

# Everyone's Connected



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1 Template

```
1 #include <bits/stdc++.h>
2 #define ll long long int
3 #define ull unsigned long long int
4
5 using namespace std;
6
7 void solve() {
8     return;
9 }
10
11 int main() {
12     ios_base::sync_with_stdio(0);
13     cin.tie(0);
14
15     int t = 1; cin >> t;
16     while (t--) solve();
17
18     return 0;
19 }
```

## 2 Data structures

### 2.1 Simplified DSU (Stolen from GGDem)

### 2.2 Disjoint Set Union

### 2.3 Segment tree

### 2.4 Segment tree Lazy

### 2.5 Trie

## 3 Graphs

### 3.1 Graph Transversal

#### 3.1.1 BFS

#### 3.1.2 DFS

### 3.2 Topological Sort

### 3.3 APSP: Floyd Warshall

### 3.4 SSSP

#### 3.4.1 Lazy Dijkstra

#### 3.4.2 Bellman-Ford

### 3.5 Strongly Connected Components: Kosaraju

### 3.6 Articulation Points and Bridges: ModTarjan

## 4 Math

### 4.1 Identities

**Coefficientes binomiales.**

$$(a+b)^n = \sum_{k=0}^n \binom{n}{k} a^{n-k} b^k$$

$$\binom{n}{k} = \binom{n}{n-k}$$

$$\binom{n}{k} = \binom{n-1}{k} + \binom{n-1}{k-1}$$

$$k \binom{n}{k} = n \binom{n-1}{k-1}$$

$$\sum_{k=0}^n n \binom{n}{k} = 2^n$$

$$\sum_{k=0}^n (-1)^k \binom{n}{k} = 0$$

$$\binom{n+m}{t} = \sum_{k=0}^t \binom{n}{k} \binom{m}{t-k}$$

$$\sum_{j=k}^n \binom{j}{k} = \binom{n+1}{k+1}$$

**Numeros Catalanos.**

$$C_n = \frac{2(2n-1)}{n+1} C_{n-1}$$

$$C_n = \frac{1}{n+1} \binom{2n}{n}$$

$$C_n \sim \frac{4^n}{n^{3/2} \sqrt{\pi}}$$

$$\Sigma(n) = O(\log(\log(n))) \text{ (number of divisors of } n)$$

$$F_{2n+1} = F_n^2 + F_{n+1}^2$$

$$F_{2n} = F_{n+1}^2 - F_{n-1}^2$$

$$\sum_{i=1}^n F_i = F_{n+2} - 1$$

$$F_{n+i} F_{n+j} - F_n F_{n+i+j} = (-1)^n F_i F_j$$

**(Möbius Function)**

0 if n is square-free

1 if n got even amount of distinct prime factors

0 if n got odd amount of distinct prime factors

**(Möbius Inv. Formula)**

Let  $g(n) = \sum_{d|n} f(d)$ , then  $f(n) = \sum_{d|n} d \mu\left(\frac{n}{d}\right)$ .

**Permutaciones objetos repetidos**

$$P(n, k) = \frac{P(n, k)}{n_1! n_2! \dots}$$

**Separadores, Ecuaciones lineales a variables = b**

$$\binom{a}{b} = \binom{a+b-1}{b} = \binom{a+b-1}{a-1}$$

**Teorema chino**

sean  $\{n_1, n_2, \dots, n_k\}$  primos relativos

$$P = n_1 \cdot n_2 \cdot \dots \cdot n_k$$

$$P_i = \frac{P}{n_i}$$

$$x \cong a_1(n_1)$$

$$x \cong a_2(n_2) \dots x \cong a_k(n_k)$$

$$P_1 S_1 \cong 1(n_1) \text{ Donde } S \text{ soluciones.}$$

$$x = P_1 S_1 a_1 + P_2 S_2 a_2 \dots P_k S_k a_k$$

## 4.2 Binary Exponentiation and modArith

### 4.3 Modular Inverse (dividir mod)

### 4.4 Modular Binomial Coefficient and Permutations

### 4.5 Non-Mod Binomial Coefficient and Permutations

### 4.6 Modular Catalan Numbers

### 4.7 Ceil Fraccionario

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### 4.12 Berlekamp Massey

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### 4.14 Matrix exponentiation

### 4.15 Ecuaciones Diofantinas

### 4.16 Pollard-Rho, Stolen from GGDem

### 4.17 FFT, Stolen from GGDem

### 4.18 Euler Totient Function

## 5 Geometry

## 6 Strings

### 6.1 Explode by token

### 6.2 Multiple Hashings DS

### 6.3 Permute chars of string

### 6.4 Longest common subsequence

### 6.5 KMP

### 6.6 Suffix Array

### 6.7 STL Suffix Array