

Istanbul Technical University- Spring 2017

BLG527E Machine Learning

Homework 1

Purpose: Better understanding of PR/ML basics.

Total worth: 6% of your grade.

Handed out: Thursday, Sept 21, 2017.

Due: Wednesday, Oct 4, 2017 22.00. (through ninova!)

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Policy: Collaboration in the form of discussions is acceptable, but you should write your own answer/code by yourself. Cheating is highly discouraged for it could mean a zero or negative grade from the homework. If a question is not clear, please let us know (via email, during office hour or in class).

Submission Instructions: Please submit through the class ninova site.

Please zip and upload all your files using filename studentID_HW1.zip. You must provide all functions you wrote with your zipped file. Functions you do not submit may cause you lose a portion of your grade. You must also include a .doc or pdf file with answers to the questions and how to call your R functions for each question so that we can run and check the results. Also make sure you add the x, y labels and title to the plots.

QUESTIONS:

Q1) [2 points][Central Limit Theorem]

Consider a univariate random variable x distributed according to $N(0,1)$ (i.e. unit normal)

Q1a) Using R,

Repeat for $i=1\dots 500$

X_i = draw $N=10$ samples of from the distribution,
compute the mean ($m_i = \text{mean}(X_i)$)

Plot the histogram of these means for 500 different experiments. Make sure you add the x, y labels, title and x-y tick values on the plot.

Q1b) Repeat Q1a) for $N=100$ instances in each sample.

Q1c) What are the differences and similarities between the plots you see in 1a) and 1b)? Why?

Q2) [4 points] [Bayesian Decision Theory]

Assume a discriminant function of the form: $g_i(x) = \ln(p(x|C_i)) + \ln(P(C_i))$

Assume that there are two classes and inputs are distributed according to Gaussians.

Likelihood for classes 1 and 2 are given as: $p(x|C_1) = N(0,1)$, $p(x|C_2) = N(1,2)$

Q2a) Derive the discriminant functions $g_1(x)$ and $g_2(x)$ for classes C_1 and C_2 . Assume $P(C_1)=P(C_2)=0.5$

Q2b) Generate two random datasets from $p(x|C_1)$ and $p(x|C_2)$, plot the histograms and $p(x|C_1)$ and $p(x|C_2)$ on the same graph. Plot $P(C_1|x)$ and $P(C_2|x)$ on another graph.

Q2c) Plot the discriminant functions and identify the decision regions R_1 and R_2 for classes C_1 and C_2 .

Q2d) Assume that $P(C_2) = 0.8$, plot the discriminant functions and identify the decision regions R_1 and R_2 for classes C_1 and C_2 .