AI algorithms: Constraint Backtracking

(Chronological) Backtracking
Backjumping
Backmarking
Intelligent Backtracking
Dynamic Search Rearrangement

Input:
A constraint network with n variables v_i and constraints $c(v_i, v_j)$
A set of possible assignments $a_{i,k}$ for each variable v_i
A variable $jumpback$ (init 1) and array $checkdepth$
A matrix $checkdepth$ and array $backup$
A set NG of no-goods
Output:
An assignment $a_{i,k}$ for each variable v_i where all constraints $c(v_i, v_j)$ are respected
Algorithm $(depth, jumpback, checkdepth, backup)$:

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for all a_{depth,k} (ordered according to a fail-first heuristic) do
  if checkdepth_{depth,k} ≥ backup_{depth} then
    v_{depth} ← a_{depth,k}
    if current assignment is covered by a no-good then
      return (backtrack)
    end if
    checkdepth_{depth,k} ← 1
    for all c(v_i, v_{depth}), backup_{depth} ≤ i < depth do
      if c(v_i, v_{depth}) holds then
        checkdepth_{depth,k} ← checkdepth_{depth,k} + 1
      end if
    end for
    if checkdepth_{depth,k} = depth then
      if depth = n then
        return solution (v_1,...,v_n)
      end if
      recurse(depth + 1, jumpback, checkdepth, backup)
      if jumpback < depth then
        return (backtrack)
      end if
    end if
  end if
end for
jumpback ← max_k(checkdepth_k)
for depth ≤ i ≤ n do
  backup_i ← depth − 1
end for
if no assignment a_{depth,k} was possible then
  Deduce no-goods and add to NG
end if
```