Codesnatchers



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1 Template

```
#include <bits/stdc++.h>
2 #define endl '\n'
   #define ll long long int
   #define ull unsigned long long int
   #define MOD7 1000000007
   #define MOD9 1000000009
   #define MAX 1000001
   using namespace std;
10
                        -SOLBEGIN----*/
11
12
   void solve() {
13
       return;
14
15
16
   int main() {
       ios_base::sync_with_stdio(0);
18
       cin.tie(0);
19
20
       int t = 1; cin >> t;
21
       while (t--) solve();
22
23
       return 0;
24
25 }
```

2 Data structures

2.1 STL Algorithms

STL stands for Standard Template Library. It is a library that provides several generic classes and functions, allowing programmers to manipulate data structures in an easy and efficient way. The STL provides a range of algorithms which can be used to manipulate data stored in containers. The following list shows some of the algorithms provided by the STL and its functions:

Non-Manipulating Algorithms

- sort(first_iterator, last_iterator) Sorts the elements in the range [first, last) in ascending order.
- sort(frst_iterator, last_iterator, greater<int>()) Sorts elements inside the vector, in descending order.

- reverse(first_iterator, last_iterator) Reverses elements inside a vector.
- *max_element(first_iterator, last_iterator) Finds the maximum element of a vector.
- *min_element(first_iterator, last_iterator) Finds the minimum element of a vector.
- accumulate(first_iterator, last_iterator, initial value of sum) Summates all the vector elements.
- count(first_iterator, last_iterator, x) Counts all occurrences 'x' inside a vector. It has a linear complexity over the quantity of occurrences inside the container; if you fill a set with just one element, the count() function over that element will have an overall complexity of O(|set|) where |set| is the cardinality of the set.
- find(first_iterator, last_iterator, x) Returns an iterator to the first occurrence of 'x' in vector and points to last address if the element is not present.
- binary_search(first_iterator, last_iterator, x) Tests if 'x' exists in sorted vector or not.
- lower_bound(first_iterator, last_iterator, x) Returns an element pointing to the first element in range [first, last), which has a value less than 'x'. Notice that it has a linear complexity over sets and multisets, to avoid this it is necessary to use the member method of those containers.
- upper_bound(first_iterator, last_iterator, x) Returns an element pointing to the first element in range [first, last), which has a value greater than 'x'.

Manipulating Algorithms

- arr.erase(position to delete) Erases selected element in vector and shifts and resizes it accordingly.
- arr.erase(unique(arr.begin(), arr.end()), arr.end()) Erases the duplicate occurrences in sorted vector in a single line.
- next_permutation(first_iterator, last_iterator) Modifies the vector to its next permutation.
- prev_permutation(first_iterator, last_iterator) Modifies the vector to its previous permutation.
- distance(first_iterator, desired_iterator) Returns the distance of the desired position from the first iterator to a desired one.

2.2 Binary Search

```
#include <bits/stdc++.h>
   using namespace std;
   vector<int> vec:
5
   int binary_search_first_occurrence(const vector<int>& vec, int value) {
       // Binary search algorithm finds the first occurrence of a value in
           a sorted vector
       // Declare left and right pointers
       int left = 0;
9
       int right = vec.size() - 1;
10
       int result = -1;
11
       // While left and right pointers do not cross, keep searching
12
       while (left <= right) {</pre>
13
           // Calculate the middle element of the vector
14
           int mid = left + (right - left) / 2;
15
           // If the middle element is the value we are looking for, return
16
                its index
           if (vec[mid] == value) {
17
               result = mid:
18
               // left = mid + 1; // Continue searching in the right half
19
                    (for last occurrence)
               right = mid - 1; // Continue searching in the left half
20
           // If the middle element is smaller than the value we are
21
               looking for, search in the right half
           } else if (vec[mid] < value) {</pre>
22
               left = mid + 1;
23
           // If the middle element is greater than the value we are
24
               looking for, search in the left half
           } else {
25
               right = mid - 1;
26
27
28
       return result; // Returns -1 if value is not found
29
30
31
   int main() {
       // Assign the variable value to the value you want to search
33
       int elements, value = 0;
34
       cin >> elements:
35
       // Read the elements of the vector
36
```

```
UACJ - Codesnatchers
      for (int i = 0; i < elements; i++) {</pre>
37
          int x;
38
          cin >> x;
39
          vec.push_back(x);
40
      }
41
      cout << binary_search_first_occurrence(vec, value);</pre>
42
43
      return 0;
44
45 }
           2.3 Simplified DSU (Stolen from GGDem)
                       2.4 Disjoint Set Union
                          2.5 Segment Tree
```

```
// MAXN = 2^k, n = size of the array
   #define MAXN 262160
   // Define the function fst to be used in the segment tree
   int stsize:
   long long int neut;
   int n;
7
   // Storing the segment tree
   long long int* st = new long long int[2 * MAXN - 1]();
   // Combine the results of two child nodes in the segment tree
   long long int fst(long long int a, long long int b);
12
   // Recursive function to build the segment tree, combining the results
       of the two child nodes
   long long int build(int sti, int csize){
14
       if(csize == 1) return st[sti];
15
       // Combine the results of the two child nodes
16
       return st[sti] = fst(build(sti * 2 + 1, csize / 2), build(sti * 2 +
17
           2, csize / 2));
18
19
   // Initialize the segment tree, setting all the nodes to a neutral value
20
   void innit(){
21
       for(int i = 0; i < stsize; i++) st[i] = neut;</pre>
22
       /*
23
       int d = 0:
24
       for(int i = stsize-n; i<stsize && d<n; i++){</pre>
25
           st[i] = arr[d]; d++;
26
```

```
}
27
       */
28
       build(0,n);
29
   }
30
31
   // Update the value of a node in the segment tree and all its ancestor
   void upd(int ind, long long int val){
       ind = stsize - n + ind;
       st[ind] = val; ind--; ind /= 2;
       while (true) {
           st[ind] = fst(st[ind * 2 + 1], st[ind * 2 + 2]);
           ind--:
           if (ind < 0) break;
           ind \neq 2;
       }
41
   }
42
   // Process a query in the segment tree, from index 1 to r
   long long int rqu(int 1, int r, int sti, int ls, int rs){
       if (1 <= ls && rs <= r) return st[sti];
       if (r < ls || 1 > rs) return neut;
       int m = (rs + ls) / 2;
       return fst(rqu(1, r, sti * 2 + 1, ls, m), rqu(1, r, sti * 2 + 2, m +
49
            1, rs));
50
51
   long long int query(int 1, int r){
       return rqu(1, r, 0, 0, n - 1);
53
54 }
                       2.6 Segment Tree Lazy
                                2.7 Trie
                              3 Graphs
                        3.1 Graph Transversal
                                3.1.1 BFS
#include <bits/stdc++.h>
using namespace std;
3
```

39

```
vector<bool> visited:
   vector<vector<int>> adj;
   void breadth_first_search(int node) {
       // BFS requieres queue data structure, starting from a given initial
8
             node
       queue<int> q;
9
       q.push(node);
10
       visited[node] = true;
11
       // While queue is not empty, pop the first element and push its
12
           children
       while (!q.empty()) {
13
           int v = q.front();
14
           cout << v << "";
15
           q.pop();
16
           // Push all children of v
17
           for (int u : adj[v]) {
18
                // If not visited, push and mark as visited
19
                if (!visited[u]) {
20
                    q.push(u);
21
                    visited[u] = true;
22
                }
23
           }
24
25
26
27
   int main() {
28
       int nodes, edges;
29
       cin >> nodes >> edges;
30
       // Initialize visited and adjacency list
31
       visited.assign(nodes, false);
32
       adj.assign(nodes, vector<int>());
33
       int u. v:
34
       // Values of nodes, given as pairs
35
       for (int i = 0; i < edges; i++) {</pre>
36
           cin >> u >> v;
37
           adj[u].push_back(v);
38
           adj[v].push_back(u); // <- Assuming undirected graph</pre>
39
       }
40
       breadth_first_search(0); // Start BFS from node x
41
42
       return 0;
43
44 | }
```

3.1.2 DFS

```
#include <bits/stdc++.h>
   using namespace std;
   vector<bool> visited:
   vector<vector<int>> adj;
6
   void depth_first_search(int node) {
       // DFS requieres stack data structure, starting from a given initial
             node
       visited[node] = true;
9
       cout << node << ''';
       // For each child of node, if it hasn't been visited, call DFS
11
           function
       for(int i = 0; i < adj[node].size(); i++) {</pre>
12
           int child = adj[node][i];
13
           if(!visited[child]) {
14
                depth_first_search(child);
15
16
       }
17
   }
18
19
   int main() {
       int nodes, edges;
       cin >> nodes >> edges;
22
       // Initialize visited and adjacency list
23
       visited.assign(nodes, false);
24
       adj.assign(nodes, vector<int>());
25
       // Values of nodes, given as pairs
26
       for(int i = 0; i < edges; i++) {</pre>
27
           int u, v;
28
           cin >> u >> v;
29
           adj[u].push_back(v);
30
           adj[v].push_back(u); // <- Assuming undirected graph</pre>
31
32
       // For each node, if it hasn't been visited, call DFS function
33
       for(int i = 0; i < nodes; i++) {</pre>
34
           if(!visited[i]) {
35
                depth_first_search(i);
36
           }
37
       }
38
```

```
5 #define GS 1000
       return 0;
41 }
                                                                                     #define INF 100000000
                                                                                     using namespace std;
                 3.1.3 BFS / DFS using queue and stack
                                                                                     // Define the graph and the distance array
   #define GS 400040
                                                                                     vector<pair<int, int>> graph[GS];
   vector<int> graph[GS];
                                                                                     int distance[GS];
   bitset <GS> vis;
                                                                                  12
                                                                                     void dijkstra(int origin, int size) {
   void bfs(int curr) {
                                                                                         // Set all distances to INF
     queue<int> q;
                                                                                         for (int i = 0; i <= size; i++) distance[i] = INF;</pre>
                                                                                  15
     q.push(curr);
7
                                                                                         // Create the priority queue and the current pair
     while (q.size()) {
8
                                                                                         priority_queue<pair<int, int>, vector<pair<int, int>>, greater<pair<</pre>
                                                                                  17
       curr = q.front(); q.pop();
9
                                                                                             int, int>>> pq;
       if (!q[curr]) {
10
                                                                                         pair<int, int> current;
         q[curr] = 1;
11
        for (int h : graph[curr]) q.push(h);
12
                                                                                         // Set the distance to the origin to 0 and push it to the queue
                                                                                  20
13
                                                                                         pq.push(make_pair(0, origin));
     }
14
                                                                                  22
15
                                                                                         // While the queue is not empty, get the top element and update the
                                                                                  23
16
                                                                                             distances
   void dfs(int curr) {
17
                                                                                         while (!pq.empty()) {
                                                                                  24
     stack<int> s;
18
                                                                                             // Get the top element and pop it
                                                                                  25
     s.push(curr);
19
                                                                                             current = pq.top();
                                                                                  26
     while (s.size()){
20
                                                                                             pq.pop();
                                                                                 27
       curr = s.top(); s.pop();
21
                                                                                  28
       if (!vis[curr]) {
22
                                                                                             // If the distance is already smaller, continue to next
                                                                                  29
         vis[curr] = 1;
23
                                                                                                 iteration
        for (int h : graph[curr]) s.push(h);
24
                                                                                             if (distance[current.second] < current.first) continue;</pre>
                                                                                  30
       }
25
                                                                                             // Update the distance
                                                                                 31
     }
26
                                                                                             distance[current.second] = current.first;
                                                                                 32
  |}
27
                                                                                  33
                                                                                             // Iterate over the neighbors and update the distances
                          3.2 Topological Sort
                                                                                 34
                                                                                             for (pair<int, int> neighbor : graph[current.second]) {
                                                                                  35
                      3.3 APSP: Floyd Warshall
                                                                                                 // If the new distance is smaller, push it to the queue
                                                                                  36
                                                                                                 if ((neighbor.second + current.first) < distance[neighbor.</pre>
                                                                                  37
                                 3.4 SSSP
                                                                                                     firstl) {
                                                                                                     pq.push(make_pair(neighbor.second + current.first,
                            3.4.1 Lazy Dijkstra
                                                                                  38
                                                                                                         neighbor.first));
1 // Lazy version of Dijkstra's algorithm usign priority queue
                                                                                  39
                                                                                             }
  // Works with negative weights while there are no negative cycles
                                                                                  40
  // If there are any negative cycles, the algorithm will not work
                                                                                  41
                                                                                 42 }
4 | #include <bits/stdc++.h>
```

3.4.2 Bellman-Ford

- 3.5 Strongly Connected Components: Kosaraju
- 3.6 Articulation Points and Bridges: ModTarjan

4 Math

4.1 Identities

Coeficientes binomiales. $(a+b)^n = \sum_{k=0}^n {n \choose k} a^{n-k} b^k$

$$(a+b)^{k} = \sum_{k=0}^{n} \binom{k}{k} a^{k} \cdot b^{k}$$

$$\binom{n}{k} = \binom{n}{n-k}$$

$$\binom{n}{k} = \binom{n-1}{k} + \binom{n-1}{k-1}$$

$$k\binom{n}{k} = n\binom{n-1}{k-1}$$

$$\sum_{k=0}^{n} \binom{n}{k} = 2^{n}$$

$$\sum_{k=0}^{n} (-1)^{k} \binom{n}{k} = 0$$

$$\binom{n+m}{t} = \sum_{k=0}^{t} \binom{n}{k} \binom{m}{t-k}$$

$$\sum_{j=k}^{n} \binom{j}{k} = \binom{n+1}{k+1}$$
Números Catalanes.
$$C_{n} = \frac{2(2n-1)}{n+1} C_{n-1}$$

$$C_{n} = \frac{1}{n+1} \binom{2n}{n}$$

$$C_{n} \sim \frac{4^{n}}{n^{3/2}\sqrt{\pi}}$$

$$\sum(n) = O(\log(\log(n))) \text{ (number of divisors of } n)$$

$$F_{2n+1} = F_{n}^{2} + F_{n+1}^{2}$$

$$F_{2n} = F_{n+1}^{2} - F_{n-1}^{2}$$

$$\sum_{i=1}^{n} F_{i} = F_{n+2} - 1$$

$$F_{n+i}F_{n+j} - F_{n}F_{n+i+j} = (-1)^{n}F_{i}F_{j}$$
(Möbius Function)

(Möbius Function)
0 if n is square-free

1 if n got even amount of distinct prime factors 0 if n got odd amount of distinct prime factors

(Möbius Inv. Formula)

Let
$$g(n) = \sum_{d|n} f(d)$$
, then $f(n) = \sum_{d|n} d \mid ng(d)\mu\left(\frac{n}{d}\right)$.

Permutaciones objetos repetidos

$$P(n,k) = \frac{P(n,k)}{n_1! n_2! \dots}$$

Separadores, Ecuaciones lineares a variables = b

$$\binom{\binom{a}{b}}{=}\binom{a+b-1}{b} = \binom{a+b-1}{a-1}$$
Teorema chino

sean $\{n_1, n_2, ..., n_k\}$ primos relativos $P = n_1 \cdot n_2 \cdot ... \cdot n_k$ $P_i = \frac{P}{n_i}$

$$x \cong a_1(n_1)$$

$$x \cong a_2(n_2) \dots x \cong a_k(n_k)$$

$$P_1S_1 \cong 1(n_1) \text{ Donde } S \text{ soluciones.}$$

$$x = P_1S_1a_1 + P_2S_2a_2...P_kS_ka_k$$

4.2 Binary Exponentiation and Modular Arithmetic

4.2.1 Binary Exponentiation

```
#include <bits/stdc++.h>
   #define ll long long
   using namespace std;
   11 \text{ inf} = 10000000007;
   ll bitPow(ll a, ll e) {
       ll res = 1;
       a %= inf;
       // while exponent is greater than zero
11
       while (e > 0) {
12
           // if exponent is odd, multiply result by base
13
14
                // multiply result by base and take the remainder
15
                res = (res * a) % inf;
           // square the base and take the remainder
17
           a = (a * a) \% inf;
           // divide the exponent by 2
19
           e >>= 1:
20
       }
21
22
23
       return res;
24 }
```

4.2.2 Modular Arithmetic

Modular airhmetic is a system of arithmetic for integers, which considers the remainder. In modulus, numbers "wrap around" upon reaching a fixed value.

Congruence

A number $x \mod N$ is the equivalent of the remainder of the division of x by N. Two numbers a and b are congruent modulo N if they have the same remainder upon division by N. We say that N if $a \mod N = b \mod N$.

• For example: $54 \equiv 24 \pmod{7}$ Both numbers are congruent modulo 7, since $54 \pmod{7} = 3$ and $24 \pmod{7} = 3$.

Another way of defining this is by saying that a and b are congruent modulo N if their difference (a-b) is an integer multiple of n, that is, if $\frac{a-b}{n}$ has a reminder of 0.

• For example: $36 \equiv 10 \pmod{13}$ 36 and 10 are congruent modulo 13, since their difference 36-10=26 is a multiple of 13 (n=13).

Addition

Properties of addition in Modular Arithmetic:

- 1. If a + b = c then $a \pmod{N} + b \pmod{N} \equiv c \pmod{N}$.
- 2. If $a \equiv b \pmod{N}$, then $a + k \equiv b + k \pmod{N}$ for any integer k.
- 3. If $a \equiv b \pmod{N}$ and $c \equiv d \pmod{N}$, then $a + c \equiv b + d \pmod{N}$.
- 4. If $a \equiv b \pmod{N}$, then $-a \equiv -b \pmod{N}$.
- For example: Find the sum of 31 and 148 in modulo 24. 31 in modulo 24 is 7 and 148 in modulo 24 is 4. Thus, $31 + 148 \equiv 7 + 4 \equiv 11 \pmod{24}$.
- Another example: Find the remainder when 123 + 234 + 32 + 56 + 22 + 12 + 78 is divided by 3.

We know that 123 mod 3 = 0, 234 mod 3 = 0, 32 mod 3 = 2, 56 mod 3 = 2, 22 mod 3 = 1, 12 mod 3 = 0, and 78 mod 3 = 0. Thus, the sum of all these numbers is 0 + 0 + 2 + 2 + 1 + 0 + 0 = 5, and 5 mod 3 = 2.

Multiplication

Properties of multiplication in Modular Arithmetic:

- 1. If $a \cdot b = c$, then $a \pmod{N} \cdot b \pmod{N} \equiv c \pmod{N}$.
- 2. If $a \equiv b \pmod{N}$, then $a \cdot k \equiv b \cdot k \pmod{N}$ for any integer k.
- 3. If $a \equiv b$ and $c \equiv d \pmod{N}$, then $a \cdot c \equiv b \cdot d \pmod{N}$.
- For example: What is $(8 \cdot 16) \pmod{7}$. Since $8 \equiv 1 \pmod{7}$ and $16 \equiv 2 \pmod{7}$, then $(8 \cdot 16) \equiv (1 \cdot 2) \equiv 2 \pmod{7}$.
- Another example: What is the remainder when $123 \cdot 234 \cdot 32 \cdot 56 \cdot 22 \cdot 12 \cdot 78$ is divided by 3.

We know that $123 \equiv 1$, $134 \equiv 2$, $23 \equiv 2$, $49 \equiv 1$, $235 \equiv 1$ and $13 \equiv 1$, therefore: $123 \cdot 234 \cdot 32 \cdot 56 \cdot 22 \cdot 12 \cdot 78 \equiv 1 \cdot 2 \cdot 2 \cdot 1 \cdot 1 \cdot 1 \equiv 4 \equiv 1 \pmod{3}$. Leaving a remainder of 1.

```
void modArithmetic (int a, int b, int x) {
    // If the result of adding a and b is greater than x, take the
        remainder of the division by x
    (a + b) % x;

// If the result of subtracting a and b is less than 0, add x to the
        result and take the modulus again
    (a - b %x + x) % x;

// If the result of multiplying a and b is greater than x, take the
        remainder of the division by x
    (a * b) % x;
}
```

4.3 Modular Inverse

The modular inverse of an integer a modulo m is an integer x such that $ax \equiv 1 \pmod{m}$.

• If a and N are integers such that gcd(a, N) = 1, then there exists an integer x such that $ax \equiv 1 \pmod{N}$. x is called the modular inverse of a modulo N.

However, $\frac{a}{b} \pmod{N}$ is not the same as $(\frac{(a \mod N)}{(b \mod N)}) \pmod{N}$.

• Lets take a=10, b=2, and N=3. $\frac{10}{2} \pmod{3} = 5 \pmod{3} = 2$; $(\frac{10 \mod 3}{2 \mod 3}) \pmod{3} = (\frac{1}{2}) \pmod{3} = 0.5$. This discrepancy is due to the fact that division is not always compatible with modular arithmetic.

On the other hand, using the extended Euclidean algorithm, we can find the modular inverse of a modulo N:

```
#include <bits/stdc++.h>
   using namespace std;
   int gcdExtended(int a, int b, int& x, int& y) {
       // Base Case
       if (b == 0) {
6
           x = 1;
7
           y = 0;
8
9
           return a;
       }
10
11
12
       int x1, y1;
```

```
int gcd = gcdExtended(b%a, a, &x1, &y1);

x = y1;
y = x1 - y1 * (a / b);

return gcd;
}
```

- 4.4 Modular Binomial Coeficient and Permutations
- 4.5 Non-Mod Binomial Coefficient and Permutations
 - 4.6 Modular Catalan Numbers
 - 4.7 Fractional Ceiling

```
long long int ceil(long long int numerator, long long int denominator) {
return (numerator + denominator - 1) / denominator;
}
```

4.8 Fibonacci Numbers

```
#include <bits/stdc++.h>
using namespace std;

int fibonacci(int x) {
   if (x == 0) return 0;
   if (x == 1) return 1;
   return fibonacci(x - 1) + fibonacci(x - 2);
}
```

4.9 Sieve Of Eratosthenes

```
#include <bits/stdc++.h>
#define MAX 1000001
using namespace std;

// Define both prime and pfix arrays
bool prime[MAX];
int pfix[MAX];

void sieve() {
    // Set all numbers as prime
    memset(prime, true, sizeof(prime));
```

4.10 Sieve-based Factorization

```
#include <bits/stdc++.h>
   #define MAX 1000001
   using namespace std;
   void sieveFactorization() {
       // smallest_prime[i] stores the smallest prime factor of i
       int smallest_prime[MAX];
8
       // Initialize the samllest prime factor of each number
9
       for (int i = 2; i < MAX; i++)
10
           // If i is prime, then the smallest prime factor of i is i,
11
               otherwise is the smallest prime factor of i
           smallest_prime[i] = (i % 2 == 0 ? 2 : i);
12
13
       // Iterate over all odd numbers
14
       for (int i = 3; i * i < MAX; i += 2)
15
           if (smallest_prime[i] == i)
16
               // Marks the smallest prime factor of all multiples of i as
17
                    i, but only if it is the smallest prime factor
               for (int j = i * i; j < MAX; j += i)
18
                   smallest_prime[j] = min(smallest_prime[j],
19
                        smallest_prime[i]);
20 }
```

- 4.11 Cycle Finding
- 4.12 Berlekamp Massey
- 4.13 Modular Berlekamp Massey
 - 4.14 Matrix exponentiation
 - 4.15 Ecuaciones Diofantinas
- 4.16 Pollard-Rho, Stolen from GGDem
 - 4.17 FFT, Stolen from GGDem
 - 4.18 Euler Totient Function
 - 5 Geometry
 - 6 Strings
 - 6.1 Explode by token

```
vector<string> explode_by_token(string const& s, char delimeter) {
     vector<string> result;
2
       // Create a string stream from the string, allowing to perform input
3
           /output operations on strings.
     istringstream iss(s);
4
       // Read the string stream, tokenizing it by the delimeter
5
     for(string token; getline(iss, token, delimeter);) {
6
           // Split the string by the delimeter and push it to the result
7
       result.push_back(move(token));
8
9
       // Return the result vector
10
     return result:
11
12 | }
```

- 6.2 Multiple Hashings DS
- 6.3 Permute chars of string
- 6.4 Longest common subsequence
 - 6.5 KMP
 - 6.6 Suffix Array
 - 6.7 STL Suffix Array
 - 7 Classics
 - 7.1 Job scheduling
 - 7.1.1 One machine, linear penalty
 - 7.1.2 One machine, deadlines
 - 7.1.3 One machine, profit
 - 7.1.4 Two machines, min time
 - 8 Flow
 - 8.1 Dinic

```
#define pb push_back
   #define mp make_pair
   #define fst first
   #define snd second
   #define ALL(s) s.begin(),s.end()
   #define SZ(x) int((x).size())
   #define fore(i, a, b) for(int i = a, to = b; i < to; ++i)</pre>
   using namespace std;
   typedef long long 11;
10
   #define INF (1LL<<62)
   // Min cut: nodes with dist >= 0 vs nodes with dist<0
   // Matching MVC: left nodes with dist < 0 + right nodes with dist > 0
13
14
   struct Dinic{
     int nodes, src, dst;
16
     vector<int> dist, q, work;
17
     struct edge {int to, rev; ll f, cap;};
```

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```
vector<vector<edge>> g;
19
     Dinic(int x):nodes(x), g(x), dist(x), q(x), work(x){}
20
     void add_edge(int s, int t, ll cap){
21
       g[s].pb((edge)\{t, SZ(g[t]), 0, cap\});
^{22}
       g[t].pb((edge){s, SZ(g[s]) - 1, 0, 0});
23
24
     bool dinic_bfs(){
25
       fill(ALL(dist), -1); dist[src] = 0;
26
       int qt = 0; q[qt++] = src;
27
       for(int qh = 0; qh < qt; qh++){
28
         int u = q[qh];
29
         fore(i, 0, SZ(g[u])){
30
           edge &e = g[u][i]; int v = g[u][i].to;
31
           if(dist[v] < 0 \&\& e.f < e.cap) dist[v] = dist[u] + 1, q[qt++] =
32
         }
33
       }
34
       return dist[dst] >= 0;
35
36
     ll dinic_dfs(int u, ll f){
37
       if(u == dst)return f;
38
       for(int &i = work[u]; i < SZ(g[u]); i++){</pre>
39
         edge &e = g[u][i];
40
         if(e.cap <= e.f)continue;</pre>
41
         int v = e.to;
42
         if(dist[v] == dist[u] + 1){
43
           11 df = dinic_dfs(v, min(f, e.cap - e.f));
44
           if(df > 0){e.f += df; g[v][e.rev].f -= df; return df;}
45
         }
46
       }
47
       return 0;
48
49
     11 max_flow(int _src, int _dst){
50
       src = _src; dst = _dst;
51
       11 result = 0;
52
       while(dinic_bfs()){
53
         fill(ALL(work), 0);
54
         while(ll delta = dinic_dfs(src, INF))result += delta;
55
       }
56
       return result;
57
58
   };
59
60
```

```
61 | int main() {
     ios_base::sync_with_stdio(false); cout.tie(NULL); cin.tie(NULL);
       //l set, r set
63
       int n, m;
64
       cin >> n >> m;
65
       m += n;
       Dinic d(n + m + 2);
       for(int i = 1; i <= n; i++) d.add_edge(0, i, 1);</pre>
       for(int i = n + 1; i <= m; i++) d.add_edge(i, m + 1, 1);</pre>
70
       int fin, q;
71
       for(int i = 1; i \le n; i++){
72
            cin >> a:
73
            while(q--){
                cin >> fin;
75
                d.add_edge(i, n + fin, 1);
            }
77
       }
78
       int res = d.max_flow(0, m + 1);
79
       m -= n;
       cout << m - res << endl;</pre>
81
82 }
```

9 Miscellaneous

9.1 Policy Based Data Structures

```
| #include "bits/stdc++.h"
   #include <bits/extc++.h>
   using namespace __gnu_pbds;
   using namespace std;
5 // Defines a new type which is an Order Statistic Tree where each node
       stores a pair of integers, ordered by the pair in ascending order.
6 | typedef tree<pair<int,int>, null_type,less<pair<int,int>>, rb_tree_tag,
       tree_order_statistics_node_update> ost;
   using namespace std;
   int main(){
       // Creates an instance of OST named tree
10
11
      // Inserts 5 elements, each one with a different id
12
       int n = 5:
13
       for(int id = 1; id <= n; id++)
14
```

```
// Inserts a pair with the value and the id
15
           for(int val = 0; val < n; val++)</pre>
16
                tree.insert({val,id});
17
       // Returns the smallest value, in case of a tie it returns the
18
            smallest id
       cout << (*tree.find_by_order(0)).first << "" << (*tree.
19
            find_by_order(0)).second << endl;</pre>
       // Returns the index (0 indexed) of the first ocurrence of .first
20
       cout << tree.order_of_key({1,-1}) << endl;</pre>
^{21}
22 | }
```

9.2 Bit Manipulation

```
#include "bits/stdc++.h"
   using namespace std;
    // Bitmasks are represented from 30 to 62 bits using signed int and
       signed long long int to avoid problems with two's complement
   int main() {
     signed int a, b;
7
     // To multiply a number by two, just apply a left shift
     a = 1;
9
     a = a << 3:
10
11
     // To divide a number by two, just apply a right shift
12
     a = 32;
13
     a = a >> 3;
14
15
       // To turn on the n-th bit of a number, just apply a bitwise OR with
16
            2^(n-1), turns on the third bit
     a = 1;
17
     b = 1 << 2;
18
     a = a \mid b;
19
20
     // To turn off the n-th bit of a number, just apply a bitwise AND with
21
          the complement of ~2^(n-1), turns off the third bit
     a = 5:
22
     b = 1 << 2:
23
     a &= ~b;
24
25
       // To check if the n-th bit of a number is on, just apply a bitwise
26
           AND with 2^(n-1) and check if the result is turned on
```

```
a = 5:
     b = 1 << 2;
28
     a = a \& b;
29
     cout << (a ? "YES" : "NO") << endl;</pre>
30
31
       // To reverse the n-th bit of a number, just power the n-th bit with
32
             2<sup>(n-1)</sup>
     a = 5;
33
     b = 1 << 2;
     a = a \hat{b};
36
       // To obtain the least significant bit of a number that is turned on
37
            , just apply a bitwise AND with the complement of the number and
             add one
     a = 12:
       log2(a & ((-1) * a)) + 1
40
       // To turn on all bits of a number
     a = (1 << 4) - 1:
42
43 }
```

9.2.1 Bitmasking

Bitmasking is a technique used in computer programming to solve problems using individual or groups of bits within a binary number.

It is a powerful tool to solve problems that involve subsets, permutations, and combinations; using bitwise operations such as AND, OR, XOR and NOT.

Some bitmasking utilities are:

- Memory efficiency: Bitmasks can be used for compact and memory efficient storage big collections of data.
- Subset, permutation and combination generation: Can be used to generate all possible subsets, permutations and combinations of a set.
- **Set operations:** Can be used to perform set operations such as union, intersection, and difference.
- Data masking and filtering: By selectively turning on or off bits, we can filter out or mask certain data.
- Optimization: Algorithm optimization can be achieved using bitmasking, substituting bit-level operations for arithmetic operations.

	10 Testin	ıg	32	221760	168	2^6*3^2*5*7*11
		9	33	277200	180	2^4*3^2*5^2*7*11
	10.1 Gen and AutoR	un testcases	34	332640	192	2^5*3^3*5*7*11
			35	498960	200	2^4*3^4*5*7*11
	10.1.1 Gen.c _I	op	36	554400	216	2^5*3^2*5^2*7*11
	10.1.2 Stress tes	sting	37	665280	224	2^6*3^3*5*7*11
	10.1.2 501655 06.	Stille	38	720720	240	2^4*3^2*5*7*11*13
	10.1.3 Autoru	ın	39	1081080	256	2^3*3^3*5*7*11*13
			40	1441440	288	2^5*3^2*5*7*11*13
	10.2 Highly Composi	te Numbers	41	2162160	320	2^4*3^3*5*7*11*13
De	articularly useful when testing numb	or theoretical solutions	42	2882880	336	2^6*3^2*5*7*11*13
1 6	arricularly useful when testing humb	er theoretical solutions.	43	3603600	360	2^4*3^2*5^2*7*11*13
1 1	1		44	4324320	384	2^5*3^3*5*7*11*13
2 2	2 2		45	6486480	400	2^4*3^4*5*7*11*13
3 4	3 2^2		46	7207200	432	2^5*3^2*5^2*7*11*13
4 6	4 2*3		47	8648640	448	2^6*3^3*5*7*11*13
5 12	6 2^2*3	3	48	10810800	480	2^4*3^3*5^2*7*11*13
6 24	8 2^3*3		49	14414400	504	2^6*3^2*5^2*7*11*13
7 36	9 2^2*3		50	17297280	512	2^7*3^3*5*7*11*13
8 48	10 2^4*3	3	51	21621600	576	2^5*3^3*5^2*7*11*13
9 60	12 2^2*3		52	32432400	600	2^4*3^4*5^2*7*11*13
10 120	16 2^3*3	3*5	53	36756720	640	2^4*3^3*5*7*11*13*17
11 180	18 2^2*3	3^2*5	54	43243200	672	2^6*3^3*5^2*7*11*13
12 240	20 2^4*3		55	61261200	720	2^4*3^2*5^2*7*11*13*17
13 360	24 2^3*3	3^2*5	56	73513440	768	2^5*3^3*5*7*11*13*17
14 720	30 2^4*3		57	110270160	800	2^4*3^4*5*7*11*13*17
15 840	32 2^3*3		58	122522400	864	2^5*3^2*5^2*7*11*13*17
16 1260		3^2*5*7	59	147026880	896	2^6*3^3*5*7*11*13*17
17 1680	40 2^4*3	3*5*7	60	183783600	960	2^4*3^3*5^2*7*11*13*17
18 2520		3^2*5*7	61	245044800	1008	2^6*3^2*5^2*7*11*13*17
19 5040		3^2*5*7	62	294053760	1024	2^7*3^3*5*7*11*13*17
20 7560	64 2^3*3	3^3*5*7	63	367567200	1152	2^5*3^3*5^2*7*11*13*17
21 10080	72 2^5*3	3^2*5*7	64	551350800	1200	2^4*3^4*5^2*7*11*13*17
22 15120		3^3*5*7	65	698377680	1280	2^4*3^3*5*7*11*13*17*19
23 20160		3^2*5*7	66	735134400	1344	2^6*3^3*5^2*7*11*13*17
24 25200		3^2*5^2*7	67	1102701600	1440	2^5*3^4*5^2*7*11*13*17
25 27720	96 2^3*3	3^2*5*7*11	68	1396755360	1536	2^5*3^3*5*7*11*13*17*19
26 45360	100 2^4*3	3^4*5*7	69	2095133040	1600	2^4*3^4*5*7*11*13*17*19
27 50400	108 2^5*3	3^2*5^2*7	70	2205403200	1680	2^6*3^4*5^2*7*11*13*17
28 55440		3^2*5*7*11	71	2327925600	1728	2^5*3^2*5^2*7*11*13*17*19
29 83160		3^3*5*7*11	72	2793510720	1792	2^6*3^3*5*7*11*13*17*19
30 110880		3^2*5*7*11	73	3491888400	1920	2^4*3^3*5^2*7*11*13*17*19
31 166320		3^3*5*7*11	74	4655851200	2016	2^6*3^2*5^2*7*11*13*17*19

75	5587021440	2048	2^7*3^3*5*7*11*13*17*19
76	6983776800	2304	2^5*3^3*5^2*7*11*13*17*19
77	10475665200	2400	2^4*3^4*5^2*7*11*13*17*19
78	13967553600	2688	2^6*3^3*5^2*7*11*13*17*19
79	20951330400	2880	2^5*3^4*5^2*7*11*13*17*19
80	27935107200	3072	2^7*3^3*5^2*7*11*13*17*19
81	41902660800	3360	2^6*3^4*5^2*7*11*13*17*19
82	48886437600	3456	2^5*3^3*5^2*7^2*11*13*17*19
83	64250746560	3584	2^6*3^3*5*7*11*13*17*19*23
84	73329656400	3600	2^4*3^4*5^2*7^2*11*13*17*19
85	80313433200	3840	2^4*3^3*5^2*7*11*13*17*19*23
86	97772875200	4032	2^6*3^3*5^2*7^2*11*13*17*19
87	128501493120	4096	2^7*3^3*5*7*11*13*17*19*23
88	146659312800	4320	2^5*3^4*5^2*7^2*11*13*17*19
89	160626866400	4608	2^5*3^3*5^2*7*11*13*17*19*23
90	240940299600	4800	2^4*3^4*5^2*7*11*13*17*19*23
91	293318625600	5040	2^6*3^4*5^2*7^2*11*13*17*19
92	321253732800	5376	2^6*3^3*5^2*7*11*13*17*19*23
93	481880599200	5760	2^5*3^4*5^2*7*11*13*17*19*23
94	642507465600	6144	2^7*3^3*5^2*7*11*13*17*19*23
95	963761198400	6720	2^6*3^4*5^2*7*11*13*17*19*23
96	1124388064800	6912	2^5*3^3*5^2*7^2*11*13*17*19*23
97	1606268664000	7168	2^6*3^3*5^3*7*11*13*17*19*23
98	1686582097200	7200	2^4*3^4*5^2*7^2*11*13*17*19*23
99	1927522396800	7680	2^7*3^4*5^2*7*11*13*17*19*23
100	2248776129600	8064	2^6*3^3*5^2*7^2*11*13*17*19*23
101	3212537328000	8192	2^7*3^3*5^3*7*11*13*17*19*23
102	3373164194400	8640	2^5*3^4*5^2*7^2*11*13*17*19*23
103	4497552259200	9216	2^7*3^3*5^2*7^2*11*13*17*19*23
104	6746328388800	10080	2^6*3^4*5^2*7^2*11*13*17*19*23
105	8995104518400	10368	2^8*3^3*5^2*7^2*11*13*17*19*23
106	9316358251200	10752	2^6*3^3*5^2*7*11*13*17*19*23*29
107	13492656777600	11520	2^7*3^4*5^2*7^2*11*13*17*19*23
108	18632716502400	12288	2^7*3^3*5^2*7*11*13*17*19*23*29
109	26985313555200	12960	2^8*3^4*5^2*7^2*11*13*17*19*23
110	27949074753600	13440	2^6*3^4*5^2*7*11*13*17*19*23*29
111	32607253879200	13824	2^5*3^3*5^2*7^2*11*13*17*19*23*29
112	46581791256000	14336	2^6*3^3*5^3*7*11*13*17*19*23*29
113	48910880818800	14400	2^4*3^4*5^2*7^2*11*13*17*19*23*29
114	55898149507200	15360	2^7*3^4*5^2*7*11*13*17*19*23*29
115	65214507758400	16128	2^6*3^3*5^2*7^2*11*13*17*19*23*29
116	93163582512000	16384	2^7*3^3*5^3*7*11*13*17*19*23*29
117	97821761637600	17280	2^5*3^4*5^2*7^2*11*13*17*19*23*29

```
130429015516800
                        18432
                                         2^7*3^3*5^2*7^2*11*13*17*19*23*29
   195643523275200
                        20160
                                2^6*3^4*5^2*7^2*11*13*17*19*23*29
                        20736
   260858031033600
                                2^8*3^3*5^2*7^2*11*13*17*19*23*29
120
   288807105787200
                        21504
                                2^6*3^3*5^2*7*11*13*17*19*23*29*31
                        23040
                                2^7*3^4*5^2*7^2*11*13*17*19*23*29
   391287046550400
   577614211574400
                        24576
                                2^7*3^3*5^2*7*11*13*17*19*23*29*31
   782574093100800
                        25920
                                2^8*3^4*5^2*7^2*11*13*17*19*23*29
   866421317361600
                        26880
                                2^6*3^4*5^2*7*11*13*17*19*23*29*31
   1010824870255200
                        27648
                                2^5*3^3*5^2*7^2*11*13*17*19*23*29*31
   1444035528936000
                        28672
                                2^6*3^3*5^3*7*11*13*17*19*23*29*31
   1516237305382800
                        28800
                                2^4*3^4*5^2*7^2*11*13*17*19*23*29*31
   1732842634723200
                        30720
                                2^7*3^4*5^2*7*11*13*17*19*23*29*31
   2021649740510400
                        32256
                               2^6*3^3*5^2*7^2*11*13*17*19*23*29*31
   2888071057872000
                        32768
                               2^7*3^3*5^3*7*11*13*17*19*23*29*31
   3032474610765600
                        34560
                               2^5*3^4*5^2*7^2*11*13*17*19*23*29*31
   4043299481020800
                        36864
                                2^7*3^3*5^2*7^2*11*13*17*19*23*29*31
   6064949221531200
                        40320
                                2^6*3^4*5^2*7^2*11*13*17*19*23*29*31
   8086598962041600
                        41472
                                2^8*3^3*5^2*7^2*11*13*17*19*23*29*31
   10108248702552000
                        43008
                                2^6*3^3*5^3*7^2*11*13*17*19*23*29*31
   12129898443062400
                        46080
                                2^7*3^4*5^2*7^2*11*13*17*19*23*29*31
   18194847664593600
                        48384
                                2^6*3^5*5^2*7^2*11*13*17*19*23*29*31
   20216497405104000
                        49152
                                2^7*3^3*5^3*7^2*11*13*17*19*23*29*31
   24259796886124800
                        51840
                                2^8*3^4*5^2*7^2*11*13*17*19*23*29*31
   30324746107656000
                        53760
                                2^6*3^4*5^3*7^2*11*13*17*19*23*29*31
   36389695329187200
                        55296
                                2^7*3^5*5^2*7^2*11*13*17*19*23*29*31
   48519593772249600
                        57600
                                2^9*3^4*5^2*7^2*11*13*17*19*23*29*31
   60649492215312000
                        61440
                                2^7*3^4*5^3*7^2*11*13*17*19*23*29*31
   72779390658374400
                        62208
                                2^8*3^5*5^2*7^2*11*13*17*19*23*29*31
   74801040398884800
                        64512
                                2^6*3^3*5^2*7^2*11*13*17*19*23*29*31*37
   106858629141264000
                       65536
                                2^7*3^3*5^3*7*11*13*17*19*23*29*31*37
   112201560598327200
                       69120
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   299204161595539200
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   748010403988848000
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   897612484786617600
                       103680 2^8*3^4*5^2*7^2*11*13*17*19*23*29*31*37
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