

Exercises: Artificial Intelligence

Planning & Logic: Blocks world

Planning & Logic: Blocks world

PROBLEM

Problem

- **Table: T & Blocks: A,B,C,D**
- **Apply STRIPS on:**
 - **Initial State, I:**
 - clear(A), clear(B), clear(C), clear(D),
on(A,T), on(B,T), on(C,T), on(D,T)
 - **Final State, F:**
 - on(A,T), on(B,A), on(C,B), on(D,C), clear(D)
- **Indicate:** *Establish & Threaten*
- **Give:** *Before relation without loops*

Planning & Logic: Blocks world

INITIAL & FINAL STATE

Initial & Final State

If	
Add	on(A,T) on(B,T) on(C,T) on(D,T) clear(A) clear(B) clear(C) clear(D)
Del	

If	on(A,T) on(B,A) on(C,B) on(D,C) clear(D)
Add	
Del	

Planning & Logic: Blocks world

OPERATORS

Operators

Operator 1	
If	on(x,y) clear(x) clear(z)
Add	on(x,z) clear(y)
Del	on(x,y) clear(z)

Operator 2	
If	on(x,y) clear(x)
Add	on(x,T) clear(y)
Del	on(x,y)

Operator 3	
If	on(x,T) clear(x) clear(z)
Add	on(x,z)
Del	on(x,T) clear(z)

Actual operators are ground instances!

Planning & Logic: Blocks world

STRIPS

STRIPS

I	
If	
Add	on(A,T)
	on(B,T)
	on(C,T)
	on(D,T)
	clear(A)
	clear(B)
	clear(C)
	clear(D)
Del	

$B(I,F)$

F	
If	
If	on(A,T)
	on(B,A)
	on(C,B)
	on(D,C)
	clear(D)
Add	
Del	



Establishes



Threatens

Before constraint:

$B(x,y)$

STRIPS

I	
If	
Add	on(A,T)
	on(B,T)
	on(C,T)
	on(D,T)
	clear(A)
	clear(B)
	clear(C)
	clear(D)
Del	

O31 (x/B,z/A)	
If	
Add	on(B,T)
	clear(A)
	clear(B)
Del	on(B,A)
	clear(A)

F	
If	
Add	on(A,T)
	on(B,A)
	on(C,B)
	on(D,C)
Del	clear(D)

$B(I,F)$

$B(O31,F)$



Establishes



Threatens

Before constraint:

$B(x,y)$

STRIPS

I	
If	
Add	on(A,T)
	on(B,T)
	on(C,T)
	on(D,T)
	clear(A)
	clear(B)
	clear(C)
	clear(D)
Del	

O31 (x/B,z/A)	
If	
	on(B,T)
	clear(A)
	clear(B)
Add	on(B,A)
Del	on(B,T) clear(A)

F	
If	
	on(A,T)
	on(B,A)
	on(C,B)
	on(D,C)
	clear(D)
Add	
Del	

$B(I,F)$

$B(I,O31)$

$B(I,O31)$

$B(I,O31)$

$B(O31,F)$



Establishes



Threatens

Before constraint:

$B(x,y)$

STRIPS

I	
If	
Add	on(A,T)
	on(B,T)
	on(C,T)
	on(D,T)
	clear(A)
	clear(B)
	clear(C)
	clear(D)
Del	

$B(I, O31)$

O31 (x/B,z/A)

$B(O31, F)$

$B(I, F)$

F	
If	
	on(A,T)
	on(B,A)
	on(C,B)
	on(D,C)
	clear(D)
Add	
Del	



Establishes



Threatens

Before constraint:

$B(x, y)$

STRIPS

I	
If	
Add	on(A,T)
	on(B,T)
	on(C,T)
	on(D,T)
	clear(A)
	clear(B)
	clear(C)
	clear(D)
Del	

O31 (x/B,z/A)	
O32 (x/C,z/B)	
If	on(C,T) clear(B) clear(C)
Add	on(C,B)
Del	on(C,T) clear(B)

F	
If	
If	on(A,T)
	on(B,A)
	on(C,B)
	on(D,C)
	clear(D)
Add	
Del	

$B(I, O31)$

$B(I, F)$

$B(O31, F)$

$B(O32, F)$



Establishes

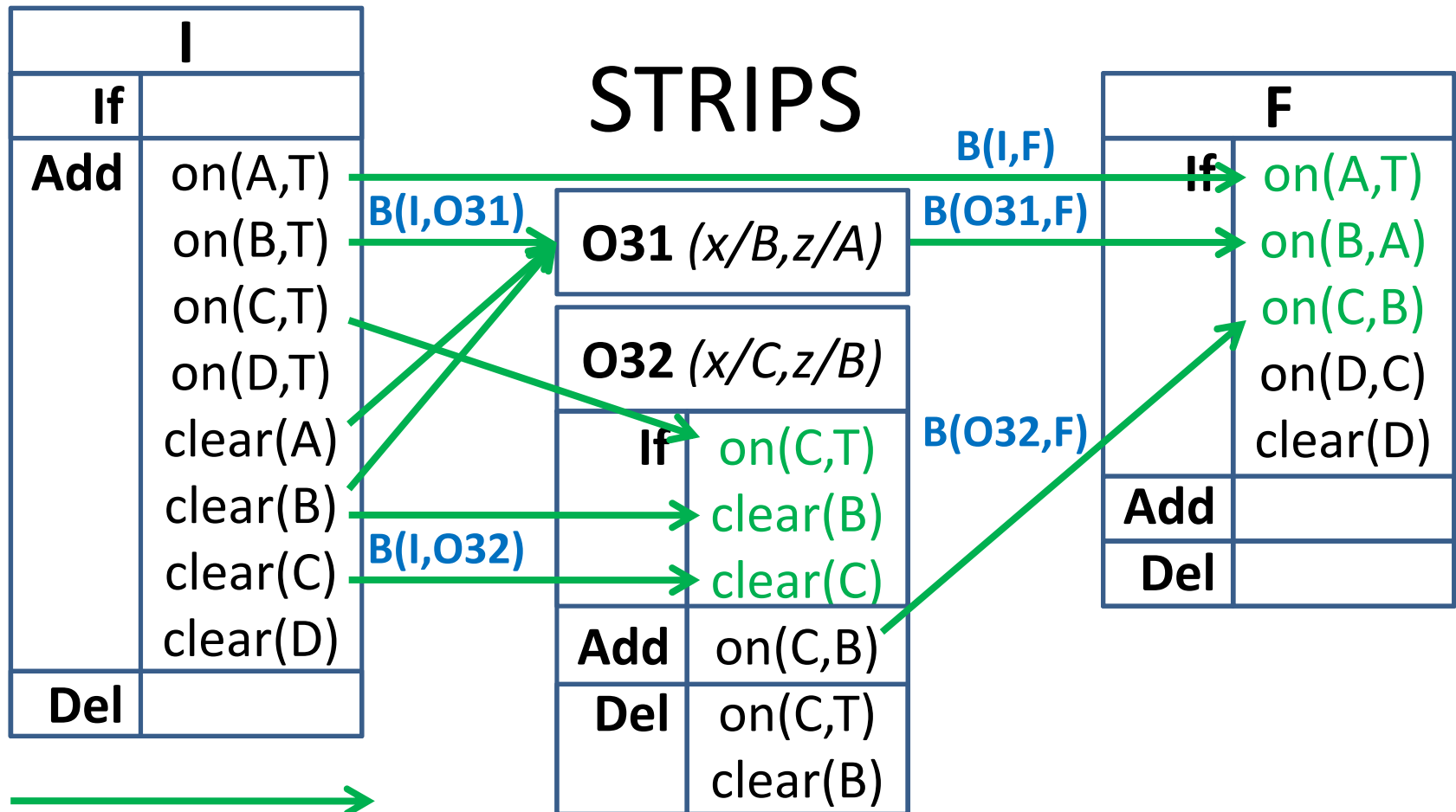


Threatens

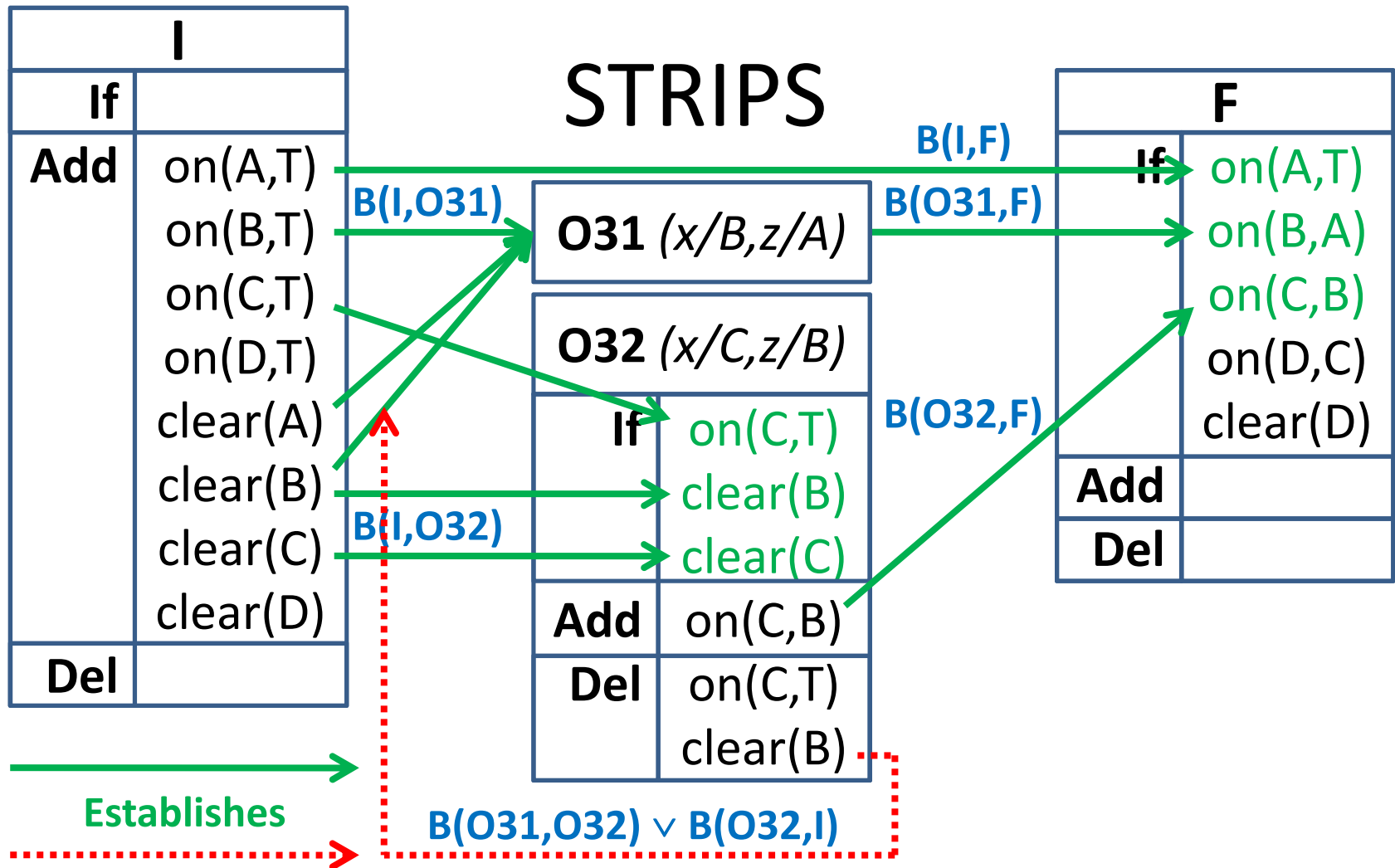
Before constraint:

$B(x, y)$

STRIPS



STRIPS



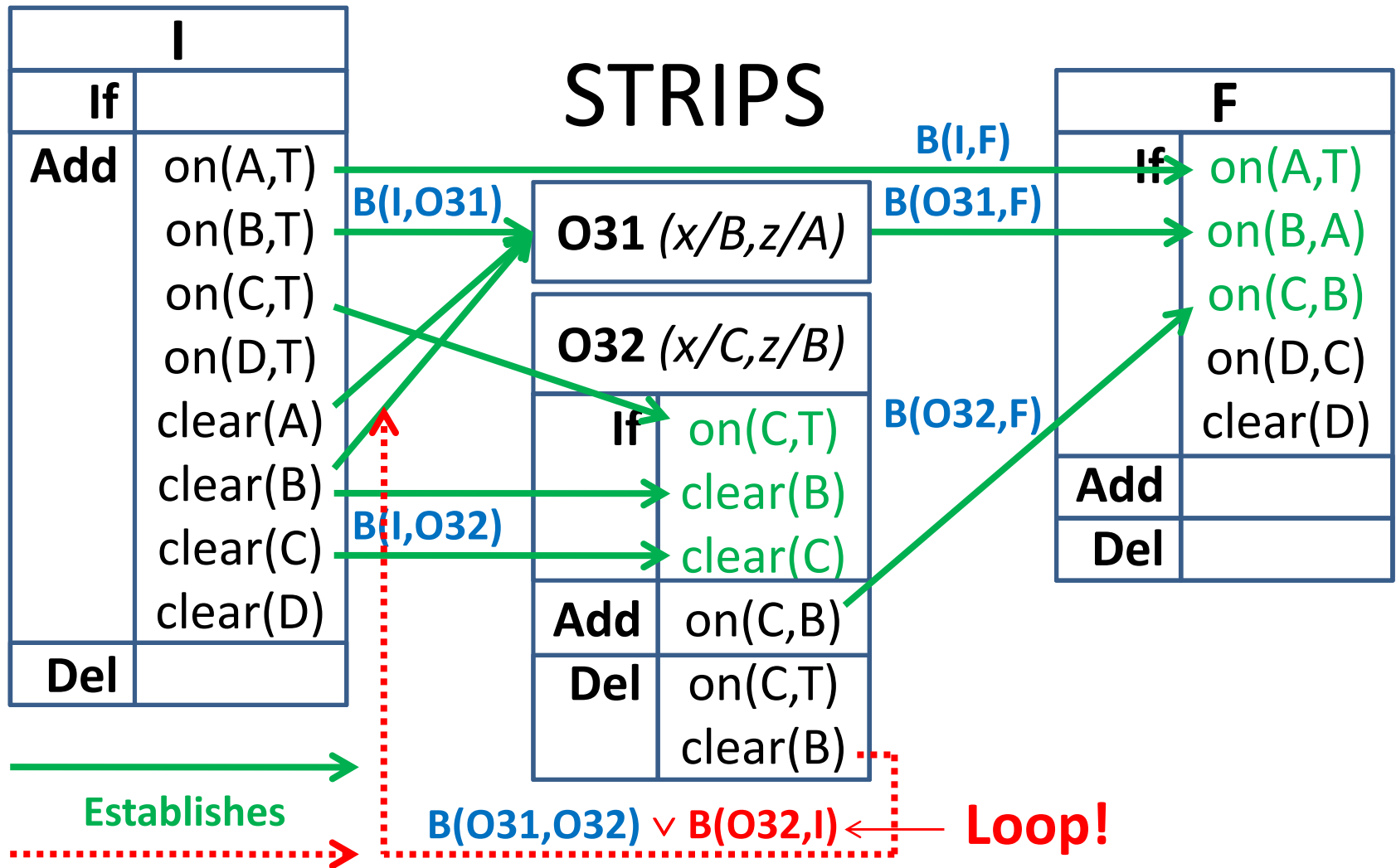
Establishes

Threatens

Before constraint:

$B(x,y)$

STRIPS



Before constraint:
B(x,y)

STRIPS

I	
If	
Add	on(A,T)
	on(B,T)
	on(C,T)
	on(D,T)
	clear(A)
	clear(B)
	clear(C)
	clear(D)
Del	

$B(I, O31)$

$B(I, O32)$

O31 (x/B,z/A)

O32 (x/C,z/B)

$B(O31, O32)$

$B(I, F)$

$B(O31, F)$

$B(O32, F)$

F	
If	
If	on(A,T)
	on(B,A)
	on(C,B)
	on(D,C)
	clear(D)
Add	
Del	



Establishes



Threatens

Before constraint:

$B(x, y)$

STRIPS

I	
If	
Add	on(A,T)
	on(B,T)
	on(C,T)
	on(D,T)
	clear(A)
	clear(B)
	clear(C)
	clear(D)
Del	

O31 (x/B,z/A)

O32 (x/C,z/B)

O33 (x/D,z/C)

If	on(D,T) clear(C) clear(D)
Add	on(D,C)
Del	on(D,T) clear(C)

F	
If	
If	on(A,T)
	on(B,A)
	on(C,B)
	on(D,C)
	clear(D)
Add	
Del	



Establishes



Threatens

Before constraint:

$B(x,y)$

$B(I,F)$

$B(I,O31)$

$B(O31,F)$

$B(I,O32)$

$B(O32,F)$

$B(O31,O32)$

$B(O33,F)$

STRIPS

I	
If	
Add	on(A,T)
	on(B,T)
	on(C,T)
	on(D,T)
	clear(A)
	clear(B)
	clear(C)
	clear(D)
Del	

O31 (x/B,z/A)

O32 (x/C,z/B)

O33 (x/D,z/C)

If	on(D,T)
	clear(C)
	clear(D)

Add	on(D,C)
Del	on(D,T)
	clear(C)

F	
If	
	on(A,T)
	on(B,A)
	on(C,B)
	on(D,C)
	clear(D)
Add	
Del	



Establishes



Threatens

Before constraint:

$B(x,y)$

$B(I,F)$

$B(I,O31)$

$B(O31,F)$

$B(I,O32)$

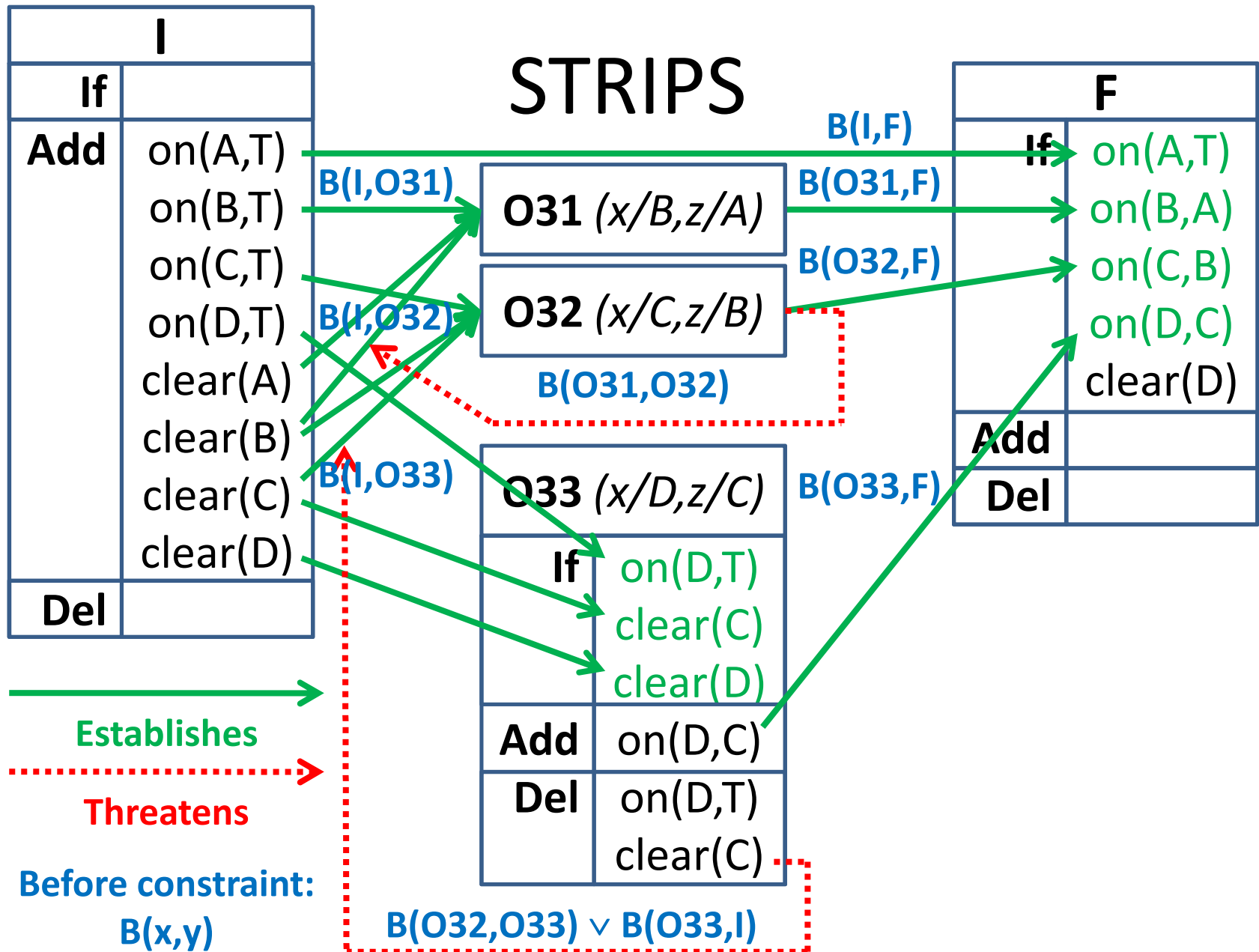
$B(O32,F)$

$B(O31,O32)$

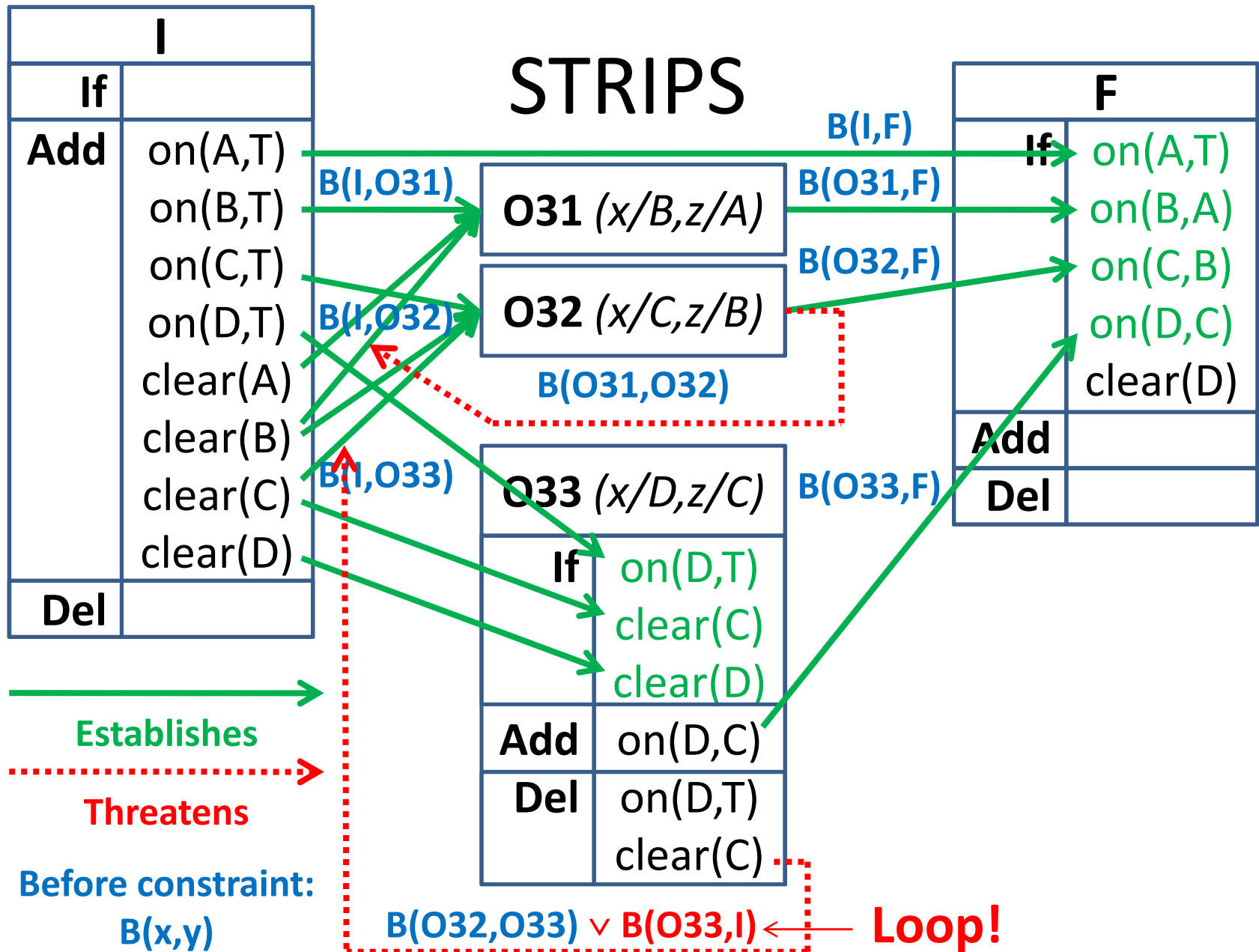
$B(I,O33)$

$B(O33,F)$

STRIPS

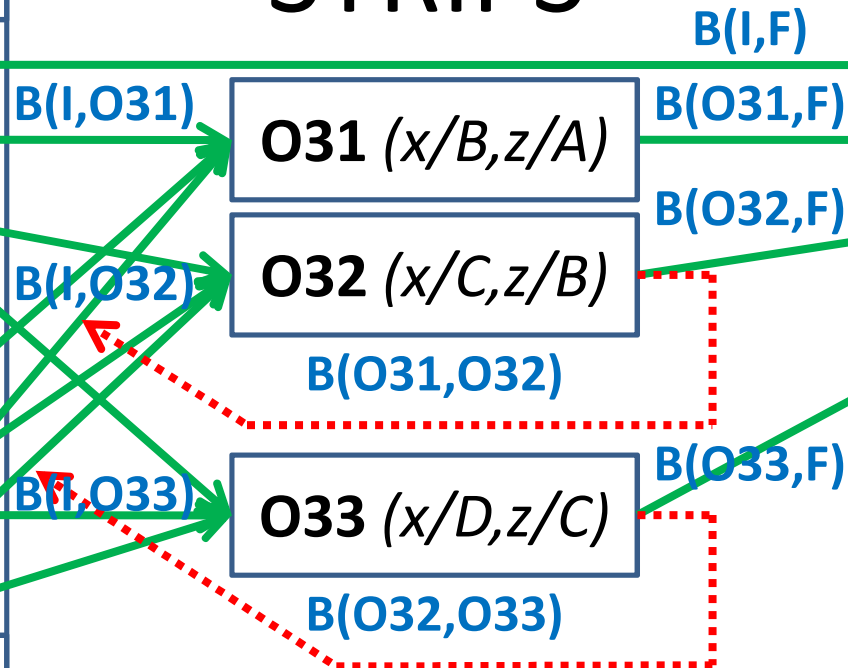


STRIPS



STRIPS

I	
If	
Add	on(A,T)
	on(B,T)
	on(C,T)
	on(D,T)
	clear(A)
	clear(B)
	clear(C)
	clear(D)
Del	



F	
If	
	on(A,T)
	on(B,A)
	on(C,B)
	on(D,C)
	clear(D)
Add	
Del	



Establishes

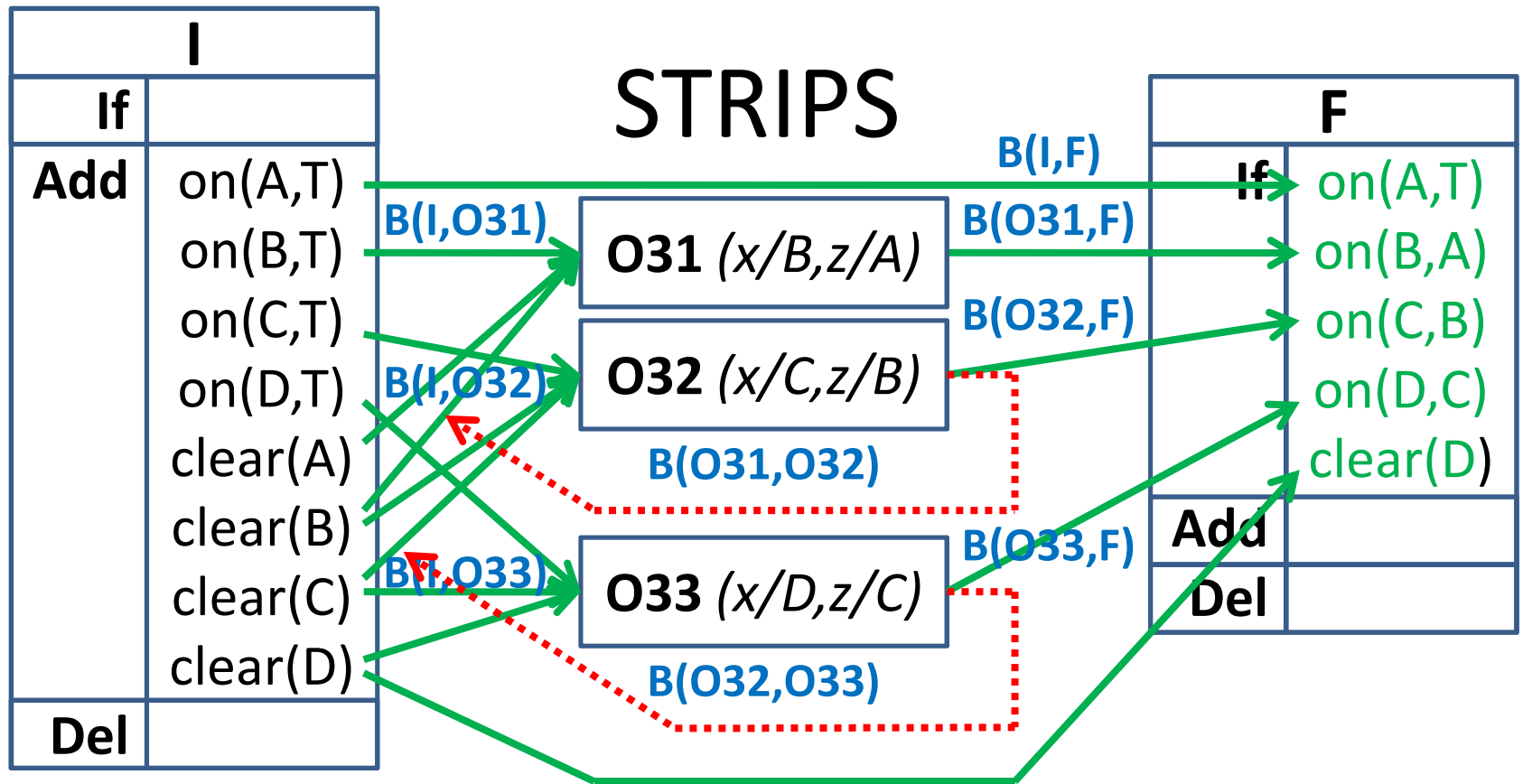


Threatens

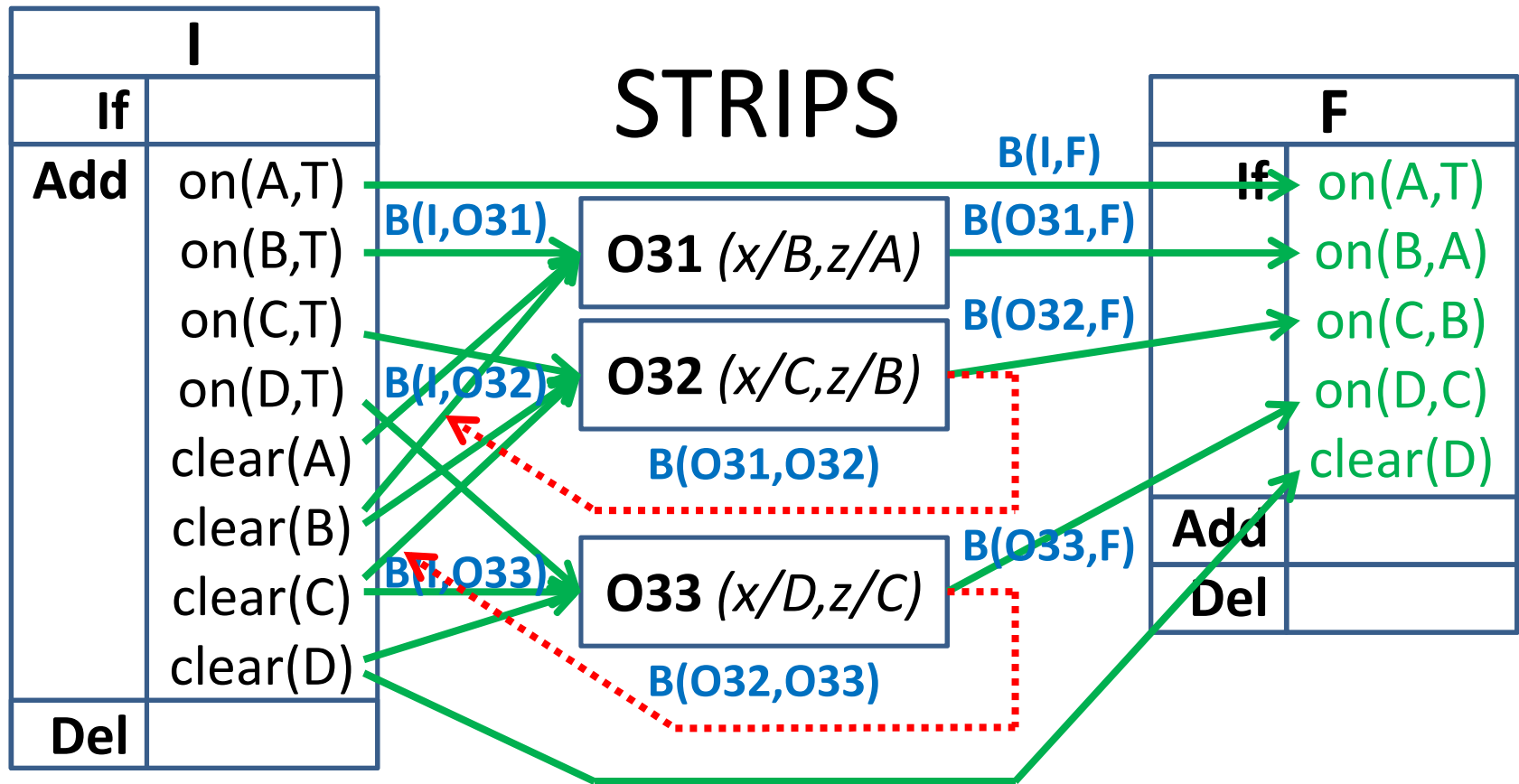
Before constraint:

$B(x,y)$

STRIPS

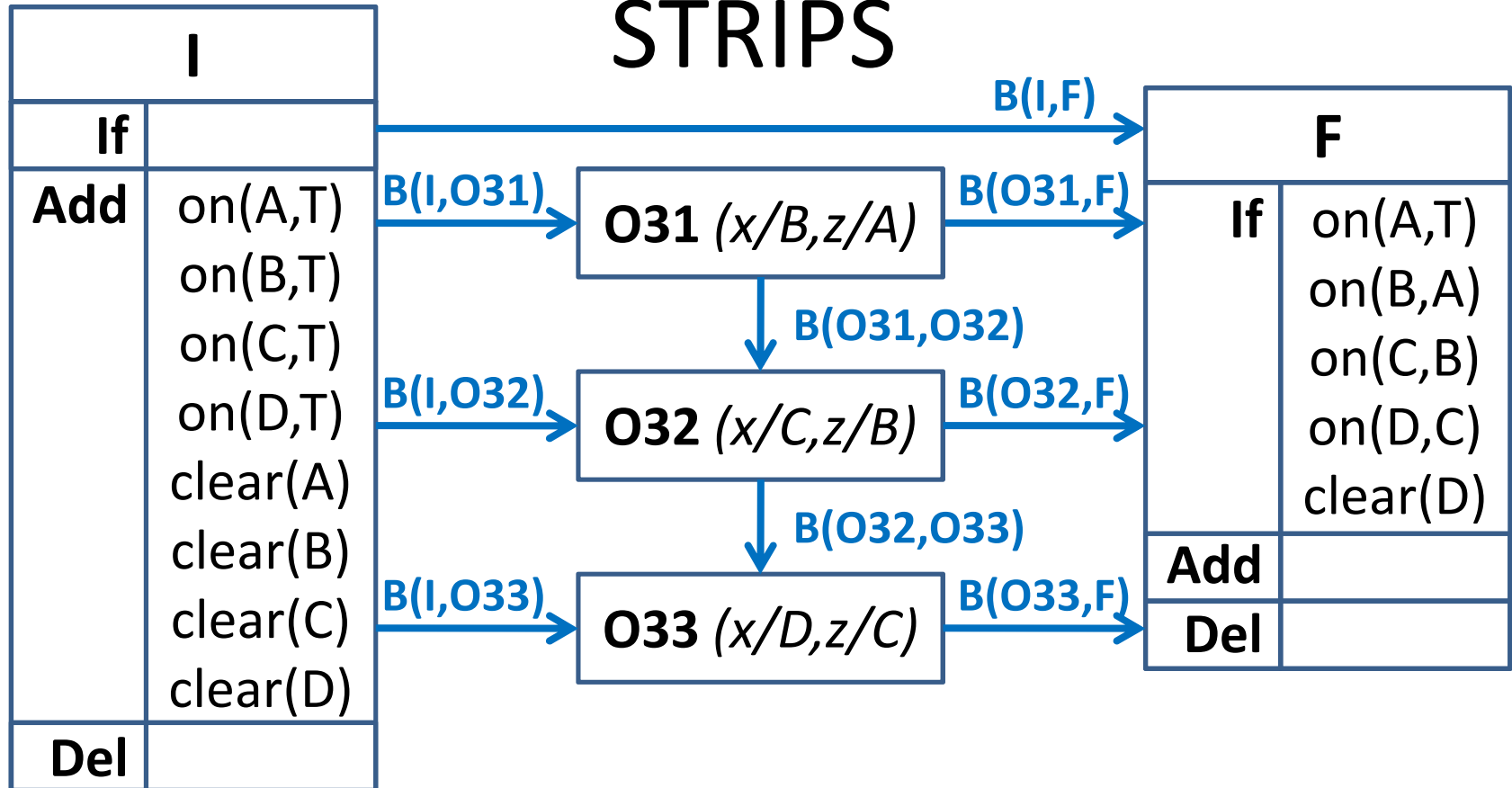


STRIPS



Are the before constraints satisfiable?

STRIPS



Are the before constraints satisfiable?

YES:

→ **O31** → **O32** → **O33** →

Exercises: Artificial Intelligence

Planning & Logic: Buying milk

Planning & Logic: Buying milk

PROBLEM

Problem

- **Apply STRIPS** on:
 - **Initial State, I:**
 - at(home)
 - **Final State, F:**
 - have(milk), at(home)
- **Indicate:** *Establish & Threaten*
- **Give:** *Before relation without loops (check!)*
- **Give:** *Possible linearisations*

Planning & Logic: Blocks world

INITIAL & FINAL STATE

Initial & Final State as Operator

I	
If	
Add	at(home)
Del	

F	
If	at(home) have(milk)
Add	
Del	

Planning & Logic: Blocks world

OPERATORS

Operators

Operator 1		Operator 2		Operator 3	
If	at(home)	If	at(home)	If	at(shop)
Add	have(money)	Add	at(shop)	Add	have(milk)
Del		Del	at(home)	Del	

Operator 4		Operator 5	
If	at(shop) paid	If	at(shop) have(money) have(milk)
Add	at(home)	Add	paid
Del	at(shop)	Del	have(money)

Planning & Logic: Blocks world

STRIPS

STRIPS

I	If	
	Add	at(home)
	Del	



Establishes



Threatens

Before constraint:

$B(x,y)$

F	
If	have(milk) at(home)
Add	
Del	

STRIPS

I	If	
	Add	at(home)
	Del	

Operator 3	
If	at(shop)
Add	have(milk)
Del	

$B(O3, F)$

F	
If	have(milk) at(home)
Add	
Del	



Establishes



Threatens

Before constraint:

$B(x, y)$

STRIPS

I	If	
	Add	at(home)
	Del	

Operator 2	
If	at(home)
Add	at(shop)
Del	at(home)

B(O2,O3)

Operator 3	
If	at(shop)
Add	have(milk)
Del	

B(O3,F)

F	
If	have(milk) at(home)
Add	
Del	



Establishes



Threatens

Before constraint:

B(x,y)

STRIPS

$B(I, O2)$

I	If	
	Add	at(home)
	Del	

Operator 2	
If	at(home)
Add	at(shop)
Del	at(home)

$B(O2, O3)$

Operator 3	
If	at(shop)
Add	have(milk)
Del	

$B(O3, F)$

F	
If	have(milk) at(home)
Add	
Del	

Establishes

Threatens

Before constraint:

$B(x, y)$

STRIPS

I	If	
	Add	at(home)
	Del	

Operator 2	
If	at(home)
Add	at(shop)
Del	at(home)

Operator 3	
If	at(shop)
Add	have(milk)
Del	

F	
If	have(milk) at(home)
Add	
Del	

$B(I, O2)$

$B(I, F)$

$B(O2, O3)$

$B(O3, F)$

Establishes

Threatens

Before constraint:

$B(x, y)$

STRIPS

I	If	
	Add	at(home)
	Del	

Operator 2		
If	→ at(home)	
Add	at(shop)	
Del	at(home)	

Operator 3		
If	← at(shop)	
Add	have(milk)	
Del		

F		
If	→ have(milk) → at(home)	
Add		
Del		

$B(I, O2)$

$B(O2, I) \vee B(F, O2)$

$B(O2, O3)$

$B(I, F)$

$B(O3, F)$

Establishes

Threatens

Before constraint:

$B(x, y)$

STRIPS

I	If	
	Add	at(home)
	Del	

Operator 2		
If	→ at(home)	
Add	at(shop)	
Del	at(home)	

Operator 3		
If	← at(shop)	
Add	have(milk)	
Del		

F		
If	→ have(milk) at(home)	
Add		
Del		

$B(I, O2)$

$B(O2, I) \vee B(F, O2)$

2 x Loop!

$B(O2, O3)$

$B(I, F)$

$B(O3, F)$

Establishes

Threatens

Before constraint:

$B(x, y)$

STRIPS

$B(I, O2)$

I	If	
	Add	at(home)
	Del	

Operator 2	
If	at(home)
Add	at(shop)
Del	at(home)

$B(O2, O3)$

Operator 3	
If	at(shop)
Add	have(milk)
Del	

$B(O3, F)$

F	
If	have(milk) at(home)
Add	
Del	

Establishes

Threatens

Before constraint:

$B(x, y)$

STRIPS

I	If	
	Add	at(home)
	Del	

$B(I, O2)$

Operator 2	
If	at(home)
Add	at(shop)
Del	at(home)

$B(O2, O3)$

Operator 3	
If	at(shop)
Add	have(milk)
Del	

$B(O3, F)$

Operator 4	
If	paid at(shop)
Add	at(home)
Del	at(shop)

$B(O4, F)$

F	
If	have(milk) at(home)
Add	
Del	

Establishes

Threatens

Before constraint:

$B(x, y)$

STRIPS

I	If	
	Add	at(home)
	Del	

$B(I, O2)$

Operator 2		
If	→ at(home)	
Add	at(shop)	
Del	at(home)	

$B(O2, O3)$

Operator 3		
If	← at(shop)	
Add	have(milk)	
Del		

$B(O3, F)$

$B(O2, O4) \vee B(F, O2)$

Operator 4		
If	paid	
	at(shop)	
Add	at(home)	
Del	at(shop)	

$B(O4, F)$

F		
If	have(milk)	
	at(home)	
Add		
Del		

Establishes

Threatens

Before constraint:

$B(x, y)$

STRIPS

I	If	
	Add	at(home)
	Del	

$B(I, O2)$

Operator 2		
If	→ at(home)	
Add	at(shop)	
Del	at(home)	

$B(O2, O3)$

Operator 3		
If	← at(shop)	
Add	have(milk)	
Del		

$B(O3, F)$

$B(O2, O4) \vee B(F, O2)$

Operator 4		
If	paid	
	at(shop)	
Add	at(home)	
Del	at(shop)	

$B(O4, F)$

F		
If	have(milk)	
	at(home)	
Add		
Del		

Establishes

Threatens

Before constraint:
 $B(x, y)$

STRIPS

$B(I, O2)$

Operator 2	
If	\rightarrow at(home)
Add	at(shop)
Del	at(home)

$B(O2, O3)$

Operator 3	
If	at(shop) \leftarrow
Add	have(milk)
Del	

$B(O2, O4)$

$B(O3, F)$

Operator 4	
If	paid at(shop)
Add	at(home)
Del	at(shop)

F	
If	have(milk) at(home)
Add	
Del	

Establishes

Threatens

Before constraint:

$B(x, y)$

STRIPS

I	If	
	Add	at(home)
	Del	

$B(I, O2)$

Operator 2	
If	at(home)
Add	at(shop)
Del	at(home)

$B(O4, O2) \vee B(O3, O4)$

Operator 3	
If	at(shop)
Add	have(milk)
Del	

$B(O2, O4)$

$B(O3, F)$

Operator 4	
If	paid at(shop)
Add	at(home)
Del	at(shop)

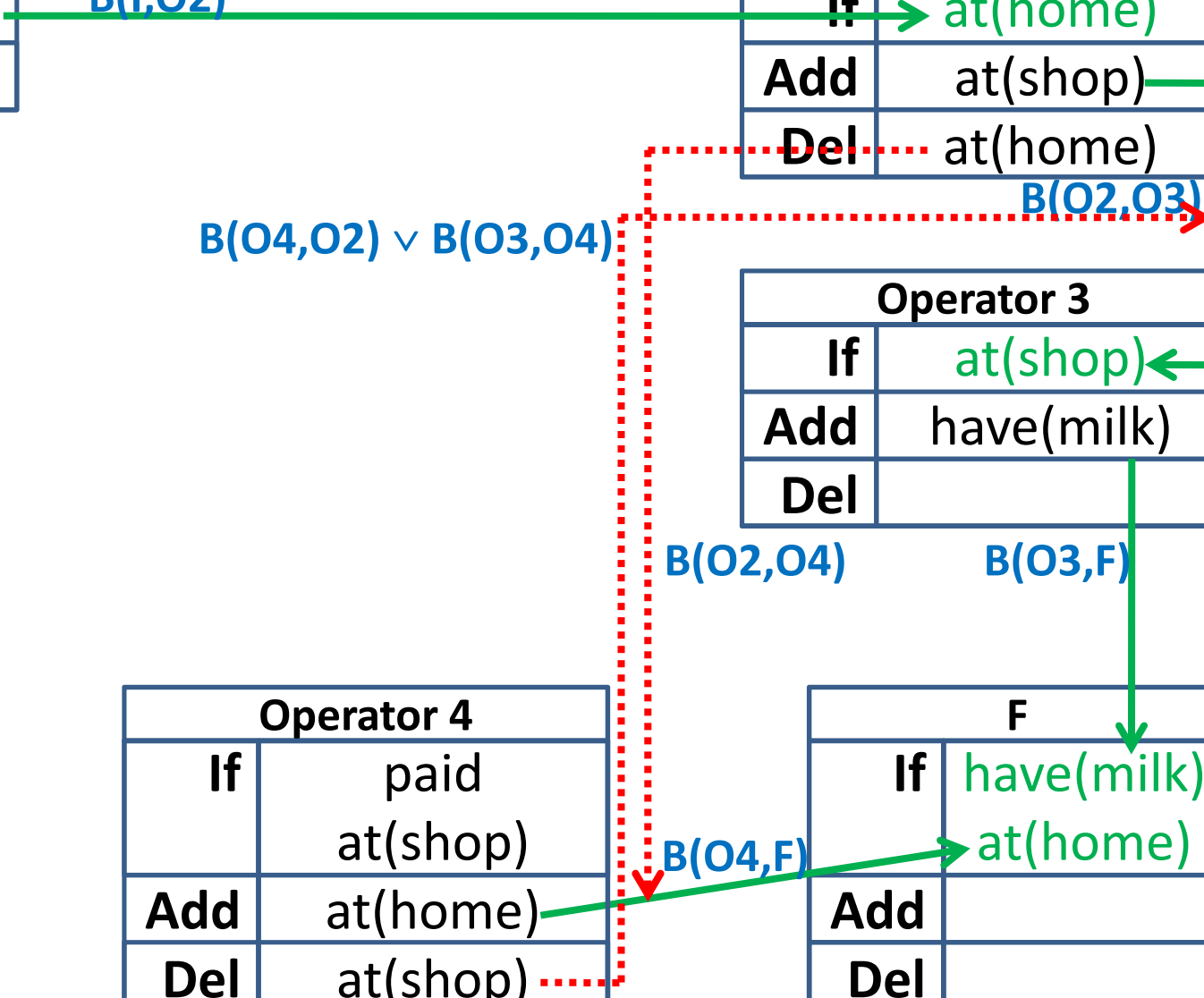
F	
If	have(milk) at(home)
Add	
Del	

Establishes

Threatens

Before constraint:

$B(x, y)$



STRIPS

I	If	
	Add	at(home)
	Del	

$B(I, O2)$

Operator 2		
If	→ at(home)	
Add	at(shop)	
Del	at(home)	

$B(O2, O3)$

$B(O4, O2) \vee B(O3, O4)$

Operator 3		
If	← at(shop)	
Add	have(milk)	
Del		

$B(O2, O4)$

$B(O3, F)$

Operator 4		
If	paid	
	at(shop)	
Add	at(home)	
Del	at(shop)	

$B(O4, F)$

F		
If	have(milk)	
	at(home)	
Add		
Del		

Establishes

Threatens

Before constraint:

$B(x, y)$

STRIPS

I	If	
	Add	at(home)
	Del	

B(I,O2)

Operator 2		
If	at(home)	
Add	at(shop)	
Del	at(home)	

B(O2,O3)

B(O3,O4)

Operator 3		
If	at(shop)	
Add	have(milk)	
Del		

B(O2,O4)

B(O3,F)

Operator 4		
If	paid	
	at(shop)	
Add	at(home)	
Del	at(shop)	

B(O4,F)

F		
If	have(milk)	
	at(home)	
Add		
Del		

Establishes

Threatens

Before constraint:

B(x,y)



STRIPS

I	If	
	Add	at(home)
	Del	

B(I,O2)

Operator 2		
If	at(home)	
Add	at(shop)	
Del	at(home)	

B(O2,O3)

Operator 5		
If	at(shop) have(money) have(milk)	
Add	paid	
Del	have(money)	

B(O5,O4)

Operator 3		
If	at(shop)	
Add	have(milk)	
Del		

B(O2,O4)

B(O3,F)

Operator 4		
If	paid at(shop)	
Add	at(home)	
Del	at(shop)	

B(O4,F)

F		
If	have(milk) at(home)	
Add		
Del		



Establishes



Threatens

Before constraint:

B(x,y)

STRIPS

I	If	
	Add	at(home)
	Del	

Operator 2		
If	→	at(home)
Add		at(shop)
Del		at(home)

B(02,05)

Operator 5		
If	→	at(shop)
		have(money)
		have(milk)
Add		paid
Del		have(money)

B(03,04)

Operator 3		
If		at(shop) ←
Add		have(milk)
Del		

B(02,03)

B(02,04)

B(03,F)

B(05,04)

Operator 4		
If		paid
		at(shop)
Add		at(home)
Del		at(shop)

B(04,F)

F		
If		have(milk)
		at(home)
Add		
Del		



Establishes



Threatens

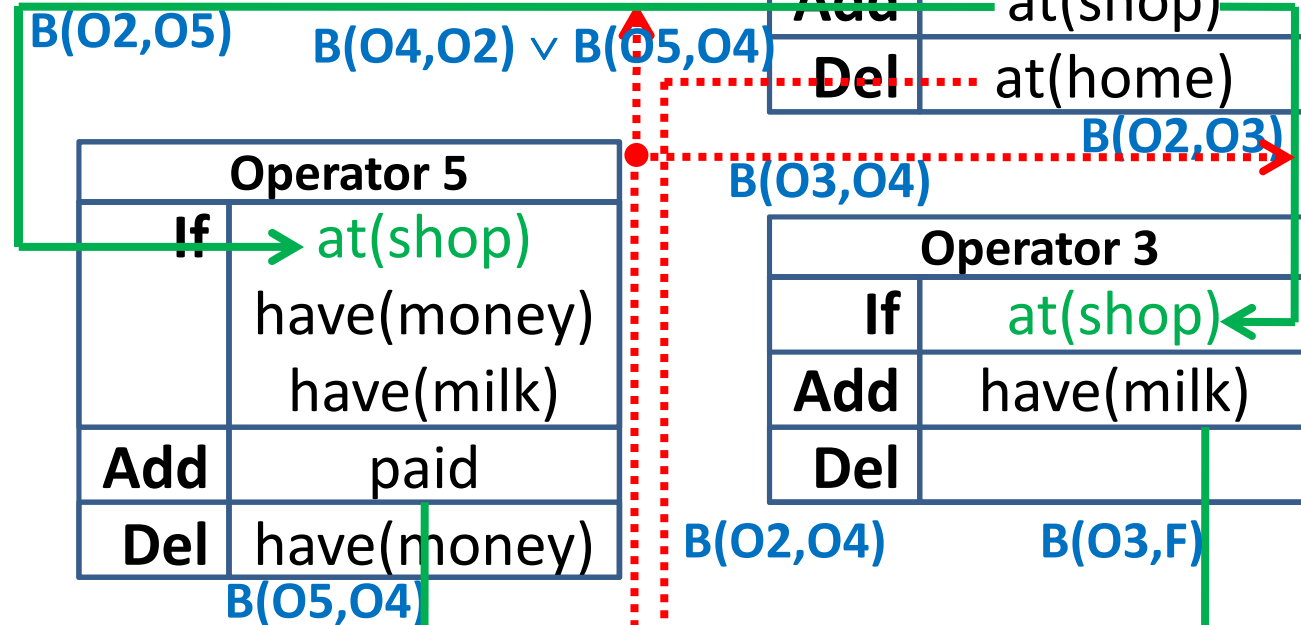
Before constraint:

B(x,y)

STRIPS

I	If	
	Add	at(home)
	Del	

Operator 2		
If	→	at(home)
Add		at(shop)
Del		at(home)



Establishes

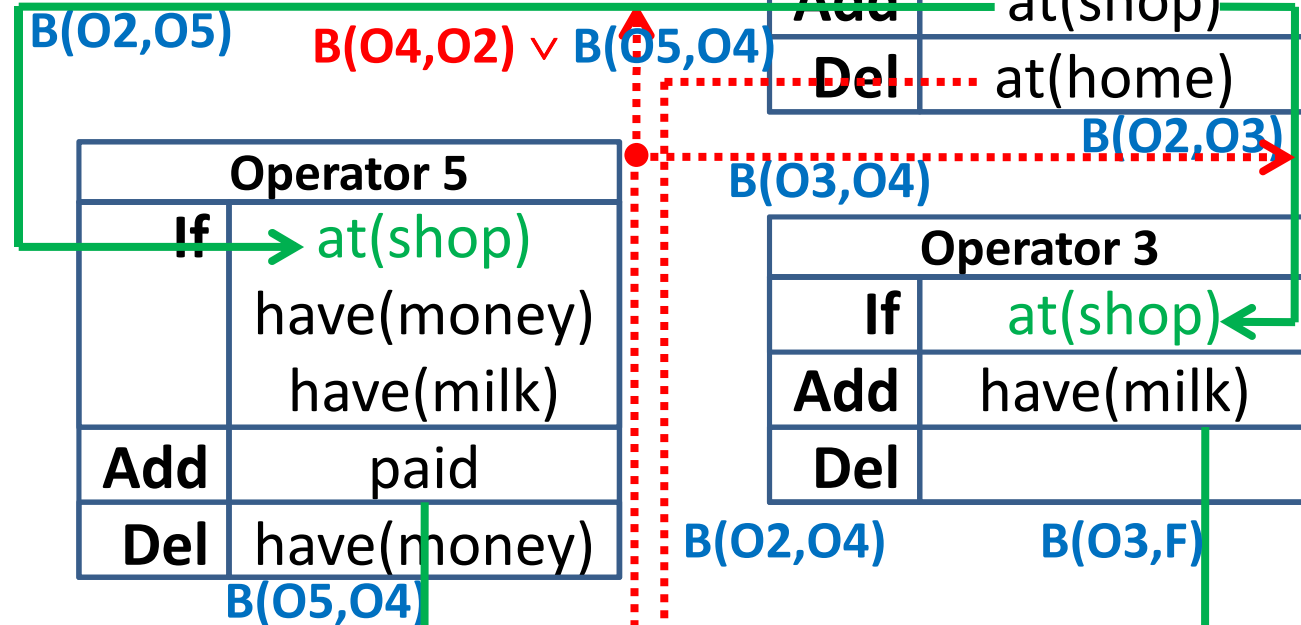
Threatens

Before constraint:
 $B(x, y)$

STRIPS

I	If	
	Add	at(home)
	Del	

Operator 2		
If	→	at(home)
Add		at(shop)
Del		at(home)



Before constraint:
 $B(x, y)$

STRIPS

I	If	
	Add	at(home)
	Del	

Operator 2		
If	→	at(home)
Add		at(shop)
Del		at(home)

$B(O2, O5)$

$B(O5, O4)$

$B(O2, O3)$

$B(O3, O4)$

Operator 5		
If	→	at(shop)
		have(money)
		have(milk)
Add		paid
Del		have(money)

$B(O5, O4)$

Operator 3		
If		at(shop) ←
Add		have(milk)
Del		

$B(O2, O4)$

$B(O3, F)$

Operator 4		
If		paid
		at(shop)
Add		at(home)
Del		at(shop)

$B(O4, F)$

F		
If		have(milk)
		at(home)
Add		
Del		

Establishes

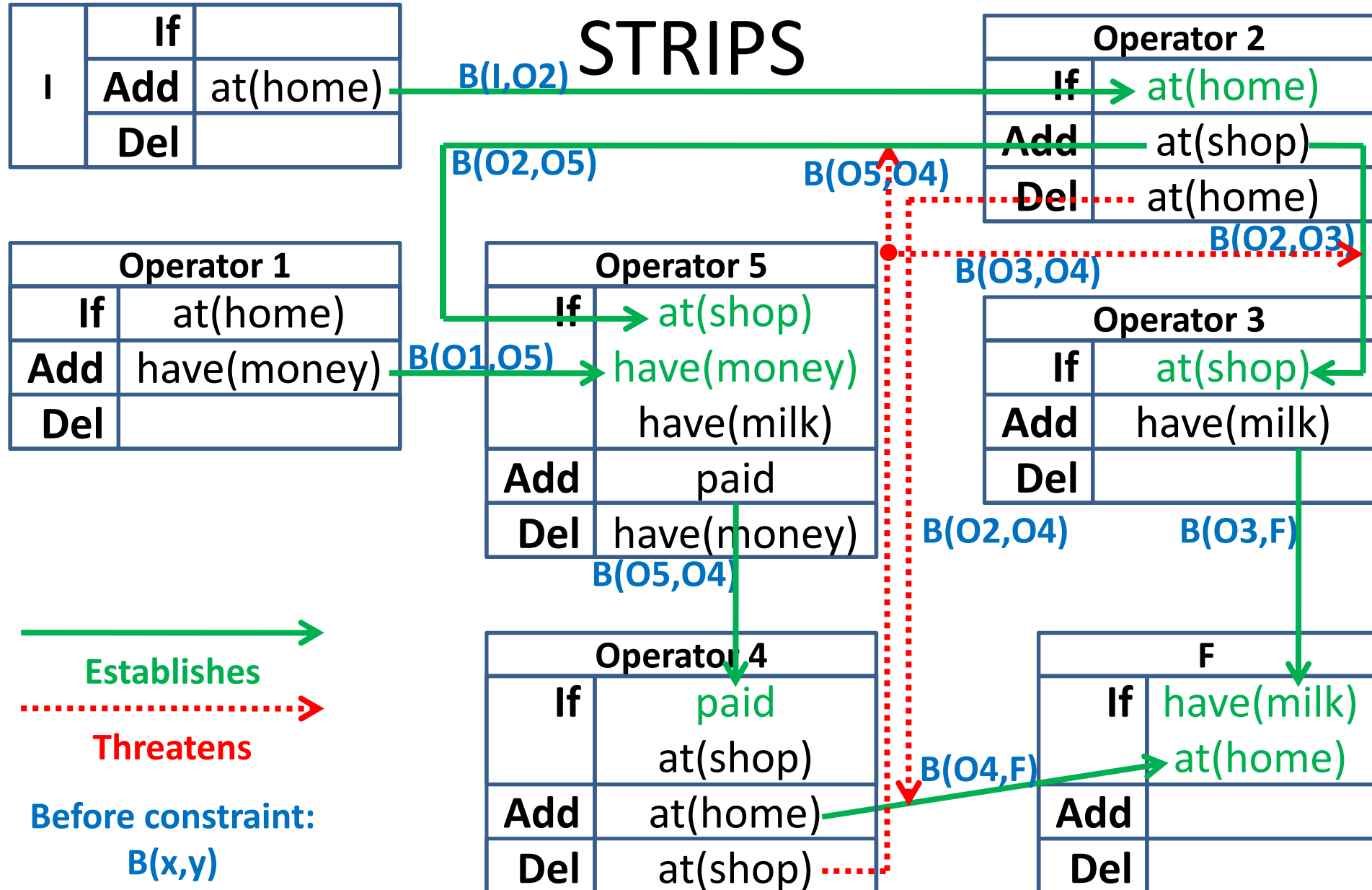
Threatens

Before constraint:

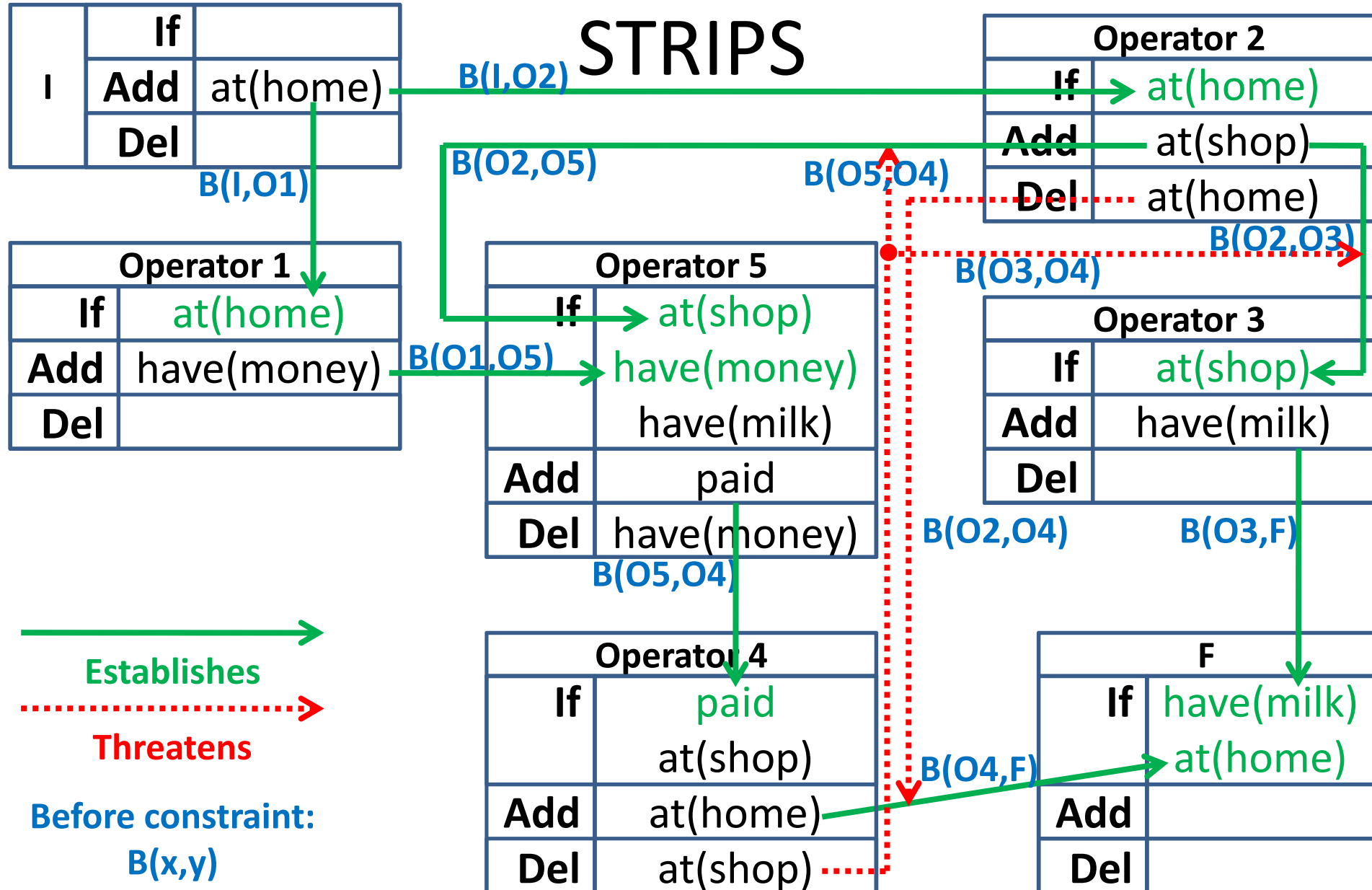
$B(x, y)$



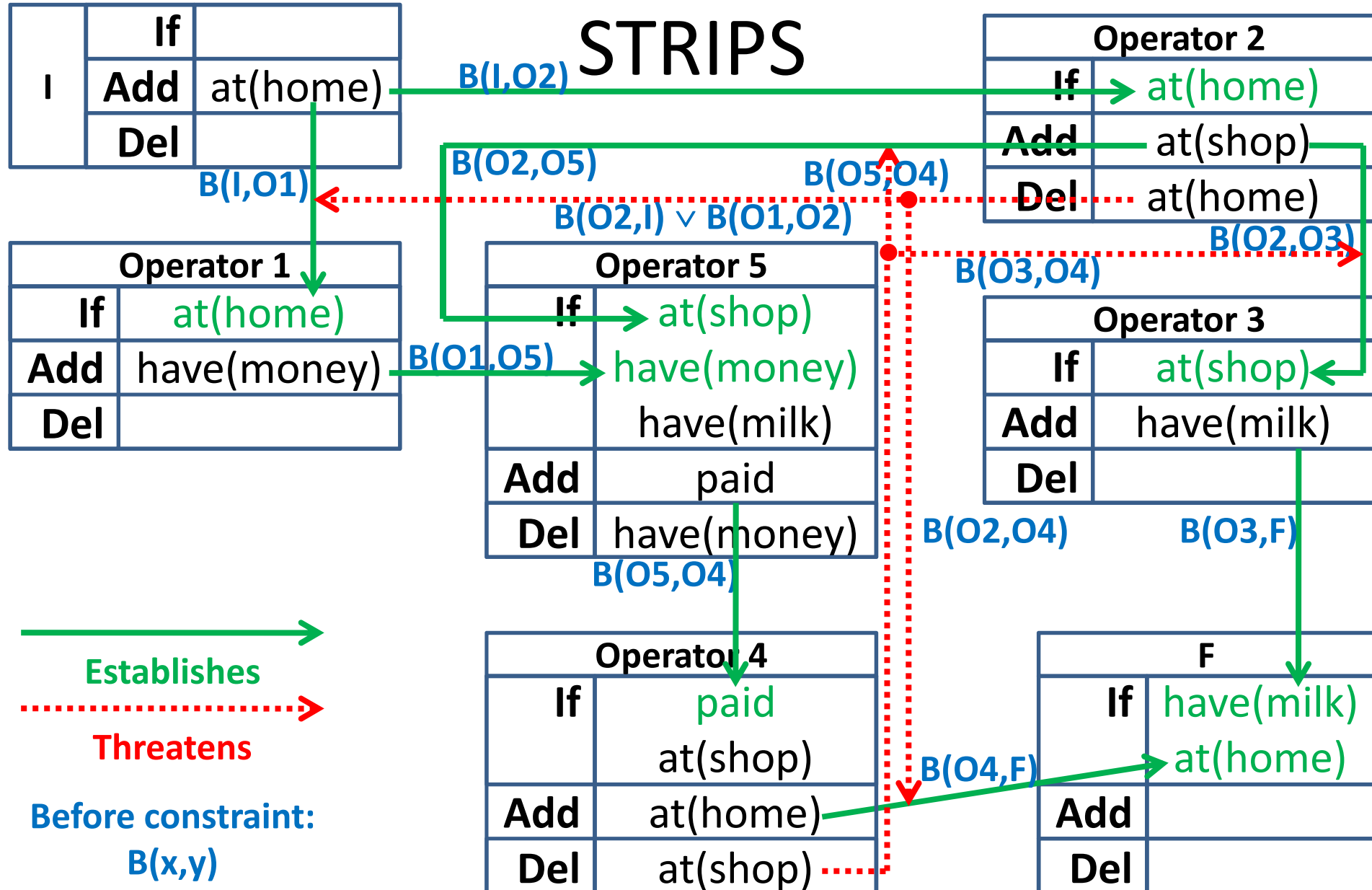
STRIPS



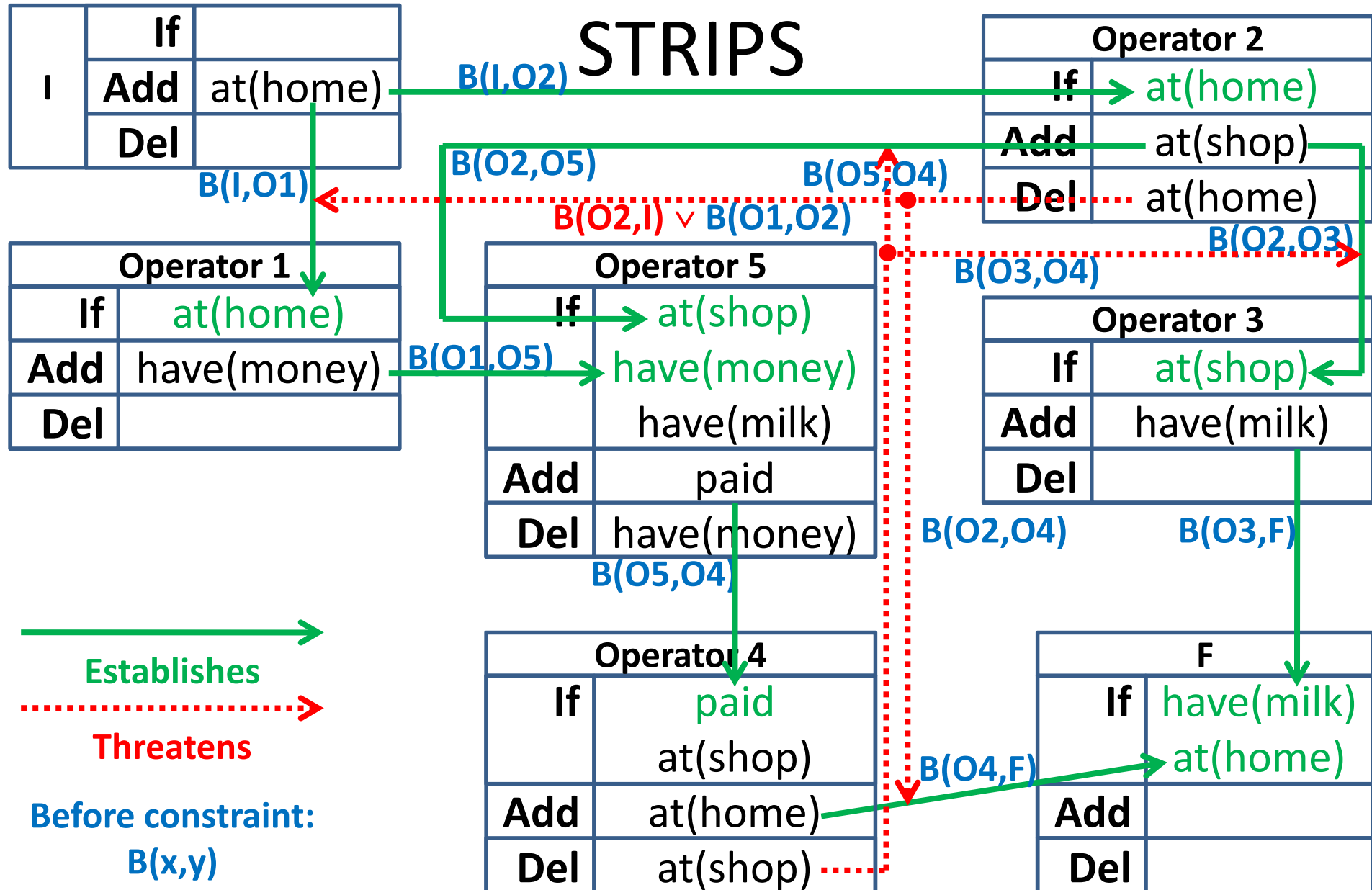
STRIPS



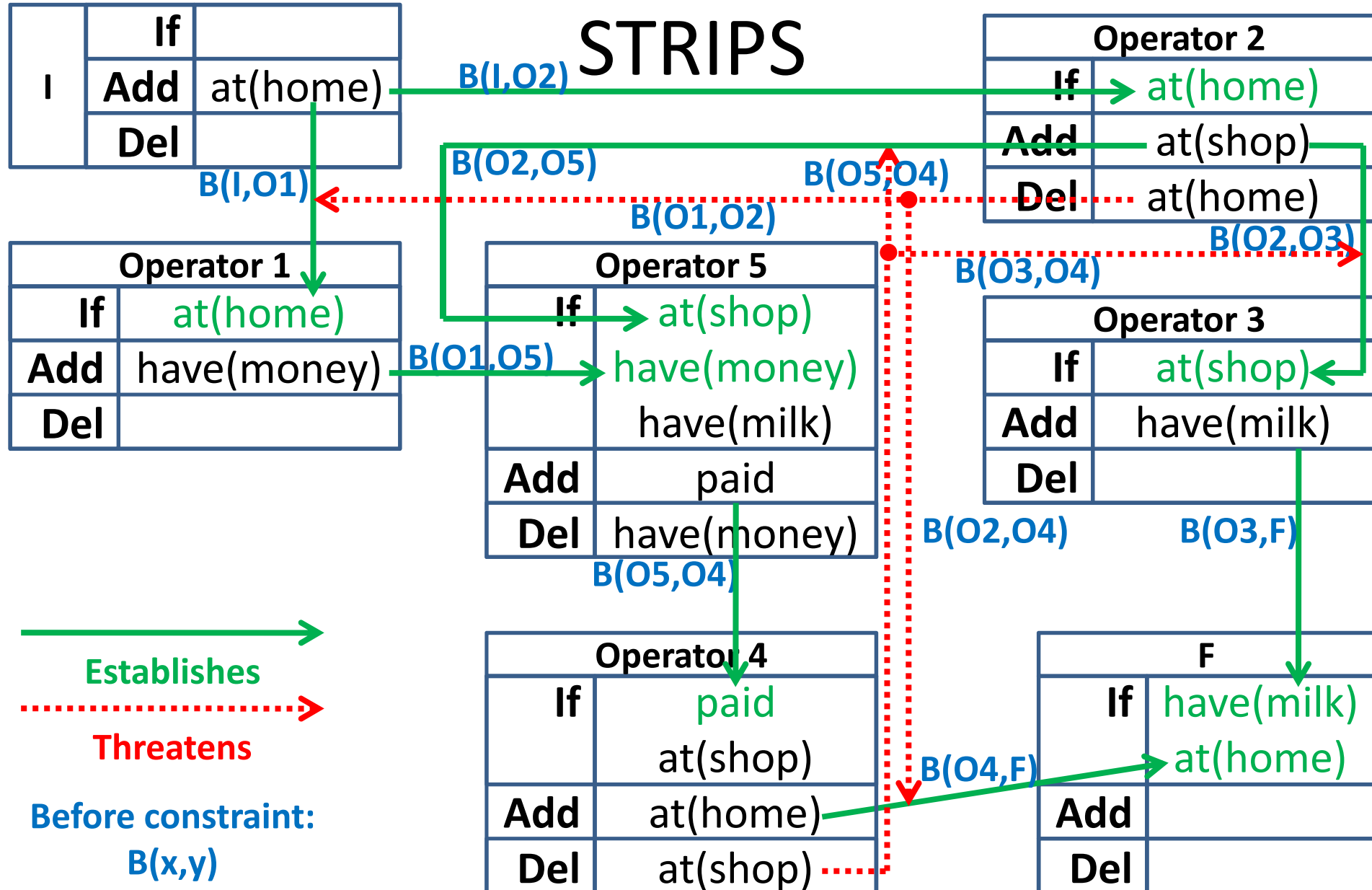
STRIPS



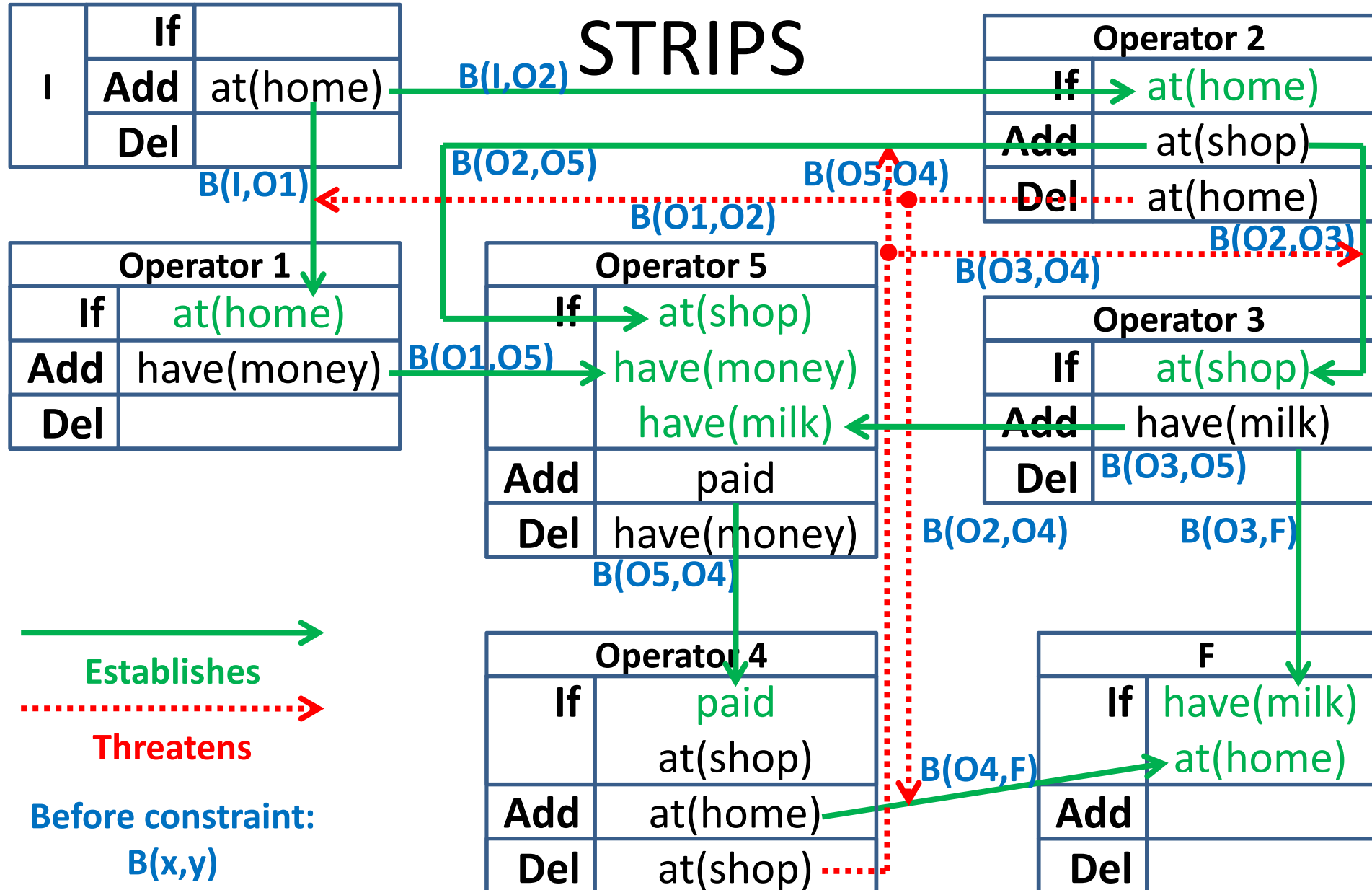
STRIPS



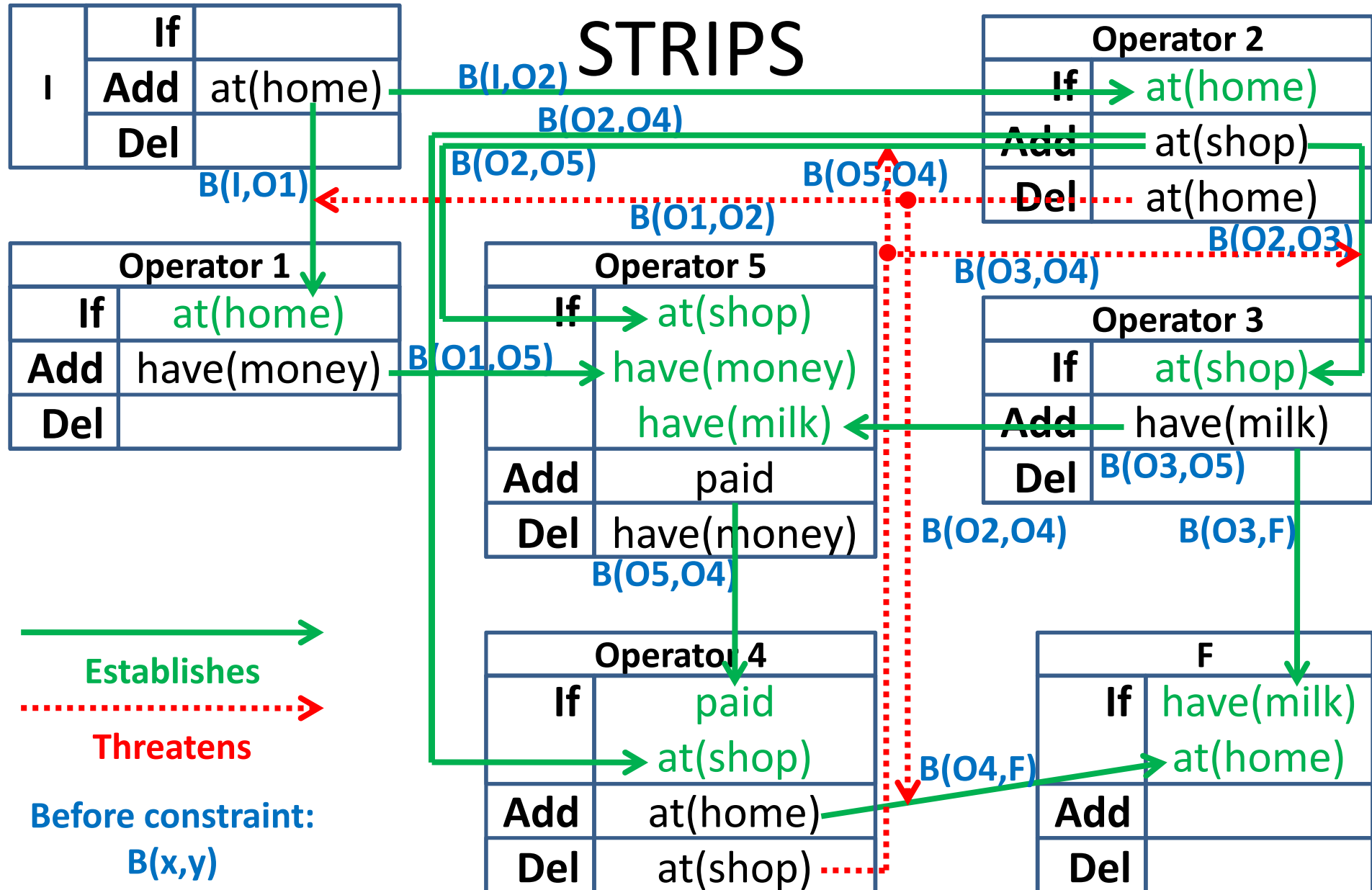
STRIPS



STRIPS



STRIPS

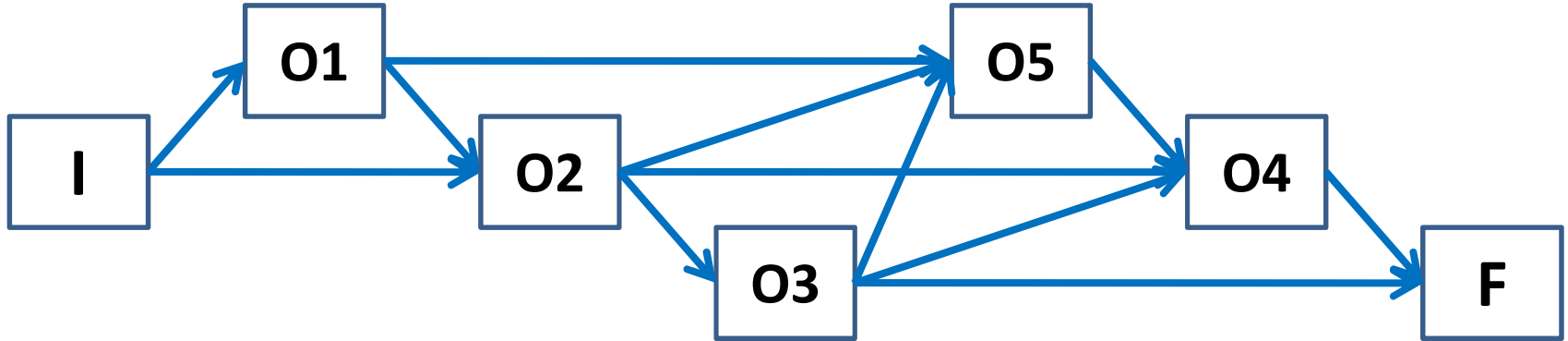


STRIPS

B(I,O1)	B(O2,O5)
B(I,O2)	B(O3,O4)
B(O1,O2)	B(O3,O5)
B(O1,O5)	B(O3,F)
B(O2,O3)	B(O4,F)
B(O2,O4)	B(O5,O4)

Are the before constraints satisfiable?

STRIPS



Are the before constraints satisfiable?

YES:

→ **O1** → **O2** → **O3** → **O5** → **O4** →

Exercises: Artificial Intelligence

Planning & Logic: English to Logic

Planning & Logic: English to Logic

PROBLEM & SOLUTION

Problem & Solution

- *Not all students take both history and biology*

Problem & Solution

- *Not all students take both history and biology*
 - ¬ $\forall x [\text{student}(x) \Rightarrow \text{takes}(x, \text{hist}) \wedge \text{takes}(x, \text{bio})]$

Problem & Solution

- *Not all students take both history and biology*
 - $\neg \forall x [\text{student}(x) \Rightarrow \text{takes}(x, \text{hist}) \wedge \text{takes}(x, \text{bio})]$
 - $\Leftrightarrow [A \Rightarrow B \Leftrightarrow \neg A \vee B]$
 - $\neg \forall x [\neg[\text{student}(x)] \vee [\text{takes}(x, \text{hist}) \wedge \text{takes}(x, \text{bio})]]$

Problem & Solution

- *Not all students take both history and biology*

$$\neg \forall x [\text{student}(x) \Rightarrow \text{takes}(x, \text{hist}) \wedge \text{takes}(x, \text{bio})]$$

$$\Leftrightarrow [A \Rightarrow B \Leftrightarrow \neg A \vee B]$$

$$\neg \forall x [\neg[\text{student}(x)] \vee [\text{takes}(x, \text{hist}) \wedge \text{takes}(x, \text{bio})]]$$

$$\Leftrightarrow [\neg \forall x (F) \Leftrightarrow \exists x (\neg F)]$$

$$\exists x \neg[\neg[\text{student}(x)] \vee [\text{takes}(x, \text{hist}) \wedge \text{takes}(x, \text{bio})]]$$

Problem & Solution

- *Not all students take both history and biology*

$$\neg \forall x [\text{student}(x) \Rightarrow \text{takes}(x, \text{hist}) \wedge \text{takes}(x, \text{bio})]$$

$$\Leftrightarrow [A \Rightarrow B \Leftrightarrow \neg A \vee B]$$

$$\neg \forall x [\neg [\text{student}(x)] \vee [\text{takes}(x, \text{hist}) \wedge \text{takes}(x, \text{bio})]]$$

$$\Leftrightarrow [\neg \forall x (F) \Leftrightarrow \exists x (\neg F)]$$

$$\exists x \neg [\neg [\text{student}(x)] \vee [\text{takes}(x, \text{hist}) \wedge \text{takes}(x, \text{bio})]]$$

$$\Leftrightarrow [\neg(A \vee B) \Leftrightarrow \neg A \wedge \neg B], [\neg(A \wedge B) \Leftrightarrow \neg A \vee \neg B]$$

$$\exists x [\text{student}(x) \wedge [\neg \text{takes}(x, \text{hist}) \vee \neg \text{takes}(x, \text{bio})]]$$

Problem & Solution

- *No person likes a smart vegetarian*

Problem & Solution

- *No person likes a smart vegetarian*

$$\forall x \forall y [\text{person}(x) \wedge \text{vegetarian}(y) \wedge \text{smart}(y) \Rightarrow \neg \text{likes}(x,y)]$$

Problem & Solution

- *No person likes a smart vegetarian*

$$\forall x \forall y [\text{person}(x) \wedge \text{vegetarian}(y) \wedge \text{smart}(y) \Rightarrow \neg \text{likes}(x,y)]$$

$$\Leftrightarrow [A \Rightarrow B \Leftrightarrow \neg A \vee B]$$

$$\forall x \forall y [\neg[\text{person}(x) \wedge \text{vegetarian}(y) \wedge \text{smart}(y)] \vee \neg \text{likes}(x,y)]$$

Problem & Solution

- *No person likes a smart vegetarian*

$$\forall x \forall y [\text{person}(x) \wedge \text{vegetarian}(y) \wedge \text{smart}(y) \Rightarrow \neg \text{likes}(x,y)]$$

$$\Leftrightarrow [A \Rightarrow B \Leftrightarrow \neg A \vee B]$$

$$\forall x \forall y [\neg[\text{person}(x) \wedge \text{vegetarian}(y) \wedge \text{smart}(y)] \vee \neg \text{likes}(x,y)]$$

$$\Leftrightarrow [\neg A \vee \neg B \Leftrightarrow \neg(A \wedge B)]$$

$$\forall x \forall y \neg[\text{person}(x) \wedge \text{vegetarian}(y) \wedge \text{smart}(y) \wedge \text{likes}(x,y)]$$

Problem & Solution

- *No person likes a smart vegetarian*

$$\forall x \forall y [\text{person}(x) \wedge \text{vegetarian}(y) \wedge \text{smart}(y) \Rightarrow \neg \text{likes}(x,y)]$$

$$\Leftrightarrow [A \Rightarrow B \Leftrightarrow \neg A \vee B]$$

$$\forall x \forall y [\neg[\text{person}(x) \wedge \text{vegetarian}(y) \wedge \text{smart}(y)] \vee \neg \text{likes}(x,y)]$$

$$\Leftrightarrow [\neg A \vee \neg B \Leftrightarrow \neg(A \wedge B)]$$

$$\forall x \forall y \neg[\text{person}(x) \wedge \text{vegetarian}(y) \wedge \text{smart}(y) \wedge \text{likes}(x,y)]$$

$$\Leftrightarrow [\forall x \neg(F) \Leftrightarrow \neg \exists x (F)]$$

$$\neg \exists x \exists y [\text{person}(x) \wedge \text{vegetarian}(y) \wedge \text{smart}(y) \wedge \text{likes}(x,y)]$$

Problem & Solution

- *There is a woman who likes all men who are not vegetarians.*

Problem & Solution

- *There is a woman who likes all men who are not vegetarians.*

$$\exists x[\text{woman}(x) \wedge [\forall y [\text{man}(y) \wedge \neg \text{vegetarian}(y) \Rightarrow \text{likes}(x,y)]]]$$

Problem & Solution

- *The best score in history was better than the best score in biology.*

Problem & Solution

- *The best score in history was better than the best score in biology.*

$$\forall x \forall y [\text{bestscore}(\text{hist}, x) \wedge \text{bestscore}(\text{bio}, y) \Rightarrow \text{better}(x, y)]$$

Problem & Solution

- *Every person who dislikes all vegetarians is smart.*

Problem & Solution

- *Every person who dislikes all vegetarians is smart.*

$$\forall x [\text{person}(x) \wedge [\forall y [\text{vegetarian}(y) \Rightarrow \neg \text{likes}(x,y)]] \Rightarrow \text{smart}(x)]$$

Problem & Solution

- *There is a barber who shaves all men in town who do not shave themselves.*

Problem & Solution

- *There is a barber who shaves all men in town who do not shave themselves.*

$$\exists x [\text{barber}(x) \wedge [\forall y [\text{townsman}(y) \wedge \neg \text{shaves}(y,y) \Rightarrow \text{shaves}(x,y)]]]$$

Problem & Solution

- *There is a barber who shaves all men in town who do not shave themselves.*

$$\exists x [\text{barber}(x) \wedge [\forall y [\text{townsman}(y) \wedge \neg \text{shaves}(y,y) \Rightarrow \text{shaves}(x,y)]]]$$

$$\Leftrightarrow$$

$$\exists x [\text{barber}(x) \wedge [\forall y [\neg [\text{townsman}(y) \wedge \neg \text{shaves}(y,y)] \vee \text{shaves}(x,y)]]]$$

Problem & Solution

- *There is a barber who shaves all men in town who do not shave themselves.*

$$\exists x [\text{barber}(x) \wedge [\forall y [\text{townsman}(y) \wedge \neg \text{shaves}(y,y) \Rightarrow \text{shaves}(x,y)]]]$$

$$\Leftrightarrow$$

$$\exists x [\text{barber}(x) \wedge [\forall y [\neg [\text{townsman}(y) \wedge \neg \text{shaves}(y,y)] \vee \text{shaves}(x,y)]]]$$

$$\Leftrightarrow$$

$$\exists x [\text{barber}(x) \wedge [\forall y \neg [\text{townsman}(y) \wedge \neg \text{shaves}(y,y) \wedge \neg \text{shaves}(x,y)]]]$$

Problem & Solution

- *There is a barber who shaves all men in town who do not shave themselves.*

$$\exists x [\text{barber}(x) \wedge [\forall y [\text{townsman}(y) \wedge \neg \text{shaves}(y,y) \Rightarrow \text{shaves}(x,y)]]]$$

$$\Leftrightarrow$$

$$\exists x [\text{barber}(x) \wedge [\forall y [\neg [\text{townsman}(y) \wedge \neg \text{shaves}(y,y)] \vee \text{shaves}(x,y)]]]$$

$$\Leftrightarrow$$

$$\exists x [\text{barber}(x) \wedge [\forall y \neg [\text{townsman}(y) \wedge \neg \text{shaves}(y,y) \wedge \neg \text{shaves}(x,y)]]]$$

$$\Leftrightarrow$$

$$\exists x [\text{barber}(x) \wedge [\neg \exists y [\text{townsman}(y) \wedge \neg \text{shaves}(y,y) \wedge \neg \text{shaves}(x,y)]]]$$

Problem & Solution

- *No person likes a professor unless the professor is smart.*

Problem & Solution

- *No person likes a professor unless the professor is smart.*

$$\forall x \forall y [\text{person}(x) \wedge \text{professor}(y) \Rightarrow [\text{likes}(x,y) \Rightarrow \text{smart}(y)]]$$

Problem & Solution

- *No person likes a professor unless the professor is smart.*

$$\forall x \forall y [\text{person}(x) \wedge \text{professor}(y) \Rightarrow [\text{likes}(x,y) \Rightarrow \text{smart}(y)]] \Leftrightarrow$$

$$\forall x \forall y [\text{person}(x) \wedge \text{professor}(y) \Rightarrow [\neg \text{likes}(x,y) \vee \text{smart}(y)]]$$

Problem & Solution

- *No person likes a professor unless the professor is smart.*

$$\forall x \forall y [\text{person}(x) \wedge \text{professor}(y) \Rightarrow [\text{likes}(x,y) \Rightarrow \text{smart}(y)]] \Leftrightarrow$$

$$\forall x \forall y [\text{person}(x) \wedge \text{professor}(y) \Rightarrow [\neg \text{likes}(x,y) \vee \text{smart}(y)]] \Leftrightarrow$$

$$\forall x \forall y [\neg [\text{person}(x) \wedge \text{professor}(y)] \vee [\neg \text{likes}(x,y) \vee \text{smart}(y)]]$$

Problem & Solution

- *No person likes a professor unless the professor is smart.*

$$\forall x \forall y [\text{person}(x) \wedge \text{professor}(y) \Rightarrow [\text{likes}(x,y) \Rightarrow \text{smart}(y)]] \Leftrightarrow$$

$$\forall x \forall y [\text{person}(x) \wedge \text{professor}(y) \Rightarrow [\neg \text{likes}(x,y) \vee \text{smart}(y)]] \Leftrightarrow$$

$$\forall x \forall y [\neg [\text{person}(x) \wedge \text{professor}(y)] \vee [\neg \text{likes}(x,y) \vee \text{smart}(y)]] \Leftrightarrow$$

$$\forall x \forall y [\neg [\text{person}(x) \wedge \text{professor}(y)] \vee \neg [\text{likes}(x,y) \wedge \neg \text{smart}(y)]]$$

Problem & Solution

- *No person likes a professor unless the professor is smart.*

$$\forall x \forall y [\text{person}(x) \wedge \text{professor}(y) \Rightarrow [\text{likes}(x,y) \Rightarrow \text{smart}(y)]] \Leftrightarrow$$

$$\forall x \forall y [\text{person}(x) \wedge \text{professor}(y) \Rightarrow [\neg \text{likes}(x,y) \vee \text{smart}(y)]] \Leftrightarrow$$

$$\forall x \forall y [\neg [\text{person}(x) \wedge \text{professor}(y)] \vee [\neg \text{likes}(x,y) \vee \text{smart}(y)]] \Leftrightarrow$$

$$\forall x \forall y [\neg [\text{person}(x) \wedge \text{professor}(y)] \vee \neg [\text{likes}(x,y) \wedge \neg \text{smart}(y)]] \Leftrightarrow$$

$$\forall x \forall y \neg [\text{person}(x) \wedge \text{professor}(y) \wedge \text{likes}(x,y) \wedge \neg \text{smart}(y)]$$

Problem & Solution

- *No person likes a professor unless the professor is smart.*

$$\forall x \forall y [\text{person}(x) \wedge \text{professor}(y) \Rightarrow [\text{likes}(x,y) \Rightarrow \text{smart}(y)]] \Leftrightarrow$$

$$\forall x \forall y [\text{person}(x) \wedge \text{professor}(y) \Rightarrow [\neg \text{likes}(x,y) \vee \text{smart}(y)]] \Leftrightarrow$$

$$\forall x \forall y [\neg [\text{person}(x) \wedge \text{professor}(y)] \vee [\neg \text{likes}(x,y) \vee \text{smart}(y)]] \Leftrightarrow$$

$$\forall x \forall y [\neg [\text{person}(x) \wedge \text{professor}(y)] \vee \neg [\text{likes}(x,y) \wedge \neg \text{smart}(y)]] \Leftrightarrow$$

$$\forall x \forall y \neg [\text{person}(x) \wedge \text{professor}(y) \wedge \text{likes}(x,y) \wedge \neg \text{smart}(y)] \Leftrightarrow$$

$$\neg \exists x \exists y [\text{person}(x) \wedge \text{professor}(y) \wedge \text{likes}(x,y) \wedge \neg \text{smart}(y)]$$

Problem & Solution

- *Only one person failed both history and biology.*

Problem & Solution

- *Only one person failed both history and biology.*

$$\exists!x \text{ student}(x) \wedge \text{failed}(x, \text{hist}) \wedge \text{failed}(x, \text{bio})$$

Problem & Solution

- *Only one person failed both history and biology.*

$$\exists!x \text{ student}(x) \wedge \text{failed}(x, \text{hist}) \wedge \text{failed}(x, \text{bio})$$

Note that: $\exists!x p(x) \Leftrightarrow \exists x p(x) \wedge [\forall y [p(y) \Rightarrow x=y]]$

Problem & Solution

- *Politicians can fool some of the people all the time, and they can fool all of the people some of the time, but they can't fool all the people all of the time.*

Problem & Solution

- *Politicians can fool some of the people all the time, and they can fool all of the people some of the time, but they can't fool all the people all of the time.*

$\forall x [\text{politician}(x) \Rightarrow [\exists y \text{ people}(y) \wedge [\forall t \text{ time}(t) \Rightarrow \text{fool}(x,y,t)]]]$

Problem & Solution

- *Politicians can fool some of the people all the time, and **they can fool all of the people some of the time**, but they can't fool all the people all of the time.*

$\forall x [\text{politician}(x) \Rightarrow [\exists y \text{ people}(y) \wedge [\forall t \text{ time}(t) \Rightarrow \text{fool}(x,y,t)]]]$

$\forall x [\text{politician}(x) \Rightarrow [\exists t \text{ time}(t) \wedge [\forall y \text{ people}(y) \Rightarrow \text{fool}(x,y,t)]]]$

Problem & Solution

- *Politicians can fool some of the people all the time, and they can fool all of the people some of the time, but **they can't fool all the people all of the time.***

$\forall x [\text{politician}(x) \Rightarrow [\exists y \text{ people}(y) \wedge [\forall t \text{ time}(t) \Rightarrow \text{fool}(x,y,t)]]]$

$\forall x [\text{politician}(x) \Rightarrow [\exists t \text{ time}(t) \wedge [\forall y \text{ people}(y) \Rightarrow \text{fool}(x,y,t)]]]$

$\forall x [\text{politician}(x) \Rightarrow \neg[\forall y \forall t [\text{people}(y) \wedge \text{time}(t)] \Rightarrow \text{fool}(x,y,t)]]]$

Exercises: Artificial Intelligence

Planning & Logic: And-Or-If

Planning & Logic: And-Or-If

PROBLEM & SOLUTION

Problem & Solution

- *One more outburst like that and you are in contempt of court.*

Problem & Solution

- *One more outburst like that and you are in contempt of court.*

outburst \Rightarrow court

Problem & Solution

- *One more outburst like that and you are in contempt of court.*

outburst \Rightarrow court

NOT: outburst \wedge court

Problem & Solution

- *Either the Red Sox win or I'm out ten dollars.*

Problem & Solution

- *Either the Red Sox win or I'm out ten dollars.*

$$\text{redSoxWin} \Leftrightarrow \neg \text{outTenDollars}$$

Problem & Solution

- *Either the Red Sox win or I'm out ten dollars.*

$\text{redSoxWin} \Leftrightarrow \neg \text{outTenDollars}$

NOT: $\text{redSoxWin} \vee \text{outTenDollars}$

Problem & Solution

- *Maybe I'll come to the party and maybe I won't.*

Problem & Solution

- *Maybe I'll come to the party and maybe I won't.*

$\text{maybeComeToParty} \vee \neg \text{maybeComeToParty}$

Problem & Solution

- *Maybe I'll come to the party and maybe I won't.*

$\text{maybeComeToParty} \vee \neg \text{maybeComeToParty}$

NOT: $\text{maybeComeToParty} \wedge \neg \text{maybeComeToParty}$

Exercises: Artificial Intelligence

Planning & Logic: Weird Logic

Planning & Logic: Weird Logic

PROBLEM & SOLUTION

Problem & Solution

- *I don't jump off the Empire State Building implies if I jump off the Empire State Building, then I float safely to the ground.*

Problem & Solution

- *I don't jump off the Empire State Building implies if I jump off the Empire State Building, then I float safely to the ground.*
 - *Translating the meaning of the sentence is not possible*

Problem & Solution

- *I don't jump off the Empire State Building implies if I jump off the Empire State Building, then I float safely to the ground.*

– *Translating the meaning of the sentence is not possible*

$$\neg \text{jumpESB} \Rightarrow [\text{jumpESB} \Rightarrow \text{floatTTGround}]$$

Problem & Solution

- *I don't jump off the Empire State Building implies if I jump off the Empire State Building, then I float safely to the ground.*
 - *Translating the meaning of the sentence is not possible*

$$\neg \text{jumpESB} \Rightarrow [\text{jumpESB} \Rightarrow \text{floatTTGround}] \Leftrightarrow$$

$$\neg \text{jumpESB} \Rightarrow [\neg \text{jumpESB} \vee \text{floatTTGround}]$$

Problem & Solution

- *I don't jump off the Empire State Building implies if I jump off the Empire State Building, then I float safely to the ground.*
 - *Translating the meaning of the sentence is not possible*

$$\begin{aligned}\neg \text{jumpESB} &\Rightarrow [\text{jumpESB} \Rightarrow \text{floatTTGround}] \Leftrightarrow \\ \neg \text{jumpESB} &\Rightarrow [\neg \text{jumpESB} \vee \text{floatTTGround}] \Leftrightarrow \\ &\text{jumpESB} \vee \neg \text{jumpESB} \vee \text{floatTTGround}\end{aligned}$$

Problem & Solution

- *It is not the case that if you attempt this exercise you will get an F. Therefore, you will attempt this exercise.*

Problem & Solution

- *It is not the case that if you attempt this exercise you will get an F. Therefore, you will attempt this exercise.*
 - *Translating the meaning of the sentence is not possible*

Problem & Solution

- *It is not the case that if you attempt this exercise you will get an F. Therefore, you will attempt this exercise.*
 - *Translating the meaning of the sentence is not possible*

$$\neg[\text{attempt} \Rightarrow \text{getF}] \Rightarrow \text{attempt}$$

Problem & Solution

- *It is not the case that if you attempt this exercise you will get an F. Therefore, you will attempt this exercise.*
 - *Translating the meaning of the sentence is not possible*

$$\neg[\text{attempt} \Rightarrow \text{getF}] \Rightarrow \text{attempt} \Leftrightarrow$$
$$\neg[\neg\text{attempt} \vee \text{getF}] \Rightarrow \text{attempt}$$

Problem & Solution

- *It is not the case that if you attempt this exercise you will get an F. Therefore, you will attempt this exercise.*

– *Translating the meaning of the sentence is not possible*

$$\neg[\text{attempt} \Rightarrow \text{getF}] \Rightarrow \text{attempt} \Leftrightarrow$$

$$\neg[\neg\text{attempt} \vee \text{getF}] \Rightarrow \text{attempt} \Leftrightarrow$$

$$[\text{attempt} \wedge \neg\text{getF}] \Rightarrow \text{attempt}$$

Problem & Solution

- *It is not the case that if you attempt this exercise you will get an F. Therefore, you will attempt this exercise.*
 - *Translating the meaning of the sentence is not possible*

$$\neg[\text{attempt} \Rightarrow \text{getF}] \Rightarrow \text{attempt} \Leftrightarrow$$

$$\neg[\neg\text{attempt} \vee \text{getF}] \Rightarrow \text{attempt} \Leftrightarrow$$

$$\neg\text{attempt} \vee \text{getF} \vee \text{attempt}$$