

Q1. (20 Marks)	Choose the correct option for following questions. All the Questions are compulsory and carry equal marks
1.	_____ is the class of decision problems that can be solved by non-deterministic polynomial algorithms.
Option A:	NP
Option B:	P
Option C:	Hard
Option D:	Complete
2.	Following data structure is used to implement LIFO Branch and Bound Strategy
Option A:	Priority Queue
Option B:	array
Option C:	stack
Option D:	Linked list
3.	For the given elements 6 4 11 17 2 24 14 using quick sort, what is the sequence after first phase, assuming the pivot as the first element?
Option A:	2 4 6 17 11 24 14
Option B:	2 4 6 11 17 14 24
Option C:	4 2 6 17 11 24 14
Option D:	2 4 6 11 17 24 14
4.	Which of the following is correct for branch and bound technique? i. It is BFS generation of problem states ii. It is DFS generation of problem states iii. It is D-search.
Option A:	Only i
Option B:	Only ii
Option C:	Only ii and iii
Option D:	Only i, and iii
5.	Consider the given graph.

		What is the weight of the minimum spanning tree using the Kruskal's algorithm?
Option A:	24	
Option B:	23	
Option C:	15	
Option D:	19	
6.	Bellman Ford algorithm is used to find out single source shortest path for negative edge weights. Bellman Ford algorithm uses which of the following strategy?	
Option A:	Greedy method	
Option B:	Dynamic Programming	
Option C:	Backtracking	
Option D:	Divide and Conquer	
7.	The optimal solution for 4-queen problem is	
Option A:	(2,3,1,4)	
Option B:	(1,3,2,4)	
Option C:	(3,1,2,4)	
Option D:	(2,4,1,3)	
8.	<p>Consider the following code snippet:</p> <pre> Bounding function(k,i) {     for(j=1 to k-1)         { if ((x[j]==i) or (Abs(x[j]-i) ==abs(j-k))) return false;         } return true } </pre> <p>The above code represents the bounding function for which of the following algorithm?</p>	
Option A:	Subset sum problem using backtracking	
Option B:	n-queens using backtracking	
Option C:	Graph coloring using backtracking	
Option D:	Subset sum using branch and bound	
9.	What do you mean by chromatic number?	
Option A:	The minimum number of colors needed to color all the vertices optimally in a Graph	

	Coloring problem
Option B:	The maximum number of colors needed to color all the vertices optimally in a Graph Coloring problem
Option C:	The number of colors using which the edges of graph have been colored in a Graph Coloring Problem
Option D:	The individual colors with which we color the vertices of a Graph in a Graph Coloring Problem
10.	Which string matching algorithm uses a Prefix Table?
Option A:	Naïve String Matching Algorithm
Option B:	Boyer Moore String Matching Algorithm
Option C:	Knuth Morris Pratt Algorithm
Option D:	Rabin Karp Algorithm

<b>Q2.</b> <b>(20 Marks)</b>	<b>Solve any Four out of Six</b>	<b>05 marks each</b>
A	Write and Explain binary search algorithm.	
B	Write a short note on job sequencing with deadline	
C	Determine the LCS of the following sequences: X: {A, B, C, B, D, A, B} Y: {B, D, C, A, B, A}	
D	Solve the sum of subsets problem for the following: n=4, m=15, w={3,5,6,7}	
E	Give the algorithm for the N-Queen's problem and give any two solutions to the 8-Queen's problem	
F	Explain and apply Naïve string matching on following strings String1: COMPANION String2: PANI	

<b>Q3.</b> <b>(20 Marks)</b>	<b>Solve any Two Questions out of Three</b>	<b>10 marks each</b>
A	Write algorithm for greedy knapsack and Obtain the solution to following knapsack problem where n=7,m=15 (p <sub>1</sub> ,p <sub>2</sub> .....p <sub>7</sub> ) = (10,5,15,7,6,18,3), (w <sub>1</sub> ,w <sub>2</sub> ,...,w <sub>7</sub> ) = (2,3, 5,7,1,4,1).	
B	Explain Dijkstra's Single source shortest path algorithm. Explain how it is different from Bellman Ford algorithm. Explain 15-puzzle problem using LC search technique.	
C	Rewrite and Compare Rabin Karp and Knuth Morris Pratt Algorithms Give the pseudo code for the KMP String Matching Algorithm.	

<b>Q4.</b> <b>(20 Marks)</b>	<b>Solve any Two Questions out of Three</b>	<b>10 marks each</b>
A	Write algorithm for quick sort and sort the following elements [40,11,4,72,17,2,49]	
B	Write multistage graph algorithm and solve following example.	

C	<p>Write algorithm for 0/1 knapsack problem using dynamic programming .Also solve the following example.</p> <p>N=4, M=21 (p1,p2,p3,p4)=(2,5,8,1), (w1,w2,w3,w4)=(10,15,6,9)</p>

**(3 Hours)**

**[Total Marks: 80]**

N.B.: (1) Question No.1 is compulsory.

- (2) Attempt **any three** out of remaining questions.  
(3) Assume Suitable data if necessary.  
(4) **Figures to the right** indicate full **marks**.

- Q1**
- a. Differentiate between Greedy method and Dynamic Programming. 5
  - b. Write an algorithm for finding minimum and maximum number from a given set 5
  - c. Explain coin changing problem 5
  - d. Explain Flow Shop Scheduling Technique 5

- Q2a.** Define AVL tree. Construct an AVL tree for the following data. 10

63, 9, 19, 27, 18, 108, 99, 81

- b. Write an algorithm for implementing Quick sort. Also, comment on its complexity. 10

- Q3a.** What is longest common subsequence problem? Find LCS for the following string: 10

String X: ABCDGH

String Y: AEDFHR

- b. Explain Rabin Karp Algorithm in detail. 10

- Q4a.** Which are the different methods of solving recurrences? Explain with suitable examples. 10

- b. Explain Travelling Salesman Problem with an example. 10

- Q5a.** Explain Huffman Algorithm. Construct a Huffman Tree and find Huffman code for the message: KARNATAKA. 10

- b. Explain Knapsack Problem with an example. 10

- Q6** Write Short notes on **(any four)** 20

- a. Genetic Algorithm
- b. Red and Black Tree
- c. Merge Sort
- d. Knuth Morris Pratt Algorithm
- e. Optimal Binary Search Tree (OBST)

(3 Hours)

[Marks: 80]

- N.B.: 1) Question No. 1 is compulsory.  
 2) Answer any three out of remaining questions.  
 3) Assume suitable data if necessary.  
 4) Figures to the right indicate full marks.

Q1. (a) Compute the worst case complexity of the following program segment:

```
void fun(int n, int arr[]){
    int i = 0, j = 0;
    for(; i < n; ++i)
        while(j < n && arr[i] < arr[j])
            j++;
}
```

(b) Differentiate between greedy method and dynamic programming? (5)

(c) . What is the optimal Huffman code for the following set of frequencies, based on the first 8 Fibonacci numbers?

a:1 b:1 c:2 d:3 e:5 f:8 g:13 h:21

(d) Find Longest Common Subsequence for the following: (5)

String x=ACBAED

String y=ABCABE

Q2. (a) Consider the instance of knapsack problem where n=6, M=15, profits are (P<sub>1</sub>, P<sub>2</sub>, P<sub>3</sub>, P<sub>4</sub>, P<sub>5</sub>, P<sub>6</sub>)=(1,2,4,4,7,2) and weights are (W<sub>1</sub>, W<sub>2</sub>, W<sub>3</sub>, W<sub>4</sub>, W<sub>5</sub>, W<sub>6</sub>)=(10,5,4,2,7,3). Find maximum profit using fractional Knapsack. (10)

(b) Explain divide and conquer approach. Write a recursive algorithm to determine the max and min from given elements. (10)

Q3. (a) Define AVL tree. Construct AVL tree for the following data: (10)

21,26,30,9,4,14,28,18,15,10,2,3,7

(b) A traveler needs to visit all the cities from a list (figure 1), where distances between all the cities are known and each city should be visited just once. What is the shortest possible route that he visits each city exactly once and returns to the origin city? (10)

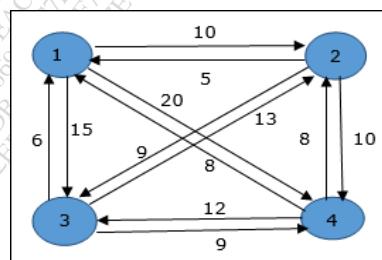


Figure 1.

Q4. (a) Construct a minimum spanning tree shown in figure 2 using Kruskal's and Prim's Algorithm and find out the cost with all intermediate steps. (10)

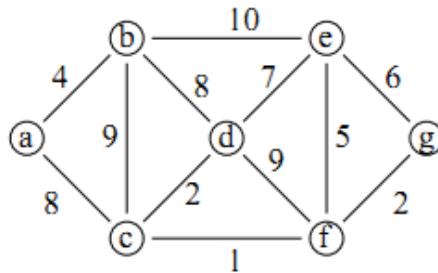


Figure 2

(b) What is optimal binary search tree? Explain with the help of example. (10)

Q5. (a) Give asymptotic upper bound for  $T(n)$  for the following recurrences and verify your answer using Masters theorem:

$$T(n) = T(n-1) + n \quad (10)$$

(b) Given a set of 9 jobs ( $J_1, J_2, J_3, J_4, J_5, J_6, J_7, J_8, J_9$ ) where each job has a deadline (5,4,3,3,4,5,2,3,7) and profit (85,25,16,40,55,19,92,80,15) associated to it. Each job takes 1 unit of time to complete and only one job can be scheduled at a time. We earn the profit if and only if the job is completed by its deadline. The task is to find the maximum profit and the number of jobs done. (10)

Q6. Explain any Two: (20)

- a) Rabin Karp Algorithm
- b) Genetic Algorithm
- c) Minimum Cost Spanning Tree
- d) Red Black Trees

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TR / Sem 2 / CBCGS / IT / ND-18 / 12-12-2018

(3 Hours)

[Total Marks: 80]

N.B.: (1) Question No.1 is compulsory.

(2) Attempt any three out of remaining questions.

(3) Assume Suitable data if necessary.

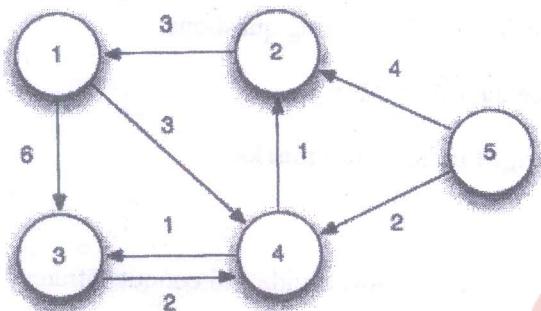
(4) Figures to the right indicate full marks.

- Q1. (a) Explain with example how divide and conquer strategy is used in Binary Search? 5  
(b) Explain flow shop scheduling technique 5  
(c) Write a note on AVL Tree. 5  
(d) Write an algorithm for finding minimum and maximum number from given set. 5
- Q2. (a) What is longest common subsequence problem? Find LCS for following string. 10  
  
X=ACBAED  
Y=ABCABE
- (b) Which are the different methods of solving recurrences? Explain with examples. 10
- Q3. (a) Compare Greedy and Dynamic Programming approach for an algorithm design. Explain how both can be used to solve knapsack problem. 10  
(b) Explain Huffman algorithm. Construct Huffman tree for MAHARASHTRA with its optimal code. 10
- Q4. (a) Explain Job sequencing with deadlines. 10  
Let  $n=4, (p_1, p_2, p_3, p_4)=(100, 10, 15, 27)$  and  $(d_1, d_2, d_3, d_4)=(2, 1, 2, 1)$ . Find feasible solution.  
  
(b) Sort the following numbers using quick sort. Also derive time complexity of quick sort. 10

27 10 36 18 25 45

Q5. (a) Apply all pair shortest path on the following graph

10



(b) Given a chain of four matrices  $A_1, A_2, A_3$  and  $A_4$  with  $P_0=5, P_1=4, P_2=6, P_3=2$  and  $P_4=7$ . Find  $m[1,4]$  using matrix multiplication

10

Q6. Write Note on (Any two)

20

- Rabin Karp Algorithm.
- Topological Sort.
- Knuth-Morrie-Pratt algorithm.
- Red-Black Tree.

( 3 Hours )

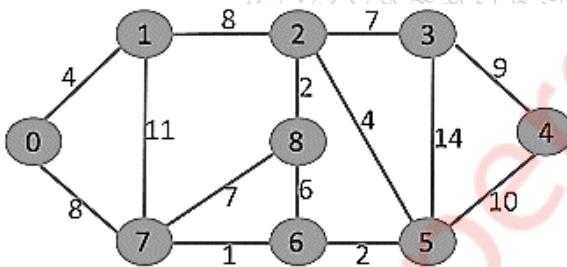
[ Total Marks : 80 ]

- N.B.:** (1) **Question No. 1 is compulsory.**  
 (2) Attempt **any three** out of the remaining **five** questions.  
 (3) Assumptions made should be **clearly stated.**

1. (a) Explain recurrences and various methods to solve recurrences. **5**  
 (b) Differentiate between P and NP. **5**  
 (c) Differentiate between Prims and Kruskals algorithm. **5**  
 (d) Explain Dynamic programming with example. **5**

2. (a) Define Branch and Bound and Explain 15 Puzzle problem. **10**  
 (b) Apply dijkstra's algorithm on the following graph. **10**

Consider vertex 0 as source.



3. (a) Find Longest Common Subsequence for Following strings : **10**

X = ababcde

Y = bacadb

- (b) Explain Backtracking with n-queen problem. **10**

4. (a) Formulate Knapsack problem , Explain and differentiate between greedy knapsack and 0/1 knapsack. **10**

- (b) Explain Multistage graph with example. **10**

5. (a) Rewrite KMP algorithm and explain with example. **10**

- (b) Define chromatic number of graph. Explain Graph coloring algorithm. **10**

6. Write a short note on following (any 4) : **20**

- a) Master theorem
- b) Rabin Karp algorithm
- c) Steps for NP Completeness proofs
- d) Assembly line scheduling problem
- e) Strassen's matrix multiplication

(3 Hours)

Total Marks: 80



N.B.: (1) Question No. 1 is compulsory.  
 (2) Attempt any three questions out of remaining five questions.

- Q1. a) Sort the following numbers using Merge Sort. Also derive the time complexity of Merge Sort.

70, 20, 30, 40, 10, 50, 60

(10)

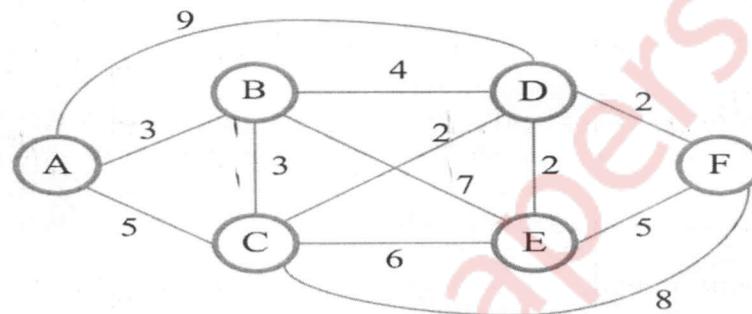
- b) Explain different string matching algorithms.

(10)

- Q2. a) Write an algorithm to find minimum and maximum value using divide and conquer and also derive its complexity.

(10)

- b) Find the shortest path from source vertex A using Dijkstra's algorithm



- Q3. a) Write an algorithm for sum of subsets. Solve the following problem.

 $M=30 \quad W=\{5, 10, 12, 13, 15, 18\}$ 

(10)

- b) Explain optimal storage on tape with example.

(10)

- Q4. a) Find an optimal solution to the knapsack instance  $n=5, m=60$

profit = {30, 20, 100, 90, 160}

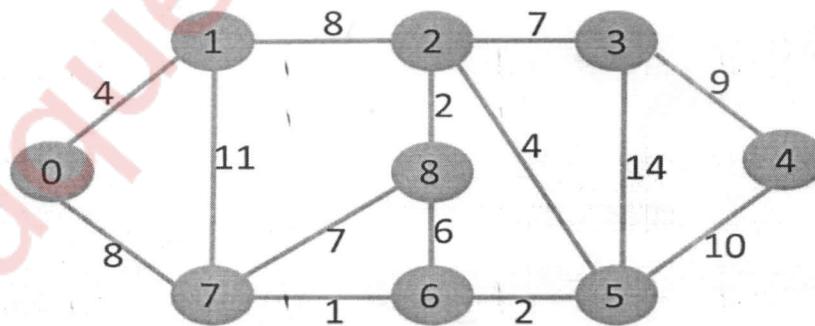
weight = {5, 10, 20, 30, 40}

(10)

- b) Explain longest common subsequence with example.

(10)

- Q5. a) Find the Minimum Spanning Tree of the following graph using prim's algorithm



- b) Explain flow shop scheduling with example.

(10)

- Q7. Write note on (any two):

(20)

- a) Strassen's matrix multiplication.
- b) 15-puzzle problem.
- c) Job sequencing with deadlines.
- d) N-Queen problem.

**Duration : 3 Hrs****Maximum Marks : 80**

Note:

- 1) Question No 1 is compulsory.  
 2) Solve any three questions out of remaining five questions.

**Q.1)****Solve any 4****20**

- 1) Derive the complexity of quick sort for best case and worst case.
- 2) What is asymptotic analysis? Define Big O, Omega and Theta notations.
- 3) Write an algorithm to find all pairs shortest path using dynamic programming.
- 4) Write a note on "Optimal Storage on Tapes".
- 5) Define master theorem. Solve the following using master method.  
 $T(n)=8T(n/2)+n^2$

**Q.2.**

- A) Write an algorithm for finding minimum and maximum using divide and conquer. Also derive its complexity.

**10**

- B) Write Kruskal's algorithm and show its working by taking suitable example of graph with 5 vertices.

**10****Q.3.**

- A) Solve fractional knapsack problem for the following.

**10**

$n=6, p=(18, 5, 9, 10, 12, 7) \quad w=(7, 2, 3, 5, 3, 2)$

- B) Write an algorithm for Knuth Morris Pratt (KMP) pattern matching.

**10****Q.4.**

- A) Write an algorithm to solve N Queens problem. Show its working for  $N = 4$ .

**10**

- B) Write an algorithm to solve sum of subset problem and solve the following problem.  $n=4, w = \{4, 5, 8, 9\}$ , required sum = 9.

**10****Q.5.**

- A) Prove that Vertex Cover problem is NP Complete.

**10**

- B) Find the longest common subsequence for the following two strings.

**10**

X=ABACABB Y= BABCAB

**Q.6)****Write short note on any 2.****20**

- (a) Assembly Line Scheduling
- (b) Job Sequencing with Deadlines
- (c) 15 Puzzle Problem (d) P, NP and NPC Classes

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**Subject: Correction in \t1T00724 - S.E.(Computer Engineering)(SEM-IV)  
(Choice Base) / 40502 - Analysis of Algorithms Qp Code 55801**

From: University of Mumbai<support@muapps.in> on Mon, 13 May 2019 15:09:42

To: <exam\_kgce2010@rediffmail.com>



University of Mumbai

Correction in 1T00724 - S.E.(Computer Engineering)(SEM-IV)(Choice Base) / 40502 - Analysis of Algorithms Qp Code 55801

**Q.3.A) Missing Information is as follows**

**Max sack capacity M=13**

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(3 Hours)

Total Marks: 80



N.B: (1) Question No.1 is compulsory

(2) Attempt any three questions of the remaining five questions

(3) Figures to the right indicate full marks

(4) Make suitable assumptions wherever necessary with proper justifications

- Q.1 (a) Explain asymptotic notations. (5)  
(b) Explain Randomized algorithms. (5)  
(c) Write an Algorithm for Merge sort and derive its best case and worst case complexity. (10)

- Q.2 (a) Explain Master's Theorem to find the complexity of a recurrence relation (10)  
(b) Explain Naïve string matching algorithm with example. (10)

- Q.3 (a) Explain Single source shortest path algorithm using Dynamic programming with suitable example. (10)  
(b) Write an Algorithm for Graph Coloring problem. Also derive its complexity. (10)

- Q.4 (a) Write an Algorithm for knapsack problem using Greedy method. (10)  
Also derive its complexity  
(b) Explain the using Travelling Salesman Problem using Branch and Bound (10)

- Q.5. (a) Explain Flow shop scheduling technique. (10)  
(b) Write an Algorithm to find minimum cost spanning tree. Also derive its complexity. (10)

- Q.6. Write Short notes on (any two) (20)  
(a) Strassen's matrix multiplication  
(b) Job- Sequencing with deadlines.  
(c) Multistage Graphs

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Time Duration: 03Hrs

Marks: 80

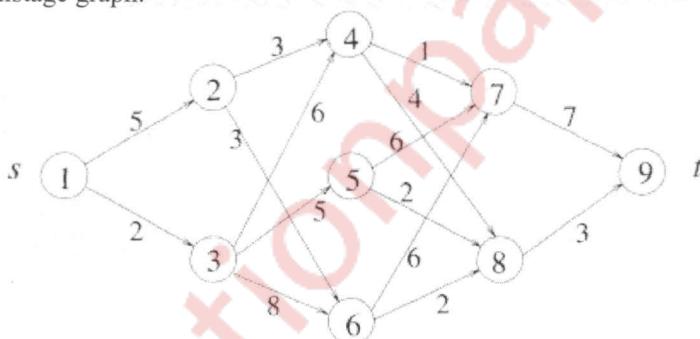
Note: Question 1 is compulsory.

Attempt any three out of remaining five questions.

Make suitable assumptions whenever necessary.



- Q.1 [a] Explain the Strassen's matrix multiplication concept with an example. [10]  
 Derive it's time complexity.
- [b] Apply the quick sort algorithm to sort the list. E,X,A,M,P,L,E in alphabetical order. Analyze the best case, worst case and average case complexities of quick sort. [10]
- Q.2 [a] Solve following problem of sum of subset and draw portion of state space tree.  
 $w = (5, 7, 10, 12, 15, 18, 20)$  and  $m=35$ .  
 Find all possible subsets of  $w$  that sum to  $m$ . [10]  
 [b] What is single source shortest path algorithm. Write an algorithm to find single source shortest path using greedy methods [10]
- Q.3 [a] Prove that vertex cover problem is NP complete. [10]  
 [b] Explain various string matching algorithms. [10]
- Q.4 [a] Find the minimum cost path from  $s$  to  $t$  in the following figure using multistage graph. [10]



- [b] Describe the Travelling sales person problem and discuss how to solve it using dynamic programming with example. [10]
- Q.5 [a] What is longest common subsequence problem? Find the LCS for the following problem. [10]  
 [b] Write a short note on 8 queen problem, Write an algorithm for the same. [10]
- Q.6 Write a short note on(Any two)  
 1.Branch and Bound Strategy. [10]  
 2.Algorithms to find minimum spanning tree. [10]  
 3.Recurrences.

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Mailbox of exam\_kgce2010

## Subject: Correction in QP CODE: 55800

From: University of Mumbai<support@muapps.in> on Tue, 27 Nov 2018 15:29:39

To: <exam\_kgce2010@rediffmail.com>



University of Mumbai

Correction in 1T00724 - S.E.(COMPUTER)(Sem IV) (Choice Based) / 40502 - ANALYSIS OF  
ALGORITHM                   **QP CODE: 55800**

Q 5 a.Whats is longest common sub sequence problem ?Find the LCS for the following problem.

s1=abcdaf

s2=acbcf.

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Time: 3 Hours

Marks: 80

## N.B

- (1) Question no. 1 is compulsory.
- (2) Attempt any 3 from the remaining questions.
- (3) Assume suitable data if necessary.
- (4) Figures to right indicate full marks.



- Q.1 a. Consider the instance of knapsack problem where  $n=6$ ,  $M=15$ , 08  
 Projects are  $(P_1, P_2, P_3, P_4, P_5, P_6) = (1, 2, 4, 4, 7, 2)$  and weights are  $(W_1, W_2, W_3, W_4, W_5, W_6) = (10, 5, 4, 2, 7, 3)$ . Find Max Profit using Fractional Knapsack. 02
- b. Compute worst case complexity of following program segment
- ```
sum = 0;
for( i = 0; i < n; i++ )
    for( j = 0; j < i; j++ )
        sum++;
```
- c. Write Quicksort algorithm using Divide and Conquer approach. Derive its complexity for all the three cases. 10
- Q.2 a. Explain Divide and Conquer approach. Write a recursive algorithm to determine the max and min from given elements and explain. 20  
 Derive the time complexity of this algorithm and compare it with a simple brute force algorithm for finding max and min.  
 For the following list of elements trace the recursive algorithm for finding max and min and determine how many comparisons have been made.  
 22,12,-5,-8,15,60,17,31,47
- Q.3 a. What is optimal binary search tree? Let  $n = 3$  and  $\{a_1, a_2, a_3\} = \{\text{do, if, while}\}$ . Let  $p(1:3) = \{0.5, 0.1, 0.05\}$  and  $q(0:3) = \{0.15, 0.1, 0.05, 0.05\}$ . Compute and construct OBST for above value using Dynamic Programming. 12  
 b. Solve 8 puzzle problem by Branch and Bound. Draw State space tree. 08

|   |   |   |
|---|---|---|
| 1 | 2 | 3 |
| 5 | 6 |   |
| 7 | 8 | 4 |

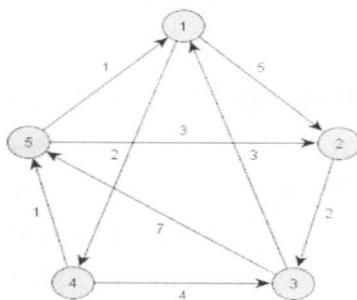
Initial state

|   |   |   |
|---|---|---|
| 1 | 2 | 3 |
| 5 | 8 | 6 |
| 7 | 4 |   |

Final State

- Q.4 Write and Explain the algorithm to compute all pair source shortest path using dynamic programming and prove that it is optimal. 20  
 For the following graph determine the all pairs source shortest path

TURN OVER



- Q.5 a. Write an algorithm to determine the sum of subsets for a given Sum and a Set of numbers. Draw the tree representation to solve the subset sum problem given the numbers set as {3,5,6,7,2} with sum = 15. Derive all the subsets. Comment on the complexity of the algorithm. 15
- Q.5 b. An algorithm takes 0.5ms for input size 100. How long will it take for an input size 500. If the running time is following 05
- Linear
  - Quadratic
  - Cubic
  - $\sqrt{n}$
  - $n \log_2 n$
- Q.6 A Explain the idea behind backtracking? Write an algorithm for N-queen problem. Draw state space tree for 4-queen problem. 12
- b What is LCS? Find LCS for string S = "ABAZDC" and T= "BACBAD" 08

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(3 Hours)

[Total Marks:80]



1. Question No. 1 is compulsory.
2. Attempt any three out of remaining five questions.
3. Make suitable assumptions wherever necessary and justify it.
4. Figures to right indicate full marks.

Q.1 Answer the following

- a. Write the difference between greedy method and dynamic programming. 5M
- b. Explain the general procedure of divide and conquer method. 5M
- c. Determine the frequency counts for all statements in the following algorithm segment. 5M

```
I=1;
While(I<=n)
{
    X=X+I;
    I=I+1;
}
```

- d. What is backtracking Approach? Explain how it is used in Graph Coloring 5M

- Q.2.a. Explain with example how divide and conquer strategy is used in binary search? 10M
- b. Solve sum of subsets problem for following  
 $N=6$   $W=\{3,5,7,8,9,15\}$  &  $M=20$  Also write the Algorithm for it. 10M

- Q.3 a. Obtain the solution to knapsack problem by Greedy method  $n=7, m=15$  ( $p_1, p_2, \dots, p_7)=(10,5,15,7,6,18,3)$ ,  $(w_1, w_2, \dots, w_7)=(2,3,5,7,1,4,1)$ ) 10M
- b. Sort the list of the elements 10,5,7,6,1,4,8,3,2,9 using merge sort algorithm and show its computing time is  $O(n \log n)$ . 10M

- Q. 4.a. Explain different string matching algorithms. 10 M
- b. What do you understand by NP Complete? Explain Is Subset sum problem NP complete? If so explain. 10M

- Q. 5.a. Write a detailed note on Hamiltonian cycles. 10 M
- b. Explain how backtracking is used for solving n-queens problem. Show the state space tree. 10M

- Q.6 Write Short Note on (any 2) 20 M
- a. Job sequencing with deadlines
  - b. 8 queens problem
  - c. Longest common subsequence

Max Marks: 80

Time Duration: 3 Hrs

Note : Question number 1 is Compulsory.

Solve any Three questions from Remaining.

Q1. Answer Following Questions (Any Four)

20M

- a) What is backtracking Approach. Explain how it is used in graph coloring.
- b) Explain Randomized algorithm with example.
- c) What is Knuth Morris Pratt Method of Pattern Matching? Give Examples.
- d) Explain in brief the concept of Multistage Graphs?
- e) Merge sort and its complexity.

Q2. A) Derive and comment on the complexity of Quick Sort algorithm.

10M

b) Solve Following Knapsack problem using dynamic approach.

10M

N=4 items, capacity of knapsack M=9

| Item i | Value vi | Weight wi |
|--------|----------|-----------|
| 1      | 18       | 2         |
| 2      | 25       | 4         |
| 3      | 27       | 5         |
| 4      | 10       | 3         |

Q3. A) What is sum of Subset problem? Write the Algorithm and solve following.

10M

array A = [2,3,5,6,7,8,9] and K = 15

b) Write the algorithm for finding strassens matrix multiplication and show how the complexity is being affected?. 10M

Q4. A) What is Longest Common subsequence Problem? Find LCS for following.

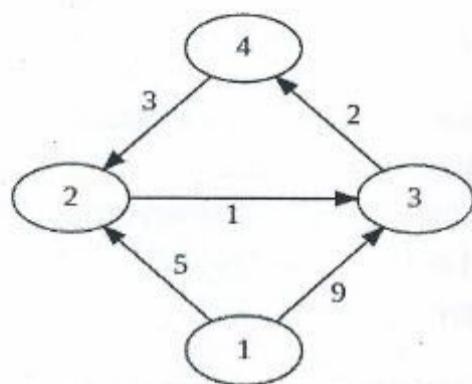
10M

String x = ACBAED

String y = ABCABE

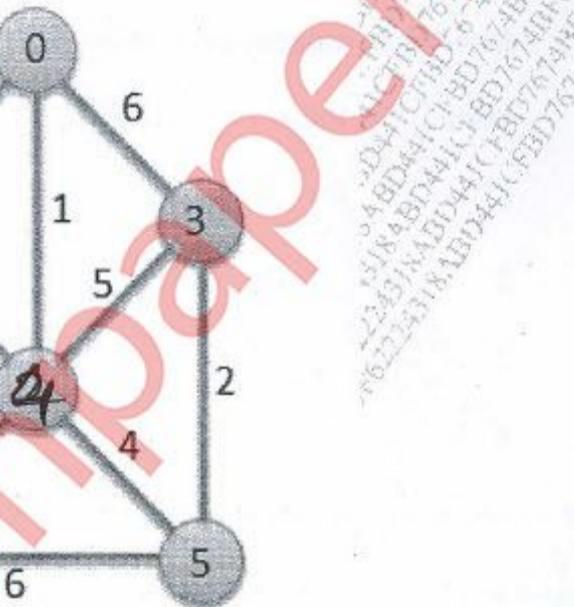
b) Explain binary search Tree? How to generate an optimal binary search tree. 10M

Q5. A) What is all pairs shortest path algorithm? Apply the same on following Graph. 10M



b) Find MST of Following Graph using Prims and Prism's Algorithm.

*(crucial)*



Q6. Write Short Notes on (Any Three)

20M

- Optimal Storage on Tapes
- 15 puzzle problem.
- Binary Search and its complexity.
- Problem of Multiplying Long Integers.

[Time: Three Hours]

[ Marks:80]

Please check whether you have got the right question paper.

N.B: Subject AOA CSC 402 CBSGS R-12 SE comp SEM IV CBSGS

1. Q.1 is compulsory.
2. Solve any three from Remaining

**Q. 1** Answer any four 20

- a) Write an algorithm for finding maximum and minimum number from given set.
- b) Write the algorithm and derived the complexity of Binary Search algorithm.
- c) Explain masters method with example
- d) Write a note on flow shop scheduling
- e) Compare divide and conquer, dynamic programming and Backtracking approache used for algorithm design.

**Q. 2** a) Write and explain string matching with finite automata with an example 10  
 b) Explain how branch and bound strategy can be used in 15 puzzle problem. 10

**Q. 3** a) What is 0/1 knapsack and fractional knapsack problem. 10  
 Solve following using 0/1 knapsack method

| Item (i) | Value (vi) | Weight(wi) |
|----------|------------|------------|
| 1        | 18         | 3          |
| 2        | 25         | 5          |
| 3        | 27         | 4          |
| 4        | 10         | 3          |
| 5        | 15         | 6          |

Knapsack capacity=12.

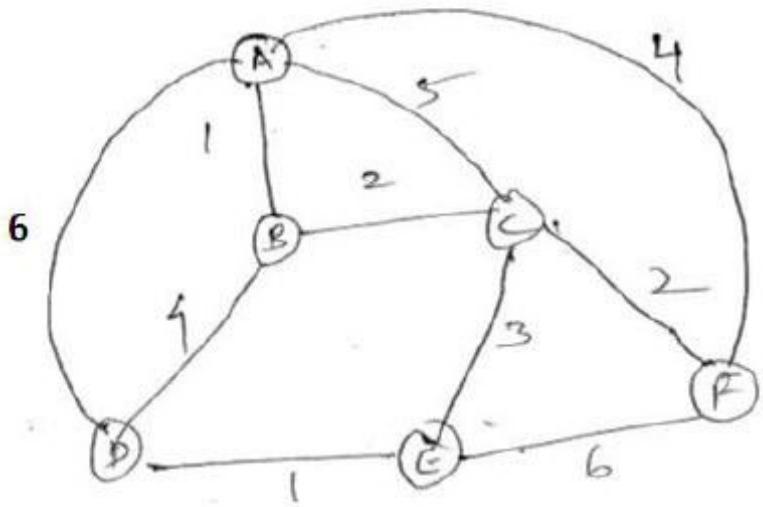
b) Explain insertion sort and derive its complexity 10

**Q. 4** a) What is a binary search tree? How to generate optimal binary search tree 10  
 b) What is a longest common subsequence problem? Find LCS for following string X = ACB AED  
 Y = ABC ABE 10

**Q. 5** a) Explain Job Sequencing with deadlines. 10  
 Let n=4,  $(P_1 P_2 P_3 P_4) = (100, 10, 15, 27)$  and  $(d_1 d_2 d_3 d_4) = (2, 1, 2, 1)$  find feasible solution.

- b) Explain prims algorithm and find minimum spanning tree for the following graph. 10

(P.T.O)



Q.6

Write short notes (any three):-

20

- a) Problem of multiplying Long Integers
- b) Strassen's matrix multiplication
- c) Knuth Morris Pratt's Pattern matching
- d) Multi stage Graphs

\*\*\*\*\*

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## Analysis of Algo.

(3 Hours)

QP Code : 541400

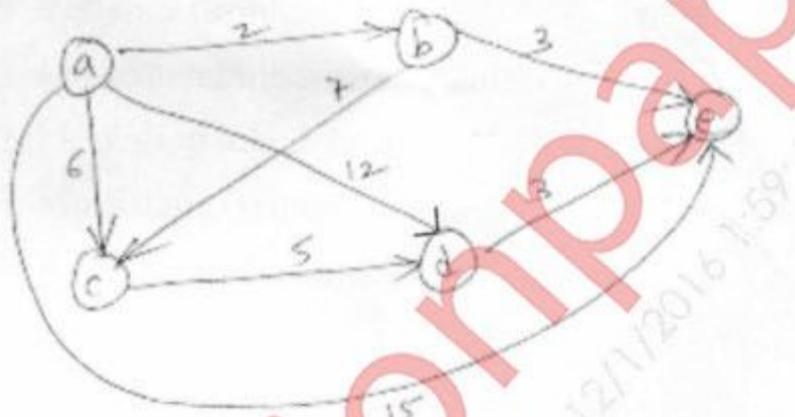
[ Total Marks: 80 ]



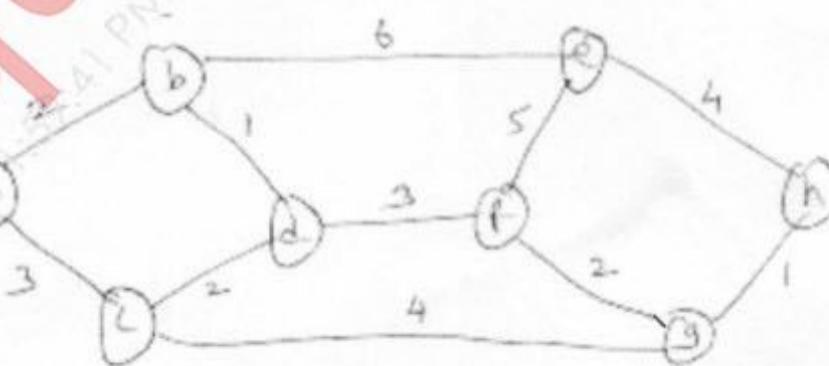
N.B.: (1) Q.1 is Compulsory.

(2) Attempt any three from remaining five questions.

1. (a) Which are the different methods of solving recurrences. Explain with examples. 10
- (b) Compare Greedy and dynamic programming approach for algorithm Design. Explain How both can be used to solve Knapsack problem? 10
2. (a) Explain the analysis of quick sort and apply the same to sort following data. [ 10 7 5 9 12 3 ] 10
- (b) Write single source shortest path algorithm & apply the same for following. 10



3. (a) Explain string matching with finite automata and apply the same technique to match following pattern. 10
- txt[] = UNIVERSITY OF MUMBAI  
pat[] = MBA
- (b) Compare Prims & Kruskal's method for finding Minimum spanning Tree find MST for following using prims method. 10



[ TURN OVER ]

4. (a) Explain with example how divide and conquer strategy is used in binary search? 10

(b) Solve sum of subsets problem for following

$$N = 6 \quad W = \{ 3, 5, 7, 8, 9, 15 \} \text{ & } M = 20$$

Also write the Algorithm for it.

5. (a) Explain longest common subsequence problem with example. 10

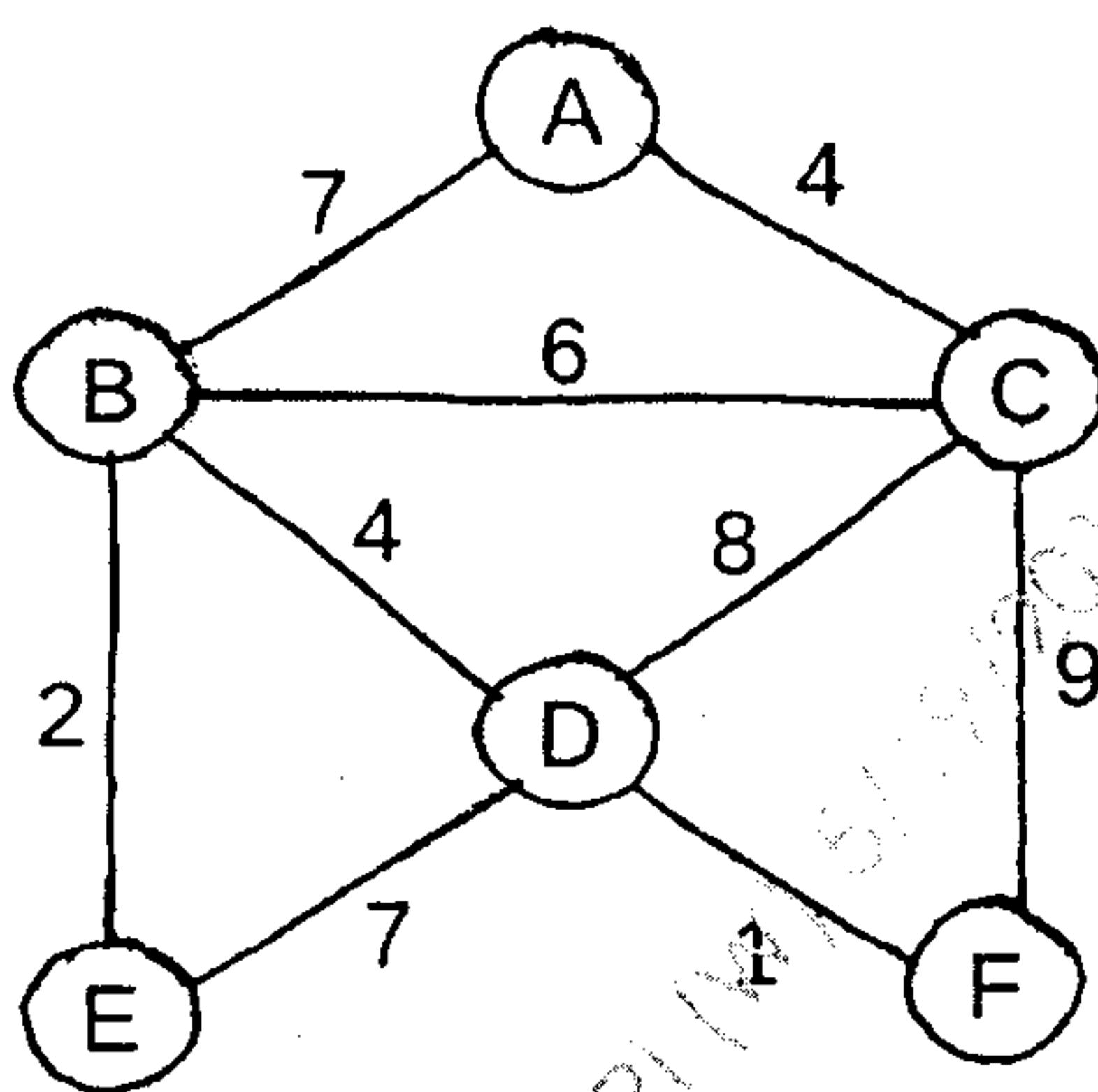
(b) What is backtracking method? How it is used in graph coloring problem? 10

6. Write short notes on **(Any Four)** 20

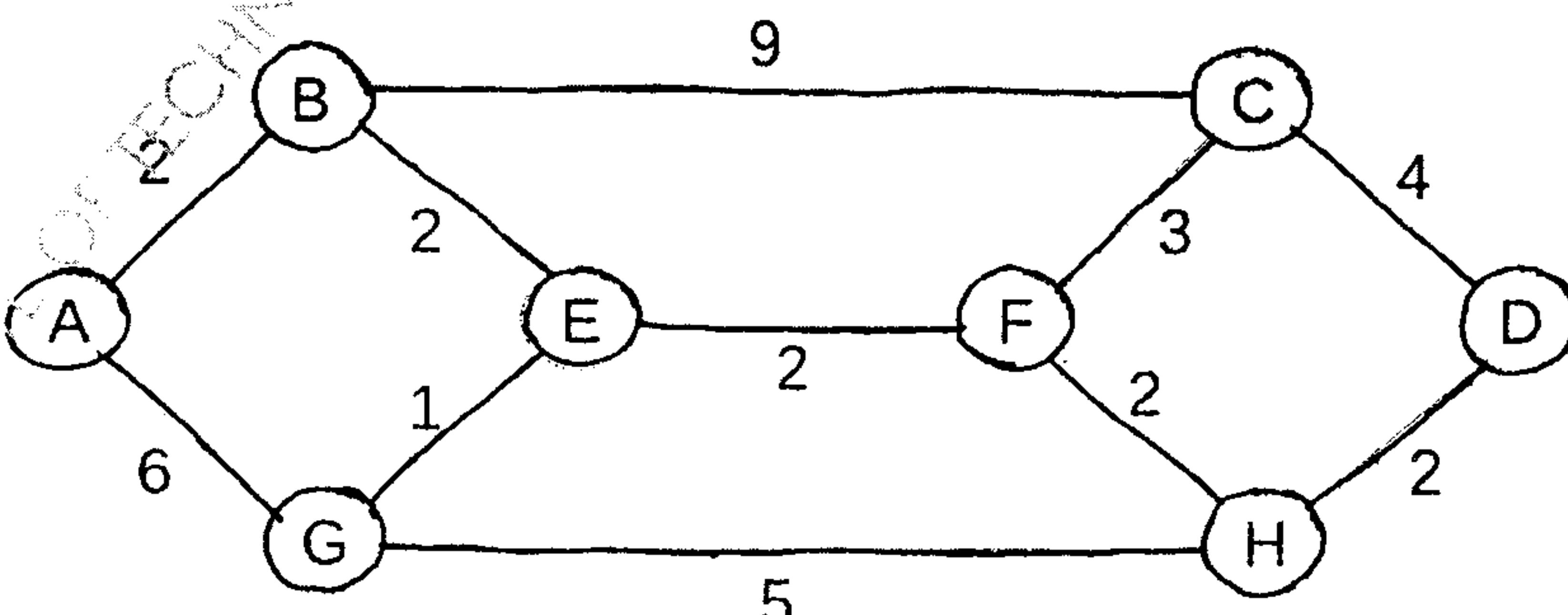
- (1) 8 queens problem
  - (2) Job sequencing with deadlines
  - (3) Flow shop scheduling
  - (4) Multistage Graphs
  - (5) A symptotic Notations
-

N.B.: (1) Question No. 1 is compulsory.  
(2) Attempt any three questions out of remaining five questions.

- Q1. a) Explain the asymptotic notations. [10]  
b) Write an algorithm to find minimum and maximum value using divide and conquer and also derive its complexity. [10]
- Q2. a) Explain the concept of multiplying long integers using divide and conquer. [10]  
b) Sort the following numbers using Quick Sort. Also derive the time complexity of Quick Sort. [10]  
50, 31, 71, 38, 77, 81, 12, 33
- Q3. a) Solve the following Job sequencing with deadlines problem [10]  
 $n=7$ , Profits( $p_1, p_2, \dots, p_7$ ) = {3, 5, 20, 18, 1, 6, 30}  
Deadlines( $d_1, d_2, \dots, d_7$ ) = {1, 3, 4, 3, 2, 1, 2}
- b) Explain different string matching algorithms. [10]
- Q4. a) Find the Minimum Spanning Tree of the following graph using Kruskal's algorithm [10]



- b) Explain flow shop scheduling with example. [10]
- Q5. a) Write an algorithm for sum of subsets. Solve the following problem. [10]  
 $M=30$        $W=\{5, 10, 12, 13, 15, 18\}$   
b) Find the shortest path from source vertex A using Dijkstra's algorithm [10]



- Q6. Write note on (any two): [20]  
a) Strassen's matrix multiplication.  
b) 8-Queen problem.  
c) Graph coloring  
d) 15-puzzle problem.

(Comp)

S.E SEM- IV CBAS

Analysis of Algorithm

30/11/15

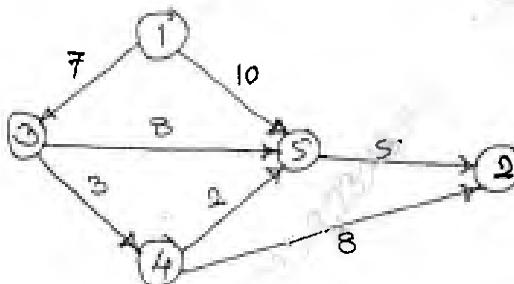
QP Code : 5359

(3 Hours)

[ Total Marks : 80 ]

- N.B. : (1) Attempt any four questions out of six.  
(2) Assume suitable data wherever required.

1. (a) Define  $O$ ,  $\Omega$ , and  $\Theta$  notations. To find the complexity of given recurrence relation. 10  
(i)  $T(n) = 4T(n/2) + n^2$   
(ii)  $T(n) = 2T(n/2) + n^3$   
(b) Implement the binary search, and derive its complexity. 10
2. (a) Explain 0/1 knapsack problem using dynamic programming  
(b) Explain optimal storage on tapes and find the optimal order for given instance. 10  
 $n = 3$ , and  $(l_1, l_2, l_3) = (5, 10, 3)$ . 10
3. (a) Let  $n = 4$ ,  $(p_1, p_2, p_3, p_4) = (100, 10, 15, 27)$  and  $(d_1, d_2, d_3, d_4) = (2, 1, 2, 1)$ . Find feasible solutions, using job sequencing with deadlines. 10  
(b) Find a minimum cost path from 3 to 2 in the given graph using dynamic programming. 10



4. (a) Explain 8 Queen problem.  
(b) Explain sum of subset problem, Find all possible subsets of weight that sum to  $m$ , let  $n = 6$ ,  $m = 30$ , and  $w[1:6] = \{5, 10, 12, 13, 15, 18\}$  10
5. (a) Write an algorithm for Kurnt-Morrie-Pratt (KMP).  
(b) Explain the strassen's Matrix multiplication. 10
6. Write note on (any two):-  
(i) Randomized Algorithms.  
(ii) Branch and bound strategy  
(iii) Huffman coding  
(iv) Rabin karp algorithm 20

(3 Hours)

[Total Marks : 80]

- N.B. (1) Question No. 1 is **compulsory**.  
 (2) Attempt any **three** from the remaining **five** question.  
 (3) Assume suitable data if **required**.

- |                                                                                                                                                                                                                                          |    |
|------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|----|
| 1. (a) Write abstract algorithm for greedy design method.                                                                                                                                                                                | 5  |
| (b) Which are different factors considered for sorting elements.                                                                                                                                                                         | 5  |
| (c) Explain flow shop scheduling technique.                                                                                                                                                                                              | 5  |
| (d) Explain three cases of master theorem.                                                                                                                                                                                               | 5  |
|                                                                                                                                                                                                                                          |    |
| 2. (a) Write and explain sum of subset algorithm for<br>$n = 5, W = \{2, 7, 8, 9, 15\} M = 17$                                                                                                                                           | 10 |
| (b) Explain randomized version of Quick sort and derive its complexity                                                                                                                                                                   | 10 |
|                                                                                                                                                                                                                                          |    |
| 3. (a) Implement the bubble sort Algorithm and derive its best case and worst case complexity.                                                                                                                                           | 10 |
| (b) Find the Huffman code for the following message<br>"COLLEGE OF ENGINEERING"                                                                                                                                                          | 10 |
|                                                                                                                                                                                                                                          |    |
| 4. (a) What is Hamiltonian cycle ? Write an algorithm to find all Hamiltonian cycles.                                                                                                                                                    | 10 |
| (b) Suppose you are given n number of coins, in that one coin is faulty, its weight is less than standard coin weight. To find the faulty coin in a list using proper searching method. What will be the complexity of searching method. | 10 |
|                                                                                                                                                                                                                                          |    |
| 5. (a) Explain Job sequencing with deadliner for the given instance.<br>$n = 5, \{P_1, P_2, P_3, P_4, P_5\} = \{20, 15, 10, 5, 3\}$<br>& $\{d_1, d_2, d_3, d_4, d_5\} = \{2, 2, 1, 3, 3\}$                                               | 10 |
| (b) Explain naive string matching algorithm with example.                                                                                                                                                                                | 10 |
|                                                                                                                                                                                                                                          |    |
| 6. Write note on : (any two)                                                                                                                                                                                                             | 20 |
| (a) Rabin karp algorithm                                                                                                                                                                                                                 |    |
| (b) 15-puzzle problem                                                                                                                                                                                                                    |    |
| (c) Travelling sales person problem                                                                                                                                                                                                      |    |
| (d) Strassen's matrix multiplication.                                                                                                                                                                                                    |    |

SE - COMP - CBCS  
 Sem IV - Analysis of Algorithm  
 DT - 23/5/14

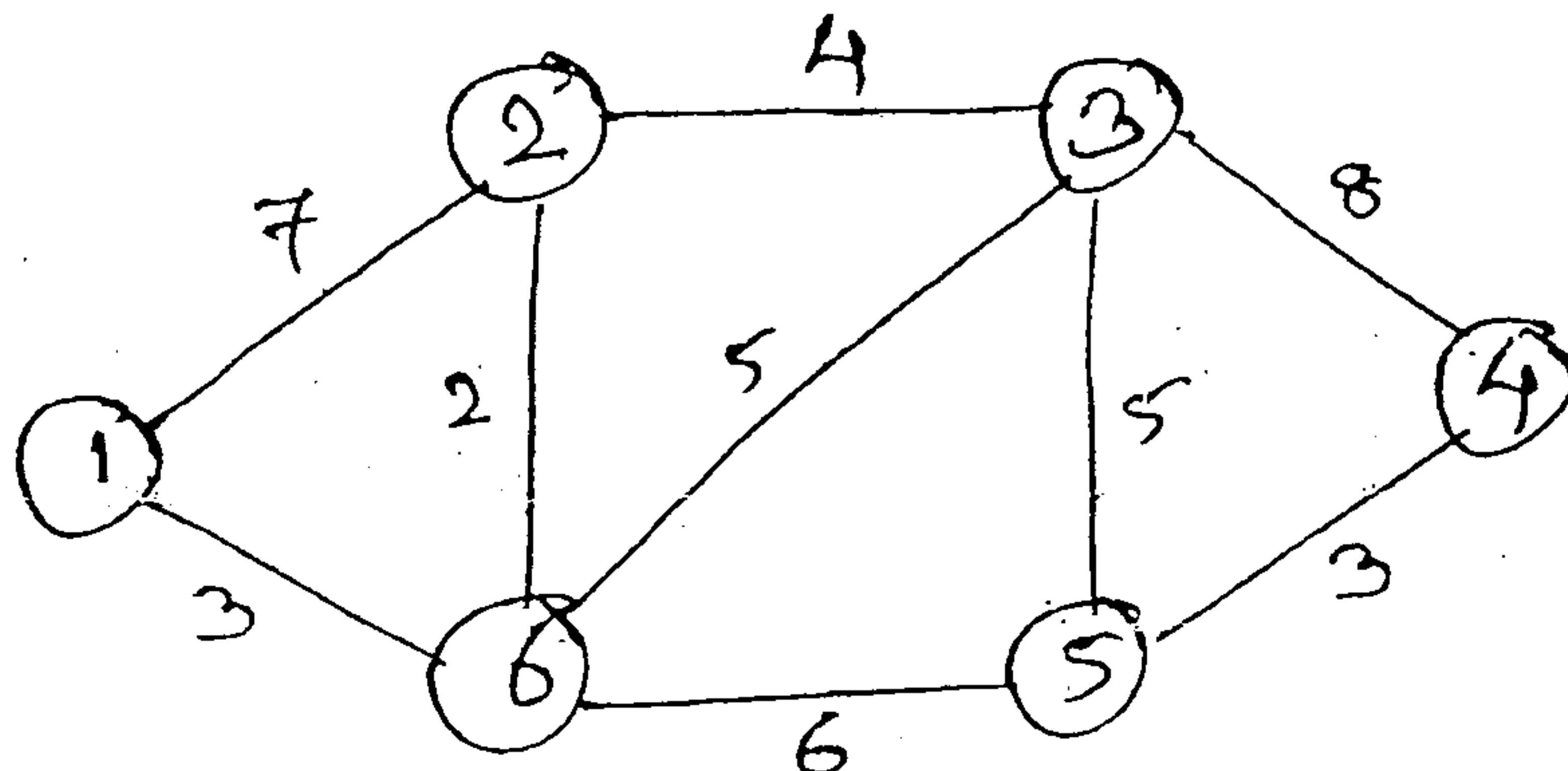
**QP Code :NP-19722**

(3 Hours)

[ Total Marks : 80 ]

- N.B. :** (1) Solve any **four** from six questions.  
 (2) Assume suitable data wherever required.

1. (a) Explain O,  $\Omega$  and  $\theta$  Notations with the help of Graph. And represent the following function using above notations. 10  
 (i)  $T(n) = 3n + 2$   
 (ii)  $T(n) = 10n^2 + 2n + 1$   
 (b) Explain 0/1 Knapsack Problem with example. 10
2. (a) Write an algorithm of sum of subsets. Solve following problem and draw portion of state space tree  $M = 35$ ,  $W = (5, 7, 10, 12, 15, 18, 20)$ . 10  
 (b) Explain longest common subsequence with example. 10
3. (a) Explain all pair shortest path algorithm with suitable example. 10  
 (b) Explain different string matching algorithms. 10
4. (a) Write a Min Max function to find minimum and maximum value from given set of values using divide and conquer. Also drive its complexities. 10  
 (b) Comment on any two modules of computation. 10
5. (a) To find Dijkstra's shortest path from vertex 1 to vertex 4 for following graph. 10



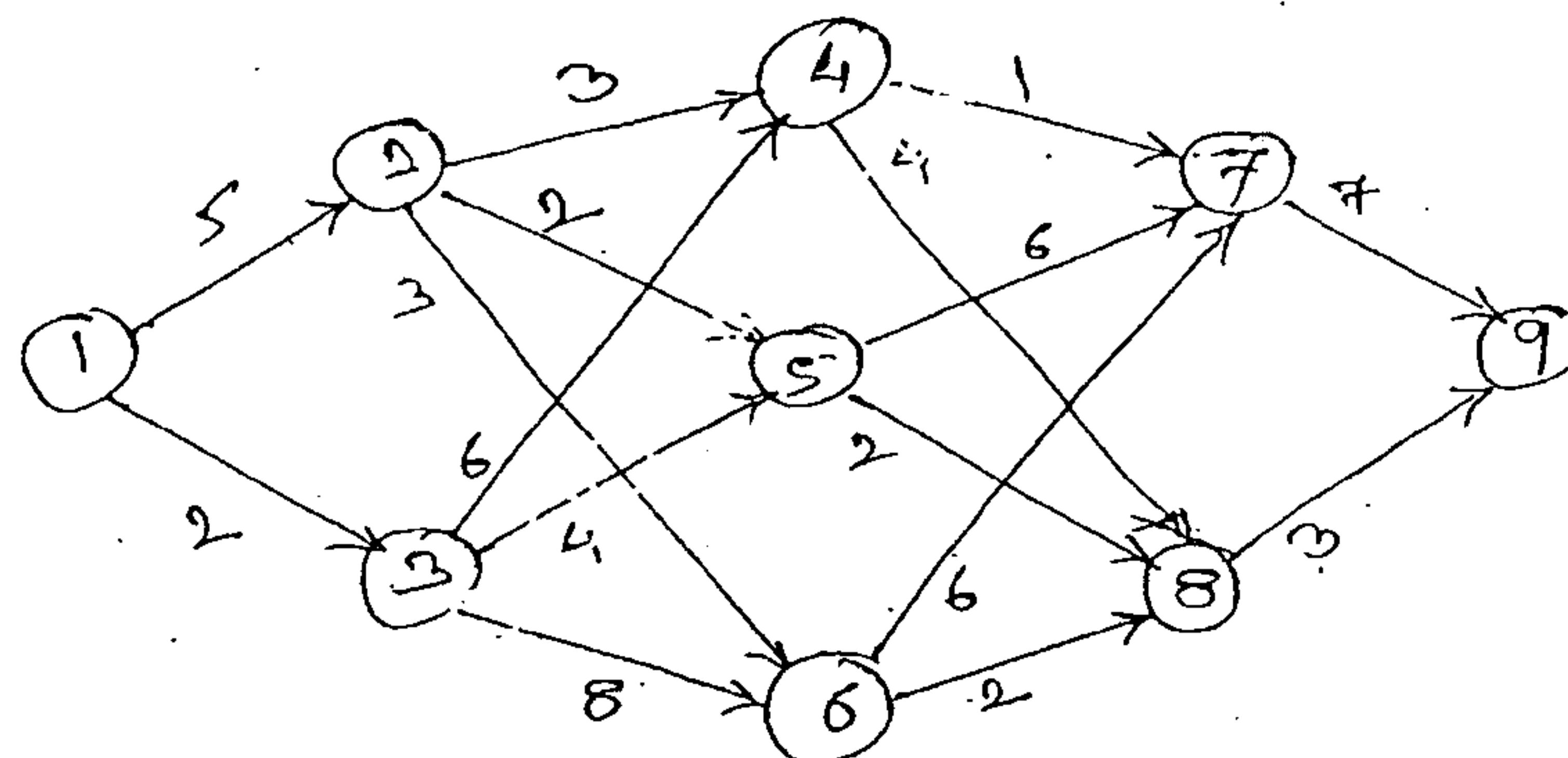
- (b) Explain flow shop scheduling with example. 10
6. Write note on :— (any two) 20
  - (a) Job sequencing with deadlines
  - (b) Randomized Algorithm
  - (c) The 15 Puzzle Problem
  - (d) N-Queen Problem.

(3 Hours)

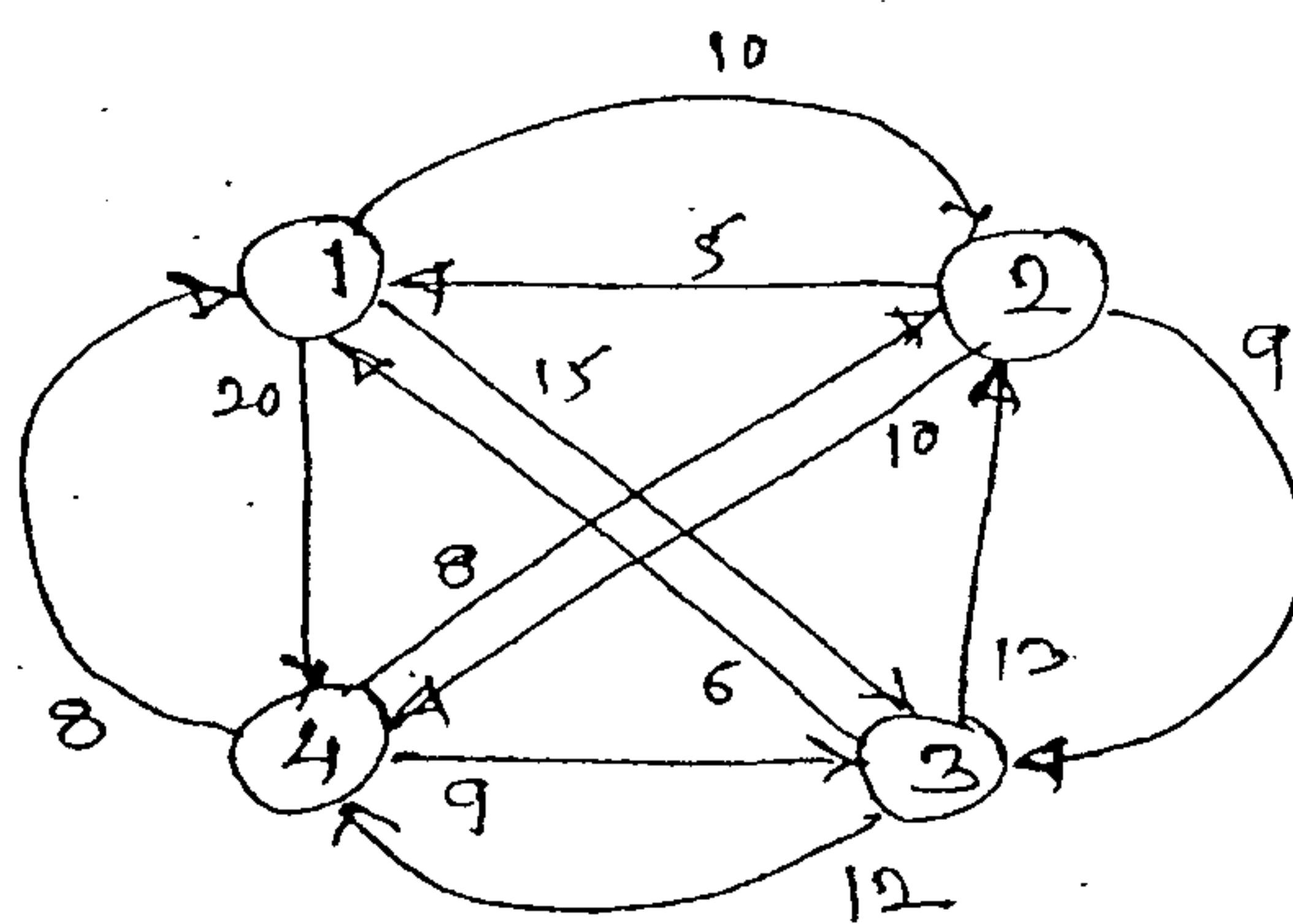
Total Marks : 80

- N. B. : (1) Attempt any four questions out of six question  
 (2) Assume suitable data if necessary.

1. (a) Write an algorithm to find minimum and maximum value using divide and conquer and also drive its complexity. 10  
 (b) To sort the given set of numbers using insertion sort and also show the result of each pass.  
 $<11, 7, 17, 3, 9, 29, 85, 9>$
2. (a) Find an optimal solution to the knapsack instance  $n = 7, m = 15$ ,  
 Profit = {10, 5, 15, 7, 6, 18, 3}  
 Weight = {2, 3, 5, 7, 1, 4, 1} 10  
 (b) Explain optimal storage on tape with example. 10
3. (a) Find a minimum cost path from 1 to 9 in the given graph using dynamic programming. 10

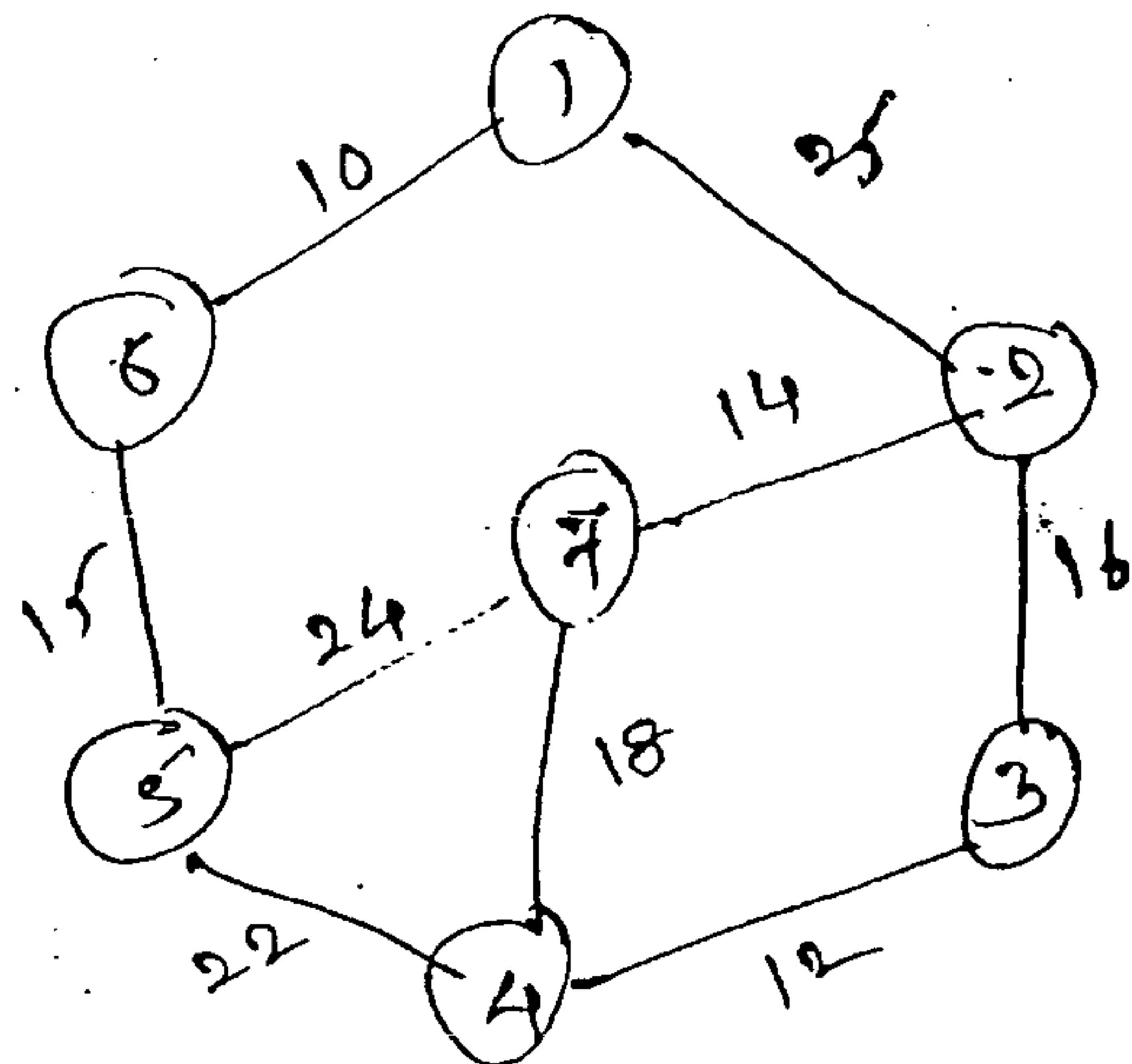


- (b) Find the path of travelling sales person problem of given graph. 10



[ TURN OVER ]

4. (a) To generate the Huffman code for given set of frequencies. 10  
1, 1, 2, 3, 4, 8, 13, 21  
(b) To implement the knuth - Morris-Pratt, string matching algorithm. 10
5. (a) To find MST of following graph using prim's and kruskal's Algorithm. 10



- (b) Explain flow shop scheduling using suitable data. 10
6. Write note on (Any two) 20
- (i) N-Queen Problem
  - (ii) Randomized Algorithm
  - (iii) Tries
  - (iv) The 15 - puzzle problem.
-

# Advanced Data Structures & Analysis of Algorithms

University of Mumbai

Examination 2020 under cluster 7 (Lead College: SCSJCE)

Program: Information Technology

Curriculum Scheme: Rev2016

Examination: TE Semester V

(10)

Course Code: ITDLO5011 and Course Name: Advanced Data Structures &amp; Analysis of Algorithms

Time: 2 hour

Max. Marks: 80

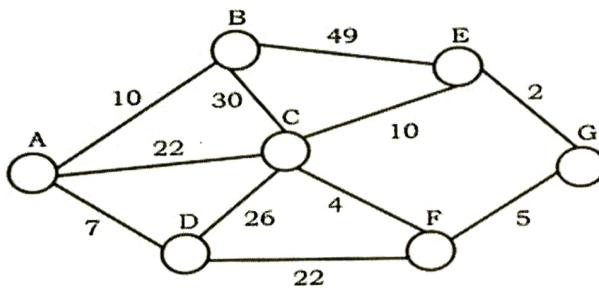
| Q1.  | Choose the correct option for following questions. All the Questions are compulsory and carry equal marks                                                                                                                                                                         |
|------|-----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| 1. 2 | Which one of the following is Substitution method<br>Option A: Forward<br>Option B: Linked list<br>Option C: Master's<br>Option D: Stack                                                                                                                                          |
| 2. 3 | Recursion is a method in which the solution of a problem depends on<br>Option A: Smaller instances of the same problem<br>Option B: Larger instances of the same problem<br>Option C: Larger instances of different problems<br>Option D: Smaller instances of different problems |
| 3. 4 | Which of the following is NOT recurrence method<br>Option A: Substitution Method<br>Option B: Master's Theorem<br>Option C: Array<br>Option D: Tree Method                                                                                                                        |
| 4. 5 | What is probabilistic analysis for hire assistant example?<br>Option A: $T(n)=O(n/2)$<br>Option B: $T(n)=O(n)$<br>Option C: $T(n)=O(\log n)$<br>Option D: $T(n)=O(1)$                                                                                                             |
| 5. 6 | A _____ is a special Tree-based data structure in which the tree is a complete binary tree.<br>Option A: Graph<br>Option B: Heap<br>Option C: List<br>Option D: Stack                                                                                                             |
| 6. 7 | Which is not an application of Topological Sorting<br>Option A: Ordered Statistics<br>Option B: Finding prerequisite of a task<br>Option C: Finding Deadlock in an Operating System<br>Option D: Finding Cycle in a graph                                                         |

|           |                                                                                                                                                                        |
|-----------|------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| 8.8       | In which of the following graph Topological Sort can be implemented?                                                                                                   |
| Option A: | Directed Acyclic Graphs                                                                                                                                                |
| Option B: | Undirected Cyclic Graphs                                                                                                                                               |
| Option C: | Directed Cyclic Graphs                                                                                                                                                 |
| Option D: | Undirected Acyclic Graphs                                                                                                                                              |
| 8.9       | In most of the cases, topological sort starts from a node which has                                                                                                    |
| Option A: | Maximum Degree                                                                                                                                                         |
| Option B: | Minimum Degree                                                                                                                                                         |
| Option C: | Any degree                                                                                                                                                             |
| Option D: | Zero Degree                                                                                                                                                            |
| 9.10      | Matrix A is of order 3*4 and Matrix B is of order 4*5. How many elements will be there in a matrix A*B multiplied recursively.                                         |
| Option A: | 12                                                                                                                                                                     |
| Option B: | 15                                                                                                                                                                     |
| Option C: | 16                                                                                                                                                                     |
| Option D: | 20                                                                                                                                                                     |
| 10.11     | What is the worst case time complexity of merge sort?                                                                                                                  |
| Option A: | $O(n \log n)$                                                                                                                                                          |
| Option B: | $O(n^2)$                                                                                                                                                               |
| Option C: | $O(n^2 \log n)$                                                                                                                                                        |
| Option D: | $O(n \log n^2)$                                                                                                                                                        |
| 11.12     | Given an array arr = {45, 77, 89, 90, 94, 99, 100} and key = 100; What are the mid values (corresponding array elements) generated in the first and second iterations? |
| Option A: | 90 and 99                                                                                                                                                              |
| Option B: | 90 and 100                                                                                                                                                             |
| Option C: | 89 and 94                                                                                                                                                              |
| Option D: | 94 and 99                                                                                                                                                              |
| 12.13     | Kruskal's algorithm is used to find                                                                                                                                    |
| Option A: | Single Source Shortest Path                                                                                                                                            |
| Option B: | Graph Traversal                                                                                                                                                        |
| Option C: | Minimum Spanning Tree                                                                                                                                                  |
| Option D: | All pair shortest Path                                                                                                                                                 |
| 13.14     | Which of the following is not greedy problem?                                                                                                                          |
| Option A: | Container loading                                                                                                                                                      |
| Option B: | Fractional Knapsack                                                                                                                                                    |
| Option C: | Flow Shop Scheduling                                                                                                                                                   |
| Option D: | Job Sequencing with deadlines                                                                                                                                          |
| 14.15     | What is the optimal storage on tapes value when n=3, (l1, l2, l3) = (5, 10, 3)?                                                                                        |
| Option A: | 29                                                                                                                                                                     |
| Option B: | 31                                                                                                                                                                     |
| Option C: | 34                                                                                                                                                                     |
| Option D: | 43                                                                                                                                                                     |

|           |                                                                                                                                                                                                    |
|-----------|----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| 15. 16    | Which is not correct solution method of Flow shop scheduling problem?                                                                                                                              |
| Option A: | Branch and Bound                                                                                                                                                                                   |
| Option B: | Dynamic Programming                                                                                                                                                                                |
| Option C: | Greedy algorithm                                                                                                                                                                                   |
| Option D: | Heuristic algorithm                                                                                                                                                                                |
| 16. 17    | Which of the following are the characteristics of dynamic programming approach?                                                                                                                    |
| Option A: | Overlapping sub problems                                                                                                                                                                           |
| Option B: | Greedy approach                                                                                                                                                                                    |
| Option C: | Optimal substructure                                                                                                                                                                               |
| Option D: | Both optimal substructure and overlapping sub problems                                                                                                                                             |
| 17. 18    | When a problem can be solved by combining optimal solutions to non-overlapping problems, the strategy is called                                                                                    |
| Option A: | Recursion                                                                                                                                                                                          |
| Option B: | Divide and Conquer                                                                                                                                                                                 |
| Option C: | Memorization                                                                                                                                                                                       |
| Option D: | Greedy                                                                                                                                                                                             |
| 18. 19    | What is the time complexity of the above dynamic programming implementation of the longest common subsequence problem where length of one string is "m" and the length of the other string is "n"? |
| Option A: | $O(n)$                                                                                                                                                                                             |
| Option B: | $O(m)$                                                                                                                                                                                             |
| Option C: | $O(m+n)$                                                                                                                                                                                           |
| Option D: | $O(mn)$                                                                                                                                                                                            |
| 19. 20    | What is the worst case running time of Rabin Karp Algorithm?                                                                                                                                       |
| Option A: | $\Theta(n)$                                                                                                                                                                                        |
| Option B: | $\Theta(n-m)$                                                                                                                                                                                      |
| Option C: | $\Theta((n-m+1)*m)$                                                                                                                                                                                |
| Option D: | $\Theta(n * \log m)$                                                                                                                                                                               |
| 20. 21    | Which of the following is a substring of "engineering"                                                                                                                                             |
| Option A: | engg                                                                                                                                                                                               |
| Option B: | gineer                                                                                                                                                                                             |
| Option C: | ning                                                                                                                                                                                               |
| Option D: | eiei                                                                                                                                                                                               |

| <b>Q2.</b><br><b>(20 Marks Each)</b> | <b>Solve any Two Questions out of Three</b>                                                                                                                                                                                                | <b>10 marks each</b> |
|--------------------------------------|--------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|----------------------|
| A                                    | Explain Probabilistic Analysis & Randomized Algorithm with the help of example.                                                                                                                                                            |                      |
| B                                    | Sort the following numbers using Heap Sort. [25, 67, 56, 32, 12, 96, 82, 44]. Show the contents of the array after every iteration. Also Derive time complexity for the same.                                                              |                      |
| C                                    | Explain Strassen's matrix multiplication rules. Solve the following example with the help of Strassen's matrix multiplication.<br>$A = \begin{bmatrix} 3 & 4 \\ 5 & 6 \end{bmatrix}$<br>$B = \begin{bmatrix} 1 & 2 \\ 3 & 4 \end{bmatrix}$ |                      |

| <b>Q3.</b><br><b>(20 Marks Each)</b> | <b>Solve any Two Questions out of Three</b>                                                                          | <b>10 marks each</b> |
|--------------------------------------|----------------------------------------------------------------------------------------------------------------------|----------------------|
| A                                    | Explain Minimum Spanning Tree. Find Minimum spanning tree of the following graph using prims and kruskals algorithm. |                      |
| B                                    | Explain 0/1 knapsack problem using dynamic programming approach.                                                     |                      |
| C                                    | Explain Rabin Karp Algorithm with a suitable example.                                                                |                      |



T.ECIT) ADSA . - V Sem .

# Advanced Data Structure and Analysis

(10)

## 0212\_IT\_Sem-V\_R19\_ADSA\_Inst. Name

1) The Question Paper will have MCQs (for 20 marks) and Subjective/Descriptive Questions (for 60 marks).

2) MCQ correct options and subjective question answers to be written on A4 size papers. Scan all pages of answer papers of Q.1 to Q.4 and create single file in pdf format to upload in the link given.

\* Required

1. Enter your Name \*

---

2. Enter your Seat Number \*

---

1) The Question Paper will have MCQs (for 20 marks) and Subjective/Descriptive Questions (for 60 marks).

2) MCQ correct options and subjective question answers to be written on A4 size papers. Scan all pages of answer papers of Q.1 to Q.4 and create single file in pdf format to upload in the link given.

0212\_IT\_Sem-  
V\_R19\_ADSA\_Inst.  
Name

Q.1) 1 to 5

|           |                                                                                                             |
|-----------|-------------------------------------------------------------------------------------------------------------|
| Q1.       | Choose the correct option for following questions. All the Questions are compulsory and carry equal marks   |
| 1.        | The asymptotic notation used to determine Average case running time of an algorithm is:                     |
| Option A: | Big Oh                                                                                                      |
| Option B: | Big Omega                                                                                                   |
| Option C: | Big Theta                                                                                                   |
| Option D: | Small Theta                                                                                                 |
| 2.        | Time Complexity for Merge Sort algorithm using Divide and Conquer is                                        |
| Option A: | $O(n)$                                                                                                      |
| Option B: | $\Theta(n \log n)$                                                                                          |
| Option C: | $O(\log n)$                                                                                                 |
| Option D: | $O(n^2)$                                                                                                    |
| 3.        | If a problem can be broken into subproblems which are reused several times, the problem possesses property. |
| Option A: | Overlapping subproblems                                                                                     |
| Option B: | Optimal substructure                                                                                        |
| Option C: | Memorization                                                                                                |
| Option D: | Greedy                                                                                                      |
| 4.        | Identify the data structure used for multilevel indexing :                                                  |
| Option A: | B Tree                                                                                                      |
| Option B: | B+ -tree                                                                                                    |
| Option C: | AVL Tree                                                                                                    |
| Option D: | Red-black Tree                                                                                              |
| 5.        | Identify the correct technique used for solving fractional Knapsack problem.                                |
| Option A: | Greedy Technique                                                                                            |
| Option B: | Divide and conquer                                                                                          |
| Option C: | Dynamic programming                                                                                         |
| Option D: | Cannot be solved                                                                                            |

Q.1) 6 to 8

|           |                                                                                                                                                    |
|-----------|----------------------------------------------------------------------------------------------------------------------------------------------------|
| 6.        | Which of the following statement is True for TSP.                                                                                                  |
| Option A: | In TSP, we know that Hamiltonian Tour exists                                                                                                       |
| Option B: | In TSP, many Hamiltonian tours exist                                                                                                               |
| Option C: | In TSP, we find a minimum weight Hamiltonian Cycle.                                                                                                |
| Option D: | In TSP, we find a maximum weight Hamiltonian Cycle.                                                                                                |
| 7.        | To merge two files containing m and n records respectively using Greedy Optimal Merge Pattern, the number of comparisons needed to merge them is : |
| Option A: | $m - n$                                                                                                                                            |
| Option B: | $m + n$                                                                                                                                            |
| Option C: | $m * n$                                                                                                                                            |
| Option D: | $m / n$                                                                                                                                            |
| 8.        | Best case number of comparisons to for a Naïve string matching algorithm is :                                                                      |
| Option A: | $O(m*(n-m+1))$                                                                                                                                     |
| Option B: | $O(m*n)$                                                                                                                                           |
| Option C: | $O(n)$                                                                                                                                             |
| Option D: | $O(1)$                                                                                                                                             |

Q.1) 9 to 10

| 9.        | Predict an optimal schedule using Job sequencing with deadlines that gives maximum profit.<br><table border="1" style="width: 100%; border-collapse: collapse;"> <thead> <tr> <th>Jobs</th><th>J1</th><th>J2</th><th>J3</th><th>J4</th><th>J5</th><th>J6</th></tr> </thead> <tbody> <tr> <td>Deadlines</td><td>4</td><td>2</td><td>3</td><td>3</td><td>3</td><td>3</td></tr> <tr> <td>Profits</td><td>60</td><td>50</td><td>26</td><td>42</td><td>20</td><td>84</td></tr> </tbody> </table> | Jobs | J1 | J2 | J3 | J4 | J5 | J6 | Deadlines | 4 | 2 | 3 | 3 | 3 | 3 | Profits | 60 | 50 | 26 | 42 | 20 | 84 |
|-----------|---------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|------|----|----|----|----|----|----|-----------|---|---|---|---|---|---|---------|----|----|----|----|----|----|
| Jobs      | J1                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          | J2   | J3 | J4 | J5 | J6 |    |    |           |   |   |   |   |   |   |         |    |    |    |    |    |    |
| Deadlines | 4                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           | 2    | 3  | 3  | 3  | 3  |    |    |           |   |   |   |   |   |   |         |    |    |    |    |    |    |
| Profits   | 60                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          | 50   | 26 | 42 | 20 | 84 |    |    |           |   |   |   |   |   |   |         |    |    |    |    |    |    |
| Option A: | 1—2—6—3.                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    |      |    |    |    |    |    |    |           |   |   |   |   |   |   |         |    |    |    |    |    |    |
| Option B: | 4—2—6—1.                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    |      |    |    |    |    |    |    |           |   |   |   |   |   |   |         |    |    |    |    |    |    |
| Option C: | 3—2—6—4.                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    |      |    |    |    |    |    |    |           |   |   |   |   |   |   |         |    |    |    |    |    |    |
| Option D: | 4—5—6—2.                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    |      |    |    |    |    |    |    |           |   |   |   |   |   |   |         |    |    |    |    |    |    |
| 10.       | State which of the following options is True:                                                                                                                                                                                                                                                                                                                                                                                                                                               |      |    |    |    |    |    |    |           |   |   |   |   |   |   |         |    |    |    |    |    |    |
| Option A: | P is set of problems that can not be solved by a deterministic Turing machine in Polynomial time.                                                                                                                                                                                                                                                                                                                                                                                           |      |    |    |    |    |    |    |           |   |   |   |   |   |   |         |    |    |    |    |    |    |
| Option B: | NP is set of decision problems that can be solved by a Non-deterministic Turing Machine in Polynomial time.                                                                                                                                                                                                                                                                                                                                                                                 |      |    |    |    |    |    |    |           |   |   |   |   |   |   |         |    |    |    |    |    |    |
| Option C: | NP is subset of P                                                                                                                                                                                                                                                                                                                                                                                                                                                                           |      |    |    |    |    |    |    |           |   |   |   |   |   |   |         |    |    |    |    |    |    |
| Option D: | P, NP, NP-Hard and NP-Complete are not related                                                                                                                                                                                                                                                                                                                                                                                                                                              |      |    |    |    |    |    |    |           |   |   |   |   |   |   |         |    |    |    |    |    |    |

Q.2

|    |                                                                                                           |              |
|----|-----------------------------------------------------------------------------------------------------------|--------------|
| Q2 | Solve any Four out of Six                                                                                 | 5 marks each |
| A  | Define the Asymptotic notations with suitable diagrams.                                                   |              |
| B  | Explain different methods used for solving recurrences.                                                   |              |
| C  | Analyze Time complexity of Binary Search using Divide and Conquer. Also write the algorithm for the same. |              |
| D  | Describe Genetic algorithms and its importance.                                                           |              |
| E  | Explain approximate algorithms with a suitable example.                                                   |              |
| F  | Describe NP-Hard and NP-Complete                                                                          |              |

Q.3

| Q3 Solve any Two Questions out of Three                                                                        |                                                                                                                                                                                                                                                                                                                                                                                         | 10 marks each |                        |    |   |   |   |                         |    |     |    |    |                        |   |    |    |    |
|----------------------------------------------------------------------------------------------------------------|-----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|---------------|------------------------|----|---|---|---|-------------------------|----|-----|----|----|------------------------|---|----|----|----|
| Apply All Pair Shortest Path algorithm to solve following problem.                                             |                                                                                                                                                                                                                                                                                                                                                                                         |               |                        |    |   |   |   |                         |    |     |    |    |                        |   |    |    |    |
| A                                                                                                              |                                                                                                                                                                                                                                                                                                                                                                                         |               |                        |    |   |   |   |                         |    |     |    |    |                        |   |    |    |    |
| Illustrate the process of finding LCS to find the Longest Common Subsequence for the following set of strings: |                                                                                                                                                                                                                                                                                                                                                                                         |               |                        |    |   |   |   |                         |    |     |    |    |                        |   |    |    |    |
| B                                                                                                              | ABCDGH<br>AEDFHR                                                                                                                                                                                                                                                                                                                                                                        |               |                        |    |   |   |   |                         |    |     |    |    |                        |   |    |    |    |
| C                                                                                                              | Solve the following Knapsack problem using Greedy method. W = 45 <table border="1"> <thead> <tr> <th>Item (O<sub>i</sub>)</th><th>A</th><th>B</th><th>C</th><th>D</th></tr> </thead> <tbody> <tr> <td>Value (P<sub>i</sub>)</td><td>50</td><td>140</td><td>60</td><td>60</td></tr> <tr> <td>Size (W<sub>i</sub>)</td><td>5</td><td>20</td><td>10</td><td>12</td></tr> </tbody> </table> |               | Item (O <sub>i</sub> ) | A  | B | C | D | Value (P <sub>i</sub> ) | 50 | 140 | 60 | 60 | Size (W <sub>i</sub> ) | 5 | 20 | 10 | 12 |
| Item (O <sub>i</sub> )                                                                                         | A                                                                                                                                                                                                                                                                                                                                                                                       | B             | C                      | D  |   |   |   |                         |    |     |    |    |                        |   |    |    |    |
| Value (P <sub>i</sub> )                                                                                        | 50                                                                                                                                                                                                                                                                                                                                                                                      | 140           | 60                     | 60 |   |   |   |                         |    |     |    |    |                        |   |    |    |    |
| Size (W <sub>i</sub> )                                                                                         | 5                                                                                                                                                                                                                                                                                                                                                                                       | 20            | 10                     | 12 |   |   |   |                         |    |     |    |    |                        |   |    |    |    |

Q.4

|                                         |                                                                                                                                                                   |               |
|-----------------------------------------|-------------------------------------------------------------------------------------------------------------------------------------------------------------------|---------------|
| Q4 Solve any Two Questions out of Three |                                                                                                                                                                   | 10 marks each |
| A                                       | Explain B Tree and Illustrate the insertion operation in a B tree of degree 3 by inserting following data values. 16, 70, 30, 10, 18, 22, 24, 5, 75, 9, 7, 2, 12. |               |
| B                                       | Explain Matrix Chain Multiplication problem.                                                                                                                      |               |
| C                                       | Demonstrate the use of adjacency matrix method to find the topological sorting order for following graph.                                                         |               |

3. Upload your answer papers \*

Files submitted:

4. Have you uploaded required pdf file of answers? \*

*Mark only one oval.*

Yes

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Google Forms

Time: 2 hour

| Q1.  | Choose the correct option for following questions. All the Questions are compulsory and carry equal marks                                                                                                                                                                                                                                                                                                                 |
|------|---------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| 3 1. | Which of the following is not $O(n^2)$ ?<br>Option A: $(5^{10}) * n + 990$<br>Option B: $N^{1.45}$<br>Option C: $n^3 / (\sqrt{n})$<br>Option D: $(3^{50}) * n$                                                                                                                                                                                                                                                            |
| 4 2. | If A is asymptotically less efficient than B, it means?<br>Option A: B will be a better choice for all inputs<br>Option B: B will be a better choice for all inputs except possibly small inputs<br>Option C: B will be a better choice for all inputs except possibly large inputs<br>Option D: B will be a better choice for small inputs                                                                               |
| 5 3. | In Quicksort algorithm, there is a procedure for finding a pivot element that splits the array into two sub-arrays, each of which contains at least Two-fifth of the elements. Let $T(n)$ be the number of comparisons required to sort $n$ elements. Then<br>Option A: $T(n) \leq 2T(n/5) + n$<br>Option B: $T(n) \leq T(2n/5) + T(3n/5) + n$<br>Option C: $T(n) \leq 2T(4n/5) + n$<br>Option D: $T(n) \leq 2T(n/2) + n$ |
| 6 4. | What is the result of following recurrences $T(n) = aT(n/b) + n^c$ ?<br>Option A: $T(n) = O(n^{\log_b a})$<br>Option B: $T(n) = O(n^c \log n)$<br>Option C: $T(n) = O(f(n))$<br>Option D: $T(n) = O(n^2)$                                                                                                                                                                                                                 |
| 7 5. | The class of decision problems that can be solved by non-deterministic polynomial algorithms are called as.<br>Option A: NP<br>Option B: P<br>Option C: Hard<br>Option D: Complete                                                                                                                                                                                                                                        |
| 8 6. | If you are sorting in ascending order with insertion sort, average case running time it will take is?<br>Option A: $O(N)$                                                                                                                                                                                                                                                                                                 |

|           |                                                                                                                                                                                 |
|-----------|---------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| Option B: | $O(N \log N)$                                                                                                                                                                   |
| Option C: | $O(\log N)$                                                                                                                                                                     |
| Option D: | $O(N^2)$                                                                                                                                                                        |
| 9.        | Worst case time complexity of merge sort is                                                                                                                                     |
| Option A: | $O(n \log n)$                                                                                                                                                                   |
| Option B: | $O(n^2)$                                                                                                                                                                        |
| Option C: | $O(n^2 \log n)$                                                                                                                                                                 |
| Option D: | $O(n \log n^2)$                                                                                                                                                                 |
| 10.       | Apply Quick sort on a given sequence 6 10 13 5 8 3 2 11. What is the sequence after first phase, pivot is first element?                                                        |
| Option A: | 5 3 2 6 10 8 13 11                                                                                                                                                              |
| Option B: | 5 2 3 6 8 13 10 11                                                                                                                                                              |
| Option C: | 6 5 13 10 8 3 2 11                                                                                                                                                              |
| Option D: | 6 5 3 2 8 13 10 11                                                                                                                                                              |
| 11.       | Consider the graph M with 3 vertices. Its adjacency matrix is shown below. Which of the following is true?<br>$\begin{matrix} 0 & 2 & 2 \\ 2 & 0 & 2 \\ 2 & 2 & 0 \end{matrix}$ |
| Option A: | Graph M has no minimum spanning tree                                                                                                                                            |
| Option B: | Graph M has a unique minimum spanning trees of cost 4                                                                                                                           |
| Option C: | Graph M has 3 distinct minimum spanning trees, each of cost 4                                                                                                                   |
| Option D: | Graph M has 3 spanning trees of different costs                                                                                                                                 |
| 12.       | Given items as {value, weight} pairs {{60,10}, {20,10}, {40,5}}. The capacity of knapsack=20. Find the maximum value output assuming items to be divisible.                     |
| Option A: | 110                                                                                                                                                                             |
| Option B: | 80                                                                                                                                                                              |
| Option C: | 100                                                                                                                                                                             |
| Option D: | 40                                                                                                                                                                              |
| 13.       | A graph with negative weight cycle is having _____ no. of shortest paths                                                                                                        |
| Option A: | One                                                                                                                                                                             |
| Option B: | Two                                                                                                                                                                             |
| Option C: | Zero                                                                                                                                                                            |
| Option D: | Infinite                                                                                                                                                                        |
| 14.       | Floyd Warshall Algorithm falls into _____                                                                                                                                       |
| Option A: | Greedy technique                                                                                                                                                                |
| Option B: | Dynamic Programming                                                                                                                                                             |
| Option C: | Linear Programming                                                                                                                                                              |
| Option D: | Backtracking                                                                                                                                                                    |
| 15.       | In assembly line scheduling problem, _____ lookup tables are required.                                                                                                          |
| Option A: | 0                                                                                                                                                                               |
| Option B: | 1                                                                                                                                                                               |
| Option C: | 2                                                                                                                                                                               |
| Option D: | 3                                                                                                                                                                               |

|            |                                                                                                                                                                                                                                                 |
|------------|-------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
|            |                                                                                                                                                                                                                                                 |
| 14.<br>16. | A travelling salesman problem with 55 cities has _____ no. of feasible tours.<br><i>Correct no. of edges in any feasible tour</i>                                                                                                               |
| Option A:  | 37 arcs                                                                                                                                                                                                                                         |
| Option B:  | 54 arcs                                                                                                                                                                                                                                         |
| Option C:  | 55 arcs                                                                                                                                                                                                                                         |
| Option D:  | 990 arcs                                                                                                                                                                                                                                        |
| 17.<br>15. | is not a branch and bound strategy to generate branches                                                                                                                                                                                         |
| Option A:  | LIFO branch and bound                                                                                                                                                                                                                           |
| Option B:  | FIFO branch and bound                                                                                                                                                                                                                           |
| Option C:  | Lowest cost branch and bound                                                                                                                                                                                                                    |
| Option D:  | Highest cost branch and bound                                                                                                                                                                                                                   |
| 18.<br>16. | Of the following given options, which one of the following is a correct option that provides an optimal solution for 4-queens problem?                                                                                                          |
| Option A:  | (3,1,4,2)                                                                                                                                                                                                                                       |
| Option B:  | (2,3,1,4)                                                                                                                                                                                                                                       |
| Option C:  | (4,3,2,1)                                                                                                                                                                                                                                       |
| Option D:  | (4,2,3,1)                                                                                                                                                                                                                                       |
| 19.<br>17. | Chromatic number of a graph is _____ no of colors required to color the vertices in graph.                                                                                                                                                      |
| Option A:  | Maximum                                                                                                                                                                                                                                         |
| Option B:  | Same                                                                                                                                                                                                                                            |
| Option C:  | Minimum                                                                                                                                                                                                                                         |
| Option D:  | More than Number of vertices                                                                                                                                                                                                                    |
| 20.<br>18. | In Rabin and Karp Algorithm, preprocessing can be done in                                                                                                                                                                                       |
| Option A:  | $\theta(m^2)$                                                                                                                                                                                                                                   |
| Option B:  | $\theta(m \log n)$                                                                                                                                                                                                                              |
| Option C:  | $\theta(m)$                                                                                                                                                                                                                                     |
| Option D:  | $O(n)$                                                                                                                                                                                                                                          |
| 21.<br>19. | What happens when the modulo value(q) is taken large?                                                                                                                                                                                           |
| Option A:  | Complexity increases                                                                                                                                                                                                                            |
| Option B:  | Spurious hits occur frequently                                                                                                                                                                                                                  |
| Option C:  | Cost of extra checking is low                                                                                                                                                                                                                   |
| Option D:  | Matching time increases                                                                                                                                                                                                                         |
| 22.<br>20. | Given a pattern of length- 5 window, find the spurious hit in the given text string.<br><br>Pattern: 7 3 9 9 2<br>Modulus: 13<br>Index: 0 1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17 18 19 20<br>Text: 2 3 5 9 0 2 3 1 4 1 5 2 6 7 3 9 9 2 1 3 9 |

|           |                |
|-----------|----------------|
|           |                |
| Option A: | 6-10           |
| Option B: | 12-16<br>10-14 |
| Option C: | 3-7            |
| Option D: | 13-17          |

| <b>Q2</b> | <b>Solve any Four out of Six</b>                           | <b>5 marks each</b> |
|-----------|------------------------------------------------------------|---------------------|
| A         | Explain Master theorem with example                        |                     |
| B         | Define P, NP, NP-Hard and NP-Complete Complexity Classes.  |                     |
| C         | Discuss Complexity of Quicksort Algorithm in all cases.    |                     |
| D         | Rewrite Binary Search Algorithm and Explain its complexity |                     |
| E         | Find LCS for strings X= "ABSDG" and Y= "GBSTR"             |                     |
| F         | Write short note on Rabin Karp Algorithm                   |                     |

| <b>Q3.</b> | <b>Solve any Two Questions out of Three</b>                                                                                                                                                                                                  | <b>10 marks each</b>                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   |
|------------|----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| A          | Apply Dijkstra algorithm on following graph. Show all intermediate steps.                                                                                                                                                                    |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        |
|            | <pre> graph LR     1((1)) -- 9 --&gt; 2((2))     1 -- 4 --&gt; 3((3))     2 -- 12 --&gt; 4((4))     2 -- 4 --&gt; 3     3 -- 5 --&gt; 4     3 -- 13 --&gt; 5((5))     4 -- 2 --&gt; 6((6))     5 -- 3 --&gt; 4     5 -- 15 --&gt; 6   </pre> |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        |
| B          | Explain 15 Puzzle problem with Branch and Bound method                                                                                                                                                                                       |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        |
| C          | Find a minimum cost path from A to L in the following multistage graph                                                                                                                                                                       | <p>V1                  V2                  V3                  V4                  V5</p> <pre> graph LR     subgraph V1     A1((A)) --- B1((B))     end     subgraph V2     C2((C)) --- D2((D))     C2 --- E2((E))     end     subgraph V3     F3((F)) --- G3((G))     F3 --- H3((H))     end     subgraph V4     I4((I)) --- J4((J))     I4 --- K4((K))     end     subgraph V5     L5((L))     end     A1 -- 7 --&gt; B1     A1 -- 6 --&gt; C2     A1 -- 5 --&gt; D2     A1 -- 9 --&gt; E2     B1 -- 8 --&gt; C2     B1 -- 10 --&gt; F3     C2 -- 3 --&gt; G3     C2 -- 11 --&gt; H3     D2 -- 5 --&gt; G3     D2 -- 6 --&gt; H3     E2 -- 12 --&gt; G3     E2 -- 10 --&gt; H3     F3 -- 12 --&gt; I4     F3 -- 7 --&gt; J4     F3 -- 5 --&gt; K4     G3 -- 9 --&gt; I4     G3 -- 5 --&gt; J4     G3 -- 8 --&gt; K4     H3 -- 7 --&gt; I4     H3 -- 10 --&gt; J4     H3 -- 11 --&gt; K4     I4 -- 7 --&gt; L5     J4 -- 8 --&gt; L5     K4 -- 11 --&gt; L5   </pre> |

Time: 2 hour 30 minutes

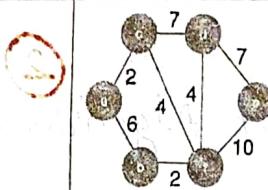
(2)

(1)

Analysis of Algorithm

Max. Marks: 80

| Q1.<br>(20 Marks) | <b>Choose the correct option for following questions. All the Questions are compulsory and carry equal marks</b>                                                                                                                                                                                            |
|-------------------|-------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| 1.                | <p>_____ is the class of decision problems that can be solved by non-deterministic polynomial algorithms.</p> <p>Option A: NP<br/>Option B: P<br/>Option C: Hard<br/>Option D: Complete</p>                                                                                                                 |
| 2.                | <p>Following data structure is used to implement LIFO Branch and Bound Strategy</p> <p>Option A: Priority Queue<br/>Option B: array<br/>Option C: stack<br/>Option D: Linked list</p>                                                                                                                       |
| 3.                | <p>For the given elements 6 4 11 17 2 24 14 using quick sort, what is the sequence after first phase, assuming the pivot as the first element?</p> <p>Option A: 2 4 6 17 11 24 14<br/>Option B: 2 4 6 11 17 14 24<br/>Option C: 4 2 6 17 11 24 14<br/>Option D: 2 4 6 11 17 24 14</p>                       |
| 4.                | <p>Which of the following is correct for branch and bound technique?</p> <p>i. It is BFS generation of problem states<br/>ii. It is DFS generation of problem states<br/>iii. It is D-search.</p> <p>Option A: Only i<br/>Option B: Only ii<br/>Option C: Only ii and iii<br/>Option D: Only i, and iii</p> |
| 5.                | Consider the given graph.                                                                                                                                                                                                                                                                                   |

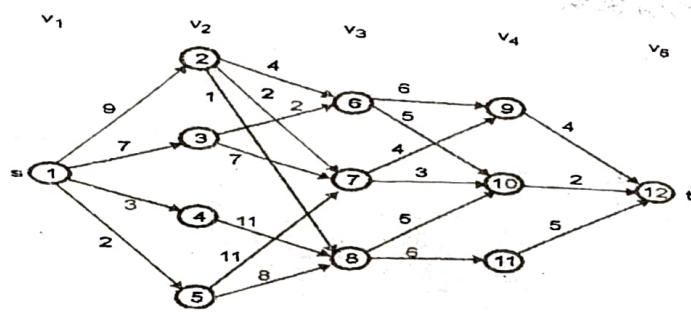
|           |                                                                                                                                                                                                                                                                                  |
|-----------|----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
|           |                                                                                                                                                                                                 |
|           | What is the weight of the minimum spanning tree using the Kruskal's algorithm?                                                                                                                                                                                                   |
| Option A: | 24                                                                                                                                                                                                                                                                               |
| Option B: | 23                                                                                                                                                                                                                                                                               |
| Option C: | 15                                                                                                                                                                                                                                                                               |
| Option D: | 19                                                                                                                                                                                                                                                                               |
| 6.        | Bellman Ford algorithm is used to find out single source shortest path for negative edge weights. Bellman Ford algorithm uses which of the following strategy?                                                                                                                   |
| Option A: | Greedy method                                                                                                                                                                                                                                                                    |
| Option B: | Dynamic Programming                                                                                                                                                                                                                                                              |
| Option C: | Backtracking                                                                                                                                                                                                                                                                     |
| Option D: | Divide and Conquer                                                                                                                                                                                                                                                               |
| 7.        | The optimal solution for 4-queen problem is                                                                                                                                                                                                                                      |
| Option A: | (2,3,1,4)                                                                                                                                                                                                                                                                        |
| Option B: | (1,3,2,4)                                                                                                                                                                                                                                                                        |
| Option C: | (3,1,2,4)                                                                                                                                                                                                                                                                        |
| Option D: | (2,4,1,3)                                                                                                                                                                                                                                                                        |
| 8.        | Consider the following code snippet:<br><pre>Bounding function(k,i) {     for(j=1 to k-1)         { if ((x[j]==i) or (Abs(x[j]-i) ==abs(j-k))) return false;         } return true }</pre> The above code represents the bounding function for which of the following algorithm? |
| Option A: | Subset sum problem using backtracking                                                                                                                                                                                                                                            |
| Option B: | n-queens using backtracking                                                                                                                                                                                                                                                      |
| Option C: | Graph coloring using backtracking                                                                                                                                                                                                                                                |
| Option D: | Subset sum using branch and bound                                                                                                                                                                                                                                                |
| 9.        | What do you mean by chromatic number?                                                                                                                                                                                                                                            |
| Option A: | The minimum number of colors needed to color all the vertices optimally in a Graph                                                                                                                                                                                               |

|           |                                                                                                        |
|-----------|--------------------------------------------------------------------------------------------------------|
|           | Coloring problem                                                                                       |
| Option B: | The maximum number of colors needed to color all the vertices optimally in a Graph<br>Coloring problem |
| Option C: | The number of colors using which the edges of graph have been colored in a Graph<br>Coloring Problem   |
| Option D: | The individual colors with which we color the vertices of a Graph in a Graph Coloring<br>Problem       |
| 10.       | Which string matching algorithm uses a Prefix Table?                                                   |
| Option A: | Naïve String Matching Algorithm                                                                        |
| Option B: | Boyer Moore String Matching Algorithm                                                                  |
| Option C: | Knuth Morris Pratt Algorithm                                                                           |
| Option D: | Rabin Karp Algorithm                                                                                   |

| <b>Q2.<br/>(20 Marks)</b> | <b>Solve any Four out of Six</b>                                                                        | <b>05 marks each</b> |
|---------------------------|---------------------------------------------------------------------------------------------------------|----------------------|
| A                         | Write and Explain binary search algorithm.                                                              |                      |
| B                         | Write a short note on job sequencing with deadline                                                      |                      |
| C                         | Determine the LCS of the following sequences:<br><br>X: {A, B, C, B, D, A, B}<br>Y: {B, D, C, A, B, A}  |                      |
| D                         | Solve the sum of subsets problem for the following: n=4, m=15, w={3,5,6,7}                              |                      |
| E                         | Give the algorithm for the N-Queen's problem and give any two solutions to the 8-Queen's problem        |                      |
| F                         | Explain and apply Naïve string matching on following strings<br><br>String1: COMPANION<br>String2: PANI |                      |

| <b>Q3.<br/>(20 Marks)</b> | <b>Solve any Two Questions out of Three</b>                                                                                                                                        | <b>10 marks each</b> |
|---------------------------|------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|----------------------|
| A                         | Write algorithm for greedy knapsack and Obtain the solution to following knapsack problem where n=7,m=15 (p1,p2.....p7) = (10,5,15,7,6,18,3), (w1,w2,.....,w7) = (2,3, 5,7,1,4,1). |                      |
| B                         | Explain Dijkstra's Single source shortest path algorithm. Explain how it is different from Bellman Ford algorithm. Explain 15-puzzle problem using LC search technique.            |                      |
| C                         | Rewrite and Compare Rabin Karp and Knuth Morris Pratt Algorithms<br>Give the pseudo code for the KMP String Matching Algorithm.                                                    |                      |

| <b>Q4.<br/>(20 Marks)</b> | <b>Solve any Two Questions out of Three</b>                                         | <b>10 marks each</b> |
|---------------------------|-------------------------------------------------------------------------------------|----------------------|
| A                         | Write algorithm for quick sort and sort the following elements [40,11,4,72,17,2,49] |                      |
| B                         | Write multistage graph algorithm and solve following example.                       |                      |



C

Write algorithm for 0/1 knapsack problem using dynamic programming .Also solve the following example.

N=4, M=21 (p<sub>1</sub>,p<sub>2</sub>,p<sub>3</sub>,p<sub>4</sub>)=(2,5,8,1), (w<sub>1</sub>,w<sub>2</sub>,w<sub>3</sub>,w<sub>4</sub>)=(10,15,6,9)

T.E - Sem - Comp  
Advanced Algorithms

University of Mumbai

Examination 2020 under cluster 4 (Lead College: PCE New Panvel)

Examinations Commencing from 7<sup>th</sup> January 2021 to 20<sup>th</sup> January 2021

Program: Computer Engineering

Curriculum Scheme: Rev2016

Examination: TE Semester V

(4)

Course Code: CSDLO5013 and Course Name: Advanced Algorithm

Time: 2 hour

Max. Marks: 80

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|            |                                                                                                                  |
|------------|------------------------------------------------------------------------------------------------------------------|
| <b>Q1.</b> | <b>Choose the correct option for following questions. All the Questions are compulsory and carry equal marks</b> |
|------------|------------------------------------------------------------------------------------------------------------------|

1. *or* In dynamic table, the amortized cost of the single operation is at the most -----

- Option A: 2  
Option B: 1  
Option C: 3  
Option D: 4

2. *03* In Hiring Problem, how many times a new office assistant will be hired if the input is considered in the order of rank of candidates where the order is <4, 5, 2, 6, 3, 7, 8, 9, 10, 1>

- Option A: 5  
Option B: 6  
Option C: 8  
Option D: 7

3. *04* A binomial tree  $B_k$  has ---

- Option A:  $K^2$  nodes and the height of the tree is  $2k$   
Option B:  $(k+2)$  nodes and the height of the tree is  $(\lg k)$   
Option C:  $K$  nodes and the height of the tree is  $(k + 2)$   
Option D:  $2^k$  nodes and the height of the tree is  $k$

4. *05* Let the capacity of the edge from vertex u to vertex v is 30 and flow from vertex u to vertex v is -10 (minus 10). The residual capacity  $C_f$  is -----

- Option A: 20  
Option B: 30  
Option C: 40  
Option D: 50

5. *06* In bipartite graph  $G = (V E)$ , vertex set can be partitioned into  $V = P \cup Q$  where - ----- and all edges in  $E$  go between  $P$  and  $Q$ .

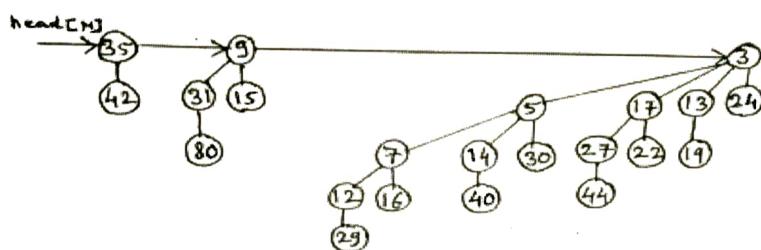
|           |                                                                                                                                                                                         |
|-----------|-----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| Option A: | P is subset of Q                                                                                                                                                                        |
| Option B: | Q is subset of P                                                                                                                                                                        |
| Option C: | $P \cap Q = \emptyset$                                                                                                                                                                  |
| Option D: | $P \cap Q \neq \emptyset$                                                                                                                                                               |
| 6.        | The sweeping algorithm which takes n line segments as input and considers endpoints in sorted order have runtime complexity of ----- to determine any pair of line segments intersects. |
| Option A: | $O(n)$                                                                                                                                                                                  |
| Option B: | $O(n \lg n)$                                                                                                                                                                            |
| Option C: | $O(n^2)$                                                                                                                                                                                |
| Option D: | $O(\lg n)$                                                                                                                                                                              |
| 7.        | Let A $\leq_p$ B. Which of the following statement is true?                                                                                                                             |
| Option A: | problems A and B are polynomial time equivalent                                                                                                                                         |
| Option B: | problem B is polynomial time reducible to problem A                                                                                                                                     |
| Option C: | problem A is polynomial time reducible to problem B.                                                                                                                                    |
| Option D: | problem A cannot be reducible to B in polynomial-time.                                                                                                                                  |
| 8.        | In Aggregate analysis for sequence of n operations worst case time is T(n). In the worst case the amortized cost per operation is given by -----                                        |
| Option A: | $n / T(n)$                                                                                                                                                                              |
| Option B: | $T(n)/n$                                                                                                                                                                                |
| Option C: | $T(n) * T(n)$                                                                                                                                                                           |
| Option D: | $n * n$                                                                                                                                                                                 |
| 9.        | In Red-Black tree, RB-DELETE_FIXUP procedure takes time ----- and performs at the most -----rotations.                                                                                  |
| Option A: | $O(n)$ and 2 rotations                                                                                                                                                                  |
| Option B: | $O(n)$ and 4 rotations                                                                                                                                                                  |
| Option C: | $O(\lg n)$ and 3 rotations                                                                                                                                                              |
| Option D: | $O(n \lg n)$ and 1 rotations                                                                                                                                                            |
| 10.       | In relabel-to-front algorithm let f is preflow. The edge from vertex u to vertex v is admissible if and only if -----                                                                   |
| Option A: | Residual capacity of edge u to v is greater than zero and height of vertex u is                                                                                                         |

|           |                                                                                                                                                                 |
|-----------|-----------------------------------------------------------------------------------------------------------------------------------------------------------------|
|           | larger than vertex v.                                                                                                                                           |
| Option B: | Residual capacity of edge v to vertex u is greater than zero and height of vertex u is less than vertex v.                                                      |
| Option C: | Residual capacity of edge u to v and height of vertex u and vertex v is equal.                                                                                  |
| Option D: | Residual capacity and height both conditions need not be fulfilled.                                                                                             |
| 11. 12    | Those problems that can be solved in polynomial time known as ----- problems.                                                                                   |
| Option A: | Decision                                                                                                                                                        |
| Option B: | Intractable                                                                                                                                                     |
| Option C: | Tractable                                                                                                                                                       |
| Option D: | Complete                                                                                                                                                        |
| 12. 13    | The convex hull of a set Q of points, denoted by $CH(Q)$ . If $ Q  \geq 3$ then at termination of Graham scan algorithm bottom to top content of stack is ----- |
| Option A: | Exactly the vertices of $CH(Q)$ in counterclockwise order                                                                                                       |
| Option B: | Exactly the vertices of $CH(Q)$ in clockwise order                                                                                                              |
| Option C: | All the vertices in $CH(Q)$                                                                                                                                     |
| Option D: | All the vertices having same polar angle.                                                                                                                       |
| 13. 14    | The time complexity of the recurrence $T(n) = 3T(n/3) + n/2$ by using master theorem is -----                                                                   |
| Option A: | $\Theta(n^2)$                                                                                                                                                   |
| Option B: | $\Theta(n \log n)$                                                                                                                                              |
| Option C: | $\Theta(\log n)$                                                                                                                                                |
| Option D: | $\Theta(n)$                                                                                                                                                     |
| 14. 15    | Let Red-Black has n number of internal nodes. Then this tree has height at most -----                                                                           |
| Option A: | $\lg(n+1)$                                                                                                                                                      |
| Option B: | n                                                                                                                                                               |
| Option C: | $2 \lg(n^2)$                                                                                                                                                    |
| Option D: | $2 \lg(n+1)$                                                                                                                                                    |
| 15. 16    | Which of the following statement is correct in case of hiring problem?                                                                                          |
| Option A: | Interviewing has higher cost than hiring.                                                                                                                       |
| Option B: | Interviewing and hiring both have equal cost.                                                                                                                   |

|           |                                                                                                                                                                                                                                                  |
|-----------|--------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| Option C: | Interviewing has lower cost whereas hiring is expensive                                                                                                                                                                                          |
| Option D: | hiring has lower cost than Interviewing                                                                                                                                                                                                          |
| 16. 17    | In Push-relabel algorithm the basic operation PUSH( $u, v$ ) that pushes flow from vertex $u$ to vertex $v$ applies if -----                                                                                                                     |
| Option A: | $u$ is an overflowing vertex, $C_f(u, v) > 0$ and vertex $u$ height = vertex $v$ height + 1.                                                                                                                                                     |
| Option B: | $v$ is an overflowing vertex, $C_f(v, u) > 0$ and vertex $v$ height = vertex $u$ height + 1.                                                                                                                                                     |
| Option C: | $u$ is an underflowing vertex, $C_f(u, v) > 0$ and vertex $u$ height = vertex $v$ height + 1.                                                                                                                                                    |
| Option D: | $v$ is an underflowing vertex, $C_f(v, u) > 0$ and vertex $v$ height = vertex $u$ height + 1.                                                                                                                                                    |
| 17. 18    | Let $M$ and $N$ are the two vectors. If the cross product $M \times N = 0$ then -----                                                                                                                                                            |
| Option A: | $M$ and $N$ are said to be colinear                                                                                                                                                                                                              |
| Option B: | $M$ is clockwise from $N$ with respect to the origin (0,0)                                                                                                                                                                                       |
| Option C: | $M$ is counterclockwise from $N$ with respect to the origin (0,0)                                                                                                                                                                                |
| Option D: | $M$ and $N$ are not related to each other.                                                                                                                                                                                                       |
| 18. 19    | Suppose two problems A and B not known to be in NP. Let problem C be an NP-Complete problem. Problem A is polynomial-time reducible to C and problem C is polynomial-time reducible to problem B. Which one of the following statements is true? |
| Option A: | Problem A is NP-hard                                                                                                                                                                                                                             |
| Option B: | Problem A is NP-Complete                                                                                                                                                                                                                         |
| Option C: | Problem B is NP-hard                                                                                                                                                                                                                             |
| Option D: | Problem B is NP-Complete                                                                                                                                                                                                                         |
| 19. 20    | In the union of two binomial heaps $H_1$ and $H_2$ , the root list of $H_1$ and $H_2$ is merged into a single linked list which is sorted by -----                                                                                               |
| Option A: | Increasing order of the key value of the root nodes.                                                                                                                                                                                             |
| Option B: | Decreasing order of the key value of the root nodes.                                                                                                                                                                                             |
| Option C: | Decreasing order of the degree of the root nodes.                                                                                                                                                                                                |
| Option D: | Increasing order of the degree of the root nodes                                                                                                                                                                                                 |
| 20. 21    | Deletion of a node in Red-Black tree takes ----- time                                                                                                                                                                                            |
| Option A: | $O(\lg n)$                                                                                                                                                                                                                                       |
| Option B: | $O(n)$                                                                                                                                                                                                                                           |
| Option C: | $O(\lg n)$ ← <i>wrong</i> <i><math>O(n \lg n)</math></i>                                                                                                                                                                                         |
| Option D: | $O(\lg(\lg n))$                                                                                                                                                                                                                                  |

|                          |                                                                                                                                                                                             |
|--------------------------|---------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| <b>Q2<br/>(20 Marks)</b> | <b>Solve any Four out of Six (5 marks each)</b>                                                                                                                                             |
| A                        | Show the red-black tree that result after successively inserting the keys 11, 10, 9, 4, 6, 1 into an initially empty red-black tree.                                                        |
| B                        | Explain how accounting method of amortized analysis is used to analyze the increment operation on a binary counter that starts at zero.                                                     |
| C                        | Use master method to find run time complexity of the following recurrence.<br>$T(n) = 6T(n/3) + n^2 \log n$                                                                                 |
| D                        | Prove that vertex-cover problem is NP-complete                                                                                                                                              |
| E                        | Consider the initial flow network as shown below. Find maximum flow from source vertex s to sink t using Relabel-to-front Algorithm. Consider initial vertex $V_1$ for discharge operation. |
| F                        | Explain analysis of hiring problem using indicator random variable.                                                                                                                         |

|                           |                                                                                                                                                                   |
|---------------------------|-------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| <b>Q3.<br/>(20 Marks)</b> | <b>Solve any Two Questions out of Three (10 marks each)</b>                                                                                                       |
| A                         | Write steps to extract the node with minimum key from binomial heap. Extract the node with minimum key from following binomial heap. Show each step clearly.      |
| B                         | Use recursion tree method to find time complexity of the following recurrence.<br>$T(n) = T(n/4) + T(n/2) + cn^2$                                                 |
| C                         | What is maximum flow in the given network from source s to sink t by Ford Fulkerson algorithm? Show all the flow networks, residual networks and augmented paths. |

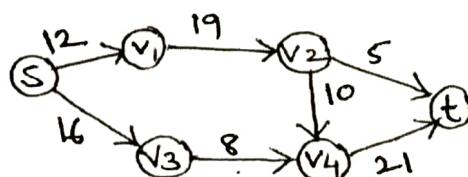


B

Use recursion tree method to find time complexity of the following recurrence.  
 $T(n) = T(n/4) + T(n/2) + cn^2$

C

What is maximum flow in the given network from source s to sink t by Ford Fulkerson algorithm? Show all the flow networks, residual networks and augmented paths.



## TE | COMP | SEM V | Choice Base | Advance Algorithm

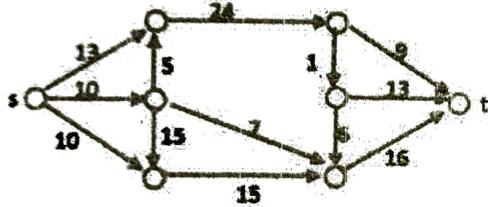
(5)

(3 Hours)

[Total Marks: 80]

- N.B. (1) Question No. 1 is compulsory  
 (2) Attempt any three out of the remaining five questions  
 (3) Assumptions made should be clearly stated

1. (a) Differentiate between P, NP, NP Complete and NP-Hard classes of Complexity. 05  
 (b) Define Red-Black tree. 05  
 (c) Write short note on bipartite matching. 05  
 (d) Explain recurrences with example. 05
2. (a) Define Maximum flow and Minimum-Cut. Apply Ford Fulkerson algorithm on following. 10



- (b) What is convex hull? Explain Jarvis March in detail. 10

3. (a) Prove that Vertex Cover is NP-Complete. 10  
 (b) Explain Master theorem, and apply on the following examples. 10
  - i)  $T(n) = 2T(n/2) + n$
  - ii)  $T(n) = 4T(n/2) + n^2$
4. (a) Explain steps to prove any problem as NP Complete problem. 10  
 (b) Define Binomial Heap, Explain its operations with example. 10
5. (a) Explain DELETE operation in Red-Black Tree. Discuss its time complexity. 10  
 (b) Prove that TSP is NP-Complete. 10
6. Write a short note on following (any 4) 20
  - (a) Amortized Analysis
  - (b) Randomized Algorithm
  - (c) Relabel to Front algorithm
  - (d) Line segment properties
  - (e) NP-Completeness

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## Advanced Algorithms.

University of Mumbai

Examination 2020 under cluster 4 (Lead College: PCE, New Panvel)

Program: Computer Engineering

Curriculum Scheme: Rev2016

(2)

Examination: Third Year Semester V

Course Code: CSDLO5013 and Course Name: Advanced Algorithms

Time: 1 hour Max. Marks: 50

For the students:- All the Questions are compulsory and carry equal marks .

|           |                                                                                                                                                                                       |
|-----------|---------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| Q1.3      | What is A if $A = \{ f(n) : \text{there exist positive constants } c_1, c_2, \text{ and } n_0 \text{ such that } 0 \leq c_1(n) \leq f(n) \leq c_2 g(n) \text{ for all } n \geq n_0\}$ |
| Option A: | $\Omega(g(n))$                                                                                                                                                                        |
| Option B: | $\Theta(g(n))$                                                                                                                                                                        |
| Option C: | $\log(n)$                                                                                                                                                                             |
| Option D: | $O(n)$                                                                                                                                                                                |
| Q2.4      | If the recurrence relation is $T(n) = 3T(n/4) + n \log(n)$ , then the solution to the recurrence is                                                                                   |
| Option A: | $T(n) = O(\log n)$                                                                                                                                                                    |
| Option B: | $T(n) = O(n)$                                                                                                                                                                         |
| Option C: | $T(n) = O(n \log n)$                                                                                                                                                                  |
| Option D: | $T(n) = O(n^2)$                                                                                                                                                                       |
| Q3.5      | Which of the following are the types of amortized analysis?                                                                                                                           |
| Option A: | Potential, Accounting, Integration                                                                                                                                                    |
| Option B: | Aggregate, Potential, Integration                                                                                                                                                     |
| Option C: | Aggregate, Accounting, Integration                                                                                                                                                    |
| Option D: | Potential, Accounting, Aggregate                                                                                                                                                      |
| Q4.6      | In dynamic tables the load factor $\alpha(T)$ of a nonempty table T is given by which of the following statements.                                                                    |
| Option A: | $\alpha(T) = (\text{Number of items stored in the table}) / (\text{size of the table})$                                                                                               |
| Option B: | $\alpha(T) = \text{Number of items stored in the table}$                                                                                                                              |
| Option C: | $\alpha(T) = (\text{size of the table}) / (\text{Number of items stored in the table})$                                                                                               |
| Option D: | $\alpha(T) = \text{size of the table}$                                                                                                                                                |
| Q5.7      | The time complexity of convex hull is :                                                                                                                                               |
| Option A: | $O(n)$                                                                                                                                                                                |
| Option B: | $O(\log n)$                                                                                                                                                                           |
| Option C: | $O(n \log n)$                                                                                                                                                                         |
| Option D: | $O(n^2)$                                                                                                                                                                              |
| Q6.8      | Package wrapping (or gift wrapping) technique to compute the convex hull of a set of points is used in :                                                                              |
| Option A: | Jarvis's march                                                                                                                                                                        |
| Option B: | Graham's scan                                                                                                                                                                         |

|           |                                                                                                                                                                                                                                                                                                                                                                                           |
|-----------|-------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| Option C: | Incremental method                                                                                                                                                                                                                                                                                                                                                                        |
| Option D: | Divide-and-conquer method                                                                                                                                                                                                                                                                                                                                                                 |
| Q7.9      | If the cross products between vector p1 and vector p2 ( $p_1 \times p_2$ ) is positive, then:<br>Option A: vector p1 is counterclockwise from vector p2 with respect to the origin (0,0).<br>Option B: vector p1 is clockwise from vector p2 with respect to the origin (0,0).<br>Option C: the boundary condition arises.<br>Option D: it can be concluded that cross products is wrong. |
| Q8.10     | Which of the following statements about red-black tree is false?<br>Option A: It is a binary tree.<br>Option B: The root is black.<br>Option C: Every leaf (NIL) is black.<br>Option D: The root is red.                                                                                                                                                                                  |
| Q9.11     | What is the maximum height of a red-black tree with n internal nodes?<br>Option A: $2 \log(n+1)$<br>Option B: $n^2$<br>Option C: $(n(n+1))/2$<br>Option D: $\log(n)$                                                                                                                                                                                                                      |
| Q10.12    | Which of the following is a properties specific to the red-black tree?<br>Option A: The root is red.<br>Option B: If a node is red, then both its children nodes are black.<br>Option C: Every leaf (NIL) is red.<br>Option D: The root node can hold any number of child nodes.                                                                                                          |
| Q11.13    | Which of the following is irrelevant to the Ford-Fulkerson method for solving the maximum-flow problem?<br>Option A: Residual networks<br>Option B: Augmenting paths<br>Option C: Minimum cuts<br>Option D: Minimum joints                                                                                                                                                                |
| Q12.14    | Select the complexity of SEARCH operation in Red Black Tree.<br>Option A: $O(n^2 \log n)$<br>Option B: $O(n)$<br>Option C: $O(n \log n)$<br>Option D: $O(\log n)$                                                                                                                                                                                                                         |
| Q13.15    | The maximum flow problem involves:<br>Option A: finding a flow between source and sink that is maximum<br>Option B: finding a flow between source and sink that is minimum<br>Option C: finding the shortest path between source and sink<br>Option D: computing a minimum spanning tree                                                                                                  |
| Q14.16    | An augmenting path is a:                                                                                                                                                                                                                                                                                                                                                                  |

|           |                                                                                                                                 |
|-----------|---------------------------------------------------------------------------------------------------------------------------------|
| Option A: | simple cyclic path between source and sink which pass through only positive weighted edges.                                     |
| Option B: | simple acyclic path between source and sink which pass through only positive weighted edges.                                    |
| Option C: | simple cyclic path between source and sink which pass through only negative weighted edges.                                     |
| Option D: | simple acyclic path between source and sink which pass through only negative weighted edges.                                    |
| Q15.17    | How many conditions have to be met if an NP- complete problem is reducible?                                                     |
| Option A: | 1                                                                                                                               |
| Option B: | 2                                                                                                                               |
| Option C: | 3                                                                                                                               |
| Option D: | 4                                                                                                                               |
| Q16.18    | A CNF-satisfiability problem belongs to which class.                                                                            |
| Option A: | NP class                                                                                                                        |
| Option B: | P class                                                                                                                         |
| Option C: | NP complete                                                                                                                     |
| Option D: | NP hard                                                                                                                         |
| Q17.19    | What is the total cost of hiring an assistant in worst case situation if Ci is the interviewing cost and Ch is the hiring cost? |
| Option A: | $O(nCi + nCh)$                                                                                                                  |
| Option B: | $O(n^2)$                                                                                                                        |
| Option C: | $O(nCi * nCh)$                                                                                                                  |
| Option D: | $O(nCh)$                                                                                                                        |
| Q18.20    | Indicator random variables provide a convenient method for _____.                                                               |
| Option A: | converting between probabilities and expectations.                                                                              |
| Option B: | converting between probabilities and randomness.                                                                                |
| Option C: | converting between randomness and expectations.                                                                                 |
| Option D: | converting between worst case and average case.                                                                                 |
| Q19.21    | A binomial tree of order k has                                                                                                  |
| Option A: | $2^k$ nodes, and height k.                                                                                                      |
| Option B: | $2^{k+1}$ nodes, and height $\log(k)$ .                                                                                         |
| Option C: | $2^k$ nodes, and height $\log(k)$ .                                                                                             |
| Option D: | k nodes, and height $\log(k)$ .                                                                                                 |
| Q20.22    | A binomial heap with 13 nodes will consist of                                                                                   |
| Option A: | three binomial trees of orders 8, 3, and 2.                                                                                     |
| Option B: | three binomial trees of orders 3, 2, and 0.                                                                                     |
| Option C: | three binomial trees of orders 6, 5, and 2.                                                                                     |
| Option D: | three binomial trees of orders 5, 5, and 2.                                                                                     |
| Q21.23    | A vertex cover of a graph is a set of vertices that includes                                                                    |
| Option A: | at least one endpoint of every edge of the graph.                                                                               |

|           |                                                                             |
|-----------|-----------------------------------------------------------------------------|
| Option B: | all vertices of the graph.                                                  |
| Option C: | all edges of the graph.                                                     |
| Option D: | number of vertices more than edges                                          |
| Q22.24    | The traveling-salesman problem is                                           |
| Option A: | P type                                                                      |
| Option B: | NP-complete type                                                            |
| Option C: | NP type                                                                     |
| Option D: | NP hard type                                                                |
| Q23.25    | Which of the following statements is true about Push-reliable algorithm?    |
| Option A: | It examines the entire residual network to find an augmenting path.         |
| Option B: | It examines only a part of the residual network to find an augmenting path. |
| Option C: | It works on one vertex at a time.                                           |
| Option D: | It works on all vertices at a time.                                         |
| Q24.26    | Extra bit in red black tree is for:                                         |
| Option A: | Address                                                                     |
| Option B: | Height                                                                      |
| Option C: | Index                                                                       |
| Option D: | Color                                                                       |
| Q25.27    | What is probabilistic analysis?                                             |
| Option A: | It is linear analysis.                                                      |
| Option B: | Probability is used in input.                                               |
| Option C: | Probability is used in output.                                              |
| Option D: | Use of probability in analyzing randomized algorithms.                      |