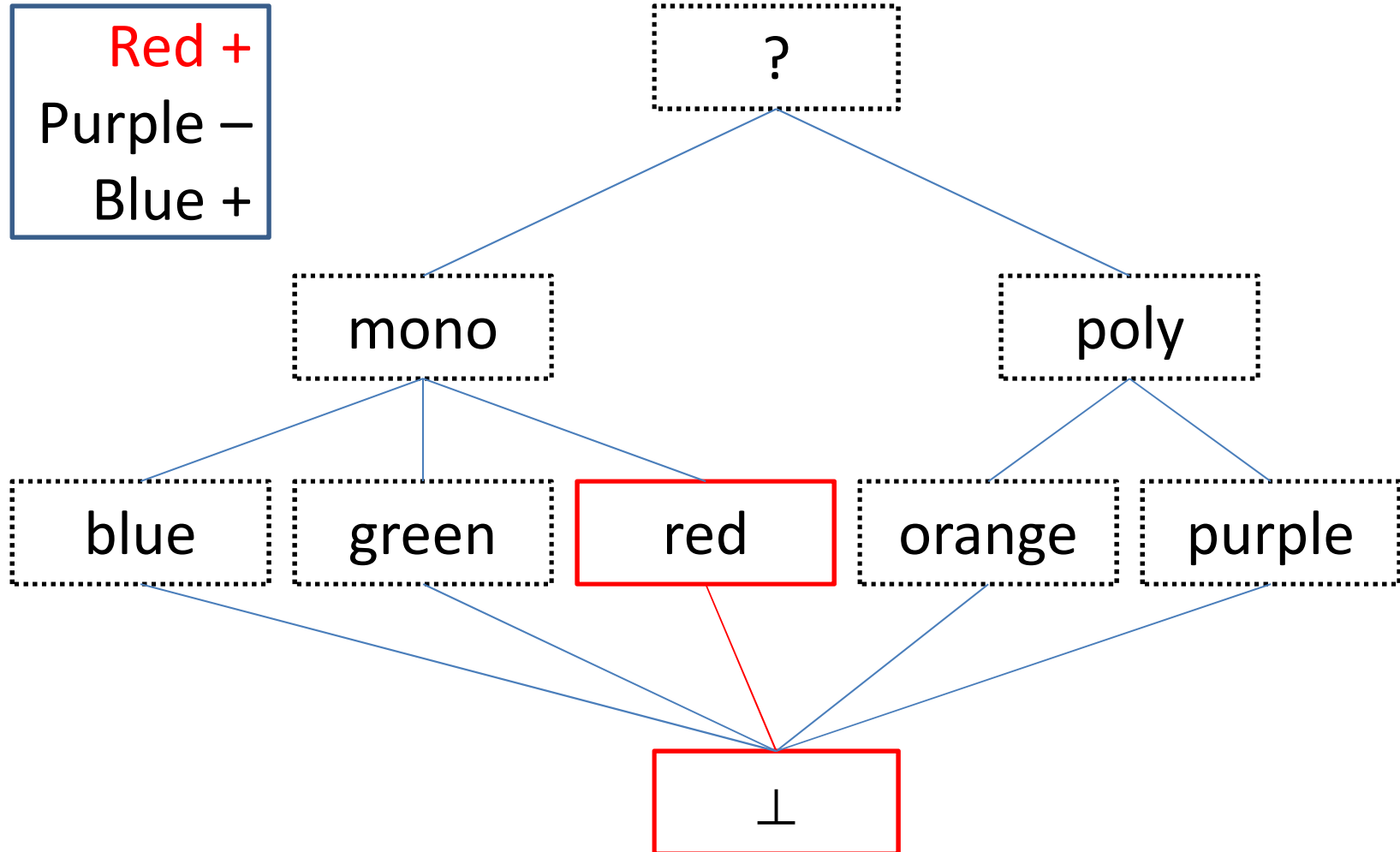


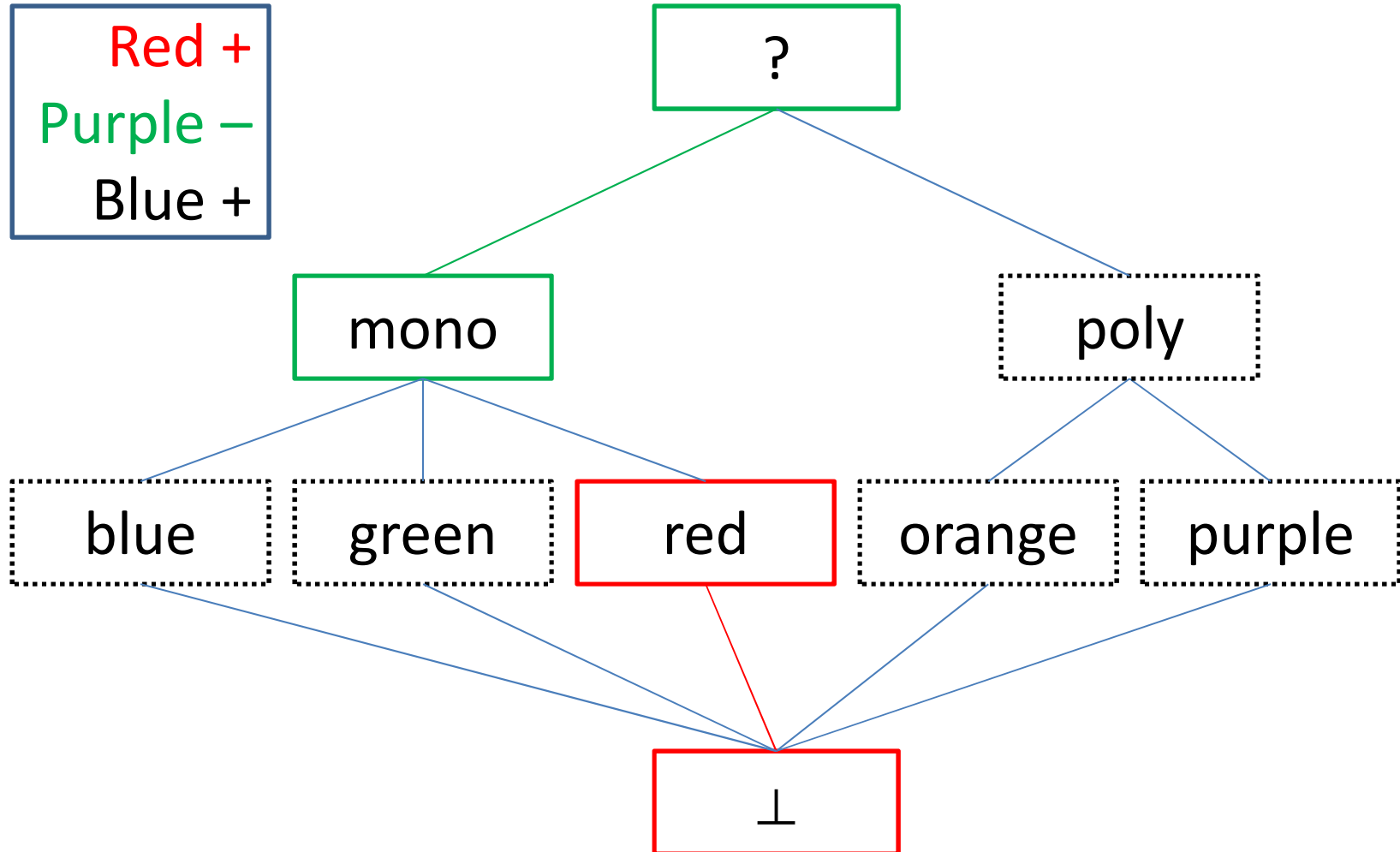
Exercises: Artificial Intelligence

Version Spaces: Colors

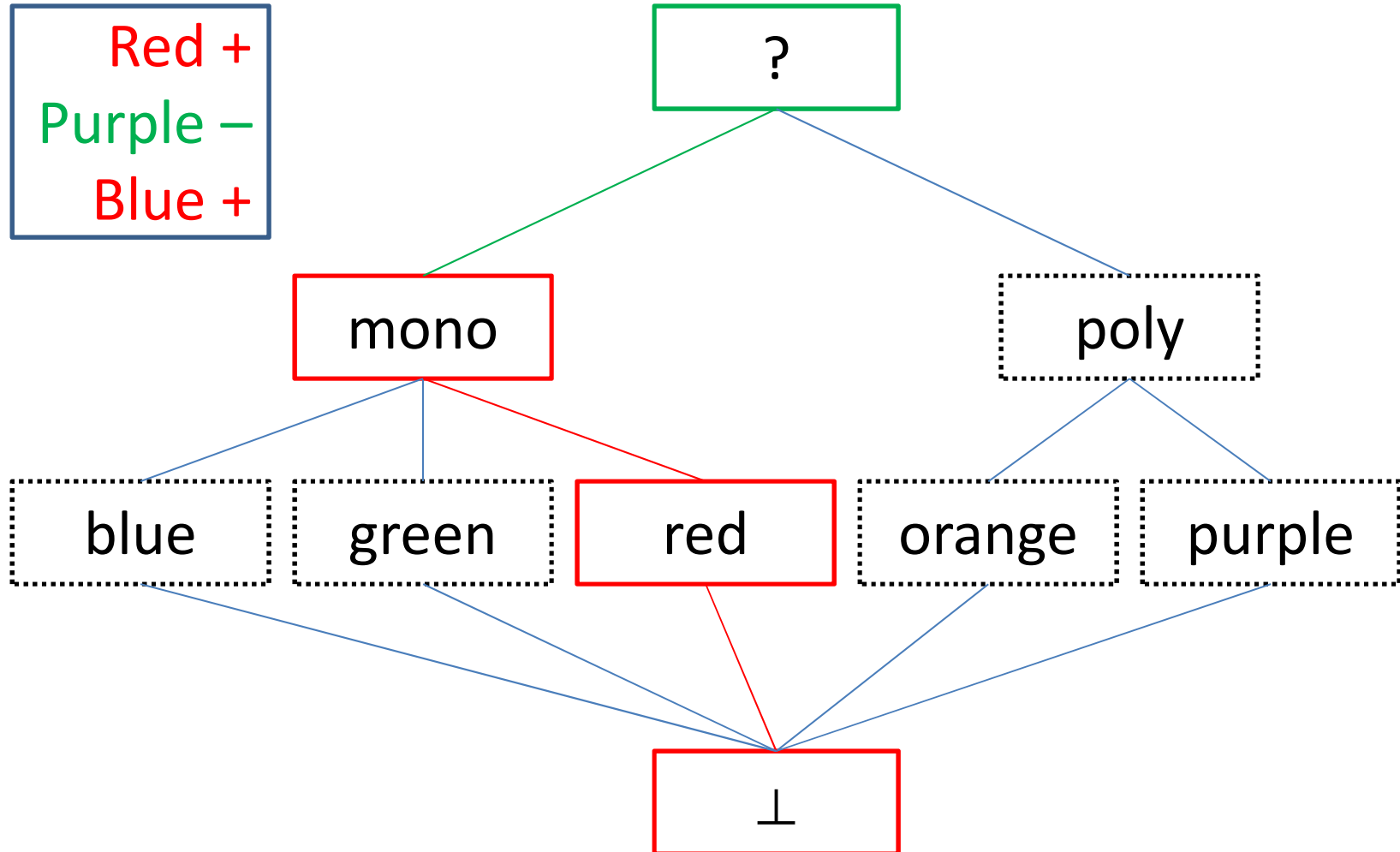
Version-Spaces Algorithm



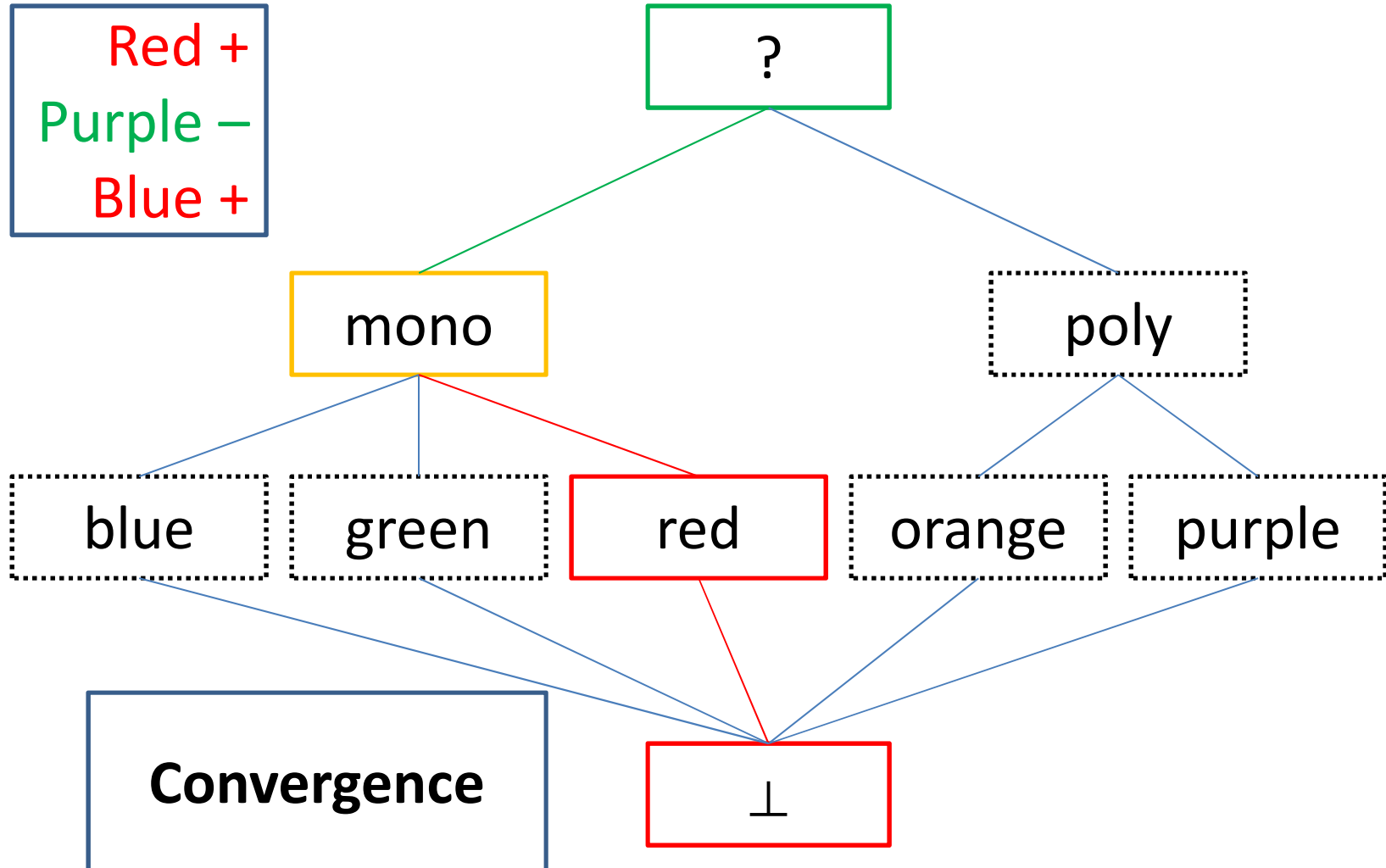
Version-Spaces Algorithm



Version-Spaces Algorithm



Version-Spaces Algorithm



Exercises: Artificial Intelligence

Version Spaces: Playing Cards

Version-Spaces Algorithm

[7,D] +

[A,C] -

[Q,H] -

[9,H] +

[8,C] -

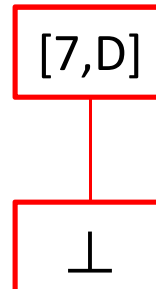
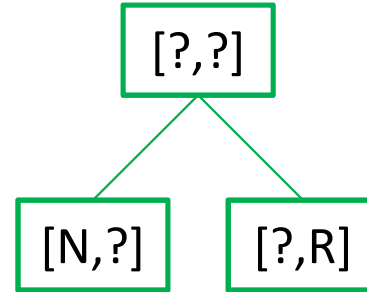
[?,?]

[7,D]

⊥

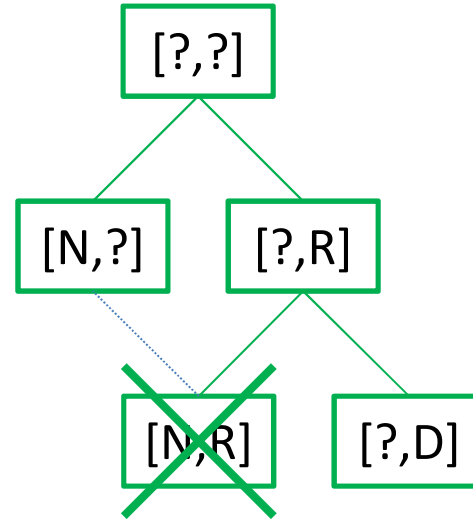
Version-Spaces Algorithm

[7,D] +
[A,C] -
[Q,H] -
[9,H] +
[8,C] -

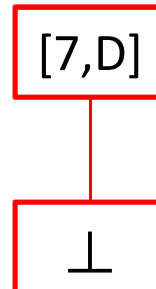


Version-Spaces Algorithm

[7,D] +
[A,C] -
[Q,H] -
[9,H] +
[8,C] -

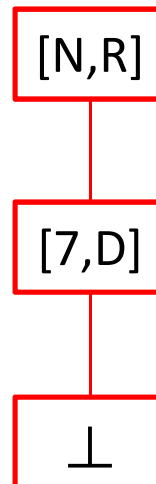
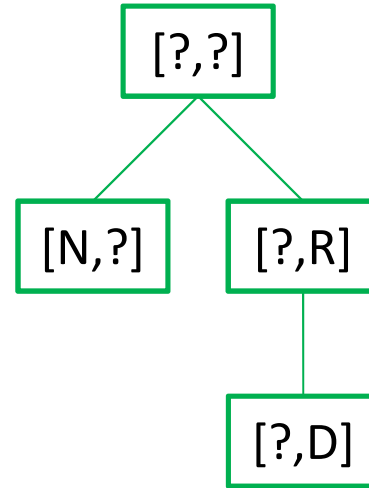


**Redundant
Hypotheses**



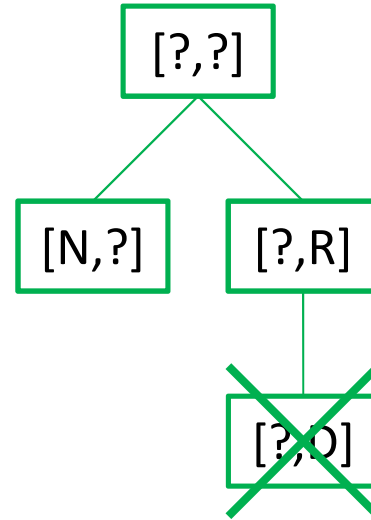
Version-Spaces Algorithm

[7,D] +
[A,C] -
[Q,H] -
[9,H] +
[8,C] -

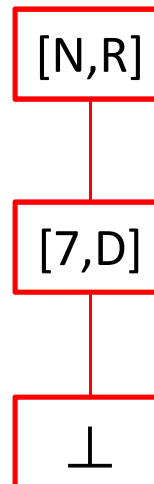


Version-Spaces Algorithm

[7,D] +
[A,C] -
[Q,H] -
[9,H] +
[8,C] -



**does not cover
last positive
example**



Version-Spaces Algorithm

[7,D] +
[A,C] −
[Q,H] −
[9,H] +
[8,C] −

[?,?]

[N,?]

[N,R]

[N,R]

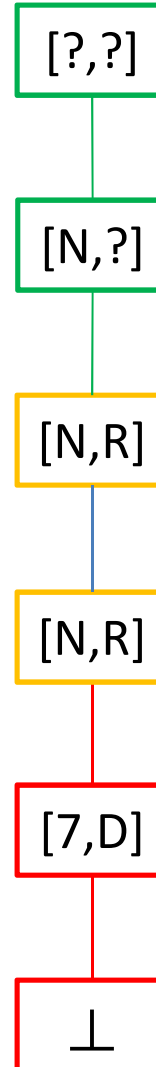
[7,D]

⊥

Version-Spaces Algorithm

$[7,D] +$
 $[A,C] -$
 $[Q,H] -$
 $[9,H] +$
 $[8,C] -$

Convergence



Exercises: Artificial Intelligence

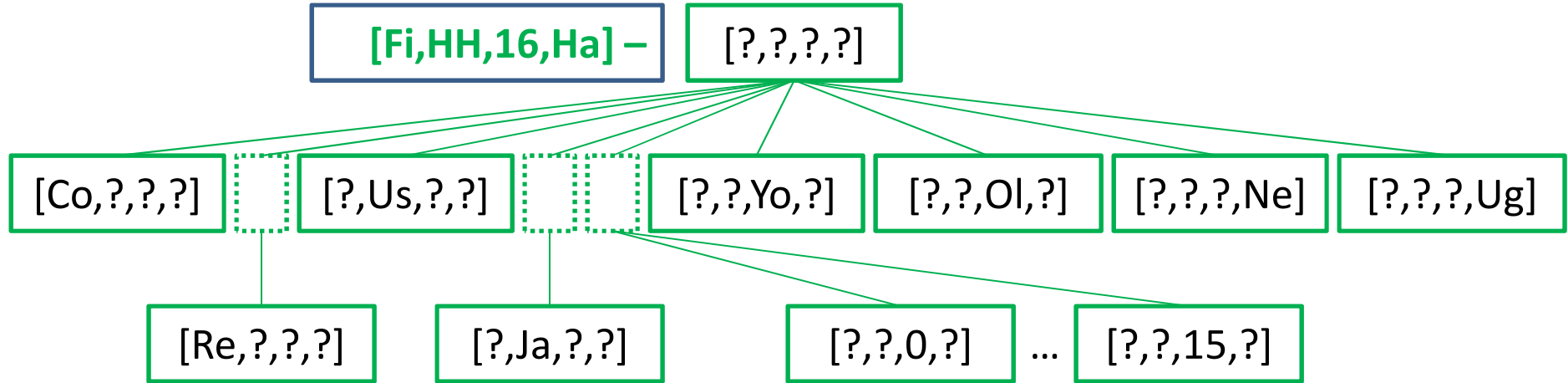
Version Spaces: Ex-exam

Version-Spaces Algorithm

[?,?,?,?]

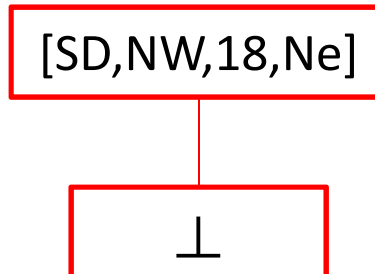
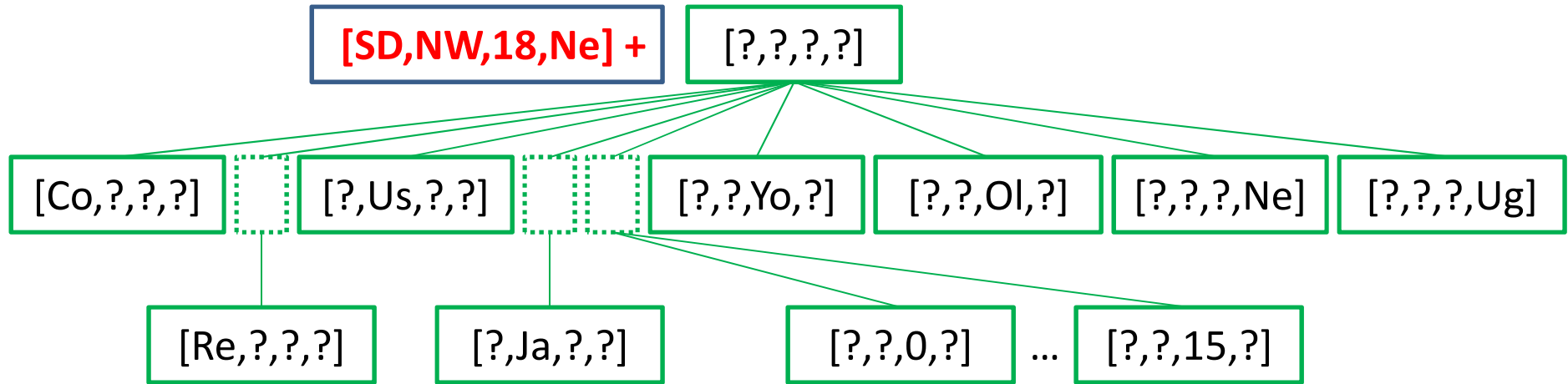
\perp

Version-Spaces Algorithm

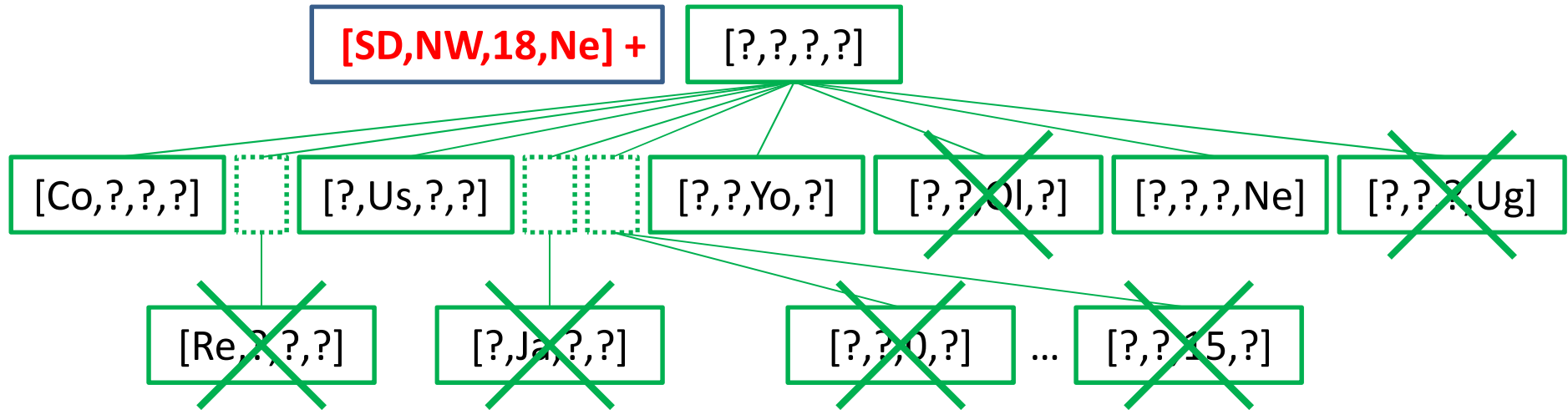


\perp

Version-Spaces Algorithm



Version-Spaces Algorithm

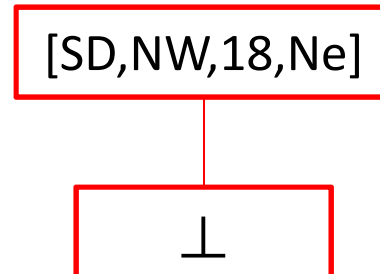
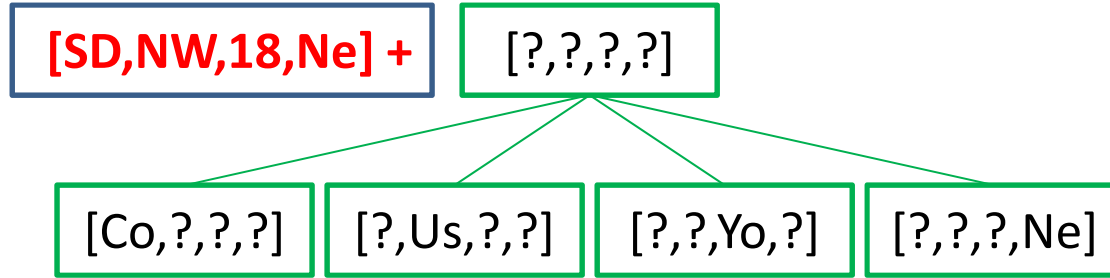


**19 out of 23 do
not cover last
positive example**

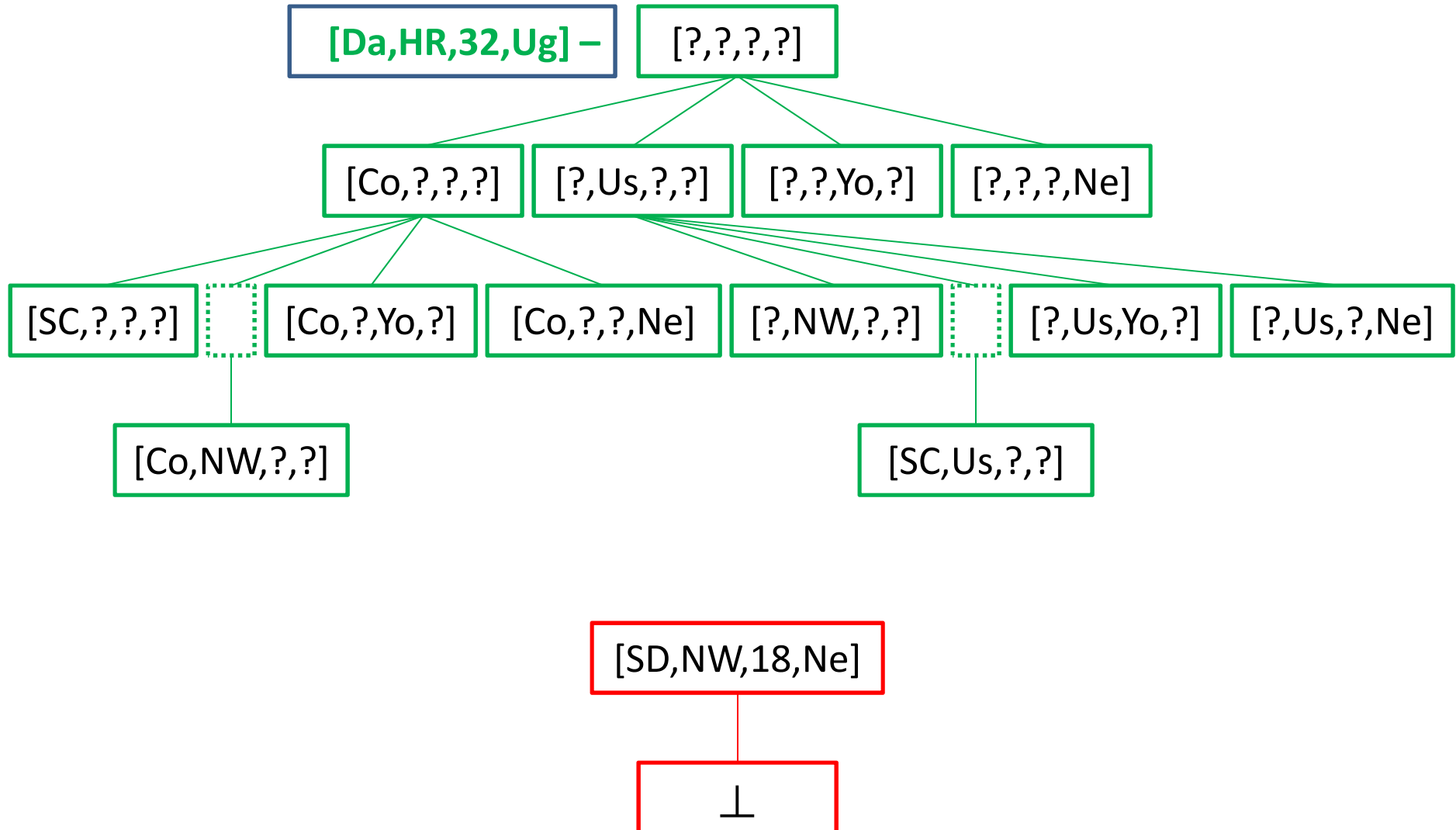
[SD,NW,18,Ne]

⊥

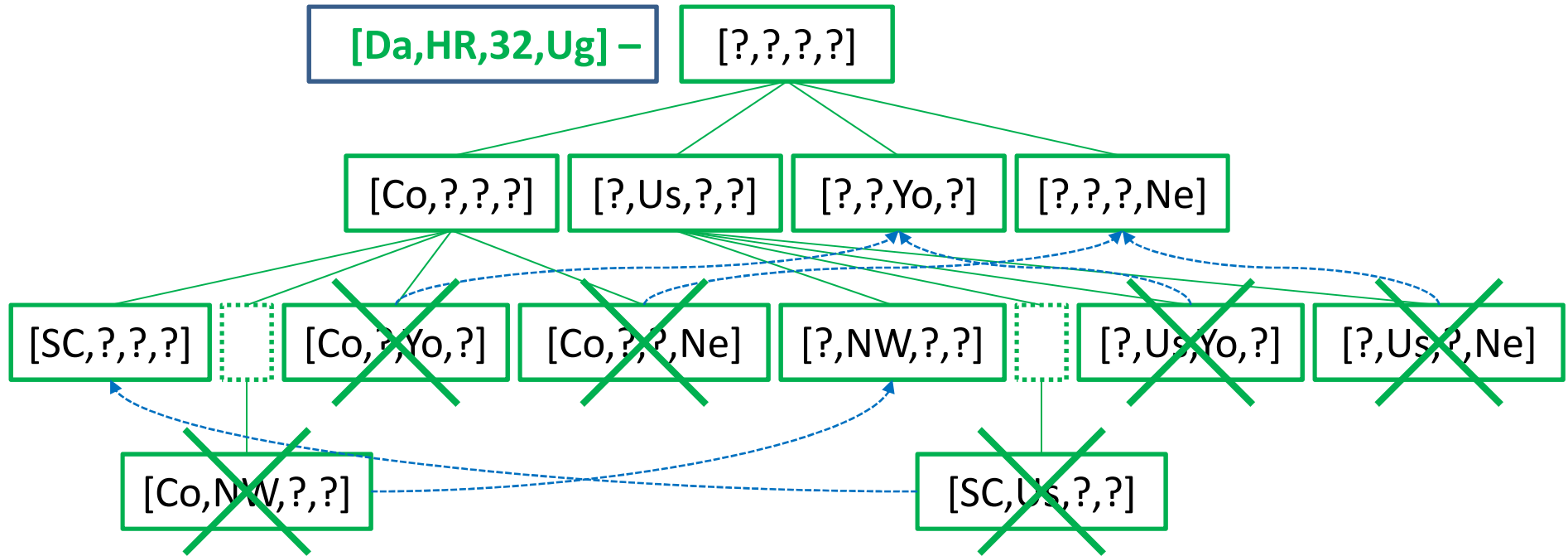
Version-Spaces Algorithm



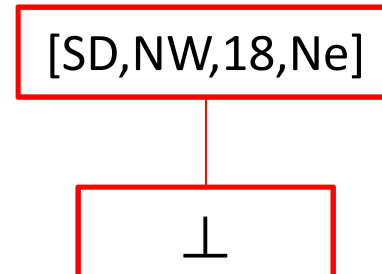
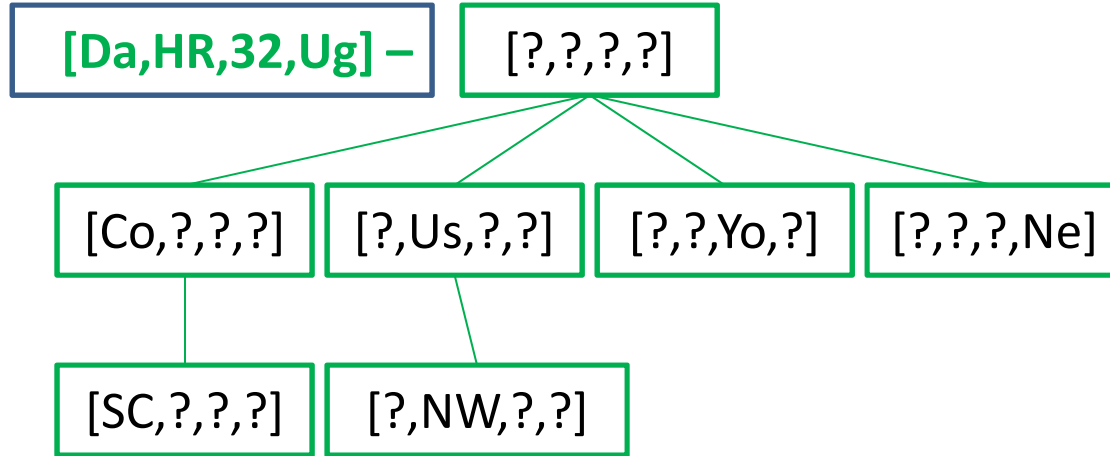
Version-Spaces Algorithm



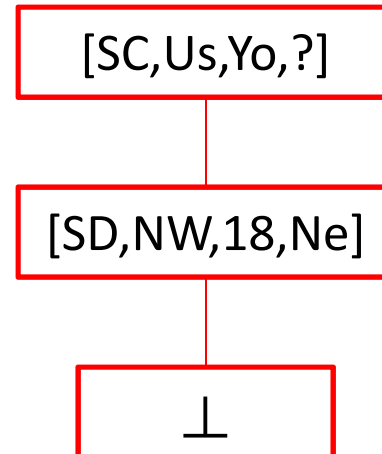
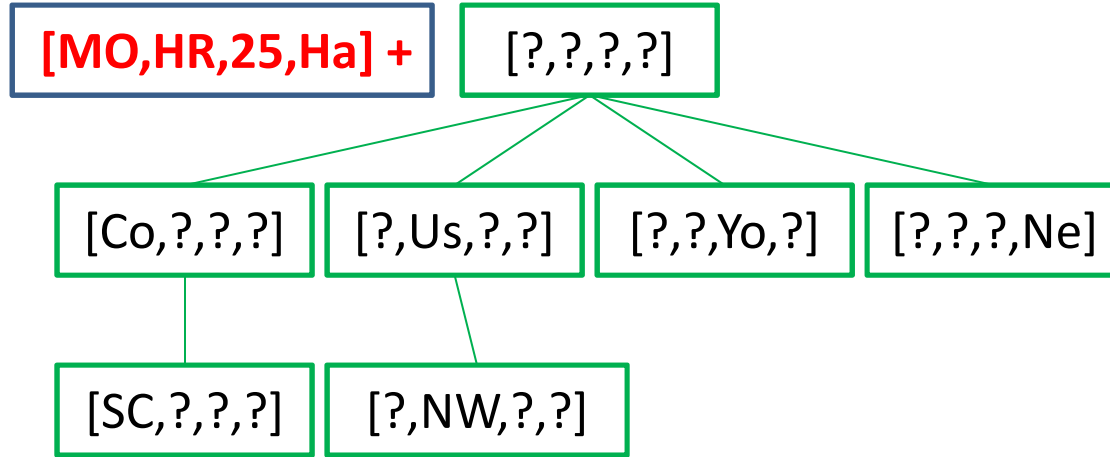
Version-Spaces Algorithm



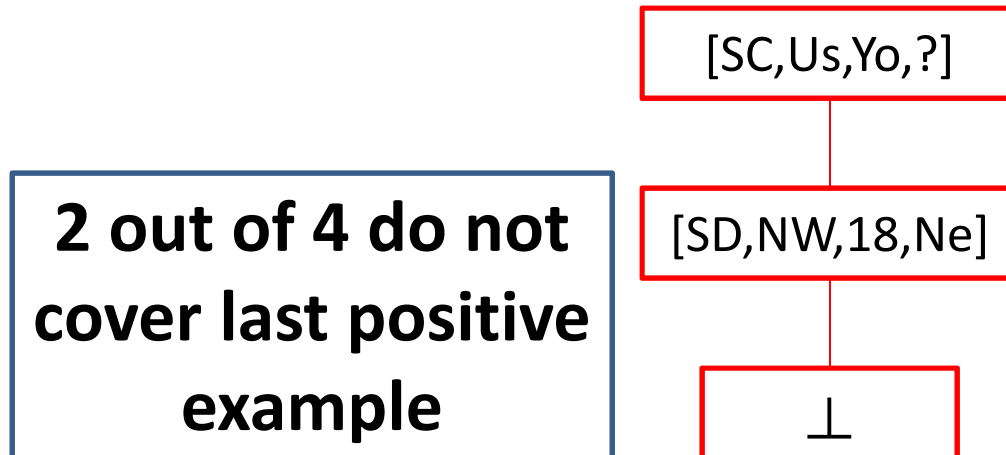
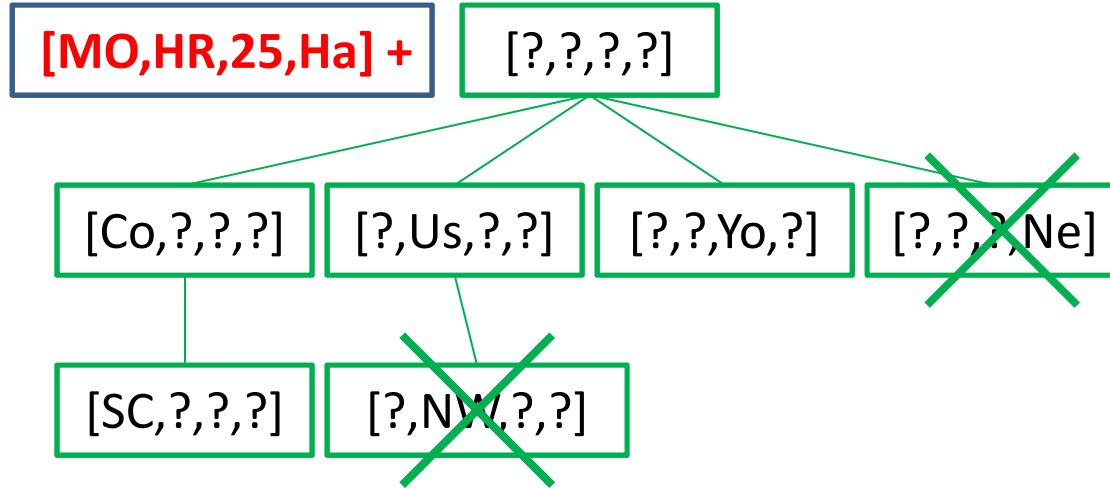
Version-Spaces Algorithm



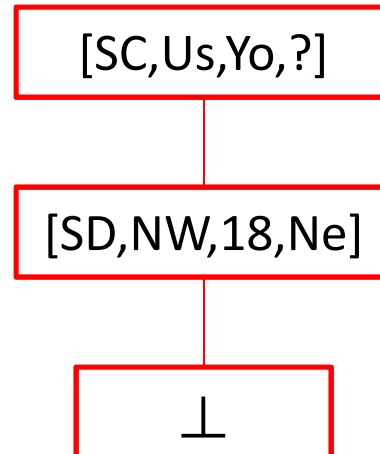
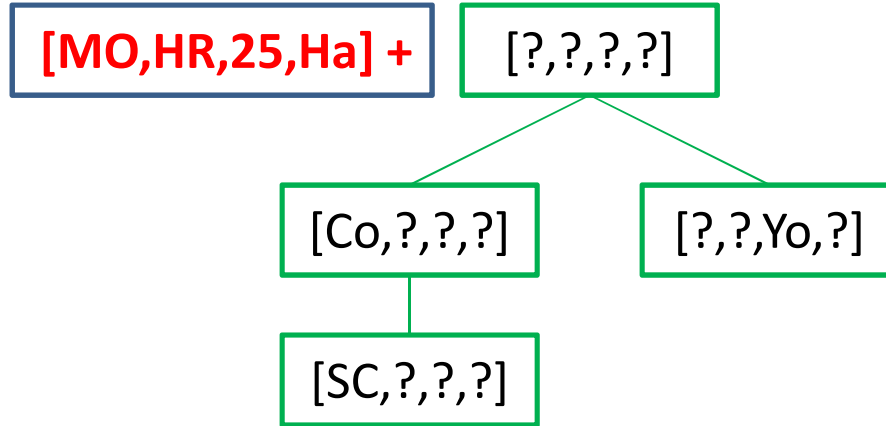
Version-Spaces Algorithm



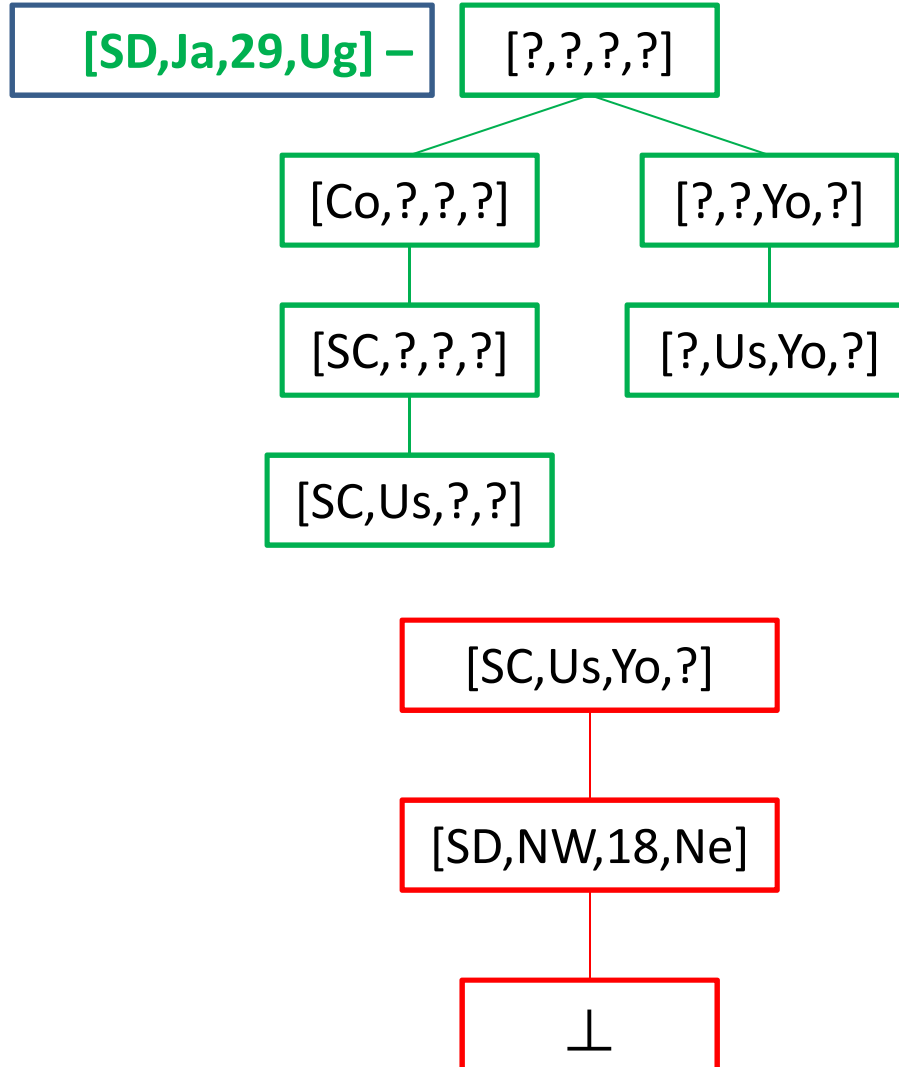
Version-Spaces Algorithm



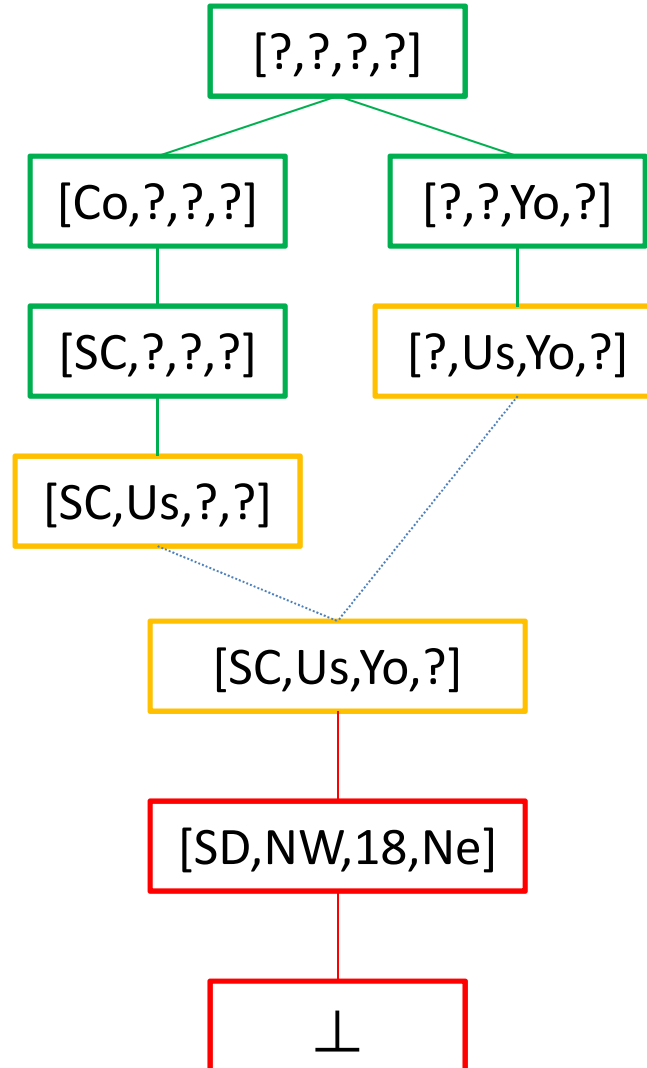
Version-Spaces Algorithm



Version-Spaces Algorithm

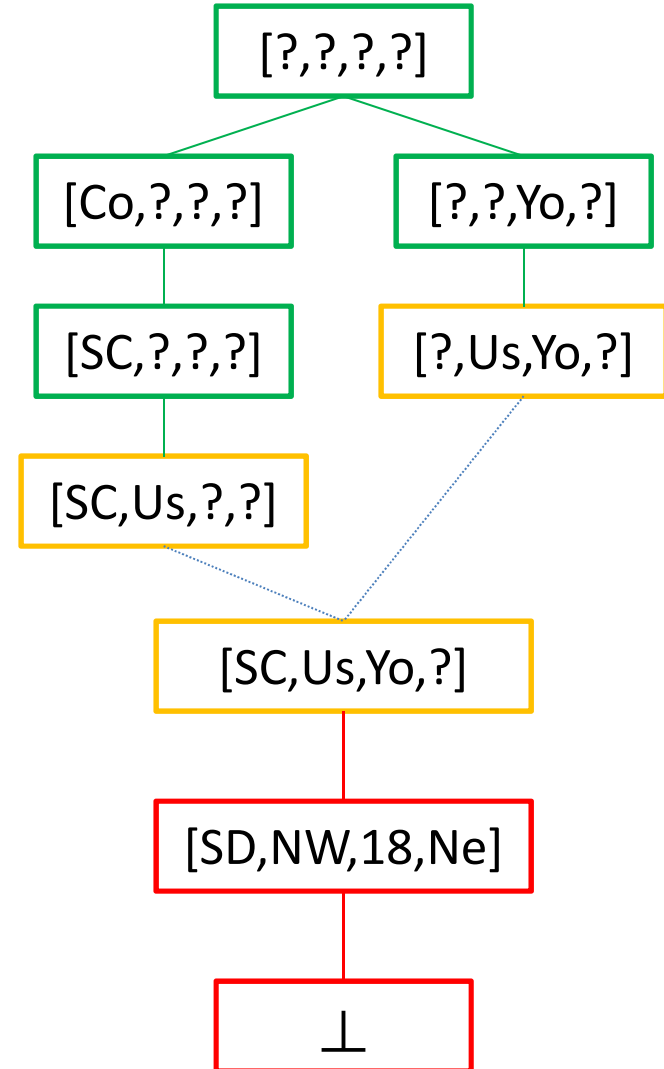


Version-Spaces Algorithm



Using the result

- [MO,HR,32,Ha]: **Maybe**
 - More Specific than [SC,Us,?,?]
 - Not more Specific than [SC,Us,Yo,?]
- [SD,HH,18,Ne]: **NO**
 - Not More Specific than [SC,Us,?,?]
 - Not More Specific than [?,Us,Yo,?]
- [Da,NW,22,Ug]: **Maybe**
 - More Specific than [?,Us,Yo,?]
 - Not more Specific than [SC,Us,Yo,?]



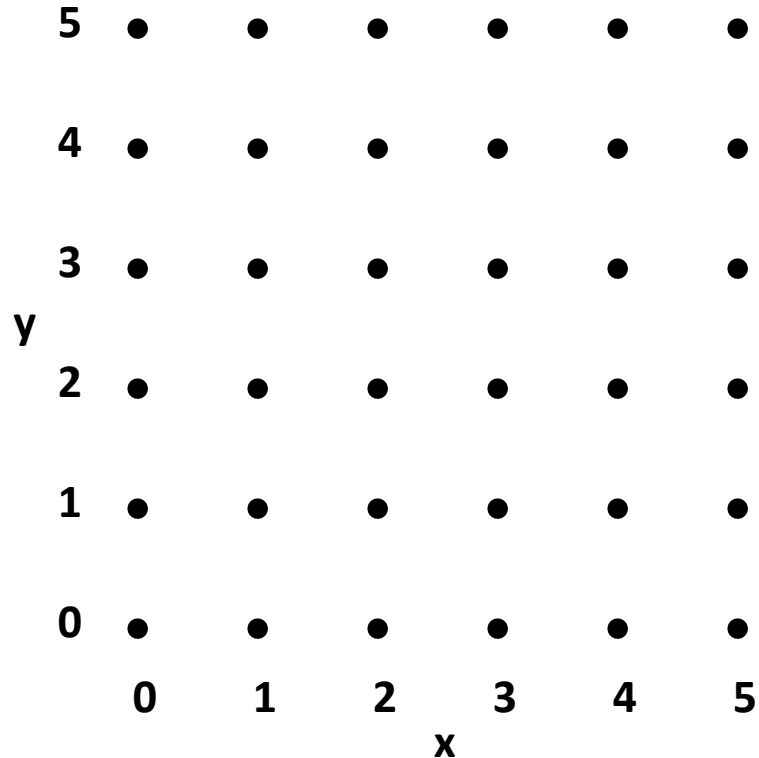
Exercises: Artificial Intelligence

Version Spaces: Computer Screen

Version-Spaces Algorithm

$G = \{[((0,0),5),\text{white}]\}$

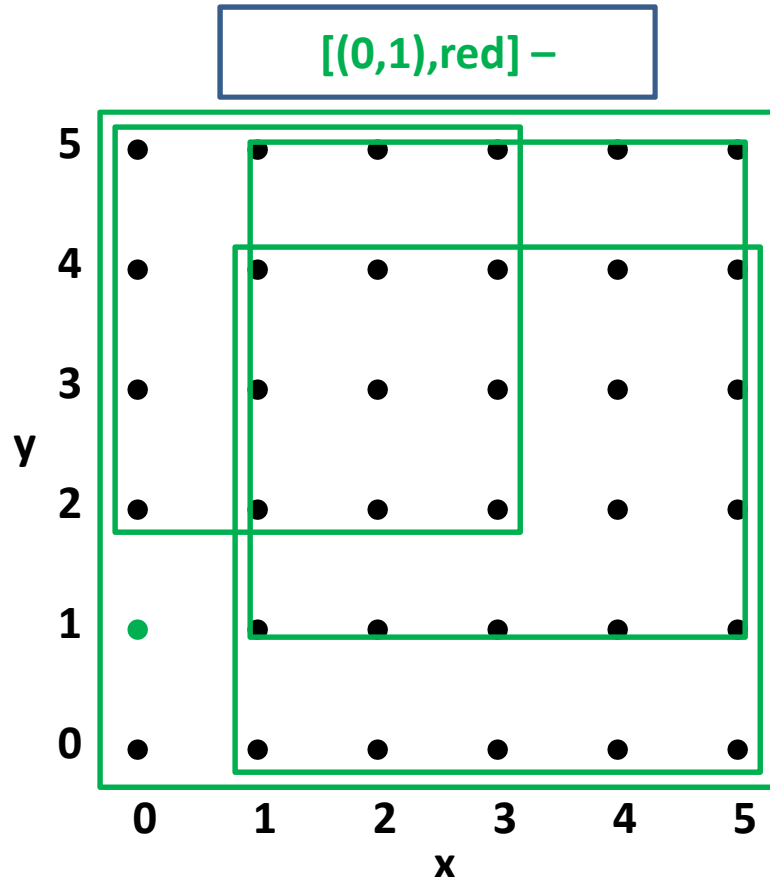
$S = \{\perp\}$



Version-Spaces Algorithm

$G = \{(((0,0),5),\text{white})\}$

$S = \{\perp\}$



$G = \{$

$(((0,2),3),\text{white}),$
 $(((1,0),4),\text{white}),$
 $(((1,1),4),\text{white}),$
 $(((0,0),5),\text{cyan})$

$\}$

Redundant:

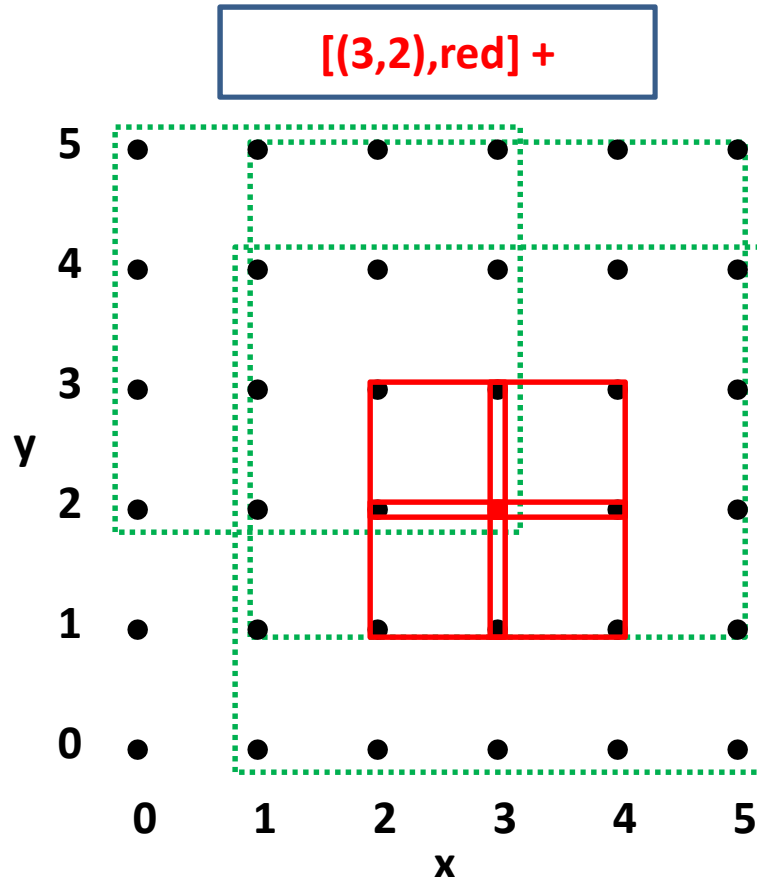
$(((0,0),5),\text{green})$
 $(((0,0),5),\text{blue})$

$S = \{\perp\}$

Version-Spaces Algorithm

$G = \{ [((0,2),3),\text{white}], [((1,0),4),\text{white}], [((1,1),4),\text{white}], [((0,0),5),\text{cyan}] \}$

$S = \{\perp\}$



$G = \{$

$[((0,2),3),\text{white}],$
 $[((1,0),4),\text{white}],$
 $[((1,1),4),\text{white}]$

$\}$

Removed:

$[((0,0),5),\text{cyan}]$

$S = \{$

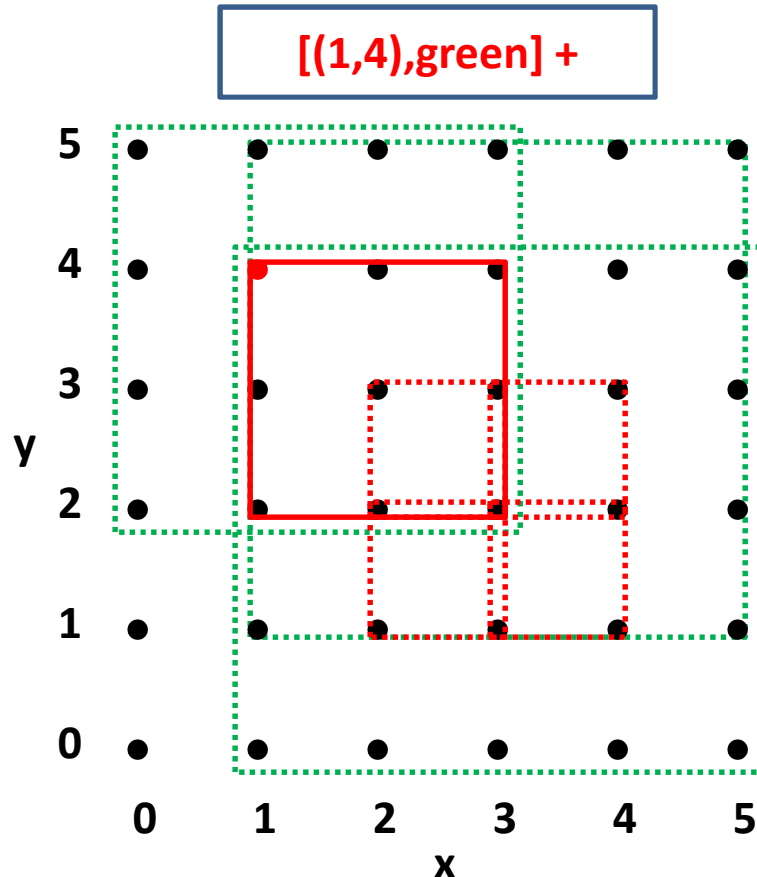
$[((2,1),1),\text{red}],$
 $[((2,2),1),\text{red}],$
 $[((3,1),1),\text{red}],$
 $[((3,2),1),\text{red}]$

$\}$

Version-Spaces Algorithm

$G = \{ [((0,2),3),\text{white}], [((1,0),4),\text{white}], [((1,1),4),\text{white}] \}$

$S = \{ [((2,1),1),\text{red}], [((2,2),1),\text{red}], [((3,1),1),\text{red}], [((3,2),1),\text{red}] \}$



$G = \{$

$[((0,2),3),\text{white}],$
 $[((1,0),4),\text{white}],$
 $[((1,1),4),\text{white}]$

$\}$

$S = \{$

$[((1,2),2),\text{yellow}]$

$\}$

Redundant:

$[((0,2),3),\text{yellow}]$

$[((1,2),3),\text{yellow}]$

$[((1,1),3),\text{yellow}]$

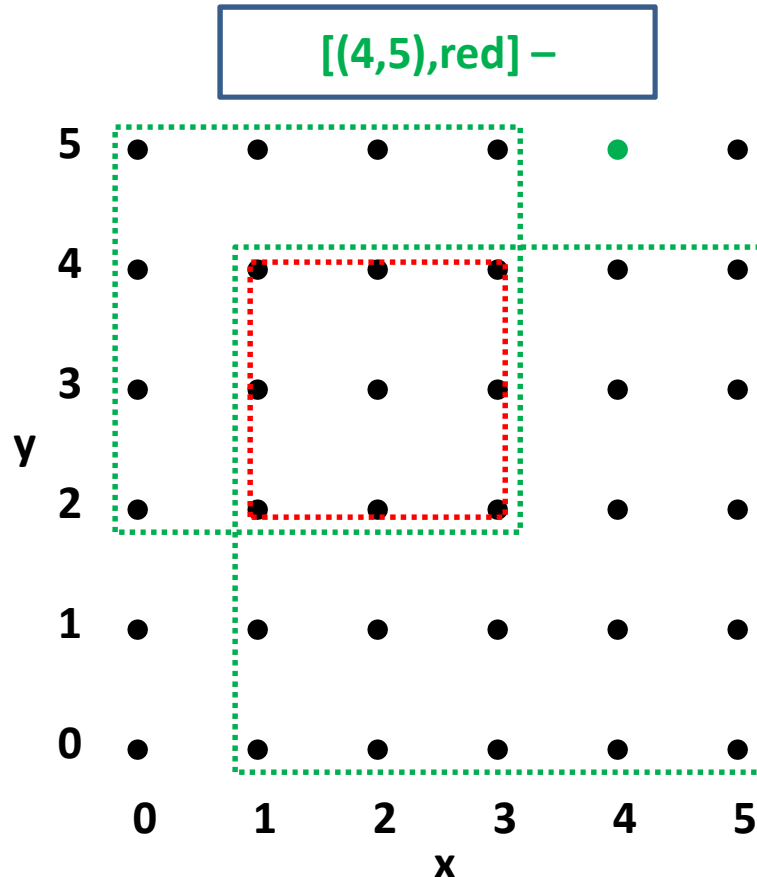
$[((1,1),4),\text{yellow}]$

$[((1,0),4),\text{yellow}]$

Version-Spaces Algorithm

$G = \{ [((0,2),3),\text{white}], [((1,0),4),\text{white}], [((1,1),4),\text{white}] \}$

$S = \{ [((1,2),2),\text{yellow}] \}$



$G = \{$
 $\quad [((0,2),3),\text{white}],$
 $\quad [((1,0),4),\text{white}]$
 $\}$

Redundant:

$[((1,1),3),\text{white}]$

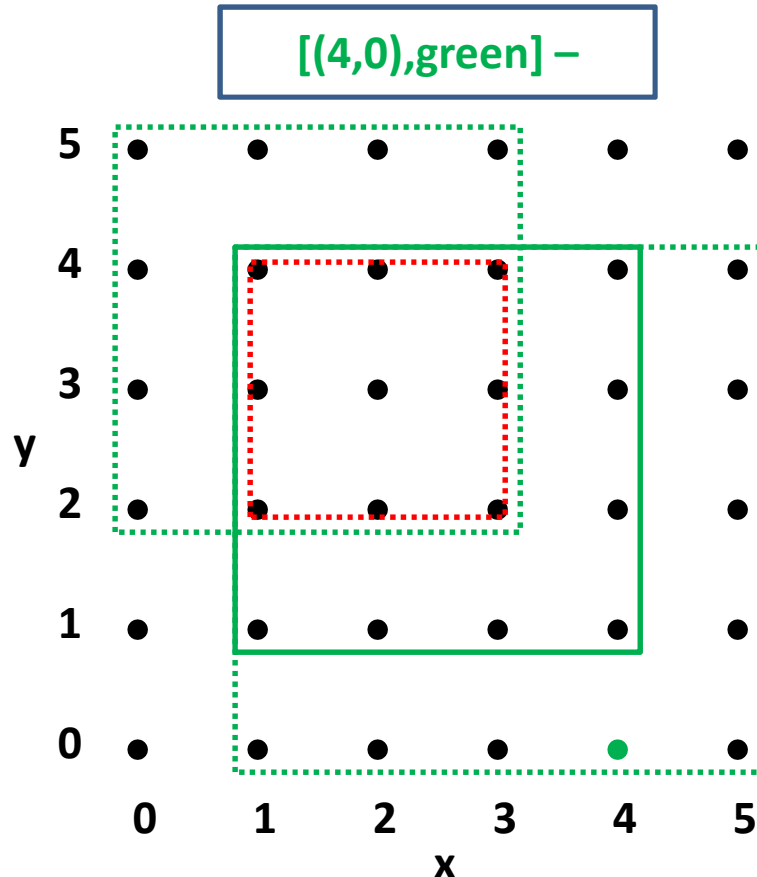
Others don't generalize S

$S = \{$
 $\quad [((1,2),2),\text{yellow}]$
 $\}$

Version-Spaces Algorithm

$G = \{ [((0,2),3),\text{white}], [((1,0),4),\text{white}] \}$

$S = \{ [((1,2),2),\text{yellow}] \}$

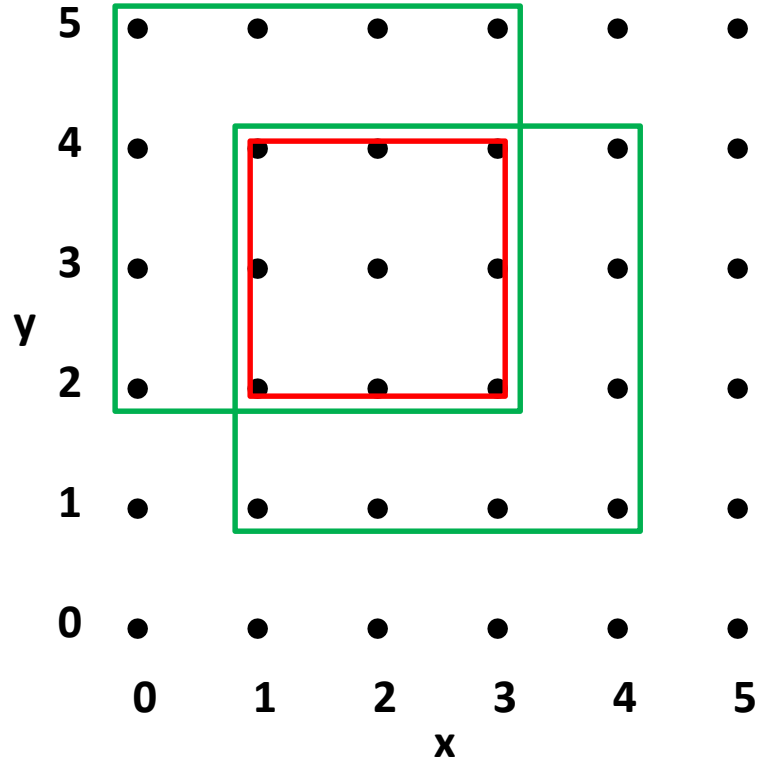


$G = \{$
 $[((0,2),3),\text{white}],$
 $[((1,1),3),\text{white}]$
 $\}$
Others don't generalize S
 $S = \{$
 $[((1,2),2),\text{yellow}]$
 $\}$

Version-Spaces Algorithm

$G = \{[((0,2),3),\text{white}],[((1,1),3),\text{white}]]\}$

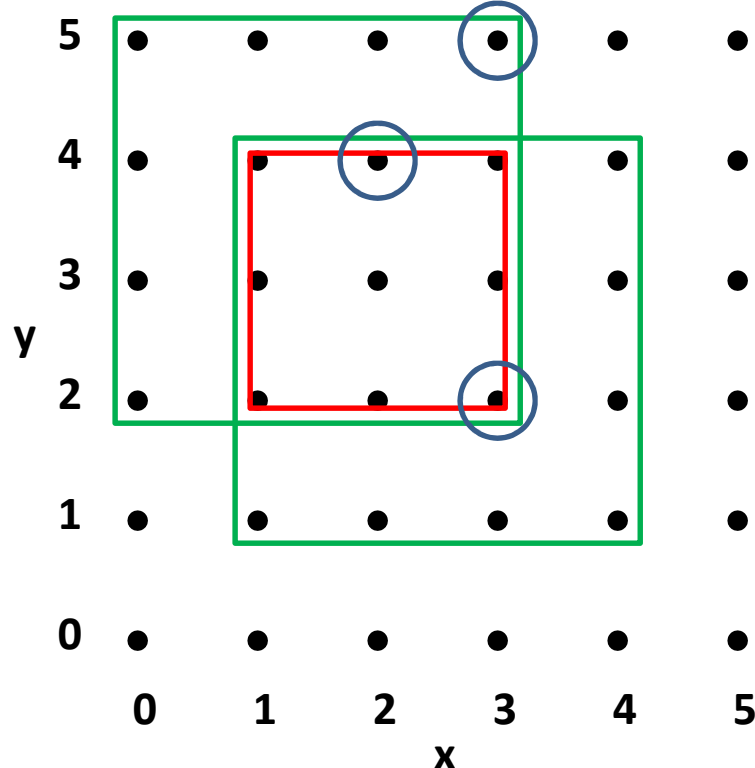
$S = \{[((1,2),2),\text{yellow}]]\}$



Using the Result

$G = \{[((0,2),3),\text{white}],[((1,1),3),\text{white}]\}$

$S = \{[((1,2),2),\text{yellow}]\}$



$[(3,2),\text{green}]$

Yes

$[(2,4),\text{red}]$

Yes

$[(3,5),\text{blue}]$

Maybe