Oefeningen Toegepaste Algebra en Differentiaalvergelijkingen

LA Zitting 3

Numerieke uitkomsten versie 2015 – 2016

Nico Scheerlinck ¹

Vraag 01: 0 , 2 , -1

Vraag 02: 0, 0, 6

Vraag 03:

Vraag 04:
$$A = P D P^{-1}$$
 met $D = \begin{bmatrix} 5 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix}$ en $P = \begin{bmatrix} -1 & -2 & 1 \\ -1 & 1 & 0 \\ 1 & 0 & 1 \end{bmatrix}$

Vraag 05:

Vraag 06:

Vraag 07:
$$\mathcal{B} = \{\mathbf{v}_1, \mathbf{v}_2\} \text{ met } \mathbf{v}_1 = \begin{bmatrix} -2 \\ 1 \end{bmatrix} \text{ en } \mathbf{v}_2 = \begin{bmatrix} 1 \\ 1 \end{bmatrix}$$

Vraag 08:

Vraag 09:
$$x = \frac{5}{2}u_1 - \frac{3}{2}u_2 + 2u_3$$
.

Vraag 10:
$$y = \begin{bmatrix} 10/3 \\ 2/3 \\ 8/3 \end{bmatrix} + \begin{bmatrix} -7/3 \\ 7/3 \\ 7/3 \end{bmatrix}$$

Vraag 11:

Vraag 12:

Vraag 13:

¹Former tutors: Bart Vandewoestyne, Dirk Nuyens & Nele Lejon

Rekenopdrachten ...

(a)
$$\lambda_1 = -2, \quad \lambda_2 = -4, \quad \boldsymbol{\xi}_1 = \begin{bmatrix} 1 \\ -3 \end{bmatrix} \quad , \quad \boldsymbol{\xi}_2 = \begin{bmatrix} 1 \\ -1 \end{bmatrix}$$

(b)
$$\lambda_1 = 2, \quad \lambda_2 = -1, \quad \boldsymbol{\xi}_1 = \begin{bmatrix} 2 \\ 1 \end{bmatrix} \quad , \quad \boldsymbol{\xi}_2 = \begin{bmatrix} 1 \\ 2 \end{bmatrix}$$

(c)
$$\lambda_1 = 0, \quad \lambda_2 = -2, \quad \boldsymbol{\xi}_1 = \begin{bmatrix} 3 \\ 4 \end{bmatrix} \quad , \quad \boldsymbol{\xi}_2 = \begin{bmatrix} 1 \\ 2 \end{bmatrix}$$

(d)
$$\lambda_1 = \lambda_2 = -2 \quad \boldsymbol{\xi}_1 = \begin{bmatrix} 1 \\ 0 \end{bmatrix} \quad , \quad \boldsymbol{\xi}_2 = \begin{bmatrix} 0 \\ 1 \end{bmatrix}$$

(e)
$$\lambda_{1,2} = -1 \pm 5i, \quad \boldsymbol{\xi}_{1,2} = \begin{bmatrix} 0 \\ 1 \end{bmatrix} \pm i \begin{bmatrix} 1 \\ 0 \end{bmatrix}$$

(f)
$$\lambda_{1,2} = 1 \pm 5i, \quad \boldsymbol{\xi}_{1,2} = \left[\begin{array}{c} 0 \\ 1 \end{array} \right] \pm i \left[\begin{array}{c} 1 \\ 0 \end{array} \right]$$

(g)
$$\lambda_{1,2} = \pm 2i, \quad \boldsymbol{\xi}_{1,2} = \begin{bmatrix} 5 \\ 1 \end{bmatrix} \pm i \begin{bmatrix} 0 \\ -2 \end{bmatrix}$$

(h)
$$\lambda_{1,2}=1\pm i,\quad \pmb{\xi}_{1,2}=\left[\begin{array}{c}1\\2\end{array}\right]\pm i\left[\begin{array}{c}0\\-1\end{array}\right]$$

Een handig hulpmiddel ...