

Machine Learning

Clustering

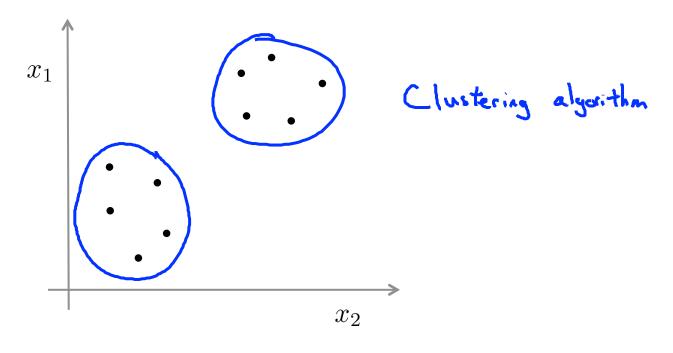
Unsupervised learning introduction

Supervised learning



Training set: $\{(x^{(1)}, y^{(1)}), (x^{(2)}, y^{(2)}), (x^{(3)}, y^{(3)}), \dots, (x^{(m)}, y^{(m)})\}$

Unsupervised learning



Training set: $\{x^{(1)}, x^{(2)}, x^{(3)}, \dots, x^{(m)}\}$

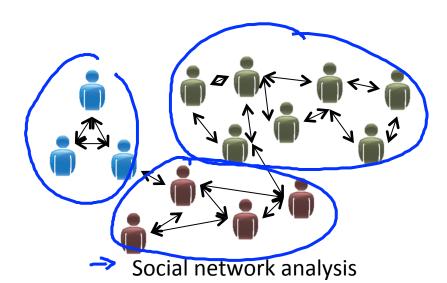
Applications of clustering

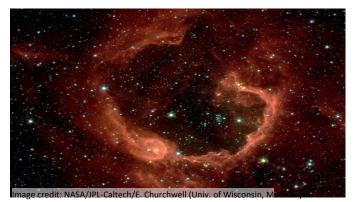


Market segmentation



Organize computing clusters





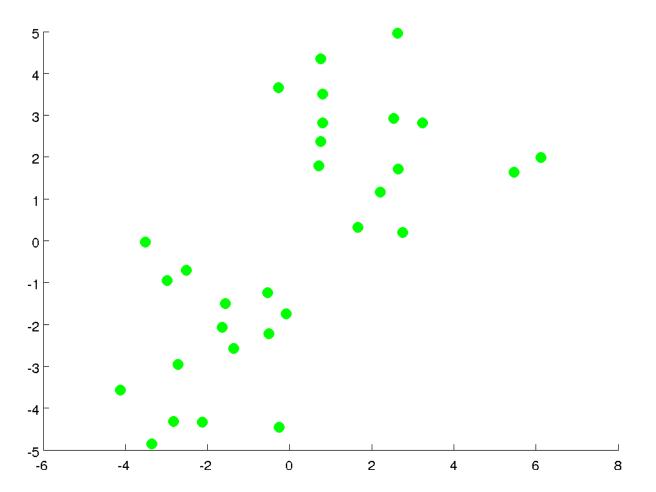
Astronomical data analysis

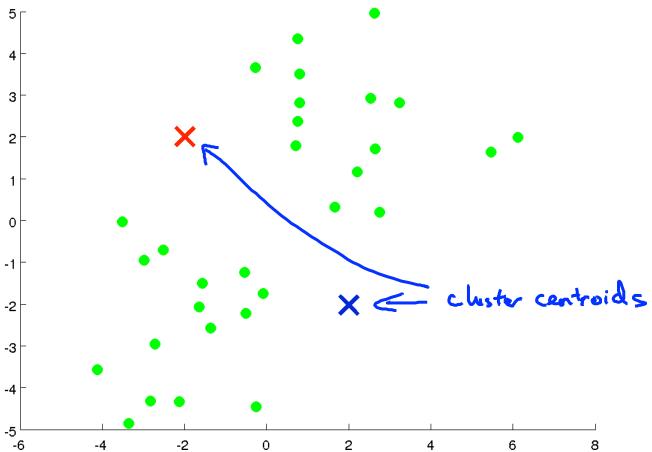


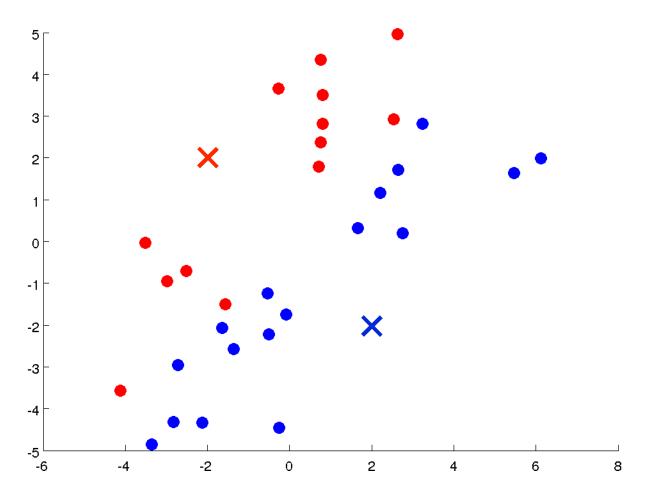
Machine Learning

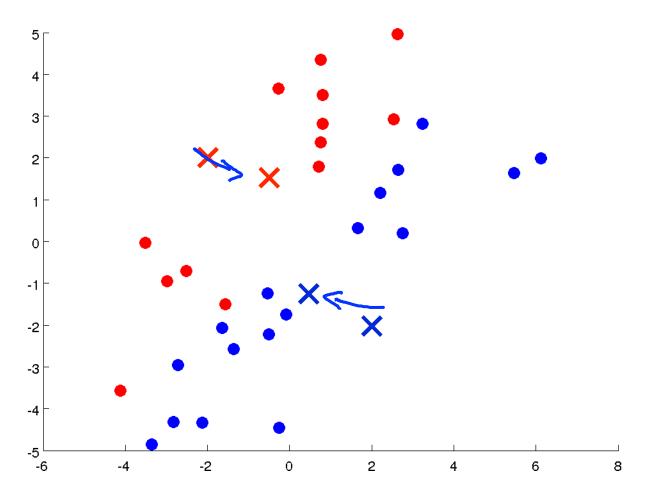
Clustering

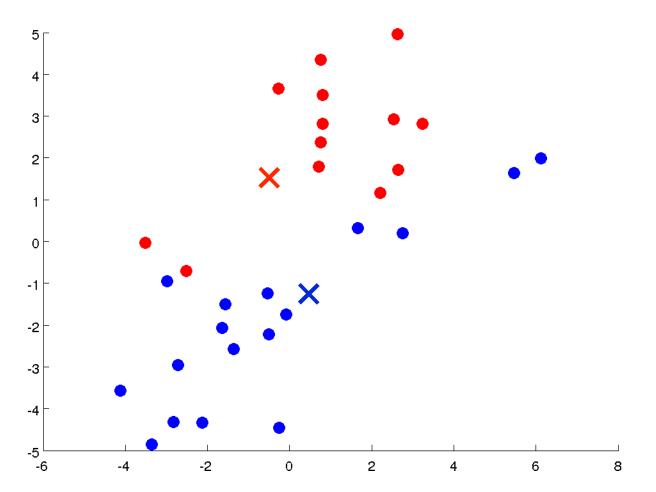
K-means algorithm

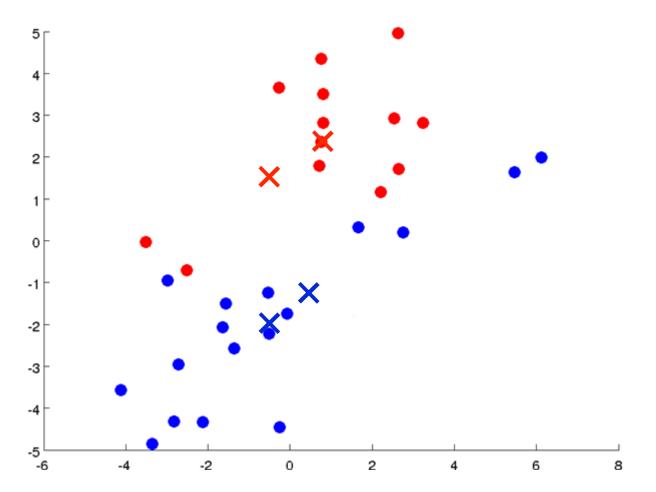


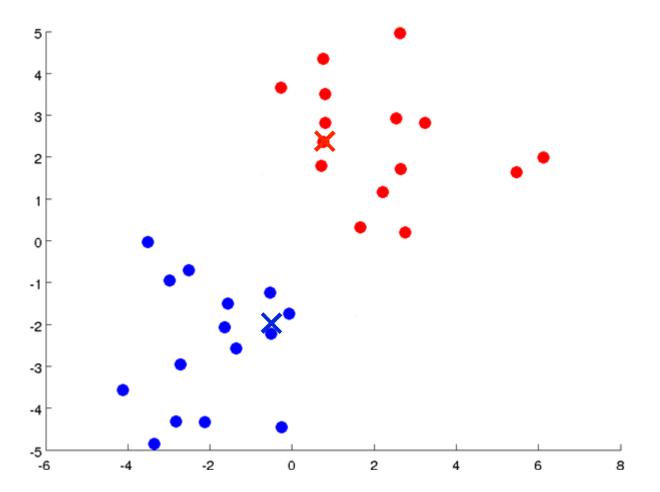


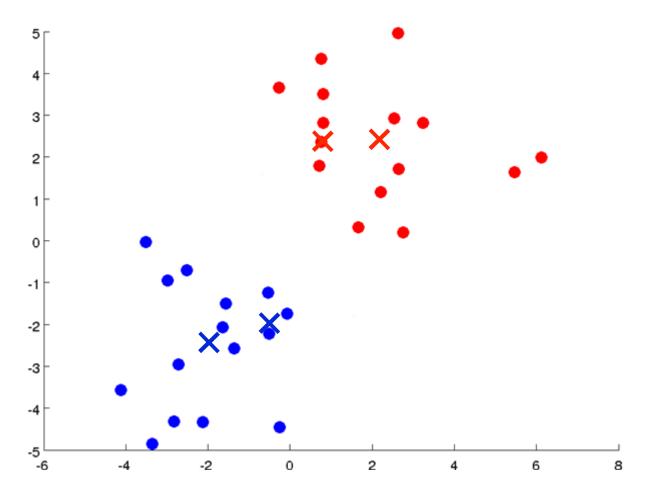


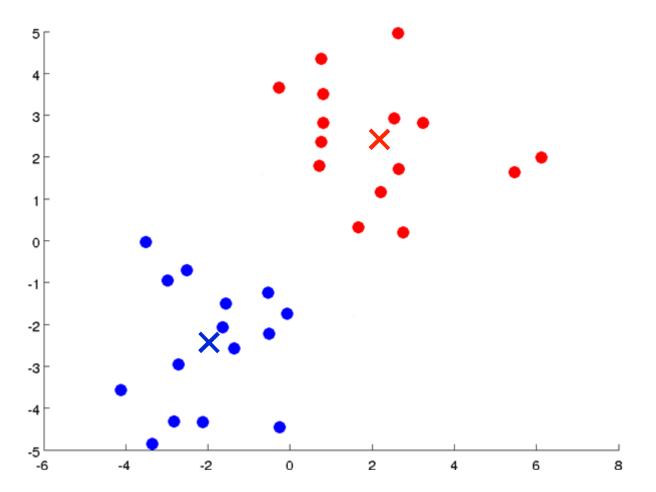












Input:

- K (number of clusters) \leftarrow
- Training set $\{x^{(1)}, x^{(2)}, \dots, x^{(m)}\}$

$$x^{(i)} \in \mathbb{R}^n$$
 (drop $x_0 = 1$ convention)

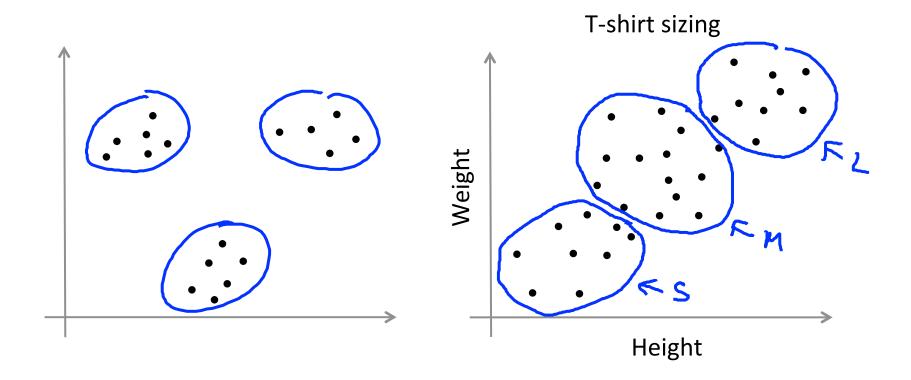


Randomly initialize K cluster centroids $\mu_1, \mu_2, \dots, \mu_K \in \mathbb{R}^n$

```
Repeat {
Cluster for i = 1 to m
c^{(i)} := index (from 1 to <math>K) of cluster centroid closest to x^{(i)}
closest to x^{(i)}
                                                                                                         الى بتحصل هنا انى بدور على أقل
                                                                                                         u و training ex(i) سىافە س
                  \rightarrow \mu_k := average (mean) of points assigned to cluster k
```

K-means for non-separated clusters







Machine Learning

Clustering Optimization objective

K-means optimization objective

- $\rightarrow c^{(i)}$ = index of cluster (1,2,...,K) to which example $x^{(i)}$ is currently assigned ke {1,2,.., k}
- $\rightarrow \mu_k$ = cluster centroid k ($\mu_k \in \mathbb{R}^n$)
 - $\mu_{c^{(i)}}$ = cluster centroid of cluster to which example $x^{(i)}$ has been assigned

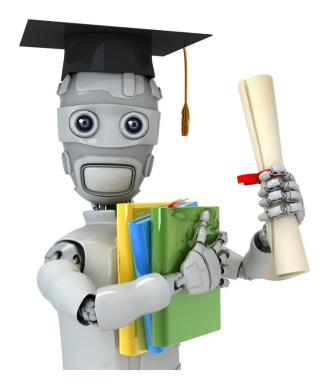
Diff. between location of example x(i) & Optimization objective: location of cluster centroid to which x(i) has

$$\min_{\Rightarrow c^{(1)}, \dots, c^{(m)}} J(c^{(1)}, \dots, c^{(m)}, \mu_1, \dots, \mu_K)$$

$$\rightarrow \mu_1, \dots, \mu_K$$
 Distortion

Trying to minimize this idistance as possible

```
Randomly initialize K cluster centroids \mu_1, \mu_2, \ldots, \mu_K \in \mathbb{R}^n cluster essignment step (n) call (n) cal
                                                                                                                            c^{(i)} := index (from 1 to K ) of cluster centroid closest to x^{(i)}
                                                                              for k = 1 to K
                                                                                                                                      \mu_k := average (mean) of points assigned to cluster k
```



Machine Learning

Clustering Random initialization

Randomly initialize K cluster centroids $\mu_1, \mu_2, \dots, \mu_K \in \mathbb{R}^n$

```
Repeat {
        for i = 1 to m
           c^{(i)} := \text{index (from 1 to } K \text{ ) of cluster centroid}
                   closest to x^{(i)}
        for k = 1 to K
            \mu_k := average (mean) of points assigned to cluster k
```

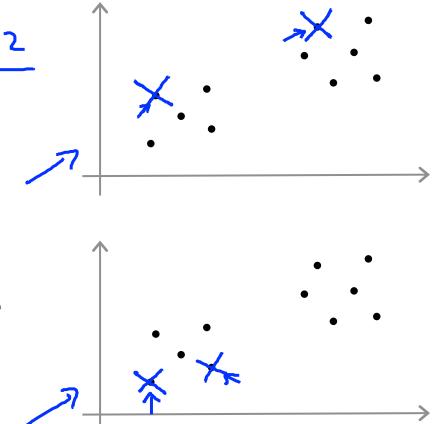
Random initialization

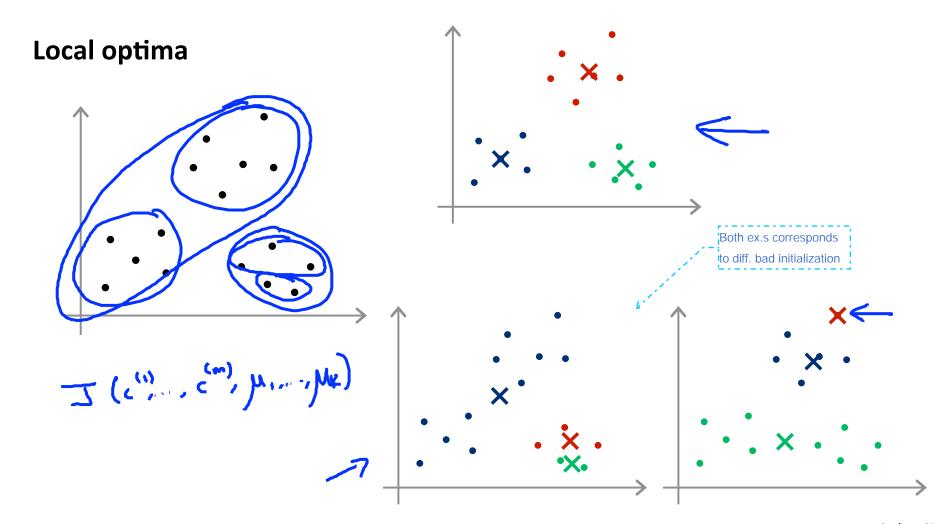
 ${\bf Should\ have}\ K < m$

Randomly pick \underline{K} training examples.

Set μ_1, \dots, μ_K equal to these K examples. $\mu_1 = \chi_1^{(i)}$

$$\mu_2 = \kappa_{(i)}$$

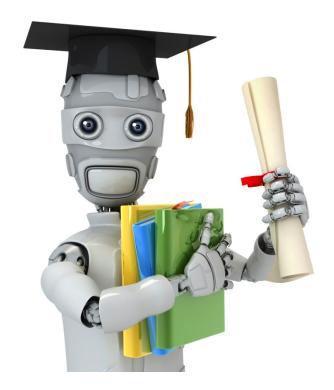




Random initialization

```
For i = 1 to 100 { Randomly initialize K-means. Run K-means. Get c^{(1)}, \dots, c^{(m)}, \mu_1, \dots, \mu_K. Compute cost function (distortion) J(c^{(1)}, \dots, c^{(m)}, \mu_1, \dots, \mu_K)
```

Pick clustering that gave lowest cost $J(c^{(1)},\ldots,c^{(m)},\mu_1,\ldots,\mu_K)$

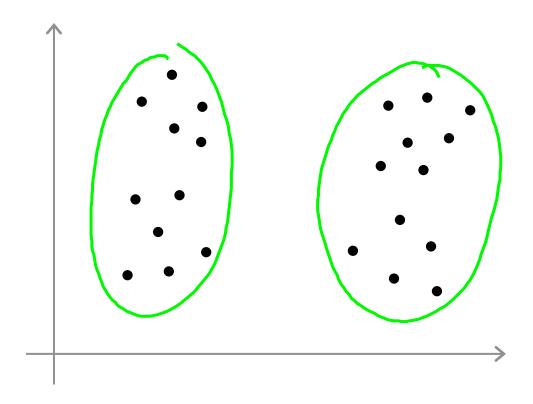


Machine Learning

Clustering

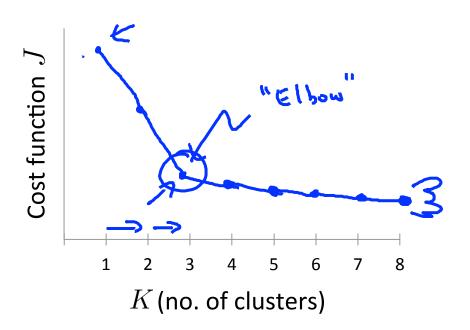
Choosing the number of clusters

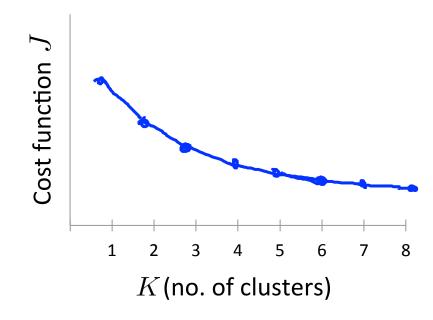
What is the right value of K?



Choosing the value of K

Elbow method:





Choosing the value of K

Sometimes, you're running K-means to get clusters to use for some later/downstream purpose. Evaluate K-means based on a metric for how well it performs for that later purpose.

