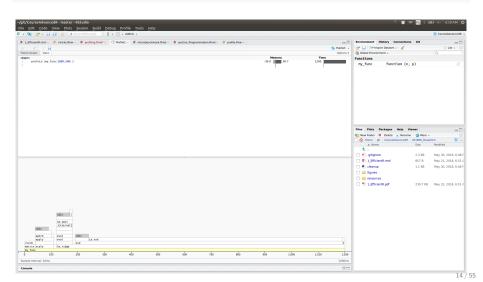
```
library(profr)
profiling <- profr({my_func(1000,500)}, interval = 0.01)
plot(profiling)</pre>
```



# Profile your code within Rstudio with profvis

Profvis integrates the profiling to the Rstudio API: try it!

```
library(profvis)
profvis({my_func(1000,500)})
```



## Outline

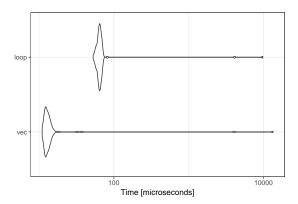
- 1 Benchmark
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# Vectorize any algebraic operation

```
Example: compute \exp(x) = \sum_{k=0}^{n} \frac{x^k}{k!}
```

```
exp_loop <- function(x, n) { ## the sad/bad/less readable way
  res <- 1
  for (k in 1:n) res <- res + 2^k/factorial(k)
  res
}</pre>
```

```
## the good way exp_vec <- function(x, n) sum(x^-(0:n)/c(1,cumprod(1:n)))
```

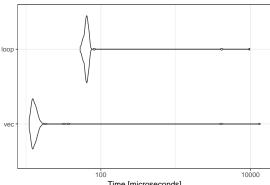


# Vectorize any algebraic operation

```
Example: compute \exp(x) = \sum_{k=0}^{n} \frac{x^k}{k!}
```

```
exp_{loop} \leftarrow function(x, n) \{ ## the sad/bad/less readable way \}
  res <- 1
  for (k in 1:n) res <- res + 2^k/factorial(k)
  res
```

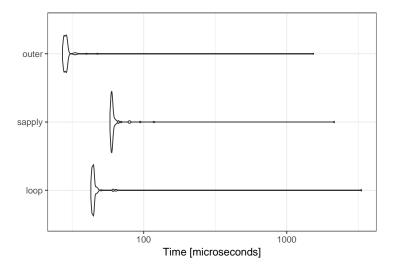
```
## the good way
\exp_{\text{vec}} \leftarrow \operatorname{function}(x, n) \operatorname{sum}(x^{(0:n)/c(1, \operatorname{cumprod}(1:n))})
```



# Vectorize, even for non-algebraic operation I

```
month_year_loop <- function(year) {
 res <- c()
  for (month in month.name)
   res <- c(res, paste(month, year, sep = " "))
  res
month_year_apply <- function(year) {
  sapply(month.name, function(month) paste(month, year, sep = " "))
month year outer <- function(year) {
  outer(month.name, year, FUN = paste, sep = '_')
head(month year outer(c(2010, 2013)), 3)
  [,1]
               [,2]
## [1,] "January 2010" "January 2013"
## [2,] "February_2010" "February_2013"
## [3,] "March_2010" "March_2013"
autoplot(microbenchmark(
  loop = month_year_loop(c(2011, 2013)),
  sapply = month year apply(c(2011, 2013)),
  outer = month year outer(c(2011, 2013))
```

# Vectorize, even for non-algebraic operation II

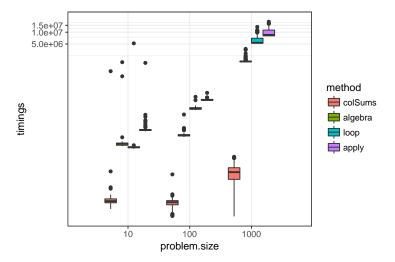


# The row/colSums family I

col/rowSums, col/rowMeans and their extensions in the matrixStats package (rank,max,min, etc.) are very efficient.

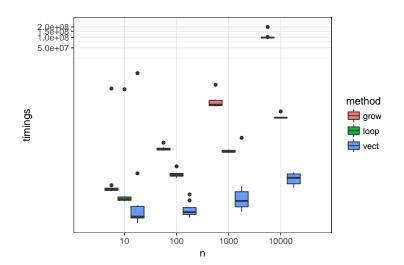
```
colSums.default <- function(x) return(colSums)
colSums.algebra <- function(x) return(crossprod(rep(1,nrow(x)), x))
colSums.apply <- function(x) return(apply(x,2,sum))
colSums.loop <- function(x) {
  res <- rep(0,ncol(x))
  for (i in 1:ncol(x)) {
    res[i] <- sum(x[,i])
  }
  res
}</pre>
```

# The row/colSums family II



# Preallocate whenever it is possible

```
grow <- function(n) {vec <- numeric(0); for (i in 1:n) vec <- c(vec,i)}
loop <- function(n) {vec <- numeric(n); for (i in 1:n) vec[i] <- i}
vect <- function(n) {1:n}</pre>
```

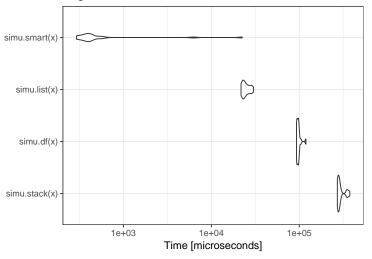


## Do not stack objects I

Even if it is tempting when the final size is unknown.

```
simu.stack <- function(x) { ## x is a n x p matrix</pre>
  out <- data.frame(mean = numeric(0), sd = numeric(0))</pre>
  for (i in 1:n) out <- rbind(out, data.frame(mean = mean(x[i,]), sd = sd(x[i,])))
  0111.
simu.df <- function(x) {
  out <- data.frame(mean = numeric(n), sd = numeric(n))</pre>
  for (i in 1:n) out[i, ] <- c(mean = mean(x[i,]), sd = sd(x[i,]))
  out
simu.list <- function(x) {
  my.list <- lapply(1:nrow(x), function(i) c(mean(x[i,]), sd(x[i,])))</pre>
  out <- data.frame(do.call(rbind, mv.list))
  colnames(out) <- c("mean"."sd")</pre>
  0111.
n \leftarrow 1000; p \leftarrow 10; x \leftarrow matrix(rnorm(n*p), n, p)
autoplot(microbenchmark(simu.stack(x), simu.df(x), simu.list(x), simu.smart(x), times=20))
```

# Do not stack objects II



Exercice: code the smart function (no loop)

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## Parallel computing

### Usual Roadmap

- $oldsymbol{0}$  Start up and intialize M 'worker' processes
- Send data required for each task to the workers
- f Split the task into M roughly equally-sized chunks and send them (including the R code needed) to the workers
- Wait for all the workers to complete their tasks, and ask them for their results
- **6** Repeat steps (2–4) for any further tasks
- 6 Shut down the worker processes

# Socketing vs Forking

Two approaches achieving the same goal

### The socket approach

- launches a new version of R on each core
- connection is done via networking all happening on your own computer

### The forking approach

- copies the entire current version of R and moves it to a new core
- several processes acheive the same task resulting in different outputs
- → Forking is only possible on Unix systems (Linux, Mac OS)

# Parallel computing with parallel

### Package parallel

- merge of packages multicore and snow
- included in base R and maintained by the R Core team

### Check your computer

```
library(parallel) ## embedded with R since version 2.9 or something
cores <- detectCores() ## How many cores do I have?
print(cores)</pre>
```

```
## [1] 4
```

→ parallel features both socketing (parLapply) and forking (mclapply)

# Forking approach with parallel::mclapply

Very easy: use parallel features as soon as you do simulations !

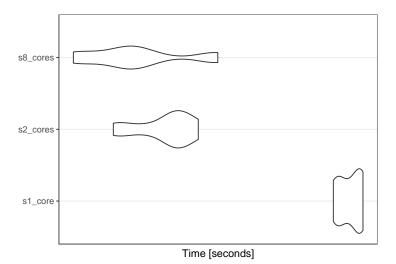
### Example: estimates the test error from ridge regression

```
one.simu <- function(i) {
    ## draw data
    n <- 1000; p <- 500
    x <- matrix(rnorm(n*p),n,p); y <- rnorm(n)
    ## return ridge's coefficients
    train <- 1:floor(n/2)
    test <- setdiff(1:n,train)
    ridge <- MASS::lm.ridge(y~x+0,lambda=1,subset=train)
    err <- (y[test] - x[test, ] %*% ridge$coef )^2
    return(list(err = mean(err), sd = sd(err)))
}</pre>
```

head(do.call(rbind, mclapply(1:8, one.simu, mc.cores = cores)), n = 3)

```
## err sd
## [1,] 11.11148 16.45305
## [2,] 13.43357 18.93762
## [3,] 14.64665 20.64142
```

# Forking approach with parallel::mclapply (cont'd)



# Socket approach with parallel::parLapply

#### Windows users need a bit more code to make it work

### A possible option: export from base workspace

```
cl <- makeCluster(4)
clusterExport(cl,"one.simu")
res <- parSapply(cl, 1:8, one.simu) # several parLapply call are possible
stopCluster(cl)
res</pre>
```

```
## [,1] [,2] [,3] [,4] [,5] [,6] [,7]
## err 13.77063 10.07072 9.917237 12.5304 12.11757 11.45066 19.36333
## sd 20.14429 14.80041 14.20996 17.55452 16.8775 16.28831 26.49789
## err 11.21091
## sd 15.20287
```

# Parallel computing with parallel: final remarks

- Parallelize pieces of code complex enough
- Do not choose stupidly the number of cores

pbmcapply::pbmcmapply(1:8, FUN = one.simu, mc.cores = 2)

Screen outputs are lost in Rstudio: use pbmcapply (progress bar)

```
## [,1] [,2] [,3] [,4] [,5] [,6] [,7]
## err 11.22125 13.80911 13.38632 11.21224 13.20718 12.01847 13.46801
## sd 16.14348 20.30204 17.2794 15.06328 19.60637 16.5494 18.06206
## [,8]
## err 13.14769
## sd 18.6168
```

## Parallel computing: exercise

Here are two function to bootstrap a table and to extract the  $\mathbb{R}^2$  from the output of lm, a linear model fit.

```
boot_df <- function(x) x[sample(nrow(x), rep = T), ]
rsquared <- function(mod) summary(mod)$r.squared
summary(lm(mpg ~ wt + disp, data = mtcars))</pre>
```

```
##
## Call:
## lm(formula = mpg ~ wt + disp, data = mtcars)
##
## Residuals:
      Min
           10 Median
                                   Max
##
                             30
## -3.4087 -2.3243 -0.7683 1.7721 6.3484
##
## Coefficients:
##
             Estimate Std. Error t value Pr(>|t|)
## (Intercept) 34.96055 2.16454 16.151 4.91e-16 ***
      -3.35082 1.16413 -2.878 0.00743 **
## disp -0.01773 0.00919 -1.929 0.06362 .
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 2.917 on 29 degrees of freedom
## Multiple R-squared: 0.7809, Adjusted R-squared: 0.7658
## F-statistic: 51.69 on 2 and 29 DF, p-value: 2.744e-10
```

### Bootstrap the $\mathbb{R}^2$ with lapply, mclapply and replicate.

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# R is a typed language

## R masks the numerical errors by printing a convenient summary of objects

```
7/13
  [1] 0.5384615
print(7/13, digits=16)
  [1] 0.5384615384615384
```

## R is a typed language

## R masks the numerical errors by printing a convenient summary of objects

```
7/13
  [1] 0.5384615
print(7/13, digits=16)
  [1] 0.5384615384615384
So do not use binary operator to compare floats because
.1 == .3/3
## [1] FALSE
print(.3/3, digits=16)
  [1] 0.0999999999999999
```

### R is a typed language

## [1] TRUE

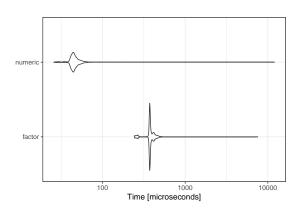
R masks the numerical errors by printing a convenient summary of objects

```
7/13
## [1] 0.5384615
print(7/13, digits=16)
  Γ17 0.5384615384615384
So do not use binary operator to compare floats because
.1 == .3/3
## [1] FALSE
print(.3/3, digits=16)
  [1] 0.0999999999999999
Try
all.equal(.1, .3/3)
```

# Factor conversion are slow (nlevels)

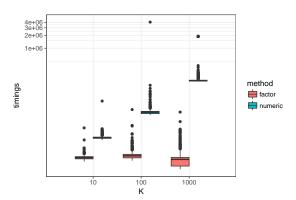
Do not convert large vector to factor if you need to perform just one operation on it.

```
n <- 1000; K <- 10
autoplot(microbenchmark(
  factor = nlevels(factor(sample(1:K, n, rep=TRUE))),
    numeric = length(unique(sample(1:K, n, rep=TRUE))), times=1000)
)</pre>
```



### Operations on factors are fast (e.g. nlevels)

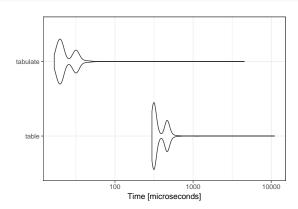
Use factor if you need repeated operations on the same vector.



### Prefer tabulate to table whenever you can

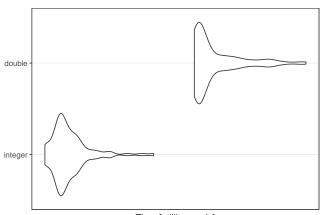
table is a complex function that should not be use for simple operations like counting the occurrences of integers in a vector.

```
n <- 1000; K <- 10
autoplot(
  microbenchmark(
    table = table (sample(1:K, n, rep=TRUE)),
    tabulate = tabulate(sample(1:K, n, rep=TRUE)),
    times=1000)
)</pre>
```



### Variable type matters

Sorting a vector of integers is much faster than a vector of double, but R is so permissive that you might loss the gain if you do not take care:



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## Interfacing C++ with R is really easy I

For a vector  $\mathbf{x} = (x_1, \dots, x_n)$ , consider the simple task of computing

$$y_k = \sum_{i=1}^k \log(x_i), \quad k = 1, \dots, n.$$

One can easily integrate some C++ version of this code with Rcpp.

```
library(Rcpp)
rcpp <- cppFunction('NumericVector rcpp(NumericVector x) {
  using namespace Rcpp;

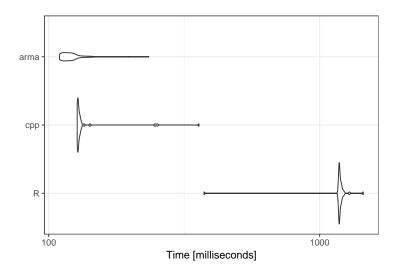
int n = x.size();
  NumericVector res(x);
  res(0) = log(x(0));
  for (int i=1; i<n; i++) {
     res(i) = res(i-1) + log(x(i));
  }
  return(wrap(res));
}')</pre>
```

# Interfacing C++ with R is really easy II

```
library(RcppArmadillo)
Arma <- cppFunction(depends = "RcppArmadillo", 'NumericVector Arma(NumericVector x) {
    using namespace Rcpp;
    using namespace arma;
    return(wrap(cumsum(log(as<vec>(x)))));
}')

x <- runif(1e7, 1,2)
res <- microbenchmark(R = cumsum(log(x)), cpp = rcpp(x), arma = Arma(x), times = 40)
print(autoplot(res))</pre>
```

# Interfacing C++ with R is really easy III



### Interfacing C++ with R is really easy I

#### Example that couples C+++ algebraic tricks

Let  ${\bf T}$  be an  $n\times n$  lower triangular matrix with nonzero elements equal to one. We need fast computation of

$$\operatorname{vec}(\mathbf{T}\mathbf{B}\mathbf{T}^{\top}) = (\mathbf{T} \otimes \mathbf{T}) \times \operatorname{vec}(\mathbf{B}).$$

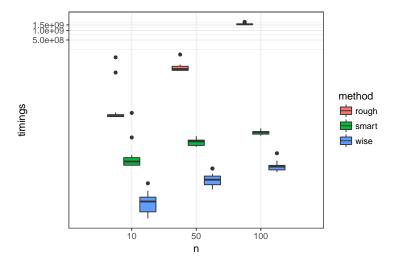
```
library(Matrix); library(inline); library(RcppArmadillo)

prod.rough <- function(B) {
    n <- ncol(B); T <- bandSparse(n,k=(-n+1):0)
    return(kronecker(T,T) %*% as.vector(B))}

prod.smart <- function(B) {
    return(as.vector(apply(apply(B,1,cumsum),1,cumsum)))}

prod.wise <- cxxfunction(signature(B="matrix"),'
    using namespace Rcpp;
    using namespace arma;
    return(wrap(vectorise(cumsum(cumsum(as<mat>(B),0),1))));
    ', plugin="RcppArmadillo")
```

### Interfacing C++ with R is really easy II



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#### The secret function rowsum I

rowsum (not to be confused with rowSums) computes sums in a vector split according a grouping variable (work for matrices).

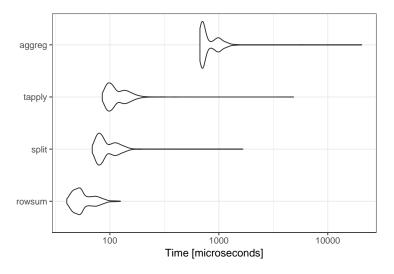
```
vec <- runif(1000)
grp <- sample(1:5, 1000, TRUE)
print(c(rowsum(vec, grp)))</pre>
```

```
## [1] 101.39001 96.82680 97.34139 99.04092 99.70550
```

#### There are many possibilities to perform the required task:

```
res <- microbenchmark(
rowsum = rowsum(vec, grp),
split = sapply(split(vec, grp), sum),
tapply = tapply(vec, grp, sum),
aggreg = aggregate(vec, list(grp), sum),
times = 1000)</pre>
```

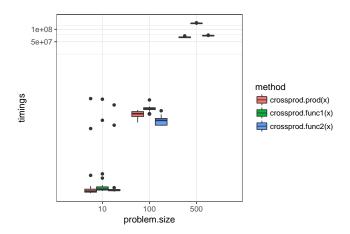
### The secret function rowsum II



### Dedicated function: cross-product

#### Generally (a bit) fastest than % \* % !

```
crossprod.prod <- function(x) return(t(x) %*% x)
crossprod.func1 <- function(x) return(crossprod(x,x))
crossprod.func2 <- function(x) return(crossprod(x))</pre>
```

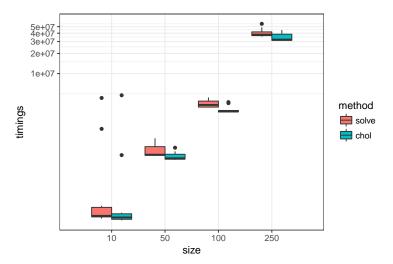


## Dedicated function: inverting a PD matrices I

#### Use a Cholesky factorization

```
use.chol <- function(n,p) {
  x <- matrix(rnorm(n*p),n,p)
  xtx <- crossprod(x)
  return(chol2inv(chol(xtx)))
use.solve <- function(n,p) {
  x <- matrix(rnorm(n*p),n,p)
  xtx <- crossprod(x)
 return(solve(xtx))
bench.p.fixed <- function(p, times) {
  res <- microbenchmark(solve = use.solve(2*p,p),
                        chol = use.chol (2*p,p), times=times)
  return(data.frame(method = res$expr,
                    timings = res$time.
                            = rep(as.character(p),times)))
                    size
```

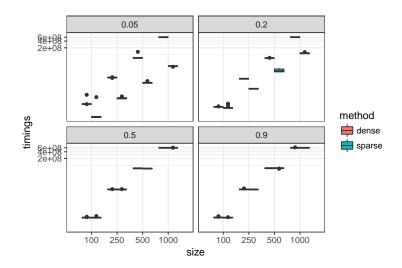
# Dedicated function: inverting a PD matrices II



## The Matrix package I

Propose a collection of functions for of matrix algebra adapted to the type of matrix at hand (sparse, diagonal, triangular, block diagonal, etc.)

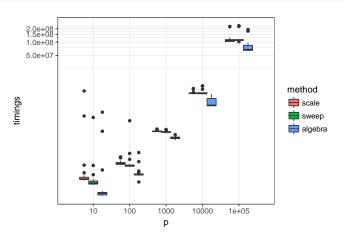
# The Matrix package II



### Mind some algebra

### Sweep is a general way to apply a statistic on a given dimension of an array.

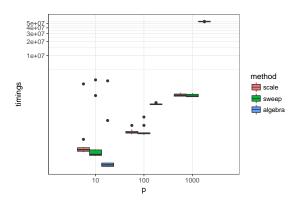
```
center1 <- function(x) return(scale(x, colMeans(x), FALSE))
center2 <- function(x) return(sweep(x, 2, colMeans(x), "-", check.margin = FALSE))
center3 <- function(x) return(x - outer(rep(1, nrow(x)), colMeans(x)) )
seq.p <- 10^(1:5); n <- 100; times <- 20</pre>
```



### Algebra does not always pay

#### Example for scaling a matrix

```
scale1 <- function(x) return(scale(x, FALSE, colSums(x^2)))
scale2 <- function(x) return(sweep(x, 2, colSums(x^2), "/", check.margin=FALSE))
scale3 <- function(x) return(x %*% diag(1/colSums(x^2)) )
seq.p <- 10^(1:3); n <- 100; times <- 20</pre>
```



#### References

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Gillespie, C., & Lovelace, R. (2016). *Efficient R programming*. "O'Reilly Media, Inc." Retrieved from https://bookdown.org/csgillespie/efficientR/

R Core Team. (2017). R: A language and environment for statistical computing. Vienna, Austria: R Foundation for Statistical Computing. Retrieved from  $\frac{1}{2} \frac{1}{2} \frac{1}{2$ 

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