

Exercises: Artificial Intelligence

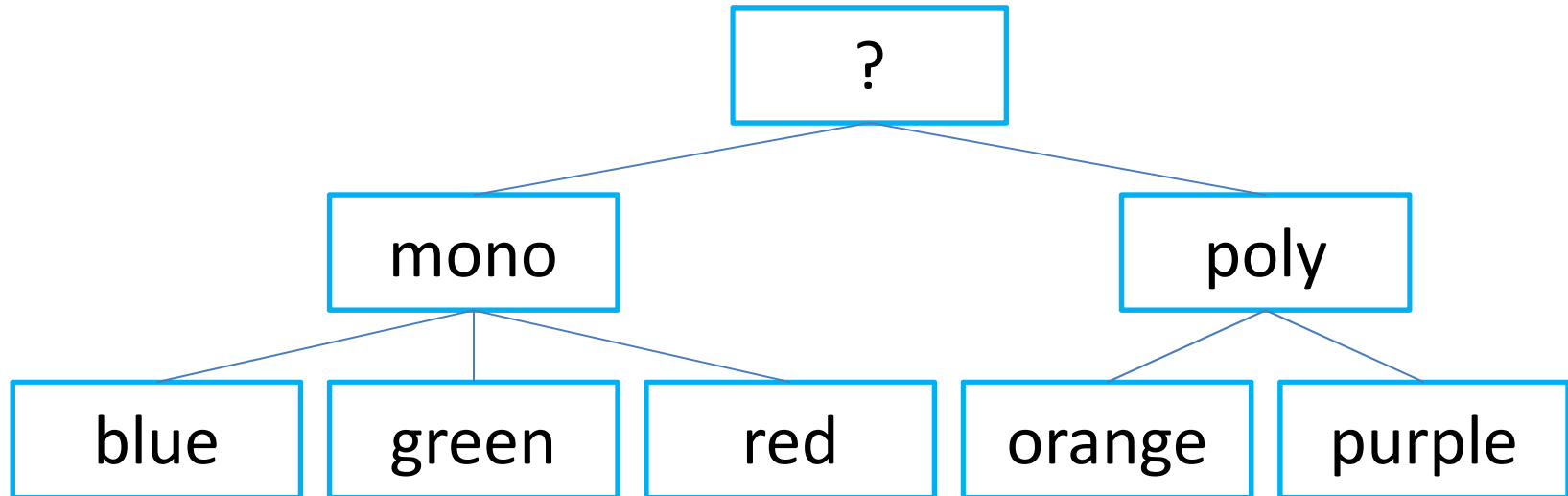
Version Spaces: Colors

Version Spaces: Colors

PROBLEM

Problem

- Consider the following concept hierarchy

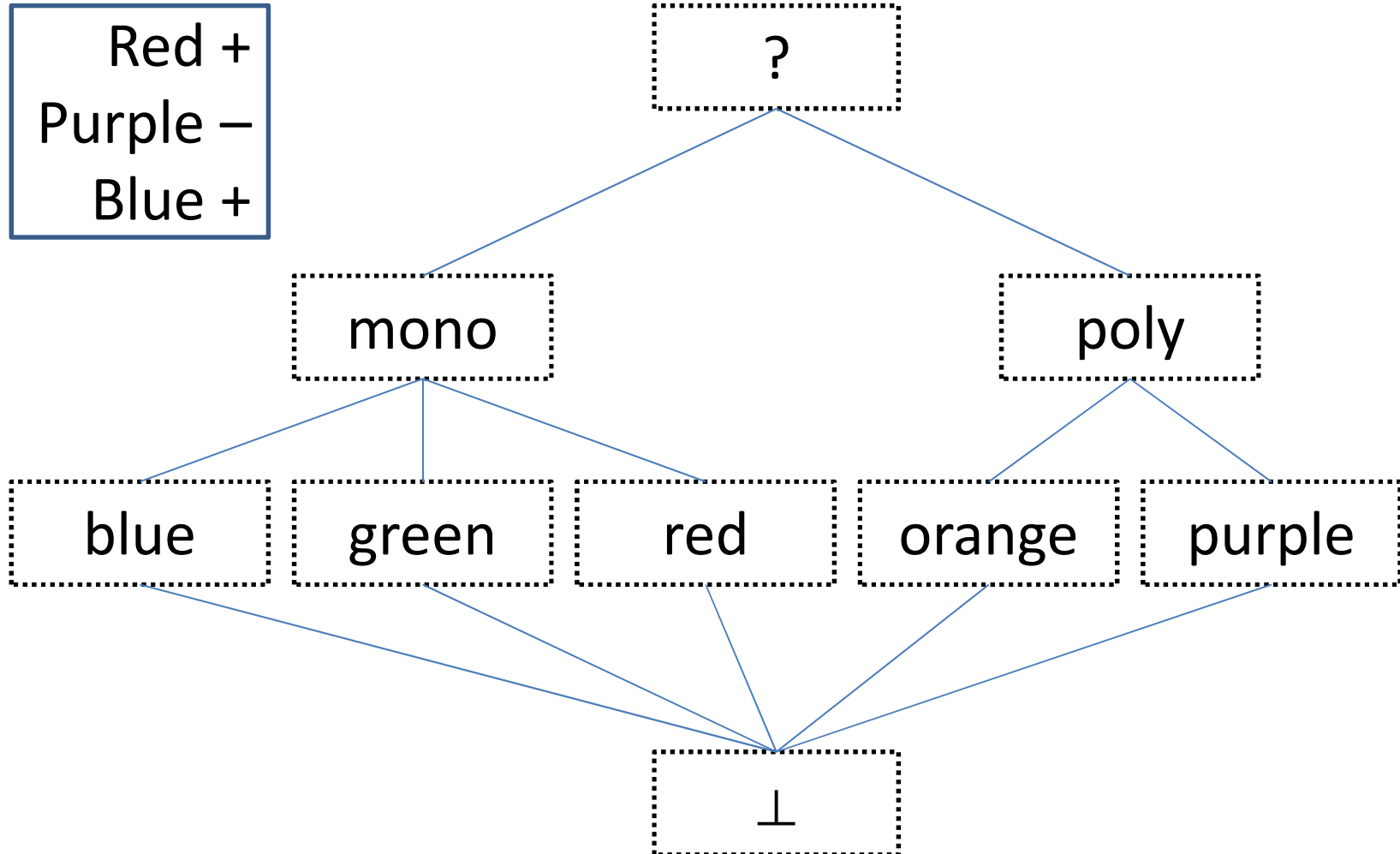


- Apply the Version-Space algorithm on:
red: + purple: – blue: +

Version Spaces: Colors

PROBLEM OVERVIEW

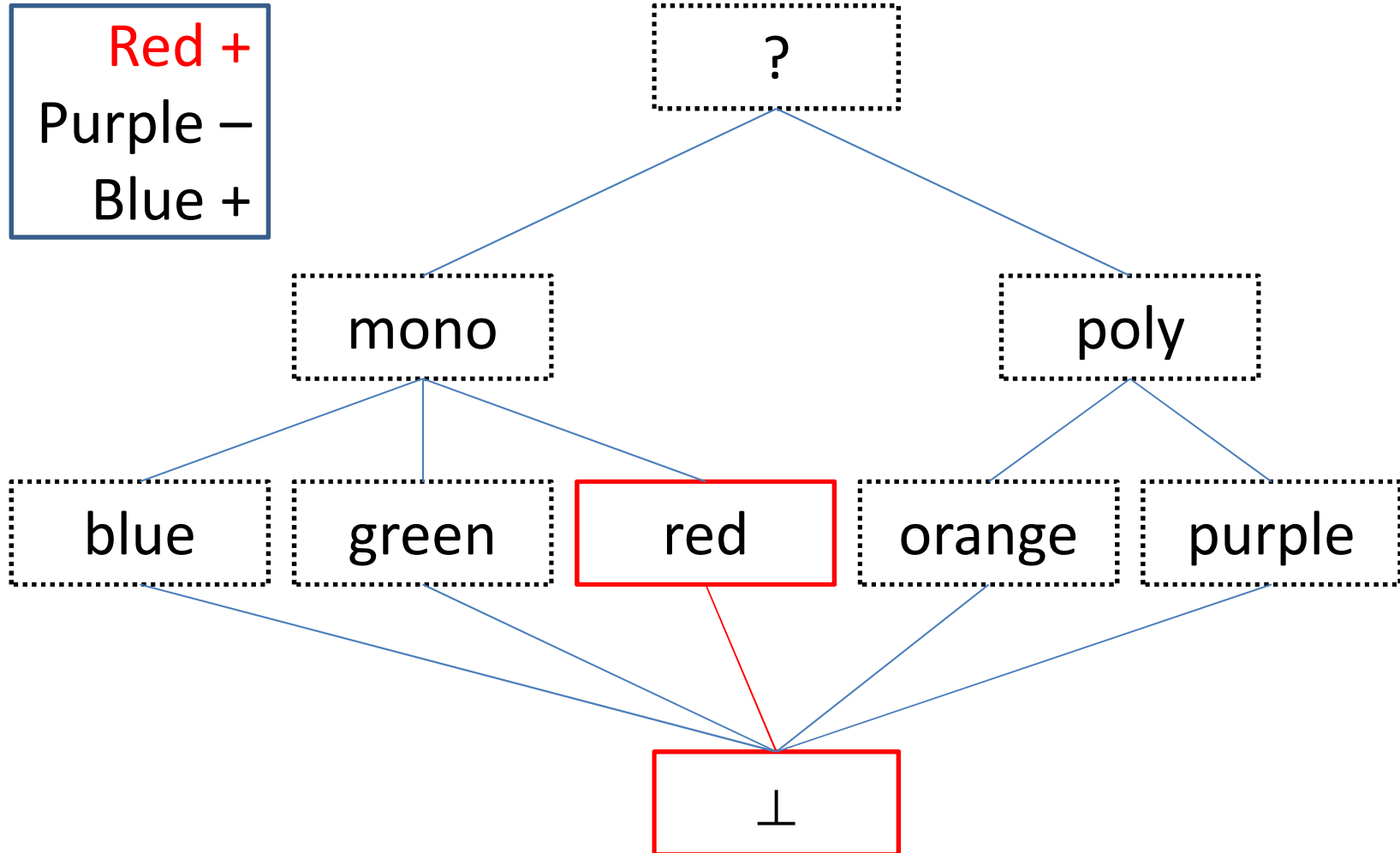
Problem overview



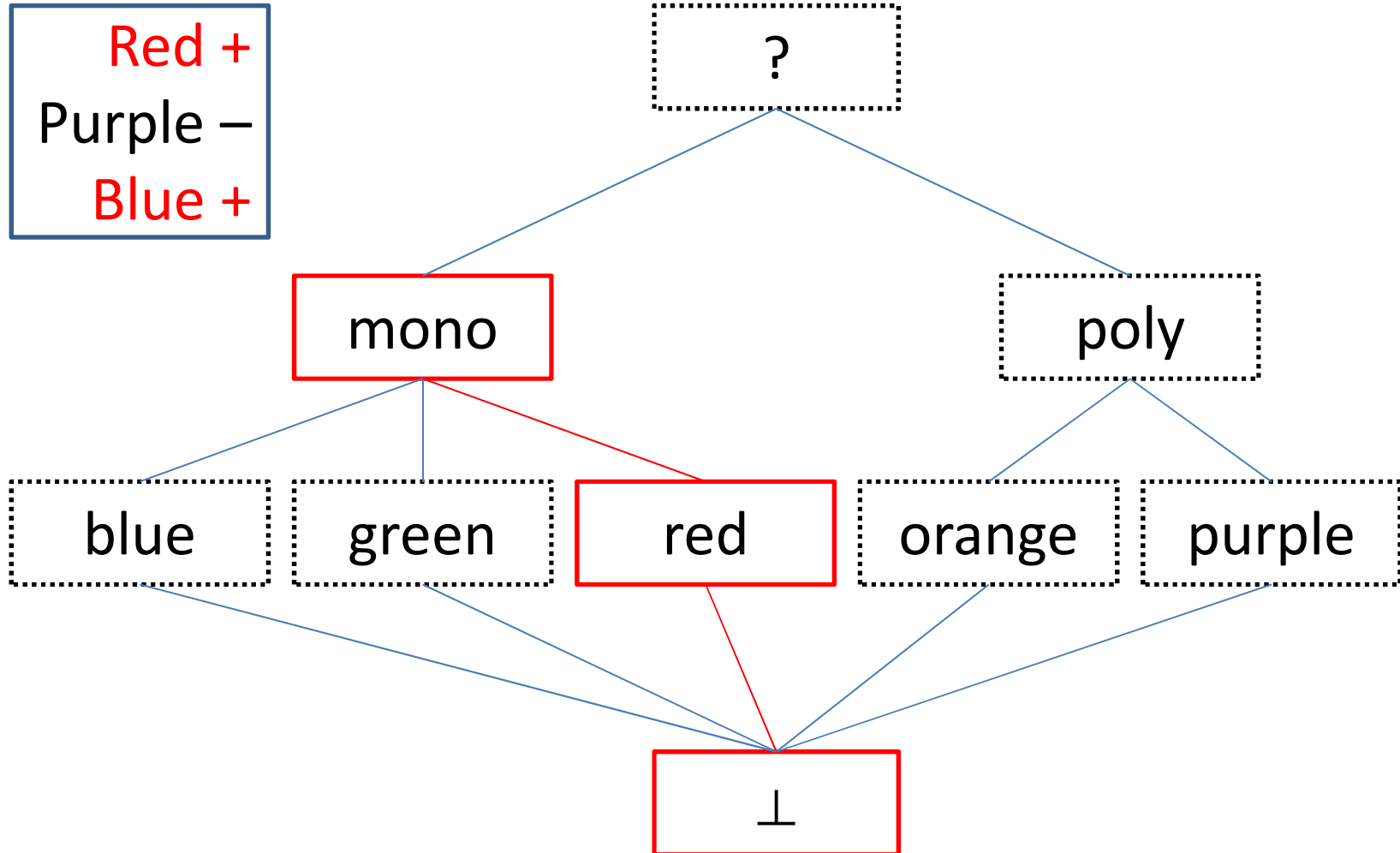
Version Spaces: Colors

FIND-S ALGORITHM

Find-S Algorithm



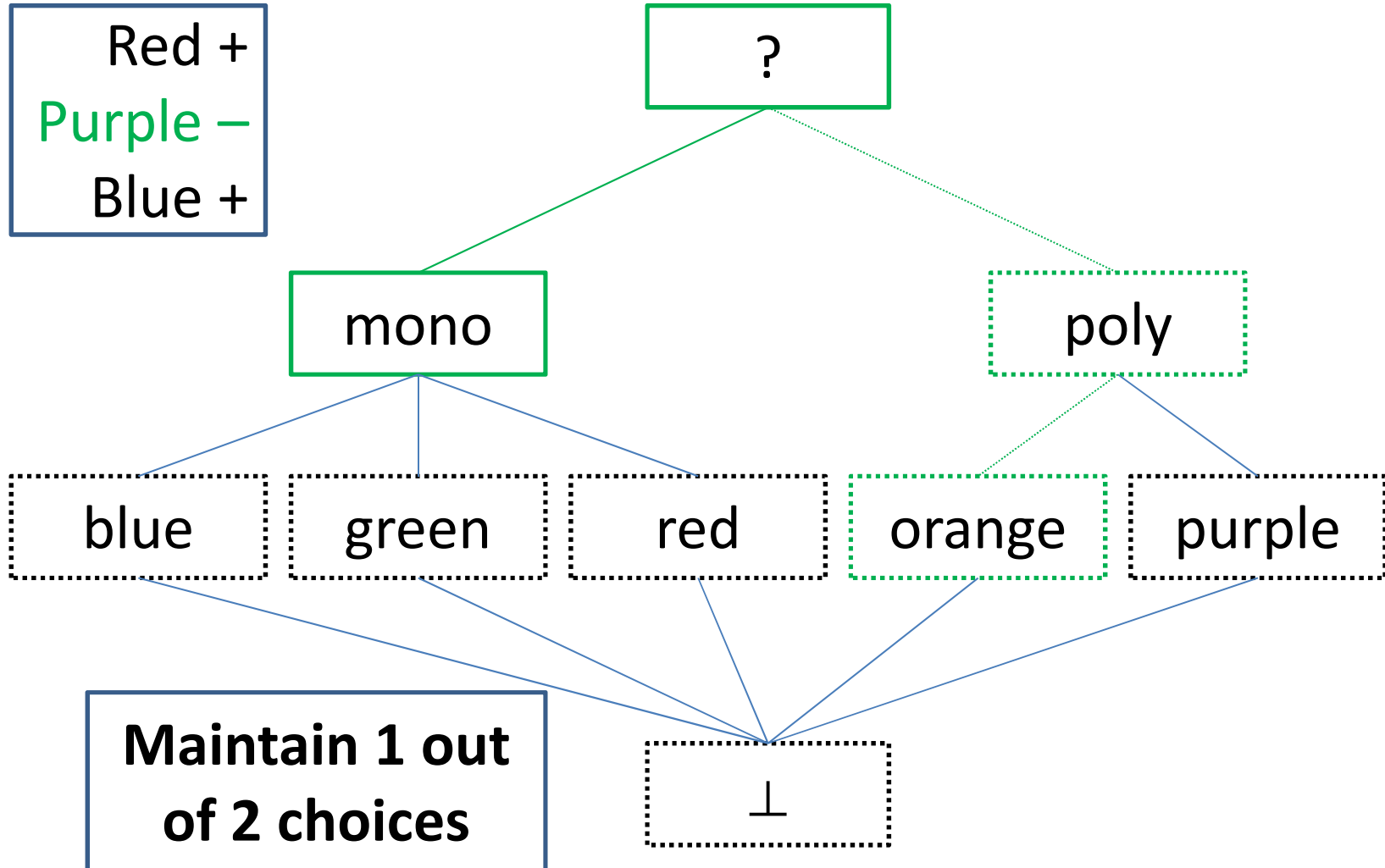
Find-S Algorithm



Version Spaces: Colors

DUAL FIND-S ALGORITHM

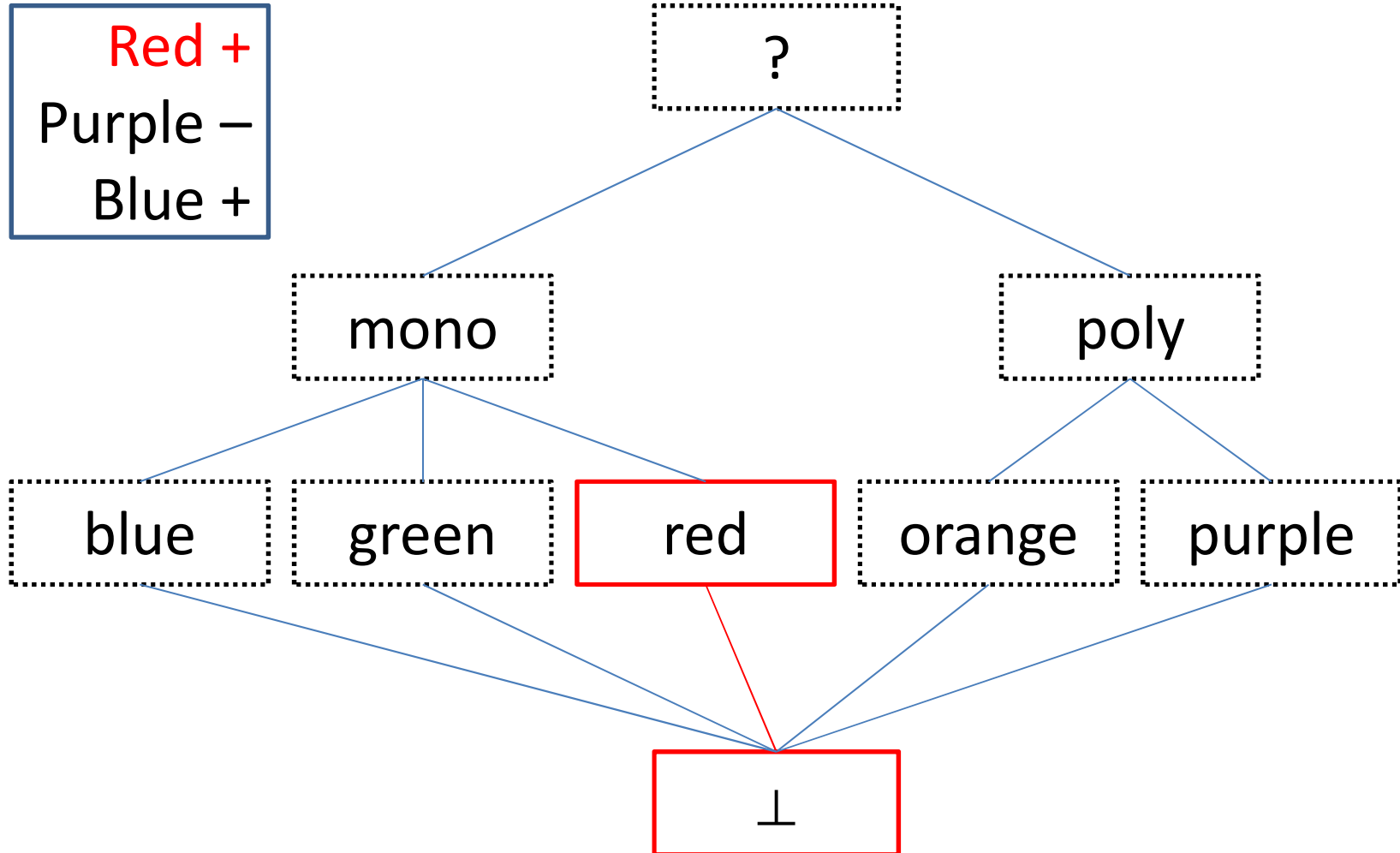
Dual Find-S Algorithm



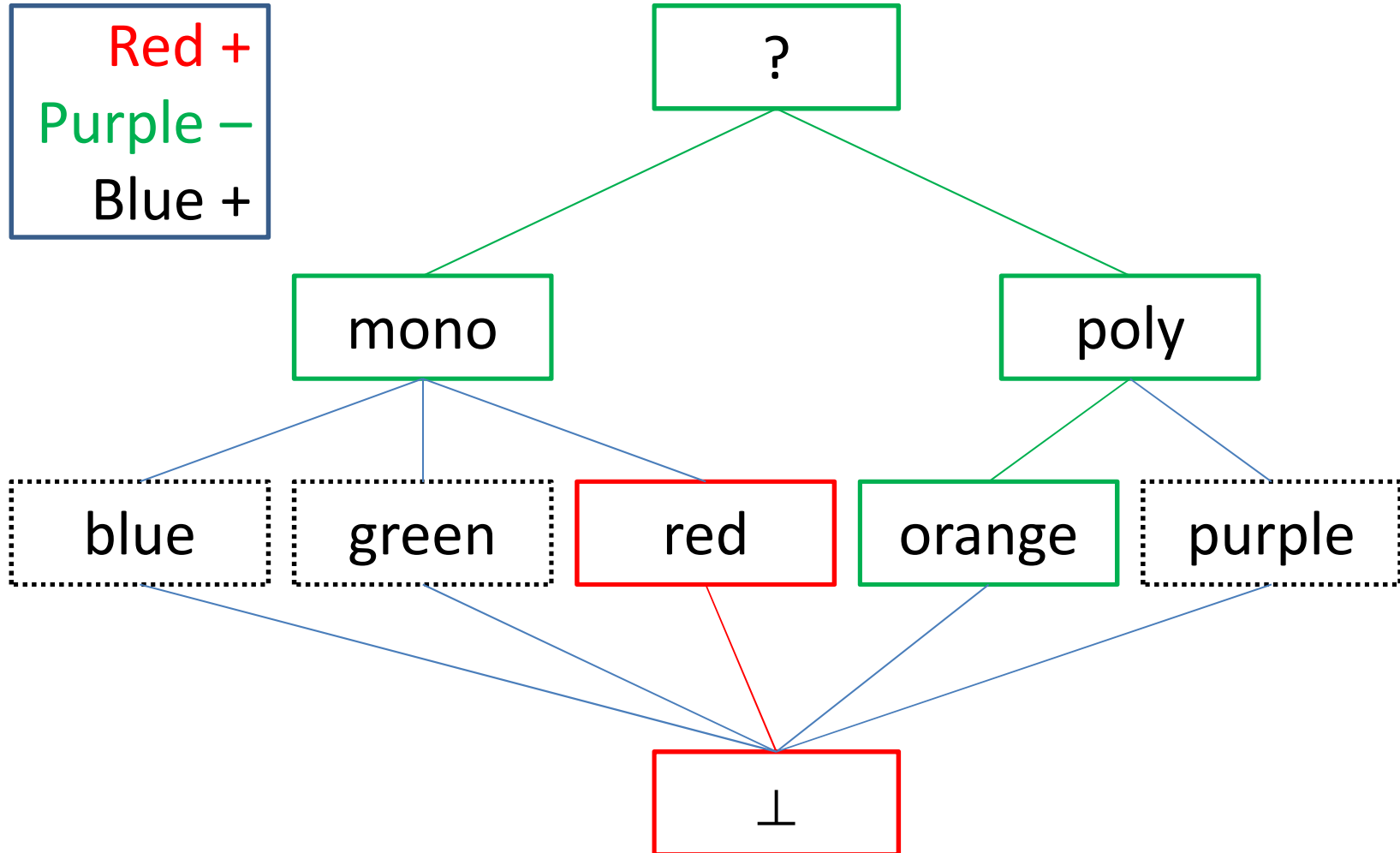
Version Spaces: Colors

VERSION-SPACES ALGORITHM

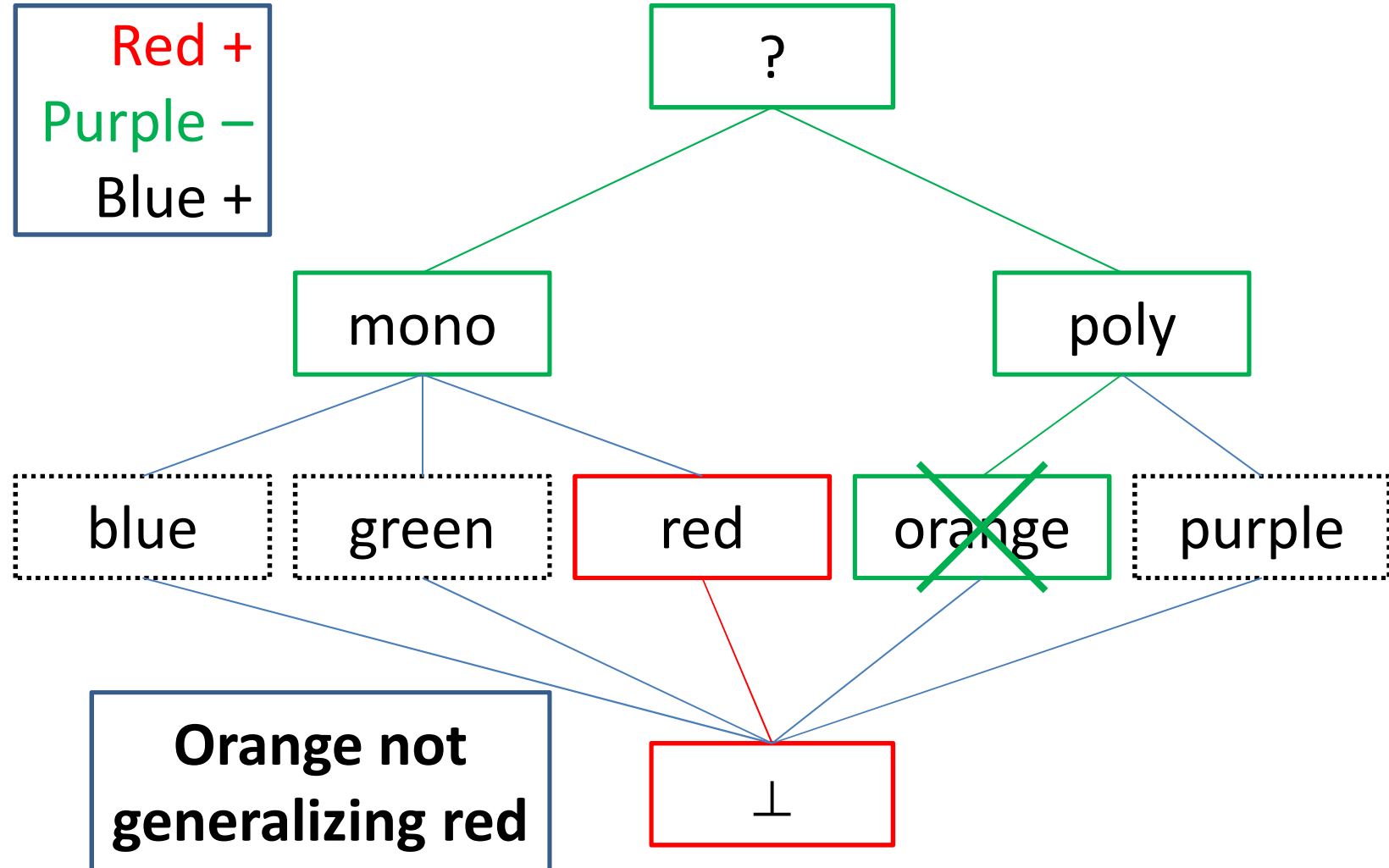
Version-Spaces Algorithm



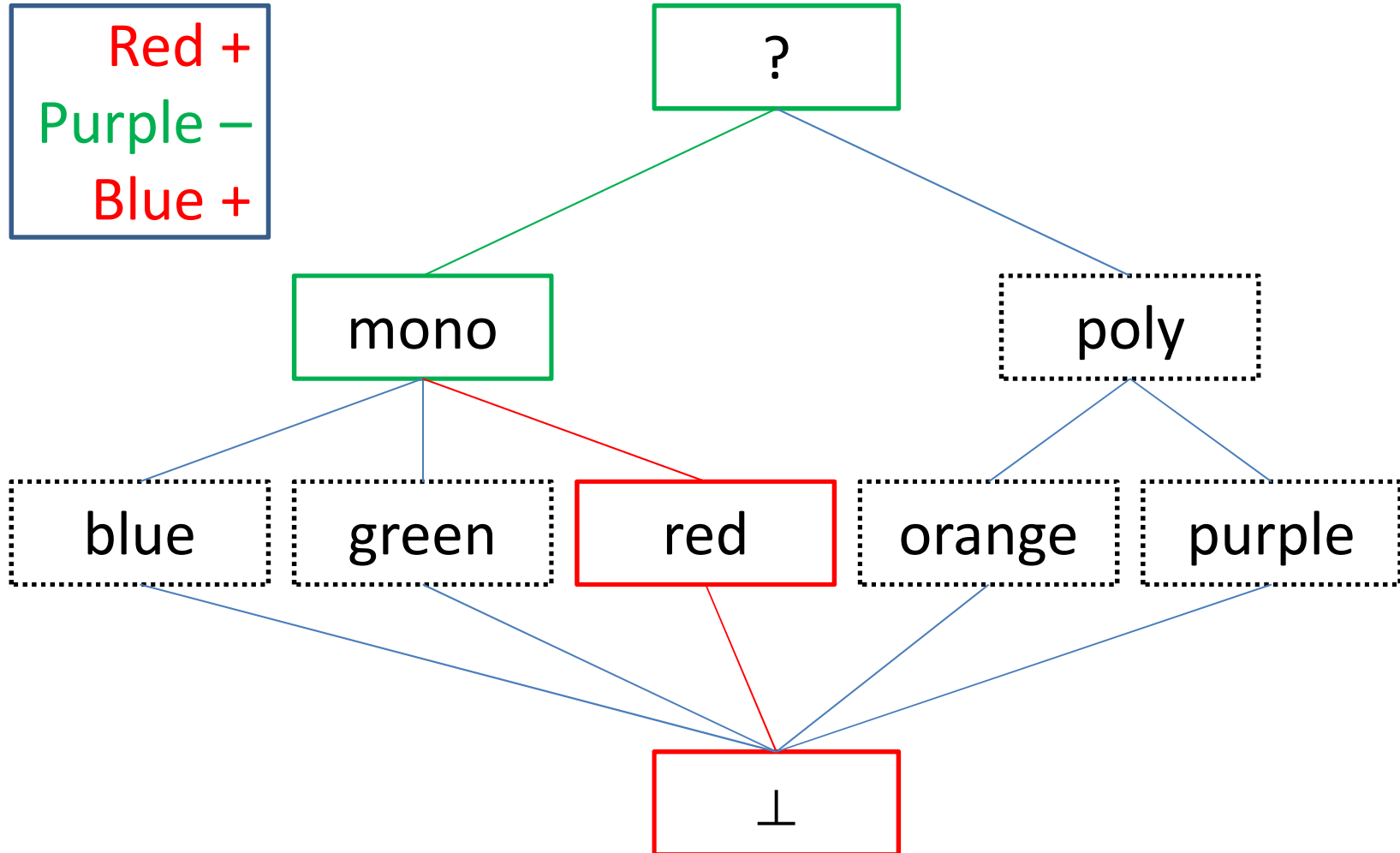
Version-Spaces Algorithm



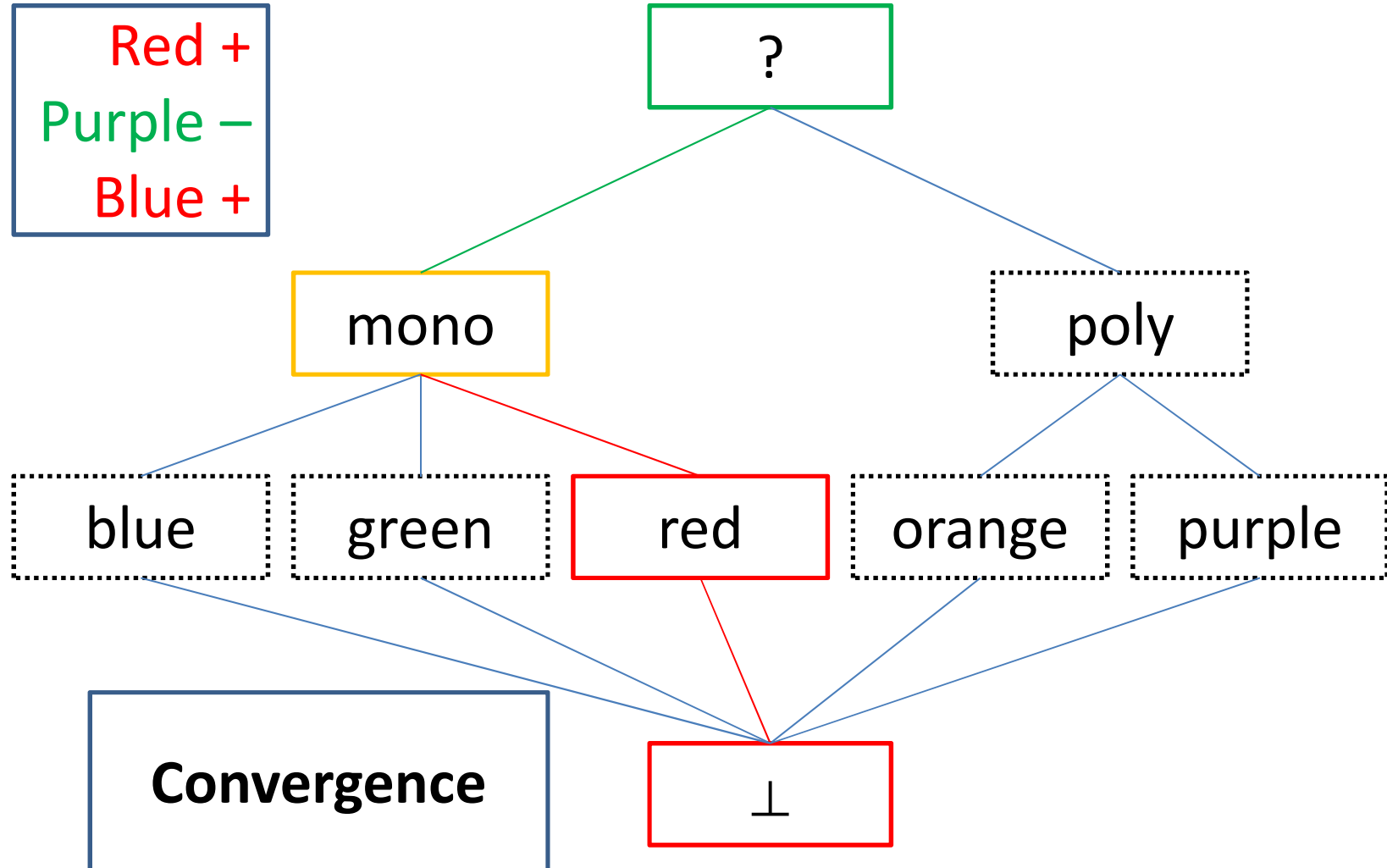
Version-Spaces Algorithm



Version-Spaces Algorithm



Version-Spaces Algorithm



Exercises: Artificial Intelligence

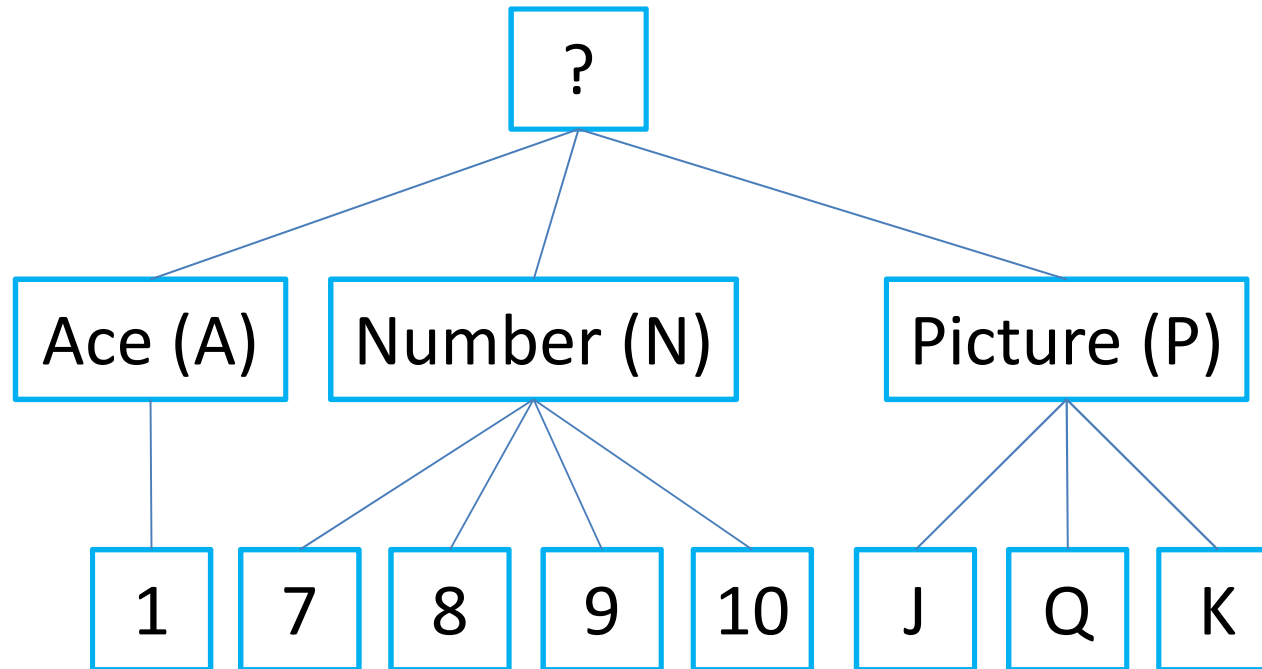
Version Spaces: Playing Cards

Version Spaces: Playing Cards

PROBLEM

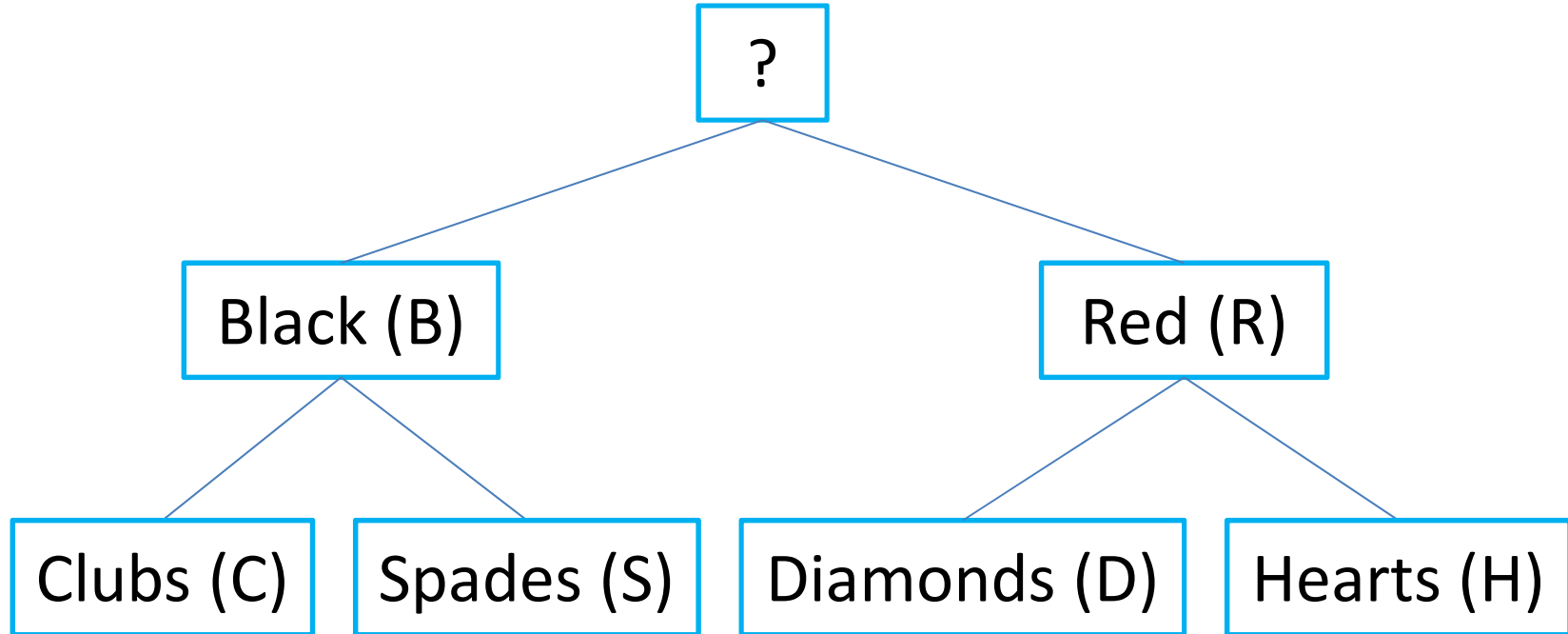
Problem

- The concept hierarchies for *value*:



Problem

- The concept hierarchies for *kind*:



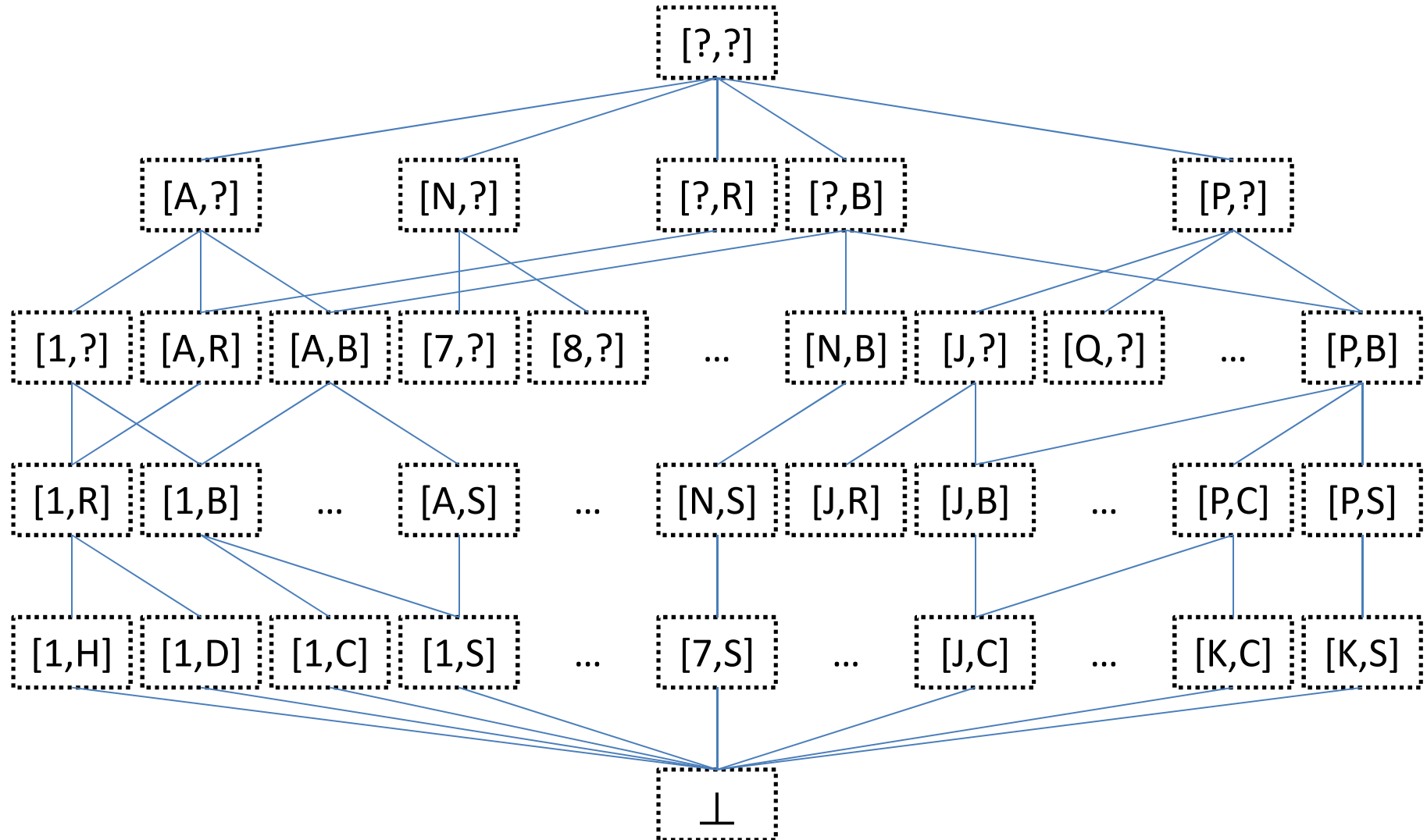
Problem

- ***Examples:***
 - 7 of Diamonds +
 - Ace of Clubs −
 - Queen of Hearts −
 - 9 of Hearts +
 - 8 of Clubs −

Version Spaces: Playing Cards

PROBLEM OVERVIEW

Problem overview (Fragment)



Version Spaces: Playing Cards

FIND-S ALGORITHM

Find-S Algorithm

[7,D] +

[A,C] -

[Q,H] -

[9,H] +

[8,C] -

[?,?]

[7,D]

⊥

Find-S Algorithm

[7,D] +
[A,C] –
[Q,H] –
[9,H] +
[8,C] –

[?,?]

[N,R]

[7,R]

[7,D]

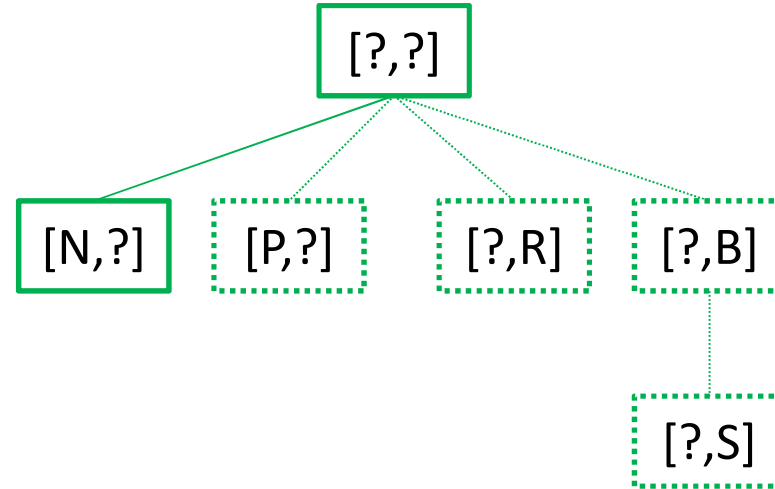
⊥

Version Spaces: Playing Cards

DUAL FIND-S ALGORITHM

Dual Find-S Algorithm

[7,D] +
[A,C] -
[Q,H] -
[9,H] +
[8,C] -

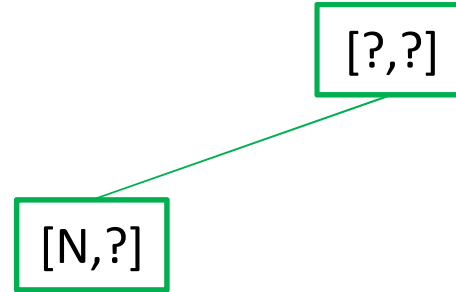


**Maintain 1 out
of 4 choices**

⊥

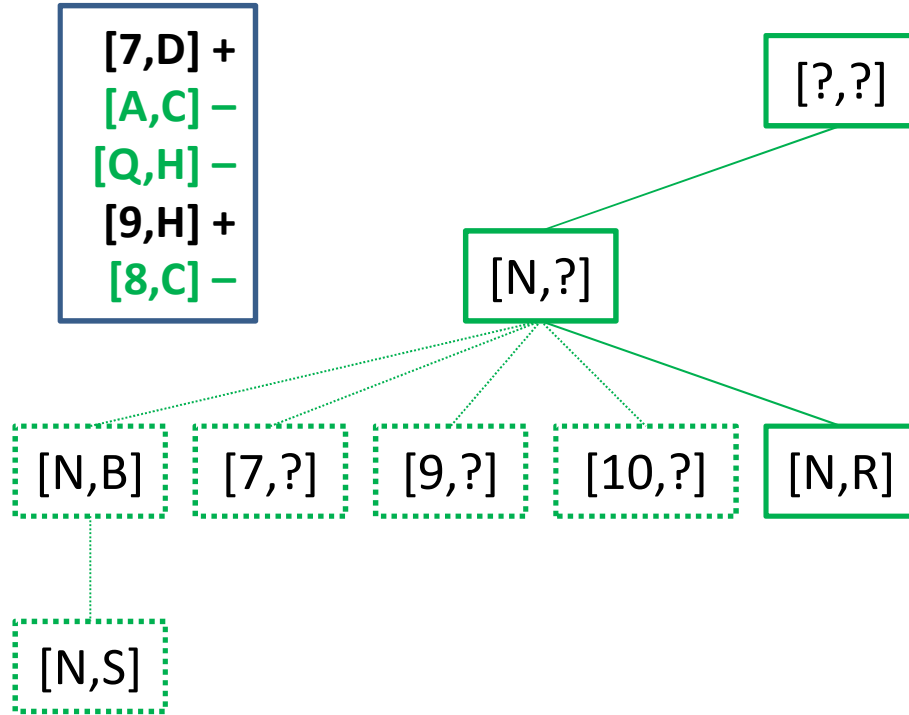
Dual Find-S Algorithm

[7,D] +
[A,C] -
[Q,H] -
[9,H] +
[8,C] -



⊥

Dual Find-S Algorithm

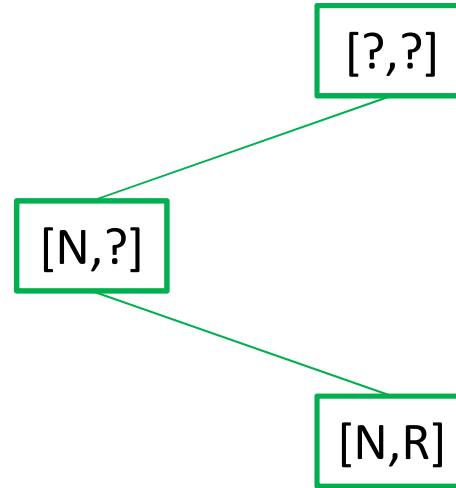


**Maintain 1 out
of 5 choices**

\perp

Dual Find-S Algorithm

[7,D] +
[A,C] -
[Q,H] -
[9,H] +
[8,C] -



⊥

Version Spaces: Playing Cards

VERSION-SPACES ALGORITHM

Version-Spaces Algorithm

[7,D] +
[A,C] −
[Q,H] −
[9,H] +
[8,C] −

[?,?]

[7,D]

⊥

Version-Spaces Algorithm

[7,D] +
[A,C] –
[Q,H] –
[9,H] +
[8,C] –

[?,?]

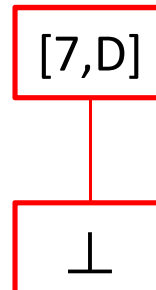
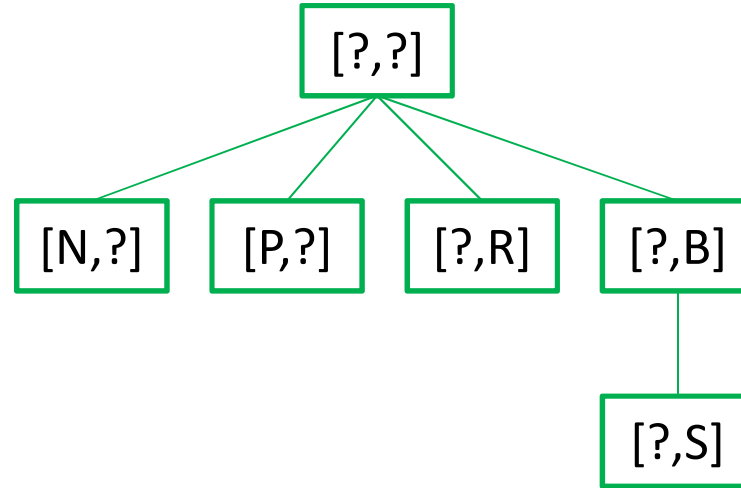
[7,D]

⊥

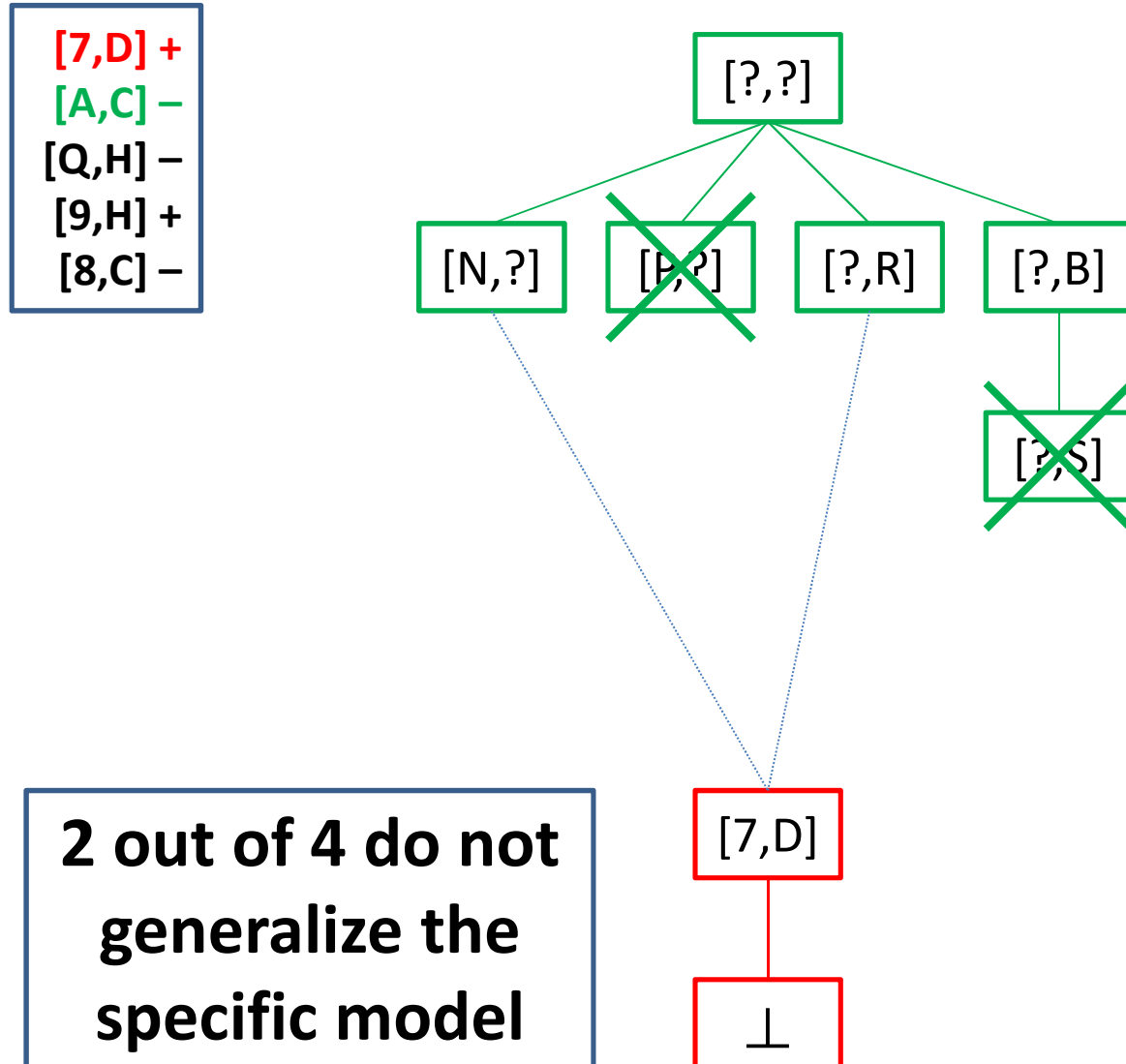


Version-Spaces Algorithm

[7,D] +
[A,C] -
[Q,H] -
[9,H] +
[8,C] -

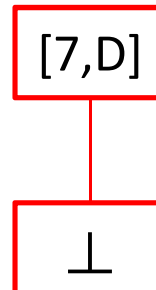
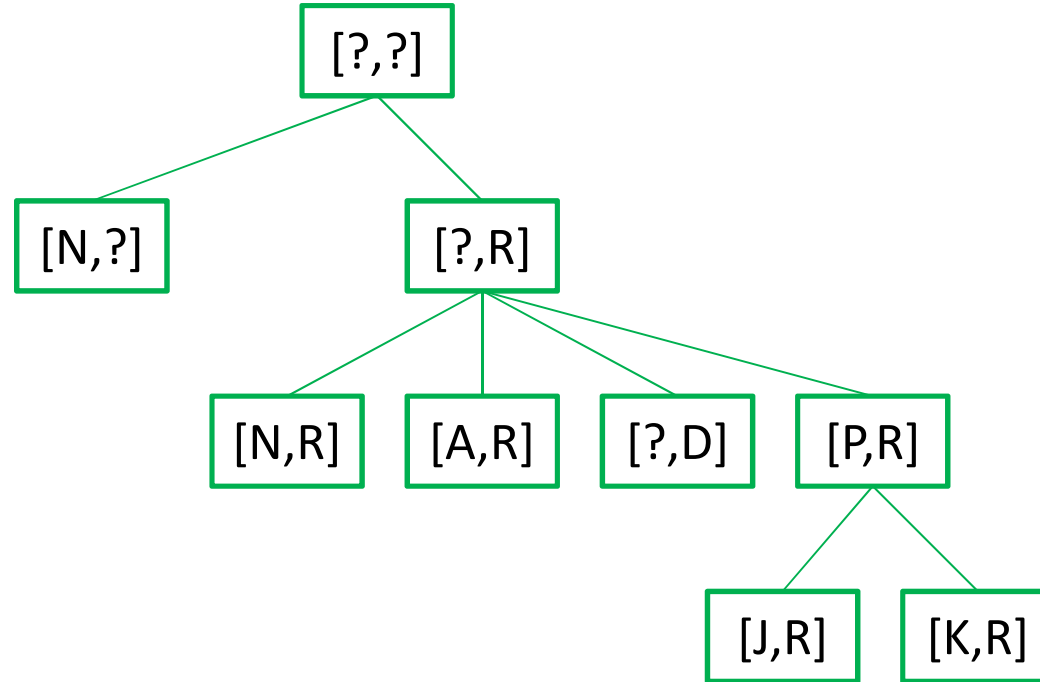


Version-Spaces Algorithm

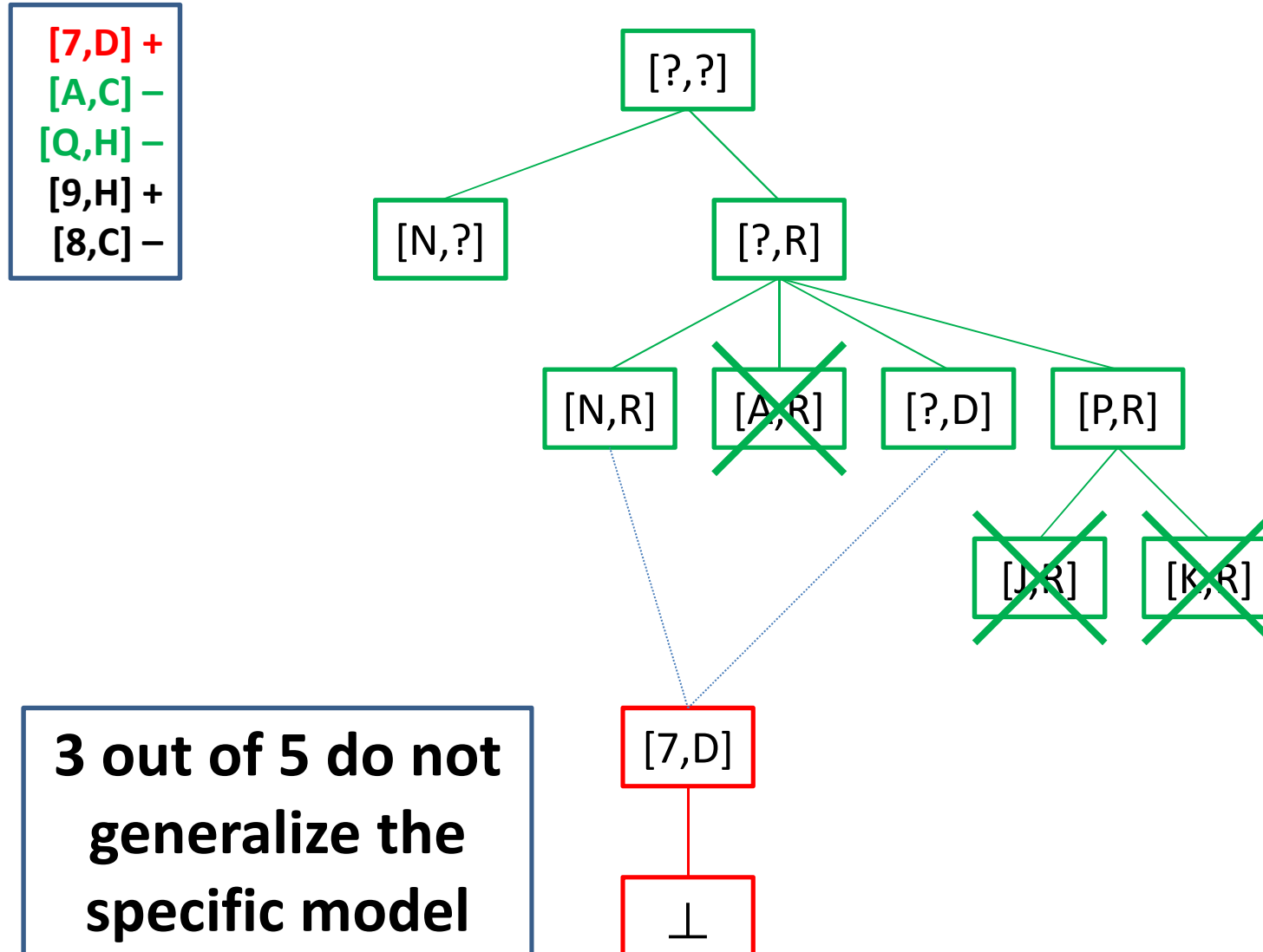


Version-Spaces Algorithm

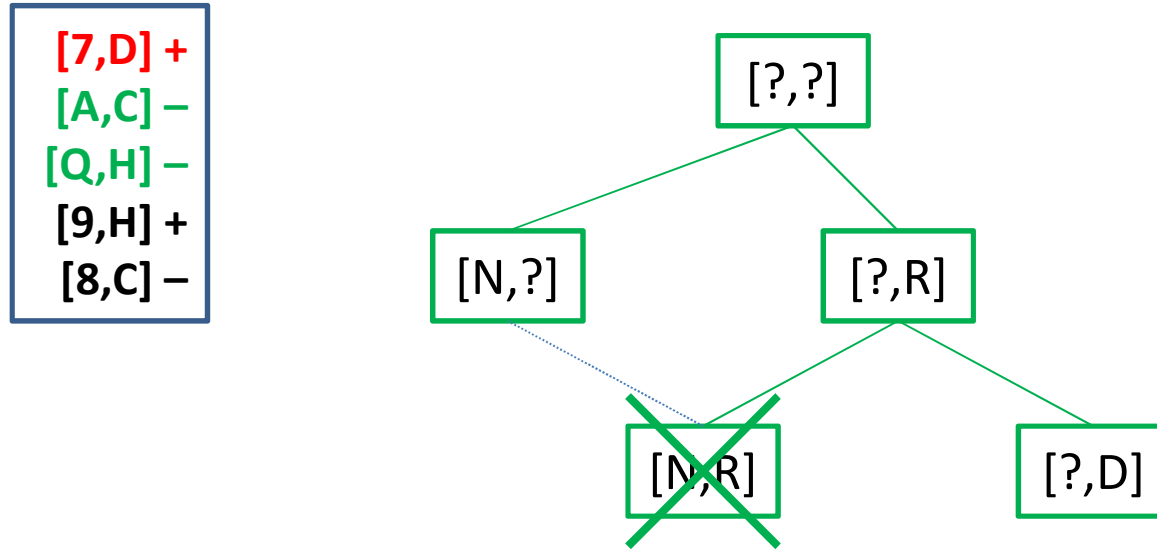
[7,D] +
[A,C] -
[Q,H] -
[9,H] +
[8,C] -



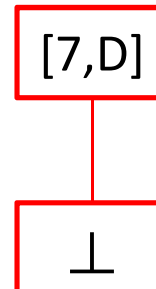
Version-Spaces Algorithm



Version-Spaces Algorithm

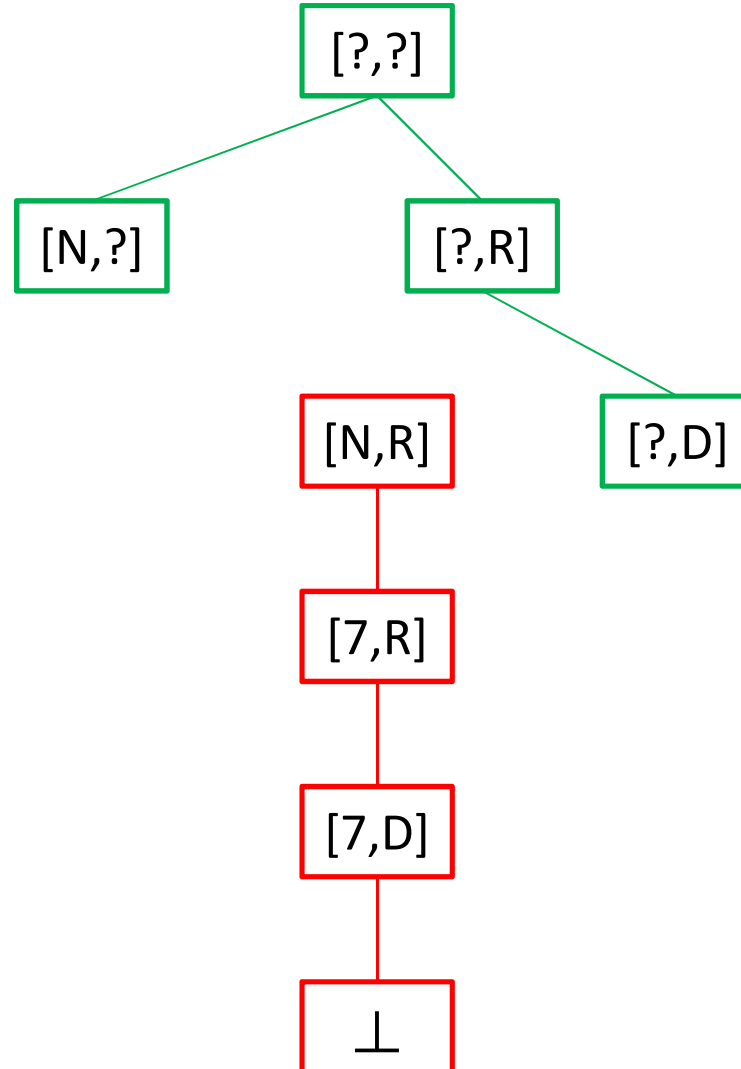


**Redundant
Hypotheses**

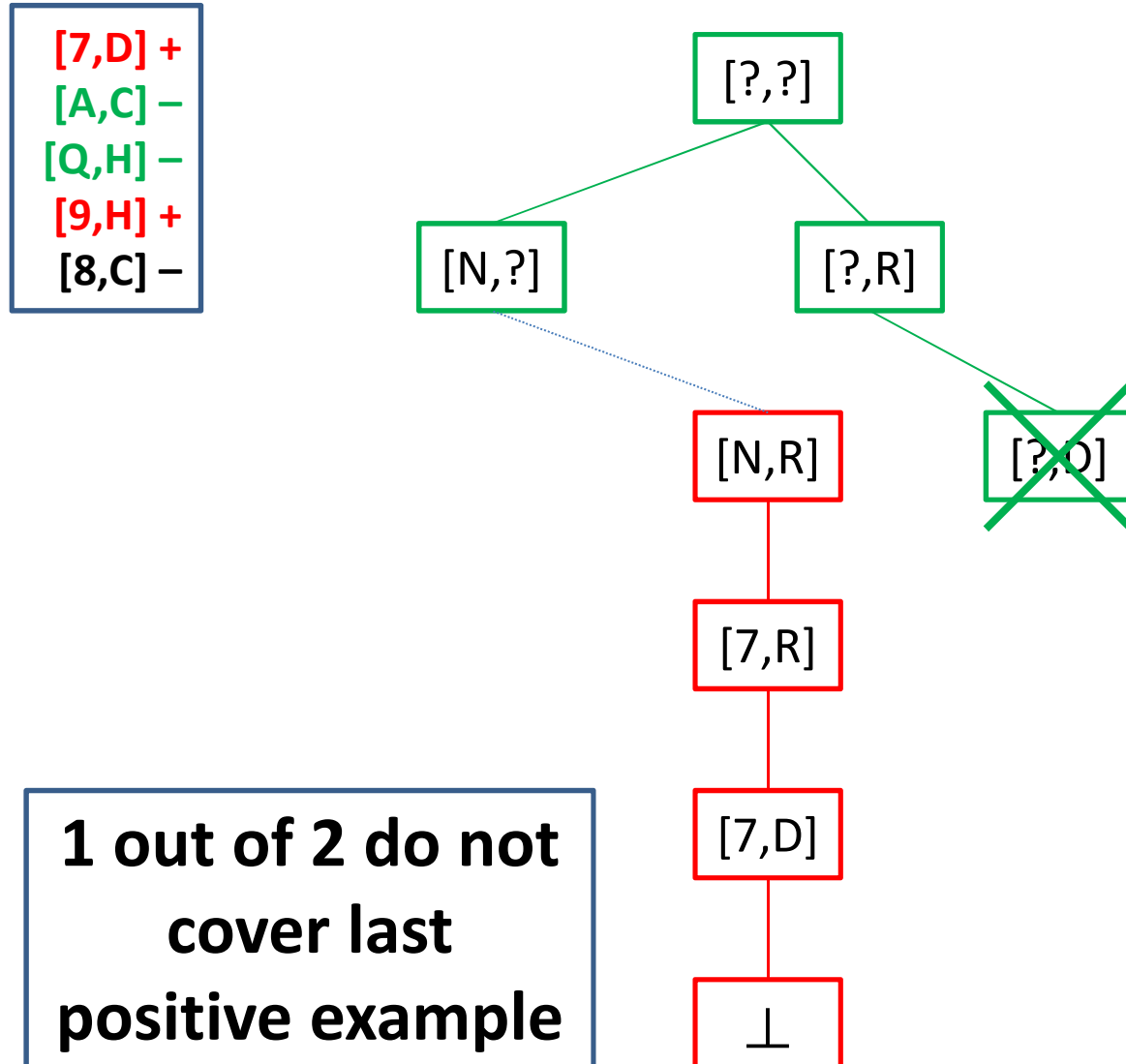


Version-Spaces Algorithm

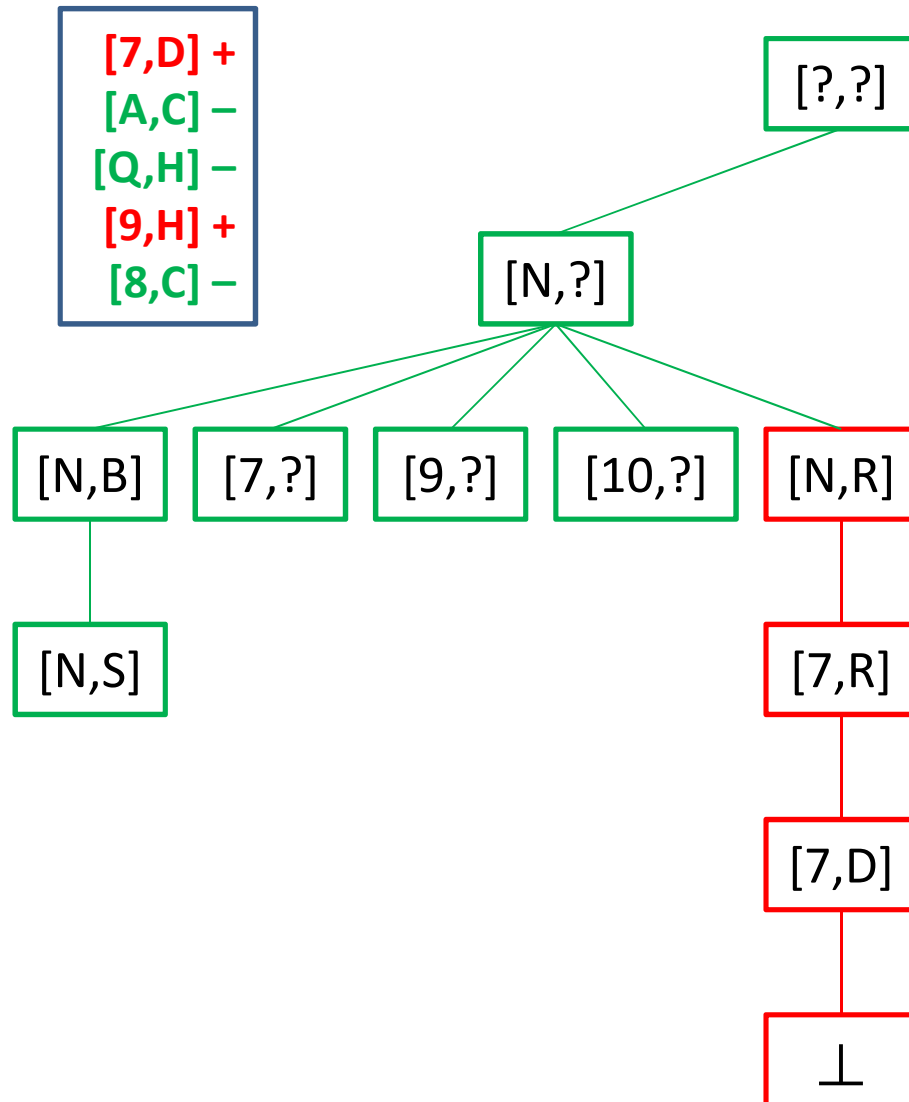
[7,D] +
[A,C] -
[Q,H] -
[9,H] +
[8,C] -



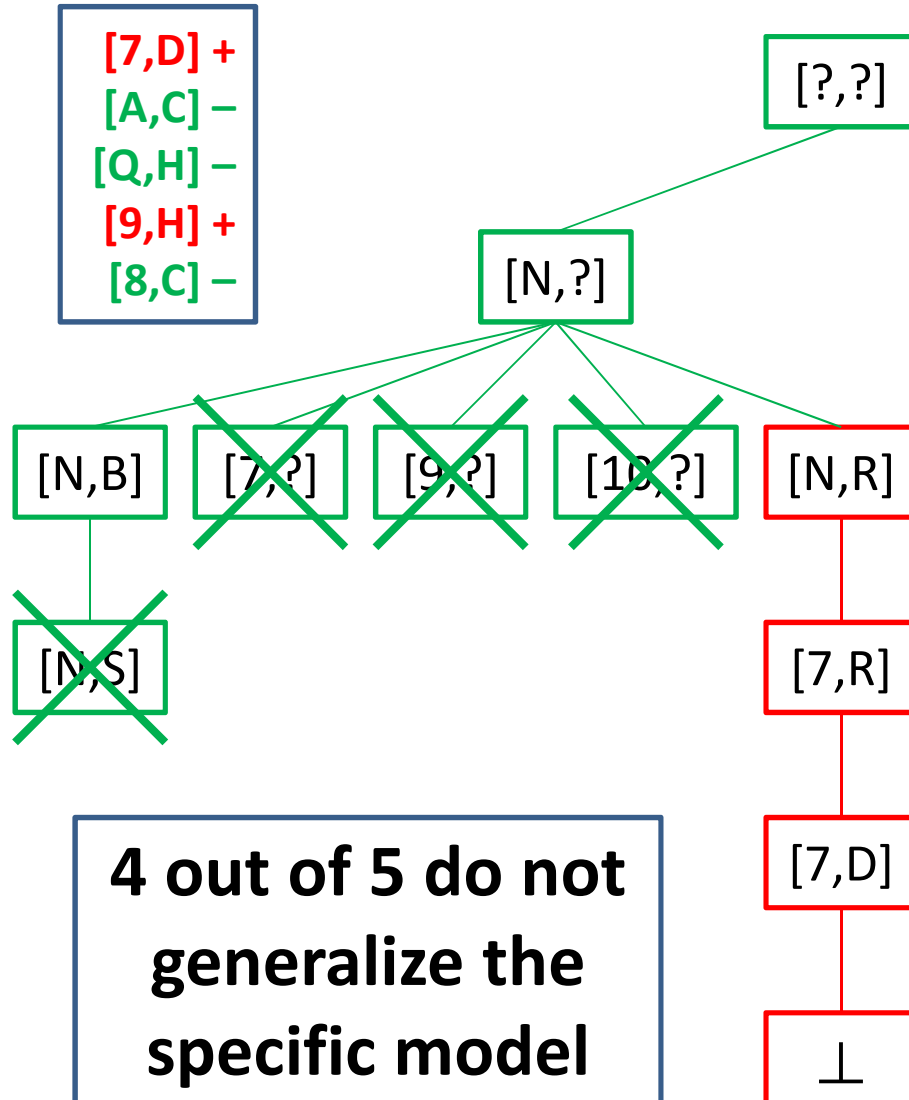
Version-Spaces Algorithm



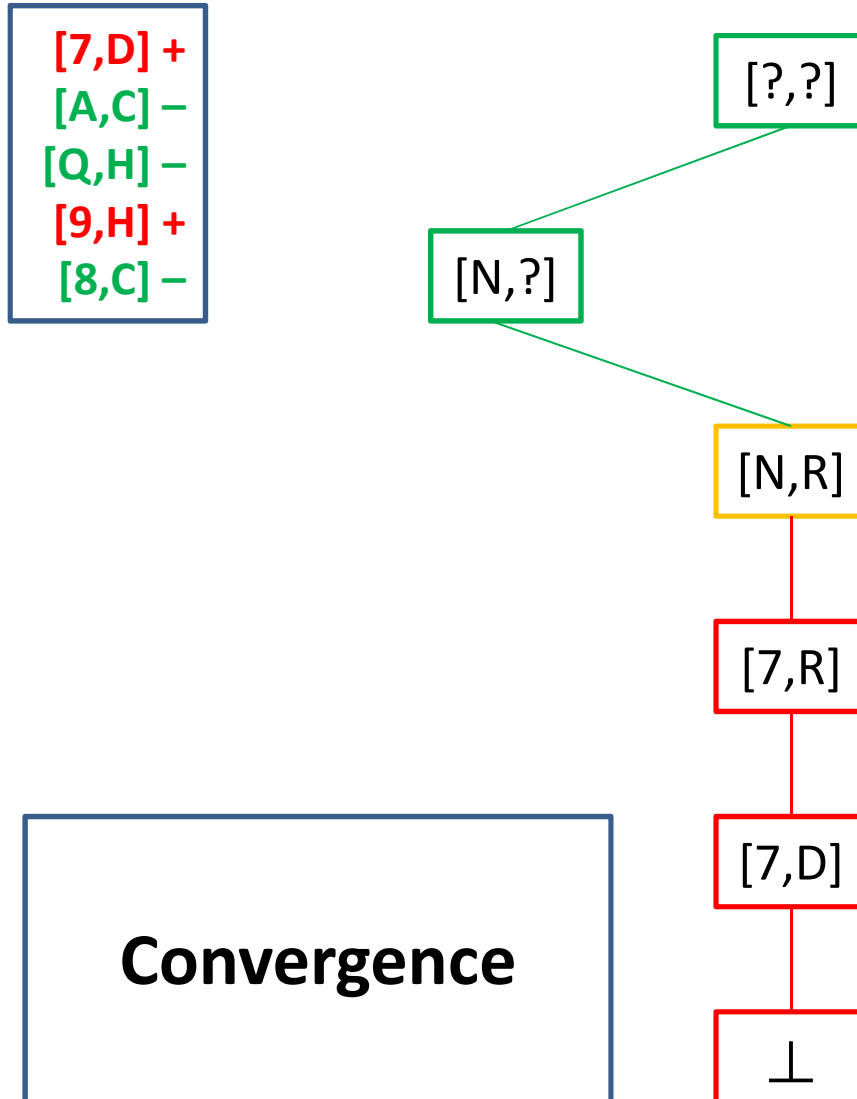
Version-Spaces Algorithm



Version-Spaces Algorithm



Version-Spaces Algorithm



Exercises: Artificial Intelligence

Version Spaces: Ex-exam

Version Spaces: Ex-exam

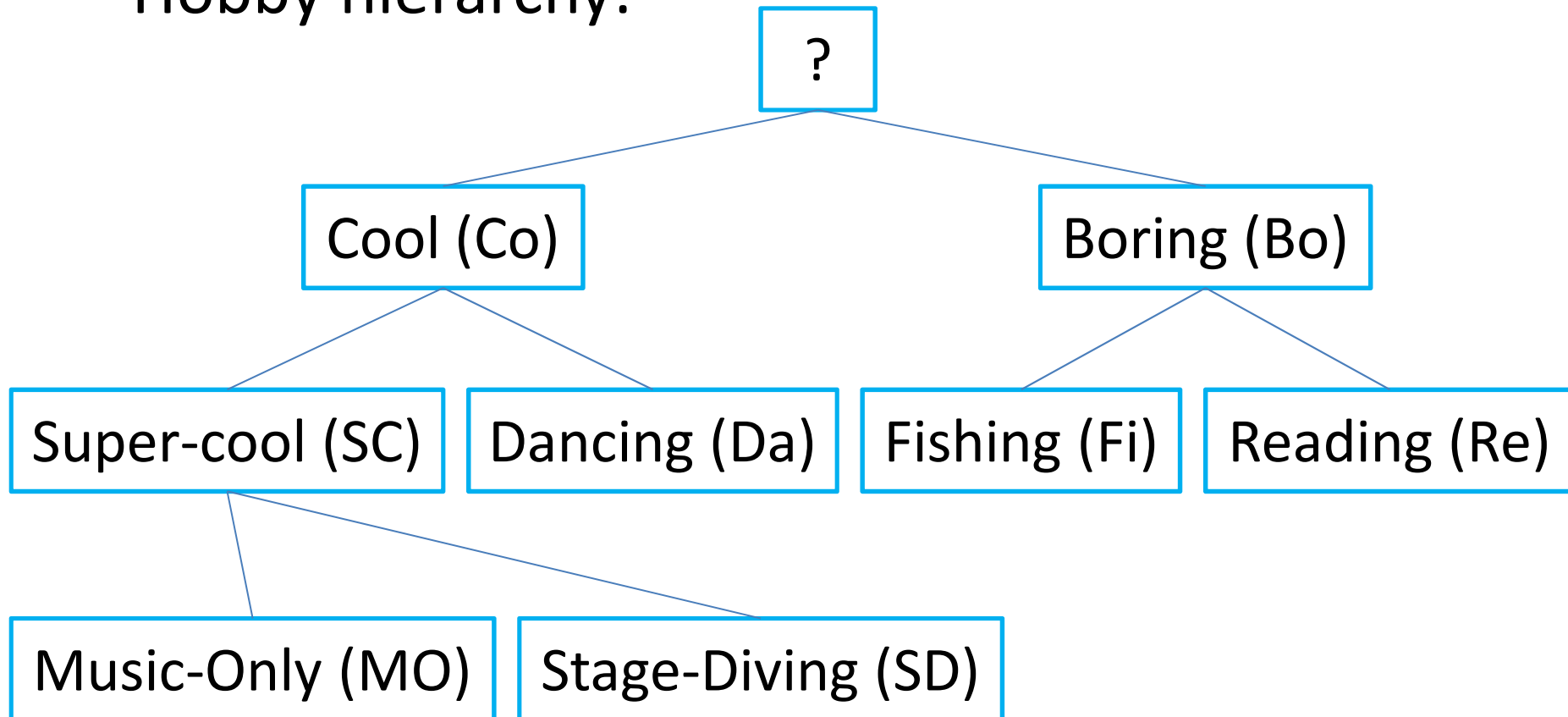
PROBLEM

Problem

- Searching for a new drummer.
 - Candidates hand in CV:
 - Hobby, Music preference, Age, Photo
 - 5 Profiles selected from 900
 - Evaluated: Accepted or Rejected
 - Learn Model, using Version Spaces
 - Conclude on 3 of the other 895 CVs using Model

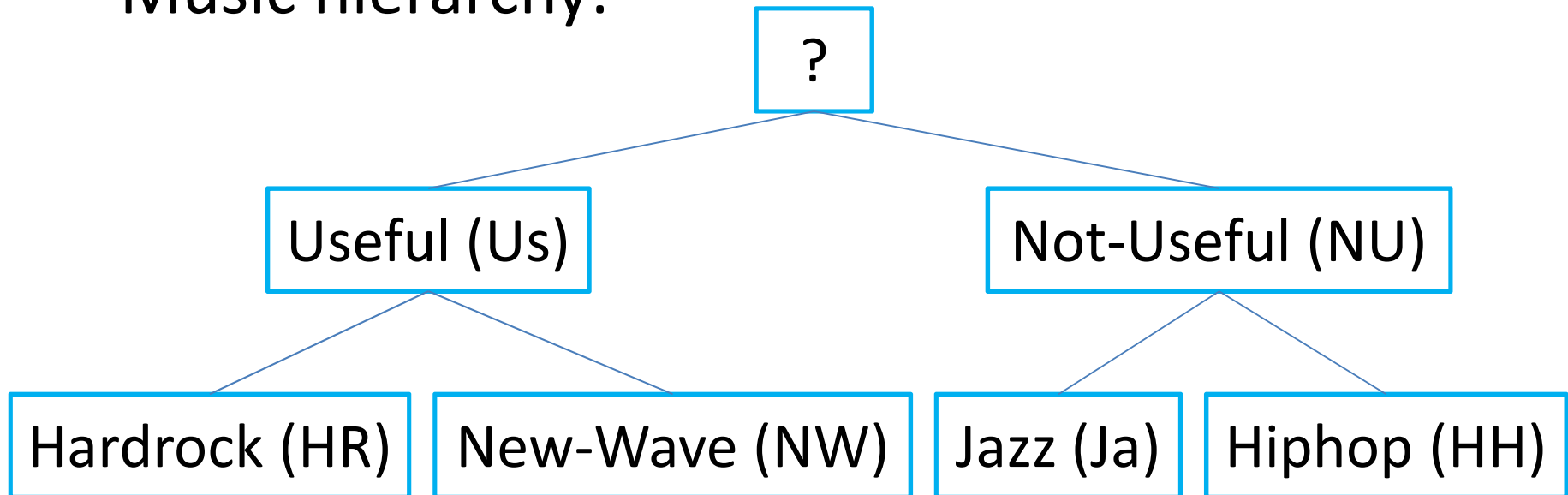
Problem

- Hobby hierarchy:



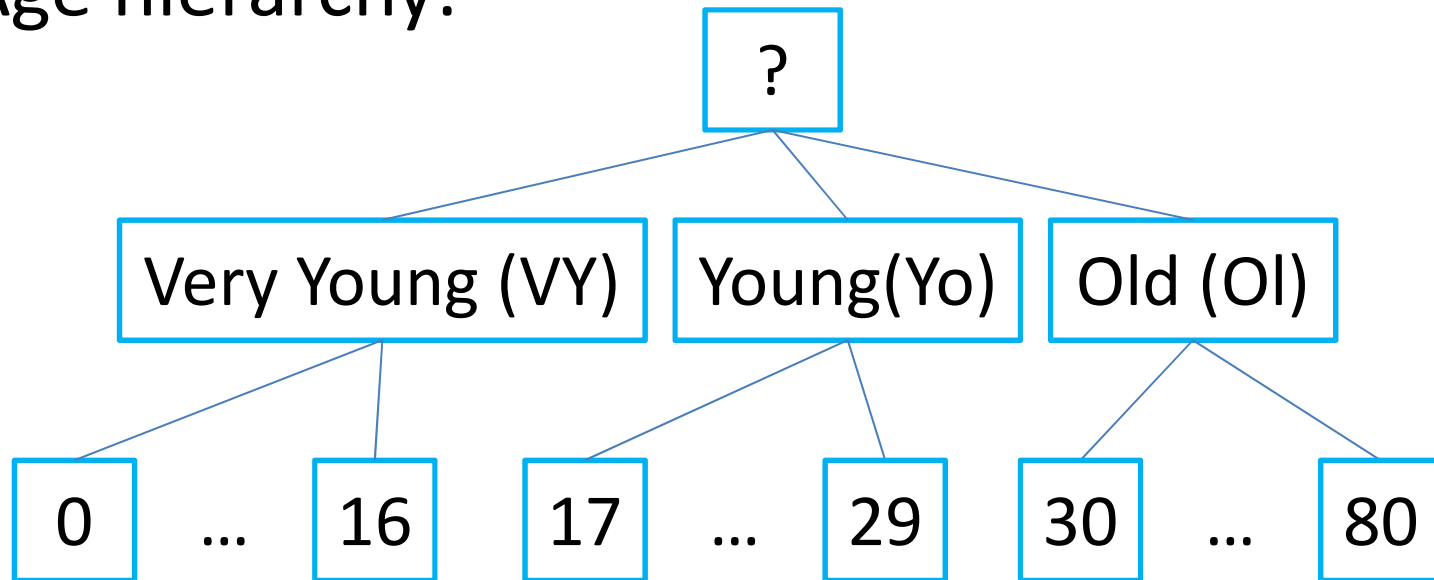
Problem

- Music hierarchy:



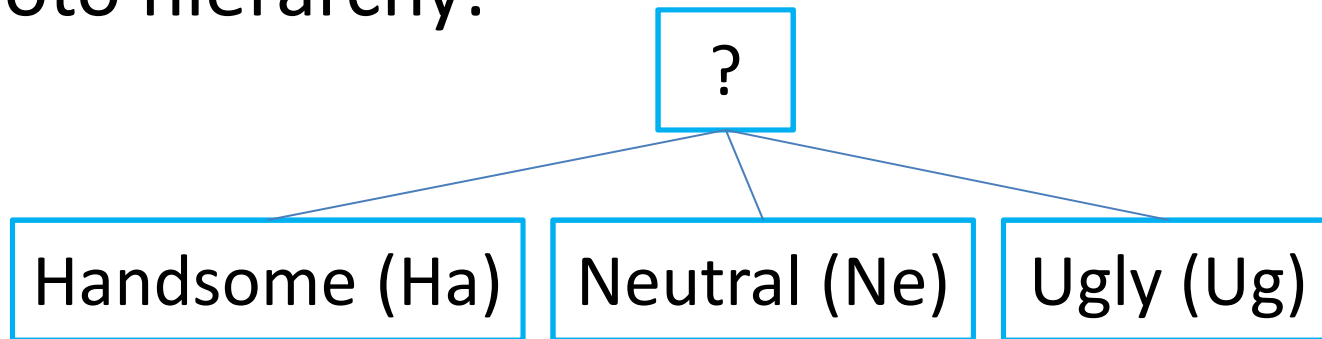
Problem

- Age hierarchy:



Problem

- Photo hierarchy:



Problem

- ***Examples:***

Hobby	Music	Age	Photo	Selected?
Fishing	Hiphop	16	Handsome	No
Stage-diving	New-wave	18	Neutral	Yes
Dancing	Hardrock	32	Ugly	No
Music-only	Hardrock	25	Handsome	Yes
Stage-diving	Jazz	29	Ugly	No

Version Spaces: Ex-exam

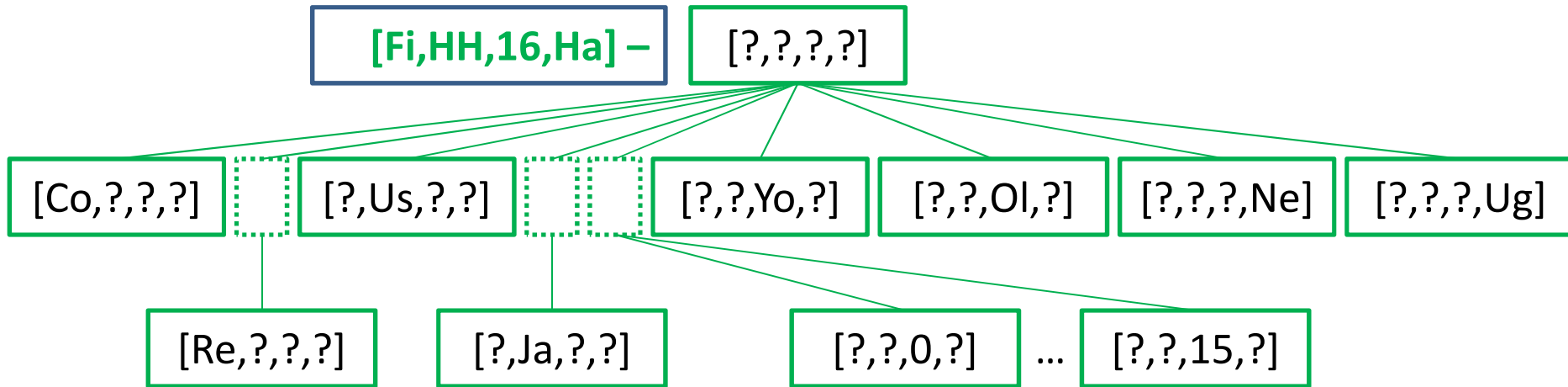
VERSION-SPACES ALGORITHM

Version-Spaces Algorithm

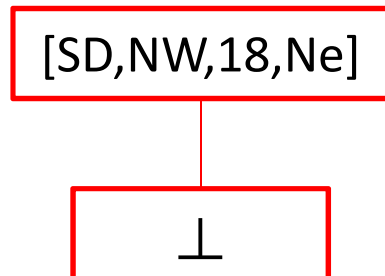
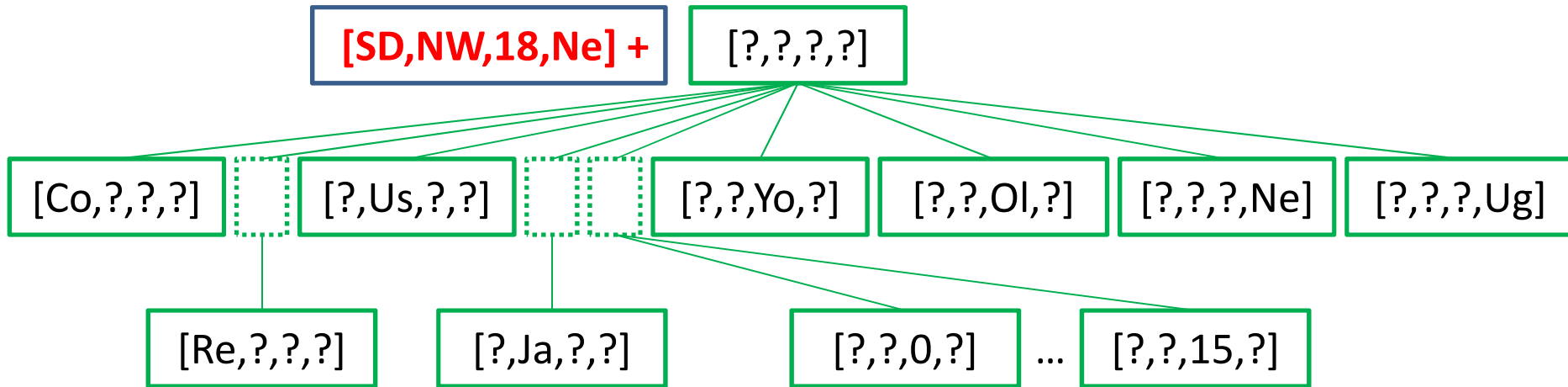
[?,?,?,?]

\perp

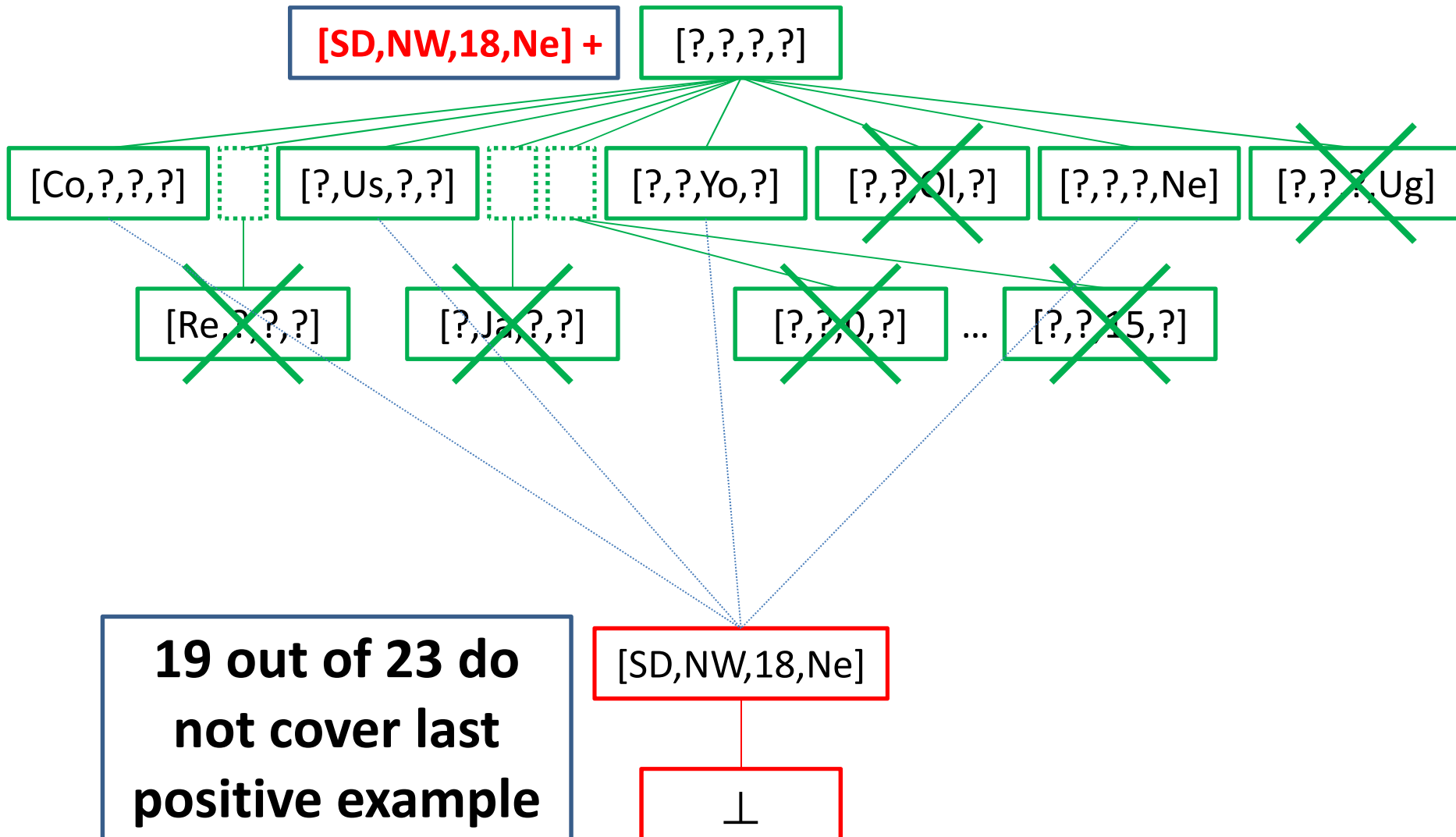
Version-Spaces Algorithm



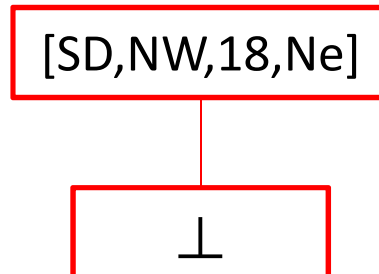
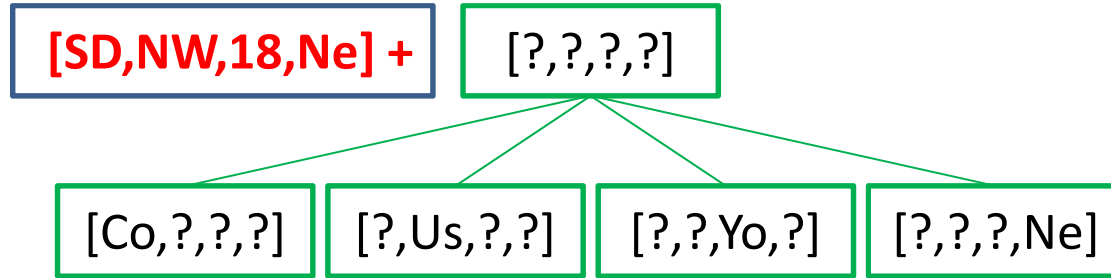
Version-Spaces Algorithm



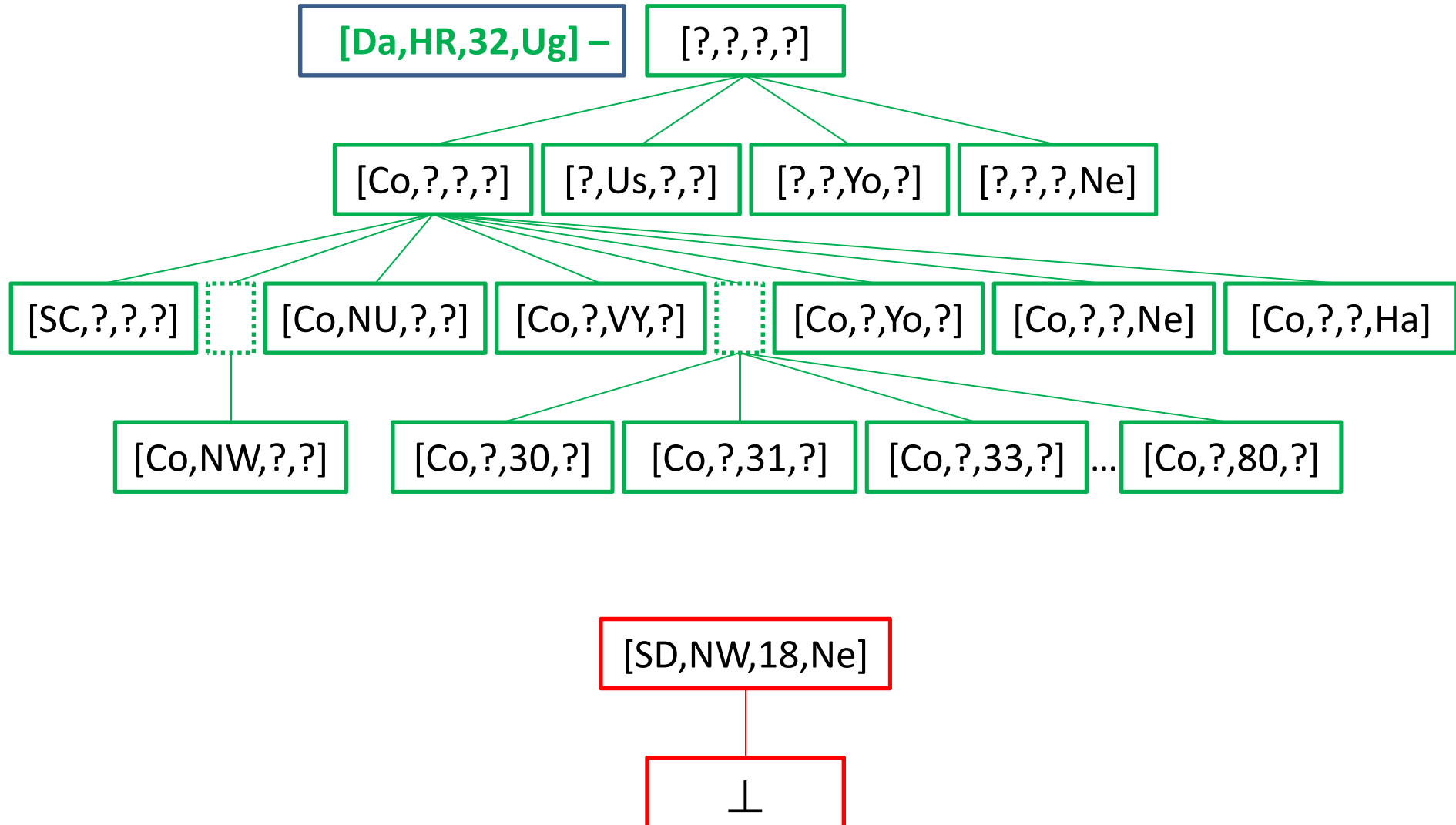
Version-Spaces Algorithm



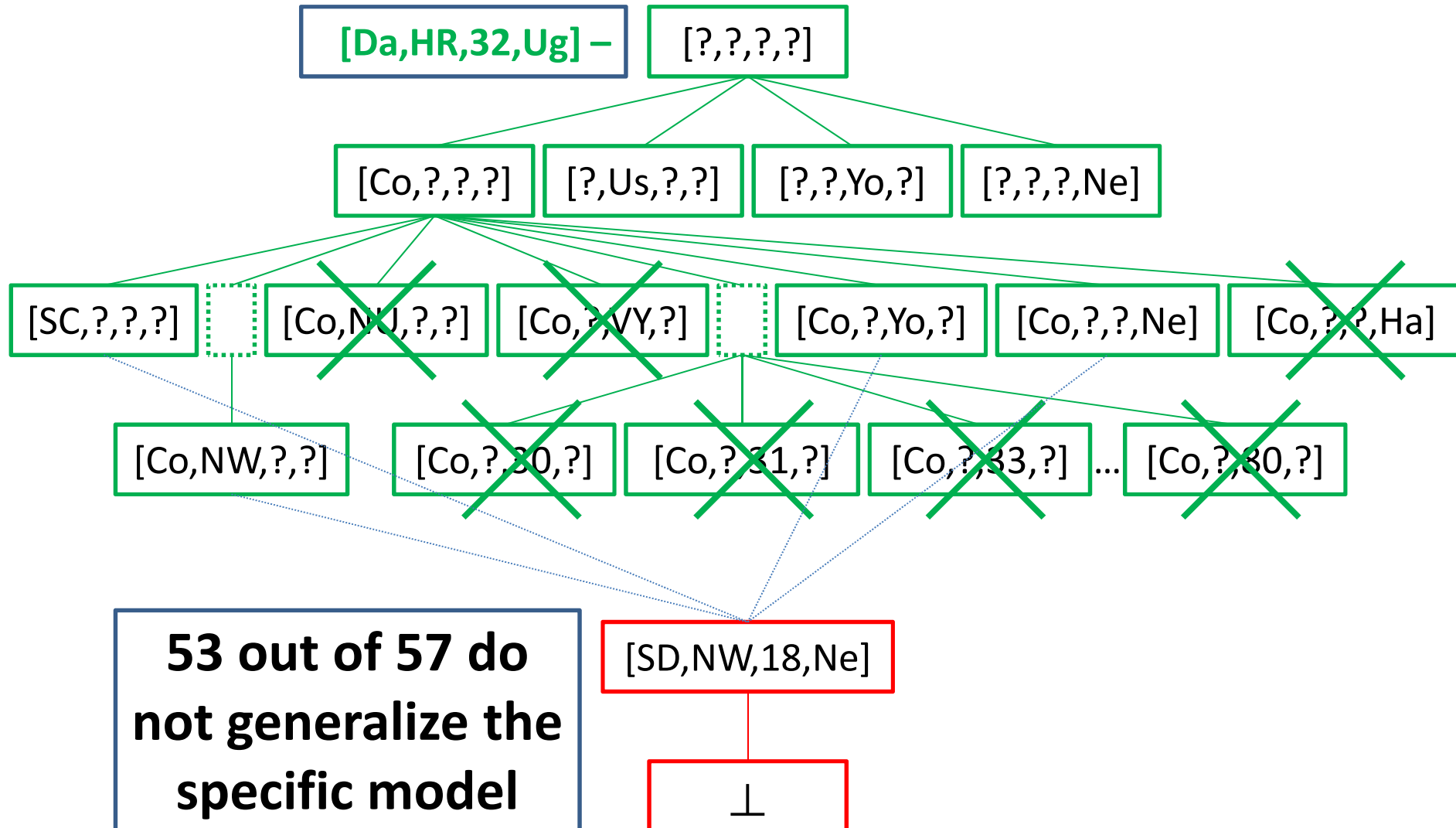
Version-Spaces Algorithm



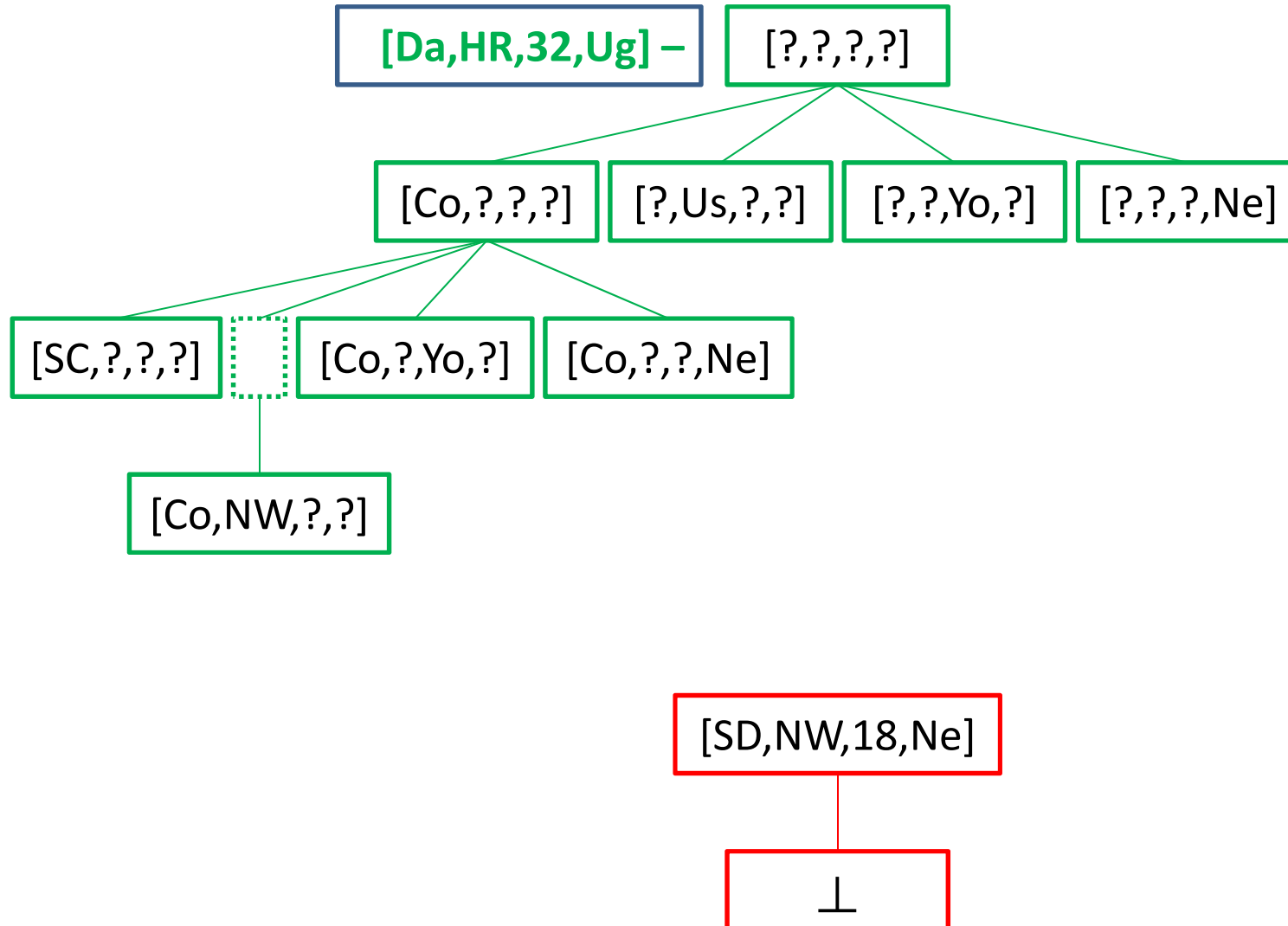
Version-Spaces Algorithm



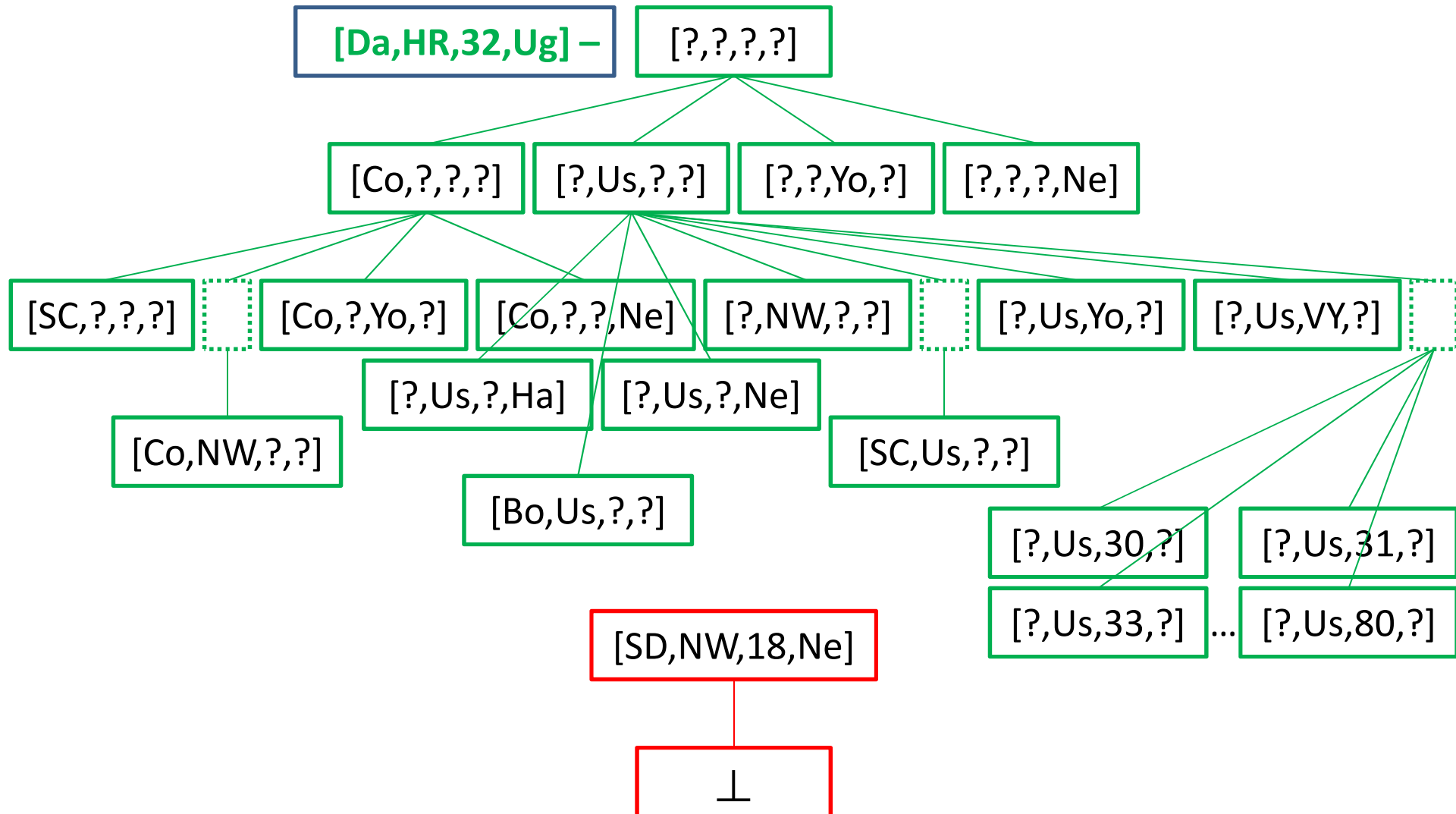
Version-Spaces Algorithm



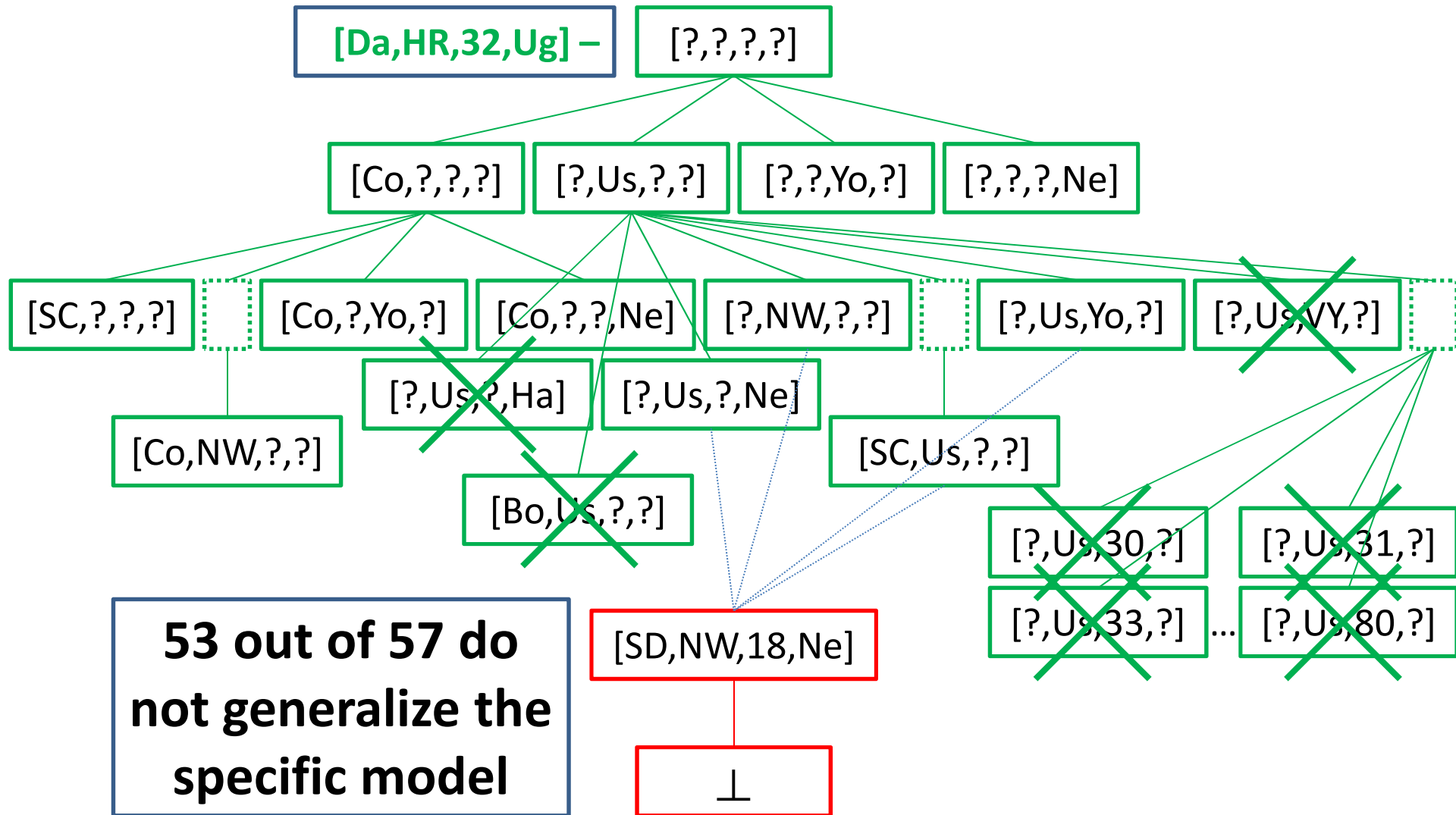
Version-Spaces Algorithm



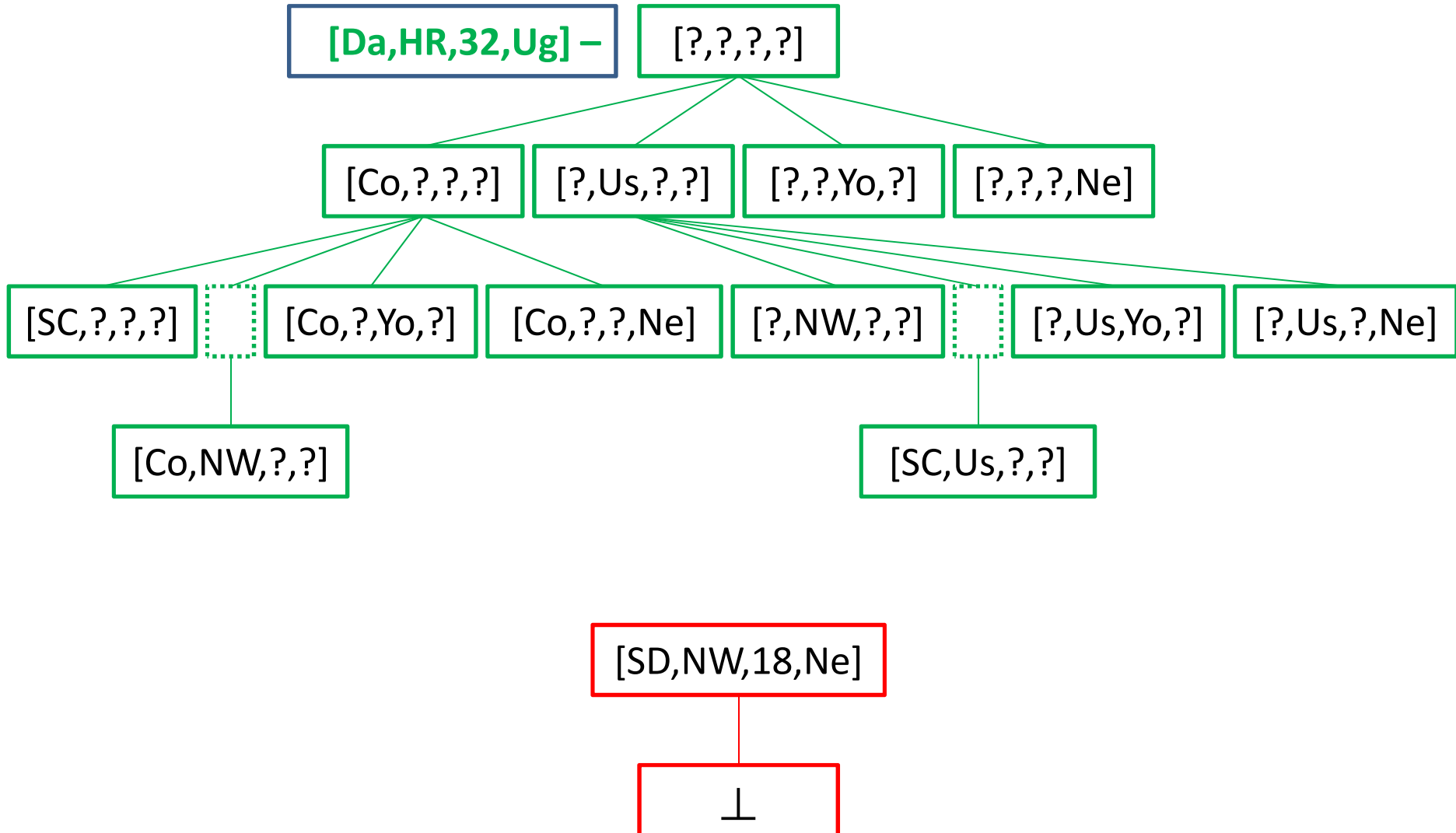
Version-Spaces Algorithm



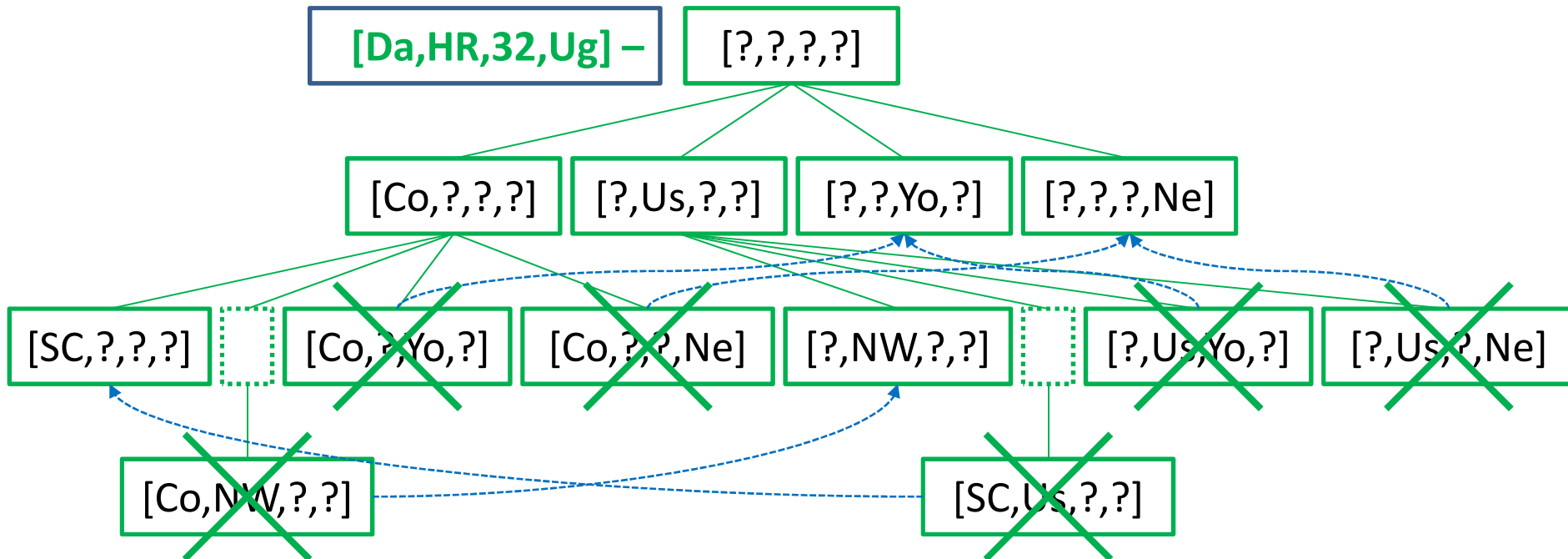
Version-Spaces Algorithm



Version-Spaces Algorithm



Version-Spaces Algorithm

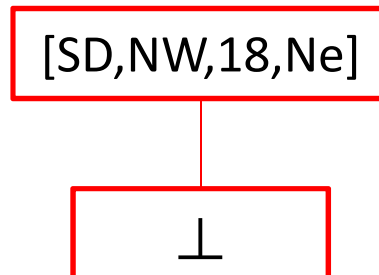
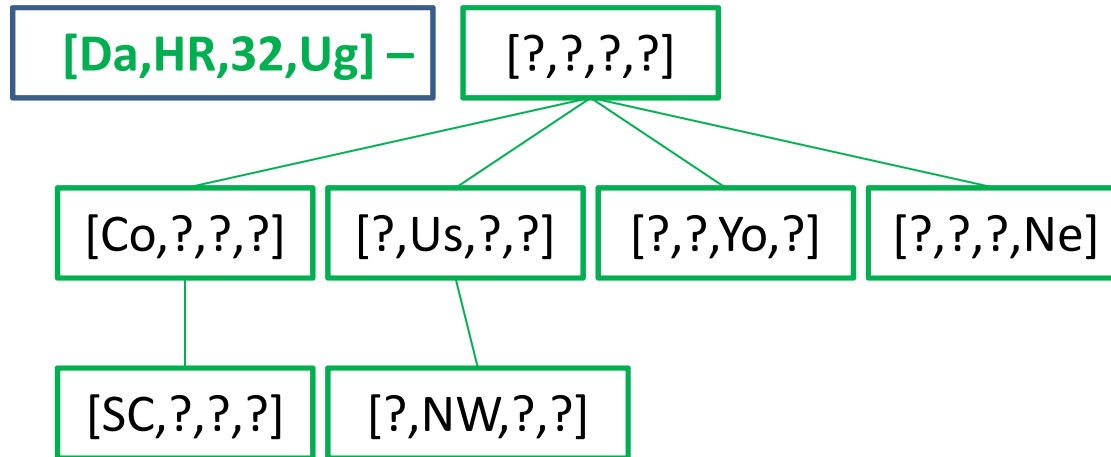


Redundant hypotheses

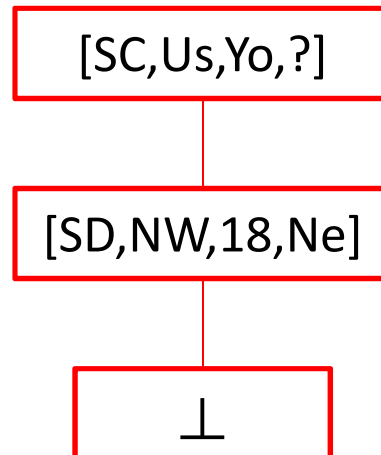
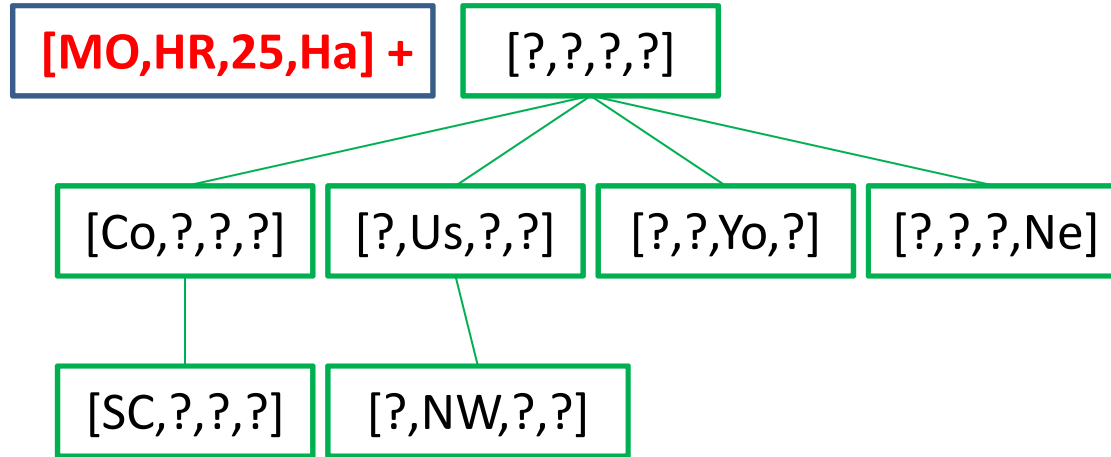
[SD,NW,18,Ne]

⊥

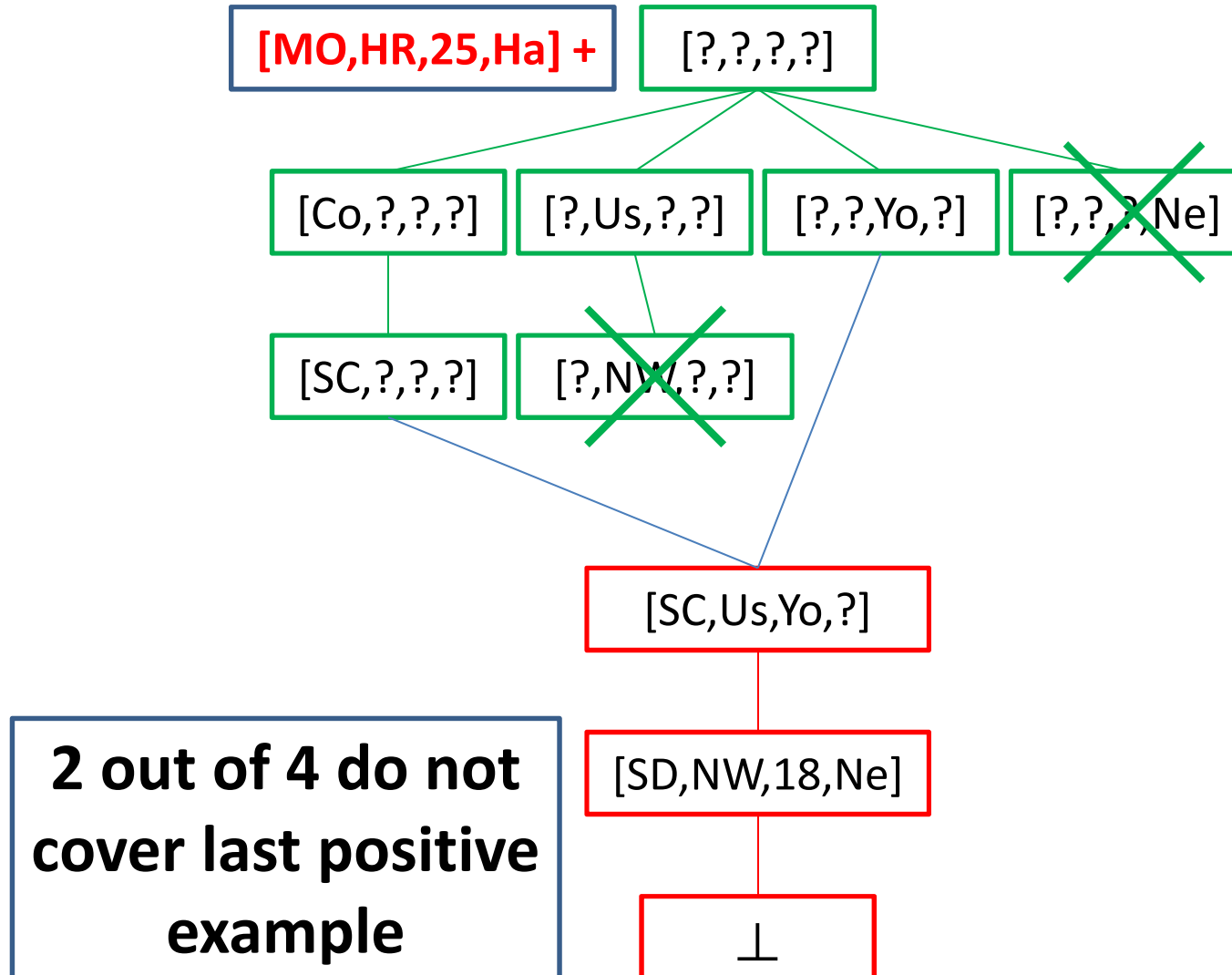
Version-Spaces Algorithm



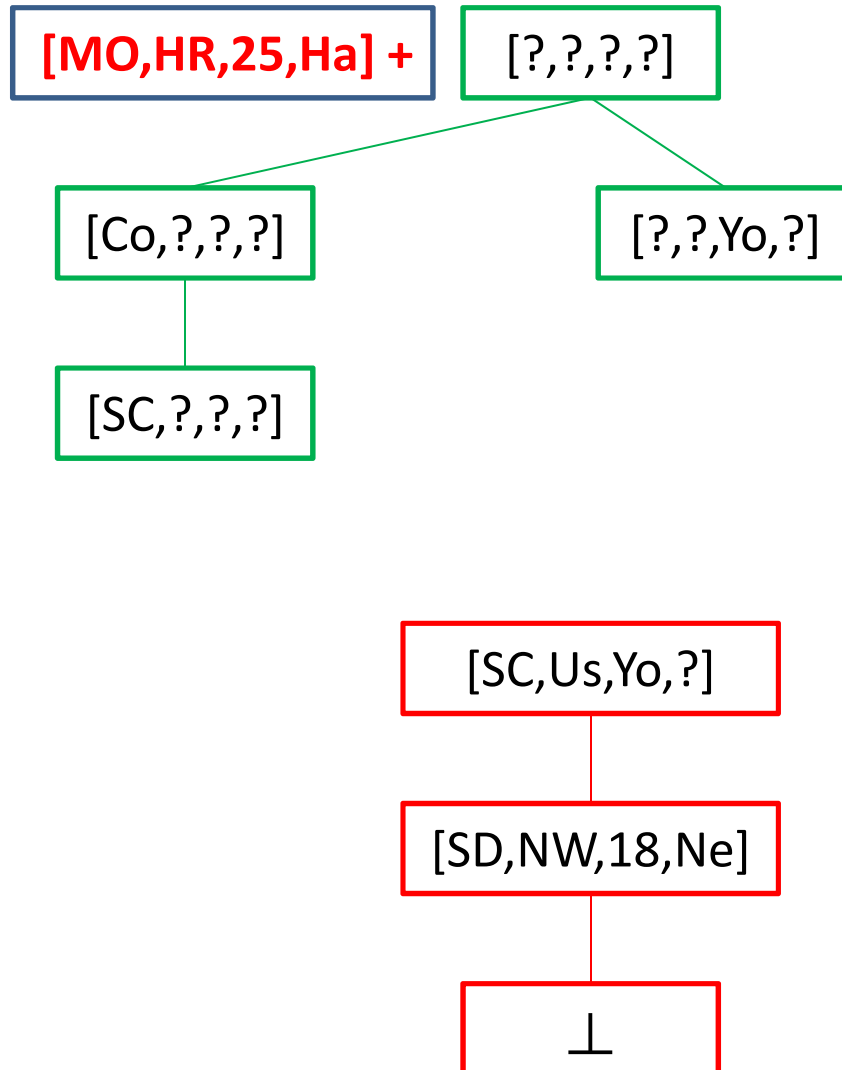
Version-Spaces Algorithm



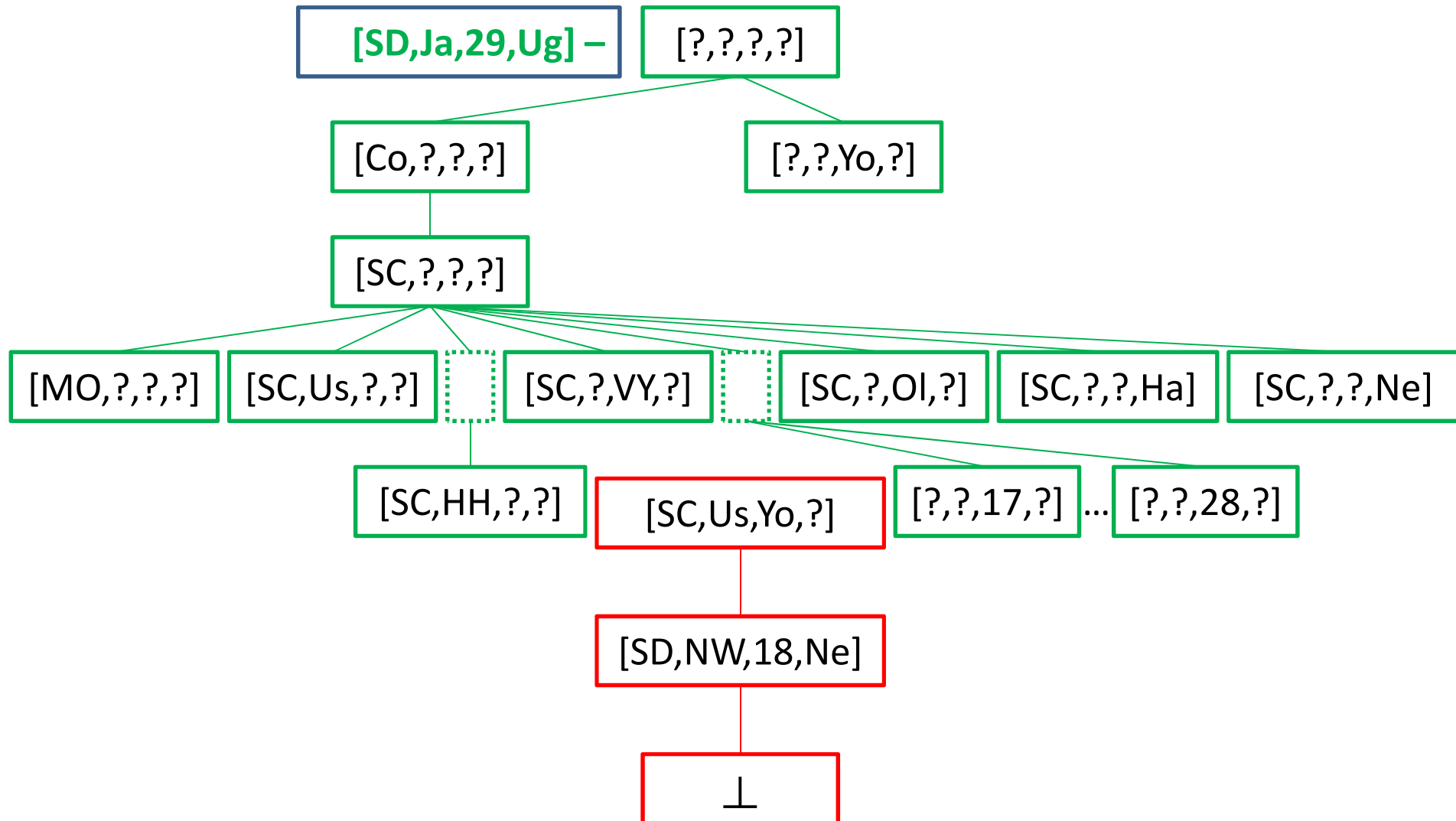
Version-Spaces Algorithm



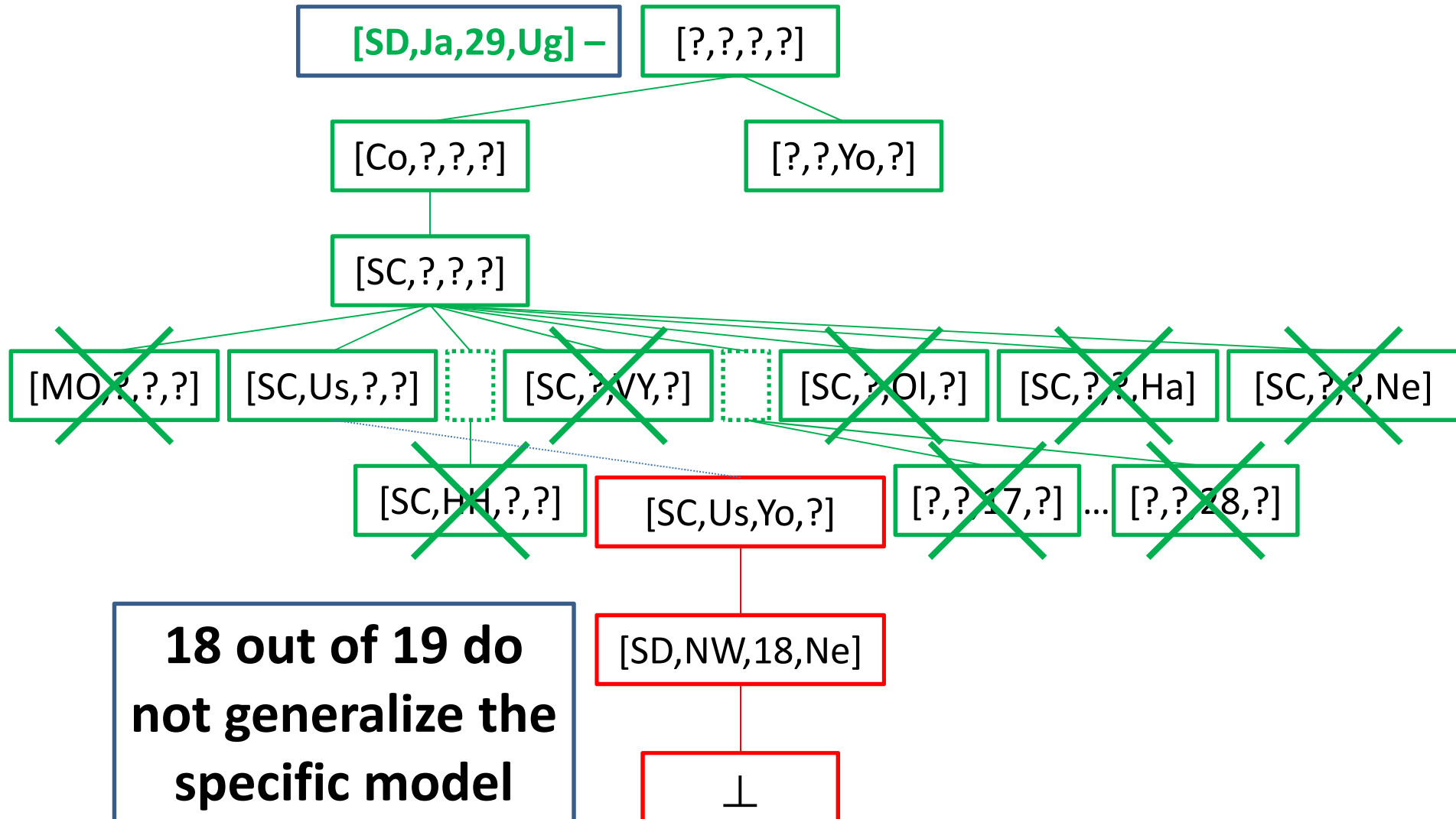
Version-Spaces Algorithm



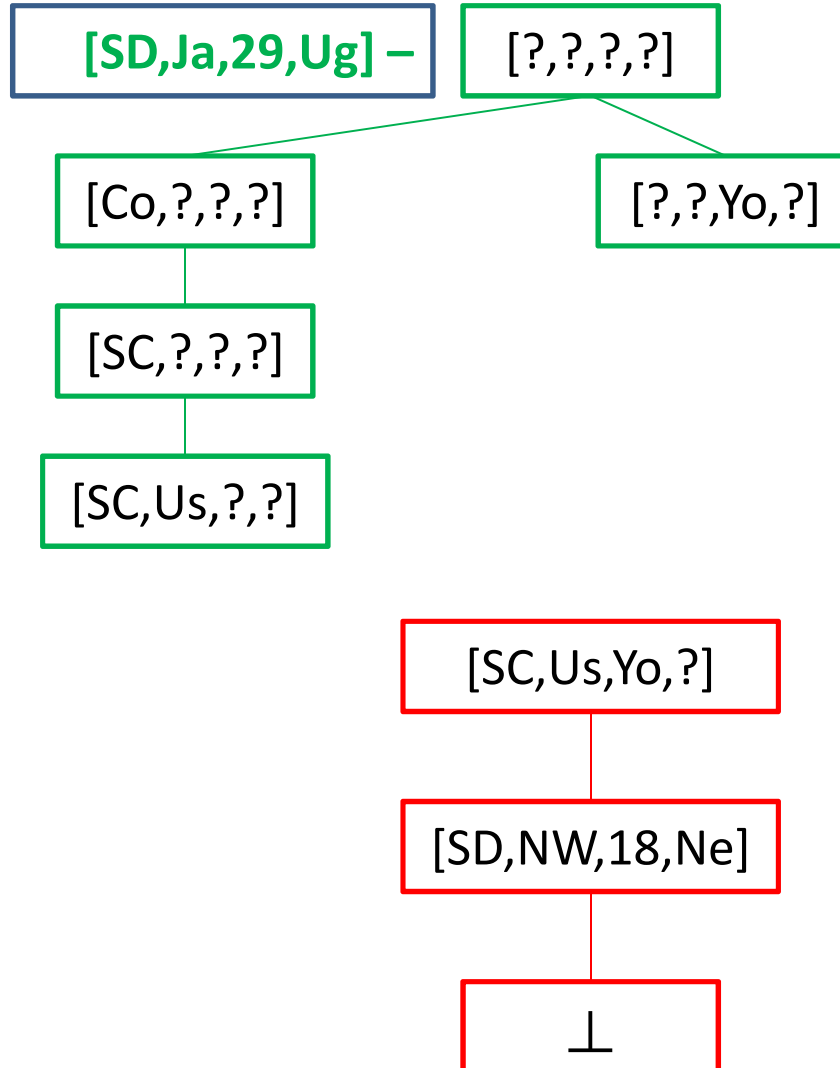
Version-Spaces Algorithm



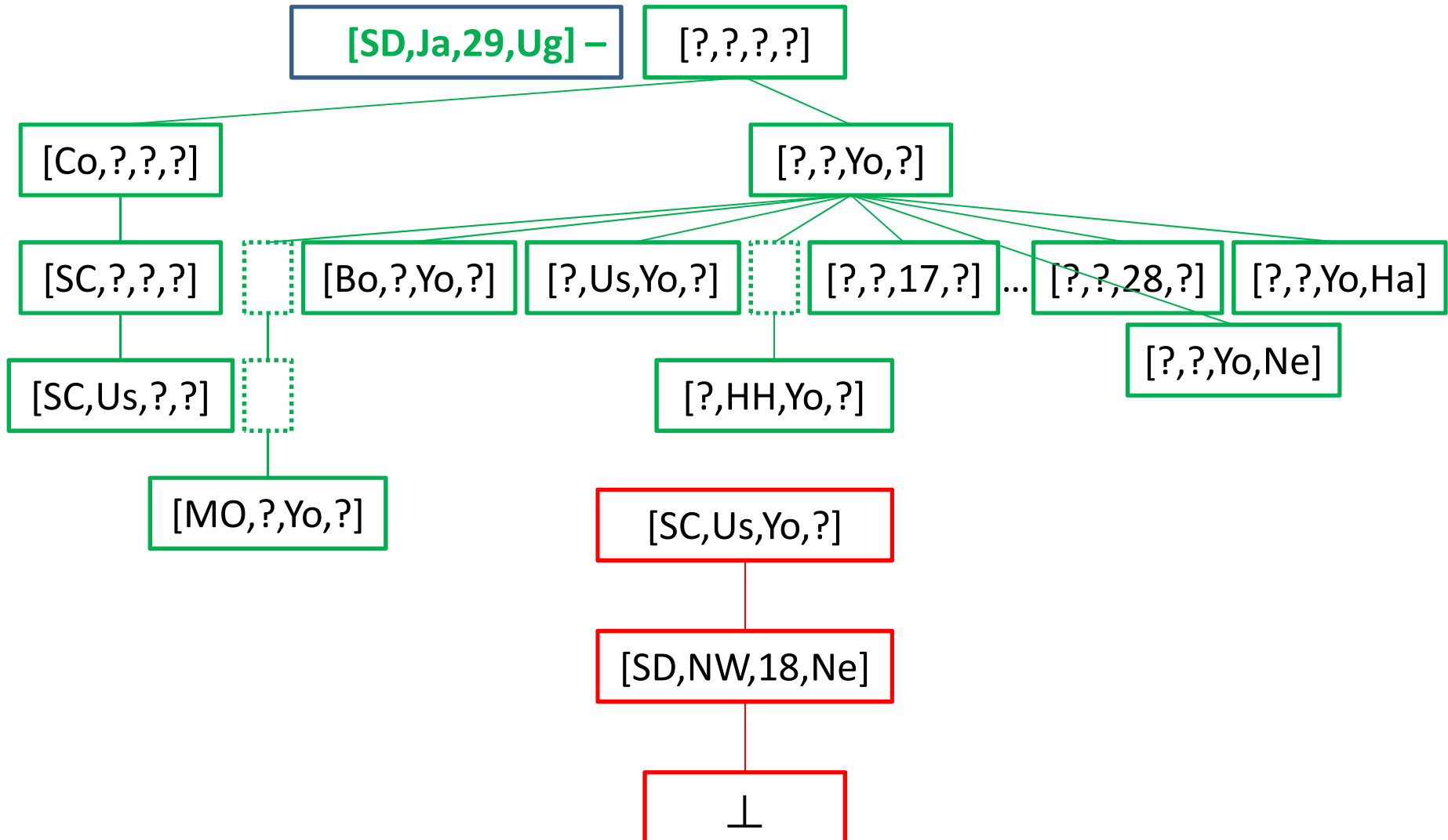
Version-Spaces Algorithm



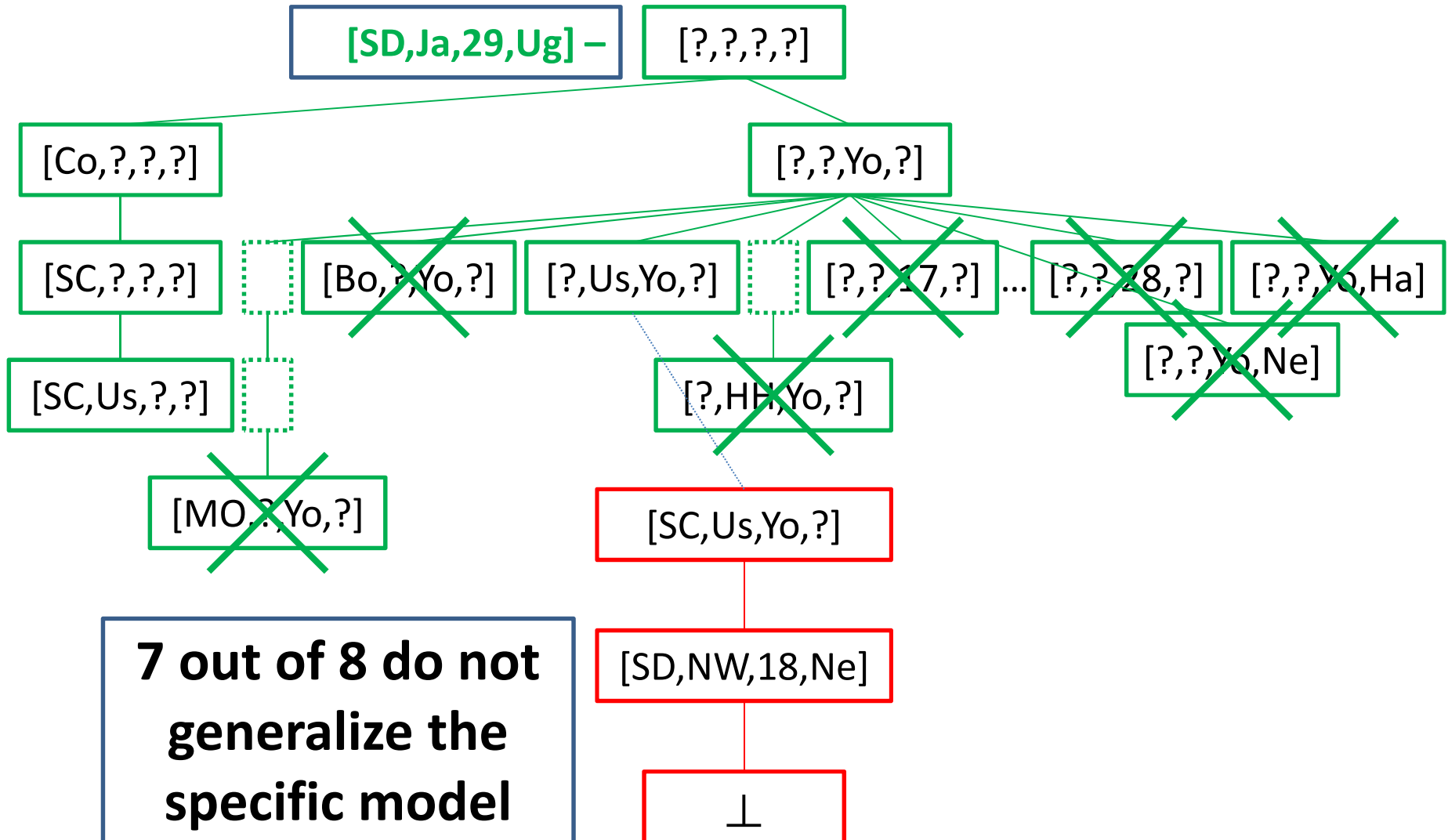
Version-Spaces Algorithm



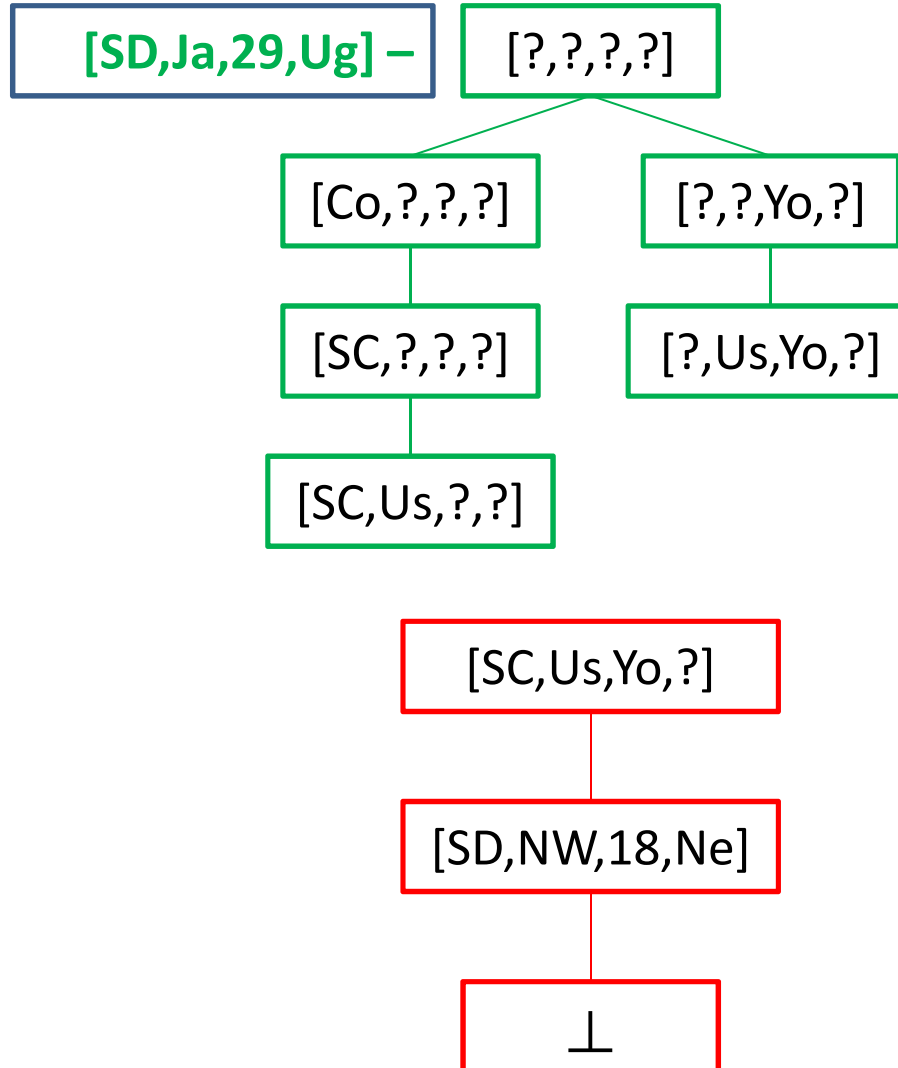
Version-Spaces Algorithm



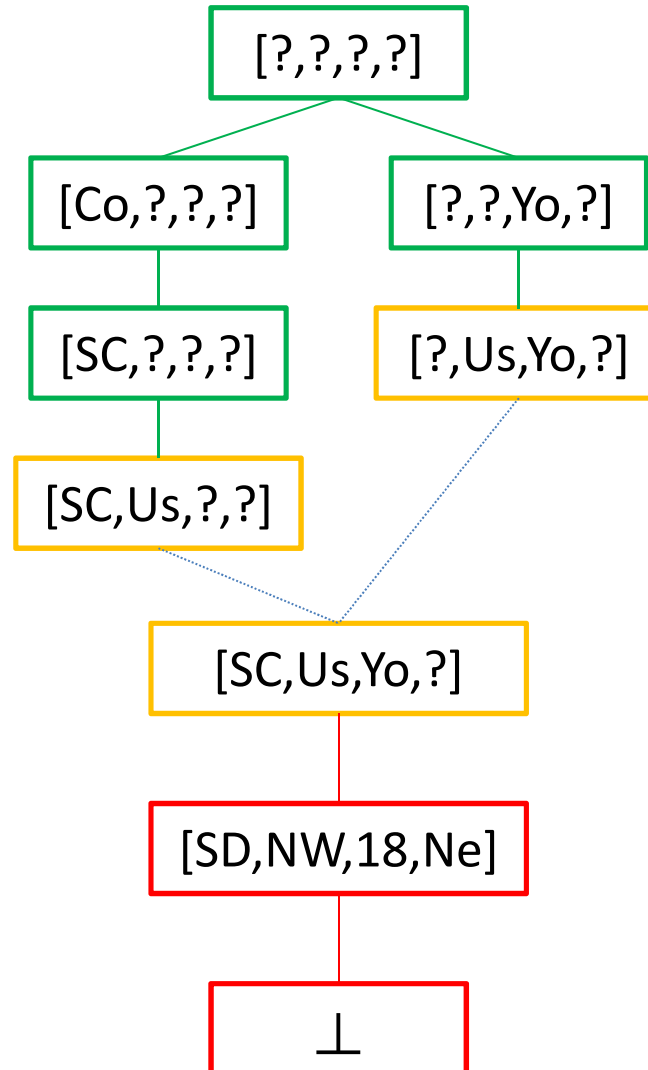
Version-Spaces Algorithm



Version-Spaces Algorithm



Version-Spaces Algorithm

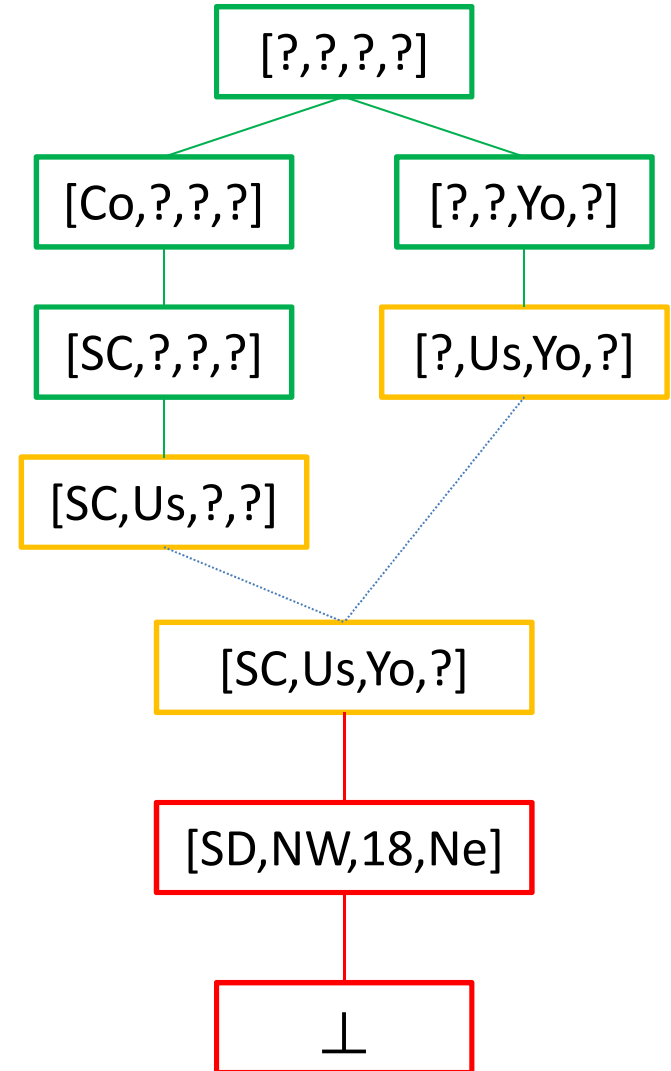


Version Spaces: Ex-exam

USING THE RESULT

Using the result

- [MO,HR,32,Ha]: **Maybe**
 - More Specific than [SC,Us,?,?]
 - Not more Specific than [SC,Us,Yo,?]
- [SD,HH,18,Ne]: **NO**
 - Not More Specific than [SC,Us,?,?]
 - Not More Specific than [?,Us,Yo,?]
- [Da,NW,22,Ug]: **Maybe**
 - More Specific than [?,Us,Yo,?]
 - Not more Specific than [SC,Us,Yo,?]



Exercises: Artificial Intelligence

Version Spaces: Computer Screen

Version Spaces: Computer Screen

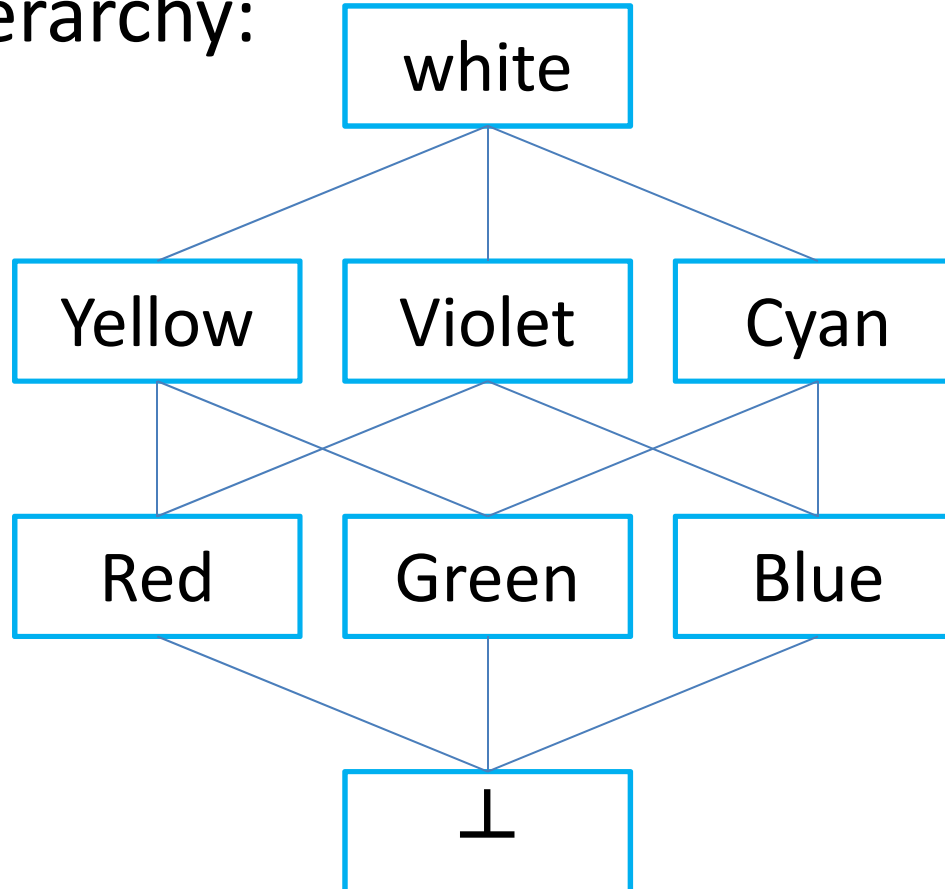
PROBLEM

Problem

- Computer Screen 6x6 pixels
 - Only colored squares can be shown:
 - $[(x,y),n,color]$
 - (x,y) : coordinates from bottom-left corner
 - $n > 0$: length of sides
 - Squares appear on the screen by examples
 - Give to the screen:
 - squares that should be lit
 - squares that shouldn't be lit
 - Which square is shown? Use Version Spaces.

Problem

- Color hierarchy:



Problem

- ***Examples:***

Location	Color	Lit?
(0,1)	Red	No
(3,2)	Red	Yes
(1,4)	Green	Yes
(4,5)	Red	No
(4,0)	green	No

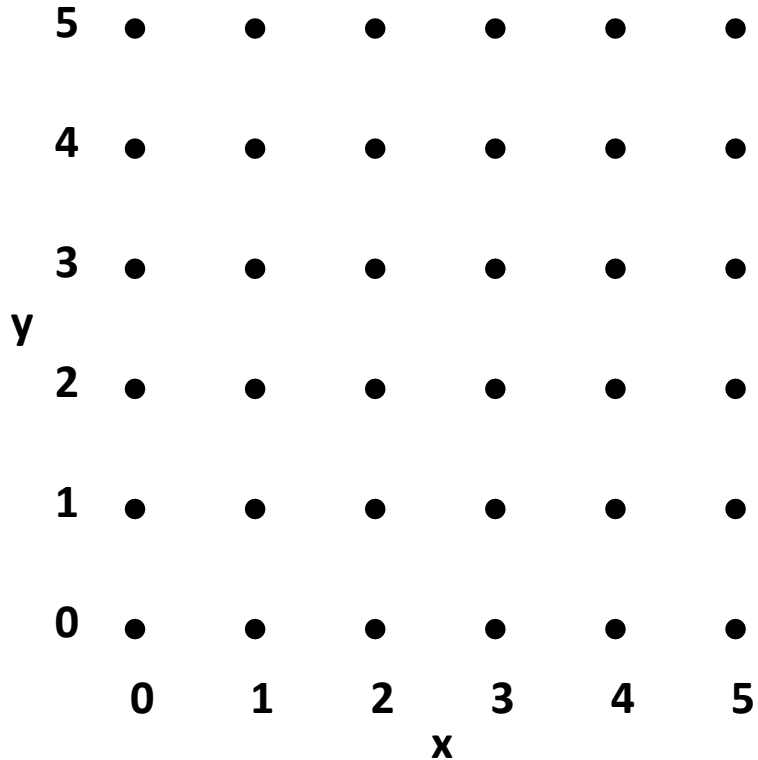
Version Spaces: Computer Screen

VERSION-SPACES ALGORITHM

Version-Spaces Algorithm

$G = \{[((0,0),5),\text{white}]\}$

$S = \{\perp\}$

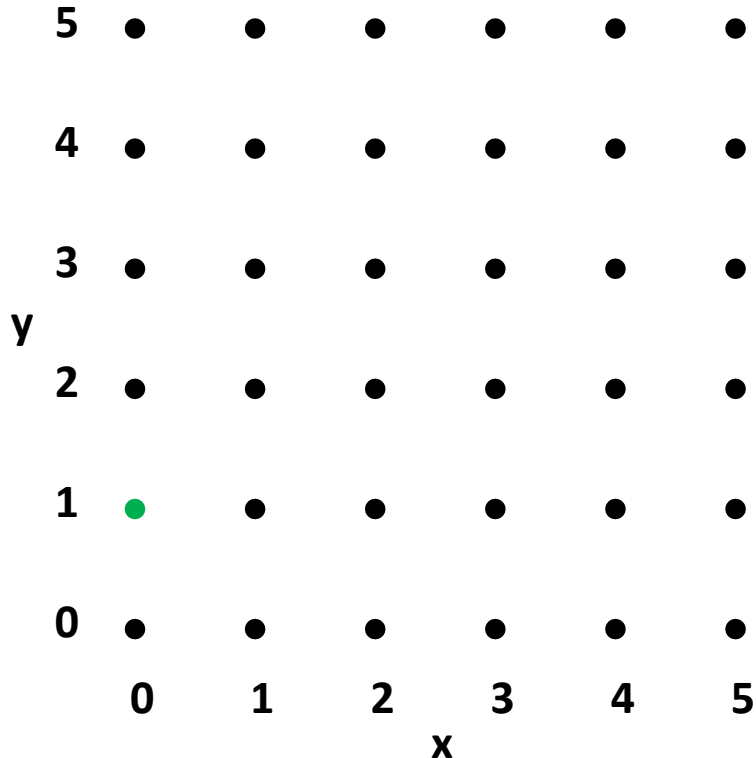


Version-Spaces Algorithm

$G = \{[(0,0),5], \text{white}]\}$

$S = \{\perp\}$

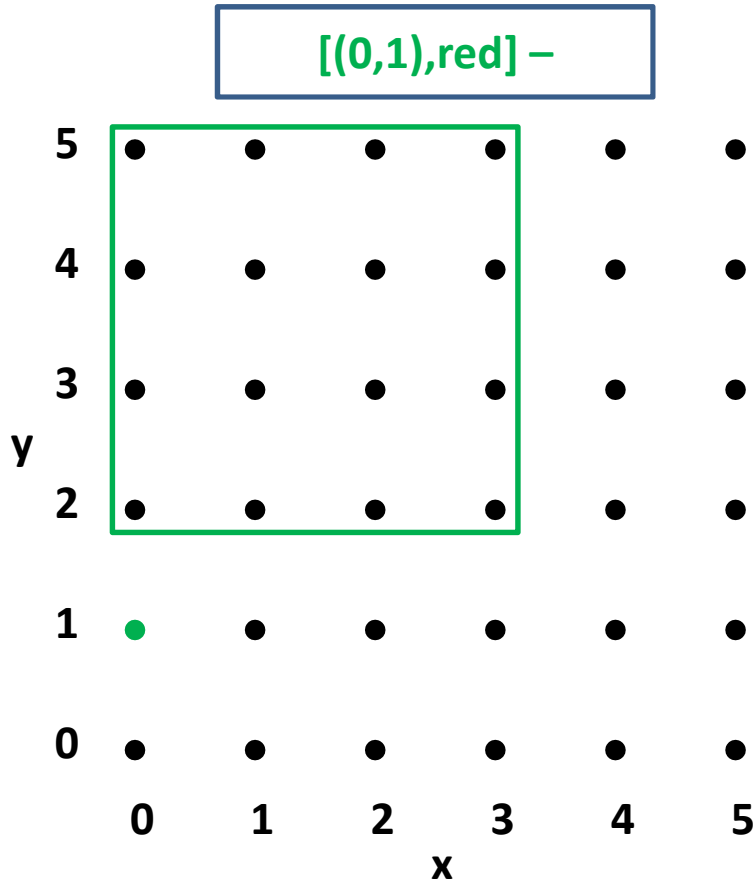
$[(0,1), \text{red}] -$



Version-Spaces Algorithm

$G = \{ [((0,0),5), \text{white}] \}$

$S = \{\perp\}$

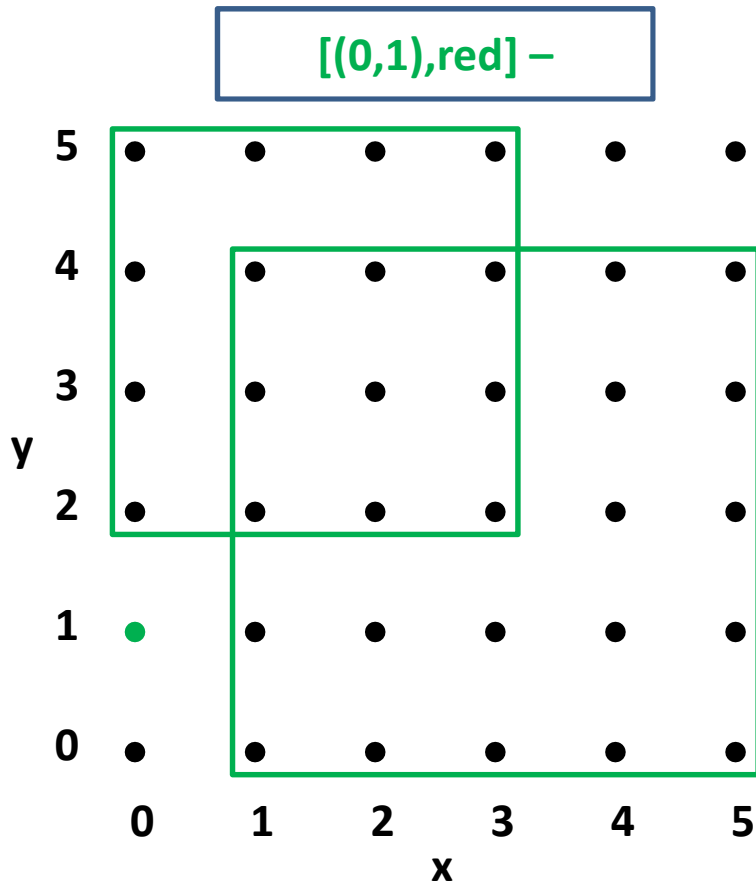


$G = \{$
 $[(0,2),3), \text{white}]$
 $\}$
 $S = \{\perp\}$

Version-Spaces Algorithm

$G = \{ [((0,0),5), \text{white}] \}$

$S = \{\perp\}$

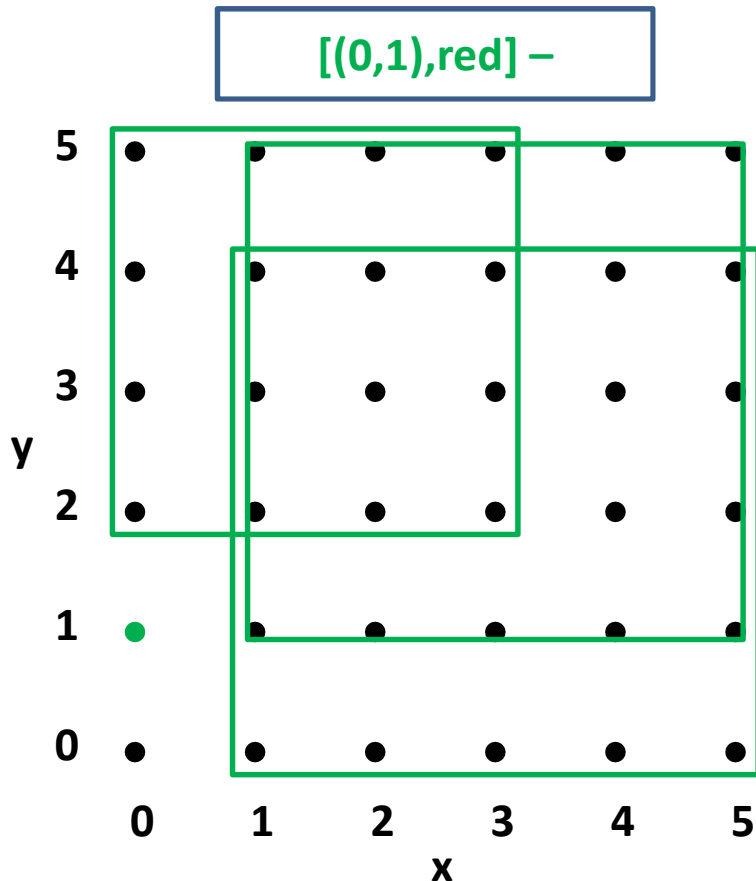


$G = \{$
 $[((0,2),3), \text{white}],$
 $[((1,0),4), \text{white}]$
 $\}$
 $S = \{\perp\}$

Version-Spaces Algorithm

$G = \{ [((0,0),5), \text{white}] \}$

$S = \{\perp\}$



$G = \{$

$[((0,2),3), \text{white}],$

$[((1,0),4), \text{white}],$

$[((1,1),4), \text{white}]$

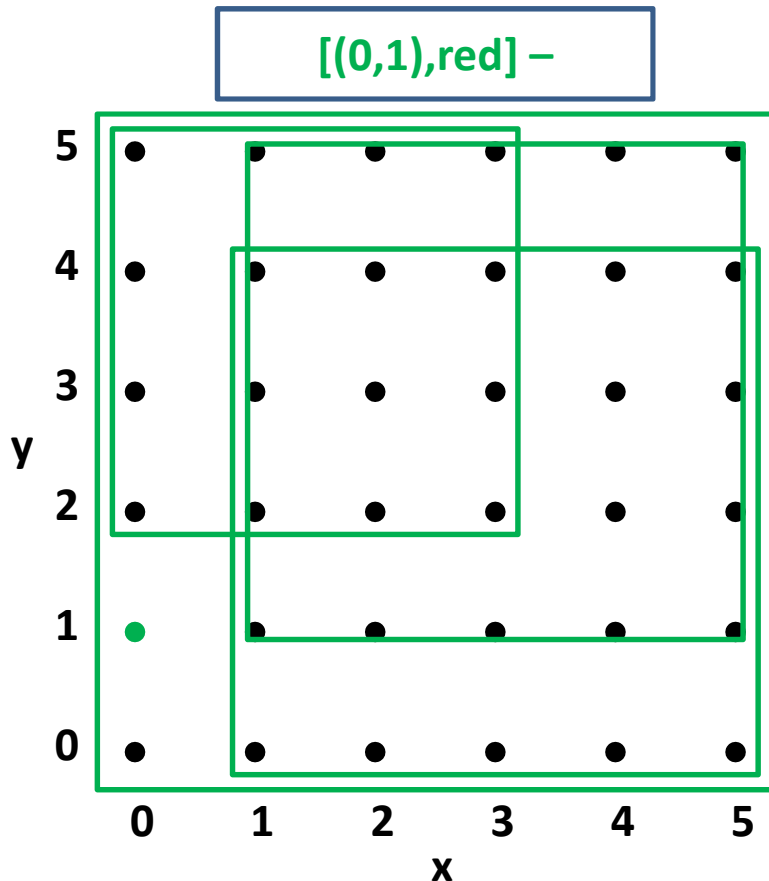
$\}$

$S = \{\perp\}$

Version-Spaces Algorithm

$G = \{ [((0,0),5), \text{white}] \}$

$S = \{\perp\}$



$G = \{$

$[((0,2),3), \text{white}],$
 $[((1,0),4), \text{white}],$
 $[((1,1),4), \text{white}],$
 $[((0,0),5), \text{cyan}]$

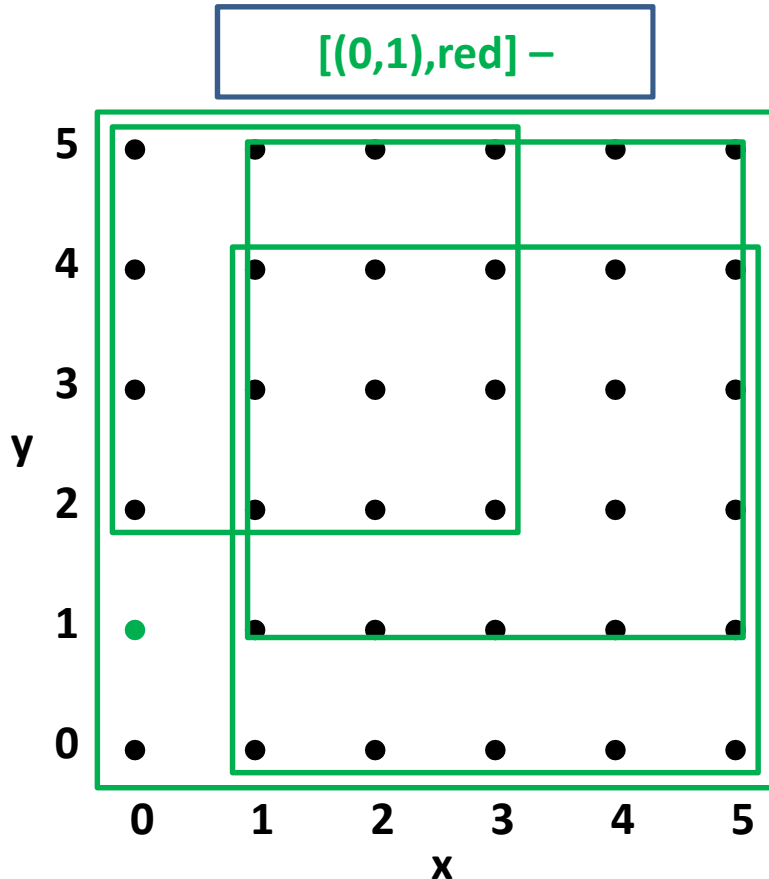
$\}$

$S = \{\perp\}$

Version-Spaces Algorithm

$G = \{(((0,0),5),\text{white})\}$

$S = \{\perp\}$



$G = \{$

$(((0,2),3),\text{white}),$
 $(((1,0),4),\text{white}),$
 $(((1,1),4),\text{white}),$
 $(((0,0),5),\text{cyan})$

$\}$

Redundant:

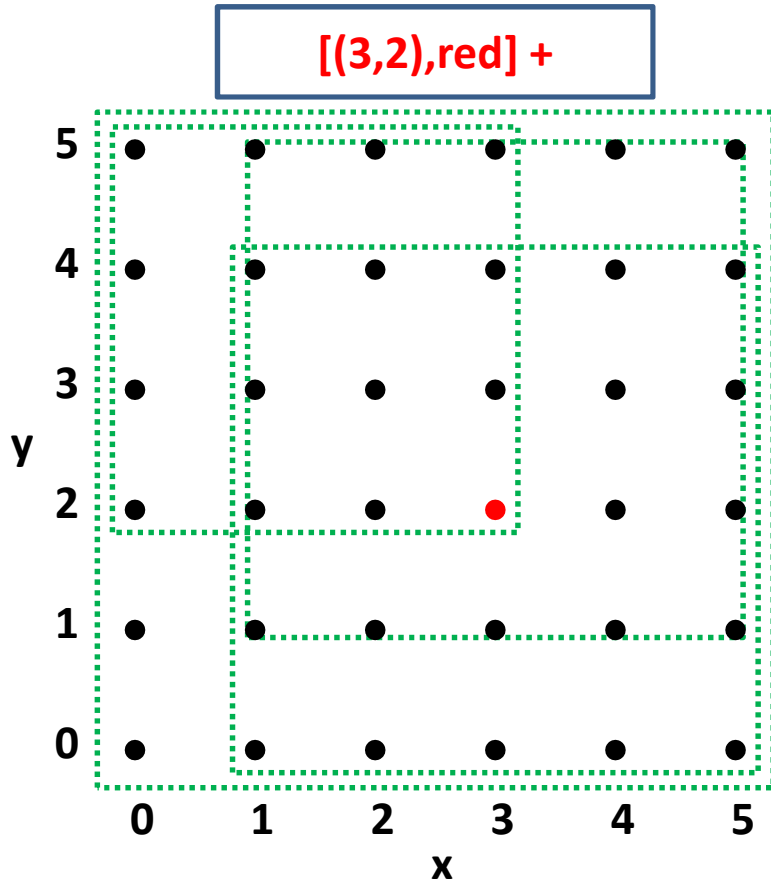
$(((0,0),5),\text{green})$
 $(((0,0),5),\text{blue})$

$S = \{\perp\}$

Version-Spaces Algorithm

$G = \{ [((0,2),3),\text{white}], [((1,0),4),\text{white}], [((1,1),4),\text{white}], [((0,0),5),\text{cyan}] \}$

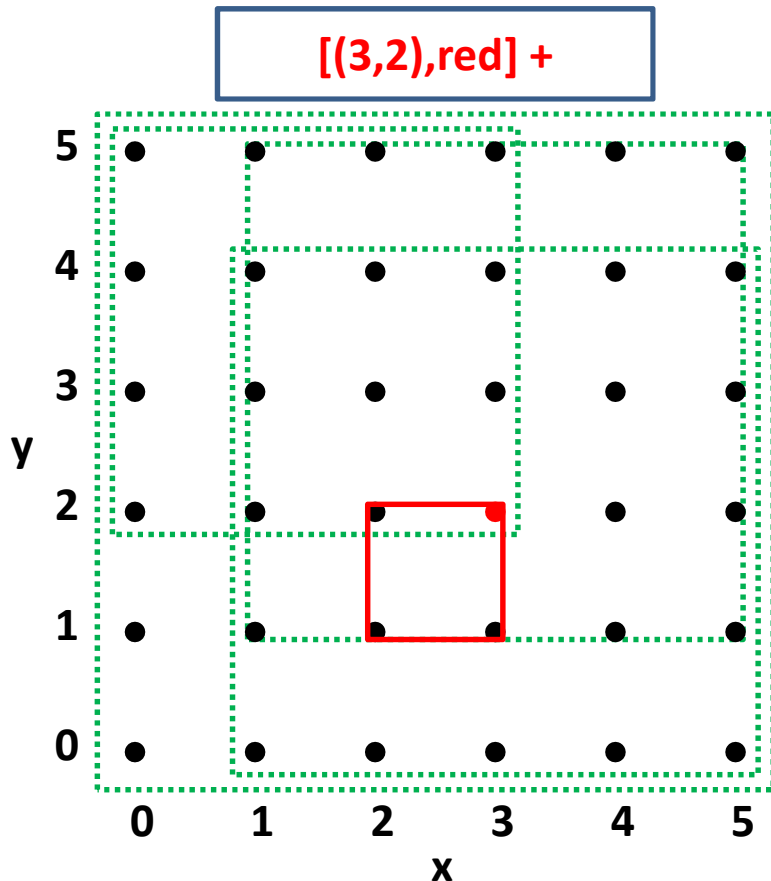
$S = \{\perp\}$



Version-Spaces Algorithm

$G = \{ [((0,2),3),\text{white}], [((1,0),4),\text{white}], [((1,1),4),\text{white}], [((0,0),5),\text{cyan}] \}$

$S = \{\perp\}$



$G = \{$

$[((0,2),3),\text{white}],$
 $[((1,0),4),\text{white}],$
 $[((1,1),4),\text{white}],$
 $[((0,0),5),\text{cyan}]$

$\}$

$S = \{$

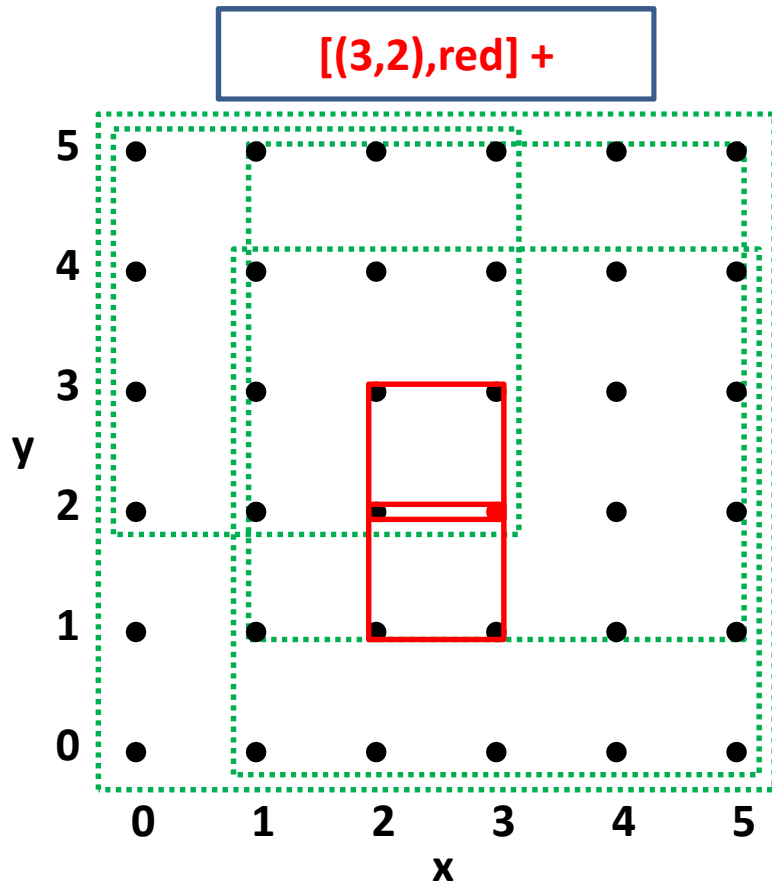
$[((2,1),1),\text{red}]$

$\}$

Version-Spaces Algorithm

$G = \{ [((0,2),3),\text{white}], [((1,0),4),\text{white}], [((1,1),4),\text{white}], [((0,0),5),\text{cyan}] \}$

$S = \{\perp\}$



$G = \{$

$[((0,2),3),\text{white}],$
 $[((1,0),4),\text{white}],$
 $[((1,1),4),\text{white}],$
 $[((0,0),5),\text{cyan}]$

$\}$

$S = \{$

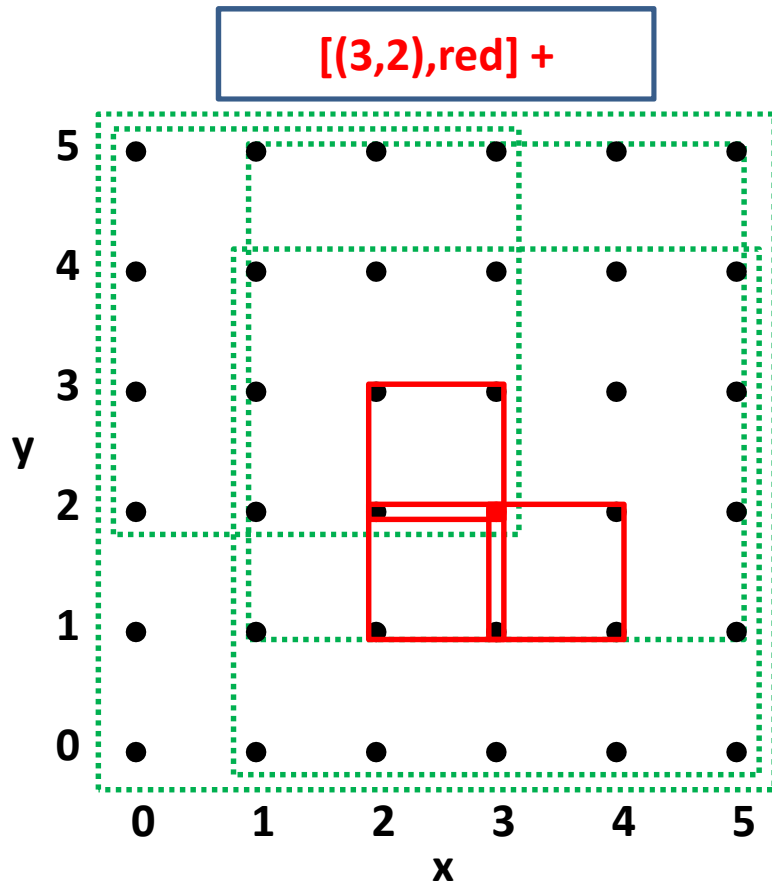
$[((2,1),1),\text{red}],$
 $[((2,2),1),\text{red}]$

$\}$

Version-Spaces Algorithm

$G = \{ [((0,2),3),\text{white}], [((1,0),4),\text{white}], [((1,1),4),\text{white}], [((0,0),5),\text{cyan}] \}$

$S = \{\perp\}$



$G = \{$

$[((0,2),3),\text{white}],$
 $[((1,0),4),\text{white}],$
 $[((1,1),4),\text{white}],$
 $[((0,0),5),\text{cyan}]$

$\}$

$S = \{$

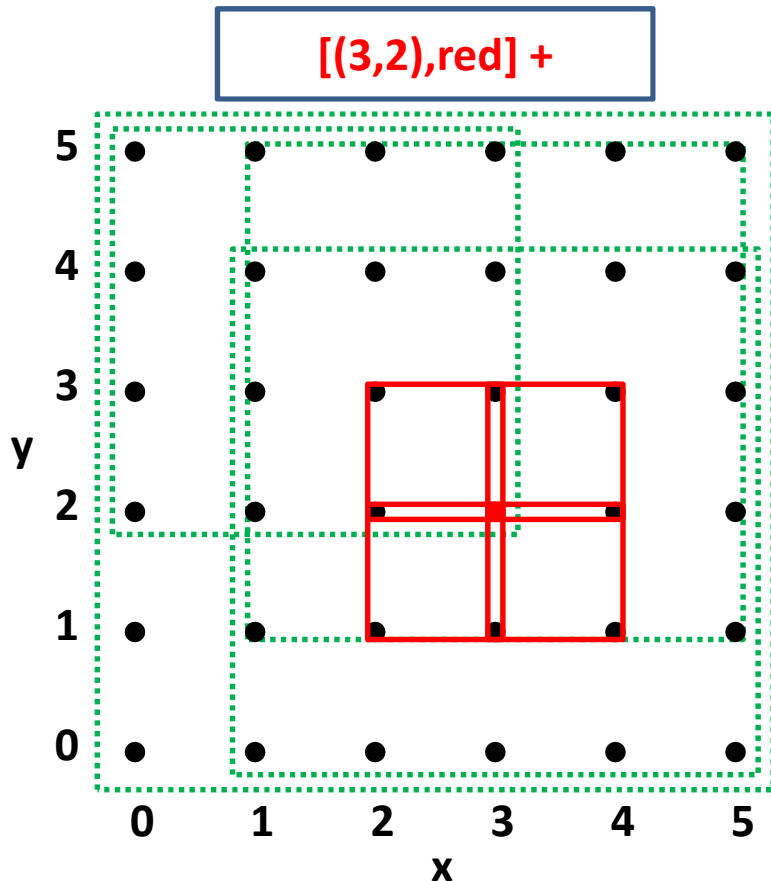
$[((2,1),1),\text{red}],$
 $[((2,2),1),\text{red}],$
 $[((3,1),1),\text{red}]$

$\}$

Version-Spaces Algorithm

$G = \{ [((0,2),3),\text{white}], [((1,0),4),\text{white}], [((1,1),4),\text{white}], [((0,0),5),\text{cyan}] \}$

$S = \{\perp\}$



$G = \{$

$[((0,2),3),\text{white}],$
 $[((1,0),4),\text{white}],$
 $[((1,1),4),\text{white}],$
 $[((0,0),5),\text{cyan}]$

$\}$

$S = \{$

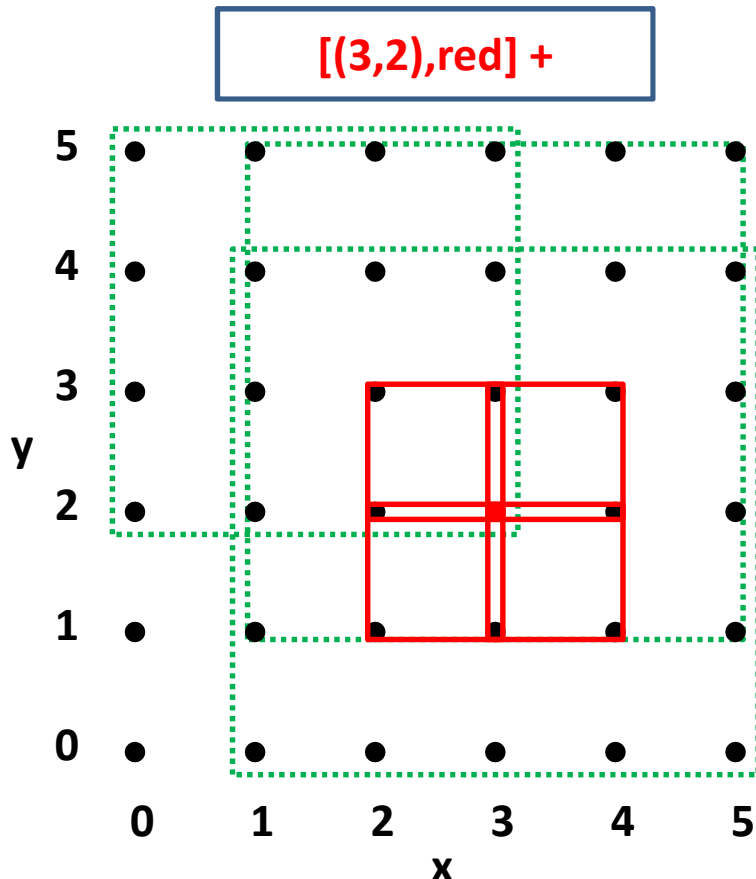
$[((2,1),1),\text{red}],$
 $[((2,2),1),\text{red}],$
 $[((3,1),1),\text{red}],$
 $[((3,2),1),\text{red}]$

$\}$

Version-Spaces Algorithm

$G = \{ [((0,2),3),\text{white}], [((1,0),4),\text{white}], [((1,1),4),\text{white}], [((0,0),5),\text{cyan}] \}$

$S = \{\perp\}$



$G = \{$

$[((0,2),3),\text{white}],$
 $[((1,0),4),\text{white}],$
 $[((1,1),4),\text{white}]$

$\}$

Removed:

$[((0,0),5),\text{cyan}]$

$S = \{$

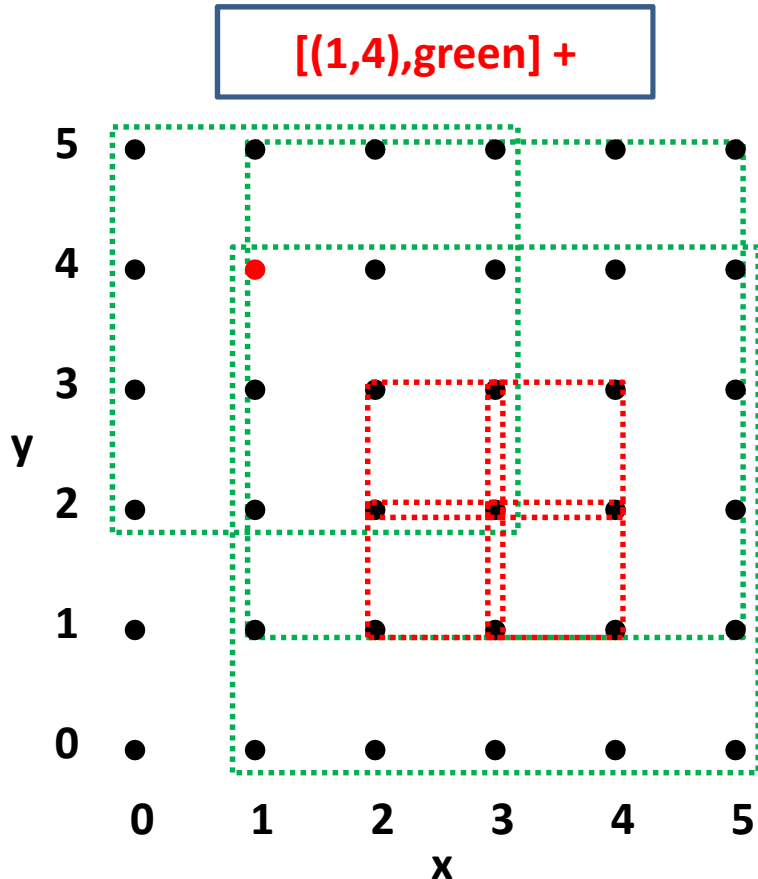
$[((2,1),1),\text{red}],$
 $[((2,2),1),\text{red}],$
 $[((3,1),1),\text{red}],$
 $[((3,2),1),\text{red}]$

$\}$

Version-Spaces Algorithm

$G = \{[((0,2),3),\text{white}], [((1,0),4),\text{white}], [((1,1),4),\text{white}]\}$

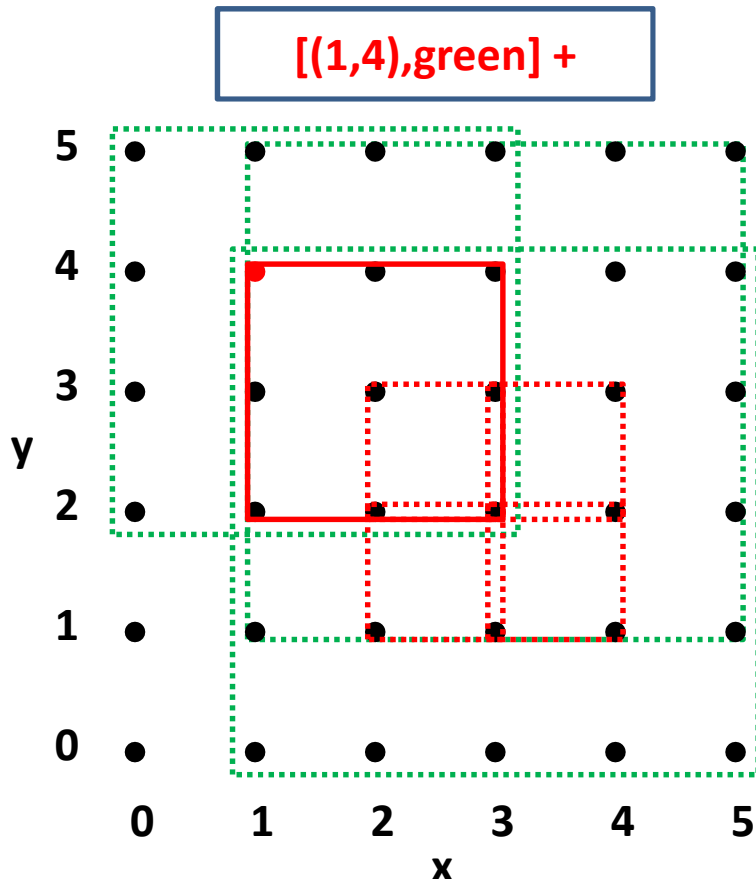
$S = \{[((2,1),1),\text{red}], [((2,2),1),\text{red}], [((3,1),1),\text{red}], [((3,2),1),\text{red}]\}$



Version-Spaces Algorithm

$G = \{ [((0,2),3),\text{white}], [((1,0),4),\text{white}], [((1,1),4),\text{white}] \}$

$S = \{ [((2,1),1),\text{red}], [((2,2),1),\text{red}], [((3,1),1),\text{red}], [((3,2),1),\text{red}] \}$



$G = \{$

$[((0,2),3),\text{white}],$
 $[((1,0),4),\text{white}],$
 $[((1,1),4),\text{white}]$

$\}$

$S = \{$

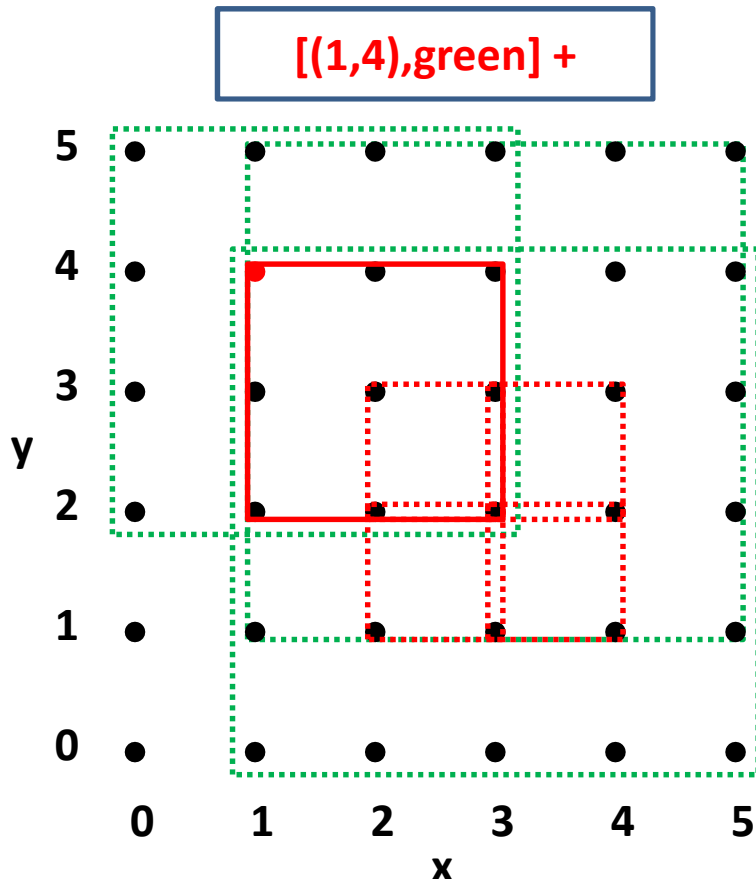
$[((1,2),2),\text{yellow}]$

$\}$

Version-Spaces Algorithm

$G = \{ [((0,2),3),\text{white}], [((1,0),4),\text{white}], [((1,1),4),\text{white}] \}$

$S = \{ [((2,1),1),\text{red}], [((2,2),1),\text{red}], [((3,1),1),\text{red}], [((3,2),1),\text{red}] \}$



$G = \{$

$[((0,2),3),\text{white}],$
 $[((1,0),4),\text{white}],$
 $[((1,1),4),\text{white}]$

$\}$

$S = \{$

$[((1,2),2),\text{yellow}]$

$\}$

Redundant:

$[((0,1),3),\text{yellow}]$

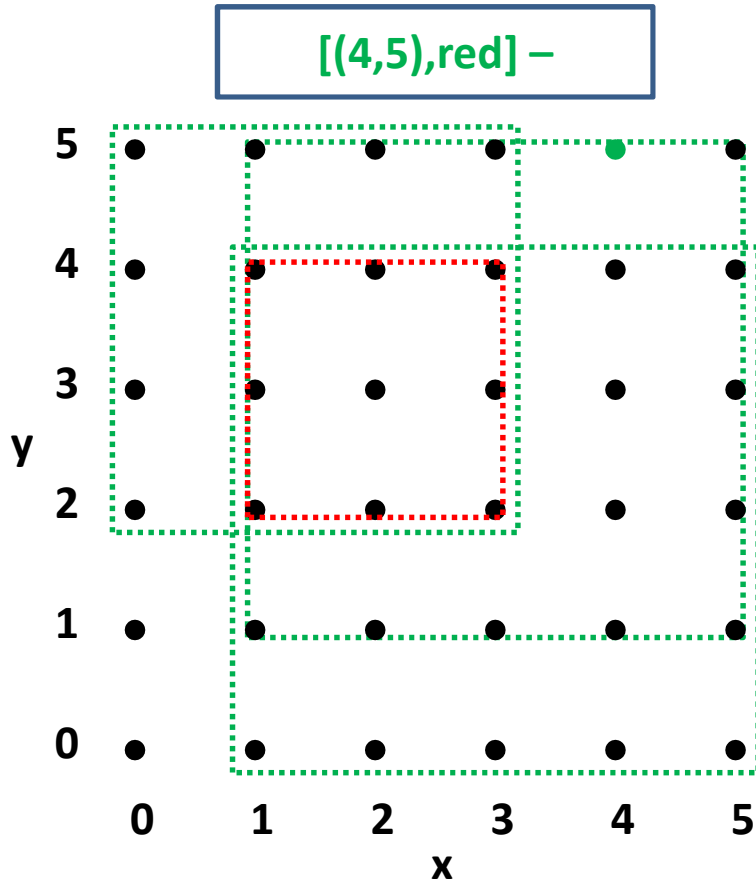
$[((1,1),3),\text{yellow}]$

$[((1,2),3),\text{yellow}]$

Version-Spaces Algorithm

$G = \{ [((0,2),3),\text{white}], [((1,0),4),\text{white}], [((1,1),4),\text{white}] \}$

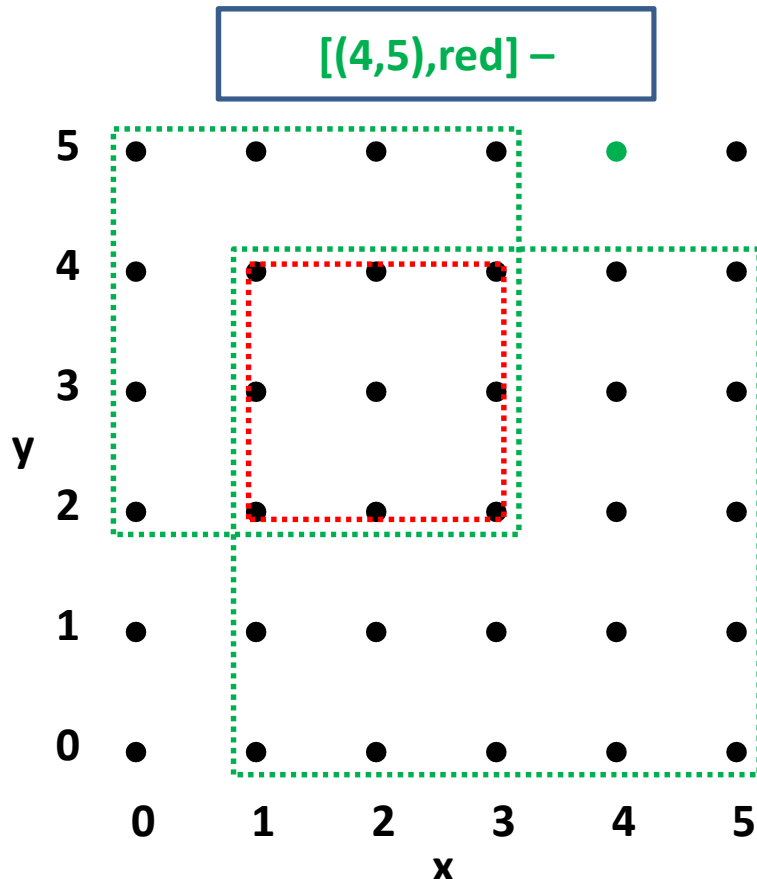
$S = \{ [((1,2),2),\text{yellow}] \}$



Version-Spaces Algorithm

$G = \{ [((0,2),3),\text{white}], [((1,0),4),\text{white}], [((1,1),4),\text{white}] \}$

$S = \{ [((1,2),2),\text{yellow}] \}$



$G = \{$

$[((0,2),3),\text{white}],$
 $[((1,0),4),\text{white}]$

$\}$

Redundant:

$[((1,1),3),\text{white}]$

Others don't generalize S

$S = \{$

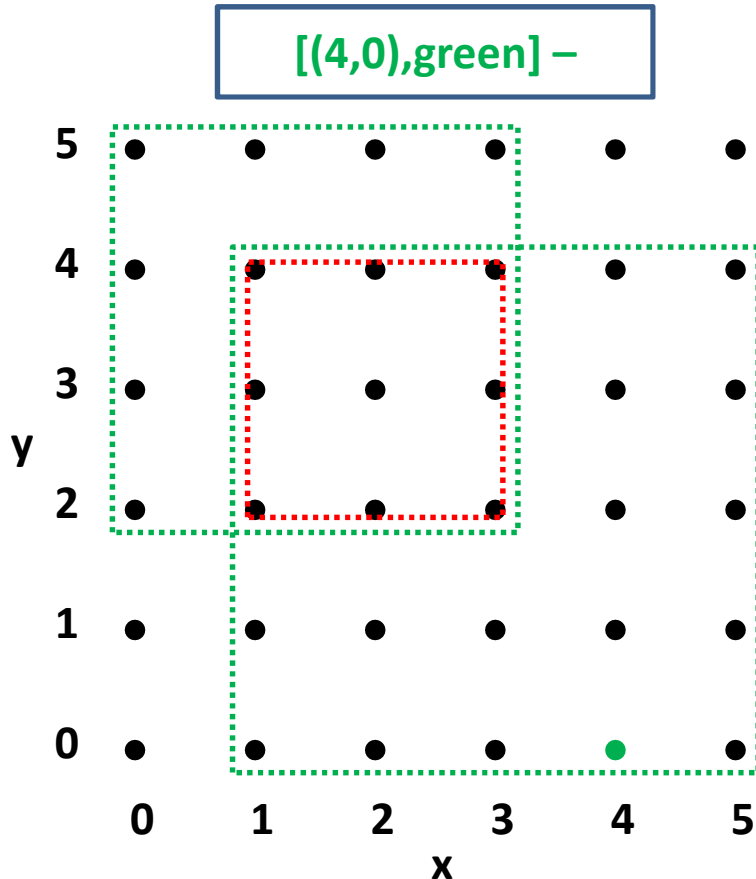
$[((1,2),2),\text{yellow}]$

$\}$

Version-Spaces Algorithm

$G = \{ [((0,2),3),\text{white}], [((1,0),4),\text{white}] \}$

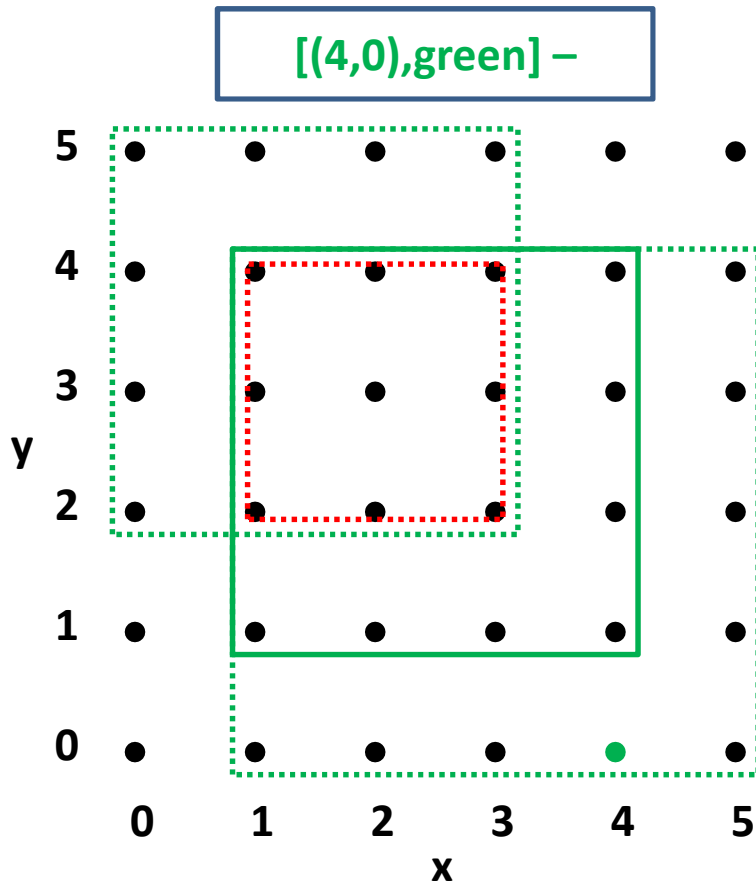
$S = \{ [((1,2),2),\text{yellow}] \}$



Version-Spaces Algorithm

$G = \{ [((0,2),3),\text{white}], [((1,0),4),\text{white}] \}$

$S = \{ [((1,2),2),\text{yellow}] \}$



$G = \{$

$[((0,2),3),\text{white}],$
 $[((1,1),3),\text{white}]$

$\}$

Others don't generalize S

$S = \{$

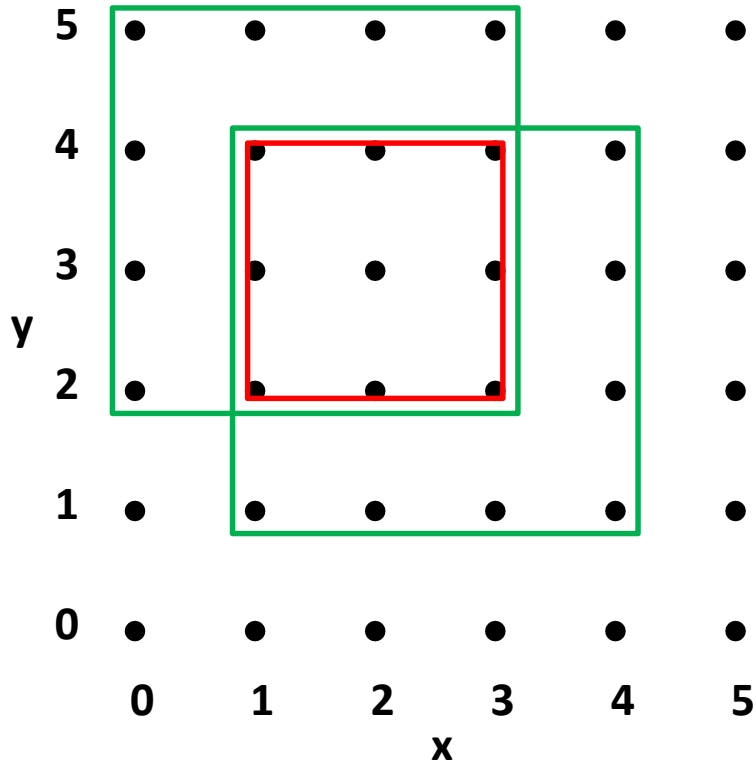
$[((1,2),2),\text{yellow}]$

$\}$

Version-Spaces Algorithm

$G = \{ [((0,2),3),\text{white}], [((1,1),3),\text{white}] \}$

$S = \{ [((1,2),2),\text{yellow}] \}$



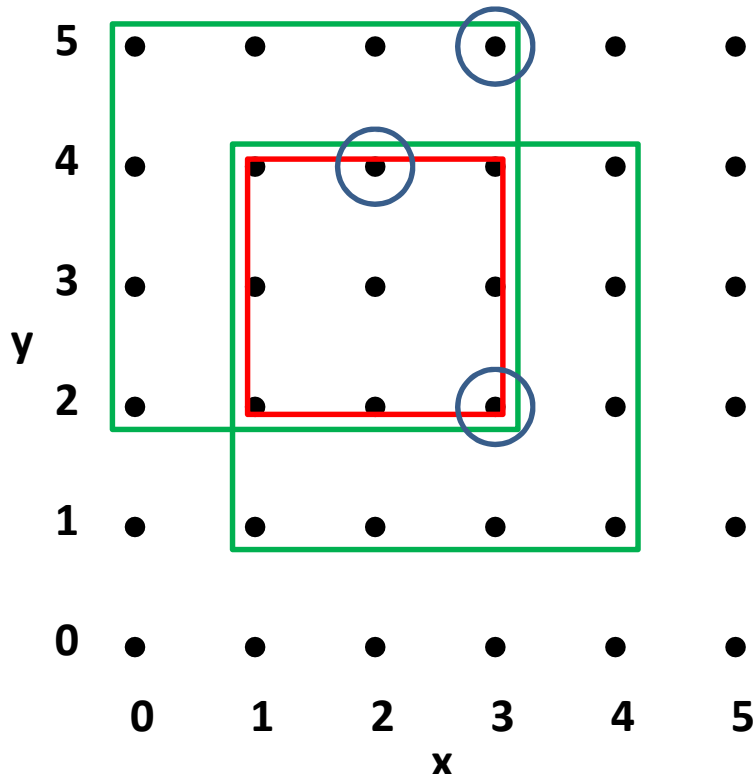
Version Spaces: Ex-exam

USING THE RESULT

Using the Result

$G = \{ [((0,2),3),\text{white}], [((1,1),3),\text{white}] \}$

$S = \{ [((1,2),2),\text{yellow}] \}$



$[(3,2),\text{green}]$

Yes

$[(2,4),\text{red}]$

Yes

$[(3,5),\text{blue}]$

Maybe