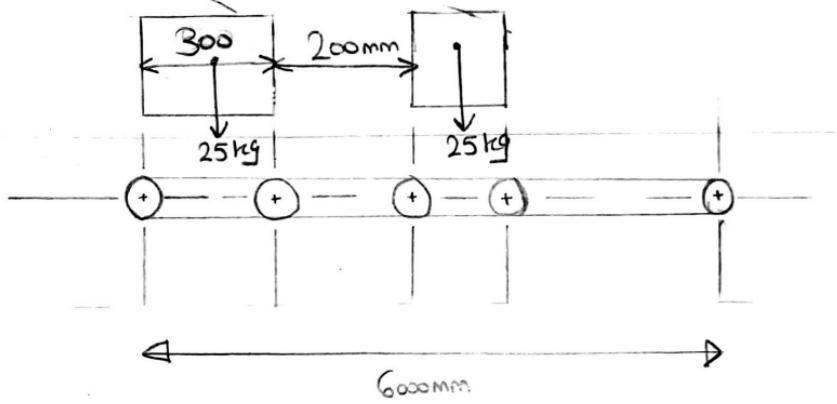


(1)

Project

Chain-Roller Conveyor

Description	Values
Conveyor Total length	6000 mm
Rollers Centred distance	250 mm
Linear Velocity	0.5 m/s & 0.7 m/s
Roller Diameter	100 → 150 mm
Box to Box distance	200 mm
Box Size	300x300x300 mm
Box Weight	25 kg



* Firstly, we need to take the losses into our Considerations. (V-Belt + Gearbox + Chain).

• Number of boxes : $\frac{\text{Total Distance}}{(\text{Rollers centre distance} + \text{distance bet the boxes})}$

$$= \frac{6000}{(300+200)} = 12 \text{ boxes}$$

• Weight of all boxes = weight of each box * Number of boxes = $(12 * 25 * 10) = 3000 \text{ N}$

• Power @ $V=0.5$ = weight of the boxes * Velocity = $3000 * 0.5 = 1500 \text{ W}$

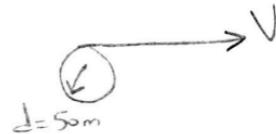
• Power @ $V=0.7$ = $3000 * 0.7 = 2100 \text{ W}$

• efficiency calculated = $(0.97)^4 = 0.885$

$$\text{Power Actual}_{V=0.5} = \frac{1500}{0.885} = 1694.9 \text{ W} \approx 1695 \text{ W}$$

$$\text{Power Actual}_{V=0.7} = \frac{2100}{0.885} = 2372.88 \text{ W}$$

@ $V = 0.5 \text{ m/s}$



$$(0.5 * 1^3) = \frac{V = w r}{2\pi n_1} * 50 \Rightarrow n_1 = 103 \text{ rPM}$$

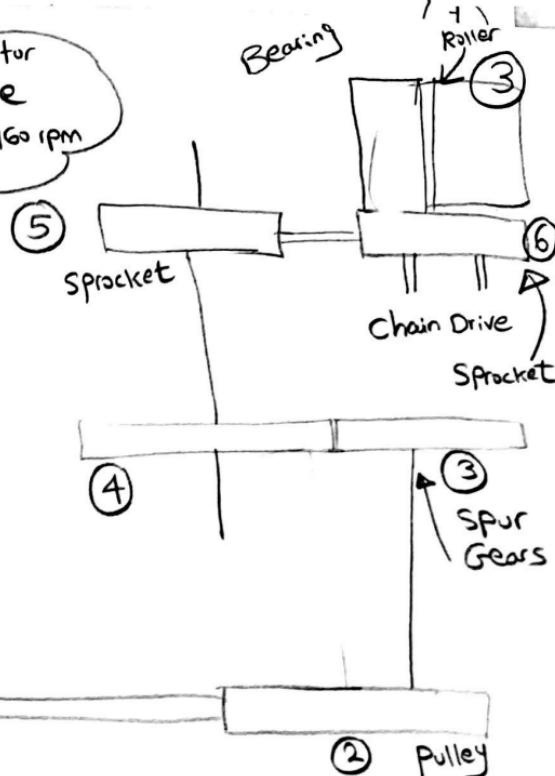
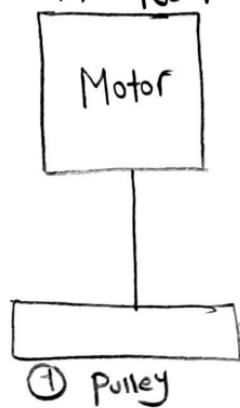
@ $V = 0.7 \text{ m/s}$

$$(0.7 * 1^3) = \frac{2\pi n_2}{60} * 50 \Rightarrow n_2 = 134 \text{ rPM}$$

From the electric Motor Catalogue, I will choose the 5.5kW with its 960 rpm

$$H = 5500 \text{ W}$$

$$n_1 = 960 \text{ rpm}$$



Firstly

$$\ast \text{Number of Boxes} = 12 \text{ boxes} = \frac{6000}{300+200}$$

$$\text{Rollers} = \frac{\text{Total Distance}}{\text{Roller Centre Distance}} = \frac{6000}{250} = 24 \text{ rollers}$$

$$\text{Chains} = 24 - 1 = 23 \text{ chains}$$

Belts

$$@ V = 0.7$$

$$\text{Total transmission ratio} = \frac{960}{134} = 7.16$$

$$\hookrightarrow i_B * i_{\text{chain}} * i_{\text{Gears}} = [1.5 * 1.5 * 3.184] \text{ respectively}$$

$$\textcircled{1} \quad H = 5500 \text{ W}, \quad n_1 = 960 \text{ rpm}$$

$$H_{\text{des}} = H * S.F = \left(\frac{5500}{1000} * 1.3 \right) = \boxed{7.15 \text{ kW}}$$

Type B

$$\textcircled{2} \quad \text{Assume } V = 20 \text{ m/s}$$

$$d_1 = \frac{60V}{\pi n_1} = \frac{60 * 20 * 10^3}{\pi * 960} = 397.88 \text{ mm}$$

Standard diameter
: 400 mm

$$\textcircled{3} \quad i_{12} = \frac{n_1}{n_2} = \frac{d_2}{d_1},$$

$$1.5 = \frac{960}{n_2} = \frac{d_2}{400},$$

$$n_2 = 640 \text{ rpm}$$

$$d_2 = 600 \text{ mm}$$

Center distance

$$D < C < 3(D+d)$$

$$600 < C < 3(600+400)$$

$$600 < C < 3000$$

$$\text{Let } C = 1200$$

$$\theta_s = \pi - \left(\frac{d_2 - d_1}{C} \right) = \pi - \left(\frac{600 - 400}{1200} \right) \quad (5)$$

$$= 2.97 \text{ rad} = 170.45^\circ$$

$$(4) L = 2C + \frac{\pi}{2}(d_2 + d_1) + \frac{(d_2 - d_1)^2}{4C}$$

$$= (2 \times 1200) + \frac{\pi}{2}(600 + 400) + \frac{(200)^2}{4 \times 1200},$$

$$2400 + 1570.796 + \frac{25}{3} = 3979.129$$

$$\text{Standard pitch length} = 4056 \text{ mm}$$

$$L_{in} = L - L_o = 4056 - 43 = 4013 \text{ mm}$$

$$(5) H_{rat} = \left[k_1 V^{-0.09} - \frac{k_2}{D_e} - k_3 \cdot 10^{-4} V^2 \right] V$$

$$k_1 = 1.08, \quad k_2 = 69.8, \quad k_3 = 1.78, \quad D_e = 175 \text{ mm}$$

$$D_e = d \cdot k_e = (400 \cdot 1.11) = 444 \text{ mm}$$

$$H_{rat} = \left[1.08(20)^{-0.09} - \frac{69.8}{175} - 1.78 \cdot 10^{-4} \cdot 400 \right] 20 =$$

$$\left[0.8247 - 0.3988 - 0.0712 \right] 20 = 7.094 \text{ hp} \approx$$

$$7.094 \cdot 0.74 = 5.249 \text{ kW}$$

$$\textcircled{6} \quad N = \frac{H_{bles}}{k_L * k_A * H_{rat}} = \frac{7.15}{1.13 * 0.9809 * 5.249} \\ = 1.2 \text{ belts} \approx \boxed{2 \text{ belts}}$$

170 0.98

170.45 ? , $k_A = 0.9809$

180 1

$$\textcircled{7} \quad L = 2C' + \frac{\pi}{2}(d_1 + d_2) + \frac{(d_2 - d_1)^2}{4C'}$$

$$4056 = 2C' + \frac{\pi}{2}(1000) + \frac{(200)^2}{4C'}$$

$$16224 C' = 8(C')^2 + 2000\pi C' + 40000$$

$$C' = 4.036 \text{ m} = \boxed{4036 \text{ mm}}$$

(8)

$$2\beta = 38$$

$$e = 19$$

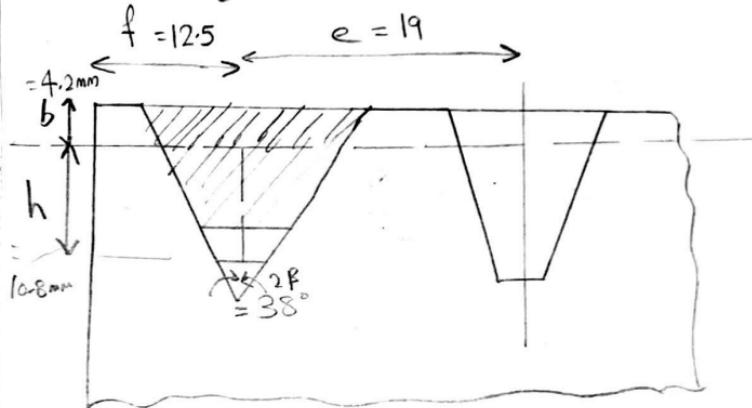
$$f = 12.5$$

$$W = (N-1)e + 2f = 19 + (2 \cdot 12.5)$$

$$= 44 \text{ mm}$$

$$f = 12.5$$

$$e = 19$$



(7)

Spur gears

$$\textcircled{1} \quad C_{34} = 3.184 \quad , \quad n_2 = n_3 = 64 \text{ rpm}$$

$$N_3 = 18 \text{ teeth}$$

$$\textcircled{2} \quad \text{From the graph, } m = 4 \text{ mm}$$

$$\textcircled{3} \quad d_3 = mN_3 = (4 * 18) = 72 \text{ mm}$$

$$C_{34} = \frac{d_4}{d_3} = \frac{N_4}{N_3} = \frac{n_3}{n_4}$$

$$3.184 = \frac{N_4}{18} \quad , \quad N_4 = (18 * 3.184) = 58 \text{ teeth}$$

$$d_4 = (mN_4) = (4 * 58) = 232 \text{ mm}$$

$$n_4 = \frac{n_3}{C_{34}} = \frac{640}{3.184} = 201.005 \text{ rpm}$$

$$C_{34} = \frac{d_3 + d_4}{2} = \frac{72 + 232}{2} = 152 \text{ mm}$$

$$\textcircled{4} \quad F = 4\pi m = (4\pi * 4) = 50 \text{ mm}$$

$$\textcircled{5} \quad \sigma = \frac{Vt}{F k v m Y} = \frac{H/V}{F k v m Y} \quad , \quad V = \omega_3 r_3$$

$$V = \frac{2\pi n_3}{60} * r_3 = \frac{2\pi * 640}{60} * 36 = 2412 \text{ m/s}$$

$$\omega_t = \frac{H}{V} = \frac{5.5 * 10^3}{2.412} = 2280.26 \text{ rad/s}$$

$$K_V = \frac{6}{6+V} = \frac{6}{6+2.412} = 0.713$$

$$Y = 0.29327$$

$$\sigma = \frac{W_t}{F_k V_m Y} = \frac{2280.26}{50 * 0.713 * 4 * 0.29327} = 54.6 M$$

$$\sigma_{des} = 4\sigma = (4 * 54.6) = 218.4 \text{ MPa}$$

⑥ USE 4140 OQT 1300

$$S_y = 469 \text{ MPa}$$

$$S_{ut} = 662 \text{ MPa}$$

$$HB = 200$$

⑦ Endurance limit

$$S_e = k_a k_b k_c k_d k_e k_f S_e'$$

$$S_e' = \frac{S_{ut}}{2}$$

$$S_e' = \frac{662}{2} = 331 \text{ MPa}$$

$$k_a = 0.73, k_b = 0.93, k_c = 0.814, k_d = k_e = k_f = 1$$

$$S_e = (0.73 * 0.93 * 0.814 * 331) = 182.9 \text{ MPa}$$

$$Q = (\text{Mining Conveyor}) = 6$$

$$K_V = 0.8 \text{ from the graph}$$

$$J = 0.325$$

$$\sigma_a = \frac{W_t}{K_V F_m J} = \frac{2280.26}{0.8 * 50 * 4 * 0.325} = 43.85 \text{ MPa}$$

$$n = \frac{n_g}{K_o \cdot km} = \frac{S_e / \sigma_a}{K_o \cdot km} = \frac{182.9 / 43.85}{1.4 * 1.25} = 2.38 > 1, \text{ Safe}$$

$$⑧ S_c = (2.76HB - 70) = (2.76 \cdot 200 - 70) = 482 \text{ MPa} \quad ⑩$$

$$C_H = 1 \rightarrow C_T = 1 \rightarrow C_L = 1 \rightarrow C_R = 0.8$$

$$S_H = \frac{C_L \cdot C_H}{C_T \cdot C_R} * S_c = \frac{482}{0.8} = 903.75 \text{ MPa}$$

$$\sigma_H = C_p \sqrt{\frac{w_{t,p}}{C_v F_d I}} = 191 \sqrt{\frac{2280 \cdot 26}{0.8 \cdot 50 \cdot 72 \cdot 0.11}} = 512.42 \text{ MPa}$$

$$S_H = \sqrt{K_0 k_m n} \sigma_H,$$

$$903.75 = \sqrt{1.4 + 1.25n} * 512.42$$

$$n = 1.77 > 1.3, \text{ Safe}$$

ChainsGiven

$$\textcircled{1} \quad H = 5.5 \text{ kW}, n_4 = n_5 = 201 \text{ rpm}$$

or, $(134 * 1.5) = 201 \text{ rpm}$

$$\text{Kw rating of chain} = \frac{\text{Kw transmitted} * k_s}{k_1 * k_2}$$

$$= \frac{(5.5 * 1.3)}{(1 * 1.26)} = 5.674 \text{ kW}$$

② Selection of Chain

$$16 \text{ A} \quad P = 25.4 \text{ mm} \rightarrow n_5 = 201 \text{ rpm}$$

$\text{Kw rat} = 5.674 \text{ kW}$

$$\textcircled{3} \quad D_1 = \frac{P}{\sin\left(\frac{180}{z_1}\right)} = \frac{25.4}{\sin\left(\frac{180}{21}\right)} = 170.42 \text{ mm}$$

$$i_{GG} = \frac{z_2}{z_1} \rightarrow z_2 = (1.5 * 21) = 31.5 \approx 32 \text{ teeth}$$

$$D_2 = \frac{P}{\sin\left(\frac{180}{z_2}\right)} = \frac{25.4}{\sin\left(\frac{180}{32}\right)} = 259.13 \text{ mm}$$

$$\textcircled{4} \quad a = 40P = (40 * 25.4) = 1016 \text{ mm}$$

$$L_n = 2 \left(\frac{a}{P} \right) + \left(\frac{z_1 + z_2}{2} \right) + \left(\frac{z_2 - z_1}{2\pi} \right)^2 * \frac{P}{a} =$$

$$2 \left(\frac{1016}{25.4} \right) + \left(\frac{32+21}{2} \right) + \left(\frac{32-21}{2\pi} \right)^2 * \frac{25.4}{1016} =$$

106 links

$$\textcircled{5} \quad a = \frac{P}{4} \left\{ \left[L_n - \left(\frac{z_1 + z_2}{2} \right) \right] + \sqrt{\left(L_n - \left(\frac{z_1 + z_2}{2} \right) \right)^2 - 8 \left(\frac{z_2 - z_1}{2\pi} \right)^2} \right\}$$

$$= \frac{25.4}{4} \left\{ \left[(106 - \left(\frac{32+21}{2} \right)) \right] + \right.$$

$$\left. \sqrt{(106 - \left(\frac{32+21}{2} \right))^2 - 8 \left(\frac{?}{2\pi} \right)^2} \right\}$$

$$, \quad 6.35 \left\{ (79.5) + \sqrt{(79.5)^2 - 16.41} \right\} =$$

$$6.35 (158.896) = \boxed{1008.99 \text{ mm}}$$

(13)

$$V = 0.5$$

Given $H = 5500 \text{ W}$,

$$\text{Total transmission ratio} = \frac{960}{100} = 9.6$$

* We should apply the constraint of equalizing the transmission ratios of the belts & the chains in both the velocities (0.5 m/s & 0.7 m/s).

$$\begin{aligned} i_{\text{tot}} &= i_{\text{belts}} * i_{\text{chain}} * i_{\text{spur gear}} \\ &= 1.5 * 1.5 * 4.266 \end{aligned}$$

Spur Gears

$$\textcircled{1} \quad N_3 = 23 \text{ teeth}, \quad i_{34} = \frac{N_3}{N_4} = \frac{960}{1.5} = 640 \text{ teeth}$$

$$\textcircled{2} \quad d_3 = 25 \text{ mm} = \text{module}$$

$$\textcircled{3} \quad d_3 = mN_3 = (25 \times 23) = 57.5 \text{ mm} \quad (\textcircled{3}^*)$$

$$n_4 = \frac{n_3}{i_{34}} = \frac{640}{4.266} = 150.023 \text{ rpm}$$

$$4.266 = \frac{d_4}{d_3}, \quad N_4 = 98 \text{ teeth}$$

$$d_4 = mN_4 = (98 \times 25) = 245 \text{ mm}$$

$$C = \frac{d_3 + d_4}{2} = \frac{57.5 + 245}{2} = 151.3 \text{ mm}$$

~~M = 375~~

$$④ F = (4\pi m) = (4 * \pi * 2.5) = 31.41 \text{ mm}$$

14

$$⑤ \sigma = \frac{W_t}{F K_v M Y}$$

$$W_t = \frac{H}{V} = \frac{5500}{\left(\frac{2\pi * 640}{60} * 28.75 \right)} = \frac{5500}{1.926} \\ = 2855.65 \text{ N}$$

$$K_v = \frac{6}{6+V} = \frac{6}{6+1.926} = 0.757$$

$$\sigma = \frac{2855.65}{31.41 * 0.757 * 2.5 * 0.29327} = 165.336 \text{ MPa}$$

$$\sigma_{des} = 4 * \sigma = (4 * 165.336) = 661.345 \text{ MPa}$$

⑥ Select OQT 700
 $\sigma_{ult} = 1590 \text{ MPa}$
 $\sigma_y = 1460 \text{ MPa}$
 $H_B = 461$

$$S_e = \frac{\sigma_{ult}}{2} = \frac{1590}{2} = 795 \text{ MPa}$$

$$S_e = k_a \cdot k_b \cdot k_c \cdot k_d \cdot k_e \cdot k_f \cdot S_e$$

$$k_a = 0.63 \rightarrow k_b = 0.974 \rightarrow k_c = 0.814$$

$$k_d = k_e = k_f = 1$$

$$= (0.63 * 0.974 * 0.814 * 1 * 795) = 397 \text{ MPa}$$

$$J = 6$$

$$k_v = 0.8$$

$$J = 0.32$$

15

$$b) \sigma_a = \frac{W_t}{k_v f_m J} = \frac{2855 \cdot 65}{0.8 \cdot 31.41 \cdot 2.5 \cdot 0.32} = 142.05 \text{ MPa}$$

$$n = \frac{S_e / \sigma_a}{k_o \cdot k_m} = \frac{397 / 142.05}{1.3 \cdot 1.5} = 2.149 \geq 1 \rightarrow \text{safe}$$

(8) $S_c = 2.76HB - 70 = (2.76 \cdot 461) - 70 = 1202.36 \text{ MPa}$

$$C_H = 1, C_T = 1, C_R = 1, C_L = 1.3$$

$$\sigma_H = C_p \sqrt{\frac{W_t P}{C_v F_d I}} = 191 \sqrt{\frac{2855 \cdot 65}{0.8 \cdot 31.41 \cdot 57.5 \cdot 0.122}}$$

$$= 768.76 \text{ MPa}$$

$$S_H = \sqrt{k_o \cdot k_m \cdot n} \quad \sigma_H$$

$$1563.055 = \sqrt{1202.36 \cdot n} \approx 768.76$$

$$n = 2.54 \geq 1 = \text{safe}$$

$$S_H = \frac{C_L C_H}{C_T C_R} S_c$$

$$= \frac{1202.36 \cdot 1.3}{1.3} = 1563.055 \text{ MPa}$$

(16)

$$\omega \quad V = 0.5 \text{ m/s}$$

as @ $V = 0.5$, $n_5 = 100 \text{ rpm}$, like mentioned before, so we will multiply it by 1.5, as it is the transmission ratio of the chain.

$$n_5 = 1.5 * 100 = 150 \text{ rpm}$$

$$\textcircled{1} \quad \text{KW rating} = \frac{\text{kW transmitted} * K_s}{K_1 * K_2} = \frac{5.5 * 1.3}{1.26} =$$

$$5.67 \text{ kW}$$

\textcircled{2} Select from table 16B

$$\text{Pitch} = 19.05 \text{ mm}$$

Interpolation

$$100 \quad 4.83$$

$$150 \quad ?$$

$$200 \quad 8.94$$

$$P_{\text{ans}} = 6.885 \text{ kW}$$

$$\textcircled{3} \quad D_1 = \frac{P}{\sin\left(\frac{180}{z_1}\right)} = \frac{25.4}{\sin\left(\frac{180}{21}\right)} = 170.816 \text{ mm}$$

$$i_{56} = \frac{z_2}{z_1} \Rightarrow 1.5 = \frac{z_2}{21} \Rightarrow z_2 = 32 \text{ teeth}$$

$$D_2 = \left(\frac{P}{\sin\left(\frac{180}{z_2}\right)} \right) = \frac{25.4}{\sin\left(\frac{180}{32}\right)} = 259.13 \text{ mm}$$

$$\textcircled{4} \quad a = 40P = (40 * 25.4) = 1016 \text{ mm}$$

$$L_n = 2 \left(\frac{a}{P} \right) + \left(\frac{z_1 + z_2}{2} \right) + \left(\frac{z_2 - z_1}{2\pi} \right)^2 * \frac{P}{1} = \quad (17)$$

$$2 \left(\frac{1016}{25.4} \right) + \left(\frac{32+21}{2} \right) + \left(\frac{9}{2\pi} \right)^2 * \frac{25.4}{1016} = \boxed{106 \text{ links}}$$

$$(5) \quad a = \frac{P}{4} \left\{ \left[L_n - \left(\frac{z_1 + z_2}{2} \right) \right] + \right.$$

$$\left. \sqrt{\left(L_n - \left(\frac{z_1 + z_2}{2} \right) \right)^2 - 8 \left(\frac{z_2 - z_1}{2\pi} \right)^2} \right\} = \\ \frac{25.4}{4} \left\{ \left[106 - \left(\frac{32+21}{2} \right) \right] + \right.$$

$$\left. \sqrt{\left(106 - (26.5) \right)^2 - 8 \left(\frac{9}{2\pi} \right)^2} \right\},$$

$$6.35 \left\{ (79.5) + 79.396 \right\} = \boxed{1009.3 \text{ mm}}$$

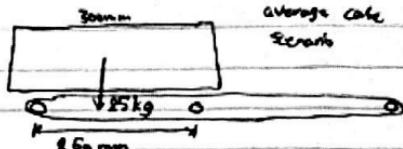
$$W = \frac{60}{60} W$$

Bearings (Deep groove)

Total distance = 6000 mm

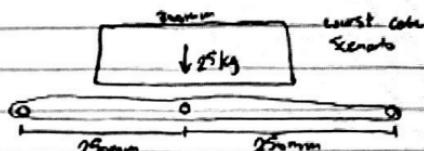
12 boxes \Rightarrow 3000 N

24 rollers



In average case Scenario

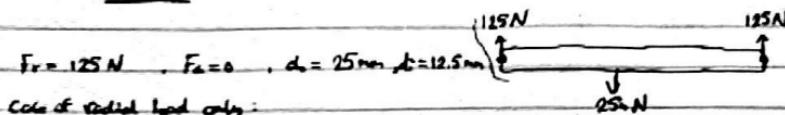
$$\text{roller force} = \frac{3000}{24} = 125 \text{ N (half box)}$$



In worst case Scenario

$$\text{roller force} = \frac{3000}{12} = 250 \text{ N (one box)}$$

Working on worst case Scenario



Case of radial load only:

$$P = 125 \text{ N} \quad & \text{ taking } k_{fr} = 1.1$$

$$F = 125 \times 1.1 = 137.5 \text{ N}$$

clearing $L = 25 \text{ mm}$, roller diameter = 10mm

$$\omega = c_7 + \frac{1}{2} \cdot \frac{1}{2} = 35 \text{ rad/s} \quad n = \frac{60}{2\pi} (25) = 334.2 \text{ rpm}$$

$$C = 137.5 \times \left(\frac{60 \times 25 \text{ mm} \times 334.2}{1.6} \right)^{\frac{1}{3}}$$

$$C = 1092.3 \text{ N}$$

clearing $L = 25 \text{ mm}$, roller diameter = 10mm
Deep Groove Ball Bearing (6205) $(d = \frac{25}{2} \text{ mm}, D = \frac{52}{2} \text{ mm})$

$$F_{ax} = 1250 \text{ N}, F_{bx} = 950 \text{ N}, n_{ax} = 3600 \text{ rpm}$$

$$C_{ax} = 14000 \text{ N}, C_{bx} = 7800 \text{ N}, n_{bx} = 19000 \text{ rpm}$$

$$C_a = 1 = 125 = 125 \text{ N}$$

$$C = 1092.3 \text{ N} < 1250 \text{ N}$$

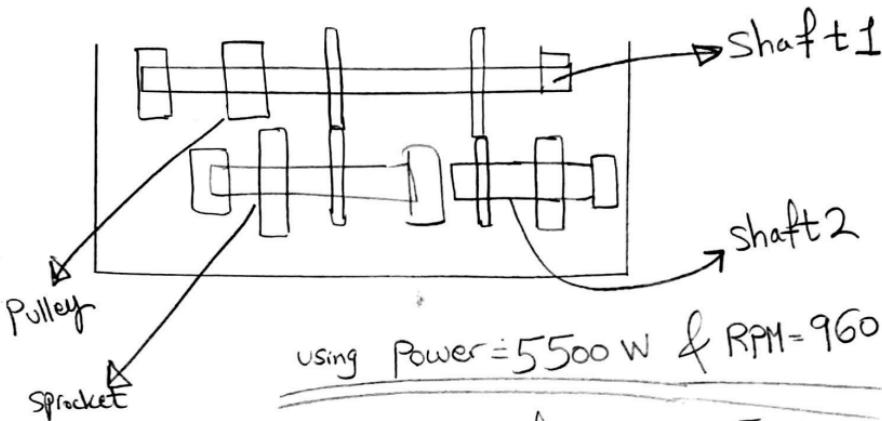
$$C_a = 125 \text{ N} < \frac{125}{2} \text{ N}$$

$$n = 324.2 \text{ rpm} < \frac{3600}{2} \text{ rpm}$$

Safe

(1)

Shaft Diameter
Calculated for
Gearbox on both
Velocities.



$$\frac{F_1}{F_2} = e^{\mu V}$$

* Diameter of Pinion = 500 mm
 * ① // Gear = 1000 mm

$$2\beta = (2 \times 17) = 34^\circ$$

$$\text{Assume } \mu = 0.4$$

$$\mu V = \frac{\mu}{\sin \beta} = \frac{0.4}{\sin(17)} = 1.368$$

$$\text{Assume wrap angle} = 160^\circ$$

$$\text{in rad, } \frac{160 \times \pi}{180} = 2.792 \text{ rad}$$

Substitute in ① ,

$$\frac{F_1}{F_2} = e^{1.368 \times 2.792} = 45.579$$

$$F_2 = \frac{F_1}{45.579}$$

$$H = (F_1 - F_2) V$$

$$5500 = \left(F_1 - \frac{F_1}{45.579} \right) \cdot wr$$

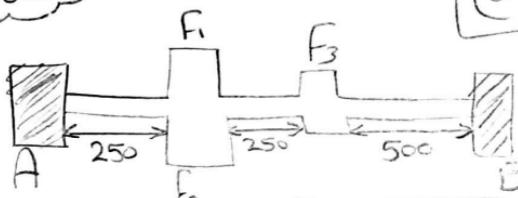
$$5500 = \left(F_1 - \frac{F_1}{45.579} \right) \cdot \left(\frac{2\pi \times 960}{60} * \frac{0.1}{2} \right)$$

$$F_1 = 1118.735 \text{ N} \quad , \quad F_2 = \frac{1118.735}{45.579} = 24.54 \text{ N}$$

Let shaft length = 1000 mm

Horizontal

@ $V = 0.7 \text{ m/s}$



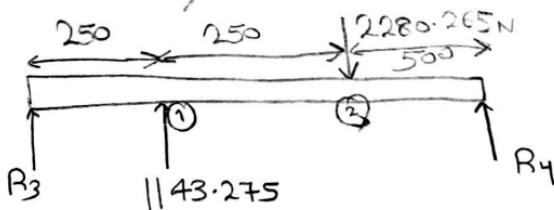
$$F_1 = 1118.735 \text{ N}$$

$$F_2 = 24.54 \text{ N} \quad , \quad F_3 = \frac{5500}{2.412} =$$

$$2280.265 \text{ N}$$

$$F_4 = (2280.265 \tan(20)) = 829.948 \text{ N}$$

For horizontal



$$\sum M @ R_4 = 0$$

$$(1000 \times R_3) + (1143.275 \times 750) - (2280.265 \times 500) = 0$$

$$R_3 = 282.67 \text{ N}$$

(3)

$$2 f_y = 0$$

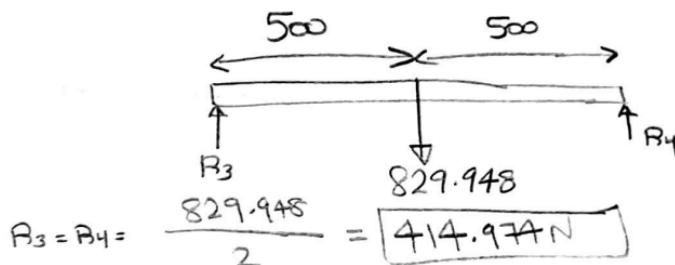
$$282.67 + 1143.275 - 2280.265 + R_4 = 0$$

$$R_4 = 854.32 \text{ N}$$

$$M_{b1} = (250 R_3) = (250 * 282.67) = 70667.5 \text{ Nmm}$$

$$M_{b2} = (500 R_4) = (500 * 854.32) = 427160 \text{ Nmm}$$

Vertical



$$M_{b2} = (500 * 414.974) = 207.487 \text{ Nm}$$

$$M_{b\max} = \sqrt{427.160^2 + 207.487^2} = 474.885 \text{ Nm}$$

$$\text{Torque} = \frac{\text{Power}}{\text{omega}} \rightarrow T = \frac{5500}{\frac{2\pi \times 60}{60}} = 82.064 \text{ Nm}$$

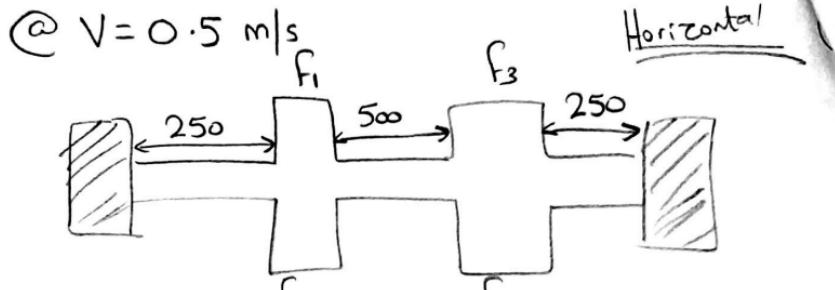
$$M_{t\max} = 82.064 \text{ Nm}$$

$$F_r \text{ on bearing A} = \sqrt{282.67^2 + 414.974^2} =$$

$$F_r \text{ on bearing B} =$$

$$502.101 \text{ N}$$

$$\sqrt{854.32^2 + 414.974^2} = 949.77 \text{ N}$$



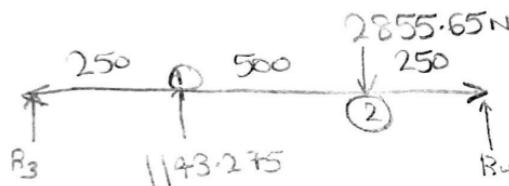
$$F_1 = 118.735 \text{ N}$$

$$F_2 = 24.54 \text{ N}$$

$$F_3 = \frac{5500}{1.926} = 2855.65 \text{ N}$$

$$F_4 = (2855.65 \tan(20)) = 1039.37 \text{ N}$$

Horizontal



$$\sum M_{R4} = 0$$

$$(1000R_3) + (1143.275 * 750) - (2855.65 * 250) = 0$$

$$R_3 = 143.54 \text{ N}$$

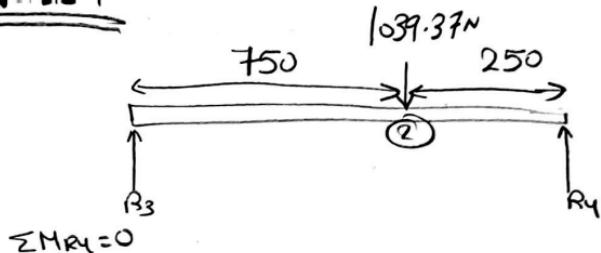
$$\sum F_y = 0$$

$$143.54 + 1143.275 + R_4 - 2855.65 = 0$$

$$R_4 = 1568.835 \text{ N}$$

$$M_{b1} = (0.25 * 143.54 * 750) = 35.885 \text{ Nm}$$

$$M_{b2} = (0.25 * 1568.835) = 392.208 \text{ Nm}$$



$$(\text{1000} * \text{R}_3) - (\text{1039.37} * \text{250}) = 0$$

$$\boxed{\text{R}_3 = 259.8425 \text{ N}}$$

$$\text{R}_4 = 259.8425 - 1039.37 = \boxed{779.527 \text{ N}}$$

$$M_{b2} = (0.2 * 779.527) = \boxed{155.9055 \text{ NM}}$$

$$M_{b\max} = \sqrt{392.208^2 + 155.9055^2} = \boxed{422.058 \text{ NM}}$$

$$M_E = \frac{H}{\omega} = \frac{5500}{214 + 642} = \boxed{82.064 \text{ NM}}$$

F_r on bearing A :

$$\sqrt{143.54^2 + 259.84^2} = \boxed{296.851 \text{ N}}$$

F_r on bearing₂:

$$\sqrt{779.527^2 + 1568.835^2} = \boxed{1751.82 \text{ N}}$$

Take the max moment = $\boxed{422.058 \text{ NM}}$

$$\boxed{M_E = 82.064 \text{ NM}}$$

$$S_y = 250 \text{ MPa}$$

$$T_g = 125 \text{ MPa}$$

$$T_{all} = 62.5 \text{ MPa}$$

$$n = 2$$

$$k = 0.6$$

$$k_b = 1.4$$

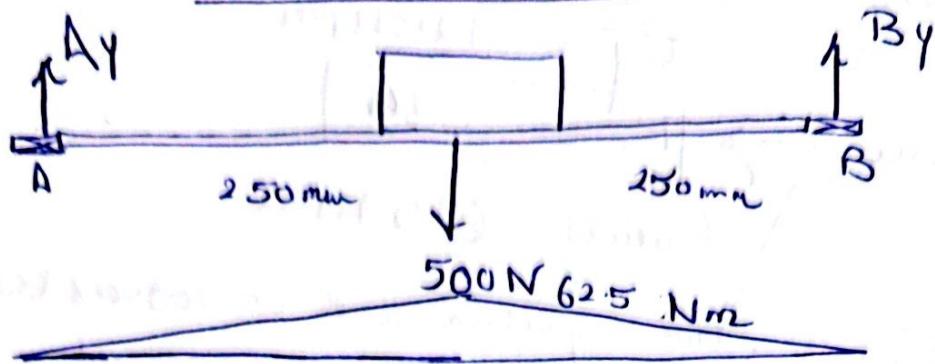
$$d_o^3 = \frac{16}{\pi * 62.5 * 10^6 (1 - 0.6^4)} *$$

$$\sqrt{(1.4 * 422.058)^2 + (1.3 * 82.064)} = 6.41 * 10^5$$

$$d_o = (ANS)^{1/3} = 0.04065 \text{ m}$$

$$d_o = 40.65 \text{ mm}$$

Shaft calculations



$$\sum M_A = 0$$

$$-500 \times 250 + B_y \times 500 = 0$$

$$\boxed{B_y = 250 \text{ N}}$$

$$\sum F_y = 0$$

$$A_y = 250 \text{ N}$$

N.B : in reality the shaft carried the 500N but we consider 500 N for safety

* for factor of safety $\sqrt{2}$

$$* w = \frac{2\pi \times 134}{60} = \frac{67}{15} \text{ rad s}^{-1}$$

$$* \boxed{5500 \text{ N} = H}$$

$$\rightarrow M_{t \max} = \frac{5500}{14 \cdot 63} \\ = 392 \text{ Nm}$$

$$* M_{lb} = 62.5 \text{ Nm}$$

$$* 2 = \boxed{125 \text{ Nm}}$$

* choose $\text{OQT} 1000 \rightarrow S_y = 1050 \text{ MPa}$

$$* \overline{t_y} = \frac{1050}{2} = 525 \text{ MPa}$$

* assume $K = 0.5$ $\overline{t_{\text{allow}}} = \frac{525}{2} = 262.5$
choose ST50 $\rightarrow S_y = 550 \text{ MPa}$, $t_y = 125 \text{ MPa}$, $t_{\text{allow}} = 62.5 \text{ MPa}$ (failed) MPa

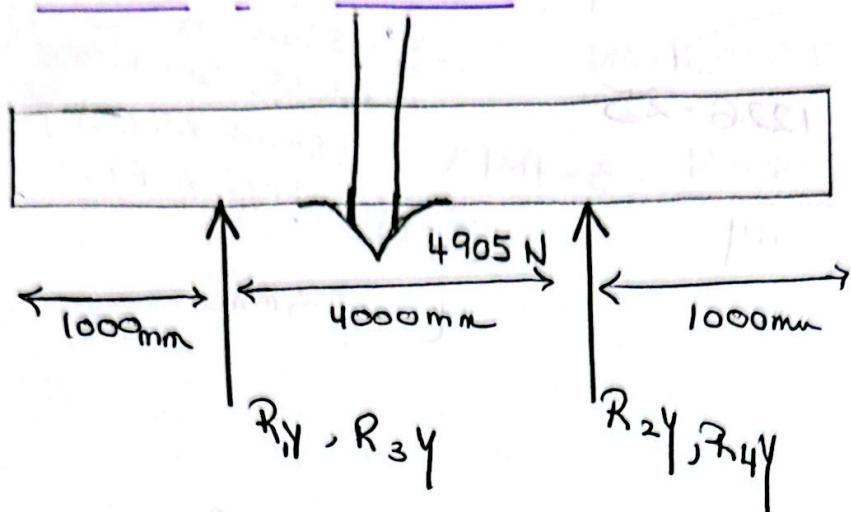
$$* d_o^3 = \frac{16}{\pi * \frac{(1 - 0.5^4) * 10^6}{62.5 \text{ or } 62.5 \text{ OQT} 1000}} t$$
$$= \sqrt{(3 * (\frac{125}{349})^2 + (3 * 392)^2)}$$

Material used

* $d_o = 0.05 \text{ m} * 1000 = 50 \text{ mm}$ for ST50
choose 45mm Standardized cross section or
press fit 50mm shaft in the roller

$$* d_i = 25 \text{ mm}$$

* frame calculations



* assuming no distances between the boxes

→ the total number of boxes is 20

→ weight = $20 * 25 = 500 \text{ kg} * 9.81 = 4905 \text{ N}$
(weight is distributed between 4 table legs)

$$\Rightarrow \sum M_{R_{2y}, R_{4y}} = 0 \quad * R_{1y} = R_{3y}$$

$$* R_{2y} = R_{4y}$$

$$-2R_{1y} * 4000 + 4905 * 2000 = 0$$

$$R_{1y} = 1226.25 \text{ N}$$

$$\sum F_y = 0$$

$$2 * 1226.25 - 4905 + 2 * R_{2y} = 0$$

$$R_{2y} = 1226.25 \text{ N}$$

assuming

$$FOS = 2$$

$$\Rightarrow T. \text{Force} = 4905 \text{ N} \rightarrow \text{Force @ 1 leg} = 1226.25 \text{ N}$$

$$F = 1226.25 \times 2.5 = 3100 \text{ N}$$

$$\sigma = \frac{3100 \text{ N}}{914} = 3.4 \text{ MPa}$$

→ assume a rectangular hollow cross section (standardized) $\rightarrow A = 914 \text{ mm}^2$

$$D \times B = 100 \text{ mm} \times 60 \text{ mm}$$

$$t = 3 \text{ mm}$$

$$F \cdot S = 2$$

$$p_{\text{eff}} = p_A - p_B$$

$$2 = \frac{S_{ut}}{3.4} \Rightarrow S_{ut} = 6.8 \text{ MPa}$$

(iteration failed)

assume the material to be used (Hot rolled 1020 Carbon Steel with $S_{ut} = 379 \text{ MPa}$)

$$2 = \frac{379}{\sigma}$$

$$\sigma = 190 \text{ MPa}$$

$$190 = \frac{3100 \text{ N}}{A}$$

$$A = 16.3 \text{ mm}^2 \rightarrow \text{nearest standardized cross-section}$$

is 12 mm \times 12 mm Square

$$\Rightarrow \sigma = \frac{3100}{42} = 74 \text{ MPa}$$

hollow cross section with thickness \square

$$n = 379 / 74 = 5$$

\Rightarrow Suitable to handle bending