

# LINEAR MODELS PROJECT REPORT

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## \* Objective

In this project, our aim was to take several screenshots that share some common locations and stitch them into a whole map.

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In this project, I took several screenshots of satellite images from Google Maps of the area in Bangalore and stitched them into a whole map. However, the code that I used for this, works fine for any and every area on Google Maps.

## \* Methodology

### Model

Suppose, I have  $m$  screenshots and  $n$  distinct places to locate on the map. I stored the screenshot number (as  $ss$  variable), the name of the place (as  $place$  variable) and the co-ordinates of the place with respect to that screenshot. I fitted linear model for predicting the x-ordinate and the y-ordinate separately. For the y-ordinate the model is,

$$y_{ij} = ss_i + place_j + \epsilon_{ij} \text{ where } i = 1, \dots, m; j = 1, \dots, n_i \text{ and } \epsilon_{ij} \stackrel{IID}{\sim} N(0, \sigma^2)$$

Note that both the inputs are factor. This is a 2-way ANOVA model. We have only two indices  $(i, j)$  as for each type  $(i, j)$  we have only one observation. Similarly for the x-ordinate the model is,

$$x_{ij} = ss_i + place_j + \epsilon_{ij} \text{ where } i = 1, \dots, m; j = 1, \dots, n_i \text{ and } \epsilon_{ij} \stackrel{IID}{\sim} N(0, \sigma^2)$$

### Design Matrix

Number of columns in design matrix is  $m + n$ . Number of rows in design matrix = Total number of clicks =  $C$  (let). the dimension of the design matrix is = (number of clicks  $\times$  (number of distinct place + number of screenshots)) =  $C \times (m + n)$

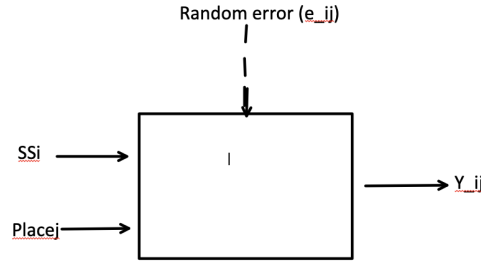


Figure 1: Blackbox diagram

## Rank of the design matrix

**Claim:** The map formed by the screenshots is connected iff  $\text{rank}(\text{design matrix}) = m+n-1$ .

**Proof:** To understand the idea, consider the screenshots as vertices of a graph and draw an edge between them if they have at least one marked place common. We know if a graph is connected there exists at least  $(m-1)$  many edges.

If  $\text{place}(j)$  is common in  $k$  many of the screenshots, there exist at least  $k - 1$  many edges in the graph. Hence total number of edges in the graph is  $\sum_j^n (k(j) - 1) = C - n$  where  $k(j)$  = number of times  $\text{place}(j)$  has occurred.

Now, for the columns, if we add all the columns corresponding to place variable we get a vector of 1's. Similarly adding up all the columns w.r.t. ss variable we get a vector of 1's. All the ss variables are independent of each other and all the place variables are independent of each other. Hence, column rank of the design matrix =  $m+n-1$ .

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## \* Documentation for R codes and outputs